T .	T. L.
Intro	1 Intro
Shortcuts	Shortcuts
Complexity	<pre>1 1 typedef vector<int> vi;</int></pre>
Limits	typedef long long ll;
Math	1
Primes	1 const int UNVISITED = -1;
Java BigInteger	<pre>2 const int INF = 1e9;</pre>
Combinatorics	<sup>2</sup> Complexity
Catalan numbers	2 Modern CPU compute 100M in 3s.
Cycle Finding	2
Game Theory	2 Worst AC Algorithm Problem
Linear Diphantine Equation	
DP	$2$ $\leq [1822]  O(2^n n)'$ e.g. DP with bitmask
LIS $O(nlogn)$	$2 \leq 100  O(n^4)$ e.g. DP with 3 dimensions
	$\leq 400$ O $\langle n^3 \rangle$ e.g. Floyd Warshall's
Data structures	$\stackrel{-}{\leq} 2K$ O $(n^2 log n)$ e.g. 2 loops + a tree-related DS
Union Find	$\stackrel{2}{\leq} 10K$ O( $n^2$ ) e.g. Selection/Insert sort
Segment Tree	$\stackrel{-}{\leq} 1M$ O $(nlogn)$ e.g. Building Segment Tree
Graph	$\leq 100M  O(n)$ I/O bottleneck
Kruskal MST	0
Bipartite check	Limits
Maximum Bipartite Cardinality Matching	$32$ -Dit int $2^{-}-1=214/403047$
Articulation points and bridges	64-bit signed long long upper limit $2^{63} - 1 = 9223372036854775807$
Dijkstra	4 Math
Bellman Ford	4 TODO tables of $2^x$ , $!x, x113$
Euler Tour	5 TODO simple geometric formulas for volumes etc?
Edmond Karp	5 TODO sin/cos
Flood Fill	<pre>5 int gcd(int a, int b) { return b == 0 ? a : gcd(b, a % b); }</pre>
Topological Sort	5 int lcm(int a, int b) { return a * (b / gcd(a, b)); }
Strongly Connected Components	6 p.
Chinese Postman	6 Primes
	// 100 first primes
$\mathbf{String}$	6 2 3 5 7 11 13 17 19 23 29 31 37 41 43 47 53 59 61 67 71 73 79 83 89 97 101
Knuth-Morris-Pratt	6 103 107 109 113 127 131 137 139 149 151 157 163 167 173 179 181 191 193 197 199 211 223 227 229 233 239 241 251 257 263 269 271 277 281 283 293 307 311
Edit Distance	6 313 317 331 337 347 349 353 359 367 373 379 383 389 397 401 409 419 421 431
LCS	6 433 439 443 449 457 461 463 467 479 487 491 499 503 509 521 523 541
Suffix Trie	6 // Some larger primes 104729 1299709 9999991 15485863 179424673 2147483647 32416190071
Geometry	6 112272535095293 54673257461630679457
Convex Hull	6

```
// prime sieve with prime checking
const int MAX_SIEVE = 1e7; // 1e7 in a few seconds
ll sieve size:
bitset < MAX_SIEVE + 10 > bs;
vi primes;
void sieve(ll upperbound) {
    sieve size = upperbound + 1:
    bs.set();
    bs[0] = bs[1] = 0:
    for (11 i = 2; i <= _sieve_size; ++i)
        if (bs[i]) {
            for (ll j = i * i; j <= _sieve_size; j += i)
            primes.push_back((int)i);
}
bool isPrime(ll N) { // works for N <= (last prime in primes)^2
   if (N <= _sieve_size) return bs[N]; // O(1) sieve check for small primes
    for (int i = 0: i < (int)primes.size(): ++i) // brute force for larger
        if (N % primes[i] == 0) return false;
    return true; // more time if N is prime!
}
Java BigInteger
 TODO fib example
BigInteger.ZERO // constants
i.mod(m) // base number conversion
i.isProbablePrime(10) // Probabilistic prime testing
i.gcd(k)
x.modPow(y, n) // calculate x^y mod n
Combinatorics
 C(n,0) = C(n,n) = 1
 C(n,k) = C(n-1,k-1) + C(n-1,k)
Catalan numbers
 1. Cat(n) Count the number of distinct binary trees with n vertices.
 2. Count number of expressions counting n correctly matched pairs of parentheses.
 3. Count ways a convex polygon can be triangulated.
 Cat(0) = 1
 Cat(n+1) = \frac{(2n+2)(2n+1)}{(n+2)(n+1)} * Cat(n)
Cycle Finding
 TODO
Game Theory
 TODO
Linear Diphantine Equation
```

TODO

## DP

## Data structures

## Union Find

```
class UnionFind { // rank ordered with path compression
public:
   UnionFind(int n) {
       rank.assign(n, 0);
       p.assign(n, 0);
       set_size.assign(n, 1);
       num sets = n:
       for (int i = 0; i < n; ++i)
            p[i] = i:
   }
   int find_set(int i) { return (p[i] == i) ? i : (p[i] = find_set(p[i])); }
   bool is_same_set(int i, int j) { return find_set(i) == find_set(j); }
    void union_set(int i, int j) {
       if (!is_same_set(i, j)) {
            --num_sets;
            int x = find_set(i), y = find_set(j);
            if (rank[x] > rank[y]) {
                p[v] = x;
                set_size[x] += set_size[y];
           }
            else {
                y = [x]q
                set_size[v] += set_size[x];
                if (rank[x] == rank[y]) rank[y]++;
       }
```

```
}
    int num_disjoint_sets() { return num_sets; }
    int size_of_set(int i) { return set_size[find_set(i)]; }
    vi rank, p, set_size;
    int num_sets;
}:
Segment Tree
class SegmentTree { // Max range query. Change >= to <= for min.
    vi st. a:
    int n:
    int left(int p) { return p << 1: } // Same as binary hear
    int right(int p) { return (p << 1) + 1; }
    void build(int p, int 1, int r) { // O(n \log n)
       if (1 == r)
            st[p] = 1:
        else {
            build(left(p), 1, (1 + r) / 2);
            build(right(p), (1 + r) / 2 + 1, r);
            int p1 = st[left(p)], p2 = st[right(p)];
            st[p] = (a[p1] >= a[p2]) ? p1 : p2; // Build max
       }
    }
    int rmq(int p, int l, int r, int i, int j) { // O(\log n)
       if (i > r \mid | j < 1) return -1; // outside of range
       if (1 >= i && r <= j) return st[p]; // inside range
        int p1 = rmq(left(p), 1, (1 + r) / 2, i, j);
        int p2 = rmq(right(p), (1 + r) / 2 + 1, r, i, j);
       if (p1 == -1) return p2;
       if (p2 == -1) return p1:
        return (a[p1] >= a[p2]) ? p1 : p2; // Return max inside
    }
    // Support for dynamic updating. O(log n)
    int update_point(int p, int 1, int r, int idx, int new_value) {
       int i = idx, j = idx;
       if (i > r || j < 1)
           return st[p];
       if (1 == i && r == j) {
            a[i] = new_value;
            return st[p] = 1;
       int p1, p2;
       p1 = update_point(left(p), 1, (1 + r) / 2, idx, new_value);
        p2 = update_point(right(p), (1 + r) / 2, r, idx, new_value);
```

```
return st[p] = (a[p1] >= a[p2]) ? p1 : p2; // Max query
    }
public:
    SegmentTree(const vi &_a) {
        a = _a; n = (int) a.size(); // Copy for local use
        st.assign(4 * n, 0); // Large enough of zeroes
        build(1, 0, n - 1);
    }
    // Return index of max O(\log n)
    int rmq(int i, int j) { return rmq(1, 0, n - 1, i, j); }
    // Update index to a new value.
    int update point(int idx, int new value) {
        return update_point(1, 0, n - 1, idx, new_value);
};
Graph
Kruskal MST
// use union find class
int kruskal_mst(vector<pair<int, ii> > &EdgeList, int V) {
    int mst cost = 0:
    UnionFind UF(V):
    for (int i = 0; i < EdgeList.size(); ++i) {</pre>
        pair<int, ii> front = EdgeList[i];
        if (!UF.isSameSet(front.second.first, front.second.second)) {
            mst_cost += front.first;
            UF.unionSet(front.second.first.front.second.second):
    }
    return mst_cost;
}
Bipartite check
bool is_bipartite(int s) {
    ai a: a.push(s):
    vi color(n, INF); color[s] = 0;
    while (!q.empty()) {
        int u = q.front(); q.pop();
        for (int j = 0; j < (int)adjs[u].size(); ++j) {
            ii v = adjs[u][j];
            if (color[v.first] == INF) {
                color[v.first] = 1 - color[u];
                a.push(v.first):
            else if (color[v.first] == color[u]) {
                return false:
```

```
// in main
                                                                                 dfsNumberCounter = 0;
    return true;
                                                                                 dfs_num.assign(V, UNVISITED);
                                                                                 dfs_low.assign(V, 0);
Maximum Bipartite Cardinality Matching
                                                                                 dfs_parent.assign(V, 0);
                                                                                 articulation vertex.assign(V. 0):
vector < vi > AdjList; // initialize
                                                                                 printf("Bridges:\n");
vi match. vis:
                                                                                 for (int i = 0: i < V: ++i)
                                                                                     if (dfs_num[i] == UNVISITED) { // special case for root
int aug(int 1) { // return 1 if augmenting path is found, 0 otherwise
                                                                                          dfsRoot = i; rootChildren = 0;
   if (vis[1]) return 0:
                                                                                          articulationPointAndBridge(i);
    vis[1] = 1;
                                                                                          articulation_vertex[dfsRoot] = (rootChildren > 1);
    for (int j = 0; j < (int)AdjList[1].size(); ++j) {</pre>
        int r = AdjList[1][j];
                                                                                 // articulation vertex contains Articulation Points
        if (match[r] == -1 || aug(match[r])) {
            match[r] = 1:
                                                                                 Diikstra
            return 1:
        }
                                                                                 vector < vector < ii> > AdjList; // pair < node, cost>
    }
                                                                                 int V. E. s. t:
    return 0;
                                                                                 int dijsktra(int s, int t) { // variant will leave duplicate nodes in queue
                                                                                     vi dist(V. INF):
// in main
                                                                                     dist[s] = 0;
int MCBM = 0: // result
                                                                                      priority queue <ii. vector <ii>, greater <ii> > pq:
match.assign(V. -1):
                                                                                     pg.push(ii(0, s)):
for (int 1 = 0; 1 < n; ++1) {
                                                                                     while (!pq.empty()) {
                                                                                          ii front = pq.top(); pq.pop();
    vis.assign(n. 0):
    MCBM += aug(1);
                                                                                          int d = front.first, u = front.second;
}
                                                                                          if (d > dist[u]) continue; // important check
                                                                                          for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
Articulation points and bridges
                                                                                              ii v = AdjList[u][j];
                                                                                              if (dist[u] + v.second < dist[v.first]) {</pre>
void articulationPointAndBridge(int u) {
                                                                                                  dist[v.first] = dist[u] + v.second: // relax
    dfs_low[u] = dfs_num[u] = dfsNumberCounter++; // dfs_low[u] <= dfs_num[u]
                                                                                                  pq.push(ii(dist[v.first], v.first));
    for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
                                                                                              }
        ii v = AdiList[u][i]:
                                                                                         }
        if (dfs_num[v.first] == UNVISITED) {
                                                                                     }
            dfs parent[v.first] = u:
                                                                                      return dist[t]:
            if (u == dfsRoot) rootChildren++:
                                                                                 }
                                                                                 Bellman Ford
            articulationPointAndBridge(v.first):
            if (dfs low[v.first] >= dfs num[u])
                                                                                 int bellman ford(int s. int t) { // O(VE) when using add list
                articulation vertex[u] = true:
                                                                                     vi dist(V. INF): dist[s] = 0:
            if (dfs low[v.first] > dfs num[u])
                                                                                     for (int i = 0; i < V - 1; ++i) // relax all edges V-1 times
                printf(" Edge (%d,%d) is a bridge\n", u, v.first);
                                                                                          for (int u = 0: u < V: ++u)
            dfs_low[u] = min(dfs_low[u], dfs_low[v.first]);
                                                                                              for (int j = 0; j< (int)AdjList[u].size(); ++j) {</pre>
                                                                                                  ii v = AdjList[u][j]; // record SP spanning here if needed
        else if (v.first != dfs parent[u]) // a back edge and not direct
                                                                                                  dist[v.first] = min(dist[v.first], dist[u] + v.second);
                                                                                              }
            dfs_low[u] = min(dfs_low[u], dfs_num[v.first]);
                                                                                      return dist[t]:
                                                                                 }
```

}

```
mf = 0:
// check if there exists a negative cycle
                                                                                     while (1) { // run \ bfs
                                                                                         f = 0:
bool hasNegativeCycle = false;
for (int u = 0: u < V: ++u)
                                                                                         bitset <MAXN > vis: vis[s] = true: // bitset is faster
   for (int j = 0; j < (int) AdjList[u].size(); ++j) {</pre>
                                                                                         queue < int > q; q.push(s);
       ii v = AdjList[u][j];
                                                                                         p.assign(MAXN, -1); // record the BFS spanning tree, from s to t
       if (dist[v.first] > dist[u] + v.second) // if still possible
                                                                                         while (!a.emptv()) {
            hasNegativeCycle = true; // then neq cycle exists
                                                                                             int u = q.front(); q.pop();
   }
                                                                                             if (u == t) break: // stop bfs if we reach t
                                                                                             for (int j = 0; j < (int)AdjList[u].size(); ++j) { // faster with
Euler Tour
                                                                                                  AdjList
                                                                                                 int v = AdjList[u][j];
list < int > cyc; // list for fast insertion in middle
                                                                                                 if (res[u][v] > 0 && !vis[v])
                                                                                                     vis[v] = true, a.push(v), p[v] = u:
void EulerTour(list<int>::iterator i, int u) {
                                                                                             }
    for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
                                                                                         }
       ii v = AdiList[u][i]:
                                                                                         augment(t, INF);
       if (v.second) {
                                                                                         if (f == 0) break:
                                                                                                               // we cannot send any more flow, terminate
            v.second = 0; // mark as to be removed
                                                                                                                 // we can still send a flow, increase the max
                                                                                         mf += f;
            for (int k = 0; k < (int)AdjList[v.first].size(); ++k) {</pre>
                                                                                              flow!
                ii uu = AdjList[v.first][k]; // remove bi-directional
                                                                                     }
                if (uu.first == u && uu.second) {
                                                                                     return mf:
                    uu.second = 0:
                                                                                 }
                    break:
                }
                                                                                 Flood Fill
            EulerTour(cyc.insert(i, u), v.first);
                                                                                 // need grid, R, C
                                                                                 int dr[8] = \{ 1, 1, 0, -1, -1, -1, 0, 1 \};
                                                                                 int dc[8] = \{ 0, 1, 1, 1, 0, -1, -1, -1 \};
                                                                                 // Return size of CC
// inside main
                                                                                 int floodfill(int r, int c, char c1, char c2) {
cvc.clear():
                                                                                     if (r < 0 | | r >= R | | c < 0 | | c >= C) return 0:
EulerTour(cyc.begin(), A); // cyc contains euler tour starting at A
                                                                                     if (grid[r][c] != c1) return 0:
for (list<int>::iterator it = cyc.begin(); it != cyc.end(); ++it)
    printf("%d\n", *it); // the Euler tour
                                                                                     int ans = 1: // Because vertex (r. c) has c1 as its color
                                                                                     grid[r][c] = c2; // Color it
Edmond Karp
                                                                                     for (int d = 0; d < 8; ++d)
                                                                                         ans += floodfill(r + dr[d], c + dc[d], c1, c2):
// setup res, s, t, AdjList as global variables
                                                                                     return ans;
int res[MAXN][MAXN], mf, f, s, t;
                                                                                 }
vector <vi> AdjList; // Don't forget backward edges!
                                                                                 Topological Sort
void augment(int v, int minEdge) { // traverse BFS spanning tree from s to t
   if (v == s) { f = minEdge; return; } // record minEdge in a global
                                                                                 vi ts: // Result in reverse order
       variable f
                                                                                 void topo(int u) {
    else if (p[v] != -1) {
                                                                                     seen[u] = 1; // Init to false
        augment(p[v], min(minEdge, res[p[v]][v]));
                                                                                     for (int i = 0; i < (int)adj_list[u].size(); ++i) {</pre>
        res[p[v]][v] -= f: res[v][p[v]] += f:
                                                                                         ii v = adi list[u][i]:
   }
                                                                                         if (!seen[v.first])
}
                                                                                             topo(v.first);
                                                                                     }
                                                                                     ts.push_back(u);
int edmond_karp() {
```

```
}
                                                                                   if (s == 0) return 0:
                                                                                   if (memo[s] != 0) return memo[s];
// use
ts.clear():
                                                                                   int best = -1:
// init seen to false
for (int i = 0; i < n; ++i)
                                                                                   int x = 0; // Choose our first node to switch as the first node with odd
   if (!seen[i]) topo(i);
                                                                                       values we can find.
                                                                                   while (((s >> x) \& 1) == 0) ++x; //x = number of trailing zeros
Strongly Connected Components
                                                                                   // Try to combine with all other odd value nodes.
vi dfs_num, dfs_low, S, visited;
                                                                                   for (int y = x + 1; y < n; ++y) {
                                                                                       if ((s >> y) & 1 == 0) continue;
void tarjanSCC(int u) {
   dfs_low[u] = dfs_num[u] = dfsNumberCounter++; // dfs_low[u] <= dfs_num[u]
                                                                                       int comb = s^{(1 << x)^{(1 << y)}} // Switch off the selected nodes.
   S.push_back(u); // stores u in a vector based on order of visitation
   visited[u] = 1:
                                                                                       // Cost will be to combine these two nodes + combining the rest.
   for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
                                                                                       int cost = d[x][y] + min_cost(comb);
       ii v = AdiList[u][i]:
       if (dfs_num[v.first] == UNVISITED)
                                                                                       if (best == -1 || cost < best)
           tarianSCC(v.first):
                                                                                           best = cost:
       if (visited[v.first])
                                                                                   }
           dfs_low[u] - min(dfs_low[u], dfs_low[v.first]);
   }
                                                                                   return memo[s] = best:
                                                                               }
   if (dfs low[u] == dfs num[u]) { // if this is a root (start) of an SCC
       printf("SCC %d:", ++numSCC): // this part is done after recursion
                                                                               String
       while (1) {
                                                                               Knuth-Morris-Pratt
           int v = S.back(); S.pop_back(); visited[v] = 0;
                                                                                 TODO
           printf(" %d", v);
           if (u == v) break:
                                                                               Edit Distance
                                                                                 TODO
       printf("\n");
                                                                               LCS
                                                                                 TODO
                                                                               Suffix Trie
// in main
                                                                                 TODO
dfs_num.assign(V, UNVISITED);
dfs_low.assign(V, 0);
                                                                               Geometry
visited.assign(V, 0):
                                                                                 TODO
dfsNumberCounter = numSCC = 0;
for (int i = 0; i < V; ++i)
                                                                               Convex Hull
   if (dfs_num[i] == UNVISITED)
                                                                                 TODO
       tarianSCC(i):
Chinese Postman
// Weight of euler tour in connected graph.
// Need to fill d[][] with min cost between any two nodes. Do floyd warshall
int memo[1 << MAX]: // dp bitmask memo structure
```

// Min cost of increasing by one the degree of set of the given odd vertices,

to make them even.
int min\_cost(int s) {