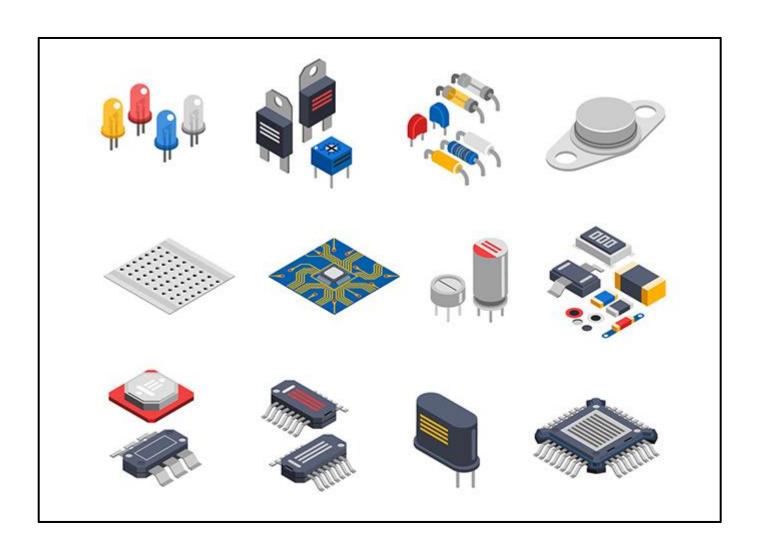
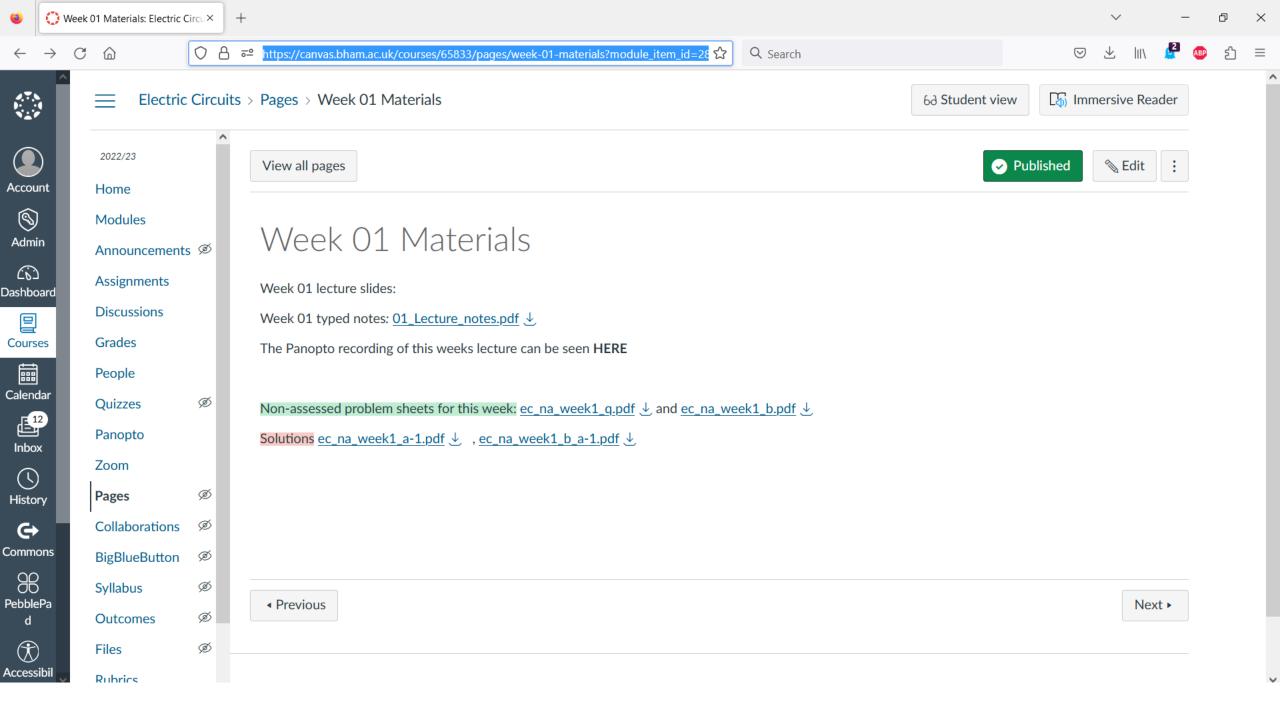
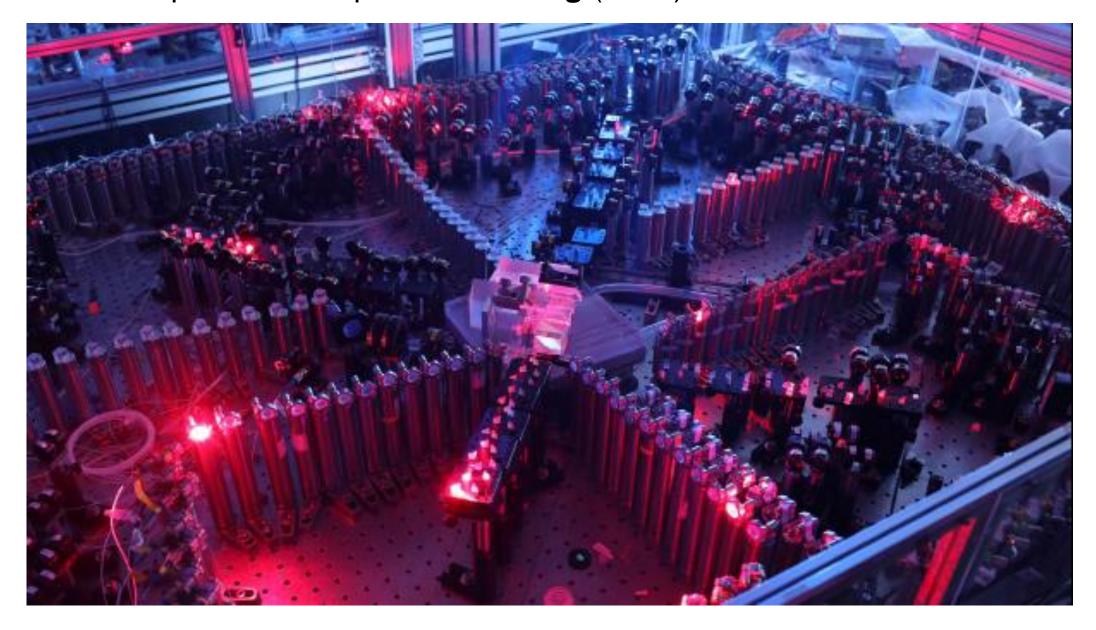
## **ELECTRIC CIRCUITS**

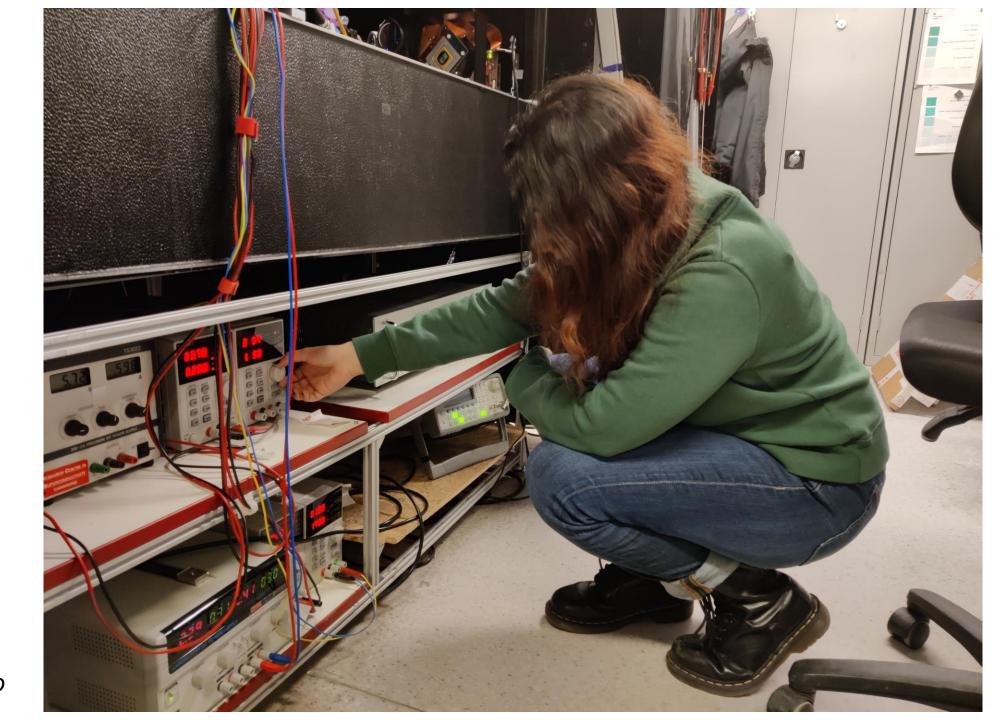


Vera Guarrera - v.guarrera@bham.ac.uk

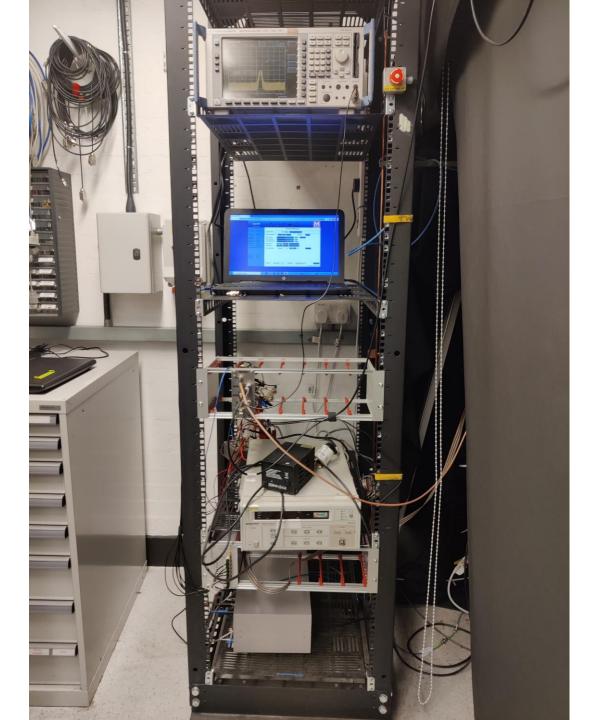


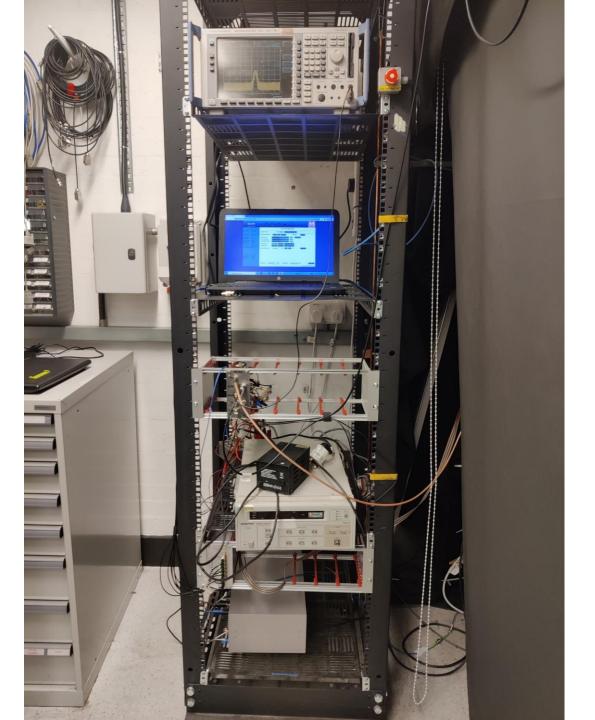
## Photonic quantum computer: Jiuzhang (2020)

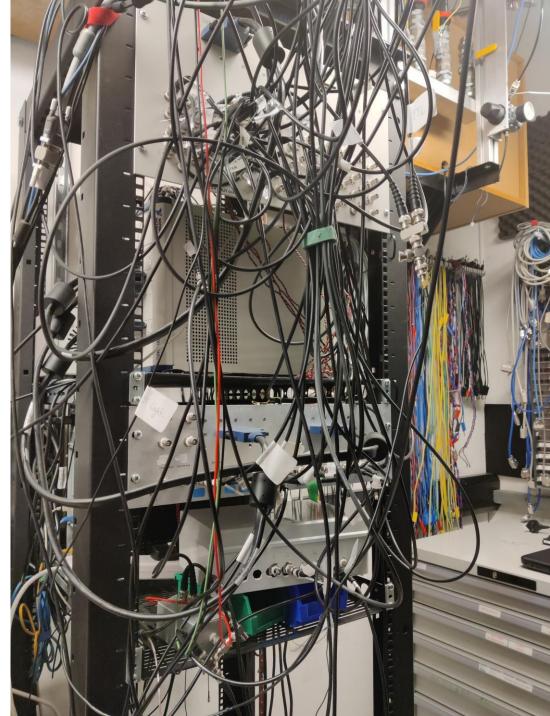




Phd student Symran working in the *Quantum Systems group* 







### Recommended textbooks

University Physics

Young and Freedman

Suggestions for further reading will be given at the end of each lecture

Introduction to Electric Circuits

Ray Powell. Highly recommended! Main Library - short loan, (5 copies)

Physics for scientists and engineers (5th edition)

Paul A. Tipler and Gene Mosca

Electric Circuits (TK3226)

P. Silvester. School of Electrical Engineering Library, (9 copies)

Introductory Circuit Theory (TK3226)

J.K.Fidler and L. Ibbotson. Main Library - short loan, (2 copies)

The art of Electronics – For advanced reading

P. Horowitz and W. Hill

## **Syllabus**

Direct current (DC) circuit analysis

 Current, voltage, Ohm's law, Kirchhoff's law, Thevenin's theorem, Superposition theorem

 Transient response

 Capacitors, inductors, RC and RL circuits, response to pulses

 Alternating current (AC)

 Circuit analysis
 (4 sessions)

Phasors, complex impedance, RC and RL filters, LCR circuits,

resonance, and Q factor.

### Week 01: material covered

Units and definitions: current, voltage, power

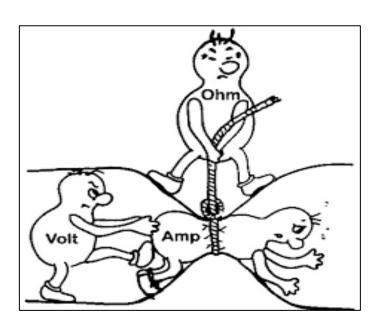
Resistance, Ohm's law

**Dimensional analysis** 

Resistors in series and in parallel

Voltage divider and current splitter

**Practical applications** 

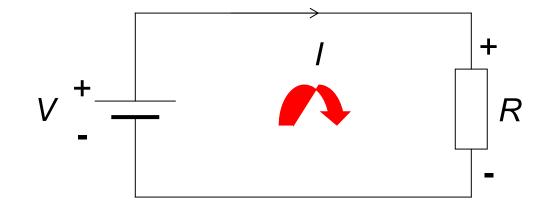


### **Definition**

### What is an Electrical Circuit?

A closed path around which an electrical current may flow.

Battery converts chemical energy into electrical potential energy.



Resistor only dissipates energy.

The terminal where the current enters a resistor is always at the higher electrical potential.

- Contains one or more active devices which deliver energy.
   e.g. battery or a source of Electromotive Force (EMF)
- Contains passive devices (e.g. resistors) which dissipate energy.
- Current is taken to flow from points of higher electrical potential to points of lower electrical potential.
- Conventional current flow is opposite to that of electrons.

## **Units**

#### Charge (Coulomb, C)

The unit of electrical charge is the Coulomb. Charge is quantized, that is, it comes in discrete amounts. The charge of an electron is  $-1.602 \times 10^{-19}$  C.

#### Current (Ampere, A)

Electric current is defined as the rate at which charge flows through a given point in a circuit:  $I = \frac{\Delta Q}{\Delta t}$ 

#### Potential Difference (Volt, V)

The work done when transferring charge from one point in a circuit to another:  $V = \frac{\Delta W}{\Delta Q}$ 

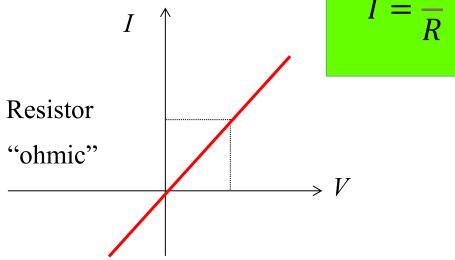
### Resistance (Ohm, Ω), Ohm's law

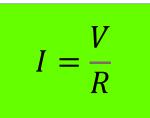
The ratio of the voltage across a circuit element to the current flowing through it.

Power (Watt, W) is defined as the rate of doing work.

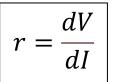
## **Resistance and Ohm's law**

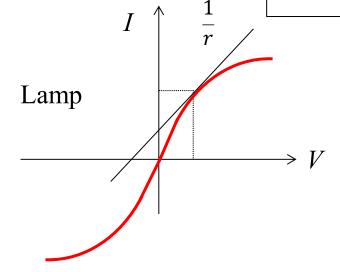
• I-V characteristics

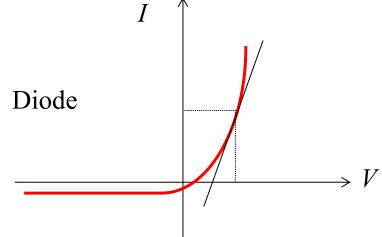




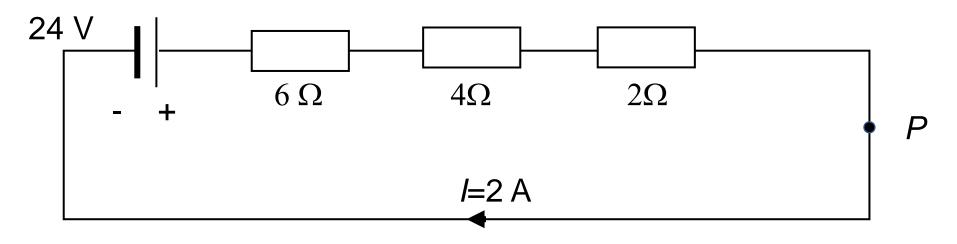
Dynamic resistance

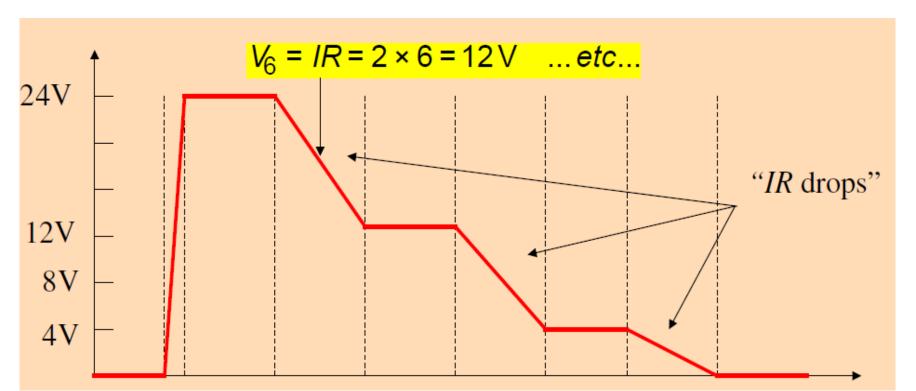




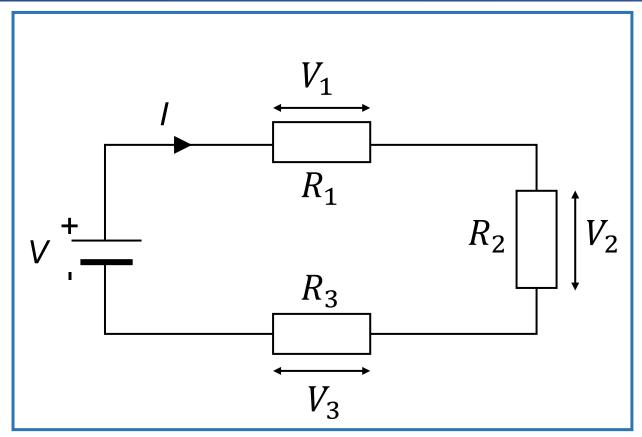


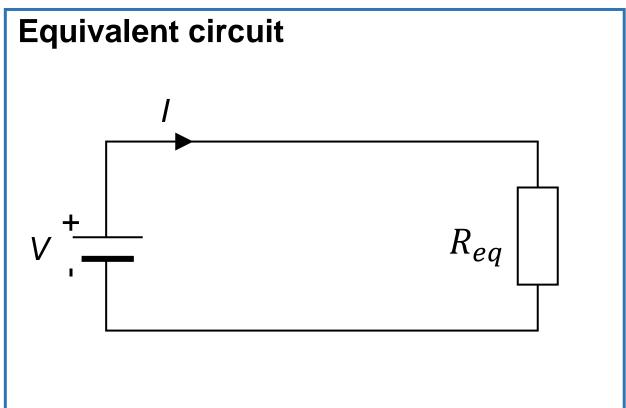
# Electrical potential in a series circuit





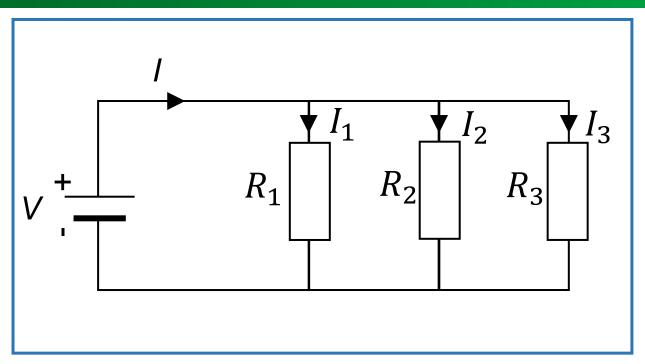
## Resistors in series

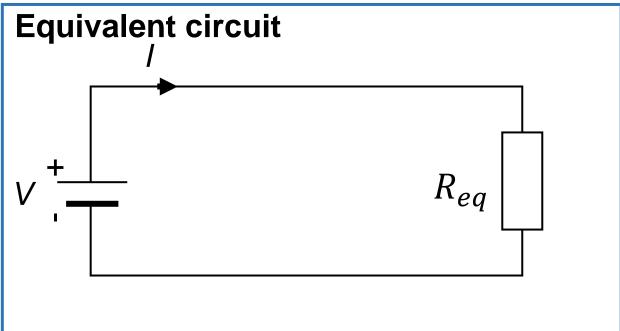




- 1) **Energy** is conserved:  $V = V_1 + V_2 + V_3$
- 2) The current through each resistor is the same.
- 3) By **Ohm's law**:  $V_1 = IR_1$ ,  $V_2 = IR_2$ , ...
- 4) Substituting 3) into 1):  $V = I(R_1 + R_2 + R_3) = IR_{eq}$   $R_{eq} = R_1 + R_2 + R_3$

# Resistors in parallel





- 1) Charge is conserved:  $I = I_1 + I_2 + I_3$
- 2) The voltage across each resistor is the same.
- 3) By **Ohm's law**:  $I_1 = \frac{V}{R_1}$ ,  $I_2 = \frac{V}{R_2}$ , ...

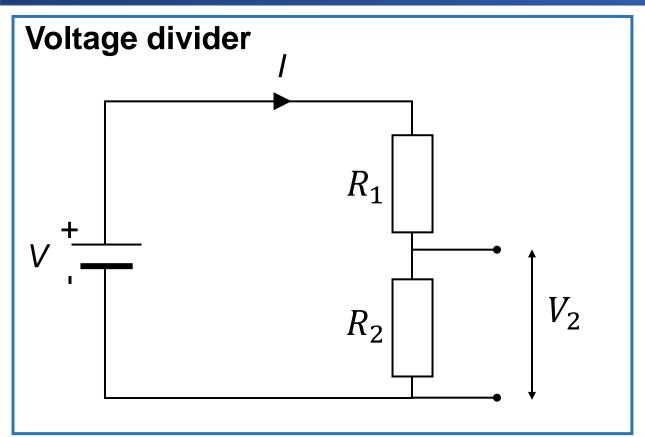
4) Substituting 3) into 1):

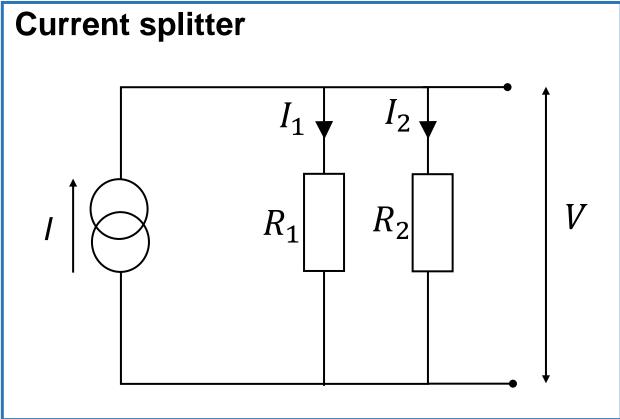
$$I = V\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}\right) = \frac{V}{R_{eq}}$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

## Two important circuit topologies





$$I = \frac{V}{R_{eq}} = \frac{V}{R_1 + R_2} = \frac{V_2}{R_2} = \frac{V_1}{R_1}$$

$$V_2 = V \frac{R_2}{R_1 + R_2}$$

$$V = IR_{eq} = I \frac{R_1 R_2}{R_1 + R_2} = I_2 R_2 = I_1 R_1$$

$$I_2 = I \frac{R_1}{R_1 + R_2}$$

# **Practical applications**

Electronic equipment is used every day at home and work.

## What fuse would you use for:

a) a typical electric lamp?	3A	5A	13A	60A
b) a 2 kW electric kettle?	3A	5A	13A	60A
c) an electric cooker?	3A	5A	13A	60A

Where do we start?

# **Starting point**

Ohm's law 
$$V = IR$$

What is V?

V is a **potential** i.e. **potential energy** per unit charge

$$V = \frac{E}{q}$$

**Energy** E = qV

$$E = qV$$

Power 
$$P = \frac{dE}{dt} = V \frac{dq}{dt} = VI$$
 assuming constant V (DC)

$$P = VI = RI^2$$

# **Practical applications**

### What fuse would you use for:

a) a typical electric lamp?

b) a 2 kW electric kettle?

c) an electric cooker?

3A 5A 13A 60A

3A 5A 13A 60A

3A 5A 13A 60A

#### Where do we start?

$$V = IR$$
  $P = IV$ 

a) Lamp  $10-20W/240V \approx 0.04-0.08 A$ 

b) Kettle  $3000W/240V \approx 12 A$ 

c) Cooker 12000W/240V ≈ 48 A

3A 5A 13A 60A 3A 5A 13A 60A 3A 5A 13A 60A

Some fuses designed to blow if current exceeds limit for short time others designed to survive current spikes.

## Week 01: summary

Units and definitions: current, voltage, power

Resistance, Ohm's law

**Dimensional analysis** 

Resistors in series and in parallel

Voltage divider and current splitter

**Practical applications** 

Further reading: Tipler, 26-1 to 26-4 Powell, Chapters 1 and 2

