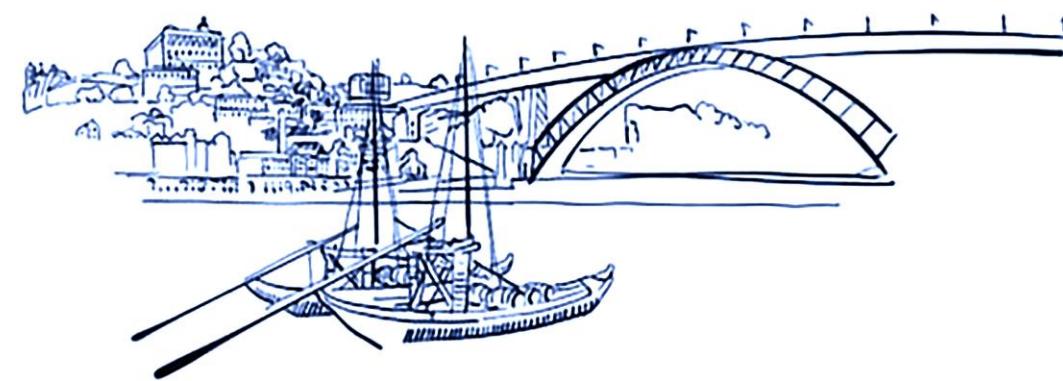


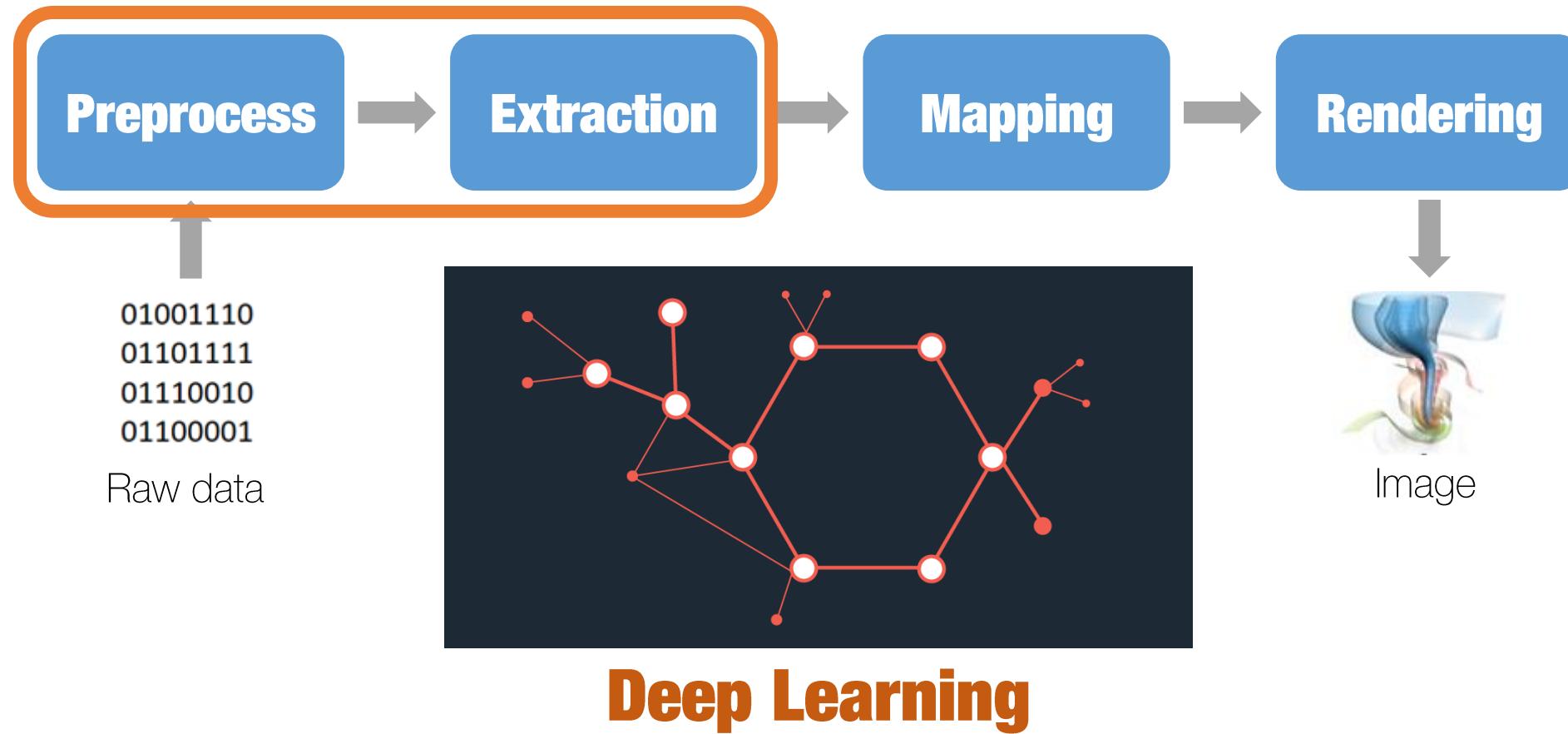


# Robust Reference Frame Extraction from Unsteady 2D Vector Fields with Convolutional Neural Networks

Byungsoo Kim, Tobias Günther

**ETH** zürich computer graphics laboratory

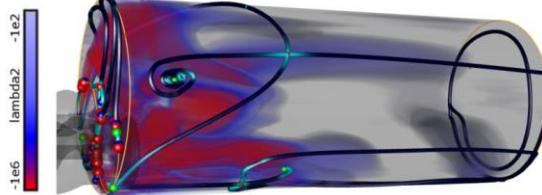




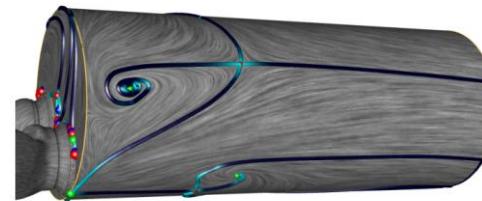


Pitching Airfoil under Dynamic Stall

[Ouro et al., Journal of Fluids Engineering, 2018]



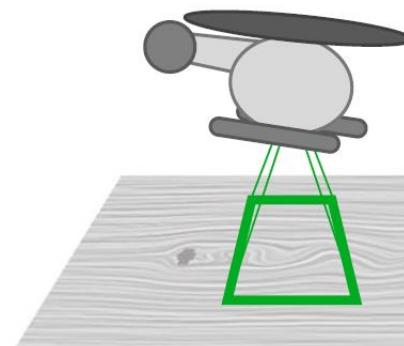
Engine Design  
[Garth et al. 2007]



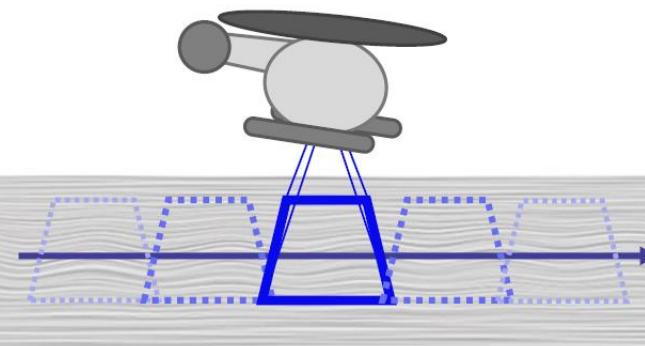
Blood Flow Analysis  
[Köhler et al. 2013]

# Extraction of Vortices

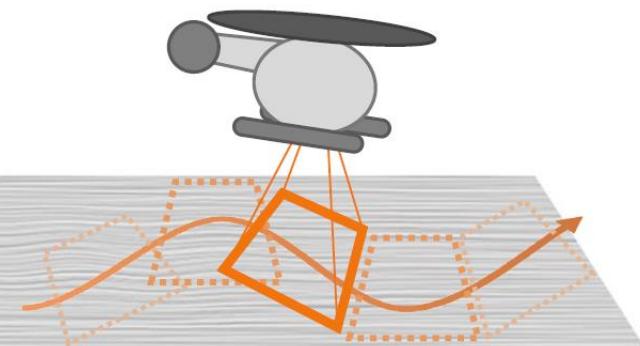
## » Reference Frames



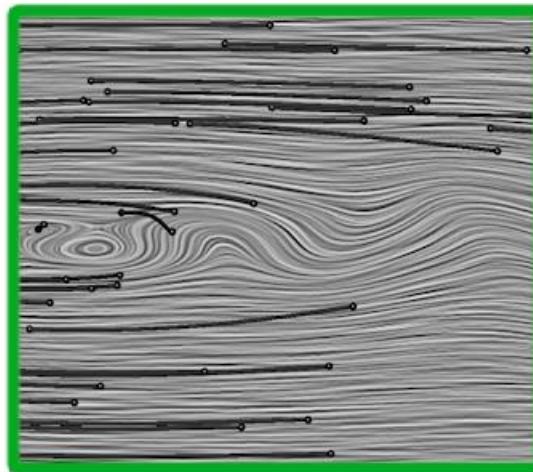
Standing still



Linearly translate



Arbitrary movement



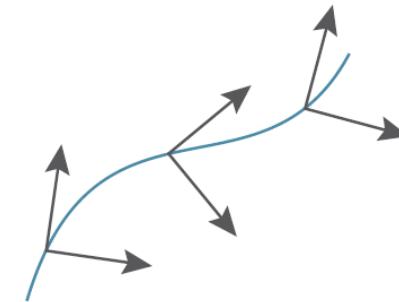
Result depends on the **reference frame**

[Slides from Günther and Theisel 2018]

Invariance to any smooth rotation and translation [Truesdell 1965]:

$$\mathbf{x}^* = \mathbf{Q}(t)\mathbf{x} + \mathbf{c}(t), \quad t^* = t - a$$

↑  
time-dep.  
rotation      ↑  
time-dep.  
translation

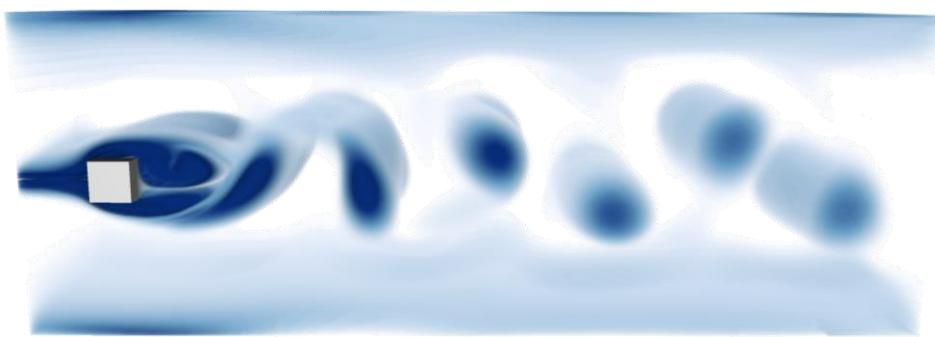


How to find vortices objectively?

### Use Objective Differential Properties

#### Objective region-based measures:

- Relative vorticity [Drouot 1976, Tabor 1994]
- $M_z$  Criterion [Haller 2005]
- LVD, LAVD [Haller 2016]



LAVD [Haller 2016]

### Find Steady Reference Frame

[Lugt 1972, Robinson 1991]

#### Steady extractors apply:

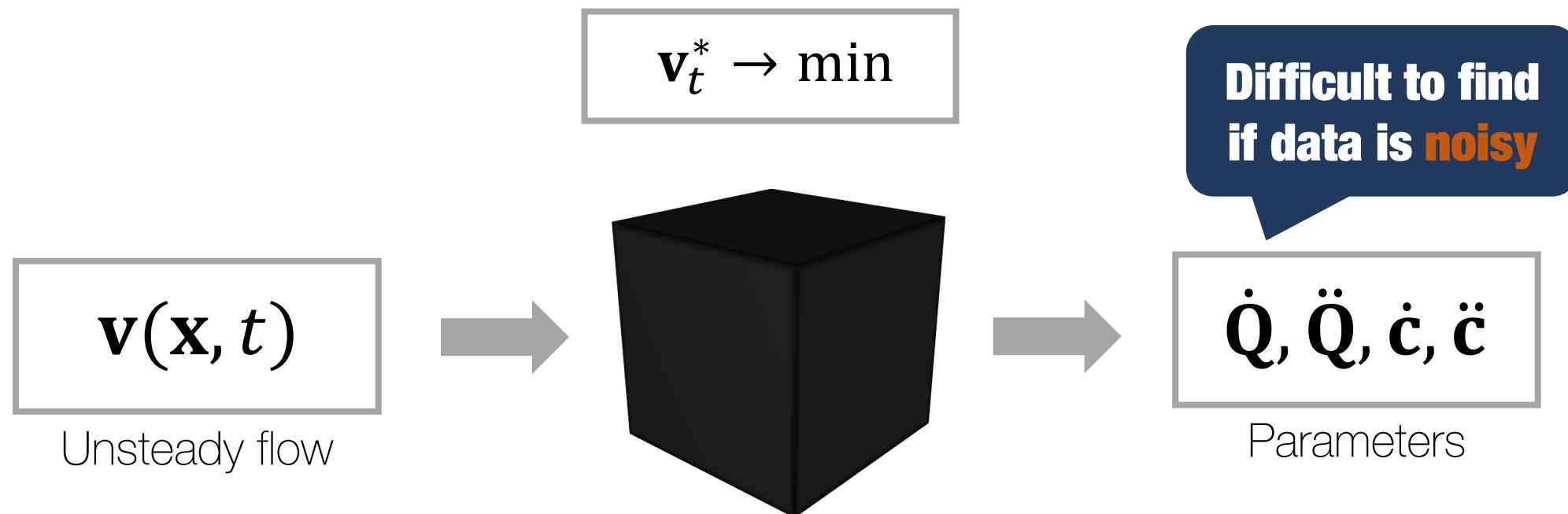
- Critical points, Sujudi-Haines

#### Optimization problem:

- Local [Günther and Theisel 2017, 2018]
- Global [Hadwiger 2019]
- Deep Learning [this paper]

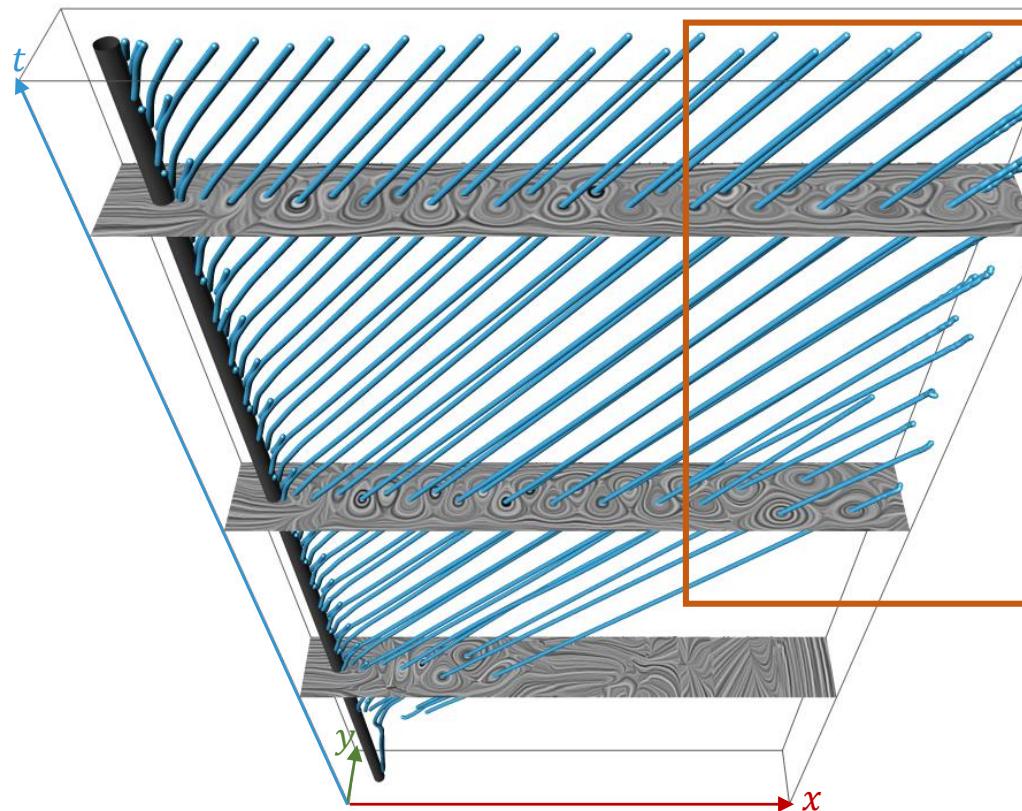
Optimization problem for the steady reference frame

- Given: unsteady vector field  $\mathbf{v}(\mathbf{x}, t)$
- Unknown: reference frame transformation  $\mathbf{x}^* = \mathbf{Q}(t) \mathbf{x} + \mathbf{c}(t)$
- Constraint: transformed field  $\mathbf{v}^*$  is steady

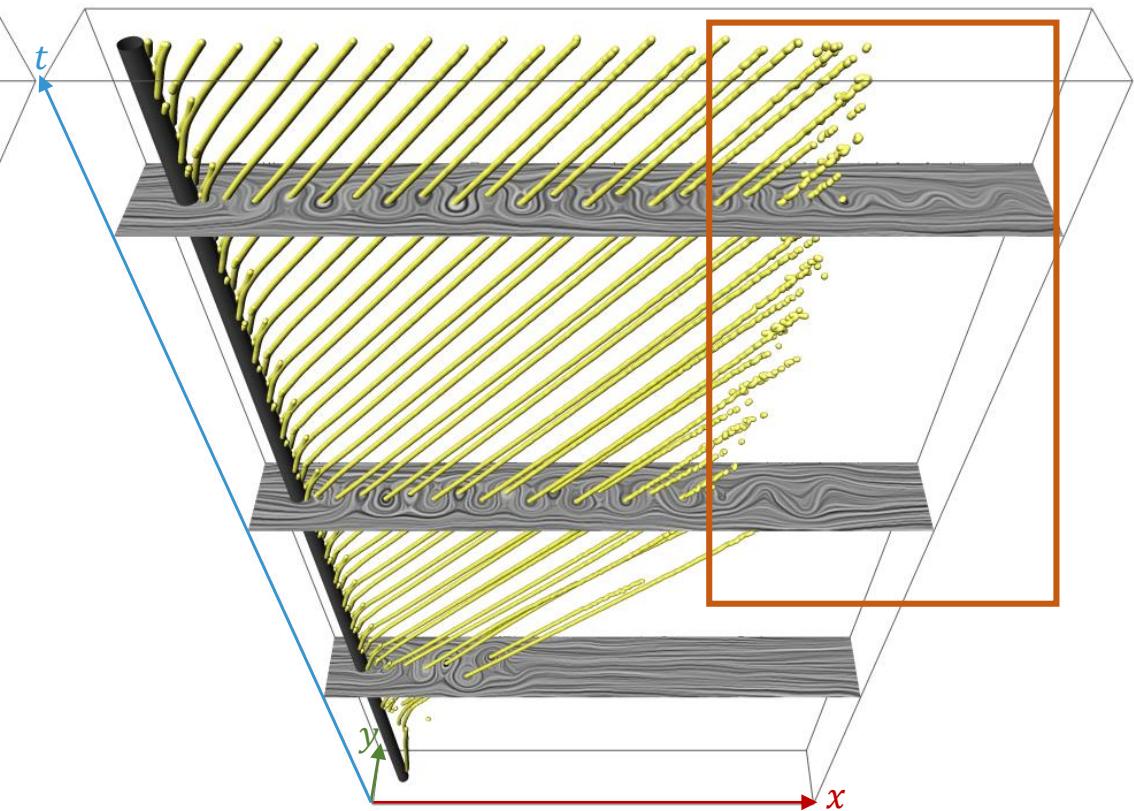


# Extraction of Vortices

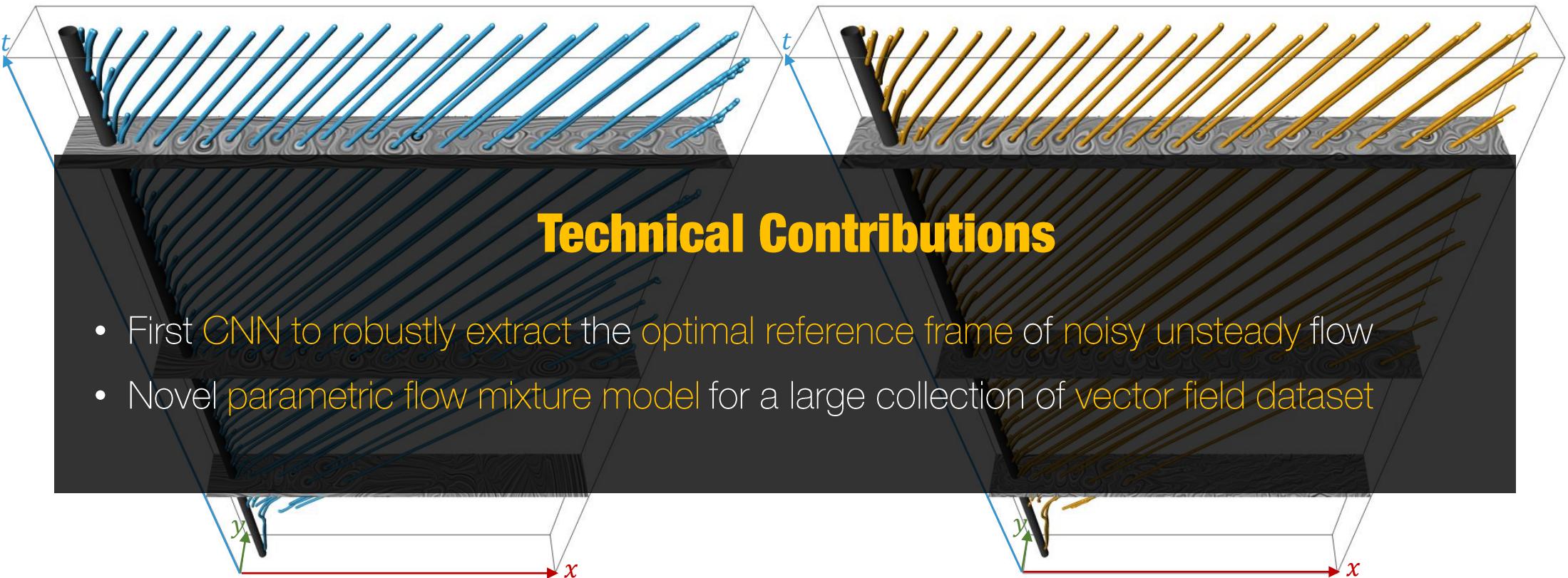
## » Optimal Reference Frames



Linear Optimization on Original Data  
[Günther et al. 2017]



Linear Optimization on **Noisy** Data



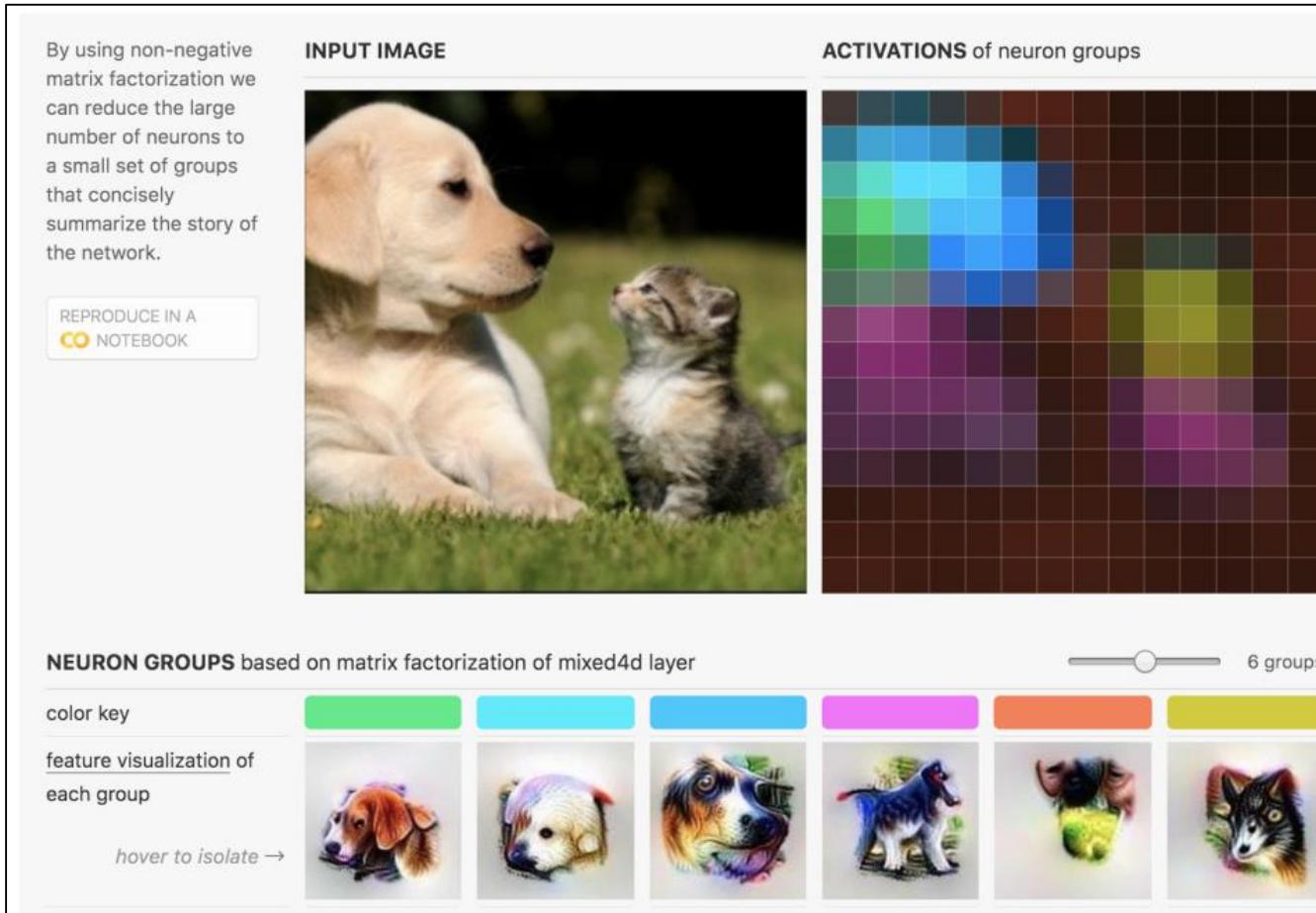
Linear Optimization on Original Data  
[Günther et al. 2017]

Our **CNN-based** approach on Noisy Data

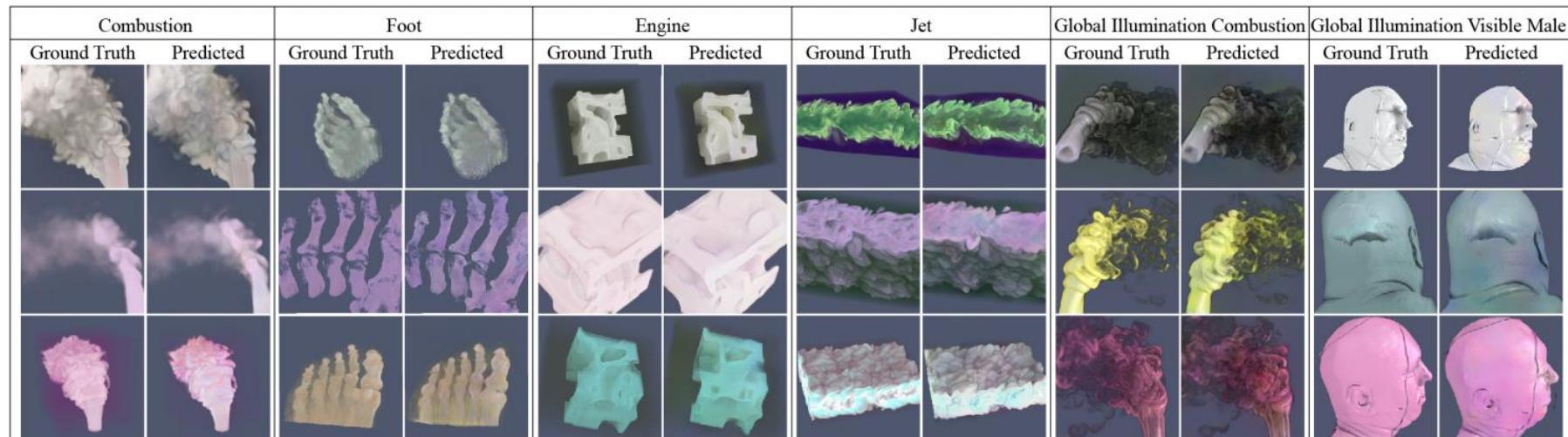
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# Machine Learning Research in Visualization

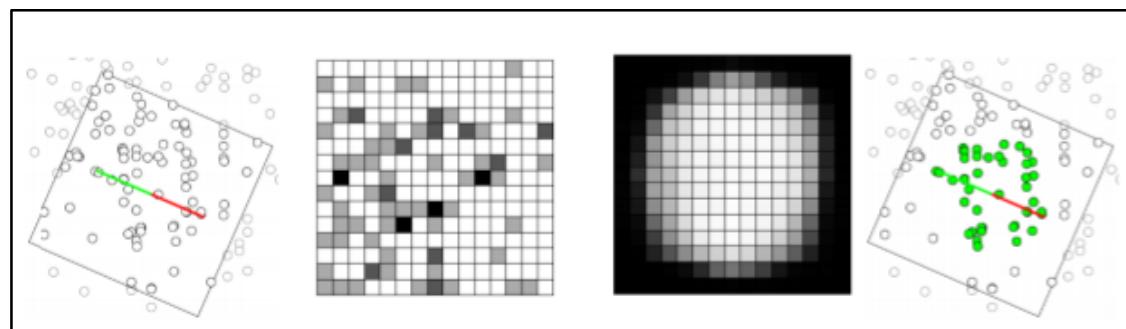
## » Black Box Visualization



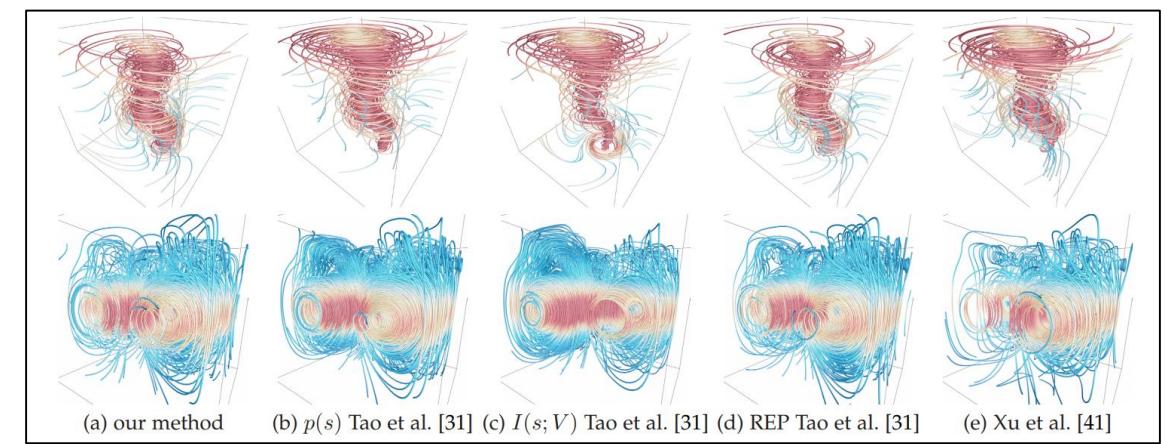
Interactive feature visualization to interpret neural networks [Olah et al. 2018]



A Generative Model for Volume Rendering [Berger et al. 2017]

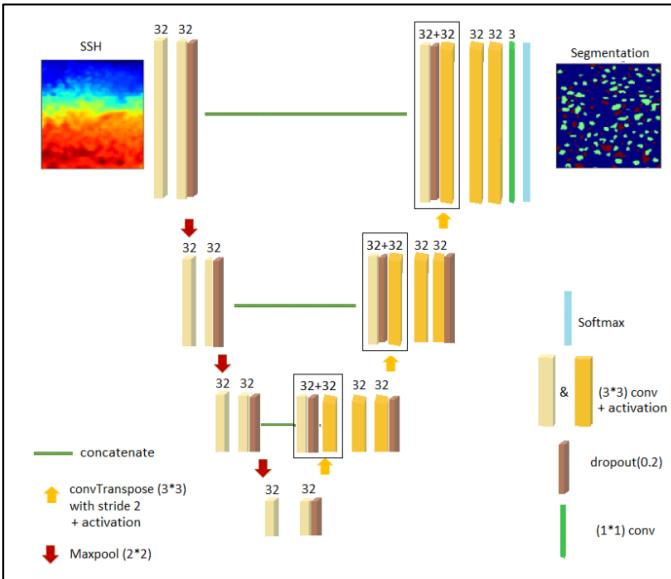


Fast & Accurate Brushing in Scatter Plots  
[Fan and Hauser 2018]

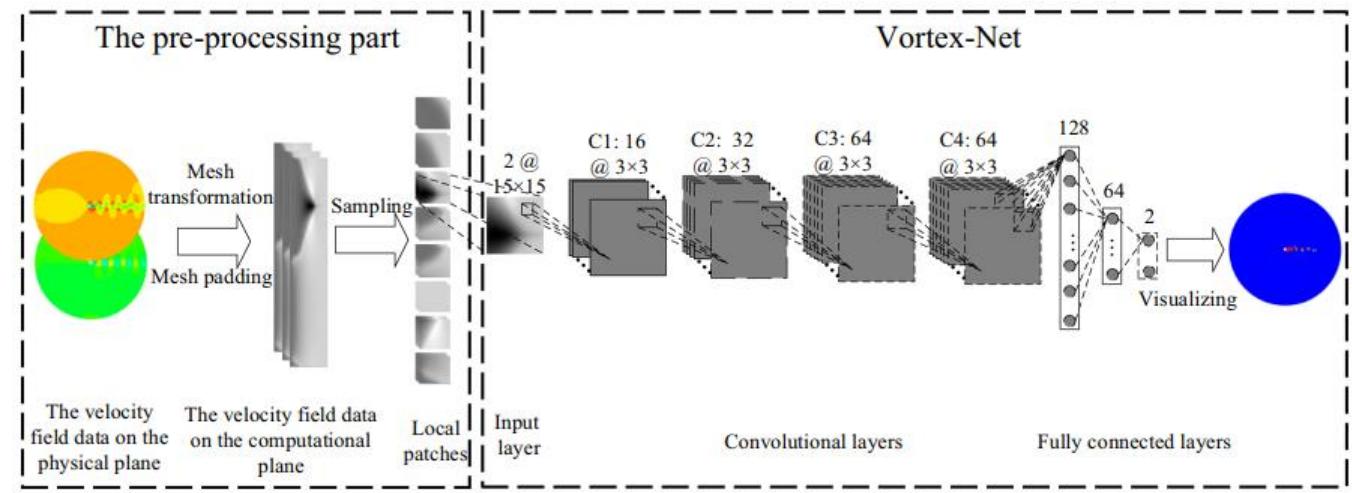


FlowNet [Han et al. 2018]

# CNNs for Vortex Extraction



EddyNet [Lguensat et al. 2017]

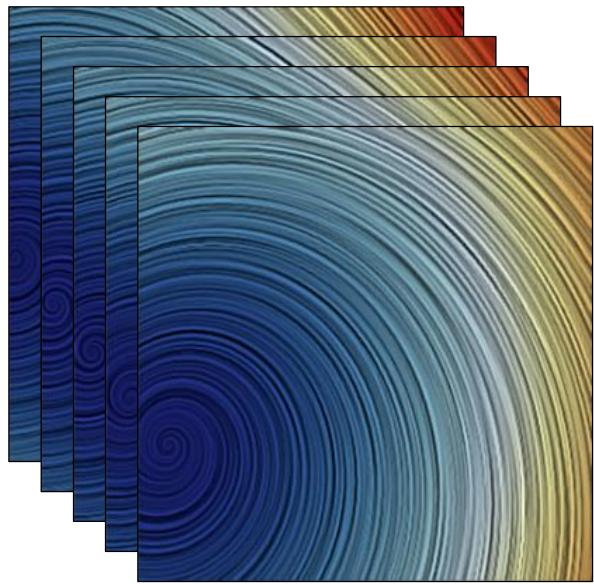


VortexNet [Deng et al. 2018]

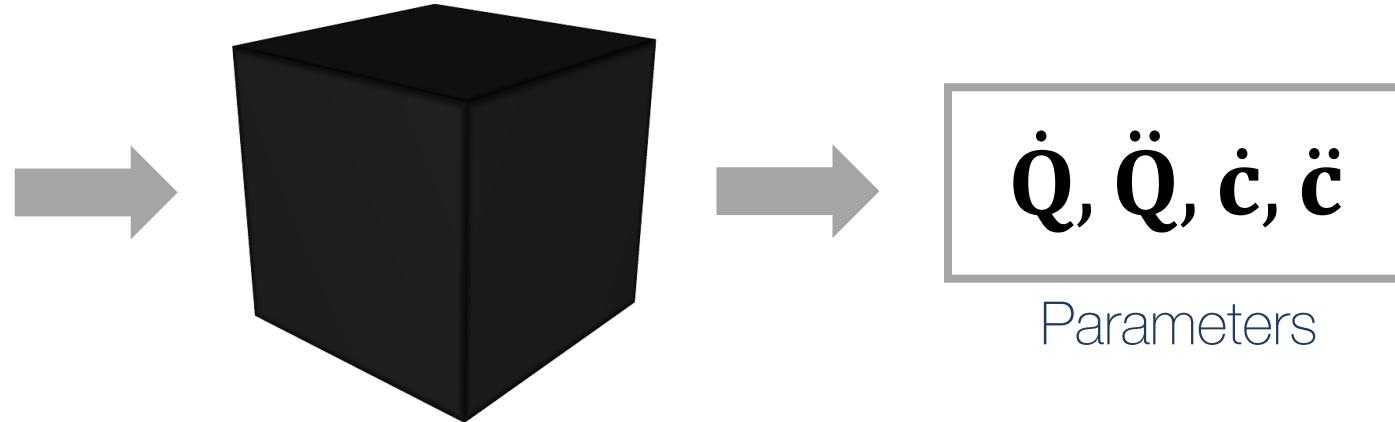
# Overview

# Deep Learning of Reference Frame Extraction

## » Overview



Corrupted Unsteady Flow

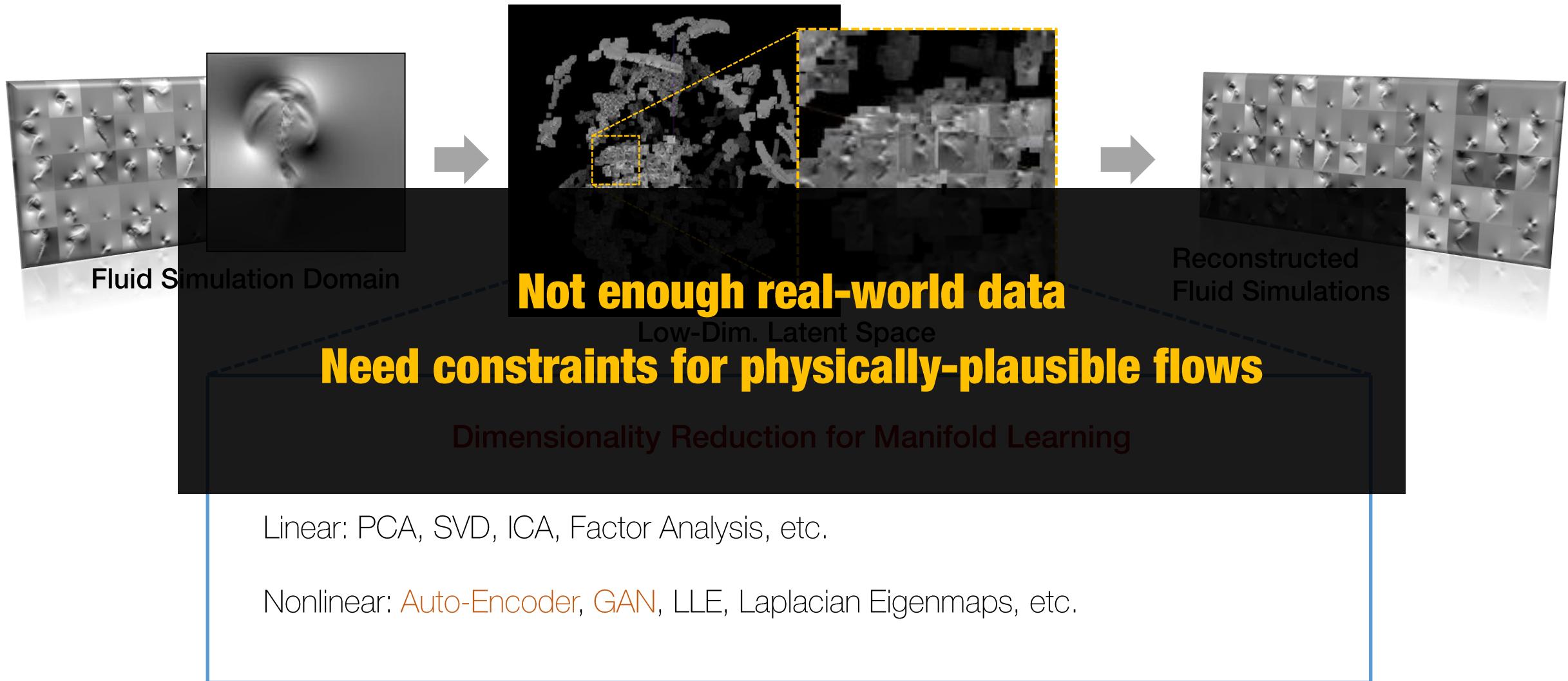


1. Synthesize a steady flow
2. Transform to unsteady flows
3. Degenerate with noise and resampling artifacts
4. Supervised learning

# Synthetic Generation of Vector Fields

# Parametric Mixture Model for Vector Fields

## » Learning a Fluid Data Manifold



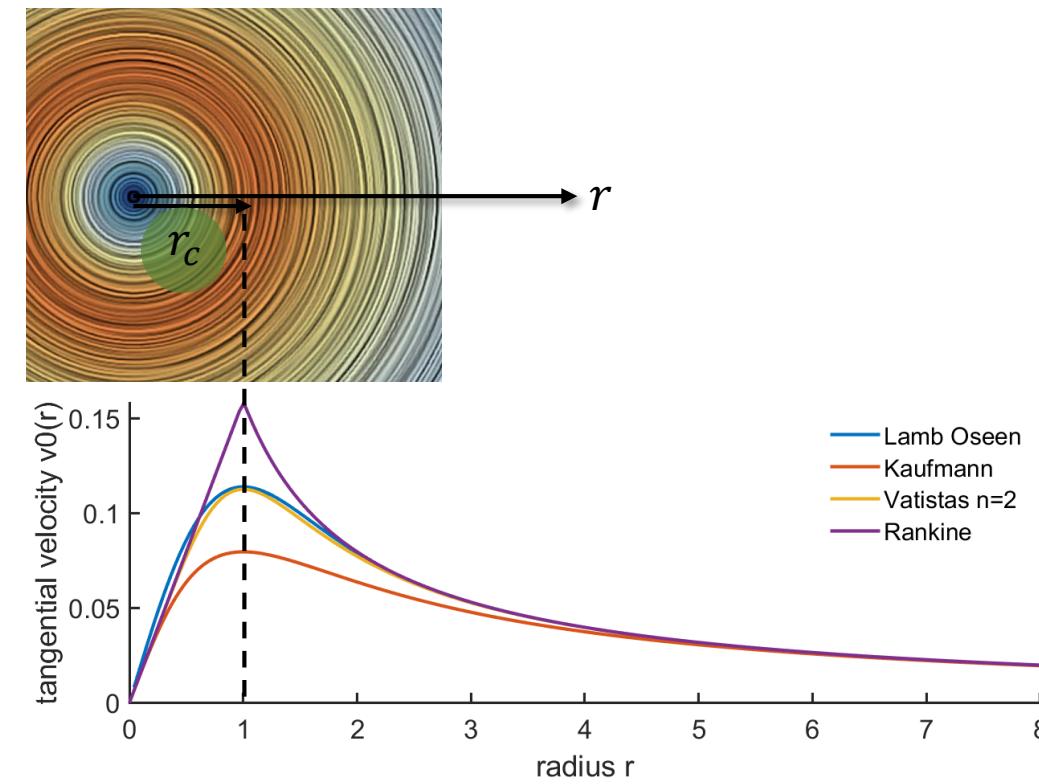
[Slide from Kim et al. 2018]

## Vatistas Vortex Velocity Profile [Vatistas et al. 1991]

- Tangential flow velocity of a rotationally-symmetric unit vortex

$$v_0(r) = \frac{r}{2\pi r_c^2 \left( \left(\frac{r}{r_c}\right)^{2n} + 1 \right)^{\frac{1}{n}}}$$

radius with maximal velocity      exponent  
shape



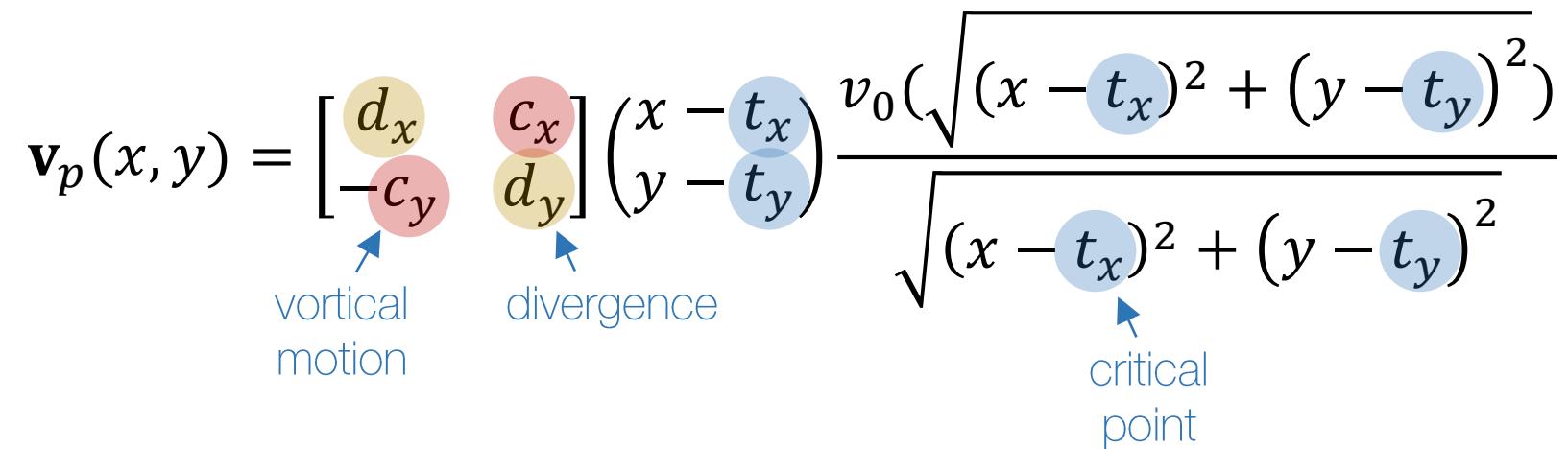
8-Dimensional Parametric Model for a Steady Flow Primitive

$$\mathbf{v}_p(x, y) = \begin{bmatrix} d_x \\ -c_y \end{bmatrix} \begin{bmatrix} c_x \\ d_y \end{bmatrix} \begin{pmatrix} x - t_x \\ y - t_y \end{pmatrix} \frac{v_0 \sqrt{(x - t_x)^2 + (y - t_y)^2}}{\sqrt{(x - t_x)^2 + (y - t_y)^2}}$$

critical point

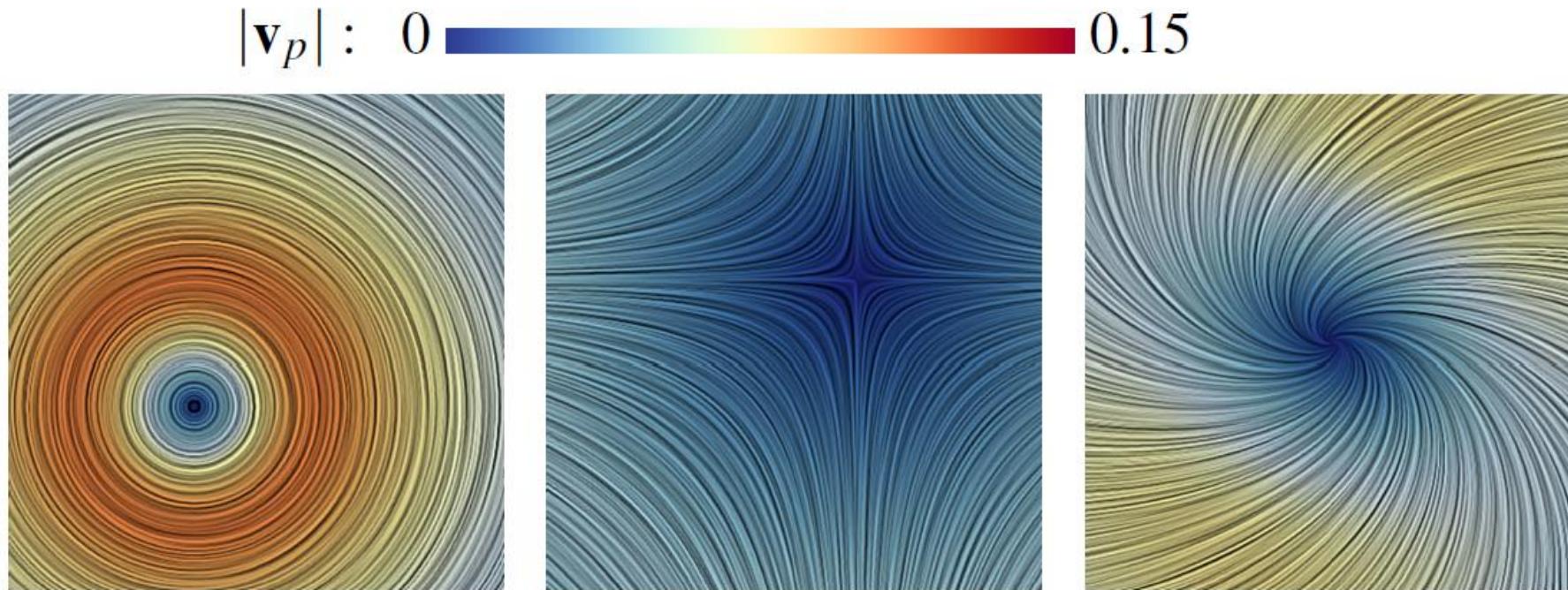
divergence

vortical motion



# Parametric Mixture Model for Vector Fields

## » Example of 2D Steady Flows from Our Model



$\mathbf{c} = (1, 1), \quad \mathbf{d} = (0, 0), \quad \mathbf{c} = (0, 0), \quad \mathbf{d} = (1, -1), \quad \mathbf{c} = (1, \frac{1}{2}), \quad \mathbf{d} = (1, 1),$   
 $\mathbf{t} = (-\frac{1}{2}, -\frac{1}{2}), r_c = 1, n = 2 \quad \mathbf{t} = (\frac{1}{2}, \frac{1}{2}), r_c = 3, n = 8 \quad \mathbf{t} = (0, 0), r_c = 2, n = 2$

## » Parameter Space Fitting

$$\mathbf{v}(x, y) = \sum_{p=1}^m \mathbf{v}_p(x, y)$$

A mixture model of  $m$  flow primitives

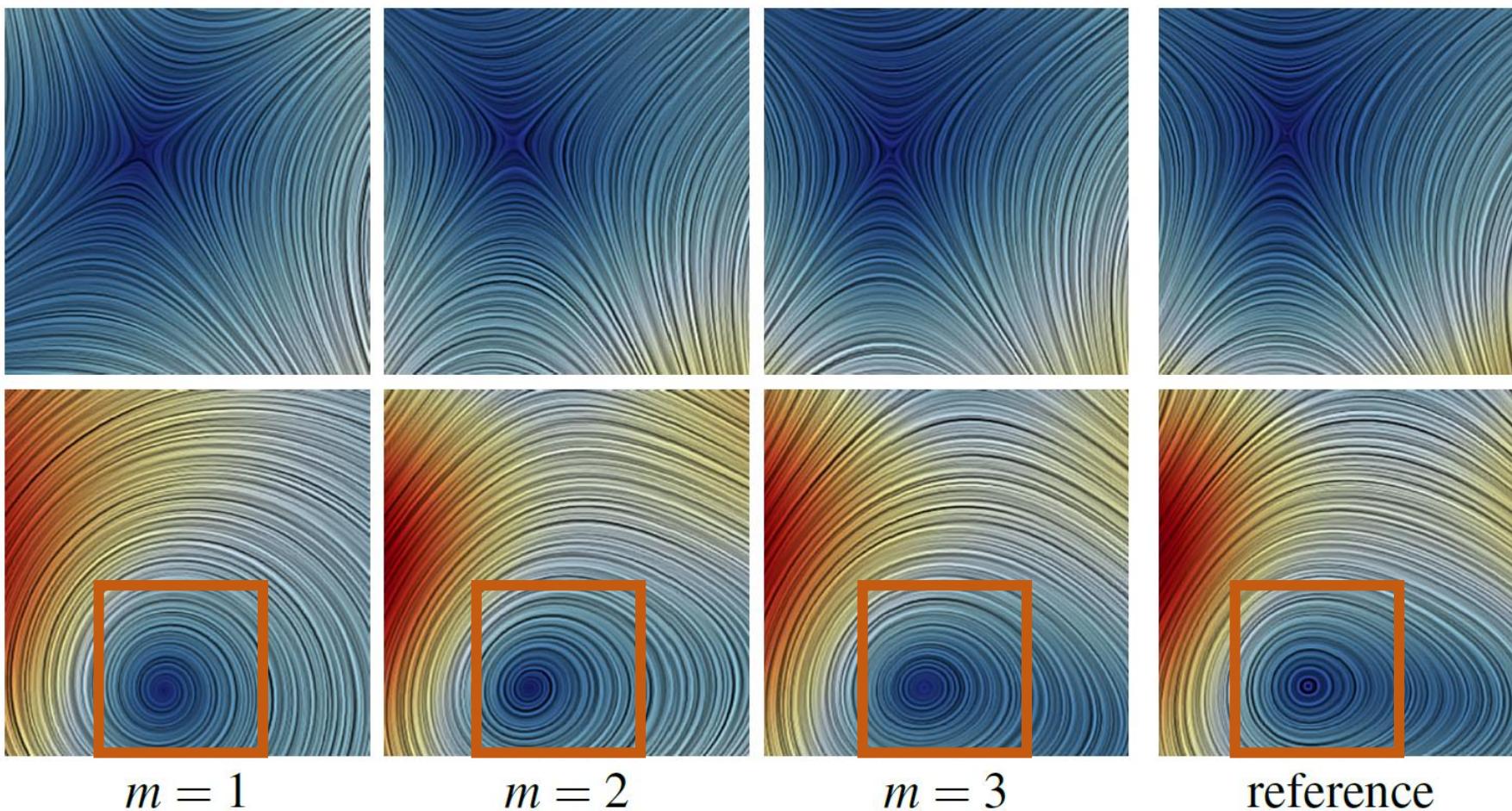
→ How can we restrict the parameter space to physically-plausible flows?

### Parameter Space Fitting!

- Extract optimal reference frame
- Simulated annealing + Gradient Descent
- $\mathcal{L}(\hat{\mathbf{v}}, \mathbf{v}) = \|\hat{\mathbf{v}} - \mathbf{v}\|_1 + \lambda \|\nabla \hat{\mathbf{v}} - \nabla \mathbf{v}\|_1$  [Kim et al. 2018]

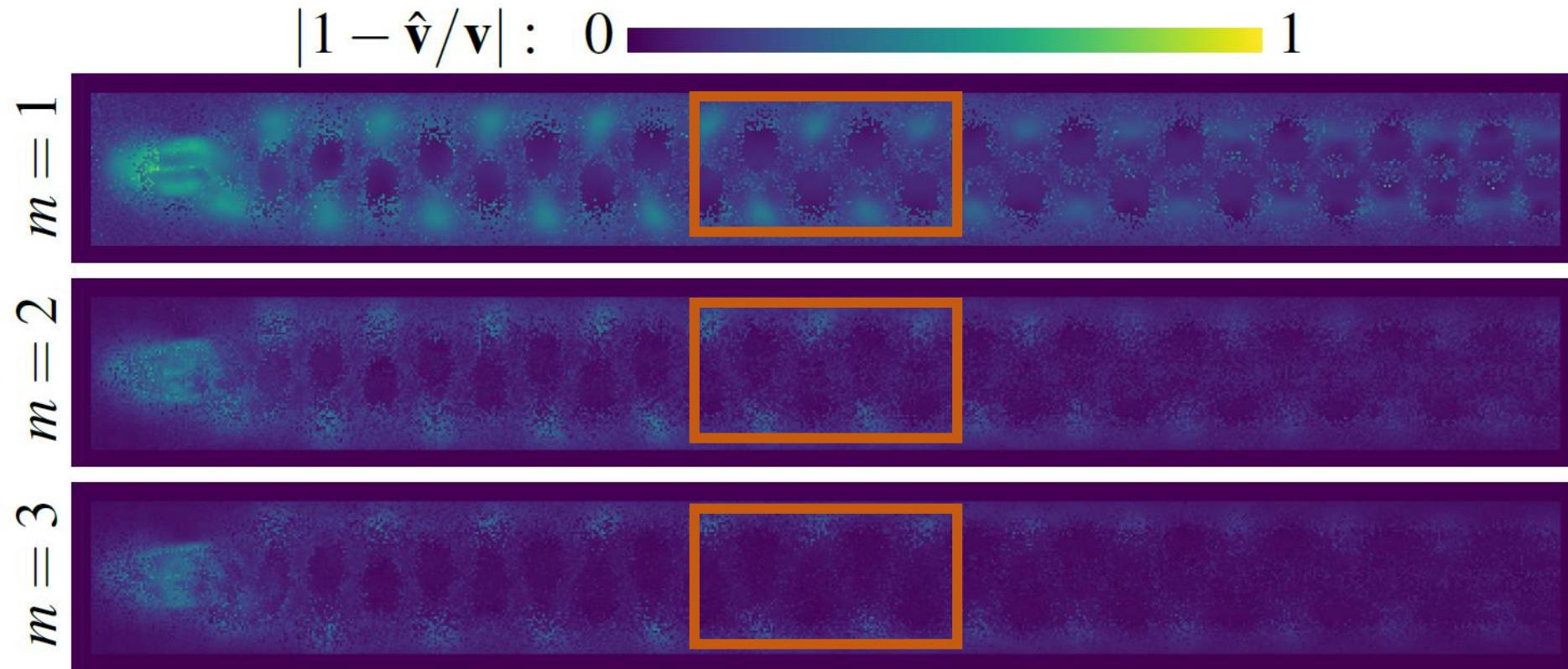
# Parametric Mixture Model for Vector Fields

## » Fitting Results for Selected Vector Field Patches



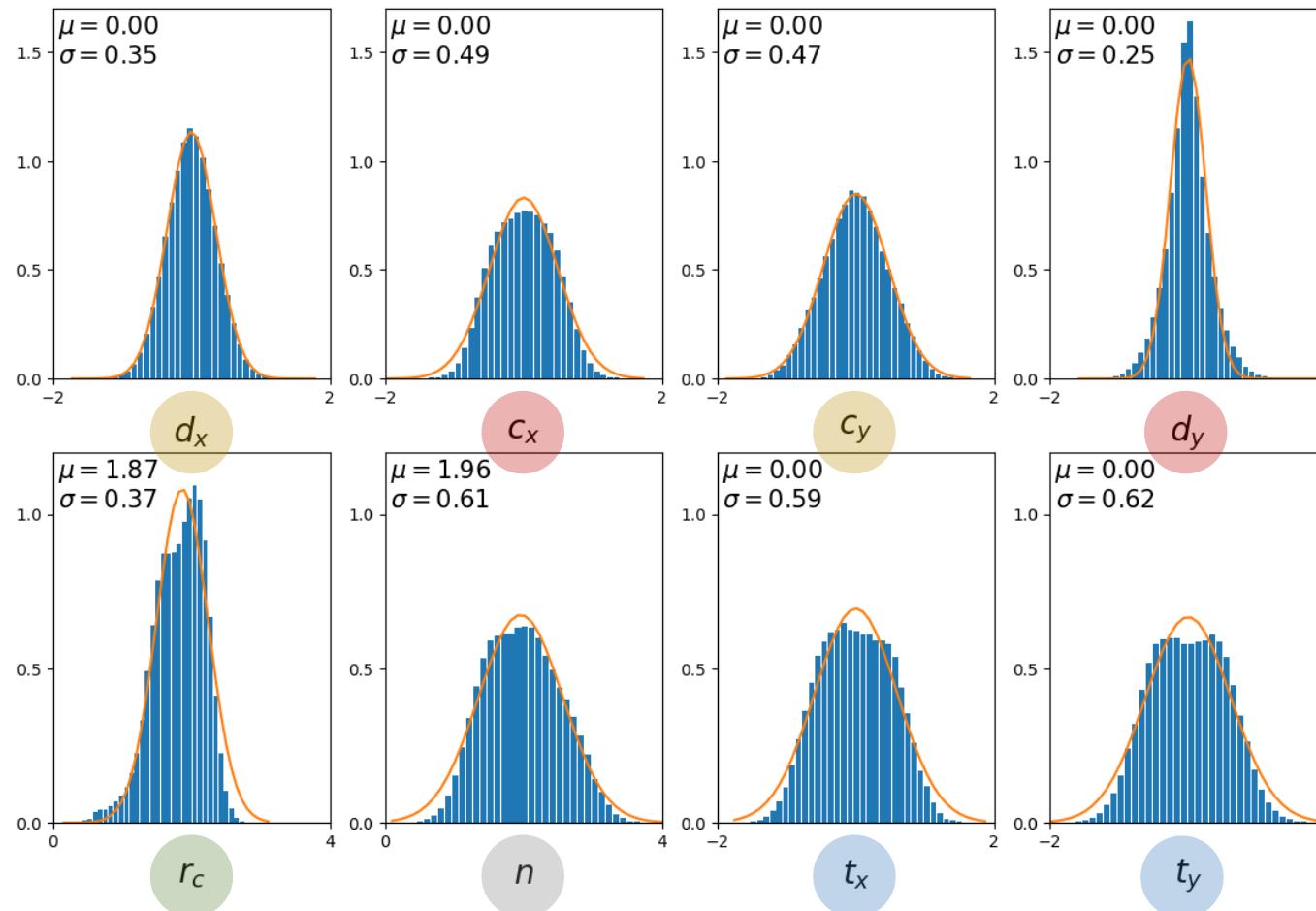
# Parametric Mixture Model for Vector Fields

## » Heat Maps of the Fitting Residual



# Parametric Mixture Model for Vector Fields

## » Histograms of the Individual Model Parameters

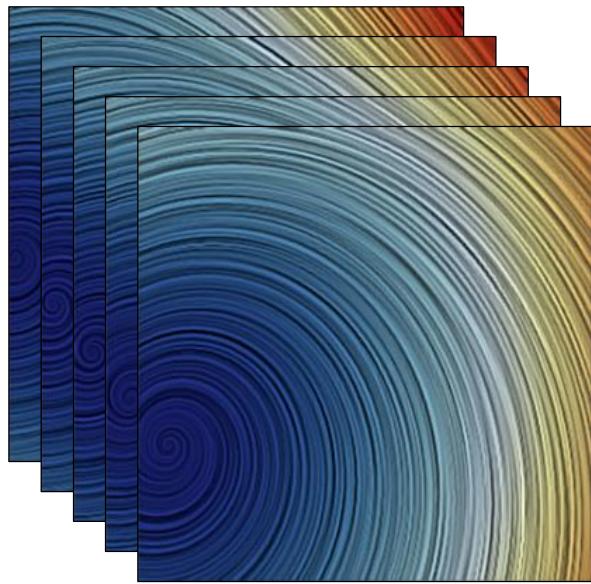


Allows sampling for further steady vector field patches

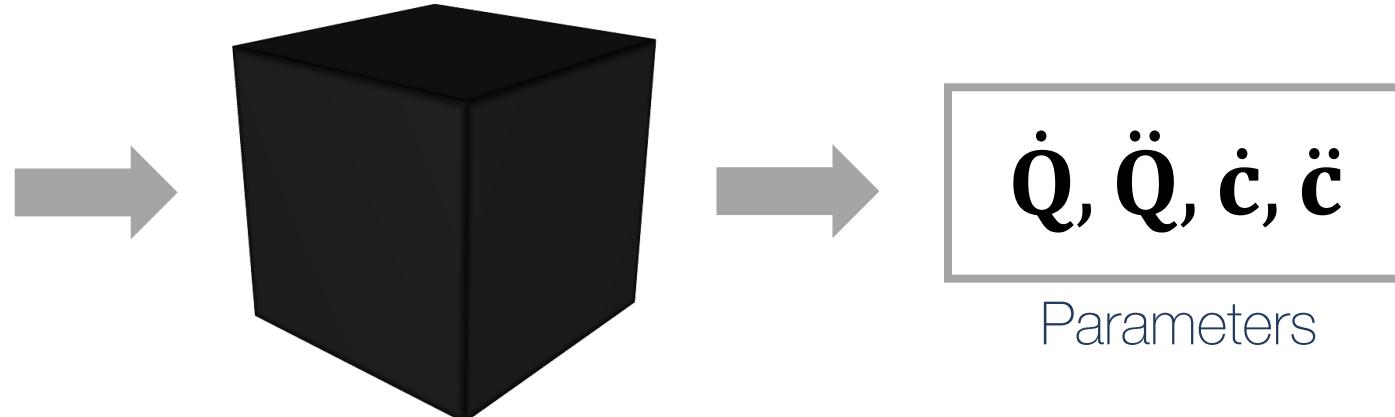
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# Deep Learning of Reference Frame Extraction

## » Overview



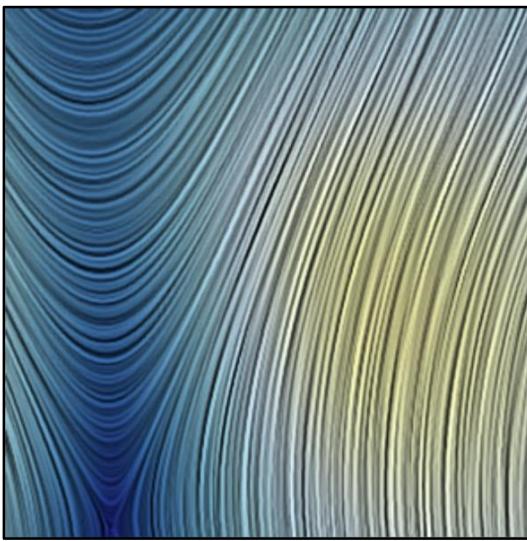
Corrupted Unsteady Flow



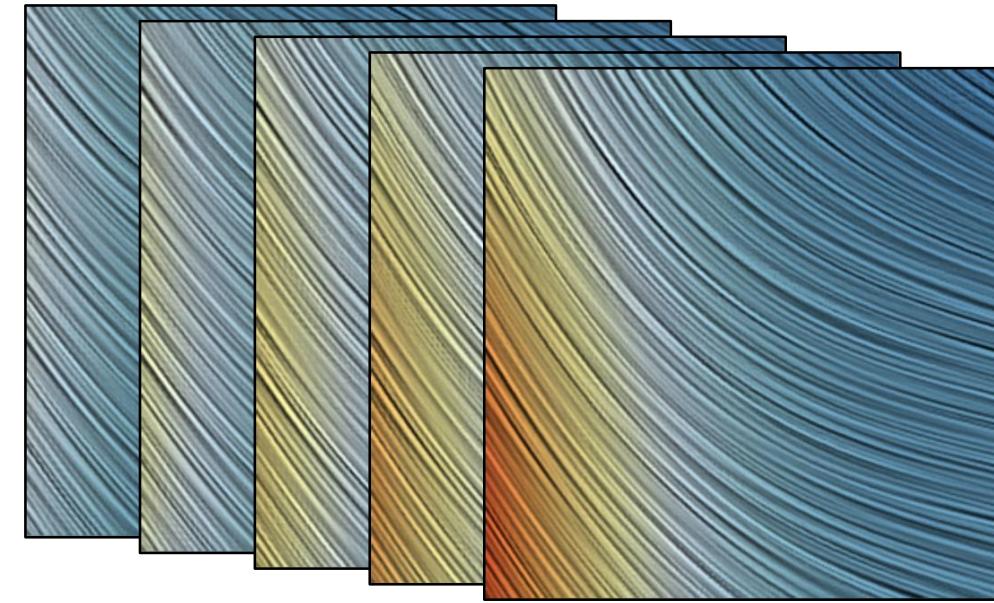
1. Synthesize a steady flow
2. Transform to unsteady flows
3. Degenerate with noise and resampling artifacts
4. Supervised learning

# Deep Learning of Reference Frame Extraction

## » Dataset



Steady Field  $\mathbf{v}$  from a  
Mixture Model

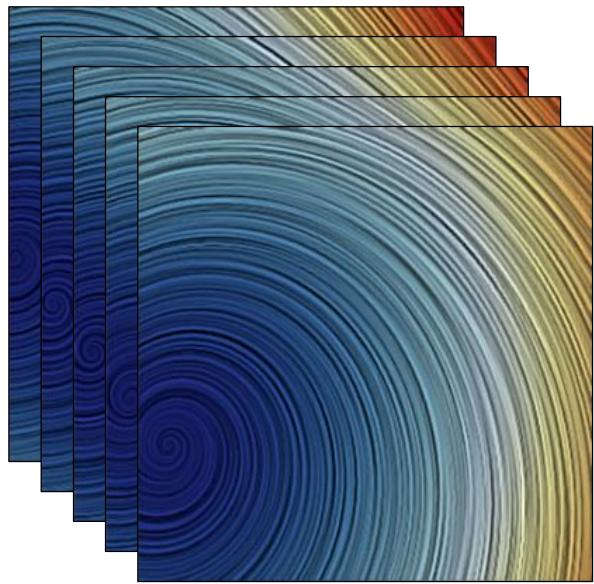


Unsteady Fields  $\mathbf{v}^*$

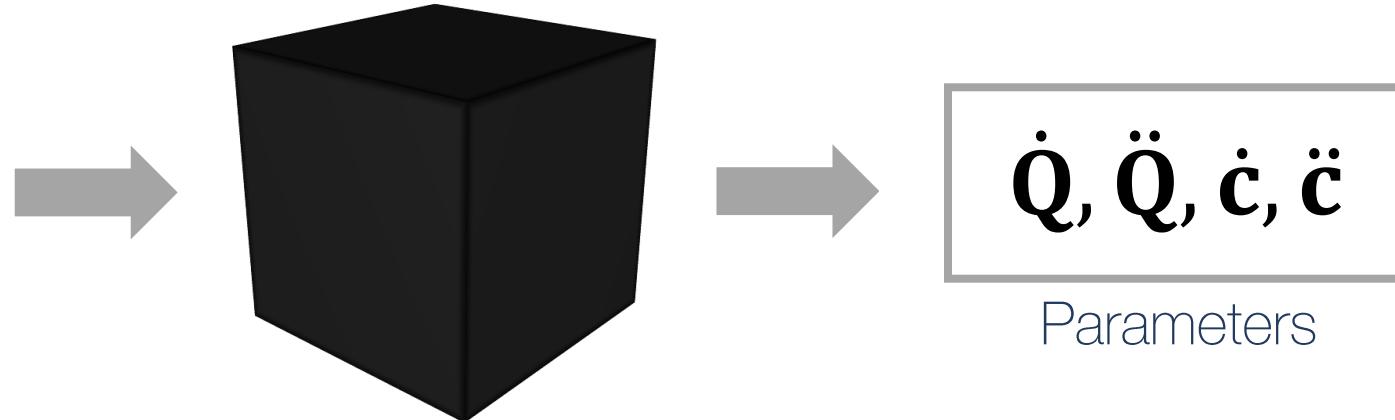
Transformation:  $\mathbf{v}^*(\mathbf{x}^*, t^*) = \mathbf{Q}(t)\mathbf{v}(\mathbf{x}, t) + \dot{\mathbf{Q}}(t)\mathbf{x} + \dot{\mathbf{c}}(t)$

$$\mathbf{x} = \mathbf{Q}(t)^T(\mathbf{x}^* - \mathbf{c}(t)), \quad t = t^* + a$$

## » Overview

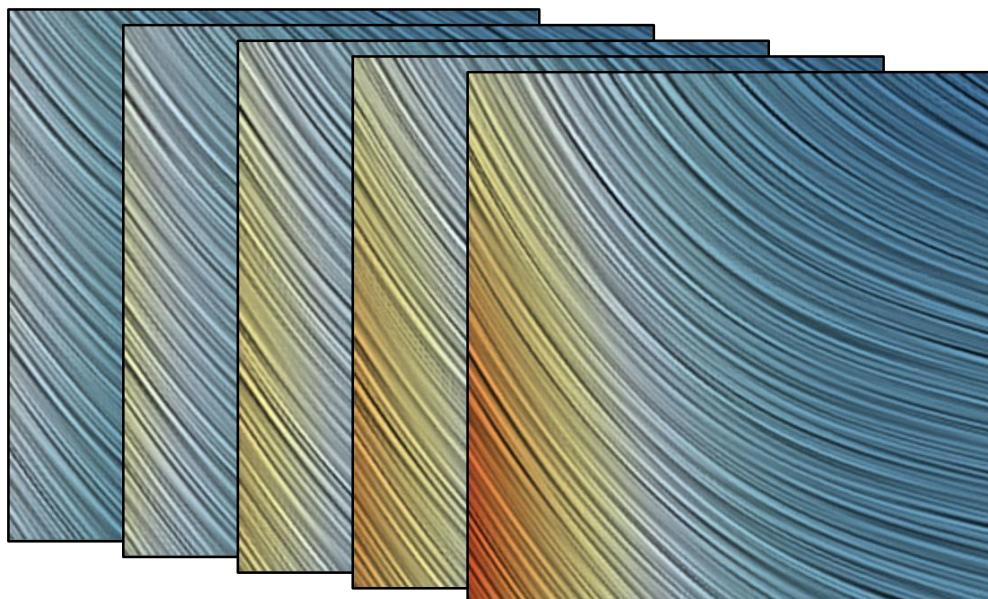


Corrupted Unsteady Flow

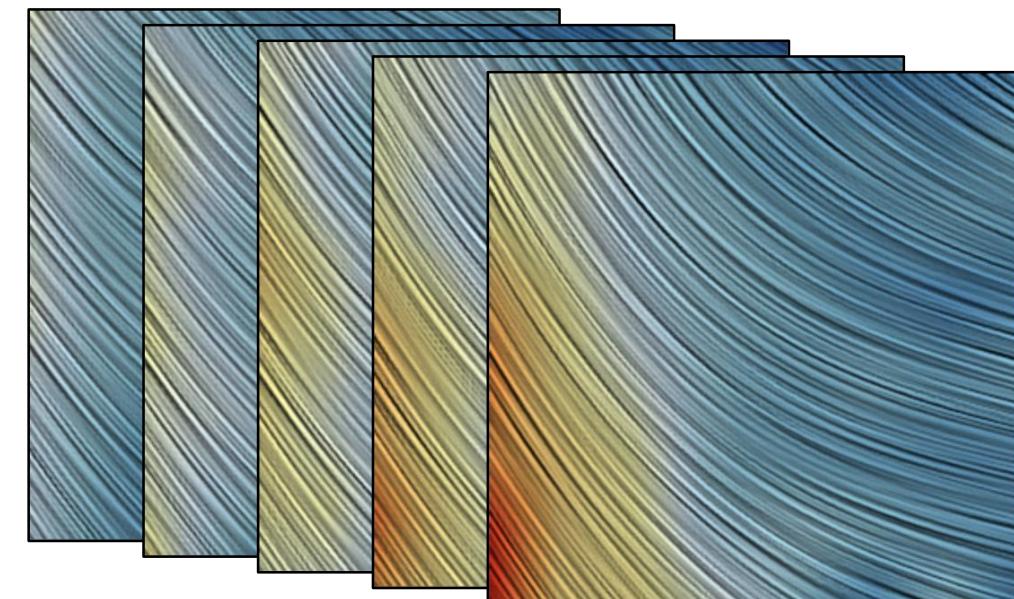


1. Synthesize a steady flow
2. Transform to unsteady flows
3. Degenerate with noise and resampling artifacts
4. Supervised learning

## » Dataset



Unsteady Fields

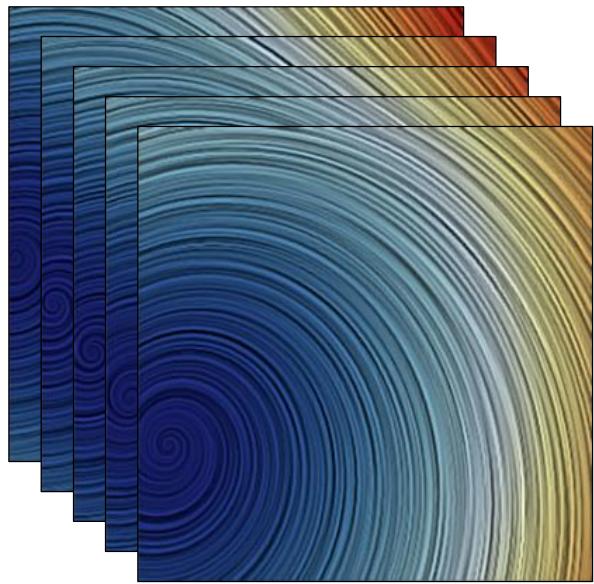


Degenerated Unsteady Fields

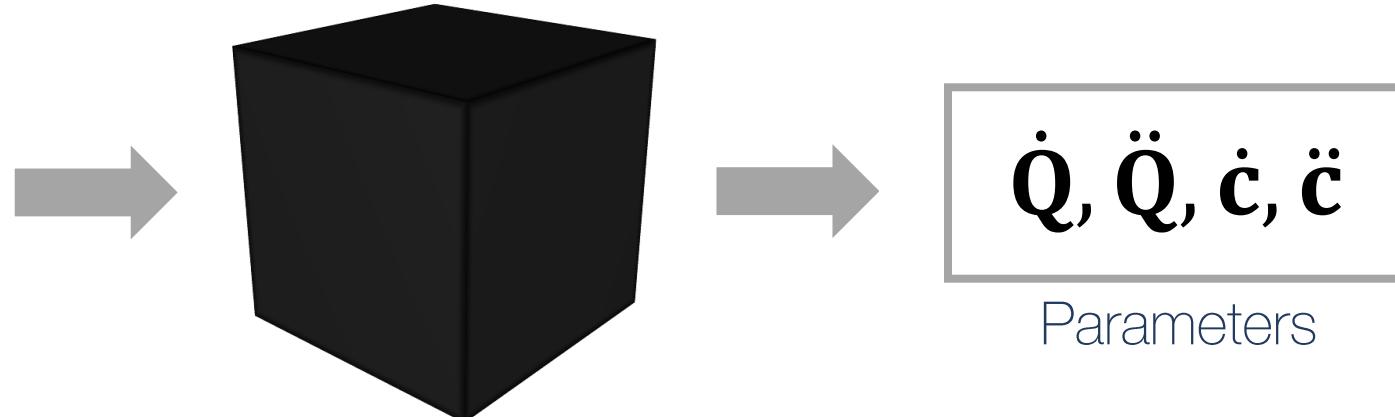
## Degeneration

- Additive uniform noise
- Down-up resampling as distortion artifacts

## » Overview



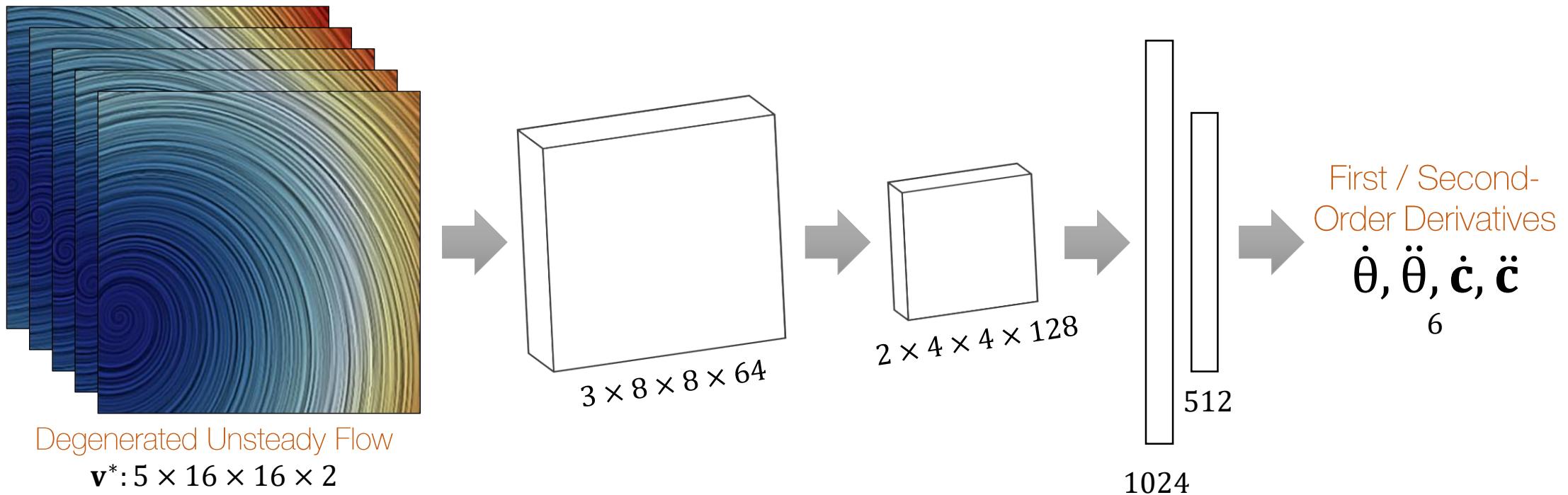
Corrupted Unsteady Flow



1. Synthesize a steady flow
2. Transform to unsteady flows
3. Degenerate with noise and resampling artifacts
4. Supervised learning

# Deep Learning of Reference Frame Extraction

## » Architecture



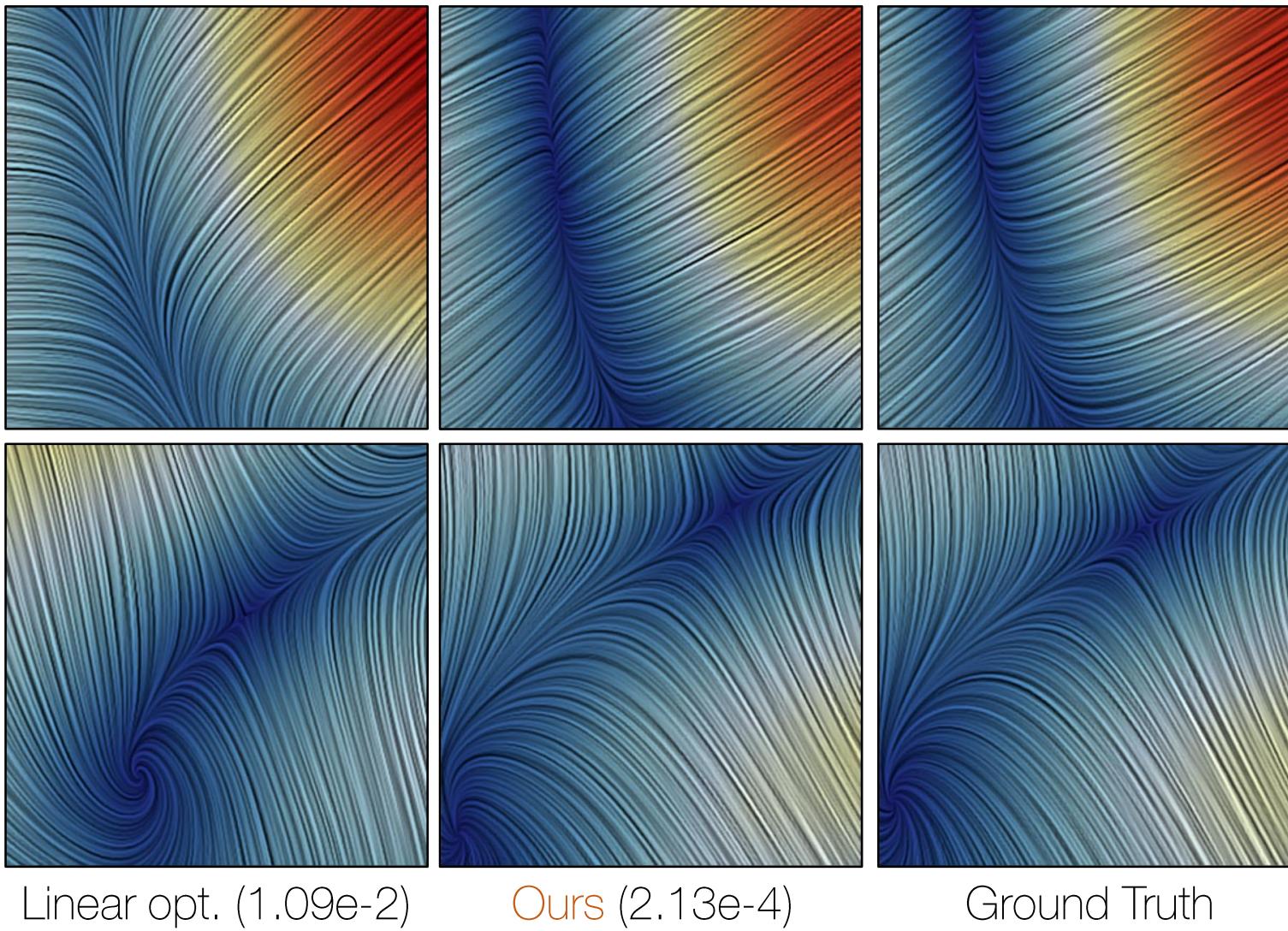
## Architecture

- 3D convolutional kernels for feature extraction
- Followed by batch normalization and ReLU layer
- MLP for the final inference

# Result

# Result

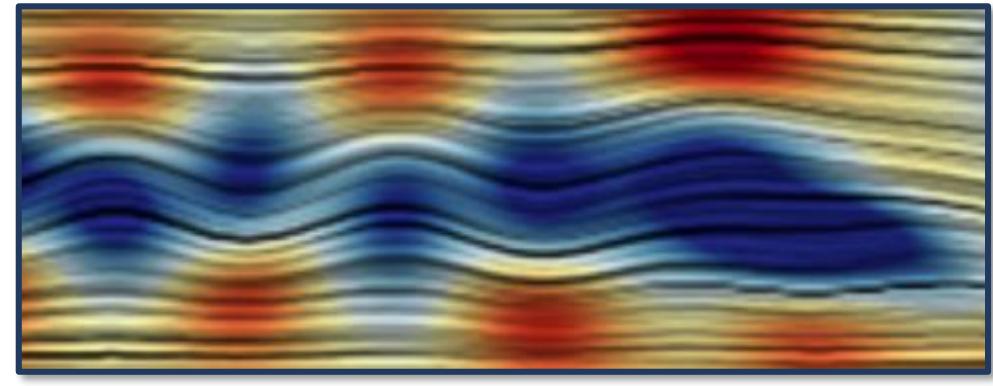
## » Vortex Extraction on Test Splits



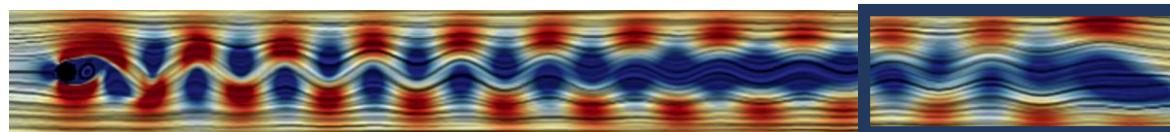
## » Validation on Numerical Data

### Cylinder flow

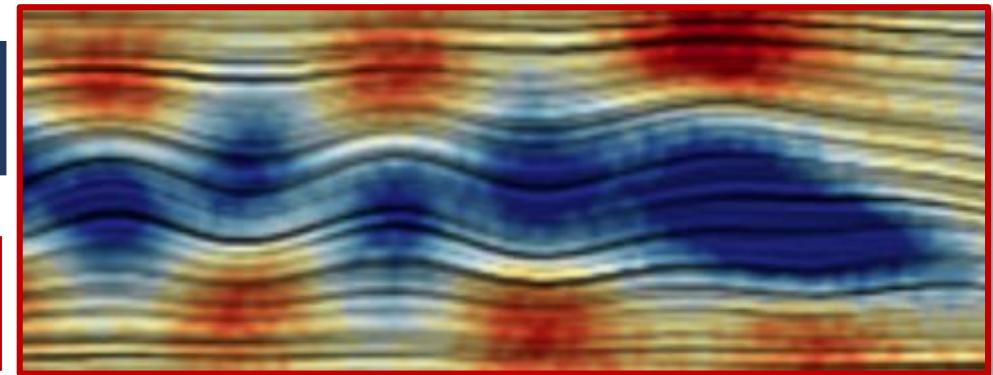
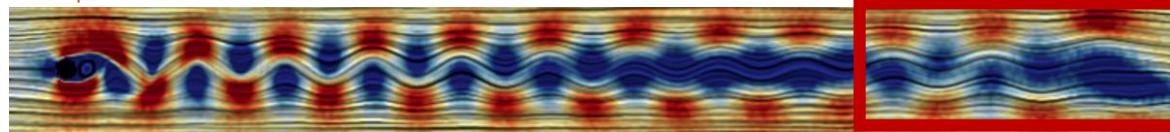
- Resolution:  $640 \times 80 \times 5$
- Window size:  $16 \times 16 \times 5$ 
  - Stride: 1, Batch size: 256
  - 159 steps for 40,625 windows



Original Data

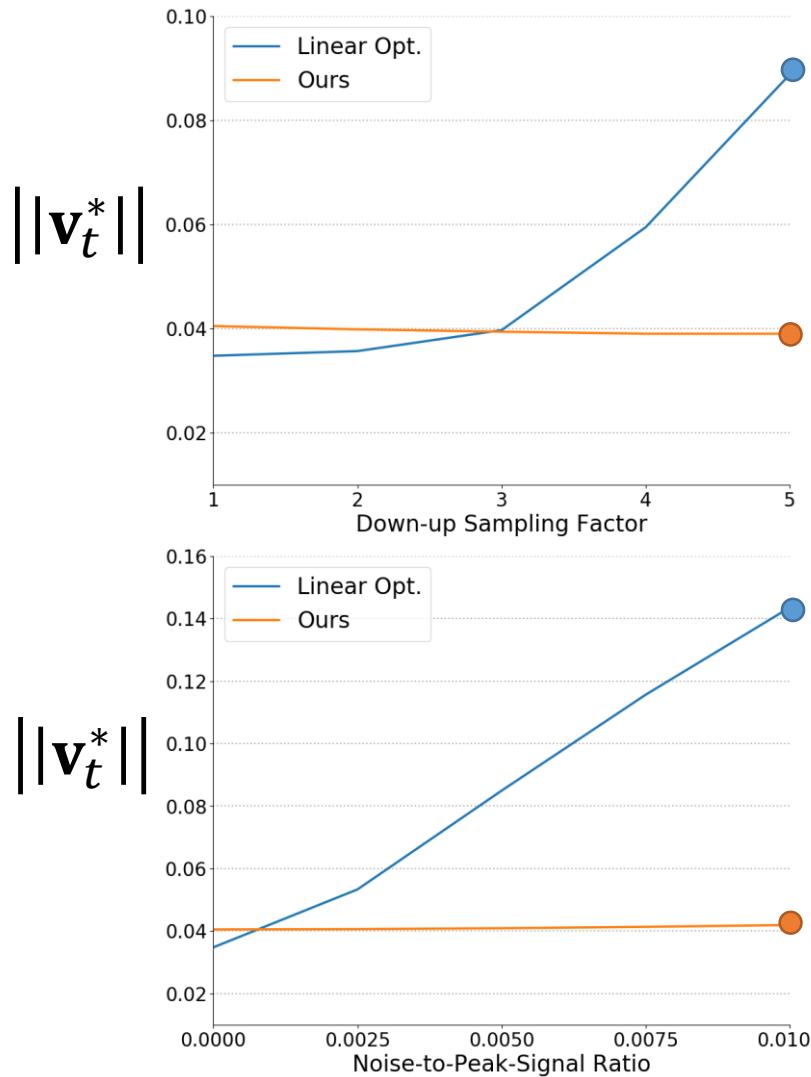


Impaired Data



# Result

## » Validation on Numerical Data



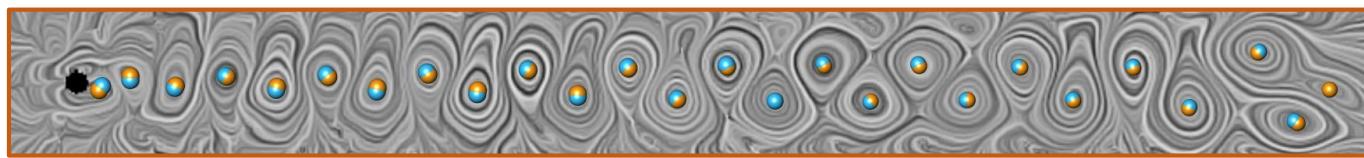
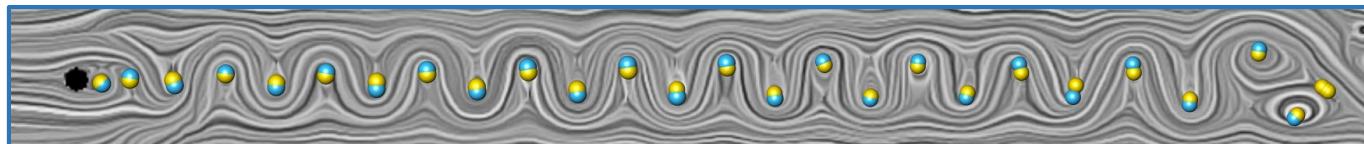
Linear Opt.

Ours

Linear Opt.

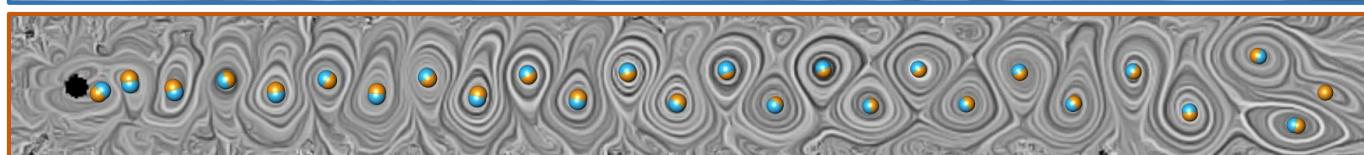
Ours

GT Linear Ours



Ours

Linear Opt.

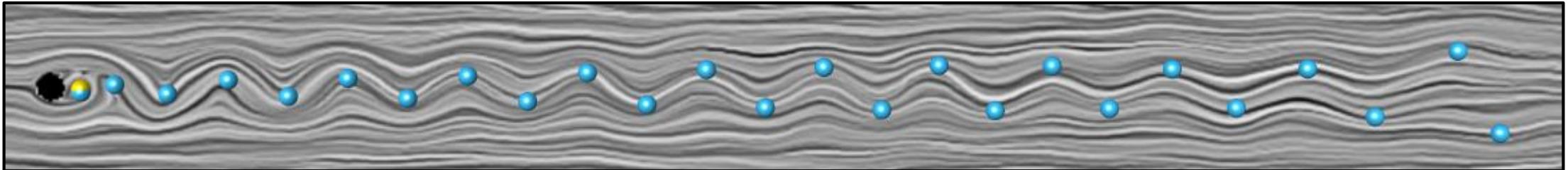


Ours

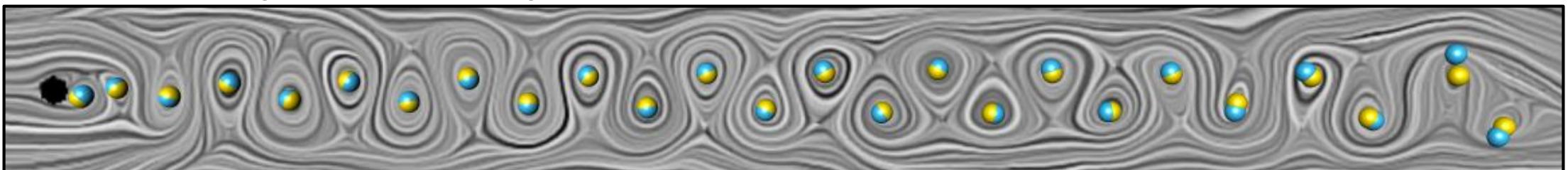
# Result

## » Validation on Numerical Data

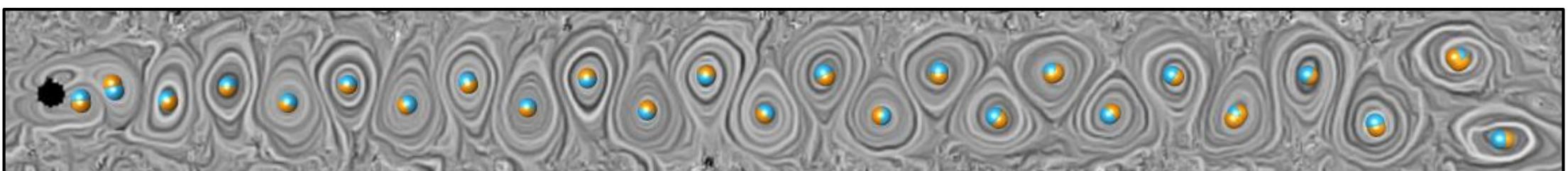
Linear Opt. on noise 10%



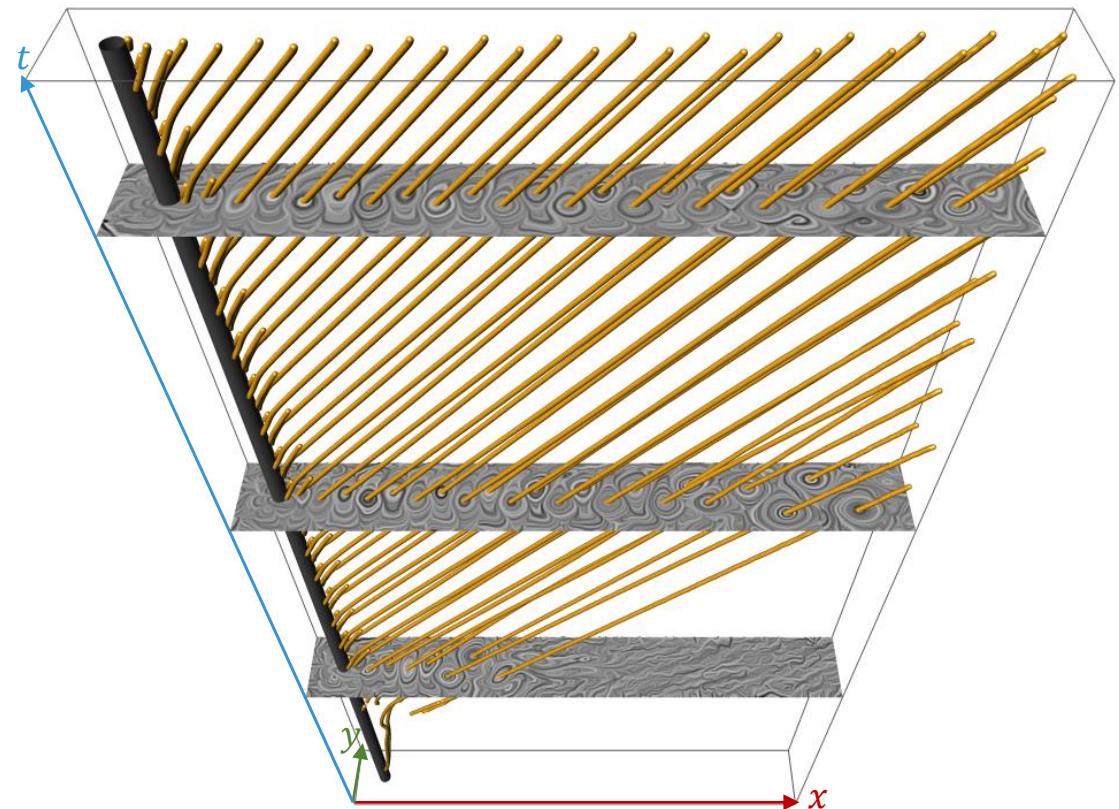
Linear Opt. after gaussian smoothing (7x7)



Ours



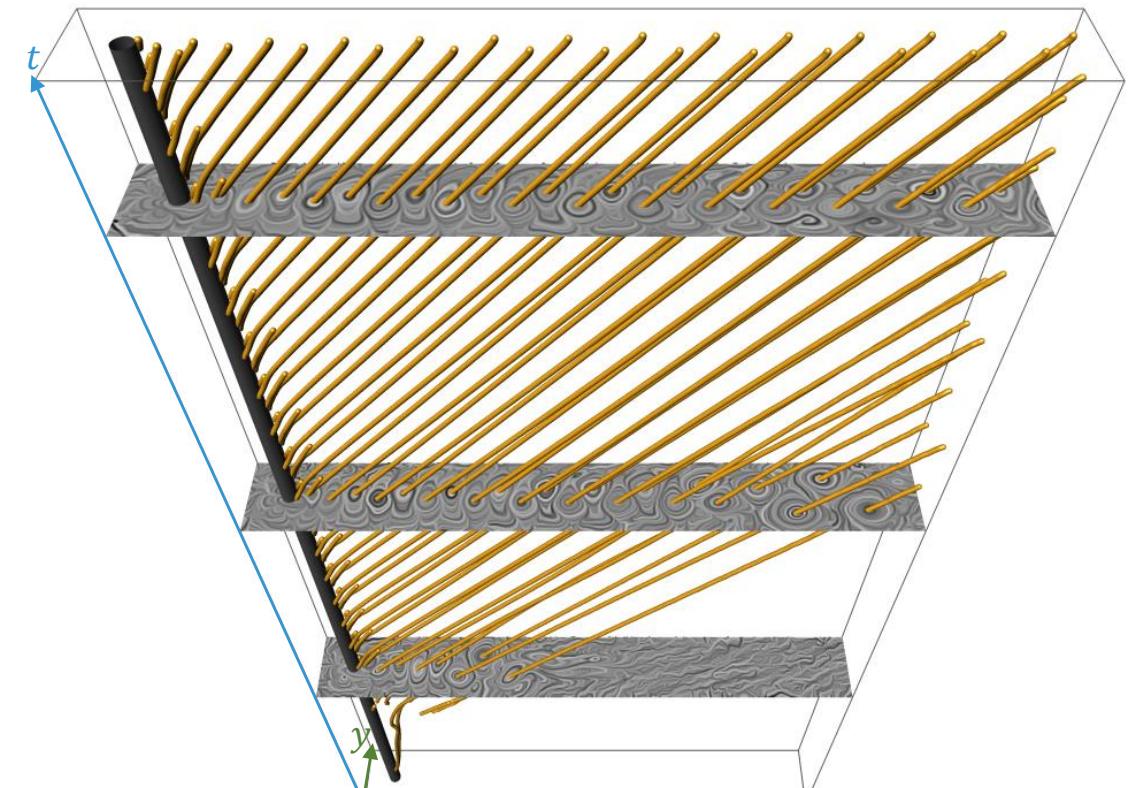
- Our network has not seen obstacles or boundary data
- Our parametric mixture model can be improved for better accuracy
- Extension to 3D



Our CNN-based approach on Noisy Data

## » Summary

- We utilize a CNN to combine two steps of the visualization pipeline in an end-to-end manner: the **filtering** and the **feature extraction**.
- By conditioning the neural network to **noisy** inputs and **resampling artifacts**, we obtain **numerically more stable** results than existing optimization-based approaches.
- We formulate a **parametric vector field mixture model** based on Vatistas velocity profile **useful** for any local **deep learning-based** feature extraction.



Our **CNN-based** approach on **Noisy Data**



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