LiU Default

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Maximum Bipartite Cardinality Matching	7	using namespace std;	
Articulation points and bridges	7	#define rep(i, a, b) for(int i = (a); i < int(b); ++i)	
Dijkstra	7	#define rrep(i, a, b) for(int i = (a); i >= int(b);i)	
Dijkstra Timetable	7	<pre>#define trav(it, v) for(typeof((v).begin()) it=(v).begin(); it!=(v).end();</pre>	++
Bellman Ford	8	<pre>it) #define all(x) (x).begin(),(x).end()</pre>	
Euler Tour	8	<pre>#define B begin()</pre>	
Edmond Karp	8	#define E end()	
Maxflow Binblock	8	#define pb push_back	
Flood Fill	9	typedef pair <int, int=""> ii; // used in comp prog algorithms</int,>	
Topological Sort	9	typedef double fl;	
Strongly Connected Components	9	typedef long double ld; typedef long long l1;	
Chinese Postman	10	typedef pair <int, int=""> pii;</int,>	

```
typedef vector <int> vi;
typedef vector <vi> vvi;
typedef map <int, int> mii;
typedef multimap <int, int> mmii;
typedef set <int> si;
typedef multiset <int> msi;
typedef complex <fl> cx;

const int UNVISITED = -1;
const int INF = 1e9;
const double EPS = 1e-9;
const double PI = acos(-1.0); // alternative (2.0 * acos(0.0))
```

Complexity

Modern CPU compute 100M in 3s.

\overline{n}	Worst AC Algorithm	Problem
$\leq [1011]$	$O(n!), O(n^6)$	e.g. Enumerating permutations
$\leq [1518]$	$O(2^n n^2)$	e.g. DP TSP
$\leq [1822]$	$O(2^n n)$	e.g. DP with bitmask
≤ 100	$O(n^4)$	e.g. DP with 3 dimensions
≤ 400	$O(n^3)$	e.g. Floyd Warshall's
$\leq 2K$	$O(n^2 log n)$	e.g. $2 loops + a tree-related DS$
$\leq 10K$	$O(n^2)$	e.g. Selection/Insert sort
$\leq 1M$	O(nlogn)	e.g. Building Segment Tree
$\leq 100M$	O(n)	I/O bottleneck

Limits

32-bit int $2^{31} - 1 = 2147483647 \approx 10^{10}$ 64-bit signed long long upper limit $2^{63} - 1 = 9223372036854775807 \approx 10^{18}$

Data structures

Union Find

```
class UnionFind { // rank ordered with path compression
public:
    UnionFind(int n) {
        rank.assign(n, 0);
        p.assign(n, 0);
        set_size.assign(n, 1);
        num_sets = n;
        for (int i = 0; i < n; ++i)
            p[i] = i;
    }
    int find_set(int i) { return (p[i] == i) ? i : (p[i] = find_set(p[i])); }
    bool is_same_set(int i, int j) { return find_set(i) == find_set(j); }
    void union_set(int i, int j) {
        if (!is_same_set(i, j)) {
            --num_sets;
    }
}</pre>
```

```
int x = find_set(i), y = find_set(j);
            if (rank[x] > rank[v]) {
                p[v] = x;
                set_size[x] += set_size[y];
            }
            else {
                p[x] = y;
                set_size[v] += set_size[x];
                if (rank[x] == rank[y]) rank[y]++;
            }
        }
    int num_disjoint_sets() { return num_sets; }
    int size_of_set(int i) { return set_size[find_set(i)]; }
private:
    vi rank, p, set_size;
    int num sets:
};
Fenwick Tree
// Ideal to answer dynamic Range Sum Queries
#define LSOne(S) (S & (-S))
struct FenwickTree {
 vi ft:
 FenwickTree() {}
  // initialization: n + 1 zeroes, ignore index 0
  FenwickTree(int n) { ft.assign(n + 1, 0); }
  int rsq(int b) { // returns RSQ(1, b), O(log n)
   int sum = 0; for (; b; b -= LSOne(b)) sum += ft[b];
    return sum:
  int rsq(int a, int b) { // returns RSQ(a, b), O(log n)
    return rsq(b) - (a == 1 ? 0 : rsq(a - 1));
  // adjusts value of the k-th element by v
  void adjust(int k, int v) { // O(log n)
    for (; k < (int)ft.size(); k += LSOne(k)) ft[k] += v;</pre>
};
Segment Tree
class SegmentTree { // Max range query. Change >= to <= for min.</pre>
    vi st, a;
    int left(int p) { return p << 1; } // Same as binary heap</pre>
    int right(int p) { return (p << 1) + 1; }</pre>
    void build(int p, int 1, int r) { // O(n log n)
        if (1 == r)
```

st[p] = 1;

```
else {
            build(left(p), 1, (1 + r) / 2);
            build(right(p), (1 + r) / 2 + 1, r);
            int p1 = st[left(p)], p2 = st[right(p)];
            st[p] = (a[p1] >= a[p2]) ? p1 : p2; // Build max
       }
   }
    int rmq(int p, int l, int r, int i, int j) { // O(log n)
        if (i > r || j < 1) return -1; // outside of range
       if (1 >= i && r <= j) return st[p]; // inside range</pre>
        int p1 = rmg(left(p), 1, (1 + r) / 2, i, j);
        int p2 = rmq(right(p), (1 + r) / 2 + 1, r, i, j);
        if (p1 == -1) return p2;
        if (p2 == -1) return p1:
        return (a[p1] >= a[p2]) ? p1 : p2; // Return max inside
    // Support for dynamic updating. O(log n)
    int update_point(int p, int 1, int r, int idx, int new_value) {
        int i = idx, j = idx;
       if (i > r || j < 1)
            return st[p];
       if (1 == i && r == j) {
            a[i] = new value:
            return st[p] = 1;
       }
        int p1, p2;
        p1 = update_point(left(p), 1, (1 + r) / 2, idx, new_value);
        p2 = update_point(right(p), (1 + r) / 2, r, idx, new_value);
        return st[p] = (a[p1] >= a[p2]) ? p1 : p2; // Max query
   }
public:
    SegmentTree(const vi &_a) {
       a = _a; n = (int) a.size(); // Copy for local use
        st.assign(4 * n, 0); // Large enough of zeroes
        build(1, 0, n - 1);
    }
    // Return index of max O(log n)
    int rmq(int i, int j) { return rmq(1, 0, n - 1, i, j); }
    // Update index to a new value.
    int update_point(int idx, int new_value) {
        return update_point(1, 0, n - 1, idx, new_value);
};
```

Math

int gcd(int a, int b) { return b == 0 ? a : gcd(b, a % b); }
$$\sum_{k=1}^{\infty} x^k = \frac{1}{1-x}, |x| < 1$$

$$\sum_{k=1}^{n} x^k = \frac{1-x^n}{1-x}, x \neq 0$$

$$\sum_{k=1}^{n} k = \frac{n(n+1)}{2}$$

$$\sum_{k=1}^{n} k^2 = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{k=1}^{n} k^2 = \frac{n^2(n+1)^2}{4}$$

$$\pi \approx 3.14159265 \approx \frac{355}{113}$$

$$\sin(\frac{pi}{4}) = \cos(\frac{pi}{4}) = \frac{1}{\sqrt{2}}$$

$$\sin(\frac{pi}{3}) = \cos(\frac{pi}{3}) = \frac{1}{2}$$

$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$$

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$= \frac{2 \tan \theta}{1 + \tan^2 \theta}$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta$$

$$= 2 \cos^2 \theta - 1$$

$$= 1 - 2 \sin^2 \theta$$

$$= \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$$

Factorial

```
1 1 2 6 24 120 720 5040 40320 362880 3628800 // 0..10 39916800 479001600 1932053504 // 11..13
```

Primes

```
// 100 first primes
2 3 5 7 11 13 17 19 23 29 31 37 41 43 47 53 59 61 67 71 73 79 83 89 97 101
103 107 109 113 127 131 137 139 149 151 157 163 167 173 179 181 191 193 197
199 211 223 227 229 233 239 241 251 257 263 269 271 277 281 283 293 307 311
313 317 331 337 347 349 353 359 367 373 379 383 389 397 401 409 419 421 431
433 439 443 449 457 461 463 467 479 487 491 499 503 509 521 523 541
// Some larger primes
104729 1299709 9999991 15485863 179424673 2147483647 32416190071
112272535095293 54673257461630679457
// prime sieve with prime checking
const int MAX_SIEVE = 1e7; // 1e7 in a few seconds
ll _sieve_size;
bitset < MAX_SIEVE + 10 > bs;
vi primes;
void sieve(ll upperbound) {
    _sieve_size = upperbound + 1;
    bs.set();
    bs[0] = bs[1] = 0:
    for (11 i = 2; i <= _sieve_size; ++i)</pre>
        if (bs[i]) {
            for (ll j = i * i; j <= _sieve_size; j += i)</pre>
                bs[i] = 0;
            primes.push_back((int)i);
        }
}
bool isPrime(11 N) { // works for N <= (last prime in primes)^2
   if (N <= _sieve_size) return bs[N]; // O(1) sieve check for small primes
    for (int i = 0; i < (int)primes.size(); ++i) // brute force for larger</pre>
        if (N % primes[i] == 0) return false;
    return true: // more time if N is prime!
}
Fibonacci
0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 // 0..15
   F(0) = 0, F(1) = 1
  F(n) = F(n-1) + F(n-2)
Combinatorics
```

$$C(n,0) = C(n,n) = 1$$

$$C(n,k) = C(n-1,k-1) + C(n-1,k)$$

Catalan numbers

```
1 1 2 5 14 42 132 429 1430 4862 16796 // 0..10
```

- 1. Cat(n) Count the number of distinct binary trees with n vertices.
- 2. Count number of expressions counting n correctly matched pairs of parentheses.
- 3. Count ways a convex polygon can be triangulated.

```
Cat(0) = 1

Cat(n) = \frac{2(2n-1)}{n+1} * Cat(n-1)
```

Powers of 2

```
1 2 4 8 16 32 64 128 256 512 1024 // 0..10
2048 4096 8192 16384 32768 65536 // 11..16
4294967296 4611686018427387904 // 32. 63
```

Extended Euclid: Linear Diphantine Equation

```
int x, y, d; // answer, give d = gcd(a, b)
void extendedEuclid(int a, int b) { // solve a*x + b*y = d
    if (b == 0) { x = 1; y = 0; d = a; return; }
    extendedEuclid(b, a % b);
    int x1 = y, y1 = x - (a /b) * y;
    x = x1; y = y1;
}
```

Cycle Finding

```
// find position and length of the repeated pattern in a generated sequence
if floydCycleFinding(int x0) { // define int f(int x) which generates the
    sequence
    // 1st phase, hare 2x speed of turtoise
    int tortoise = f(x0), hare = f(f(x0));
    while (tortoise != hare) { tortoise = f(tortoise); hare = f(f(hare)); }
    // 2nd phase, find mu, same speed
    int mu = 0; hare = x0;
    while (tortoise != hare) { tortoise = f(tortoise); hare = f(hare); ++mu;
        }
    // 3rd phase, find lambda, hare moves tortoise still
    int lambda = 1; hare = f(tortoise);
    while (tortoise != hare) { hare = f(hare); ++lambda; }
    return ii(mu, lambda); // mu: start of cycle, lambda: cycle length
}
```

Game Theory

The Nim Game. Two players take turns to remove objects from distinct heaps. On each turn, a player must remove at least one object and may remove any number of objects, but only from the same heap. For the starting player to win, $n_1 \hat{\ } ... \hat{\ } n_k \neq 0$. (bitwise xor)

}

Java BigInteger

```
BigInteger.ZERO // constants
i.mod(m) // base number conversion
i.isProbablePrime(10) // Probabilistic prime testing
x.modPow(y, n) // calculate x^y mod n
// Catalan numbers with BigInteger
import java.util.Scanner;
import java.math.BigInteger;
class Main {
    public static BigInteger[] mem;
    public static BigInteger cat(int n) {
        if (n == 0) return BigInteger.ONE;
        if (mem[n] != null) return mem[n];
        BigInteger k = BigInteger.valueOf(2 * (2 * n - 1)).multiplv(cat(n -
       return mem[n] = k.divide(BigInteger.valueOf(n + 1));
    }
    public static void main(String[] args) {
       Scanner sc = new Scanner(System.in);
       mem = new BigInteger[11]; // adjust as necessary
       while (sc.hasNextInt()) {
            System.out.println(cat(sc.nextInt()));
       }
```

DP

Longest Increasing Subsequence

```
vi lis(vi a) { // O(n log k)
   int L[MAX];
   vi dp(a.size());
   int lis = 0;
   for (int i = 0; i < a.size(); ++i) {
        // LIS ending at a[i] is at length pos + 1
        int pos = lower_bound(L, L + lis, a[i]) - L;
        L[pos] = a[i];
        dp[i] = pos + 1;

        if (pos + 1 > lis) lis = pos + 1;
    }
    return dp; // Return lis array
}
```

Knapsack

```
// vector<int> knapsack(capasity, vector<pair<weight, value> >)
// O(NC)
// M(NC)
vi knapsack(int c, vector<pii>&o){
  vi res;
  vector < vi > dp(o.size()+1); //[obj][cap]
  trav(it,dp) it->resize(c+1);
  rep(i,0,o.size()) rep(j,o[i].first,c+1)
    dp[i+1][j]=max(dp[i][j], dp[i][j-o[i].first]+o[i].second);
 int mx=0; rep(i,0,c+1) if(dp.back()[i]>dp.back()[mx]) mx=i;
  rrep(i, o. size() -1,0) if(dp[i][mx] < dp[i+1][mx]){</pre>
    res.push_back(i); mx-=o[i].first;
  return res;
Graph
Kruskal MST
// use union find class
int kruskal_mst(vector<pair<int, ii> > &EdgeList, int V) {
    int mst_cost = 0;
    UnionFind UF(V):
    for (int i = 0: i < EdgeList.size(): ++i) {</pre>
        pair<int, ii> front = EdgeList[i];
        if (!UF.isSameSet(front.second.first, front.second.second)) {
            mst cost += front.first:
            UF.unionSet(front.second.first, front.second.second);
    }
    return mst cost:
}
Bipartite check
bool is_bipartite(int s) {
    qi q; q.push(s);
    vi color(n, INF); color[s] = 0;
    while (!q.empty()) {
        int u = q.front(); q.pop();
        for (int j = 0; j < (int)adjs[u].size(); ++j) {</pre>
            ii v = adis[u][i];
            if (color[v.first] == INF) {
                color[v.first] = 1 - color[u];
                q.push(v.first);
            else if (color[v.first] == color[u]) {
                return false:
            }
        }
    }
    return true;
```

6

```
Maximum Bipartite Cardinality Matching
                                                                                   dfs_parent.assign(V, 0);
                                                                                   articulation_vertex.assign(V, 0);
vector < vi > AdjList; // initialize
                                                                                   printf("Bridges:\n");
vi match, vis;
                                                                                   for (int i = 0: i < V: ++i)</pre>
                                                                                       if (dfs_num[i] == UNVISITED) { // special case for root
int aug(int 1) { // return 1 if augmenting path is found, 0 otherwise
                                                                                           dfsRoot = i: rootChildren = 0:
    if (vis[1]) return 0:
                                                                                           articulationPointAndBridge(i);
    vis[1] = 1;
                                                                                           articulation_vertex[dfsRoot] = (rootChildren > 1);
    for (int j = 0; j < (int)AdjList[1].size(); ++j) {</pre>
        int r = AdjList[1][j];
                                                                                   // articulation_vertex contains Articulation Points
        if (match[r] == -1 || aug(match[r])) {
            match[r] = 1:
                                                                                  Dijkstra
            return 1;
        }
                                                                                   vector < vector < ii> > AdiList: // pair < node. cost>
                                                                                   int V, E, s, t;
    return 0;
                                                                                   int dijsktra(int s, int t) { // variant will leave duplicate nodes in queue
                                                                                       vi dist(V, INF);
// in main
                                                                                       dist[s] = 0:
int MCBM = 0; // result
                                                                                       priority_queue < ii, vector < ii >, greater < ii > > pq;
match.assign(V, -1);
                                                                                       pq.push(ii(0, s));
                                                                                       while (!pq.empty()) {
for (int 1 = 0; 1 < n; ++1) {</pre>
                                                                                           ii front = pq.top(); pq.pop();
    vis.assign(n, 0);
                                                                                           int d = front.first, u = front.second;
    MCBM += aug(1);
}
                                                                                           if (d > dist[u]) continue; // important check
                                                                                           for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
Articulation points and bridges
                                                                                               ii v = AdjList[u][j];
                                                                                               if (dist[u] + v.second < dist[v.first]) {</pre>
void articulationPointAndBridge(int u) {
                                                                                                   dist[v.first] = dist[u] + v.second; // relax
    dfs_low[u] = dfs_num[u] = dfsNumberCounter++; // dfs_low[u] <= dfs_num[u]</pre>
                                                                                                   pq.push(ii(dist[v.first], v.first));
    for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
                                                                                               }
        ii v = AdjList[u][j];
                                                                                           }
        if (dfs_num[v.first] == UNVISITED) {
                                                                                       }
            dfs parent[v.first] = u:
                                                                                       return dist[t];
            if (u == dfsRoot) rootChildren++;
                                                                                   }
                                                                                  Dijkstra Timetable
            articulationPointAndBridge(v.first);
            if (dfs low[v.first] >= dfs num[u])
                                                                                   // vector < dist > djikstra (vector < vector < egde < dst, len, starttime, period > > >,
                articulation_vertex[u] = true;
                                                                                        int source, vector int<path>);
            if (dfs low[v.first] > dfs num[u])
                                                                                   // Complexity O(ElogN)
                printf(" Edge (%d,%d) is a bridge\n", u, v.first);
                                                                                   struct Edge{
            dfs_low[u] = min(dfs_low[u], dfs_low[v.first]);
                                                                                    int dst,1,ts,tp;
                                                                                     Edge(int a, int b, int c, int d){dst=a; l=b; ts=c; tp=d;};
        else if (v.first != dfs_parent[u]) // a back edge and not direct
            dfs_low[u] = min(dfs_low[u], dfs_num[v.first]);
                                                                                   vi djikstra(vector<vector<Edge> >& g, int s, vi&path){
                                                                                     vi res(g.size(),-1); path.resize(g.size());
                                                                                     set < pii > Q; vector < bool > av(g.size(),1);
                                                                                     res[s]=0; Q.insert(pii(0,s));
// in main
                                                                                     while(!Q.empty()){
                                                                                      int cur = Q.B->second;
dfsNumberCounter = 0;
dfs_num.assign(V, UNVISITED);
                                                                                       Q.erase(Q.B);
```

dfs_low.assign(V, 0);

av[cur]=0;

```
trav(it, g[cur]){
                                                                                              }
      if(it->tp==0 && it->ts < res[cur]) continue;</pre>
                                                                                              EulerTour(cyc.insert(i, u), v.first);
      int nxt = res[cur]-it->ts;
      if(res[cur]<=it->ts) nxt=it->ts: else nxt=it->ts + (nxt/it->tp)*(it->tp
          ) + (nxt\%it->tp ? it->tp : 0);
      nxt+=it->1:
      int& dst=res[it->dst]:
                                                                                  // inside main
      if(dst!=-1 && dst<=nxt) continue;</pre>
                                                                                  cvc.clear();
     if(dst>-1) Q.erase(pii(dst, it->dst));
                                                                                  EulerTour(cyc.begin(), A); // cyc contains euler tour starting at A
                                                                                  for (list<int>::iterator it = cyc.begin(); it != cyc.end(); ++it)
                                                                                      printf("%d\n", *it): // the Euler tour
      Q.insert(pii(dst, it->dst));
      path[it->dst]=cur;
                                                                                  Edmond Karp
 }
                                                                                  // setup res, s, t, AdjList as global variables
  return res;
                                                                                  int res[MAXN][MAXN], mf, f, s, t;
                                                                                  vector < vi > AdjList; // Don't forget backward edges!
Bellman Ford
                                                                                  void augment(int v, int minEdge) { // traverse BFS spanning tree from s to t
int bellman ford(int s. int t) { // O(VE) when using adj list
                                                                                      if (v == s) { f = minEdge; return; } // record minEdge in a global
    vi dist(V, INF); dist[s] = 0;
                                                                                          variable f
    for (int i = 0; i < V - 1; ++i) // relax all edges V-1 times
                                                                                      else if (p[v] != -1) {
        for (int u = 0: u < V: ++u)
                                                                                          augment(p[v], min(minEdge, res[p[v]][v]));
            for (int j = 0; j < (int) AdjList[u].size(); ++j) {</pre>
                                                                                          res[p[v]][v] -= f: res[v][p[v]] += f:
                ii v = AdjList[u][j]; // record SP spanning here if needed
                                                                                     }
                dist[v.first] = min(dist[v.first], dist[u] + v.second);
                                                                                 }
                                                                                  int edmond_karp() {
    return dist[t];
                                                                                     mf = 0:
}
                                                                                     while (1) { // run bfs
                                                                                          f = 0:
// check if there exists a negative cycle
                                                                                          bitset < MAXN > vis; vis[s] = true; // bitset is faster
bool hasNegativeCycle = false;
                                                                                          queue < int > q; q.push(s);
for (int u = 0; u < V; ++u)
                                                                                          p.assign(MAXN, -1); // record the BFS spanning tree, from s to t
    for (int j = 0; j < (int) AdjList[u].size(); ++j) {</pre>
                                                                                          while (!q.empty()) {
        ii v = AdiList[u][i]:
                                                                                              int u = q.front(); q.pop();
        if (dist[v.first] > dist[u] + v.second) // if still possible
                                                                                              if (u == t) break; // stop bfs if we reach t
            hasNegativeCycle = true;
                                       // then neg cycle exists
                                                                                              for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
   }
                                                                                                  int v = AdjList[u][j];
                                                                                                  if (res[u][v] > 0 && !vis[v])
Euler Tour
                                                                                                      vis[v] = true, q.push(v), p[v] = u;
                                                                                              }
list <int> cyc; // list for fast insertion in middle
void EulerTour(list<int>::iterator i, int u) {
                                                                                          augment(t, INF);
    for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
                                                                                          if (f == 0) break; // we cannot send any more flow, terminate
        ii v = AdjList[u][j];
                                                                                          mf += f; // we can still send a flow, increase the max flow!
        if (v.second) {
                                                                                     }
            v.second = 0: // mark as to be removed
                                                                                      return mf:
            for (int k = 0; k < (int)AdjList[v.first].size(); ++k) {</pre>
                ii uu = AdiList[v.first][k]: // remove bi-directional
                if (uu.first == u && uu.second) {
                                                                                 Maxflow Binblock
                    uu.second = 0:
                                                                                  // int maxflow(vector < vector < pair < dest, cap > > network, int source, int
                    break:
                }
                                                                                     dest, vector < vector < pair < dest, flow > > resultflow)
```

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```
// Complexity O(VE) (:
                                                                                          ans += floodfill(r + dr[d], c + dc[d], c1, c2);
// Works with noninteger values
                                                                                      return ans;
vvi G; vector < bool > av;
                                                                                  }
vector <si> GE:
                                                                                  Topological Sort
bool dfs(int s, int t, int c){
                                                                                  vi ts: // Result in reverse order
 if(s==t) return 1:
 av[s]=0;
                                                                                  void topo(int u) {
                                                                                      seen[u] = 1: // Init to false
 trav(it, GE[s]){
                                                                                      for (int i = 0; i < (int)adj_list[u].size(); ++i) {</pre>
   if(!av[*it]|| c>G[s][*it]) continue;
                                                                                          ii v = adj_list[u][i];
    if(dfs(*it, t, c)){
                                                                                          if (!seen[v.first])
     G[s][*it]-=c:
                                                                                              topo(v.first);
     G[*it][s]+=c;
      return 1;
                                                                                      }
   }
                                                                                      ts.push_back(u);
                                                                                  }
 }
 return 0:
                                                                                  // use
                                                                                  ts.clear():
int maxflow(vector<vector<pii> >&g, int s, int t, vector<vector<pii> > &resf)
                                                                                 // init seen to false
                                                                                  for (int i = 0; i < n; ++i)</pre>
                                                                                      if (!seen[i]) topo(i);
 int n=g.size();
 G.resize(n); trav(it, G) it->resize(n);
                                                                                  Strongly Connected Components
 GE.resize(n):
 rep(i,0,n) trav(it,g[i]) {G[i][it->first]+=it->second; GE[i].insert(it->
                                                                                  vi dfs num. dfs low. S. visited:
     first); GE[it->first].insert(i);}
 vvi GG=G:
                                                                                  void tarianSCC(int u) {
 int res=0: av.resize(n.1):
                                                                                      dfs_low[u] = dfs_num[u] = dfsNumberCounter++; // dfs_low[u] <= dfs_num[u]
 rrep(i,30,0) {fill(all(av),1); while(dfs(s,t,1 << i)){fill(all(av),1); res</pre>
                                                                                      S.push_back(u); // stores u in a vector based on order of visitation
      += 1<<i:}}
                                                                                      visited[u] = 1;
 resf.resize(g.size());
                                                                                      for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
 rep(i,0,n) trav(it, g[i]) {
                                                                                          ii v = AdjList[u][j];
   int d=min(GG[i][it->first]-G[i][it->first]. it->second):
                                                                                          if (dfs num[v.first] == UNVISITED)
    if(d<=0) continue;</pre>
   GG[i][it->first]-=d:
                                                                                              tarjanSCC(v.first);
                                                                                          if (visited[v.first])
   resf[i].pb(pii(it->first,d));
                                                                                              dfs_low[u] - min(dfs_low[u], dfs_low[v.first]);
                                                                                      }
 return res;
}
                                                                                      if (dfs_low[u] == dfs_num[u]) { // if this is a root (start) of an SCC
Flood Fill
                                                                                          printf("SCC %d:", ++numSCC); // this part is done after recursion
                                                                                          while (1) {
// need grid, R, C
                                                                                              int v = S.back(); S.pop_back(); visited[v] = 0;
int dr[8] = \{ 1, 1, 0, -1, -1, -1, 0, 1 \}:
                                                                                              printf(" %d", v):
int dc[8] = \{ 0, 1, 1, 1, 0, -1, -1, -1 \};
                                                                                              if (u == v) break;
// Return size of CC
                                                                                          printf("\n");
int floodfill(int r, int c, char c1, char c2) {
                                                                                      }
    if (r < 0 | | r >= R | | c < 0 | | c >= C) return 0;
                                                                                  }
    if (grid[r][c] != c1) return 0;
                                                                                  // in main
    int ans = 1: // Because vertex (r. c) has c1 as its color
                                                                                  dfs_num.assign(V, UNVISITED);
    grid[r][c] = c2; // Color it
                                                                                  dfs_low.assign(V, 0);
    for (int d = 0; d < 8; ++d)
                                                                                  visited.assign(V, 0);
```

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```
dfsNumberCounter = numSCC = 0;
                                                                                 }
for (int i = 0; i < V: ++i)
                                                                                 Edit Distance
    if (dfs_num[i] == UNVISITED)
        tarianSCC(i):
                                                                                 vector < vi > dp;
                                                                                 int edit_distance(string A, string B) { // align A with B
Chinese Postman
                                                                                     dp.assign((int)A.size() + 1, vi()); // dynamic dp matrix
// Weight of euler tour in connected graph.
                                                                                     for (int i = 0; i <= A.size(); ++i)</pre>
// Need to fill d[][] with min cost between any two nodes. Do floyd warshall
                                                                                          dp[i].assign((int)B.size() + 1, 0);
int memo[1 << MAX]:</pre>
                                                                                     for (int i = 1; i <= A.size(); ++i)</pre>
int min_cost(int s) { // incr odd degrees and make all even
                                                                                          dp[i][0] = i * -1: // delete substring A[1..i]. score -1
    if (s == 0) return 0;
                                                                                     for (int i = 1; i <= B.size(); ++i)</pre>
    if (memo[s] != 0) return memo[s];
                                                                                          dp[0][i] = i * -1; // insert space in B[1..i], score -1
    int best = -1:
    int x = 0; // Choose our first node to switch as the first node with odd
                                                                                     for (int i = 1; i <= A.size(); ++i)</pre>
        values we can find.
                                                                                         for (int j = 1; j <= B.size(); ++j) {</pre>
    while (((s >> x) & 1) == 0) ++x; // x = number of trailing zeros
                                                                                              // Match +2. Mismatch -1
    // Try to combine with all other odd value nodes.
                                                                                              dp[i][j] = dp[i - 1][j - 1] + (A[i - 1] == B[j - 1]?2:-1);
    for (int v = x + 1; v < n; ++v) {
                                                                                              dp[i][j] = max(dp[i][j], dp[i - 1][j] - 1); // delete
        if ((s >> v) & 1 == 0) continue;
                                                                                              dp[i][j] = max(dp[i][j], dp[i][j-1]-1); // insert
        int comb = s^(1 << x)^(1 << y); // Switch off the selected nodes.
       // Cost will be to combine these two nodes + combining the rest.
        int cost = d[x][y] + min_cost(comb);
                                                                                     return dp[A.size()][B.size()]; // max alignment score
        if (best == -1 || cost < best)</pre>
            best = cost;
                                                                                 Longest Common Subsequence
    return memo[s] = best:
                                                                                 vector < vi > dp:
                                                                                 int lcs(string A, string B) { // turn edit distance into lcs
                                                                                     dp.assign((int)A.size() + 1, vi()); // dynamic dp matrix
String
                                                                                     for (int i = 0; i <= A.size(); ++i)</pre>
Knuth-Morris-Pratt
                                                                                          dp[i].assign((int)B.size() + 1, 0); // all edge cases 0
int b[MAXN]: // back table
                                                                                     for (int i = 1: i <= A.size(): ++i)
void kmpPreprocess(string P) {
                                                                                         for (int j = 1; j <= B.size(); ++j) {</pre>
   int i = 0, j = -1; b[0] = -1;
                                                                                              // Match 1. Mismatch -INF
    while (i < P.size()) {</pre>
                                                                                              dp[i][j] = dp[i-1][j-1] + (A[i-1] == B[j-1]?1:-INF);
        while (i >= 0 \&\& P[i] != P[i]) i = b[i];
                                                                                              dp[i][j] = max(dp[i][j], dp[i - 1][j]); // delete cost 0
        ++i: ++i:
                                                                                              dp[i][j] = max(dp[i][j], dp[i][j - 1]); // insert cost 0
        b[i] = j;
                                                                                         }
}
                                                                                     return dp[A.size()][B.size()]; // max alignment score
                                                                                 }
void kmpSearch(string T, string P) { // does P match T?
    kmpPreprocess(P); // must prepare P
                                                                                 Suffix Array
    int i = 0, j = 0;
    while (i < T.size()) {</pre>
                                                                                 // Suffix Array is a simpler version of Suffix Tree.
        while (j \ge 0 \&\& T[i] != P[j]) j = b[j];
                                                                                 // It is slower to construct, O(n log n) vs O(n)
        ++i; ++j;
                                                                                 // but it's a lot simpler to program.
        if (j == P.size()) {
            printf("P is found at index %d in T\n", i - j);
                                                                                 // ex. find all Longest Common Substrings of a and b, O(n log n)
            i = b[i]: // prepare for next possible match
                                                                                 string T = a + "$" + b + "#"; // Chars lower, combine input strings
                                                                                 n = T.size(); m = b.size(); // for ease of programming
    }
                                                                                 constructSA(T); // Construct Suffix Array
```

```
computeLCP(T); // LCS depends on LCP, so must do this
                                                                                              if (RA[SA[i]] == RA[SA[i - 1]] && RA[SA[i] + k] == RA[SA[i - 1] +
                                                                                                  k])
set < string > res = allLCS(T); // Can also use LCS()
                                                                                                  tmpRA[SA[i]] = r;
if (res.emptv()) printf("No common sequence.\n");
for (set<string>::iterator i = res.begin(); i != res.end(); ++i) {
                                                                                                  tmpRA[SA[i]] = ++r;
    printf("%s\n", i->c str()):
}
                                                                                          for (int i = 0; i < n; ++i) // update rank array
                                                                                              RA[i] = tmpRA[i];
                                                                                         if (RA[SA[n - 1]] == n - 1) break; // optimization
// ex. find Longest Repeated Substring (min 2 times), O(n log n)
T += "$"; // input string T, append '$'
                                                                                     }
n = T.size(): // for ease of programming
                                                                                 }
constructSA(T); // Construct Suffix Array
computeLCP(T); // LRS depends on LCP
                                                                                 void computeLCP(string &T) { // Longest Common Prefix, O(n)
                                                                                     Phi[SA[O]] = -1:
pair<string, int> ans = LRS(T); // LRS string and #repetitions
                                                                                     for (int i = 1; i < n; ++i)
if (ans.first.size()) printf("%s %d\n", ans.first.c_str(), ans.second);
                                                                                         Phi[SA[i]] = SA[i - 1];
else printf("No repetitions found!\n");
                                                                                     for (int i = 0: i < n: ++i) {
                                                                                         int L = 0;
                                                                                         if (Phi[i] == -1) { PLCP[i] = 0; continue; }
// impl
const int MAXN = 100010; // ok up to ~100k
                                                                                         while (T[i + L] == T[Phi[i] + L]) ++L:
int RA[MAXN], tmpRA[MAXN]; // rank array + tmp
                                                                                         PLCP[i] = L;
int SA[MAXN], tmpSA[MAXN]; // suffix array + tmp
                                                                                         L = max(L - 1, 0):
int c[MAXN]; // freq table for counting sort
                                                                                     }
int n, m; // globals for T and P
                                                                                     for (int i = 0; i < n; ++i)</pre>
int Phi[MAXN]; // for computing longest common prefix
                                                                                         LCP[i] = PLCP[SA[i]]:
                                                                                 }
int PLCP[MAXN];
int LCP[MAXN]; // LCP[i] stores the LCP between previous suffix T + SA[i-1]
                                               // and current suffix T + SA[i] int owner(int idx) { return (idx < n - m - 1) ? 1 : 2: }
void countingSort(int k, int n) { // sort RA, res in SA
                                                                                 // Longest Common Substring in O(n)
    int sum, maxi = max(300, n); // up to 255 ASCII chars of length n
                                                                                 ii LCS() { // return < LCS length, index >, where SA[index] gives index in T
                                                                                     int idx = 0, maxLCP = -1;
    memset(c, 0, sizeof c);
    for (int i = 0; i < n; ++i) // count freq of each integer rank</pre>
                                                                                     for (int i = 1; i < n; ++i)
        c[i + k < n ? RA[i + k] : 0]++;
                                                                                          if (owner(SA[i]) != owner(SA[i - 1]) && LCP[i] > maxLCP)
    for (int i = sum = 0; i < maxi; ++i) {</pre>
                                                                                              maxLCP = LCP[i], idx = i:
        int t = c[i]; c[i] = sum; sum += t;
                                                                                      return ii(maxLCP, idx);
                                                                                 }
    for (int i = 0; i < n; ++i) // shuffle suffix array if necessary</pre>
        tmpSA[c[SA[i] + k < n ? RA[SA[i] + k] : 0]++] = SA[i];
                                                                                 set < string > allLCS(string &T) { // return all unique longest substrings O(n
    for (int i = 0; i < n; ++i) // update suffix array</pre>
                                                                                     log n)
        SA[i] = tmpSA[i]:
                                                                                     int maxLCP = -1:
}
                                                                                     set < string > res;
                                                                                     for (int i = 0; i < n; ++i) {</pre>
void constructSA(string &T) { // Construct Suffix Array in O(n log n)
                                                                                         if (owner(SA[i]) == owner(SA[i - 1])) continue;
    int n = T.size();
                                                                                         if (LCP[i] == 0) continue;
    for (int i = 0: i < n: ++i) RA[i] = T[i]:
                                                                                         if (LCP[i] > maxLCP) res.clear();
    for (int i = 0; i < n; ++i) SA[i] = i;</pre>
                                                                                         if (LCP[i] >= maxLCP) {
    for (int k = 1; k < n; k <<= 1) { // repeat sort log n times
                                                                                              maxLCP = LCP[i];
        countingSort(k, n); // radix sort
                                                                                              res.insert(T.substr(SA[i], maxLCP));
        countingSort(0, n); // stable sort on first item
        int r = 0; tmpRA[SA[0]] = 0; // re-rank from rank r = 0
                                                                                     }
        for (int i = 1: i < n: ++i) {
                                                                                      return res:
            // if same pair => r otherwise increase rank
                                                                                 }
```

}

// Euclidian distance

// A vector is not a point here

};

```
// Longest Repeated Substring (substring 2 times or more)
                                                                                  double cross(vec a, vec b) { return a.x * b.y - a.y * b.x; }
ii LRS() { // returns < LRS length, index >, where SA[index] gives index in T
    int idx = 0. maxLCP = -1:
                                                                                  bool ccw(point p, point q, point r) {
    for (int i = 1; i < n; i++)</pre>
                                                                                      return cross(toVec(p, q), toVec(p, r)) > 0;
        if (LCP[i] > maxLCP)
          maxLCP = LCP[i], idx = i;
    return ii(maxLCP, idx);
                                                                                  bool collinear(point p, point q, point r) {
}
pair < string , int > LRS(string &T) { // return LRS and #repetitions
    int maxLCP = -1, rep = 0;
                                                                                  // Move a point
    string s;
    for (int i = 1; i < n; i++) {</pre>
        string curr = T.substr(SA[i], LCP[i]);
        if (LCP[i] > maxLCP) {
            maxLCP = LCP[i]: rep = 2:
            s = curr;
                                                                                  }
        else if (s == curr) ++rep;
   }
    return make_pair(s, rep);
                                                                                  // Rotate p w.r.t pivot
}
Geometry
                                                                                  }
Points and Lines
struct point_i { // prefer
    int x, y;
    point i() { x = v = 0; }
    point_i(int _x, int _y) : x(_x), y(_y) { }
                                                                                      vec oa = toVec(o, a), ob = toVec(o, b);
}:
struct point { // only if double needed, prefer ints
    double x, y;
    point() { x = y = 0.0; }
    point(double _x, double _y) : x(_x), y(_y) { }
    bool operator < (point other) const {</pre>
                                                                                      vec ap = toVec(a, p), ab = toVec(a, b);
        if (fabs(x - other.x) > EPS) // EPS comparison!
                                                                                      double u = dot(ap, ab) / norm_sq(ab);
            return x < other.x;</pre>
                                                                                      c = translate(a, scale(ab, u));
        return y < other.y;</pre>
                                                                                      return dist(p, c):
   }
                                                                                  }
    bool operator == (point other) const { // EPS comparison
```

return (fabs(x - other.x) < EPS && (fabs(y - other.y) < EPS));</pre>

double dist(point p1, point p2) { return hypot(p1.x - p2.x, p1.y - p2.y); }

struct vec { double x, y; vec(double _x, double _y) : x(_x), y(_y) { } };

vec toVec(point a, point b) { return vec(b.x - a.x, b.y - a.y); }

vec scale(vec v, double s) { return vec(v.x * s, v.y * s); }

return fabs(cross(toVec(p, q), toVec(p, r))) < EPS;</pre> point translate(point p, vec v) { return point(p.x + v.x, p.y + v.y); } // Rotate p by theta degrees CCW w.r.t origin (0, 0) point rotate(point p, double theta) { // call with 360 - theta for CW double rad = DEG to RAD(theta): // multiply theta with PI / 180.0 return point(p.x * cos(rad) - p.y * sin(rad), p.x * sin(rad) + p.y * cos(rad)); point rotate_around(point p, point pivot, double angle) { point o = translate(p, vec(-pivot.x, -pivot.y)); return translate(rotate(o, angle), toVec(pivot)); double dot(vec a, vec b) { return a.x * b.x + a.y * b.y; } double norm_sq(vec v) { return v.x * v.x + v.y * v.y; } double angle(point a, point o, point b) { // return angle aob in rad return acos(dot(a, ob) / sqrt(norm_sq(oa) * norm_sq(ob))); // Closest point to the line defined by a and b (must be different!) double distToLine(point p, point a, point b, point &c) { // Closest point to line segment between a and b (OK if a == b) double distToLineSegment(point p, point a, point b, point &c) { vec ap = toVec(a, p), ab = toVec(a, b); double u = dot(ap, ab) / norm_sq(ab); if (u < 0.0) { c = point(a.x, a.y); return dist(p, a); } if (u > 1.0) { c = point(b.x, b.y); return dist(p, b); } return distToLine(p, a, b, c); } // ax + by + c = 0, b = 0.0 if vertical, 1.0 otherwise

```
struct line { double a, b, c; };
void pointsToLine(point p1, point p2, line &1) {
    if (fabs(p1.x - p2.x) < EPS) { // special for vertical
       1.a = 1.0; 1.b = 0.0; 1.c = -p1.x;
   }
    else {
       1.a = -(double)(p1.y - p2.y) / (p1.x - p2.x);
       1.b = 1.0:
       1.c = -(double)(1.a * p1.x) - p1.y;
}
bool areParallel(line 11, line 12) { // check a & b
    return (fabs(11.a - 12.a) < EPS) && (fabs(11.b - 12.b) < EPS);
bool areSame(line 11, line 12) { // check c
    return areParallel(11, 12) && (fabs(11.c - 12.c) < EPS);
// Check lines, not line segments
bool areIntersect(line 11, line 12, point &p) {
   if (areParallel(11, 12)) return false;
   p.x = (12.b * 11.c - 11.b * 12.c) / (12.a * 11.b - 11.a * 12.b);
   if (fabs(11.b) > EPS) p.y = -(11.a * p.x + 11.c);
    else
                         p.y = -(12.a * p.x + 12.c);
    return true:
}
Circles
double DEG_to_RAD(double d) { return d * PI / 180.0; }
double RAD to DEG(double r) { return r * 180.0 / PI: }
// 2: inside, 1: border, 0: outside. Exakt int calc
int insideCircle(point_i p, point_i c, int r) {
   int dx = p.x - c.x, dy = p.y - c.y;
   int Euc = dx * dx + dv * dv, rSa = r * r:
    return Euc < rSq ? 2 : Euc == rSq ? 1 : 0;</pre>
}
// Given to points p1, p2 and the radius of a circle.
// Return if there can be a circle with the given radius and
// if so return it's center. To get both possible centers,
// call again with p1 and p2 swapped.
bool circle2PtsRad(point p1, point p2, double r, point &c) {
    double d2 = (p1.x - p2.x) * (p1.x - p2.x) +
               (p1.y - p2.y) * (p1.y - p2.y);
    double det = r * r / d2 - 0.25:
    if (det < 0.0) return false;</pre>
    double h = sart(det):
    c.x = (p1.x + p2.x) * 0.5 + (p1.y - p2.y) * h;
    c.v = (p1.v + p2.v) * 0.5 + (p2.x - p1.x) * h;
```

```
return true;
}
Triangles
double perimeter(double ab, double bc, double ca) {
    return ab + bc + ca:
double perimeter(point a, point b, point c) {
    return dist(a, b) + dist(b, c) + dist(c, a);
double area(double ab, double bc, double ca) {
    double s = 0.5 * perimeter(ab, bc, ca): // Heron's formula
    return sqrt(s) * sqrt(s - ab) * sqrt(s - bc) * sqrt(s - ca);
double area(point a, point b, point c) {
    return area(dist(a, b), dist(b, c), dist(c, a));
// Radius of a circle described inside the triangle
double rInCircle(double ab, double bc, double ca) {
    return area(ab, bc, ca) / (0.5 * perimeter(ab, bc, ca));
double rInCircle(point a, point b, point c) {
    return rInCircle(dist(a, b), dist(b, c), dist(c, a));
// 1 if there is a circle inside the triangle. ctr will be the center
// and r the radi
int inCircle(point p1, point p2, point p3, point &ctr, double &r) {
    r = rInCircle(p1, p2, p3);
    if (fabs(r) < EPS) return 0; // not in circle</pre>
    line 11, 12;
    double ratio = dist(p1, p2) / dist(p1, p3);
    point p = translate(p2, scale(toVec(p2, p3), ratio / (1 + ratio)));
    pointsToLine(p1, p, l1);
    ratio = dist(p2, p1) / dist(p2, p3);
    p = translate(p1, scale(toVec(p1, p3), ratio / (1 + ratio)));
    pointsToLine(p2, p, 12);
    areIntersect(11, 12, ctr);
    return 1:
}
// Radius of the circle outside the triangle
double rCircumCircle(double ab. double bc. double ca) {
    return ab * bc * ca / (4.0 * area(ab, bc, ca));
}
```

```
double rCircumCircle(point a, point b, point c) {
    return rCircumCircle(dist(a, b), dist(b, c), dist(c, a));
// 1 if there is a circle circums the triangle. ctr will be the center
// and r the radi
int circumCircle(point p1, point p2, point p3, point &ctr, double &r) {
    double a = p2.x - p1.x, b = p2.y - p1.y;
    double c = p3.x - p1.x, d = p3.y - p1.y;
    double e = a * (p1.x + p2.x) + b * (p1.y + p2.y);
    double f = c * (p1.x + p3.x) + d * (p1.y + p3.y);
    double g = 2.0 * (a * (p3.y - p2.y) - b * (p3.x - p2.x));
    if (fabs(g) < EPS) return 0;</pre>
    ctr.x = (d * e - b * f) / g;
    ctr.v = (a * f - c * e) / g;
    r = dist(p1, ctr);
    return 1;
bool canFormTriangle(double a, double b, double c) {
    return (a + b > c) && (a + c > b) && (b + c > a);
}
Polygons
// returns the perimeter, which is the sum of Euclidian distances
// of consecutive line segments (polygon edges)
double perimeter(const vector<point> &P) {
    double result = 0.0:
    for (int i = 0; i < (int)P.size() - 1; i++) // P[0] == P[n - 1]
        result += dist(P[i], P[i + 1]);
    return result:
}
double area(const vector<point> &P) {
    double result = 0.0, x1, y1, x2, y2;
    for (int i = 0; i < (int)P.size() - 1; i++) {</pre>
        x1 = P[i].x; x2 = P[i + 1].x;
        y1 = P[i].y; y2 = P[i + 1].y;
        result += (x1 * y2 - x2 * y1);
    return fabs(result) / 2.0:
}
bool isConvex(const vector<point> &P) {
    int sz = (int)P.size():
    if (sz <= 3) return false:
    bool isLeft = ccw(P[0], P[1], P[2]):
    for (int i = 1; i < sz - 1; ++i)</pre>
        if (ccw(P[i], P[i+1], P[(i+2) == sz?1:i+2]) != isLeft)
            return false; // different sign -> this polygon is concave
    return true;
```

```
}
// true if pt in polygon, either convex or concave
bool inPolygon(point pt, const vector<point> &P) { // Assume P[0] == P[n - 1]
    if ((int)P.size() == 0) return false;
    double sum = 0:
    for (int i = 0; i < (int)P.size() - 1; i++) {</pre>
        if (ccw(pt, P[i], P[i + 1]))
           sum += angle(P[i], pt, P[i + 1]);
        else sum -= angle(P[i], pt, P[i + 1]);
    return fabs(fabs(sum) - 2 * PI) < EPS;</pre>
}
// Convex hull pivot check
point pivot(0, 0); // global pivot for CH compare fun
bool angleCmp(point a, point b) {
    if (collinear(pivot, a, b))
        return dist(pivot, a) < dist(pivot, b);</pre>
    double d1x = a.x - pivot.x, d1y = a.y - pivot.y;
    double d2x = b.x - pivot.x, d2y = b.y - pivot.y;
    return (atan2(d1y, d1x) - atan2(d2y, d2x)) < 0;
}
vector<point> CH(vector<point> P) { // contents in P may be reshuffled
    int n = (int)P.size();
    if (n <= 3) {
        if (!(P[0] == P[n-1])) P.push_back(P[0]); // corner case
        return P; // special case, CH is P
    }
    int PO = 0; // first, find PO lowest Y, tie: lowest X
    for (int i = 1; i < n; ++i)</pre>
        if (P[i].y < P[P0].y \mid (P[i].y == P[P0].y && P[i].x < P[P0].x))
    swap(P[0], P[P0]); // second, sort w.r to angle to P0
    pivot = P[0]:
    sort(++P.begin(), P.end(), angleCmp); // Don't sort P[0]
    //third, ccw tests
    vector <point > S:
    S.push_back(P[n - 1]); S.push_back(P[0]); S.push_back(P[1]);
    int i = 2:
    while (i < n) {
        int j = (int)S.size() - 1;
        if (ccw(S[j - 1], S[j], P[i])) S.push_back(P[i++]); // left turn
        else S.pop_back(); // right turn, bad point
    }
    return S;
```

Misc

Interval Cover

```
}
// O(n log n) vector<int> cover(start, end, vector<inteval pair>)
vi cover(fl s, fl e, vector<pair<fl,fl> >& m){
                                                                                  Prefix Sum
 int lst=-1;
 vector < pair < type of (m[0]), int > > tm(m.size());
                                                                                  vector<ll> bt;
 rep(i,0,m.size()) tm[i]=make_pair(m[i],i);
 sort(all(tm));
                                                                                  void add(int i, ll v){
 vi res;
                                                                                    if(!i){bt[0]+=v; return;}
 while(lst<int(m.size())){</pre>
                                                                                    while (i<int(bt.size())){</pre>
   int cur=lst:
                                                                                      bt[i]+=v;
   for(int i=lst+1; i<int(m.size()) && tm[i].first.first<=s; i++){</pre>
                                                                                      i+=(i&-i);
     if((cur!=-1 && tm[i].first.second > tm[cur].first.second) ||
                                                                                    } return;
              (cur==-1 && tm[i].first.second >=s)) cur=i;
   }
   if (cur==1st) break;
                                                                                  11 sum(int i){
   lst=cur;
                                                                                    ll res=bt[0];
   res.push_back(tm[lst].second);
                                                                                    while(i>0){
   s=tm[lst].first.second:
                                                                                      res+=bt[i];
   if (s>=e && res.size()) return res;
                                                                                      i-=(i&-i);
                                                                                    } return res:
 res.clear();
                                                                                  }
 return res;
```