


AC  $i = I \sin(\omega t)$

  
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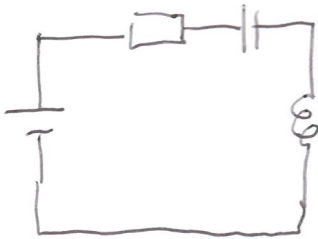
Resistance :  $V_R = V \sin(\omega t) = IR \sin(\omega t)$

Capacitors :  $V_C = V \sin(\omega t - \frac{\pi}{2}) = \frac{I}{\omega C} \sin(\omega t - \frac{\pi}{2}) = I X_C \sin(\omega t - \frac{\pi}{2})$

Inductors :  $V_L = V \sin(\omega t + \frac{\pi}{2}) = I \omega L \sin(\omega t + \frac{\pi}{2}) = I X_L \sin(\omega t + \frac{\pi}{2})$

All together

LRC circuit



$\left. \begin{aligned} \rightarrow I e^{j\omega t} \\ \rightarrow V e^{j\omega t} \end{aligned} \right\}$

$V = I \left( j\omega L + R + \frac{1}{j\omega C} \right) = I \underline{Z}$

← Equivalent ohm's law to use in AC

↳ complex impedance

$Z_R = R$

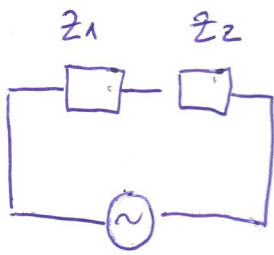
$Z_C = \frac{1}{j\omega C} = -j \frac{1}{\omega C}$

$Z_L = j\omega L$

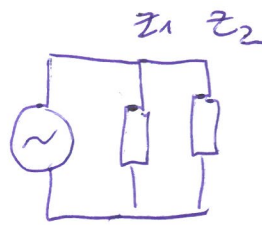
$Z = R + j(X_L - X_C)$

Now,  $V$  and  $I$  is a complex number

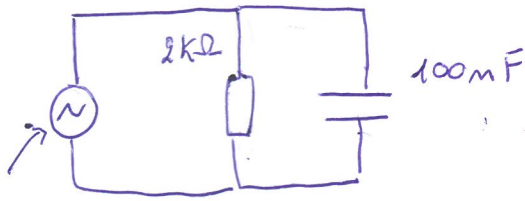
$\tan \phi = \frac{\text{Im}(Z)}{\text{Re}(Z)} ; V = |Z| I e^{j\phi}$



$$Z_{eq} = Z_1 + Z_2$$



$$\frac{1}{Z_{eq}} = \frac{1}{Z_1} + \frac{1}{Z_2}$$



$$i = 5\text{mA} \sin(\omega t)$$

$$f = 1\text{kHz}$$

$$\omega = \frac{2\pi}{T} = 2\pi f = 2\pi (1\text{kHz})$$

$$a) \quad \frac{1}{Z} = \frac{1}{Z_R} + \frac{1}{Z_C} = \frac{1}{R} + j\omega C$$

$$Z = \frac{R}{1 + j\omega RC} \cdot \frac{(1 - j\omega RC)}{(1 - j\omega RC)} = \frac{R}{(1 + (\omega RC)^2)} - j \frac{\omega R^2 C}{1 + (\omega RC)^2}$$

$$= (775 - j 974) \Omega$$

$$|Z| = \frac{1}{1 + (\omega RC)^2} \sqrt{R^2 + \omega^2 R^4 C^2} = \sqrt{775^2 + 974^2} \Omega = \boxed{1245 \Omega}$$

b) Ohm's law

$$V = I \cdot Z = 5\text{mA} \cdot (775 - j 974) \Omega = 3.875\text{V} - j 4.87\text{V}$$

$$|V| = I \cdot |Z| = 5\text{mA} \cdot 1245 \Omega = 6.23\text{V}$$

c) Ohm's law

$$I = \frac{V}{R} = \frac{V}{Z_R}$$

$$\Rightarrow I = \frac{|V|}{R} = \frac{6.23\text{V}}{2000 \Omega} = 3.12\text{mA}$$

$$d) \quad I = \frac{V}{Z_c} = \sqrt{I_{sc} C}$$

$$I = \frac{|V|}{Z_c} = |V| \sqrt{I_{sc} C} = 5 \cdot 3.91 \text{ mA}$$

$$e) \quad \phi = \tan^{-1} \left( \frac{\text{Im } Z}{\text{Re } Z} \right) = \tan^{-1} \left( \frac{-\omega^2 C R^2}{1 + (\omega R C)^2} \cdot \frac{1 + (\omega R C)^2}{R} \right)$$

$$= \tan^{-1}(-\omega R C) = -51.4^\circ$$