

%use the three methods with at least two initial vectors randomly generated
 %by randn(n,1) to solve the following problems. To ensure two generated
 %vectors are different, you may consider setting the random number
 %generator rng. Compare their performance in terms of the number of
 %iterations and the error (use l-inf-norm) between the actual eigenvalue/eigenvectors and
 %their respective estimations. If the initial random vectors are changed,
 %then iter and error will be changed accordingly in the results.

% a) Find the rank of each webpage in the network shown in Figure 1 with 15
 % webpages. Construct adjacency matrix B and the modified adjacency matrix
 % M, then execute eigfinder.m.

```
B=[0 0 1 0 0 0 0 0 0 0 0 0 0 0 0
    1 0 0 0 0 0 0 0 0 0 1 0 0 0 0
    0 1 0 0 1 0 0 0 0 0 0 0 0 0 0
    1 1 0 0 0 0 0 0 0 0 0 0 1 0 0
    0 0 0 0 0 1 0 1 0 0 0 0 0 0 0
    0 0 0 0 0 0 1 1 0 0 0 0 0 0 0
    0 0 0 0 0 0 0 0 1 0 0 0 0 0 0
    0 0 0 0 0 0 0 0 1 1 0 0 0 0 0
    0 0 0 0 1 0 0 0 0 0 1 0 0 0 0
    0 0 0 0 0 0 0 0 1 0 1 0 0 1 0
    0 0 0 0 0 0 0 0 0 0 0 0 0 1 0
    0 0 0 0 0 0 0 0 0 0 0 0 1 0 0
    0 0 0 0 0 0 0 0 0 0 0 0 0 0 1
    0 0 0 0 0 0 0 0 0 0 0 0 1 0 0
    0 0 0 0 0 0 0 0 0 0 0 0 0 1 0];
```

```
M=zeros(15); %preallocate for speed
for i=1:15
    for j=1:15
        M(i,j)=.85*(B(i,j)/sum(B(i,:)))+(1-.85)/15;
    end
end
```

```
rng; %set random number generator
x0=rand(15,1);
```

```
paras.tol=10^-6;
paras.maxiter=100;
paras.q=(x0'*M*x0)/(x0'*x0);
paras.option='power1';
```

```
[ lambda1, v1, iter1 ] = eigfinder( M, x0, paras );  
v1=v1/norm(v1);
```

```
paras.option='power2';  
[ lambda2, v2, iter2 ] = eigfinder( M, x0, paras );  
v2=v2/norm(v2);
```

```
paras.option='invpower';  
[ lambda3, v3, iter3 ] = eigfinder( M, x0, paras );  
v3=v3/norm(v3);
```

```
x0=rand(15,1);
```

```
paras.tol=10^-6;  
paras.maxiter=100;  
paras.q=(x0'*M*x0)/(x0'*x0);  
paras.option='power1';
```

```
[ lambda4, v4, iter4 ] = eigfinder( M, x0, paras );  
v4=v4/norm(v4);
```

```
paras.option='power2';  
[ lambda5, v5, iter5 ] = eigfinder( M, x0, paras );  
v5=v5/norm(v5);
```

```
paras.option='invpower';  
[ lambda6, v6, iter6 ] = eigfinder( M, x0, paras );  
v6=v6/norm(v6);
```

```
%Compute the actual dominant eigenvalue and its associated eigenvector  
[x,y]=eig(M);  
eigvec_a=x(:,1); %only look at the first column because that's the dominant  
%eigvalue/eigenvector  
eigvalue_a=y(1,1);
```

```
error1=norm(abs(eigvec_a-v1),Inf)  
error2=norm(abs(eigvec_a-v2),Inf)  
error3=norm(abs(eigvec_a-v3),Inf)
```

```
error4=norm(abs(eigvec_a-v4),Inf)
error5=norm(abs(eigvec_a-v5),Inf)
error6=norm(abs(eigvec_a-v6),Inf)
```

% b) Find the dominant eigenvalue and the dominant eigenvector of the
% matrix A

```
rng; %set random number generator
```

```
A=[2.395798 0.234169 0.127074 0.146184 0.183889
    0.113724 5.103374 0.243386 0.030779 0.241161
    0.183743 0.199444 7.642053 0.199313 0.145211
    0.085881 0.144653 0.104811 9.013056 0.024832
    0.053909 0.180566 0.126246 0.249744 3.774798];
```

```
x0=rand(5,1);
```

```
paras.tol=10^-6;
paras.maxiter=100;
paras.q=(x0'*A*x0)/(x0'*x0);
```

```
paras.option='power1';
[ lambda1b, v1b, iter1b ] = eigfinder( A, x0, paras );
v1b=v1b/norm(v1b);
```

```
paras.option='power2';
[ lambda2b, v2b, iter2b ] = eigfinder( A, x0, paras );
v2b=v2b/norm(v2b);
```

```
paras.option='invpower';
[ lambda3b, v3b, iter3b ] = eigfinder( A, x0, paras );
v3b=v3b/norm(v3b);
```

```
x0=rand(5,1);
```

```
paras.tol=10^-6;
```

```
paras.maxiter=100;  
paras.q=(x0'*A*x0)/(x0'*x0);  
paras.option='power1';
```

```
[ lambda5b, v4b, iter4b ] = eigfinder( A, x0, paras );  
v4b=v4b/norm(v4b);
```

```
paras.option='power2';  
[ lambda5b, v5b, iter5b ] = eigfinder( A, x0, paras );  
v5b=v5b/norm(v5b);
```

```
paras.option='invpower';  
[ lambda6b, v6b, iter6b ] = eigfinder( A, x0, paras );  
v6b=v6b/norm(v6b);
```

```
%Compute the actual dominant eigenvalue and its associated eigenvector  
[x,y]=eig(A);  
eigvec_b=x(:,1); %only look at the first column because that's the dominant  
%eigvalue/eigenvector  
eigvalue_b=y(1,1);
```

```
error1b=norm(abs(-1.*eigvec_b-v1b),Inf)  
error2b=norm(abs(-1.*eigvec_b-v2b),Inf)  
error3b=norm(abs(-1.*eigvec_b-v3b),Inf)  
error4b=norm(abs(-1.*eigvec_b-v4b),Inf)  
error5b=norm(abs(-1.*eigvec_b-v5b),Inf)  
error6b=norm(abs(-1.*eigvec_b-v6b),Inf)
```