LiU Default

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Maximum Bipartite Cardinality Matching	7	using namespace stu,	
Articulation points and bridges	7	#define rep(i, a, b) for(int i = (a); i < int(b); ++i)	
Dijkstra	7	#define rrep(i, a, b) for(int i = (a); i >= int(b);i)	
Dijkstra Timetable	8	<pre>#define trav(it, v) for(typeof((v).begin()) it=(v).begin(); it!=(v).end(); it)</pre>	++
Bellman Ford	8	<pre>#define all(x) (x).begin(),(x).end()</pre>	
Euler Tour	8	<pre>#define B begin()</pre>	
Edmond Karp	8	<pre>#define E end()</pre>	
Maxflow Binblock	9	#define pb push_back	
Flood Fill	9	typedef pair <int, int=""> ii; // used in comp prog algorithms</int,>	
Topological Sort	9 0	typedef double fl;	
Strongly Connected Components	10	typedef long double ld;	
	_	typedef long long 11;	
Chinese Postman	10	<pre>typedef pair<int, int=""> pii;</int,></pre>	

```
typedef vector <int> vi;
typedef vector <vi> vvi;
typedef map <int, int> mii;
typedef multimap <int, int> mmii;
typedef set <int> si;
typedef multiset <int> msi;
typedef complex <fl> cx;

const int UNVISITED = -1;
const int INF = 1e9;
const double EPS = 1e-9;
const double PI = acos(-1.0); // alternative (2.0 * acos(0.0))
```

Complexity

Modern CPU compute 100M in 3s.

\overline{n}	Worst AC Algorithm	Problem
$\leq [1011]$	$O(n!), O(n^6)$	e.g. Enumerating permutations
$\leq [1518]$	$O(2^n n^2)$	e.g. DP TSP
$\leq [1822]$	$O(2^n n)$	e.g. DP with bitmask
≤ 100	$O(n^4)$	e.g. DP with 3 dimensions
≤ 400	$O(n^3)$	e.g. Floyd Warshall's
$\leq 2K$	$O(n^2 log n)$	e.g. $2 \text{ loops} + \text{a tree-related DS}$
$\leq 10K$	$O(n^2)$	e.g. Selection/Insert sort
$\leq 1M$	O(nlogn)	e.g. Building Segment Tree
$\leq 100M$	O(n)	I/O bottleneck

Limits

32-bit int $2^{31} - 1 = 2147483647 \approx 10^{10}$ 64-bit signed long long upper limit $2^{63} - 1 = 9223372036854775807 \approx 10^{18}$

Data structures

Union Find

```
class UnionFind { // rank ordered with path compression
public:
    UnionFind(int n) {
        rank.assign(n, 0);
        p.assign(n, 0);
        set_size.assign(n, 1);
        num_sets = n;
        for (int i = 0; i < n; ++i)
            p[i] = i;
    }
    int find_set(int i) { return (p[i] == i) ? i : (p[i] = find_set(p[i])); }
    bool is_same_set(int i, int j) { return find_set(i) == find_set(j); }
    void union_set(int i, int j) {
        if (!is_same_set(i, j)) {
            --num_sets;
    }
}</pre>
```

```
int x = find_set(i), y = find_set(j);
            if (rank[x] > rank[v]) {
                p[v] = x;
                set_size[x] += set_size[y];
            }
            else {
                p[x] = y;
                set_size[v] += set_size[x];
                if (rank[x] == rank[y]) rank[y]++;
            }
        }
    int num_disjoint_sets() { return num_sets; }
    int size_of_set(int i) { return set_size[find_set(i)]; }
private:
    vi rank, p, set_size;
    int num sets:
};
Fenwick Tree
// Ideal to answer dynamic Range Sum Queries
#define LSOne(S) (S & (-S))
struct FenwickTree {
 vi ft:
 FenwickTree() {}
  // initialization: n + 1 zeroes, ignore index 0
  FenwickTree(int n) { ft.assign(n + 1, 0); }
  int rsq(int b) { // returns RSQ(1, b), O(log n)
   int sum = 0; for (; b; b -= LSOne(b)) sum += ft[b];
    return sum:
  int rsq(int a, int b) { // returns RSQ(a, b), O(log n)
    return rsq(b) - (a == 1 ? 0 : rsq(a - 1));
  // adjusts value of the k-th element by v
  void adjust(int k, int v) { // O(log n)
    for (; k < (int)ft.size(); k += LSOne(k)) ft[k] += v;</pre>
};
Segment Tree
class SegmentTree { // Max range query. Change >= to <= for min.</pre>
    vi st, a;
    int left(int p) { return p << 1; } // Same as binary heap</pre>
    int right(int p) { return (p << 1) + 1; }</pre>
    void build(int p, int 1, int r) { // O(n log n)
        if (1 == r)
```

st[p] = 1;

```
else {
            build(left(p), 1, (1 + r) / 2);
            build(right(p), (1 + r) / 2 + 1, r);
            int p1 = st[left(p)], p2 = st[right(p)];
            st[p] = (a[p1] >= a[p2]) ? p1 : p2; // Build max
        }
   }
    int rmq(int p, int l, int r, int i, int j) { // O(log n)
        if (i > r || j < 1) return -1; // outside of range
        if (1 >= i && r <= j) return st[p]; // inside range</pre>
        int p1 = rmg(left(p), 1, (1 + r) / 2, i, j);
        int p2 = rmq(right(p), (1 + r) / 2 + 1, r, i, j);
        if (p1 == -1) return p2;
        if (p2 == -1) return p1:
        return (a[p1] >= a[p2]) ? p1 : p2; // Return max inside
    // Support for dynamic updating. O(log n)
    int update_point(int p, int 1, int r, int idx, int new_value) {
        int i = idx, j = idx;
        if (i > r || j < 1)</pre>
            return st[p];
        if (1 == i && r == j) {
            a[i] = new value:
            return st[p] = 1;
        }
        int p1, p2;
        p1 = update_point(left(p), 1, (1 + r) / 2, idx, new_value);
        p2 = update_point(right(p), (1 + r) / 2, r, idx, new_value);
        return st[p] = (a[p1] >= a[p2]) ? p1 : p2; // Max query
   }
public:
    SegmentTree(const vi &_a) {
        a = _a; n = (int) a.size(); // Copy for local use
        st.assign(4 * n, 0); // Large enough of zeroes
        build(1, 0, n - 1);
    }
    // Return index of max O(log n)
    int rmq(int i, int j) { return rmq(1, 0, n - 1, i, j); }
    // Update index to a new value.
    int update_point(int idx, int new_value) {
        return update_point(1, 0, n - 1, idx, new_value);
};
```

Math

int gcd(int a, int b) { return b == 0 ? a : gcd(b, a % b); }
$$\sum_{k=1}^{\infty} x^k = \frac{1}{1-x}, |x| < 1$$

$$\sum_{k=1}^{n} x^k = \frac{1-x^n}{1-x}, x \neq 0$$

$$\sum_{k=1}^{n} k = \frac{n(n+1)}{2}$$

$$\sum_{k=1}^{n} k^2 = \frac{n(n+1)(2n+1)}{6}$$

$$\sum_{k=1}^{n} k^2 = \frac{n^2(n+1)^2}{4}$$

$$\pi \approx 3.14159265 \approx \frac{355}{113}$$

$$\sin(\frac{pi}{4}) = \cos(\frac{pi}{4}) = \frac{1}{\sqrt{2}}$$

$$\sin(\frac{pi}{3}) = \cos(\frac{pi}{3}) = \frac{1}{2}$$

$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$$

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

$$= \frac{2 \tan \theta}{1 + \tan^2 \theta}$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta$$

$$= 2 \cos^2 \theta - 1$$

$$= 1 - 2 \sin^2 \theta$$

$$= \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$$

Factorial

```
1 1 2 6 24 120 720 5040 40320 362880 3628800 // 0..10 39916800 479001600 1932053504 // 11..13
```

Primes

```
// 100 first primes
2 3 5 7 11 13 17 19 23 29 31 37 41 43 47 53 59 61 67 71 73 79 83 89 97 101
103 107 109 113 127 131 137 139 149 151 157 163 167 173 179 181 191 193 197
199 211 223 227 229 233 239 241 251 257 263 269 271 277 281 283 293 307 311
313 317 331 337 347 349 353 359 367 373 379 383 389 397 401 409 419 421 431
433 439 443 449 457 461 463 467 479 487 491 499 503 509 521 523 541
// Some larger primes
104729 1299709 9999991 15485863 179424673 2147483647 32416190071
112272535095293 54673257461630679457
// prime sieve with prime checking
const int MAX_SIEVE = 1e7; // 1e7 in a few seconds
ll _sieve_size;
bitset < MAX_SIEVE + 10 > bs;
vi primes;
void sieve(ll upperbound) {
   _sieve_size = upperbound + 1;
    bs.set();
    bs[0] = bs[1] = 0:
    for (11 i = 2; i <= _sieve_size; ++i)</pre>
        if (bs[i]) {
            for (ll j = i * i; j <= _sieve_size; j += i)</pre>
                bs[i] = 0;
            primes.push_back((int)i);
       }
}
bool isPrime(11 N) { // works for N <= (last prime in primes)^2
   if (N <= _sieve_size) return bs[N]; // O(1) sieve check for small primes
    for (int i = 0; i < (int)primes.size(); ++i) // brute force for larger</pre>
        if (N % primes[i] == 0) return false;
    return true: // more time if N is prime!
}
Fibonacci
0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 // 0..15
   F(0) = 0, F(1) = 1
```

$$F(0) = 0, F(1) = 1$$

$$F(n) = F(n-1) + F(n-2)$$

Combinatorics

$$C(n,0) = C(n,n) = 1$$

 $C(n,k) = C(n-1,k-1) + C(n-1,k)$

Catalan numbers

```
1 1 2 5 14 42 132 429 1430 4862 16796 // 0..10
```

- 1. Cat(n) Count the number of distinct binary trees with n vertices.
- 2. Count number of expressions counting n correctly matched pairs of parentheses.
- 3. Count ways a convex polygon can be triangulated.

$$Cat(0) = 1$$

 $Cat(n) = \frac{2(2n-1)}{n+1} * Cat(n-1)$

Powers of 2

1 2 4 8 16 32 64 128 256 512 1024 // 0..10 2048 4096 8192 16384 32768 65536 // 11..16 4294967296 4611686018427387904 // 32, 63

Extended Euclid: Linear Diphantine Equation

```
int x, y, d; // answer, give d = gcd(a, b)
void extendedEuclid(int a, int b) { // solve a*x + b*y = d
    if (b == 0) { x = 1; y = 0; d = a; return; }
    extendedEuclid(b, a % b);
    int x1 = y, y1 = x - (a /b) * y;
    x = x1; y = y1;
}
```

Cycle Finding

```
// find position and length of the repeated pattern in a generated sequence
if floydCycleFinding(int x0) { // define int f(int x) which generates the
    sequence
    // 1st phase, hare 2x speed of turtoise
    int tortoise = f(x0), hare = f(f(x0));
    while (tortoise != hare) { tortoise = f(tortoise); hare = f(f(hare)); }
    // 2nd phase, find mu, same speed
    int mu = 0; hare = x0;
    while (tortoise != hare) { tortoise = f(tortoise); hare = f(hare); ++mu;
        }
    // 3rd phase, find lambda, hare moves tortoise still
    int lambda = 1; hare = f(tortoise);
    while (tortoise != hare) { hare = f(hare); ++lambda; }
    return ii(mu, lambda); // mu: start of cycle, lambda: cycle length
}
```

Game Theory

Nim Game

Two players take turns to remove objects from distinct heaps. On each turn, a player must remove at least one object and may remove any number of objects, but only from the same heap. For the starting player to win, n_1 ^...^ $n_k \neq 0$. (bitwise xor)

Josephus

```
/* Description: n people numberd 1..n are standing in a circle and we elim-
 * inate every k:th person until there is only one left. The problem is to
     find
 * who survives, i.e. the index of that person.
 * josephus2 solves this problem when k = 2. The next[] array in the
     simulation
 * has to be as large as n.
 * Time: 0 (k log n), 0 (log n), 0 (k * n)
int josephus(int n, int k) {
 int d=1:
 while (d \le (k-1)*n) d = (k*d+k-2)/(k-1);
 return k*n+1-d:
int josephus2(int n) {
 int d=1:
 while (d<<1<=n) d<<=1;
 return 2*(n& d)+1:
int josephus_simulation(int n, int k) {
 int next[10000], current = 0;
 for(int i=0;i<n;++i) next[i]=(i+1)%n;</pre>
 while(n>1) {
    const int steps = (k-2)\%(n--);
   for(int i=0;i<steps;++i) current=next[current];</pre>
    current = next[current] = next[next[current]];
 }
  return current+1;
Java BigInteger
BigInteger.ZERO // constants
i.mod(m) // base number conversion
i.isProbablePrime(10) // Probabilistic prime testing
i.gcd(k)
x.modPow(y, n) // calculate x^y mod n
// Catalan numbers with BigInteger
import java.util.Scanner;
import java.math.BigInteger;
class Main {
    public static BigInteger[] mem;
    public static BigInteger cat(int n) {
        if (n == 0) return BigInteger.ONE;
        if (mem[n] != null) return mem[n];
        BigInteger k = BigInteger.valueOf(2 * (2 * n - 1)).multiply(cat(n -
            1));
```

```
return mem[n] = k.divide(BigInteger.valueOf(n + 1));
}

public static void main(String[] args) {
    Scanner sc = new Scanner(System.in);
    mem = new BigInteger[11]; // adjust as necessary
    while (sc.hasNextInt()) {
        System.out.println(cat(sc.nextInt()));
    }
}
```

6

DP

Longest Increasing Subsequence

```
vi lis(vi a) { // O(n log k)
   int L[MAX];
   vi dp(a.size());
   int lis = 0;
   for (int i = 0; i < a.size(); ++i) {
        // LIS ending at a[i] is at length pos + 1
        int pos = lower_bound(L, L + lis, a[i]) - L;
        L[pos] = a[i];
        dp[i] = pos + 1;

        if (pos + 1 > lis) lis = pos + 1;
    }
    return dp; // Return lis array
}
```

Knapsack

```
// vector<int> knapsack(capasity, vector<pair<weight, value> >)
// O(NC)
// M(NC)
vi knapsack(int c, vector<pii>&o){
  vi res;
  vector<vi> dp(o.size()+1); //[obj][cap]
  trav(it,dp) it->resize(c+1);
  rep(i,0,o.size()) rep(j,o[i].first,c+1)
    dp[i+1][j]=max(dp[i][j], dp[i][j-o[i].first]+o[i].second);

int mx=0; rep(i,0,c+1) if(dp.back()[i]>dp.back()[mx]) mx=i;
  rrep(i,o.size()-1,0) if(dp[i][mx]<dp[i+1][mx]){
    res.push_back(i); mx-=o[i].first;
  }
  return res;
}</pre>
```

Graph

Kruskal MST

```
7
```

```
// use union find class
                                                                                  // in main
int kruskal_mst(vector<pair<int, ii> > &EdgeList, int V) {
                                                                                  int MCBM = 0; // result
    int mst_cost = 0;
                                                                                  match.assign(V, -1);
    UnionFind UF(V):
                                                                                  for (int 1 = 0: 1 < n: ++1) {
    for (int i = 0; i < EdgeList.size(); ++i) {</pre>
                                                                                      vis.assign(n, 0);
                                                                                      MCBM += aug(1);
        pair < int , ii > front = EdgeList[i];
        if (!UF.isSameSet(front.second.first, front.second.second)) {
            mst_cost += front.first;
                                                                                  Articulation points and bridges
            UF.unionSet(front.second.first, front.second.second);
        }
    }
                                                                                  void articulationPointAndBridge(int u) {
                                                                                      dfs_low[u] = dfs_num[u] = dfsNumberCounter++; // dfs_low[u] <= dfs_num[u]
                                                                                      for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
    return mst_cost;
}
                                                                                          ii v = AdjList[u][j];
                                                                                          if (dfs num[v.first] == UNVISITED) {
Bipartite check
                                                                                              dfs_parent[v.first] = u;
                                                                                              if (u == dfsRoot) rootChildren++;
bool is_bipartite(int s) {
    qi q; q.push(s);
                                                                                              articulationPointAndBridge(v.first);
    vi color(n. INF): color[s] = 0:
    while (!q.empty()) {
                                                                                              if (dfs_low[v.first] >= dfs_num[u])
        int u = q.front(); q.pop();
                                                                                                  articulation vertex[u] = true:
                                                                                              if (dfs_low[v.first] > dfs_num[u])
        for (int j = 0; j < (int)adjs[u].size(); ++j) {</pre>
            ii v = adjs[u][j];
                                                                                                  printf(" Edge (%d,%d) is a bridge\n", u, v.first);
            if (color[v.first] == INF) {
                                                                                              dfs_low[u] = min(dfs_low[u], dfs_low[v.first]);
                color[v.first] = 1 - color[u];
                q.push(v.first);
                                                                                          else if (v.first != dfs_parent[u]) // a back edge and not direct
            else if (color[v.first] == color[u]) {
                                                                                              dfs_low[u] = min(dfs_low[u], dfs_num[v.first]);
                return false;
                                                                                      }
                                                                                  }
        }
                                                                                  // in main
                                                                                  dfsNumberCounter = 0;
    return true;
                                                                                  dfs_num.assign(V, UNVISITED);
                                                                                  dfs_low.assign(V, 0);
Maximum Bipartite Cardinality Matching
                                                                                  dfs_parent.assign(V, 0);
                                                                                  articulation_vertex.assign(V, 0);
vector < vi > AdjList; // initialize
                                                                                  printf("Bridges:\n");
vi match, vis;
                                                                                  for (int i = 0; i < V; ++i)</pre>
                                                                                      if (dfs_num[i] == UNVISITED) { // special case for root
int aug(int 1) { // return 1 if augmenting path is found, 0 otherwise
                                                                                          dfsRoot = i; rootChildren = 0;
    if (vis[1]) return 0;
                                                                                          articulationPointAndBridge(i);
    vis[1] = 1:
                                                                                          articulation vertex[dfsRoot] = (rootChildren > 1):
    for (int j = 0; j < (int)AdjList[1].size(); ++j) {</pre>
        int r = AdjList[1][j];
                                                                                  // articulation_vertex contains Articulation Points
        if (match[r] == -1 || aug(match[r])) {
            match[r] = 1;
                                                                                  Diikstra
            return 1;
        }
                                                                                  vector<vector<ii>> AdjList; // pair<node, cost>
    }
                                                                                  int V, E, s, t;
    return 0:
                                                                                  int dijsktra(int s, int t) { // variant will leave duplicate nodes in queue
                                                                                      vi dist(V, INF);
```

```
dist[s] = 0;
                                                                                  int bellman_ford(int s, int t) { // O(VE) when using adj list
    priority_queue <ii, vector <ii>, greater <ii> > pq;
                                                                                      vi dist(V, INF); dist[s] = 0;
                                                                                      for (int i = 0; i < V - 1; ++i) // relax all edges V-1 times
    pq.push(ii(0, s));
    while (!pa.emptv()) {
                                                                                          for (int u = 0: u < V: ++u)
        ii front = pq.top(); pq.pop();
                                                                                              for (int j = 0; j < (int) AdjList[u].size(); ++j) {</pre>
        int d = front.first. u = front.second:
                                                                                                  ii v = AdiList[u][i]: // record SP spanning here if needed
                                                                                                  dist[v.first] = min(dist[v.first], dist[u] + v.second);
        if (d > dist[u]) continue; // important check
        for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
                                                                                              }
            ii v = AdiList[u][i]:
            if (dist[u] + v.second < dist[v.first]) {</pre>
                                                                                      return dist[t];
                dist[v.first] = dist[u] + v.second: // relax
                pq.push(ii(dist[v.first], v.first));
                                                                                  // check if there exists a negative cycle
        }
                                                                                  bool hasNegativeCycle = false;
                                                                                  for (int u = 0; u < V; ++u)
    return dist[t];
                                                                                      for (int j = 0; j < (int) AdjList[u].size(); ++j) {</pre>
                                                                                          ii v = AdiList[u][i]:
                                                                                          if (dist[v.first] > dist[u] + v.second) // if still possible
Dijkstra Timetable
                                                                                              hasNegativeCycle = true;
                                                                                                                          // then neg cycle exists
                                                                                      }
// vector < dist > djikstra (vector < vector < egde < dst, len, starttime, period > >,
     int source, vector int<path>);
                                                                                  Euler Tour
// Complexity O(ElogN)
                                                                                  list <int> cvc: // list for fast insertion in middle
struct Edge{
                                                                                  void EulerTour(list<int>::iterator i, int u) {
 int dst,1,ts,tp;
                                                                                      for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
 Edge(int a, int b, int c, int d){dst=a; l=b; ts=c; tp=d;};
                                                                                          ii v = AdiList[u][i]:
}:
                                                                                          if (v.second) {
                                                                                              v.second = 0; // mark as to be removed
vi djikstra(vector<vector<Edge> >& g, int s, vi&path){
                                                                                              for (int k = 0: k < (int)AdiList[v.first].size(): ++k) {</pre>
 vi res(g.size(),-1); path.resize(g.size());
                                                                                                  ii uu = AdjList[v.first][k]; // remove bi-directional
  set<pii>Q: vector<bool> av(g.size().1);
                                                                                                  if (uu.first == u && uu.second) {
  res[s]=0; Q.insert(pii(0,s));
                                                                                                       uu.second = 0:
  while(!Q.empty()){
                                                                                                       break:
    int cur = Q.B->second:
    Q.erase(Q.B);
    av[cur]=0:
                                                                                              EulerTour(cyc.insert(i, u), v.first);
    trav(it, g[cur]){
      if(it->tp==0 && it->ts < res[cur]) continue;</pre>
                                                                                      }
      int nxt = res[cur]-it->ts:
      if(res[cur]<=it->ts) nxt=it->ts; else nxt=it->ts + (nxt/it->tp)*(it->tp
          ) + (nxt\%it->tp ? it->tp : 0);
                                                                                  // inside main
      nxt+=it->1:
                                                                                  cvc.clear():
      int& dst=res[it->dst]:
                                                                                  EulerTour(cyc.begin(), A); // cyc contains euler tour starting at A
      if(dst!=-1 && dst<=nxt) continue:</pre>
                                                                                  for (list<int>::iterator it = cyc.begin(); it != cyc.end(); ++it)
      if(dst>-1) Q.erase(pii(dst, it->dst));
                                                                                      printf("%d\n", *it); // the Euler tour
      dst=nxt;
      Q.insert(pii(dst, it->dst)):
                                                                                  Edmond Karp
      path[it->dst]=cur;
                                                                                  // setup res, s, t, AdjList as global variables
                                                                                  int res[MAXN][MAXN]. mf. f. s. t:
  return res;
                                                                                  vi p;
                                                                                  vector < vi > AdiList: // Don't forget backward edges!
Bellman Ford
                                                                                  void augment(int v, int minEdge) { // traverse BFS spanning tree from s to t
```

```
if (v == s) { f = minEdge; return; } // record minEdge in a global
        variable f
    else if (p[v] != -1) {
        augment(p[v], min(minEdge, res[p[v]][v]));
        res[p[v]][v] -= f; res[v][p[v]] += f;
    }
}
int edmond_karp() {
    mf = 0:
    while (1) { // run bfs
        f = 0:
        bitset < MAXN > vis; vis[s] = true; // bitset is faster
        queue < int > q; q.push(s);
        p.assign(MAXN, -1); // record the BFS spanning tree, from s to t
        while (!q.empty()) {
            int u = q.front(); q.pop();
            if (u == t) break; // stop bfs if we reach t
            for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
                int v = AdiList[u][i]:
                if (res[u][v] > 0 && !vis[v])
                    vis[v] = true, q.push(v), p[v] = u;
            }
        augment(t, INF);
        if (f == 0) break; // we cannot send any more flow, terminate
        mf += f: // we can still send a flow, increase the max flow!
    }
    return mf;
Maxflow Binblock
// int maxflow(vector< vector<pair<dest,cap> > network, int source, int
    dest, vector < vector < pair < dest, flow > > resultflow)
// Complexity O(VE) (:
// Works with noninteger values
vvi G; vector < bool > av;
vector <si> GE:
bool dfs(int s, int t, int c){
 if(s==t) return 1;
  av[s]=0;
  trav(it. GE[s]){
    if(!av[*it]|| c>G[s][*it]) continue;
    if(dfs(*it, t, c)){
     G[s][*it]=c;
     G[*it][s]+=c;
      return 1;
    }
 }
  return 0;
```

```
int maxflow(vector<vector<pii> >&g, int s, int t, vector<vector<pii> > &resf)
  int n=g.size();
 G.resize(n): trav(it, G) it->resize(n):
  GE.resize(n);
 rep(i,0,n) trav(it,g[i]) {G[i][it->first]+=it->second; GE[i].insert(it->
      first); GE[it->first].insert(i);}
  vvi GG=G;
 int res=0; av.resize(n,1);
  rrep(i,30,0) {fill(all(av),1); while(dfs(s,t,1 << i)){fill(all(av),1); res</pre>
      += 1<<i:}}
  resf.resize(g.size());
  rep(i,0,n) trav(it, g[i]) {
    int d=min(GG[i][it->first]-G[i][it->first], it->second);
    if(d<=0) continue;
    GG[i][it->first]-=d;
    resf[i].pb(pii(it->first.d)):
 }
 return res;
7
Flood Fill
// need grid, R, C
int dr[8] = \{ 1, 1, 0, -1, -1, -1, 0, 1 \}:
int dc[8] = \{ 0, 1, 1, 1, 0, -1, -1, -1 \};
// Return size of CC
int floodfill(int r, int c, char c1, char c2) {
    if (r < 0 | | r >= R | | c < 0 | | c >= C) return 0;
    if (grid[r][c] != c1) return 0:
    int ans = 1; // Because vertex (r, c) has c1 as its color
    grid[r][c] = c2; // Color it
    for (int d = 0; d < 8; ++d)
        ans += floodfill(r + dr[d], c + dc[d], c1, c2):
    return ans;
}
Topological Sort
vi ts; // Result in reverse order
void topo(int u) {
    seen[u] = 1: // Init to false
    for (int i = 0; i < (int)adj_list[u].size(); ++i) {</pre>
        ii v = adj_list[u][i];
        if (!seen[v.first])
            topo(v.first);
    ts.push_back(u);
}
// use
```

ts.clear();

```
// init seen to false
                                                                                      for (int y = x + 1; y < n; ++y) {
for (int i = 0; i < n; ++i)</pre>
                                                                                          if ((s >> y) & 1 == 0) continue;
    if (!seen[i]) topo(i);
                                                                                          int comb = s ^ (1 << x) ^ (1 << y); // Switch off the selected nodes.
                                                                                          // Cost will be to combine these two nodes + combining the rest.
Strongly Connected Components
                                                                                          int cost = d[x][y] + min_cost(comb);
                                                                                          if (best == -1 || cost < best)
vi dfs num. dfs low. S. visited:
                                                                                              best = cost:
                                                                                      }
void tarianSCC(int u) {
                                                                                      return memo[s] = best:
    dfs_low[u] = dfs_num[u] = dfsNumberCounter++; // dfs_low[u] <= dfs_num[u]
    S.push_back(u); // stores u in a vector based on order of visitation
    visited[u] = 1:
                                                                                  String
    for (int j = 0; j < (int)AdjList[u].size(); ++j) {</pre>
                                                                                  Knuth-Morris-Pratt
        ii v = AdjList[u][j];
        if (dfs num[v.first] == UNVISITED)
                                                                                  int b[MAXN]: // back table
            tarjanSCC(v.first);
                                                                                  void kmpPreprocess(string P) {
        if (visited[v.first])
                                                                                      int i = 0, j = -1; b[0] = -1;
            dfs_low[u] - min(dfs_low[u], dfs_low[v.first]);
                                                                                      while (i < P.size()) {</pre>
   }
                                                                                          while (j \ge 0 \&\& P[i] != P[j]) j = b[j];
                                                                                          ++i; ++j;
    if (dfs_low[u] == dfs_num[u]) { // if this is a root (start) of an SCC
                                                                                          b[i] = i;
        printf("SCC %d:", ++numSCC); // this part is done after recursion
                                                                                      }
                                                                                  }
            int v = S.back(); S.pop_back(); visited[v] = 0;
            printf(" %d", v);
                                                                                  void kmpSearch(string T, string P) { // does P match T?
            if (u == v) break;
                                                                                      kmpPreprocess(P); // must prepare P
                                                                                      int i = 0, j = 0;
        printf("\n");
                                                                                      while (i < T.size()) {</pre>
                                                                                          while (j \ge 0 \&\& T[i] != P[j]) j = b[j];
                                                                                          ++i: ++i:
                                                                                          if (j == P.size()) {
// in main
                                                                                              printf("P is found at index %d in T\n", i - j);
dfs_num.assign(V, UNVISITED);
                                                                                              j = b[j]; // prepare for next possible match
dfs_low.assign(V, 0);
visited.assign(V, 0);
                                                                                      }
dfsNumberCounter = numSCC = 0;
                                                                                  }
for (int i = 0; i < V; ++i)</pre>
    if (dfs num[i] == UNVISITED)
                                                                                  Edit Distance
        tarjanSCC(i);
                                                                                  vector < vi > dp;
Chinese Postman
                                                                                  int edit_distance(string A, string B) { // align A with B
                                                                                      dp.assign((int)A.size() + 1, vi()); // dynamic dp matrix
// Weight of euler tour in connected graph.
                                                                                      for (int i = 0; i <= A.size(); ++i)</pre>
                                                                                          dp[i].assign((int)B.size() + 1, 0);
// Need to fill d[][] with min cost between any two nodes. Do floyd warshall
   before.
int memo[1 << MAX];</pre>
                                                                                      for (int i = 1; i <= A.size(); ++i)</pre>
int min_cost(int s) { // incr odd degrees and make all even
                                                                                          dp[i][0] = i * -1; // delete substring A[1..i], score -1
   if (s == 0) return 0:
                                                                                      for (int i = 1; i <= B.size(); ++i)</pre>
   if (memo[s] != 0) return memo[s];
                                                                                          dp[0][i] = i * -1; // insert space in B[1..i], score -1
   int best = -1:
    int x = 0; // Choose our first node to switch as the first node with odd
                                                                                      for (int i = 1; i <= A.size(); ++i)</pre>
        values we can find.
                                                                                          for (int j = 1; j <= B.size(); ++j) {</pre>
    while (((s >> x) \& 1) == 0) ++x; // x = number of trailing zeros
                                                                                              // Match +2, Mismatch -1
    // Try to combine with all other odd value nodes.
                                                                                              dp[i][j] = dp[i-1][j-1] + (A[i-1] == B[j-1]?2:-1);
```

```
dp[i][j] = max(dp[i][j], dp[i - 1][j] - 1); // delete
                                                                                 // impl
            dp[i][j] = max(dp[i][j], dp[i][j-1]-1); // insert
                                                                                 const int MAXN = 100010; // ok up to ~100k
                                                                                 int RA[MAXN], tmpRA[MAXN]; // rank array + tmp
                                                                                 int SA[MAXN], tmpSA[MAXN]; // suffix array + tmp
    return dp[A.size()][B.size()]; // max alignment score
                                                                                 int c[MAXN]; // freq table for counting sort
                                                                                 int n, m; // globals for T and P
                                                                                 int Phi[MAXN]; // for computing longest common prefix
Longest Common Subsequence
                                                                                 int PLCP[MAXN];
                                                                                 int LCP[MAXN]; // LCP[i] stores the LCP between previous suffix T + SA[i-1]
vector < vi > dp;
                                                                                                                                // and current suffix T + SA[i]
int lcs(string A, string B) { // turn edit distance into lcs
    dp.assign((int)A.size() + 1, vi()); // dynamic dp matrix
                                                                                 void countingSort(int k, int n) { // sort RA, res in SA
    for (int i = 0; i <= A.size(); ++i)</pre>
                                                                                     int sum, maxi = max(300, n); // up to 255 ASCII chars of length n
        dp[i].assign((int)B.size() + 1, 0): // all edge cases 0
                                                                                     memset(c, 0, sizeof c);
                                                                                     for (int i = 0; i < n; ++i) // count freq of each integer rank
    for (int i = 1; i <= A.size(); ++i)</pre>
                                                                                         c[i + k < n ? RA[i + k] : 0]++;
        for (int j = 1; j <= B.size(); ++j) {</pre>
                                                                                     for (int i = sum = 0: i < maxi: ++i) {</pre>
            // Match 1, Mismatch -INF
                                                                                         int t = c[i]; c[i] = sum; sum += t;
            dp[i][j] = dp[i-1][j-1] + (A[i-1] == B[j-1]?1:-INF);
            dp[i][j] = max(dp[i][j], dp[i - 1][j]); // delete cost 0
                                                                                     for (int i = 0; i < n; ++i) // shuffle suffix array if necessary</pre>
            dp[i][j] = max(dp[i][j], dp[i][j - 1]); // insert cost 0
                                                                                         tmpSA[c[SA[i] + k < n ? RA[SA[i] + k] : 0]++] = SA[i];
        }
                                                                                     for (int i = 0; i < n; ++i) // update suffix array</pre>
                                                                                         SA[i] = tmpSA[i];
    return dp[A.size()][B.size()]; // max alignment score
                                                                                 }
                                                                                 void constructSA(string &T) { // Construct Suffix Array in O(n log n)
Suffix Array
                                                                                     int n = T.size():
                                                                                     for (int i = 0: i < n: ++i) RA[i] = T[i]:
// Suffix Array is a simpler version of Suffix Tree.
                                                                                    for (int i = 0; i < n; ++i) SA[i] = i;</pre>
// It is slower to construct, O(n log n) vs O(n)
                                                                                    for (int k = 1; k < n; k <<= 1) { // repeat sort log n times
// but it's a lot simpler to program.
                                                                                         countingSort(k, n); // radix sort
                                                                                         countingSort(0, n); // stable sort on first item
// ex. find all Longest Common Substrings of a and b, O(n log n)
                                                                                         int r = 0; tmpRA[SA[0]] = 0; // re-rank from rank r = 0
string T = a + "$" + b + "#": // Chars lower, combine input strings
                                                                                         for (int i = 1; i < n; ++i) {
n = T.size(); m = b.size(); // for ease of programming
                                                                                             // if same pair => r otherwise increase rank
constructSA(T); // Construct Suffix Array
                                                                                             if (RA[SA[i]] == RA[SA[i-1]] & RA[SA[i] + k] == RA[SA[i-1] +
computeLCP(T); // LCS depends on LCP, so must do this
                                                                                                  k])
                                                                                                 tmpRA[SA[i]] = r;
set < string > res = allLCS(T): // Can also use LCS()
                                                                                             else
if (res.empty()) printf("No common sequence.\n");
                                                                                                 tmpRA[SA[i]] = ++r;
for (set<string>::iterator i = res.begin(); i != res.end(); ++i) {
    printf("%s\n", i->c_str());
                                                                                         for (int i = 0; i < n; ++i) // update rank array
                                                                                             RA[i] = tmpRA[i];
                                                                                         if (RA[SA[n - 1]] == n - 1) break; // optimization
// ex. find Longest Repeated Substring (min 2 times), O(n log n)
                                                                                     }
T += "$"; // input string T, append '$'
                                                                                 }
n = T.size(); // for ease of programming
constructSA(T); // Construct Suffix Array
                                                                                 void computeLCP(string &T) { // Longest Common Prefix, O(n)
computeLCP(T); // LRS depends on LCP
                                                                                     Phi[SA[O]] = -1:
                                                                                    for (int i = 1; i < n; ++i)
pair < string , int > ans = LRS(T); // LRS string and #repetitions
                                                                                         Phi[SA[i]] = SA[i - 1]:
if (ans.first.size()) printf("%s %d\n", ans.first.c_str(), ans.second);
                                                                                    for (int i = 0: i < n: ++i) {</pre>
else printf("No repetitions found!\n");
                                                                                         int L = 0;
```

```
if (Phi[i] == -1) { PLCP[i] = 0; continue; }
        while (T[i + L] == T[Phi[i] + L]) ++L;
        PLCP[i] = L:
        L = max(L - 1, 0):
    }
    for (int i = 0: i < n: ++i)
        LCP[i] = PLCP[SA[i]]:
}
int owner(int idx) { return (idx < n - m - 1) ? 1 : 2; }
// Longest Common Substring in O(n)
ii LCS() { // return < LCS length, index >, where SA[index] gives index in T
    int idx = 0, maxLCP = -1;
    for (int i = 1; i < n; ++i)</pre>
        if (owner(SA[i]) != owner(SA[i - 1]) && LCP[i] > maxLCP)
            maxLCP = LCP[i], idx = i:
    return ii(maxLCP, idx);
}
set < string > allLCS(string &T) { // return all unique longest substrings O(n
    log n)
    int maxLCP = -1;
    set < string > res;
    for (int i = 0; i < n; ++i) {</pre>
        if (owner(SA[i]) == owner(SA[i - 1])) continue;
        if (LCP[i] == 0) continue;
        if (LCP[i] > maxLCP) res.clear();
        if (LCP[i] >= maxLCP) {
            maxLCP = LCP[i]:
            res.insert(T.substr(SA[i], maxLCP));
        }
    }
    return res;
// Longest Repeated Substring (substring 2 times or more)
ii LRS() { // returns < LRS length, index >, where SA[index] gives index in T
    int idx = 0, maxLCP = -1;
    for (int i = 1; i < n; i++)</pre>
        if (LCP[i] > maxLCP)
          maxLCP = LCP[i], idx = i;
    return ii(maxLCP, idx);
}
pair < string, int > LRS(string &T) { // return LRS and #repetitions
    int maxLCP = -1, rep = 0;
    for (int i = 1; i < n; i++) {</pre>
        string curr = T.substr(SA[i], LCP[i]);
        if (LCP[i] > maxLCP) {
            maxLCP = LCP[i]: rep = 2:
            s = curr;
```

```
}
    else if (s == curr) ++rep;
}
return make_pair(s, rep);
}
```

Geometry

Points and Lines

```
struct point_i { // prefer
    int x, y;
    point_i() { x = y = 0; }
    point_i(int _x, int _y) : x(_x), y(_y) { }
}:
struct point { // only if double needed, prefer ints
    double x. v:
    point() { x = y = 0.0; }
    point(double _x, double _y) : x(_x), y(_y) { }
    bool operator < (point other) const {</pre>
        if (fabs(x - other.x) > EPS) // EPS comparison!
            return x < other.x:</pre>
        return v < other.v:</pre>
    }
    bool operator == (point other) const { // EPS comparison
        return (fabs(x - other.x) < EPS && (fabs(v - other.v) < EPS)):
    }
}:
// Euclidian distance
double dist(point p1, point p2) { return hypot(p1.x - p2.x, p1.y - p2.y); }
// A vector is not a point here
struct vec { double x, y; vec(double _x, double _y) : x(_x), y(_y) { } };
vec toVec(point a, point b) { return vec(b.x - a.x, b.y - a.y); }
vec scale(vec v, double s) { return vec(v.x * s, v.y * s); }
double cross(vec a, vec b) { return a.x * b.y - a.y * b.x; }
bool ccw(point p, point q, point r) {
    return cross(toVec(p, q), toVec(p, r)) > 0;
}
bool collinear(point p, point q, point r) {
    return fabs(cross(toVec(p, q), toVec(p, r))) < EPS;</pre>
// Move a point
point translate(point p, vec v) { return point(p.x + v.x, p.y + v.y); }
// Rotate p by theta degrees CCW w.r.t origin (0, 0)
point rotate(point p, double theta) { // call with 360 - theta for CW
    double rad = DEG_to_RAD(theta); // multiply theta with PI / 180.0
    return point(p.x * cos(rad) - p.y * sin(rad),
```

```
p.x * sin(rad) + p.y * cos(rad));
}
// Rotate p w.r.t pivot
point rotate_around(point p, point pivot, double angle) {
    point o = translate(p, vec(-pivot.x, -pivot.y));
    return translate(rotate(o, angle), toVec(pivot));
}
double dot(vec a, vec b) { return a.x * b.x + a.y * b.y; }
double norm sq(vec v) { return v.x * v.x + v.v * v.v: }
double angle(point a, point o, point b) { // return angle aob in rad
    vec oa = toVec(o, a), ob = toVec(o, b);
    return acos(dot(a, ob) / sqrt(norm_sq(oa) * norm_sq(ob)));
// Closest point to the line defined by a and b (must be different!)
double distToLine(point p, point a, point b, point &c) {
    vec ap = toVec(a, p), ab = toVec(a, b);
    double u = dot(ap, ab) / norm_sq(ab);
    c = translate(a, scale(ab, u));
    return dist(p, c);
}
// Closest point to line segment between a and b (OK if a == b)
double distToLineSegment(point p, point a, point b, point &c) {
    vec ap = toVec(a, p), ab = toVec(a, b):
    double u = dot(ap, ab) / norm_sq(ab);
    if (u < 0.0) { c = point(a.x. a.v); return dist(p. a); }
    if (u > 1.0) { c = point(b.x, b.y); return dist(p, b); }
    return distToLine(p, a, b, c):
}
// ax + bv + c = 0, b = 0.0 if vertical, 1.0 otherwise
struct line { double a, b, c; };
void pointsToLine(point p1, point p2, line &1) {
    if (fabs(p1.x - p2.x) < EPS) { // special for vertical
       1.a = 1.0; 1.b = 0.0; 1.c = -p1.x;
    else {
       1.a = -(double)(p1.y - p2.y) / (p1.x - p2.x);
       1.b = 1.0;
       1.c = -(double)(1.a * p1.x) - p1.y;
}
bool areParallel(line 11, line 12) { // check a & b
    return (fabs(11.a - 12.a) < EPS) && (fabs(11.b - 12.b) < EPS);
bool areSame(line 11, line 12) { // check c
```

```
return areParallel(11, 12) && (fabs(11.c - 12.c) < EPS);
}
// Check lines. not line segments
bool areIntersect(line 11, line 12, point &p) {
   if (areParallel(11, 12)) return false:
    p.x = (12.b * 11.c - 11.b * 12.c) / (12.a * 11.b - 11.a * 12.b);
    if (fabs(11.b) > EPS) p.y = -(11.a * p.x + 11.c);
                         p.y = -(12.a * p.x + 12.c);
    return true;
}
Circles
double DEG to RAD(double d) { return d * PI / 180.0: }
double RAD_to_DEG(double r) { return r * 180.0 / PI; }
// 2: inside, 1: border, 0: outside. Exakt int calc
int insideCircle(point_i p, point_i c, int r) {
    int dx = p.x - c.x. dy = p.y - c.y:
    int Euc = dx * dx + dy * dy, rSq = r * r;
    return Euc < rSq ? 2 : Euc == rSq ? 1 : 0;</pre>
}
// Given to points p1, p2 and the radius of a circle.
// Return if there can be a circle with the given radius and
// if so return it's center. To get both possible centers,
// call again with p1 and p2 swapped.
bool circle2PtsRad(point p1, point p2, double r, point &c) {
    double d2 = (p1.x - p2.x) * (p1.x - p2.x) +
               (p1.y - p2.y) * (p1.y - p2.y);
    double det = r * r / d2 - 0.25;
    if (det < 0.0) return false;</pre>
    double h = sqrt(det);
    c.x = (p1.x + p2.x) * 0.5 + (p1.y - p2.y) * h;
    c.y = (p1.y + p2.y) * 0.5 + (p2.x - p1.x) * h;
    return true;
}
Triangles
double perimeter(double ab, double bc, double ca) {
   return ab + bc + ca;
double perimeter(point a, point b, point c) {
    return dist(a, b) + dist(b, c) + dist(c, a);
double area(double ab, double bc, double ca) {
    double s = 0.5 * perimeter(ab, bc, ca); // Heron's formula
    return sgrt(s) * sgrt(s - ab) * sgrt(s - bc) * sgrt(s - ca):
}
```

```
double area(point a, point b, point c) {
    return area(dist(a, b), dist(b, c), dist(c, a));
// Radius of a circle described inside the triangle
double rInCircle(double ab. double bc. double ca) {
    return area(ab, bc, ca) / (0.5 * perimeter(ab, bc, ca));
double rInCircle(point a, point b, point c) {
    return rInCircle(dist(a, b), dist(b, c), dist(c, a)):
}
// 1 if there is a circle inside the triangle. ctr will be the center
// and r the radi
int inCircle(point p1, point p2, point p3, point &ctr, double &r) {
    r = rInCircle(p1, p2, p3):
    if (fabs(r) < EPS) return 0; // not in circle
    line 11. 12:
    double ratio = dist(p1, p2) / dist(p1, p3);
    point p = translate(p2, scale(toVec(p2, p3), ratio / (1 + ratio)));
    pointsToLine(p1, p, l1);
    ratio = dist(p2, p1) / dist(p2, p3);
    p = translate(p1, scale(toVec(p1, p3), ratio / (1 + ratio)));
    pointsToLine(p2, p, 12);
    areIntersect(11, 12, ctr);
    return 1:
}
// Radius of the circle outside the triangle
double rCircumCircle(double ab, double bc, double ca) {
    return ab * bc * ca / (4.0 * area(ab, bc, ca)):
double rCircumCircle(point a, point b, point c) {
    return rCircumCircle(dist(a, b), dist(b, c), dist(c, a));
// 1 if there is a circle circums the triangle. ctr will be the center
// and r the radi
int circumCircle(point p1, point p2, point p3, point &ctr, double &r) {
    double a = p2.x - p1.x, b = p2.y - p1.y;
    double c = p3.x - p1.x, d = p3.y - p1.y;
    double e = a * (p1.x + p2.x) + b * (p1.y + p2.y);
    double f = c * (p1.x + p3.x) + d * (p1.y + p3.y);
    double g = 2.0 * (a * (p3.y - p2.y) - b * (p3.x - p2.x));
    if (fabs(g) < EPS) return 0;</pre>
    ctr.x = (d * e - b * f) / g:
    ctr.y = (a * f - c * e) / g;
```

```
r = dist(p1, ctr);
    return 1:
bool canFormTriangle(double a, double b, double c) {
   return (a + b > c) && (a + c > b) && (b + c > a):
Polygons
// returns the perimeter, which is the sum of Euclidian distances
// of consecutive line segments (polygon edges)
double perimeter(const vector<point> &P) {
    double result = 0.0;
    for (int i = 0; i < (int)P.size() - 1; i++) // P[0] == P[n - 1]
        result += dist(P[i], P[i + 1]);
    return result:
7
double area(const vector<point> &P) {
    double result = 0.0, x1, y1, x2, y2;
    for (int i = 0; i < (int)P.size() - 1; i++) {</pre>
       x1 = P[i].x; x2 = P[i + 1].x;
       y1 = P[i].y; y2 = P[i + 1].y;
        result += (x1 * y2 - x2 * y1);
    }
    return fabs(result) / 2.0;
}
bool isConvex(const vector<point> &P) {
    int sz = (int)P.size():
    if (sz <= 3) return false;</pre>
   bool isLeft = ccw(P[0], P[1], P[2]);
   for (int i = 1: i < sz - 1: ++i)
        if (ccw(P[i], P[i+1], P[(i+2) == sz?1:i+2]) != isLeft)
            return false; // different sign -> this polygon is concave
    return true;
}
// true if pt in polygon, either convex or concave
bool inPolygon(point pt, const vector<point> &P) { // Assume P[0] == P[n - 1]
   if ((int)P.size() == 0) return false;
    double sum = 0;
    for (int i = 0; i < (int)P.size() - 1; i++) {</pre>
        if (ccw(pt, P[i], P[i + 1]))
           sum += angle(P[i], pt, P[i + 1]);
        else sum -= angle(P[i], pt, P[i + 1]);
    return fabs(fabs(sum) - 2 * PI) < EPS;</pre>
}
// Convex hull pivot check
point pivot(0, 0); // global pivot for CH compare fun
bool angleCmp(point a, point b) {
```

```
if (collinear(pivot, a, b))
        return dist(pivot, a) < dist(pivot, b);</pre>
    double d1x = a.x - pivot.x, d1y = a.y - pivot.y;
    double d2x = b.x - pivot.x, d2v = b.v - pivot.v;
    return (atan2(d1y, d1x) - atan2(d2y, d2x)) < 0;
}
vector<point> CH(vector<point> P) { // contents in P may be reshuffled
    int n = (int)P.size();
    if (n <= 3) {
        if (!(P[0] == P[n-1])) P.push_back(P[0]); // corner case
        return P; // special case, CH is P
   }
    int PO = 0; // first, find PO lowest Y, tie: lowest X
    for (int i = 1; i < n; ++i)</pre>
        if (P[i].v < P[P0].v || (P[i].v == P[P0].v && P[i].x < P[P0].x))
            P0 = i:
    swap(P[0], P[P0]); // second, sort w.r to angle to P0
    sort(++P.begin(), P.end(), angleCmp); // Don't sort P[0]
    //third, ccw tests
    vector < point > S;
    S.push_back(P[n - 1]); S.push_back(P[0]); S.push_back(P[1]);
    int i = 2;
    while (i < n) {
        int j = (int)S.size() - 1;
        if (ccw(S[j - 1], S[j], P[i])) S.push_back(P[i++]); // left turn
        else S.pop_back(); // right turn, bad point
   }
    return S;
Misc
Interval Cover
// O(n log n) vector<int> cover(start, end, vector<inteval pair>)
vi cover(fl s, fl e, vector < pair < fl, fl > & m) {
 int lst=-1:
```

```
vector < pair < type of (m[0]), int > > tm(m.size());
  rep(i,0,m.size()) tm[i]=make_pair(m[i],i);
  sort(all(tm));
  vi res:
  while(lst<int(m.size())){</pre>
    int cur=lst:
    for(int i=lst+1; i<int(m.size()) && tm[i].first.first<=s; i++){</pre>
      if((cur!=-1 && tm[i].first.second > tm[cur].first.second) ||
              (cur==-1 && tm[i].first.second >=s)) cur=i:
    if (cur==lst) break:
    lst=cur:
    res.push_back(tm[lst].second);
    s=tm[lst].first.second;
    if (s>=e && res.size()) return res;
  res.clear():
  return res;
Prefix Sum
vector<11> bt;
void add(int i, ll v){
  if(!i){bt[0]+=v; return;}
  while (i<int(bt.size())){</pre>
    bt[i]+=v;
    i+=(i&-i);
  } return:
11 sum(int i){
  ll res=bt[0];
  while(i>0){
```

res+=bt[i]:

i-=(i&-i):

} return res;