

# 15-826: Multimedia Databases and Data Mining

Lecture #8: Fractals - introduction

C. Faloutsos



#### **Must-read Material**

 Christos Faloutsos and Ibrahim Kamel, <u>Beyond Uniformity and Independence:</u> <u>Analysis of R-trees Using the Concept of</u> <u>Fractal Dimension</u>, Proc. ACM SIGACT-SIGMOD-SIGART PODS, May 1994, pp. 4-13, Minneapolis, MN.

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#### **Recommended Material**

optional, but very useful:

- Manfred Schroeder Fractals, Chaos, Power Laws: Minutes from an Infinite Paradise
   W.H. Freeman and Company, 1991
  - Chapter 10: boxcounting method
  - Chapter 1: Sierpinski triangle

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#### **Outline**

Goal: 'Find similar / interesting things'

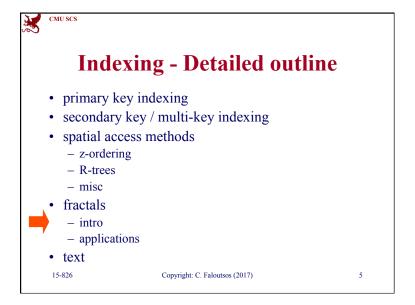
• Intro to DB

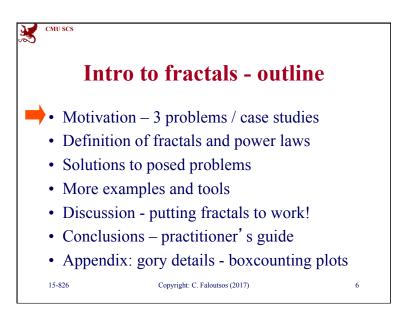


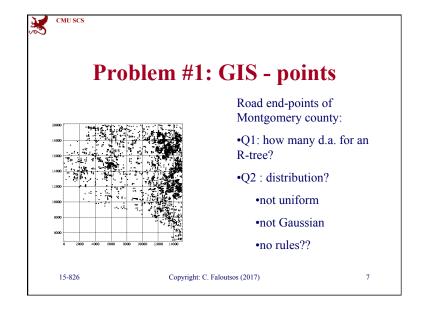
- Indexing similarity search
- Data Mining

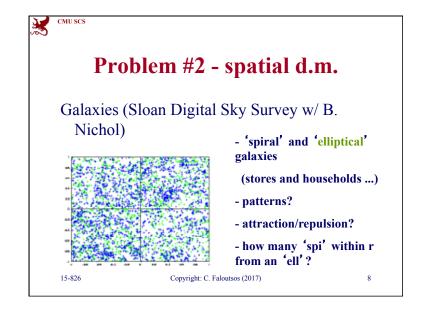
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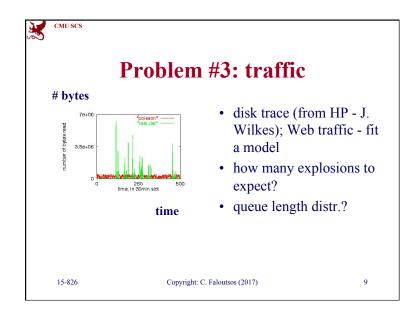
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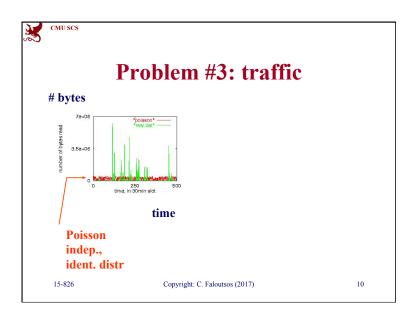


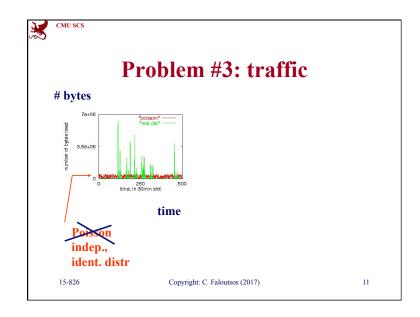


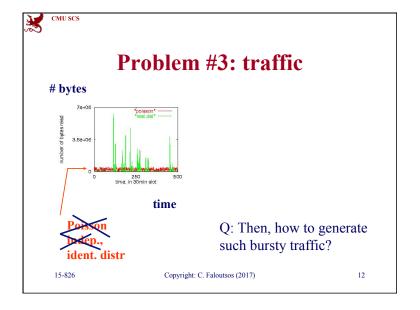














#### **Common answer:**

- Fractals / self-similarities / power laws
- Seminal works from Hilbert, Minkowski, Cantor, Mandelbrot, (Hausdorff, Lyapunov, Ken Wilson, ...)

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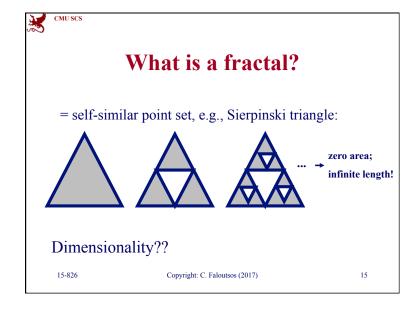


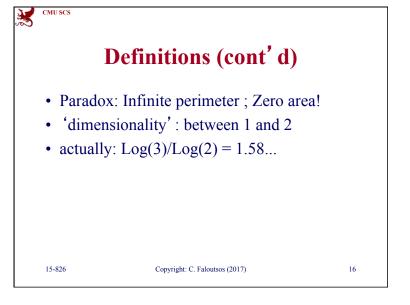
## Road map

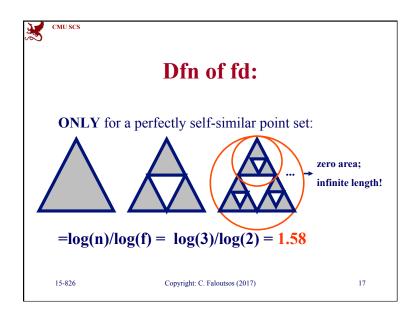
- Motivation 3 problems / case studies
- Definition of fractals and power laws
  - Solutions to posed problems
  - More examples and tools
  - Discussion putting fractals to work!
  - Conclusions practitioner's guide
  - Appendix: gory details boxcounting plots

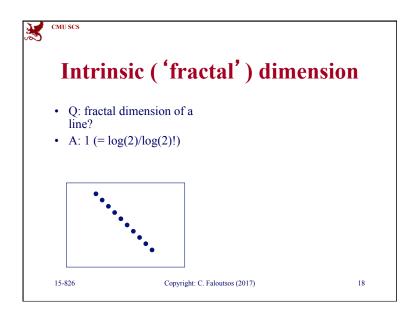
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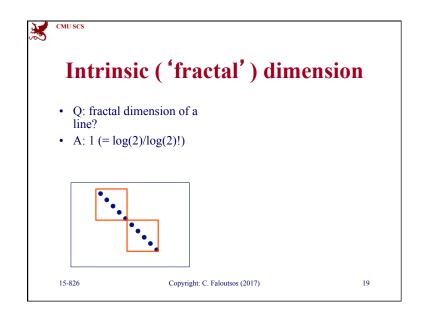
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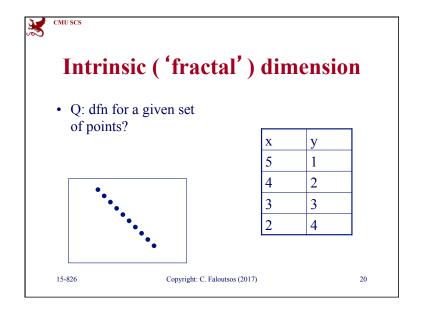


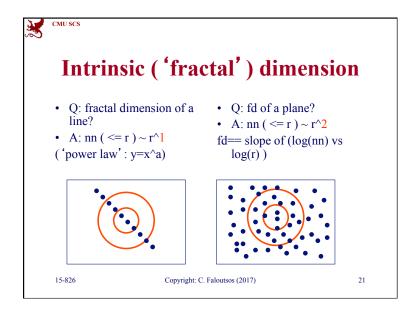


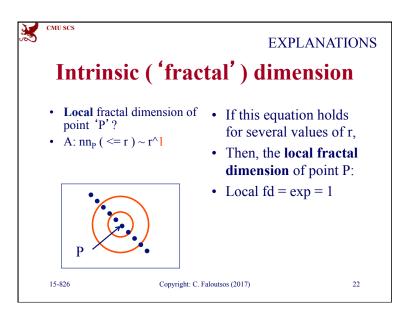


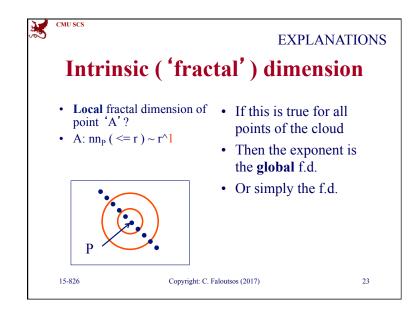


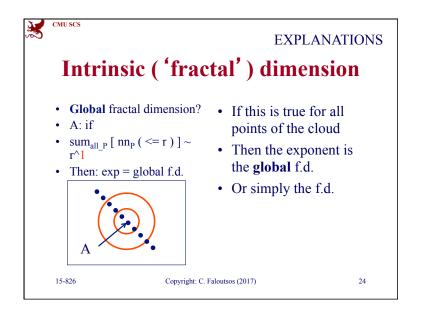














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**EXPLANATIONS** 

# Intrinsic ('fractal') dimension

• Algorithm, to estimate it?

Notice

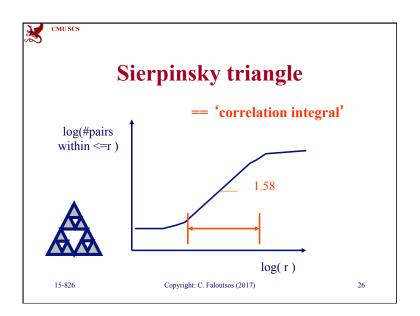
•  $Sum_{all\_P} [nn_P (\le r)]$  is exactly  $tot\#pairs(\le r)$ 

including 'mirror' pairs

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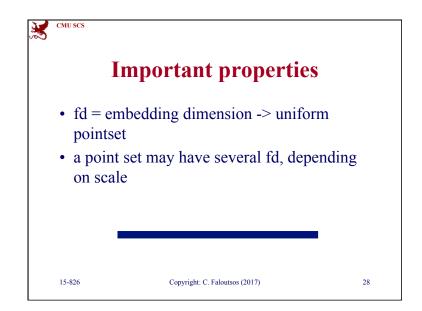
### **Observations:**

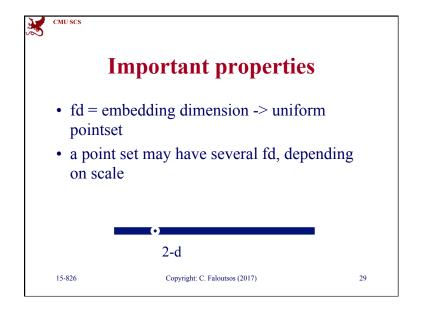
- Euclidean objects have **integer** fractal dimensions
  - point: 0
  - lines and smooth curves: 1
  - smooth surfaces: 2
- fractal dimension -> roughness of the periphery

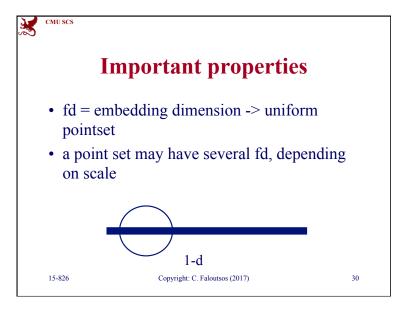
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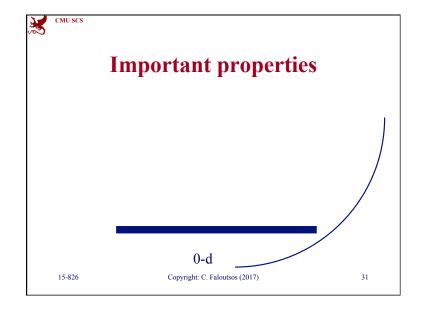
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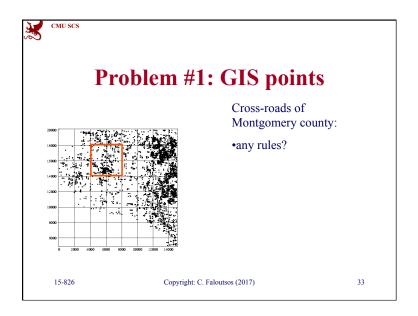


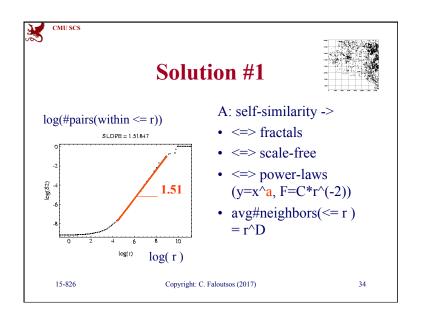


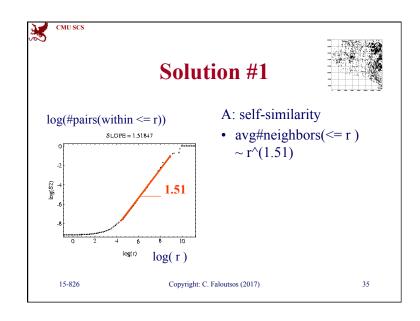


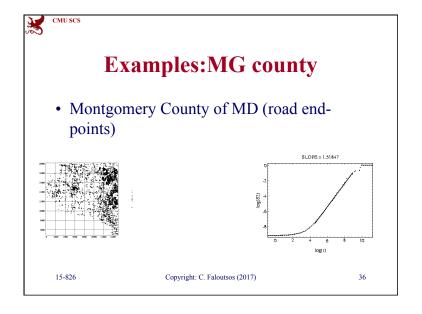


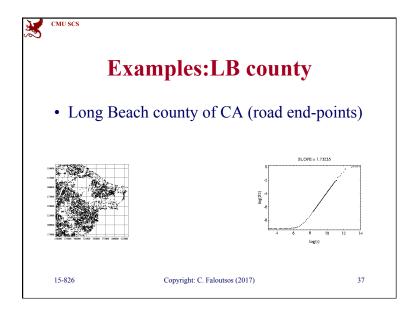


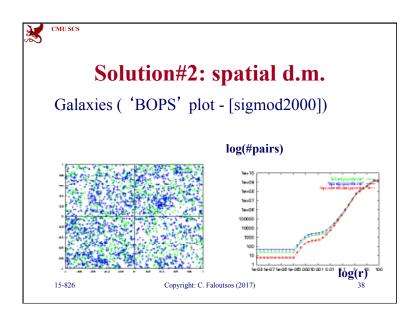


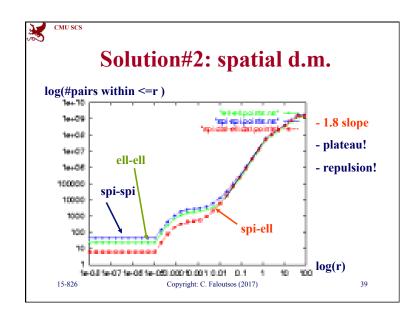


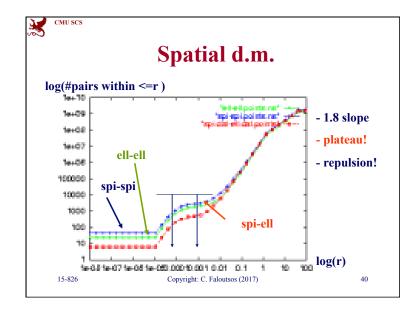


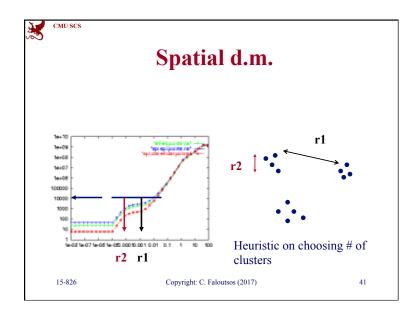


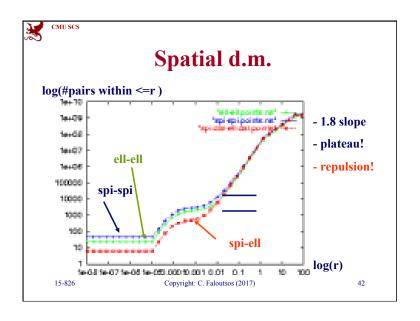


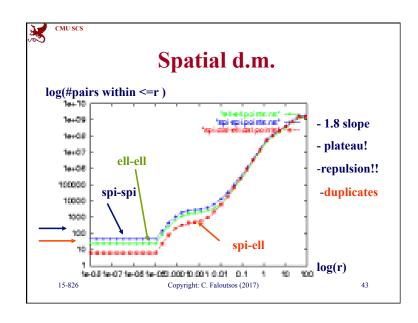


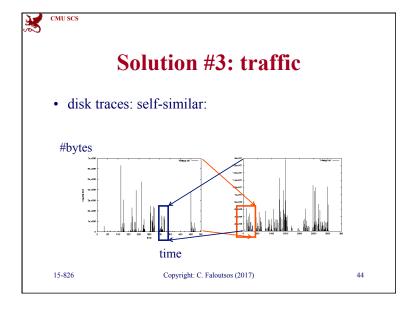


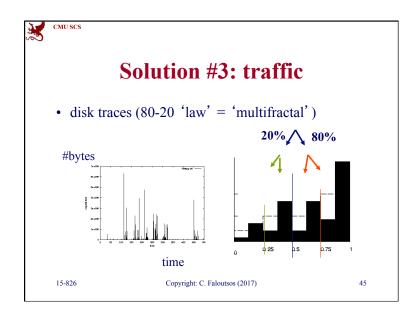


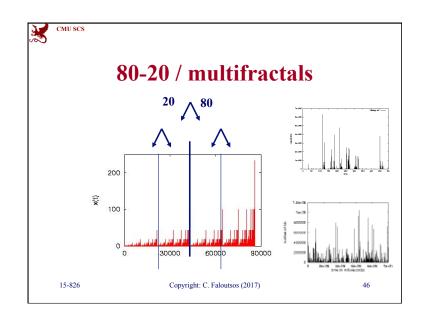


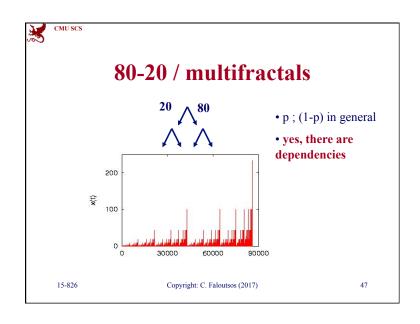


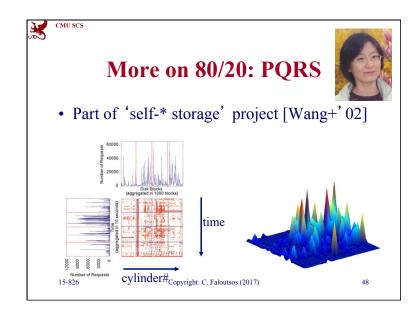


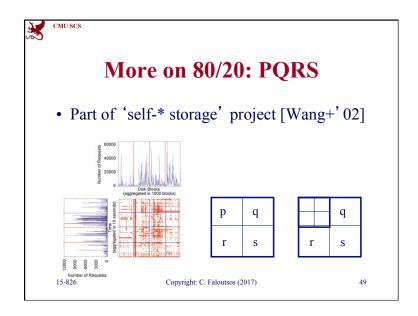


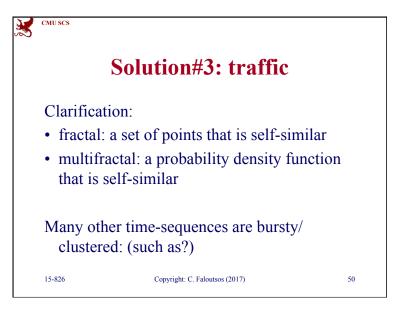


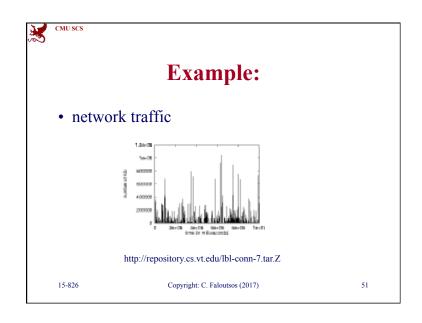


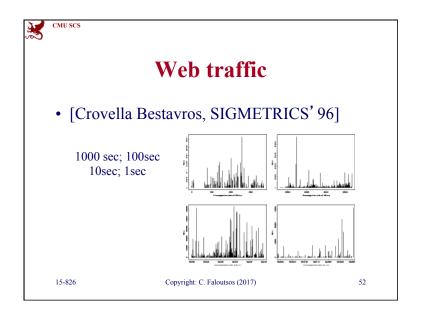


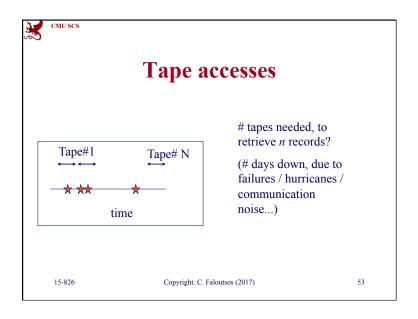


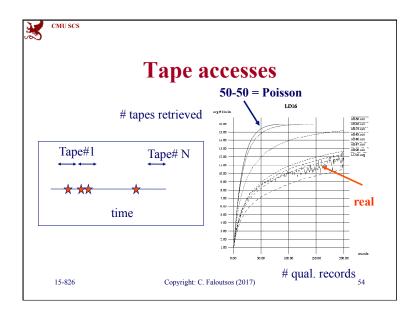




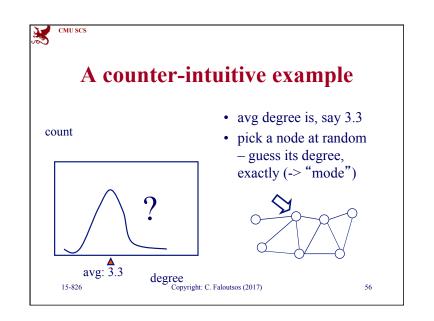


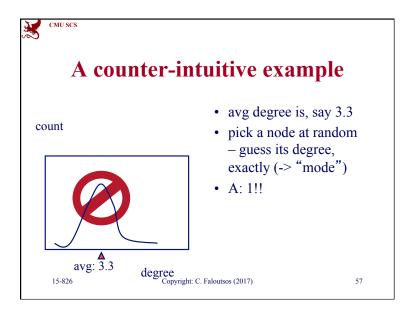


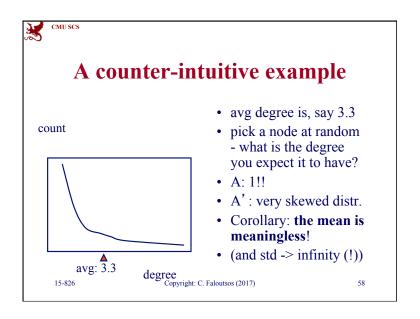


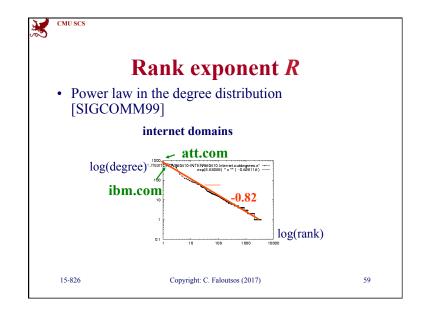




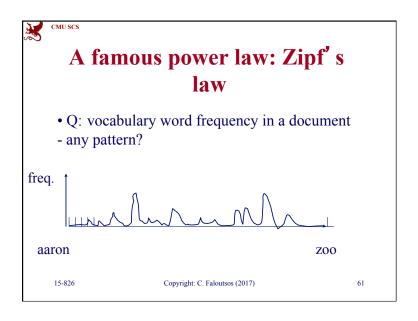


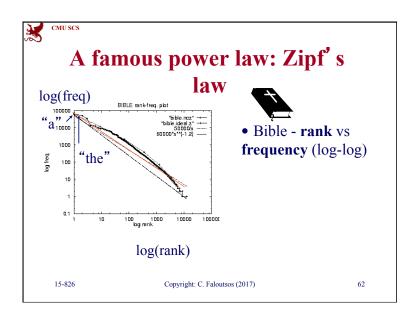


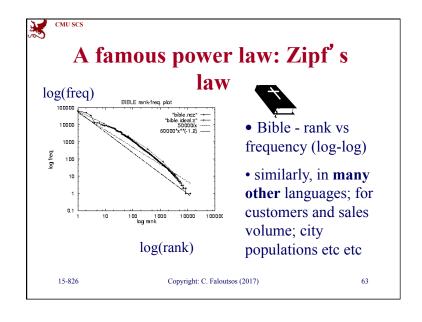


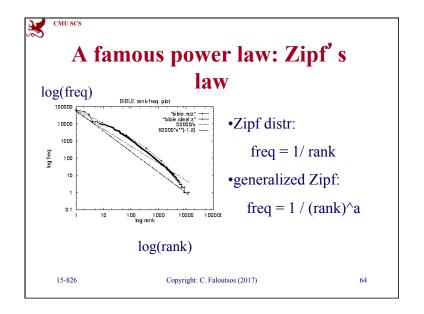


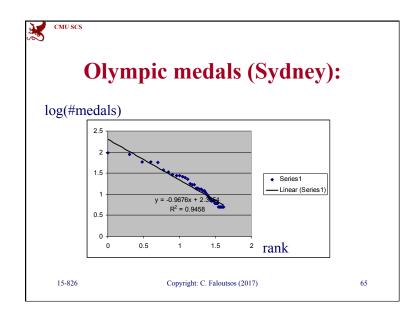


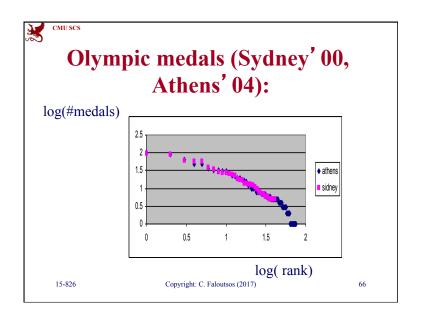


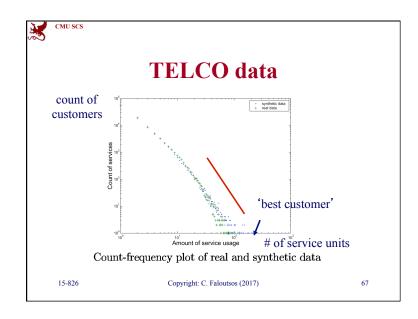


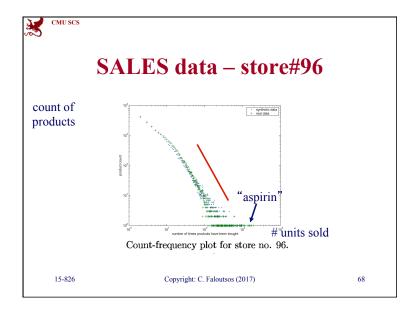


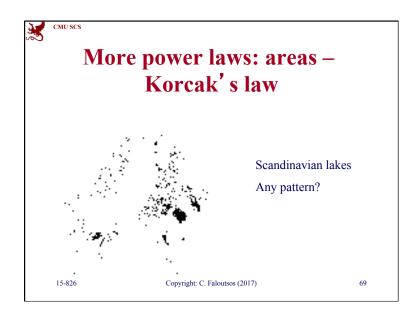


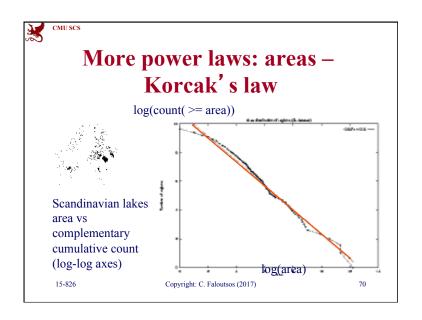


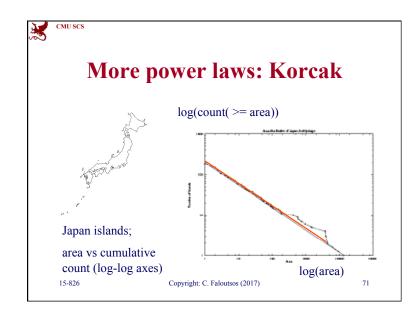




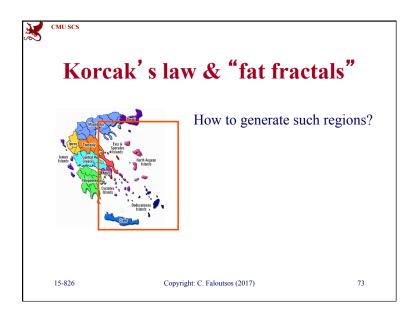


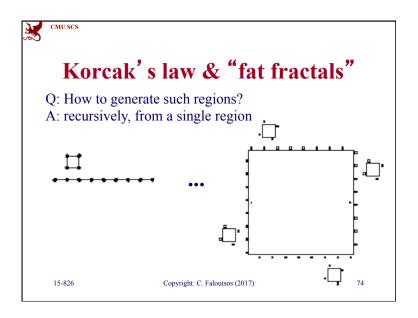


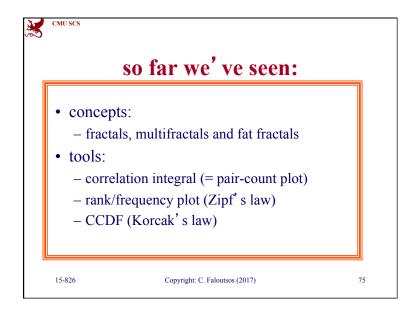


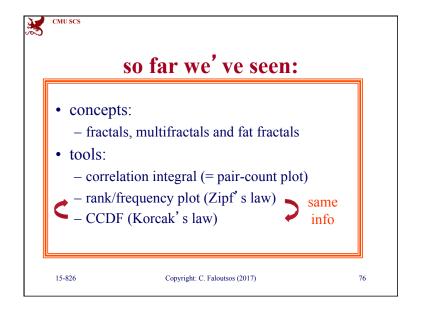














# **Next:**

- More examples / applications
- Practitioner's guide
- Box-counting: fast estimation of correlation integral

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