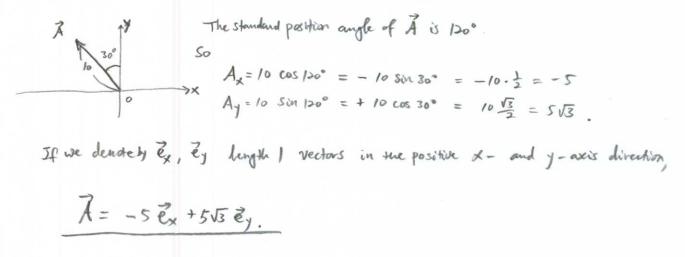
Midterm Examination 1 MTH 13 Section E01 21 February 2017 18:00–19:50

Instructions: Please answer the following and be sure to show your work or support your answer. You are not allowed to use the textbook, workbook, or notes. You cannot talk to other sudents. You can use your calculator.

1. The vector \overrightarrow{A} of length 10 is in the second-quadrant. The angle between \overrightarrow{A} and the y-axis is 30°. Resolve the vector \overrightarrow{A} (i.e. write \overrightarrow{A} into the sum $\overrightarrow{A}_x + \overrightarrow{A}_y$).



2. B's car is in mud. B, his wife, and their two children are trying to pull the car from it. B is applying 100 Newton of force to the East, and his wife 100 Newton to the North. Each children is pulling the car in $50\sqrt{2}$ Newton of force to the Southeast. What is the total force applied to the car?

Note that the sum of forces applied by B's two dildren

B's car

S 100 \(\sigma \) N to the Southeast. It is resolved into a

SOUTH ONLY of force to the south and another 100 N of
force to the East. The 100 N to the South Cancers

the force applied by B'S wife, and the 100 N to the

East adds to the 100 N of force applied by B. Hence

the total force is 200 N to the East.

3. Add two vectors \overrightarrow{A} an \overrightarrow{B} where the lengths of these vectors are A=3 and B=4. The angles in standard position of these vectors are 0° and 90° , respectively. Give your answer in "length \angle angle" form. You may use $53.13^{\circ} = \tan^{-1}\left(\frac{4}{3}\right)$.

The length of
$$A + B$$
 is

$$\sqrt{A^2 + B^2} = \sqrt{3^2 + 4^2} = \sqrt{25} = 5$$
where A is the length of B and B the length of B

The angle (in Standard position) is

$$\sqrt{A^2 + B^2} = \sqrt{3^2 + 4^2} = \sqrt{25} = 5$$
The angle (in Standard position) is

tan'
$$\left(\frac{(\vec{A}+\vec{B})_y}{(\vec{A}+\vec{B})_x}\right) = \tan^{-1}\left(\frac{4}{3}\right) = 53.13^\circ$$
. So $52.53.13^\circ$.

4. Add three vectors \overrightarrow{A} , \overrightarrow{B} , and \overrightarrow{C} where the lengths of these vectors are A=10, B=20, and C=30. The angles in standard position of these vectors are 0° , 120° , and 225° , respectively. Give your answer in "length \angle angle" form. You may use $\tan^{-1}\left(1-\sqrt{\frac{2}{3}}\right)=10$, 4°

Angle =
$$ton^{-1}\left(\frac{(R+B+C)_{y}}{(R+B+C)_{x}}\right) = ton^{-1}\left(\frac{10\sqrt{3}-15\sqrt{2}}{-15\sqrt{2}}\right) = 10.4^{\circ}$$

Length = $\int (R+B+C)_{x}^{2} + (R+B+C)_{y}^{2} = \sqrt{225\cdot 2} + 300 - 300\sqrt{6} + 225\cdot 2$
= $\sqrt{1200 - 300\sqrt{6}} = 10\sqrt{12 - 3\sqrt{6}} = 21.56$ Answer: $21.56 < 10.4^{\circ}$

5. Find values of x and y that satisfies the following equation: 9 - i = xi + 1 - y.

Real part
$$9 = 1 - y \Rightarrow y = -8$$

Imaginary part $-1 = x \Rightarrow x = -1$.

$$X = -1, \ \mathcal{Y} = -8$$

6. Express the following expression in the form of a + bi.

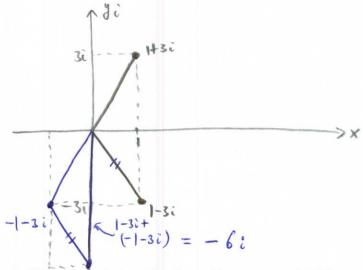
$$\frac{i}{1+i} - \frac{8-i}{2+i}$$

$$\frac{i(2+i)}{(1+i)(2+i)} - \frac{(8-i)(1+i)}{(2+i)(1+i)} = \frac{2i-1-8+i-8i-1}{(1+i)(2+i)}$$

$$= \frac{-10-5i}{1+3i} = \frac{(-10-5i)(1-3i)}{(1+3i)(1-3i)} = \frac{-25+25i}{10}$$

$$= -\frac{5}{2}+\frac{5}{2}i$$
Answer

7. Subtract 1 + 3i from 1 - 3i graphically.



8. Write -4 + 3i in polar form. You may use $36.87^{\circ} = \tan^{-1}\left(\frac{3}{4}\right)$.

Standard position augle
$$180^{\circ} - 36.87^{\circ} = 143.13^{\circ}$$

Answer: 5 < 143./3°

9. Express $\frac{\sqrt{2}}{2} - \frac{\sqrt{2}}{2}i$ in exponential form.

Polar form: length =
$$\sqrt{\frac{5}{3}}^2 + (-\frac{5}{3})^2 = 1$$

Angle

 $\sqrt{\frac{5}{2}}$

Angle

 $\sqrt{\frac{5}{2}}$
 $\sqrt{\frac{5}{2}}$

Standard position angle

 $\sqrt{\frac{7}{4}}\pi$

exponental

 $\sqrt{\frac{7}{4}}\pi$
 $\sqrt{\frac{7}{4}}\pi$

10. Find all three roots of $z^3 = 1$, where z is a complex variable.

$$| = | \cdot (\cos(0+2n\pi) + i\sin(0+2n\pi))$$
Cubic roots of $| = \{ 1 \frac{1}{3} (\cos \frac{\pi}{3} + i\sin \frac{\pi}{3}) = -\frac{1}{3} + \frac{\pi}{3}$

$$| \frac{1}{3} (\cos \frac{\pi}{3} + i\sin \frac{\pi}{3}) = -\frac{1}{3} + \frac{\pi}{3}$$

$$| \frac{1}{3} (\cos \frac{\pi}{3} + i\sin \frac{\pi}{3}) = -\frac{1}{3} - \frac{\pi}{3}$$

$$\left\{ 1, \frac{-1+\sqrt{3}i}{2}, \frac{-1-\sqrt{3}i}{2} \right\}$$