

# INTRODUCTORY GUIDE TO MESSAGE PASSING IN DISTRIBUTED SYSTEMS

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## Abstract

Message passing in distributed systems is a model to exchange messages within a process pair by making use of several standards and implementation details. Those have been developed to offer the right message passing models for the different areas of applications. The programming language Erlang natively supports an asynchronous message passing model which makes the implementation of concurrent applications transparent to the software developer.

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# 1 MESSAGE ORIENTED COMMUNICATION

## 1.1 INTRODUCTION

Communication in distributed systems defines a distributed system itself: N systems execute one or more tasks by computing and communicating with each other. Every time systems shall communicate with each other to provide services, a proficient communication model has to be implemented. There are several models of communication in distributed systems such as Remote Procedure Calls (RPC) or object method invocation (Tanenbaum & Steen, 2007, chap. 4.3 / p. 203). With this paper I'll introduce you to the message passing model in distributed systems.

As human beings we already have a deep understanding of different models of message passing. While you read these words, I am passing a message to you, which seems to be a trivial thing to people who can read. In more philosophical terms, now that you are reading those words, a message is being passed from one entity (me, the writer) to another entity (you, the reader) which is obviously non trivial considering all the assumptions we would have to make to actually realize this message passing model between human beings.

Message passing in distributed systems is based on messages, composed of bit strings, exchanged within a process pair - which would be the equivalent to the entity pair. It is important to understand that message passing is a model designed for Inter-Process Communication (IPC). Whether those processes are located on one or on two systems, is irrelevant to the provided functionality.

## 1.2 REQUIREMENTS IN THEORY

The following items are the theoretical basic requirements for a system to provide the functionality of message passing:

- **Connectivity:** A connection to communicate has to be established between the process pair
- **Ability:** Each process has to be able to receive or send messages
- **Integrity:** Sent messages have to be delivered as is
- **Intelligibility:** The receiving process has to be able to interpret the message as intended
- **Executability:** The delivered message has to lead to an execution of the desired instructions

### 1.3 REQUIREMENTS PROVIDER IN PRACTICE

To provide the above mentioned requirements there have been developed several message passing models resulting in well defined standards and concrete implementations in the last decades. To facilitate understanding the relations between the theoretical requirements and a concrete implementation, I will choose the Transmission Control Protocol / Internet Protocol (TCP/IP) which uses several socket primitives as example (Tanenbaum & Steen, 2007, chap 4.3.1 on p. 141 - 142):

- **Connectivity:** TCP/IP provides the *Socket* primitive to create that end point and also the *Bind* primitive to bind a local address to that socket. The *Connect* primitive then provides the functionality to establish a connection.
- **Ability:** TCP/IP provides the two primitives *Send* and *Receive* to simply send and receive data via the connection.
- **Integrity:** TCP/IP provides several mechanisms to ensure that there has been no data loss when sending or receiving messages. On the other hand this makes the protocol slower than other protocols such as the Real-Time Transport Protocol (RTP) or the User Datagram Protocol (UDP).

The requirements of **Intelligibility** and **Executability** do not come under the area of responsibility of TCP/IP and thus other standards have to take place, such as Extensible Markup Language (XML) or JavaScript Object Notation (JSON) to structure the messages in a standardized manner, and the message parsing implementation to call the desired instructions.

There are other socket primitives than the above mentioned to provide the functionality of TCP/IP (Tanenbaum & Steen, 2007, ch. 4.3.1 on p. 141). The referenced book (Tanenbaum & Steen, 2007) provides useful and valuable information on this topic.

It is also important to understand that this was just a round-up of how one can make basic use of the socket primitives to implement message passing in an application. There is plenty to discuss about how message passing is realized, such as the Open Systems Interconnection Reference Model (OSI) which was developed by the International Organization for Standardization (ISO) to model the different layers of network oriented communication (Tanenbaum & Steen, 2007, ch. 4.1.1 on p. 116). Furthermore, the Operating System (OS) has to reserve local memory to provide a buffer for the in- and outgoing messages.

### 1.4 ASYNCHRONOUS VS. SYNCHRONOUS MESSAGE PASSING

After discussing a protocol to handle the socket primitives, it is necessary to consider one major difference in message passing models, which is whether

to use asynchronous or synchronous message passing. Passing a message synchronously means that the called message send routine returns after the request has been successfully transmitted (or an error occurred). Receiving a message synchronously means that the called message receiving routine reads a specific amount of bytes from the socket and returns that message.

To pass or receive a message asynchronously, another application layer i.e. middleware has to take place. The call of a send routine can either return when the middleware took over the transmission of the request, or when it successfully sent the request to the receiver, or when it successfully sent the request to the receiver, assuring this by a corresponding message (Tanenbaum & Steen, 2007, ch. 4.1 on p. 125).

The middleware can also perform some preparatory work e.g. separating stand-alone request bit strings and parsing them into a data structure and returning it when calling the receive routine of the message passing middleware.

One key model to provide such middleware functionalities are message queues. A message queue is a queue to store messages by the First In - First Out (FIFO) principle. This enables the application to asynchronously send and receive messages by offering an incoming message queue and an outgoing message queue. This makes all the send and receive mechanisms fully transparent to the application (Tanenbaum & Steen, 2007, ch. 4.3.2 on p. 145 - 147).

## **2 DEFINITION OF MESSAGE PASSING IN DISTRIBUTED SYSTEMS**

*Message passing in distributed systems is a model to exchange messages within a process pair by making use of several standards and implementation details. The specifically used message passing model can diverge extremely in its provided functionality and defines how to provide the connection and send or receive messages whereas the physical conditions and the implementation of executing the desired instructions is undefined.*

## **3 MESSAGE-PASSING INTERFACE STANDARD**

The Message-Passing Interface (MPI) is a message-passing library interface specification, made for high performance and scalable distributed systems where high-efficiency is needed. The MPI standard was designed by the Message-Passing Interface Forum (MPIF) which is an open group with representatives from many organizations. The current version of the MPI standard is MPI-3.0 (Message Passing Interface Forum, 2012, ch. Abstract/ii & Acknowledge-

ments/xx & 1.1 on p. 1).

The MPIF aims to offer a standard which establishes a practical, portable, efficient and flexible way of implementing message-passing in various high-level programming languages (e.g. C, C++, Fortran) (Message Passing Interface Forum, 2012, ch. History/iii). Furthermore, the MPI simplifies the communication primitives and brings them to an abstraction level to perfectly fit the programmer's needs of writing efficient and clean code for such distributed systems (Tanenbaum & Steen, 2007).

TCP/IP does not fit those requirements. While the socket primitives *read* and *write* are sufficient for several general-purpose protocols, (managing the communication across networks) they are insufficient for high-speed interconnection networks such as super computers or server clusters. The MPI standard offers a set of functions and datatypes with which the software developer is able to explicitly execute synchronous and asynchronous message passing routines (Tanenbaum & Steen, 2007, ch. 4.3 on p. 143).

## 4 MESSAGE PASSING IN ERLANG

### 4.1 Introduction

Erlang is a functional, declarative programming language that was written for the need of real-time, non-stop, concurrent, very large and distributed system applications (Armstrong, 1996, chap. 1 / p. 1). While the language was originally designed by Joe Armstrong, Robert Virding and Mike Williams for Ericsson (a Swedish telecommunications provider) in 1986, it finally became open source in 1998, thanks to the open source initiatives lead by Linux (Däcker, 2000, chap. 8 on p. 39).

Joe Armstrong, who started to design Erlang by adding functionality to Prolog, named it after the Danish mathematician Agner Krarup Erlang (creator of the Erlang loss formula) following the tradition of naming programming languages after dead mathematicians (Däcker, 2000, chap. 4.1 on p. 13).

Erlang uses a native, asynchronous message passing model to communicate between light weight processes, also called actors (Armstrong, 1996, chap. 1 on p. 1). Erlang does not make heavy use of the executing OS to provide the described concurrency model which implicitly means that Erlang decouples the underlying OS and thus providing a cross-platform and transparent message passing model (Armstrong, 1996, chap. 1 & 3 on p. 1 - 3).

## 4.2 Concurrency in Erlang

Erlang provides semantics and built-in functions to parallelize applications by message passing (Ericsson AB, 2015, ch. 4.3 on p. 95 - 104):

- `spawn(Module, Exported Function, List of Arguments)`  
Function which creates a new actor by running the *Exported Function* with the *List of Arguments* located in the *Module* (a set of functions located in one file) and which returns the Process Identifier (pid), which uniquely identifies the created actor.
- The `receive` construct allows the function executed by an actor to receive messages by using a message queue.
- The `!` operator sends the right-handed term to the left handed pid. The right-handed term is the sent message.
- `self()`  
Function that returns the pid of the actor executing the function.

Although the semantics and functions described above require a little knowledge on the Erlang programming language, it was important for me to show that Erlang is not only offering an easily intelligible interface for concurrency, it rather is a concurrent functional programming language. I recommend to take a look at the referenced official Erlang documentation or to *learn you some Erlang* on [www.learnyousomeerlang.com](http://www.learnyousomeerlang.com).

## 4.3 Implementation of a Simple Diffie-Hellman Key Exchange in Erlang

The following implementation of a Diffie-Hellman key exchange algorithm in Erlang is simplified. Please note that this Erlang application is not in any way acceptable as an adequate implementation of the Diffie-Hellman key exchange algorithm for use in the field! The code demonstrates the simplicity of implementing concurrent applications in Erlang by using message passing. You can find the code on Github:

[https://github.com/c-bebop/message\\_passing](https://github.com/c-bebop/message_passing)

and is licensed under the MIT License. You're welcome to contribute!

```
1 %%% @author      Florian Willich
2 %%% @copyright   The MIT License (MIT) Copyright (c) 2014
3 %%%              University of Applied Sciences, Berlin, Germany
4 %%%              Florian Willich
5 %%%              For more detailed information, please read the
6 %%%              licence.txt in the erlang root directory.
7 %%% @doc         This module represents a simple implementation of
8 %%%              the Diffie-Hellman key exchange algorithm and is
```

```

9 %%%          part of my technical report 'Introductory Guide
10 %%%          to Message Passing in Distributed Systems'.
11 %%% @end
12 %%% Created 2015-06-06
13
14 -module(diffie_hellman).
15 -author("Florian Willich").
16 -export([ computeMyPublicComponentKey/3,
17           computeSharedPrivateKey/3,
18           startKeyExchange/5,
19           listenKeyExchange/2,
20           startExample/0,
21           startRemoteExample/1,
22           startRemoteExample/5]).
23
24 %%% @doc Public data represents the data which is publicly shared
25 %%%       within two communication partners when exchanging keys
26 %%%       with the Diffie-Hellman key exchange algorithm.
27 %%%       p: The public prime number
28 %%%       g: The public prime number (1 ... p - 1)
29 %%%       componentKey: The computed component key
30 %%%       pid: The pid of the one who instantiated this record
31 %%%       name: The name of whom creates this public data.
32 -record(publicData, {p, g, componentKey, pid, name}).
33
34 %%% @doc Returns the value G to the power of MySecretKey Modulo P
35 %%%       which is the public component key for the Diffie-Hellman
36 %%%       key exchange algorithm.
37 %%%       For more information see http://goo.gl/pzdiH
38 %%% @end
39 -spec computeMyPublicComponentKey(pos_integer(), pos_integer(),
40                                   pos_integer()) -> pos_integer().
41 computeMyPublicComponentKey(P, G, MySecretKey) ->
42   my_math:pow(G, MySecretKey) rem P.
43
44 %%% @doc Returns the value ComponentKey to the power of
45 %%%       MySecretKey Modulo P which is the private
46 %%%       shared key for the Diffie-Hellman key exchange
47 %%%       algorithm.
48 %%%       For more information see http://goo.gl/pzdiH.
49 %%% @end
50 -spec computeSharedPrivateKey(pos_integer(), pos_integer(),
51                               pos_integer()) -> pos_integer().
52 computeSharedPrivateKey(P, ComponentKey, MySecretKey) ->
53   my_math:pow(ComponentKey, MySecretKey) rem P.
54
55 %%% @doc Starts the Diffie-Hellman key exchange algorithm by
56 %%%       taking P (a prime number), G (1 ... P - 1), MySecretKey
57 %%%       is the secret integer of the one who executes this
58 %%%       function and the PartnerPID which is the PID of the
59 %%%       communication partner with whom a key exchange shall be
60 %%%       initiated. MyName shall be the name of the executing
61 %%%       partner. This function sends the term
62 %%%       {startKeyExchange, PublicData} to the PartnerPID where
63 %%%       PublicData is of type publicData. Afterwards, the
64 %%%       function starts a receive construct which is receiving
65 %%%       the following:

```



```

64 %%%      {componentKey, PublicData}:
65 %%%          The message including all information needed for
66 %%%          computing the private shared key and then prints it
67 %%%          out.
68 %%%      UnexpectedMessage:
69 %%%          Prints out any unexpected incoming message and
70 %%%          calls a recursion.
71 %%%      After 3000 milliseconds:
72 %%%          The function will return timeout.
73 %%% @end
74 -spec startKeyExchange(pos_integer(), pos_integer(), pos_integer(),
    term(), string()) -> term() | {error, atom()}.
75 startKeyExchange(P, G, MySecretKey, PartnerPID, MyName) ->
76   MyComponentKey = computeMyPublicComponentKey(P, G, MySecretKey),
77   MyPublicData = #publicData{p = P, g = G, componentKey =
    MyComponentKey, pid = self(), name = MyName},
78   PartnerPID ! {startKeyExchange, MyPublicData},
79
80   receive
81
82     {componentKey, #publicData{p = P, g = G, componentKey =
    PartnerComponentKey, pid = PartnerPID, name = PartnerName}}
    ->
83       PrivateSharedKey = computeSharedPrivateKey(P,
    PartnerComponentKey, MySecretKey),
84       printSharedPrivateKey(self(), MyName, PartnerName,
    PrivateSharedKey);
85
86   UnexpectedMessage ->
87     printUnexpectedMessage(UnexpectedMessage),
88     startKeyExchange(P, G, MySecretKey, PartnerPID, MyName)
89
90   after 3000 ->
91     {error, timeout_after_3000_ms}
92
93   end.
94
95 %%% @doc Listens on Messages to start the Diffie-Hellman key
96 %%% with the transferred MySecretKey and MyName
97 %%% which shall be the name of the executing partner.
98 %%% exchange by starting the following receive construct:
99 %%% {startKeyExchange, PublicData}:
100 %%%     The message including all information needed to
101 %%%     start the key exchange by computing the own public
102 %%%     data which will then be send to the PartnerPID as
103 %%%     follows: {componentKey, MyPublicData}.
104 %%%     Afterwards, the private shared key will be printed
105 %%%     out and the function calls a recursion.
106 %%% terminante:
107 %%%     Prints out that this function terminates with the
108 %%%     executing PID and returns ok.
109 %%% UnexpectedMessage:
110 %%%     Prints out any unexpected incoming message and
111 %%%     calls a recursion.
112 %%% @end
113 -spec listenKeyExchange(pos_integer(), string()) -> term().
114 listenKeyExchange(MySecretKey, MyName) ->

```

```

115 receive
116
117     {startKeyExchange, #publicData{p = P, g = G, componentKey =
        PartnerComponentKey, pid = PartnerPID, name = PartnerName}}
        ->
118     MyComponentKey    = computeMyPublicComponentKey(P, G,
        MySecretKey),
119     MyPublicData      = #publicData{p = P, g = G, componentKey =
        MyComponentKey, pid = self(), name = MyName},
120     PartnerPID ! {componentKey, MyPublicData},
121     PrivateSharedKey = computeSharedPrivateKey(P,
        PartnerComponentKey, MySecretKey),
122     printSharedPrivateKey(self(), MyName, PartnerName,
        PrivateSharedKey),
123     listenKeyExchange(MySecretKey, MyName);
124
125 terminate ->
126     io:format("~p terminates!~n", [self()]),
127     ok;
128
129 UnexpectedMessage ->
130     printUnexpectedMessage(UnexpectedMessage),
131     listenKeyExchange(MySecretKey, MyName)
132
133 end.
134
135 %%% @doc Prints out the UnexpectedMessage as follows:
136 %%% Received an unexpected message: 'Unexpected Message'
137 %%% @end
138 -spec printUnexpectedMessage(string()) -> term().
139 printUnexpectedMessage(UnexpectedMessage) ->
140     io:format("Received an unexpected message: ~p~n", [
        UnexpectedMessage]).
141
142 %%% @doc Prints out the shared private key as follows:
143 %%% 'MyName' ('PID'): The shared private Key,
144 %%% exchanged with 'PartnerName' is: 'SharedKey'
145 %%% @end
146 -spec printSharedPrivateKey(term(), string(), string(), string())
        -> term().
147 printSharedPrivateKey(PID, MyName, PartnerName, SharedKey) ->
148     io:format("~p (~p): The shared private Key, exchanged with ~p is:
        ~p~n", [MyName, PID, PartnerName, SharedKey]).
149
150 %%% @doc Starts a key exchange example by spawning the Alice
151 %%% process, which executes the listenKeyExchange function
152 %%% with MySecretKey = 15, and the Bob process, which
153 %%% executes the startKeyExchange function with P = 23,
154 %%% G = 5, MySecretKey = 6 and PartnerPID = Alice. Returns
155 %%% {Alice, Bob} (pids).
156 %%%
157 -spec startExample() -> term().
158 startExample() ->
159     Alice = spawn(diffie_hellman, listenKeyExchange, [15, "Alice"])
        ,
160     Bob   = spawn(diffie_hellman, startKeyExchange, [23, 5, 6,
        Alice, "Bob"]),

```

```

161 {Alice, Bob}.
162
163 %%% @doc Starts a key exchange remote example by spawning the
164 %%% Alice process, which executes the listenKeyExchange
165 %%% function with MySecretKey = 15, and the Bob process,
166 %%% located on the RemoteNode, which executes the
167 %%% startKeyExchange function with P = 23, G = 5,
168 %%% MySecretKey = 6 and Alice PID.
169 %%% Returns the pids of Alice and Bob.
170 %%% @end
171 -spec startRemoteExample(atom()) -> term().
172 startRemoteExample(RemoteNode) ->
173   Alice = spawn(RemoteNode, diffie_hellman, listenKeyExchange, [
174     15, "Alice"]),
175   Bob = spawn(diffie_hellman, startKeyExchange, [23, 5, 6,
176     Alice, "Bob"]),
177   {Alice, Bob}.
178
179 %%% @doc Starts a key exchange remote example by spawning the
180 %%% Alice process, which executes the listenKeyExchange
181 %%% function with AliceSecretKey, and the Bob process,
182 %%% located on the RemoteNode, which executes the
183 %%% startKeyExchange function with P, G,
184 %%% BobSecretKey and Alice PID.
185 %%% Returns the pids of Alice and Bob.
186 %%% @end
187 -spec startRemoteExample(atom(), pos_integer(), pos_integer(),
188   pos_integer(), pos_integer()) -> term().
189 startRemoteExample(RemoteNode, P, G, BobSecretKey, AliceSecretKey)
190 ->
191   Alice = spawn(RemoteNode, diffie_hellman, listenKeyExchange, [
192     AliceSecretKey, "Alice"]),
193   Bob = spawn(diffie_hellman, startKeyExchange, [P, G,
194     BobSecretKey, Alice, "Bob"]),
195   {Alice, Bob}.

```

## 4.4 Running the Simple Diffie-Hellman Key Exchange in Erlang

To run the applicatoin (4.3) in a Linux shell one shall do the following (assuming that Erlang is already installed, help can be found at [http://www.erlang.org/doc/installation\\_guide/INSTALL.html](http://www.erlang.org/doc/installation_guide/INSTALL.html)).

### 4.4.1 Preparatory Work

Open a Linux shell, go to the *source* directory of the Erlang code and type:

```
1 $ erl -sname bob
```

Which will output (meta data depends of the executing system):

```

1 Erlang/OTP 17 [erts-6.3] [source] [64-bit] [smp:4:4] [async-threads
  :10] [hipe] [kernel-poll:false]
2
3 Eshell V6.3 (abort with ^G)

```

```
4 (bob@localhost)1>
```

The option *-sname bob* tells the Erlang shell to run on a node called *bob*. First one shall compile the two modules and afterwards:

```
1 (bob@localhost)1> c(diffie_hellman).
2 {ok,diffie_hellman}
3 (bob@localhost)2> c(my_math).
4 {ok,my_math}
```

#### 4.4.2 Running the Application on One Node

Now execute the *startExample* function as follows:

```
1 (bob@localhost)3> diffie_hellman:startExample().
2 "Alice" (<0.50.0>): The shared private Key, exchanged with "Bob" is
   : 2
3 "Bob" (<0.51.0>): The shared private Key, exchanged with "Alice" is
   : 2
4 {<0.50.0>,<0.51.0>}
```

Executing the function *startExample* spawns a process that executes the *listenKeyExchange* function with 15 as the *private key* and "Alice" as the name and binds the returning pid to the value called Alice. Afterwards, *startExample* spawns another process that executes the *startKeyExchange* function with 23 for *P*, 5 for *G*, 6 for the *private key*, the pid of Alice and "Bob" as the name which binds the returning pid to the value called Bob. At the end the function returns the two pids of *Alice* and *Bob*. As we can see from the output, Alice has the pid <0.50.0> and the calculated private key, exchanged with Bob is 2. Bob has the pid <0.51.0> and has computed the same private key.

#### 4.4.3 Running the Application on Two Nodes

Now run the key exchange algorithm on two nodes. Open another shell, go to the *source* directory of the Erlang code and type:

```
$ erl -sname alice
```

Which will output (meta data depends of the executing system):

```
1 Erlang/OTP 17 [erts-6.3] [source] [64-bit] [smp:4:4] [async-threads
   :10] [hipe] [kernel-poll:false]
2
3 Eshell V6.3 (abort with ^G)
4 (alice@localhost)1>
```

This means we're now running another Erlang shell on the node *alice* (compile both files in the new Erlang shell, too). Now in the Erlang shell running the node *bob* execute the function *startRemoteExample* with the atom *alice@localhost* as the transferred parameter to specify on which node the actor shall be spawned that executes the *listenKeyExchange* function:

```
(bob@localhost)4> diffie_hellman:startRemoteExample(alice@localhost
).
```

This will output the following:

```
{<9879.54.0>,<0.58.0>}  
"Alice" (<9879.54.0>): The shared private Key, exchanged with "Bob"  
    is: 2  
"Bob" (<0.58.0>): The shared private Key, exchanged with "Alice" is  
    : 2
```

All transferred parameters are the same with the difference that the *Alice* actor is now located on the node *alice*. The output is still printed out in the *bob* node, since the Erlang io system recognizes where the process is spawned from and sends all the output there (Ericsson AB, 2015, ch. 4.3.4 on p. 104).

## A my\_math Erlang Module

```
1 %%% @author      Florian Willich
2 %%% @copyright   The MIT License (MIT) Copyright (c) 2014
3 %%%              University of Applied Sciences, Berlin, Germany
4 %%%              Florian Willich
5 %%%              For more detailed information, please read the
6 %%%              licence.txt in the erlang root directory.
7 %%% @doc         This is my math module for mathematical
8 %%%              functions not provided by the erlang standard
9 %%%              library.
10 %%% @end
11 %%% Created 2015-06-06
12
13 -module(my_math).
14 -author("Florian Willich").
15 -export([pow/2]).
16
17 %%% @doc Returns the value of Base to the power of Exponent.
18 %%%      If Base and Exponent is 0 the function returns
19 %%%      {error, undefined_arithmetic_expression},
20 %%%      The motivation to implement this function was that
21 %%%      there is no erlang standard library pow function
22 %%%      returning an integer.
23 %%% @end
24 -spec pow(integer(), integer()) -> number() | {error, atom()}.
25 pow(0, 0) ->
26     {error, undefined_arithmetic_expression};
27
28 pow(Base, 0) ->
29     case Base < 0 of
30         true -> -1;
31         false -> 1
32     end;
33
34 pow(Base, Exponent) ->
35     case Exponent < 0 of
36         true -> 1 / pow(Base, -Exponent, 0);
37         false -> pow(Base, Exponent, 0)
38     end.
39
40 %%% @doc Returns the value of Base to the power of Exponent.
41 %%%      Acc should be 0 for initiating computation.
42 %%%      The motivation to implement this function was that
43 %%%      there is no erlang standard library pow function
44 %%%      returning an integer.
45 %%% @end
46 -spec pow(pos_integer(), non_neg_integer(), non_neg_integer()) ->
47     integer().
48 pow(_, 0, Acc) -> Acc;
49
50 pow(Base, Exponent, 0) ->
51     pow(Base, Exponent - 1, Base);
52
53 pow(Base, Exponent, Acc) ->
54     pow(Base, Exponent - 1, Acc * Base).
```

## **B Acronyms**

### **Acronyms**

**FIFO** First In - First Out. 5

**IPC** Inter-Process Communication. 3

**ISO** International Organization for Standardization. 4

**JSON** JavaScript Object Notation. 4

**MPI** Message-Passing Interface. 5, 6

**MPIF** Message-Passing Interface Forum. 5, 6

**OS** Operating System. 4, 6

**OSI** Open Systems Interconnection Reference Model. 4

**pid** Process Identifier. 7, 12

**RPC** Remote Procedure Calls. 3

**RTP** Real-Time Transport Protocol. 4

**TCP/IP** Transmission Control Protocol / Internet Protocol. 3, 4, 6

**UDP** User Datagram Protocol. 4

**XML** Extensible Markup Language. 4

## References

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