induced graph $\mathcal{G}_{\mathbf{R}}$