induced graph  $\mathcal{G}_{\mathbf{R}}$ 

