

# Optics and Waves

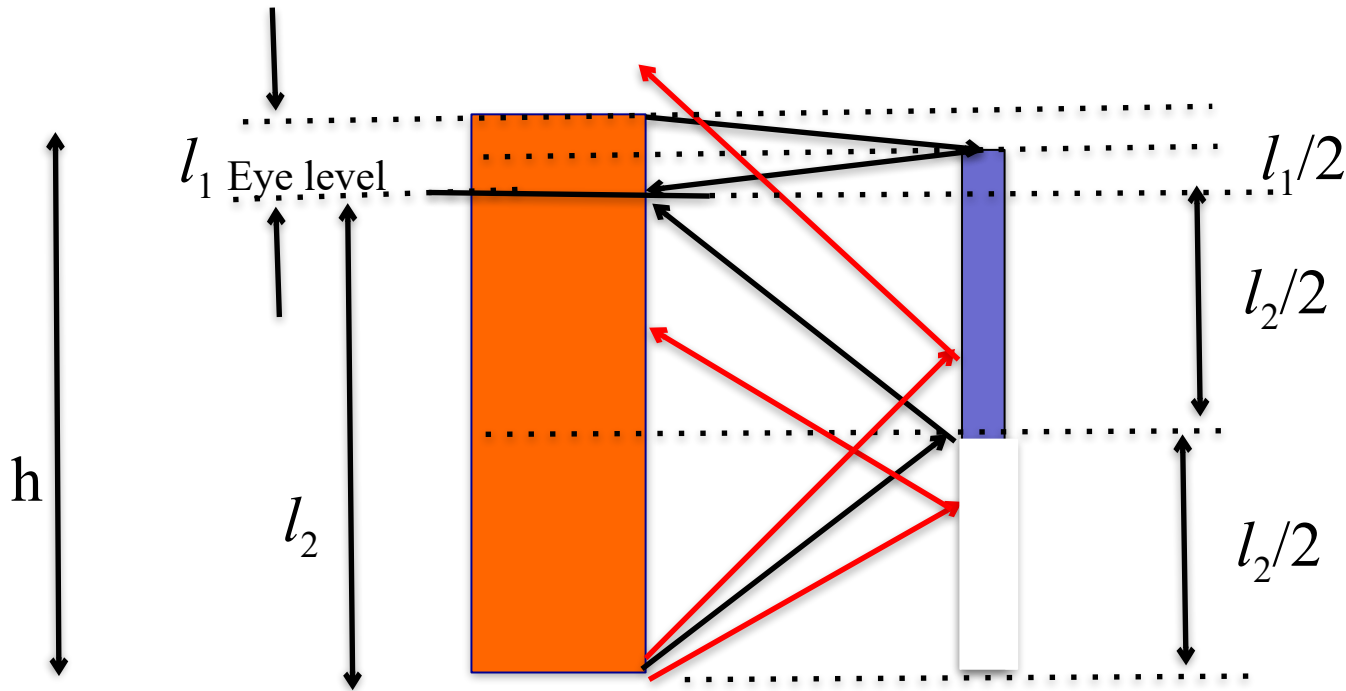
## Lecture 11

Reflection and Refraction  
(Cont.)  
Examples

## Choose the mirror



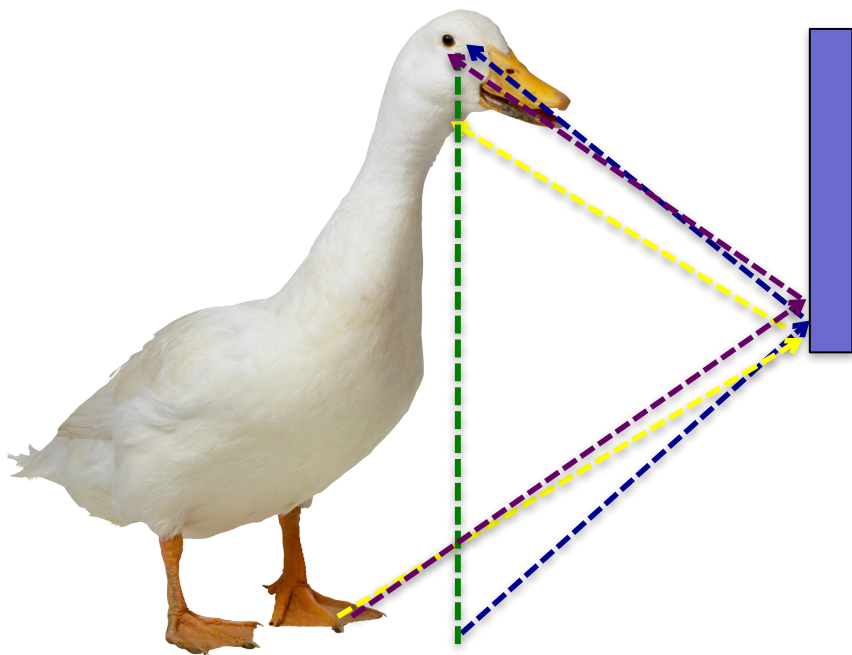
The man, standing in front of a mirror, is  $h$  meters high. What is the minimum height of the mirror if he wants to see a full image of himself?



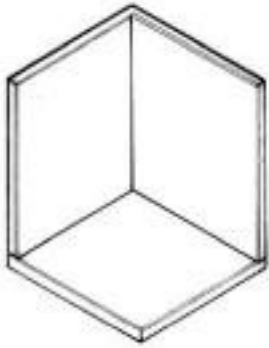
The minimum height of the mirror should be:

$$l_1/2 + l_2/2 = (l_1 + l_2)/2 = h/2$$

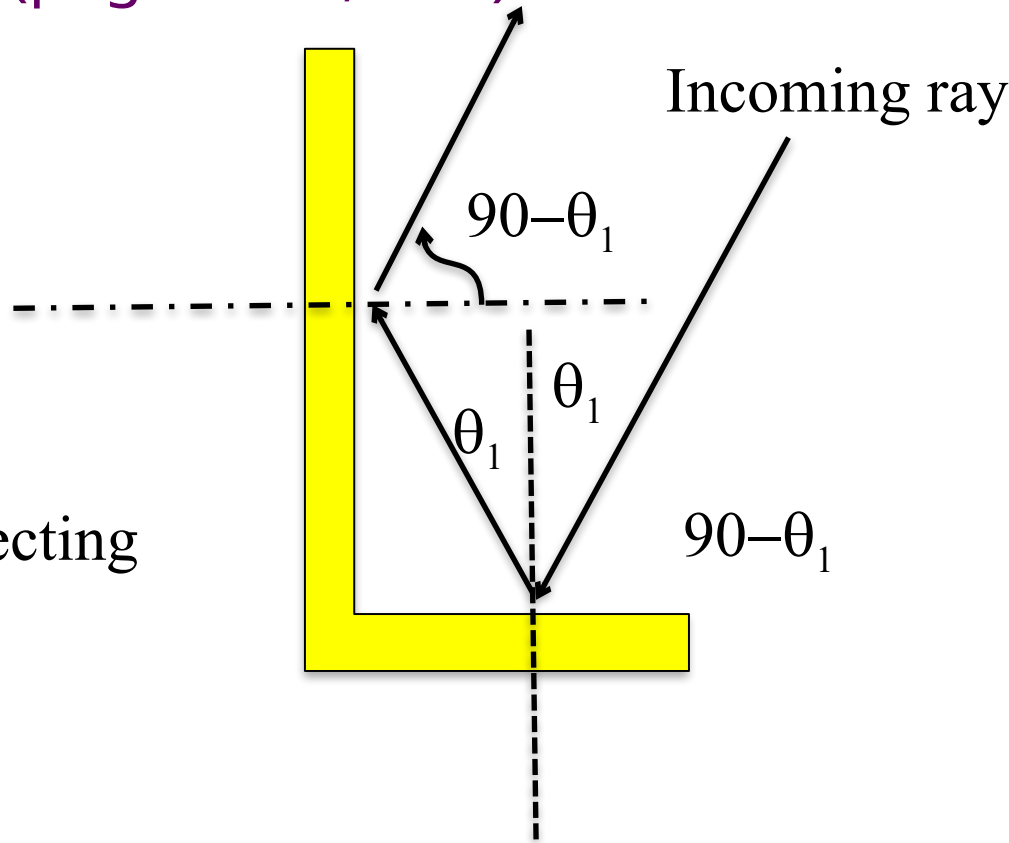
Top of the mirror half way between eye level and top of the head.



## Corner cube reflector (page 1088, Y&F)



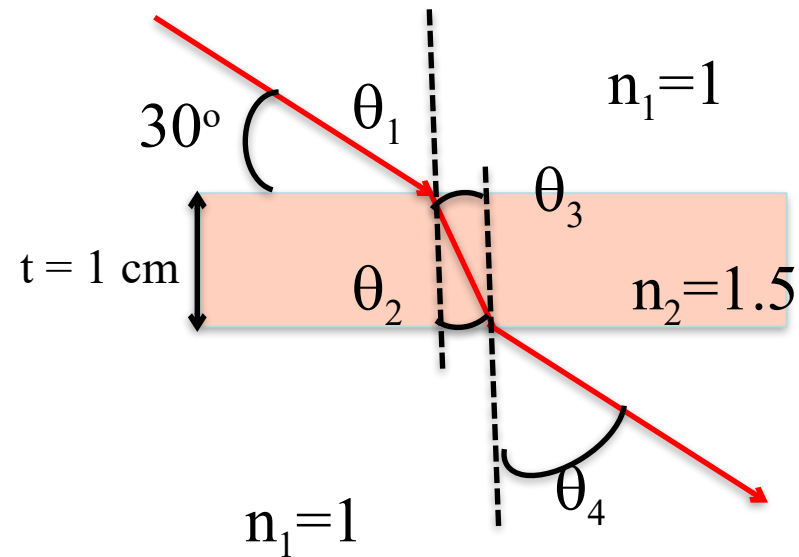
Three mutually orthogonal reflecting surfaces.



The ray is reflected twice:  
Once at each mirror.

Reflected ray travels in the opposite direction of the incoming ray.  
Compare this with a plane mirror.

## Light travelling through a piece of glass



$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\theta_2 = \sin^{-1}\left(\frac{n_1 \sin \theta_1}{n_2}\right) = 35.3^\circ$$

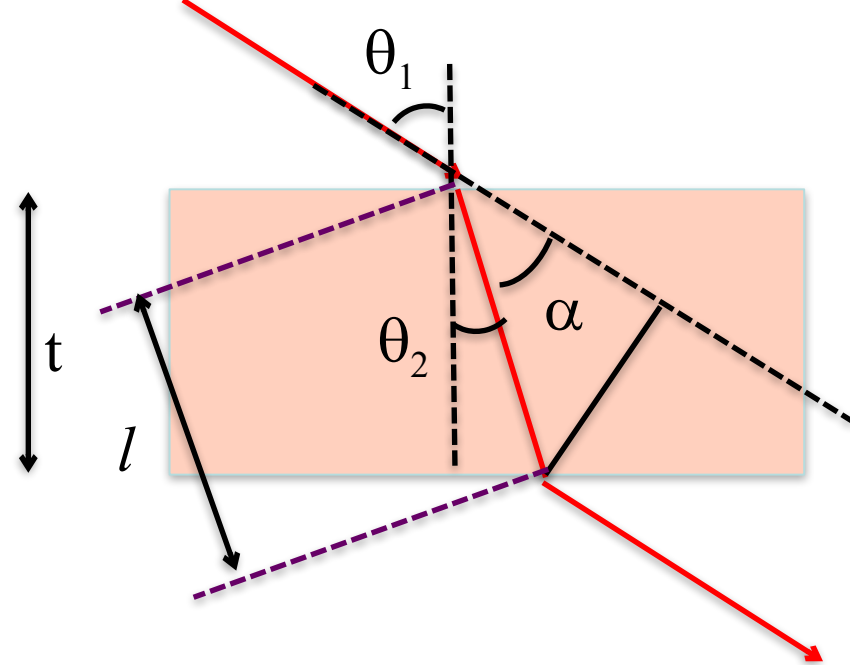
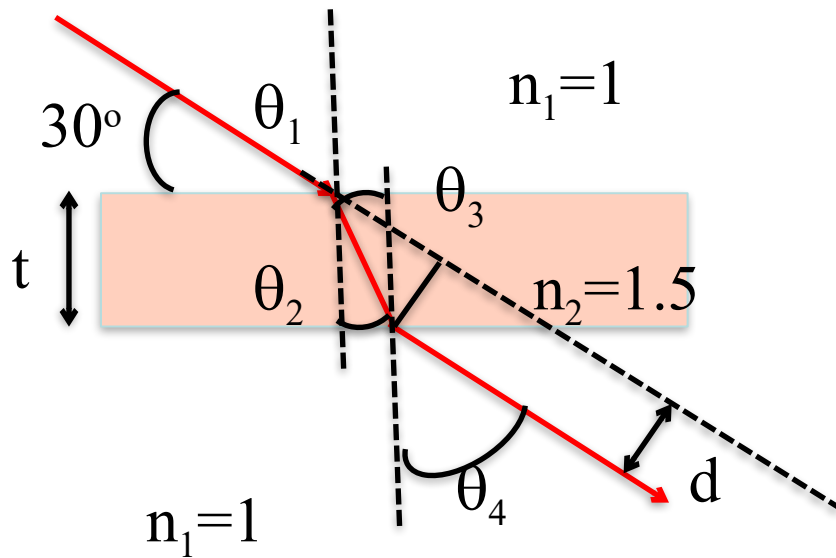
$$n_2 \sin \theta_3 = n_1 \sin \theta_4$$

$$\theta_2 = \theta_3$$

$$\theta_4 = \sin^{-1}\left(\frac{n_2 \sin \theta_3}{n_1}\right) = 60^\circ$$

The outgoing beam travels in the same direction as the original incoming beam, (independent of thickness of glass), but it is displaced.

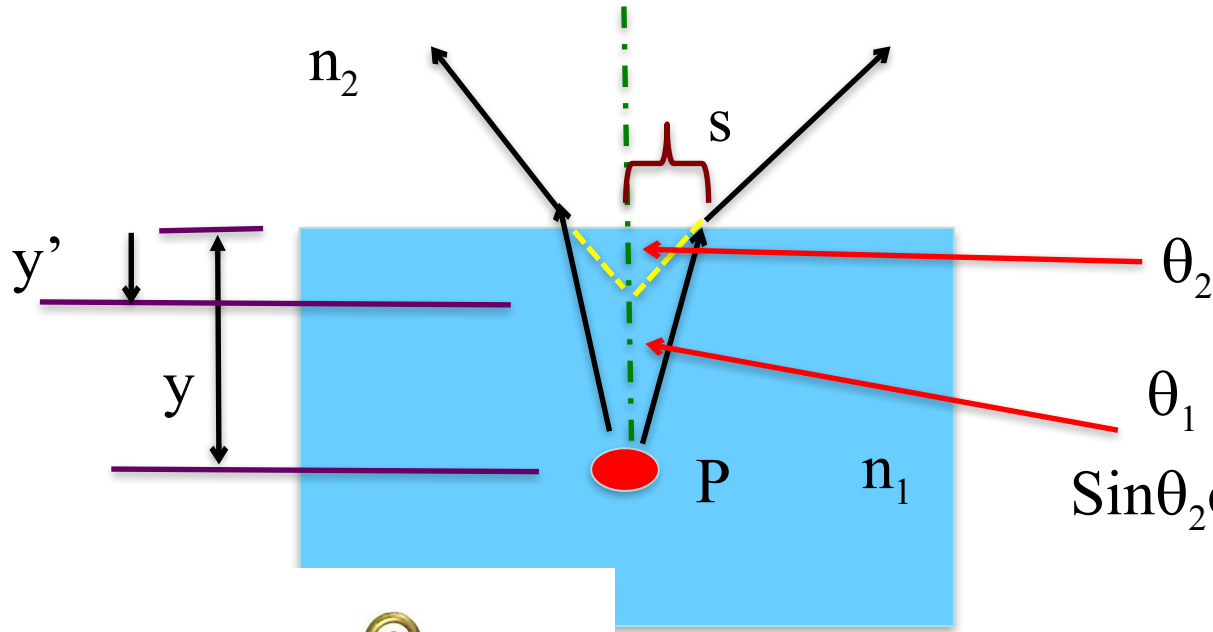
To find the displacement  $d$ :



$$d = l \sin \alpha = l \sin(\theta_1 - \theta_2)$$

$$= \frac{t}{\cos \theta_2} \sin(\theta_1 - \theta_2) = 0.51 \text{ cm}$$

# Apparent depth of an object



$$\tan\theta_2 = s/y'$$

$$\tan\theta_1 = s/y$$

$$\tan\theta_2 / \tan\theta_1 = y/y'$$

$$\frac{\sin\theta_2 \cos\theta_1}{\sin\theta_1 \cos\theta_2} = y/y'$$

For very small angles,  
 $\cos\theta_1 = \cos\theta_2 = 1$

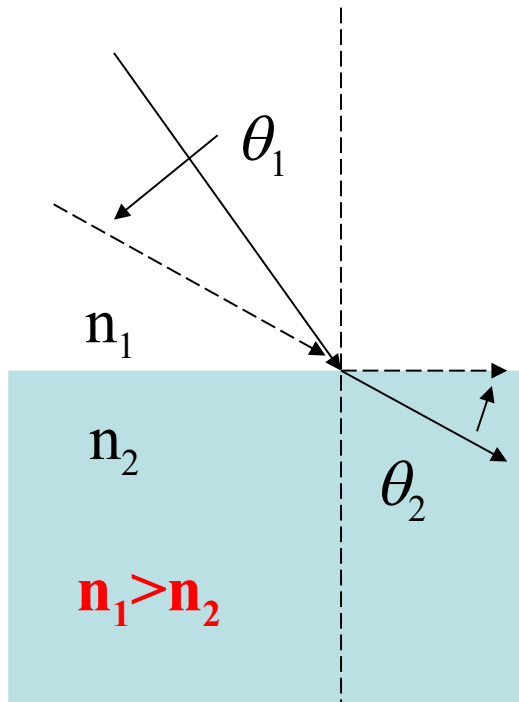
$$\frac{\sin\theta_2}{\sin\theta_1} = y/y' = n_1/n_2$$

$$y' = (n_2/n_1)y$$





# Total internal reflection



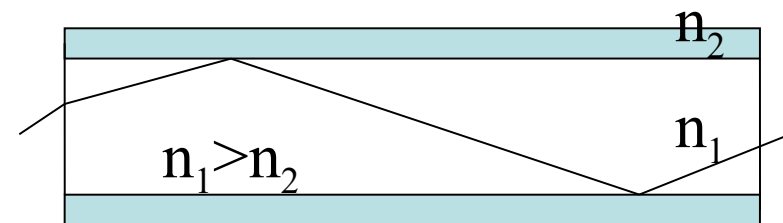
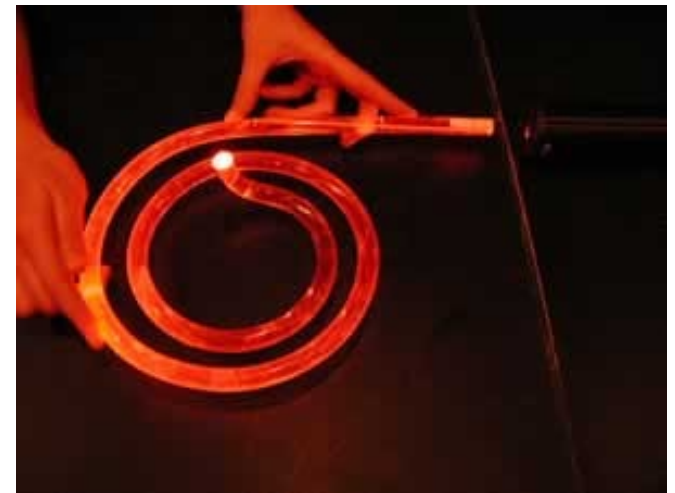
Snell's Law  $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$

when  $\theta_2 = \pi / 2$   $n_1 \sin(\theta_1) = n_2$

i.e.

$\sin(\theta_c) = n_2 / n_1$  ( $\theta_c = 48.6^\circ$  for water to air)

$\theta_c$  is called the critical angle



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