

ec_na_week1_b_a SOLUTIONS

1. (a) Find the equivalent resistance of the parallel combination of two $8\ \Omega$ resistors.

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2} = \frac{8 \times 8}{8 + 8} = \frac{64}{16} = 4\ \Omega$$

Find the equivalent resistance of the resulting parallel combination.

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2} = \frac{(16+8) \cdot (4+8)}{(16+8) + (4+8)} = \frac{24 \cdot 12}{24+12} = \frac{288}{36} = 8\ \Omega$$

- (b) If the potential difference between a and b is 16 V , the total current is

$$I = \frac{V}{R_{eq}} = \frac{16}{8} = 2\text{ A}$$

The current in each branch may be found using the current splitter theorem.

$$I_A = I \frac{R_2}{R_1 + R_2} = 2 \frac{(4+8)}{(4+8) + (16+8)} = 2 \frac{12}{36} = \frac{2}{3}\text{ A}$$

Therefore, the current series combination of a $16\ \Omega$ resistor and a $8\ \Omega$ resistor is $2/3\text{ A}$.

$$I_2 = I \frac{R_1}{R_1 + R_2} = 2 \cdot \frac{(16+8)}{(4+8) + (16+8)} = 2 \cdot \frac{24}{36} = \frac{4}{3}\text{ A}$$

or applying Kirchhoff's current law at node a

$$I_2 = I - I_1 = 2 - \frac{2}{3} = \frac{4}{3}\text{ A}$$

Therefore the current through the series $8\ \Omega$ resistor is $4/3\text{ A}$. Since the current is split equally by the parallel combination of two $8\ \Omega$ resistors, the current in each of the resistors is $2/3\text{ A}$.