

```
# Keller K(4) Clique - BY Bouneb Zine El Abidine
# example of solution found by our program clique size: 12 and
validated by hand
# Clique vertices: [23, 33, 47, 65, 79, 89, 135, 160, 171,
197, 204, 233]
# Each vertex and its neighbors in the graph
#####
#####
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Vertex 1: ID = 23 [0,1,1,3]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 1 | 5 | 9 | 12 | 13 | 14 | 15 | 17 | 25 | 28 | 29 | 30 | 33 | 37 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 41 | 44 | 45 | 46 | 47 | 48 | | | | | | | | | |
| | 49 | 50 | 51 | 52 | 53 | 54 | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 |
| 65 | 69 | 73 | 76 | 77 | 78 | | | | | | | | | |
| | 79 | 81 | 85 | 89 | 92 | 93 | 94 | 95 | 97 | 101 | 105 | 108 | 109 | 110 |
| 111 | 112 | 113 | 114 | 115 | 116 | | | | | | | | | |
| | 117 | 118 | 119 | 120 | 121 | 122 | 123 | 124 | 125 | 126 | 127 | 128 | 129 | 130 |
| 131 | 132 | 133 | 134 | 135 | 136 | | | | | | | | | |
| | 137 | 138 | 139 | 140 | 141 | 142 | 143 | 144 | 145 | 146 | 147 | 148 | 149 | 150 |
| 152 | 153 | 154 | 155 | 156 | 157 | | | | | | | | | |
| | 158 | 159 | 160 | 161 | 162 | 163 | 164 | 165 | 166 | 167 | 168 | 169 | 170 | 171 |
| 172 | 173 | 174 | 175 | 176 | 177 | | | | | | | | | |
| | 178 | 179 | 180 | 181 | 182 | 183 | 184 | 185 | 186 | 187 | 188 | 189 | 190 | 191 |
| 193 | 197 | 201 | 204 | 205 | 206 | | | | | | | | | |
| | 207 | 209 | 213 | 217 | 220 | 221 | 222 | 223 | 225 | 229 | 233 | 236 | 237 | 238 |
| 239 | 240 | 241 | 242 | 243 | 244 | | | | | | | | | |
| | 245 | 246 | 247 | 248 | 249 | 250 | 251 | 252 | 253 | 254 | 255 | | | |

Vertex 2: ID = 33 [0,2,0,1]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

0 2 3 4 5 6 7 8 9 10 11 12 13 14
15 19 23 24 25 26

| | | | | | | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| | 27 | 31 | 39 | 40 | 42 | 43 | 47 | 51 | 55 | 56 | 57 | 58 | 59 | 63 |
| 64 | 65 | 66 | 67 | 68 | 69 | | | | | | | | | |
| | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 83 | 87 | 88 | 89 |
| 90 | 91 | 95 | 99 | 103 | 104 | | | | | | | | | |
| | 105 | 106 | 107 | 111 | 115 | 119 | 120 | 121 | 122 | 123 | 127 | 128 | 129 | 130 |
| 131 | 132 | 133 | 134 | 135 | 136 | | | | | | | | | |
| | 137 | 138 | 139 | 140 | 141 | 142 | 143 | 144 | 145 | 146 | 147 | 148 | 149 | 150 |
| 151 | 152 | 153 | 154 | 155 | 156 | | | | | | | | | |
| | 157 | 158 | 159 | 160 | 162 | 163 | 164 | 165 | 166 | 167 | 168 | 169 | 170 | 171 |
| 172 | 173 | 174 | 175 | 176 | 177 | | | | | | | | | |
| | 178 | 179 | 180 | 181 | 182 | 183 | 184 | 185 | 186 | 187 | 188 | 189 | 190 | 191 |
| 192 | 193 | 194 | 195 | 196 | 197 | | | | | | | | | |
| | 198 | 199 | 200 | 201 | 202 | 203 | 204 | 205 | 206 | 207 | 211 | 215 | 216 | 217 |
| 218 | 219 | 223 | 227 | 231 | 232 | | | | | | | | | |
| | 233 | 234 | 235 | 239 | 243 | 247 | 248 | 249 | 250 | 251 | 255 | | | |

Vertex 3: ID = 47 [0,2,3,3]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 14 | 17 | 20 | 21 | 22 | 23 | | | | | | | | | |
| | 25 | 29 | 33 | 36 | 37 | 38 | 41 | 49 | 52 | 53 | 54 | 55 | 57 | 61 |
| 64 | 65 | 66 | 67 | 68 | 69 | | | | | | | | | |
| | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 81 | 84 | 85 | 86 |
| 87 | 89 | 93 | 97 | 100 | 101 | | | | | | | | | |
| | 102 | 103 | 105 | 109 | 113 | 116 | 117 | 118 | 119 | 121 | 125 | 128 | 129 | 130 |
| 131 | 132 | 133 | 134 | 135 | 136 | | | | | | | | | |
| | 137 | 138 | 139 | 140 | 141 | 142 | 143 | 144 | 145 | 146 | 147 | 148 | 149 | 150 |
| 151 | 152 | 153 | 154 | 155 | 156 | | | | | | | | | |
| | 157 | 158 | 159 | 160 | 161 | 162 | 163 | 164 | 165 | 166 | 167 | 168 | 169 | 170 |
| 171 | 172 | 173 | 174 | 176 | 177 | | | | | | | | | |
| | 178 | 179 | 180 | 181 | 182 | 183 | 184 | 185 | 186 | 187 | 188 | 189 | 190 | 191 |
| 192 | 193 | 194 | 195 | 196 | 197 | | | | | | | | | |
| | 198 | 199 | 200 | 201 | 202 | 203 | 204 | 205 | 206 | 207 | 209 | 212 | 213 | 214 |
| 215 | 217 | 221 | 225 | 228 | 229 | | | | | | | | | |
| | 230 | 231 | 233 | 237 | 241 | 244 | 245 | 246 | 247 | 249 | 253 | | | |

Vertex 4: ID = 65 [1,0,0,1]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 3 | 7 | 8 | 9 | 10 | 11 | 15 | 19 | 23 | 24 | 25 | 26 | 27 | 31 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 32 | 33 | 34 | 35 | 36 | 37 | | | | | | | | | |
| | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 51 | 55 | 56 | 57 |
| 58 | 59 | 63 | 71 | 72 | 74 | | | | | | | | | |
| | 75 | 79 | 83 | 87 | 88 | 89 | 90 | 91 | 95 | 96 | 98 | 99 | 100 | 101 |
| 102 | 103 | 104 | 105 | 106 | 107 | | | | | | | | | |
| | 108 | 109 | 110 | 111 | 115 | 119 | 120 | 121 | 122 | 123 | 127 | 131 | 135 | 136 |
| 137 | 138 | 139 | 143 | 147 | 151 | | | | | | | | | |
| | 152 | 153 | 154 | 155 | 159 | 160 | 161 | 162 | 163 | 164 | 165 | 166 | 167 | 168 |
| 169 | 170 | 171 | 172 | 173 | 174 | | | | | | | | | |
| | 175 | 179 | 183 | 184 | 185 | 186 | 187 | 191 | 192 | 194 | 195 | 196 | 197 | 198 |
| 199 | 200 | 201 | 202 | 203 | 204 | | | | | | | | | |
| | 205 | 206 | 207 | 208 | 209 | 210 | 211 | 212 | 213 | 214 | 215 | 216 | 217 | 218 |
| 219 | 220 | 221 | 222 | 223 | 224 | | | | | | | | | |
| | 225 | 226 | 227 | 228 | 229 | 230 | 231 | 232 | 233 | 234 | 235 | 236 | 237 | 238 |
| 239 | 240 | 241 | 242 | 243 | 244 | | | | | | | | | |
| | 245 | 246 | 247 | 248 | 249 | 250 | 251 | 252 | 253 | 254 | 255 | | | |

Vertex 5: ID = 79 [1,0,3,3]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 1 | 4 | 5 | 6 | 7 | 9 | 13 | 17 | 20 | 21 | 22 | 23 | 25 | 29 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 32 | 33 | 34 | 35 | 36 | 37 | | | | | | | | | |
| | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 49 | 52 | 53 | 54 |
| 55 | 57 | 61 | 65 | 68 | 69 | | | | | | | | | |
| | 70 | 73 | 81 | 84 | 85 | 86 | 87 | 89 | 93 | 96 | 97 | 98 | 99 | 100 |
| 101 | 102 | 103 | 104 | 105 | 106 | | | | | | | | | |
| | 107 | 108 | 109 | 110 | 113 | 116 | 117 | 118 | 119 | 121 | 125 | 129 | 132 | 133 |
| 134 | 135 | 137 | 141 | 145 | 148 | | | | | | | | | |
| | 149 | 150 | 151 | 153 | 157 | 160 | 161 | 162 | 163 | 164 | 165 | 166 | 167 | 168 |
| 169 | 170 | 171 | 172 | 173 | 174 | | | | | | | | | |
| | 175 | 177 | 180 | 181 | 182 | 183 | 185 | 189 | 192 | 193 | 194 | 195 | 196 | 197 |

198 199 200 201 202 203
204 205 206 208 209 210 211 212 213 214 215 216 217 218
219 220 221 222 223 224
225 226 227 228 229 230 231 232 233 234 235 236 237 238
239 240 241 242 243 244
245 246 247 248 249 250 251 252 253 254 255

Vertex 6: ID = 89 [1,1,2,1]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 0 | 1 | 2 | 3 | 7 | 11 | 15 | 16 | 17 | 18 | 19 | 23 | 27 | 31 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 32 | 33 | 34 | 35 | 39 | 43 | | | | | | | | | |
| | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | | | | | | | | | |
| | 67 | 71 | 75 | 79 | 80 | 82 | 83 | 87 | 95 | 96 | 97 | 98 | 99 | 103 |
| 107 | 111 | 112 | 113 | 114 | 115 | | | | | | | | | |
| | 116 | 117 | 118 | 119 | 120 | 122 | 123 | 124 | 125 | 126 | 127 | 128 | 129 | 130 |
| 131 | 135 | 139 | 143 | 144 | 145 | | | | | | | | | |
| | 146 | 147 | 151 | 155 | 159 | 160 | 161 | 162 | 163 | 167 | 171 | 175 | 176 | 177 |
| 178 | 179 | 180 | 181 | 182 | 183 | | | | | | | | | |
| | 184 | 185 | 186 | 187 | 188 | 189 | 190 | 191 | 192 | 193 | 194 | 195 | 196 | 197 |
| 198 | 199 | 200 | 201 | 202 | 203 | | | | | | | | | |
| | 204 | 205 | 206 | 207 | 208 | 209 | 210 | 211 | 212 | 213 | 214 | 215 | 216 | 218 |
| 219 | 220 | 221 | 222 | 223 | 224 | | | | | | | | | |
| | 225 | 226 | 227 | 228 | 229 | 230 | 231 | 232 | 233 | 234 | 235 | 236 | 237 | 238 |
| 239 | 240 | 241 | 242 | 243 | 244 | | | | | | | | | |
| | 245 | 246 | 247 | 248 | 249 | 250 | 251 | 252 | 253 | 254 | 255 | | | |

Vertex 7: ID = 135 [2,0,1,3]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 15 | 16 | 17 | 18 | 19 | 20 | | | | | | | | | |
| | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 |

Vertex 8: ID = 160 [2,2,0,0]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 14 | 15 | 16 | 17 | 18 | 19 | | | | | | | | | |
| | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 33 | 34 |
| 35 | 36 | 37 | 38 | 39 | 40 | | | | | | | | | |
| | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 |
| 55 | 56 | 57 | 58 | 59 | 60 | | | | | | | | | |
| | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 |
| 75 | 76 | 77 | 78 | 79 | 82 | | | | | | | | | |
| | 86 | 88 | 89 | 90 | 91 | 94 | 98 | 102 | 104 | 105 | 106 | 107 | 110 | 114 |
| 118 | 120 | 121 | 122 | 123 | 126 | | | | | | | | | |
| | 129 | 130 | 131 | 132 | 133 | 134 | 135 | 136 | 137 | 138 | 139 | 140 | 141 | 142 |
| 143 | 146 | 150 | 152 | 153 | 154 | | | | | | | | | |
| | 155 | 158 | 166 | 169 | 170 | 171 | 174 | 178 | 182 | 184 | 185 | 186 | 187 | 190 |
| 192 | 193 | 194 | 195 | 196 | 197 | | | | | | | | | |
| | 198 | 199 | 200 | 201 | 202 | 203 | 204 | 205 | 206 | 207 | 210 | 214 | 216 | 217 |
| 218 | 219 | 222 | 226 | 230 | 232 | | | | | | | | | |
| | 233 | 234 | 235 | 238 | 242 | 246 | 248 | 249 | 250 | 251 | 254 | | | |

Vertex 9: ID = 171 [2,2,2,3]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | | | | | | | | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| 14 | 15 | 16 | 17 | 18 | 19 | | | | | | | | | |
| | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 |
| 34 | 35 | 36 | 37 | 38 | 39 | | | | | | | | | |
| | 40 | 41 | 42 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 |
| 55 | 56 | 57 | 58 | 59 | 60 | | | | | | | | | |
| | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 |
| 75 | 76 | 77 | 78 | 79 | 80 | | | | | | | | | |
| | 81 | 82 | 83 | 85 | 89 | 93 | 96 | 97 | 98 | 99 | 101 | 105 | 109 | 112 |
| 113 | 114 | 115 | 117 | 121 | 125 | | | | | | | | | |
| | 128 | 129 | 130 | 131 | 132 | 133 | 134 | 135 | 136 | 137 | 138 | 140 | 141 | 142 |
| 143 | 144 | 145 | 146 | 147 | 149 | | | | | | | | | |
| | 153 | 157 | 160 | 161 | 162 | 165 | 173 | 176 | 177 | 178 | 179 | 181 | 185 | 189 |
| 192 | 193 | 194 | 195 | 196 | 197 | | | | | | | | | |
| | 198 | 199 | 200 | 201 | 202 | 203 | 204 | 205 | 206 | 207 | 208 | 209 | 210 | 211 |
| 213 | 217 | 221 | 224 | 225 | 226 | | | | | | | | | |
| | 227 | 229 | 233 | 237 | 240 | 241 | 242 | 243 | 245 | 249 | 253 | | | |

Vertex 10: ID = 197 [3,0,1,1]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

166 167 168 169 170 171 172 173 174 175 179 183 187 188
189 190 191 195 203 204
206 207 211 215 219 220 221 222 223 224 225 226 227 228
230 231 232 233 234 235
236 237 238 239 243 247 251 252 253 254 255

Vertex 11: ID = 204 [3,0,3,0]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 2 | 4 | 5 | 6 | 7 | 10 | 14 | 18 | 20 | 21 | 22 | 23 | 26 | 30 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 32 | 33 | 34 | 35 | 36 | 37 | | | | | | | | | |
| | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 50 | 52 | 53 | 54 |
| 55 | 58 | 62 | 64 | 65 | 66 | | | | | | | | | |
| | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 77 | 78 | 79 | 80 | 81 |
| 82 | 83 | 84 | 85 | 86 | 87 | | | | | | | | | |
| | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 | 101 |
| 102 | 103 | 104 | 105 | 106 | 107 | | | | | | | | | |
| | 108 | 109 | 110 | 111 | 112 | 113 | 114 | 115 | 116 | 117 | 118 | 119 | 120 | 121 |
| 122 | 123 | 124 | 125 | 126 | 127 | | | | | | | | | |
| | 130 | 132 | 133 | 134 | 135 | 138 | 142 | 146 | 148 | 149 | 150 | 151 | 154 | 158 |
| 160 | 161 | 162 | 163 | 164 | 165 | | | | | | | | | |
| | 166 | 167 | 168 | 169 | 170 | 171 | 172 | 173 | 174 | 175 | 178 | 180 | 181 | 182 |
| 183 | 186 | 190 | 194 | 197 | 198 | | | | | | | | | |
| | 199 | 202 | 210 | 212 | 213 | 214 | 215 | 218 | 222 | 224 | 225 | 226 | 227 | 228 |
| 229 | 230 | 231 | 232 | 233 | 234 | | | | | | | | | |
| | 235 | 237 | 238 | 239 | 242 | 244 | 245 | 246 | 247 | 250 | 254 | | | |

Vertex 12: ID = 233 [3,2,2,1]

Total neighbors: 171

Neighbors in clique: 11/11

All neighbors (171):

| | 67 | 68 | 69 | 70 | 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 81 | 82 | 83 | 84 | 85 | 86 | | | | | | | | | |
| | 87 | 88 | 89 | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |
| 101 | 102 | 103 | 104 | 106 | 107 | | | | | | | | | |
| | 108 | 109 | 110 | 111 | 112 | 113 | 114 | 115 | 116 | 117 | 118 | 119 | 120 | 121 |
| 122 | 123 | 124 | 125 | 126 | 127 | | | | | | | | | |
| | 128 | 129 | 130 | 131 | 132 | 133 | 134 | 135 | 136 | 137 | 138 | 139 | 140 | 141 |
| 142 | 143 | 144 | 145 | 146 | 147 | | | | | | | | | |
| | 151 | 155 | 159 | 160 | 161 | 162 | 163 | 167 | 171 | 175 | 176 | 177 | 178 | 179 |
| 183 | 187 | 191 | 192 | 193 | 194 | | | | | | | | | |
| | 195 | 196 | 197 | 198 | 199 | 200 | 202 | 203 | 204 | 205 | 206 | 207 | 208 | 209 |
| 210 | 211 | 215 | 219 | 223 | 224 | | | | | | | | | |
| | 226 | 227 | 231 | 239 | 240 | 241 | 242 | 243 | 247 | 251 | 255 | | | |

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