Announcements: projects

- -805 students: Project proposals are due Sun 10/2. If you'd like to work with 605 students then indicate this on your proposal.
- -605 students: the week after 10/2 I will post the proposals on the wiki and you will have time to contact 805 students and join teams.
- -805 students: let me know your team by 10/9: I will approve the teams.

Announcements: guinea pig tips

 One student reported localization problems that were fixed by setting

% export LC_ALL=C

-Try this out and let me know if there are problems with it: I will make it default for next class

Announcements: Spark followup

ReduceByKey is a **transformation**Reduce is an **action**

Sounds crazy but it's not:

- -actions are eager, and return something (small) to the driver program
- transformations are lazy, and transform a (large) RDD

LEARNING AS OPTIMIZATION: MOTIVATION

Learning as optimization: warmup

Goal: Learn the parameter θ of a binomial

Dataset: $D = \{x_1, ..., x_n\}$, x_i is 0 or 1, k of them are 1

$$P(X = x_i | \theta) = \theta^{x_i} (1 - \theta)^{1 - x_i}$$

- $\rightarrow P(D/\theta) = \theta^k (1-\theta)^{n-k}$
- → $d/d\theta P(D/\theta) = k\theta^{k-1}(1-\theta)^{n-k} + \theta^k(n-k)(1-\theta)^{n-k-1}$

$$\frac{\partial}{\partial \theta} P(D) = \theta^{k-1} (1 - \theta)^{n-k-1} \left(k(1 - \theta) - \theta(n - k) \right)$$

Learning as optimization: warmup

Goal: Learn the parameter θ of a binomial

Dataset: $D = \{x_1, ..., x_n\}$, x_i is 0 or 1, k of them are 1

$$\frac{\partial}{\partial \theta} P(D) = \theta^{k-1} (1 - \theta)^{n-k-1} \left(k(1 - \theta) - \theta(n - k) \right) = 0$$

$$\theta = 0$$

$$\theta = 1$$

$$k - k\theta - n\theta + k\theta = 0$$

$$\rightarrow n\theta = k$$

$$\rightarrow \theta = k/n$$

Learning as optimization: general procedure

- Goal: Learn parameter θ (or weight vector \mathbf{w})
- Dataset: $D = \{(x_1, y_1), ..., (x_n, y_n)\}$
- Write down loss function: how well w fits the data D as a function of w
 - -Common choice: $\log Pr(D|\mathbf{w})$
- Maximize by differentiating
 - -Then **gradient descent**: repeatedly take a small step in the direction of the gradient

Learning as optimization: general procedure for SGD (stochastic gradient descent)

- Big-data problem: we don't want to load all the data D into memory, and the gradient depends on all the data
- Solution:
 - pick a small subset of examples B<<D
 - approximate the gradient using them
 - "on average" this is the right direction
 - take a step in that direction
 - repeat....
- Math: find gradient of w for a single example, not a dataset

B = one example is a very popular choice

SGD vs streaming

- Streaming:
 - pass through the data once
 - hold model + one example in memory
 - update model for each example
- Stochastic gradient:
 - pass through the data multiple times
 - stream through a disk file repeatedly
 - hold model + B examples in memory
 - update model via gradient step

B = **one** example is a very popular choice

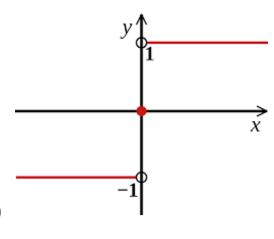
its simple ©

sometimes its cheaper to evaluate 100 examples at once than one example 100 times



Logistic Regression vs Rocchio

Rocchio looks like:



$$f(d) = \operatorname{argmax}_{y} \mathbf{v}(d) \cdot \mathbf{v}(y)$$

• Two classes, y=+1 or y=-1:

$$f(d) = \operatorname{sign}([\mathbf{v}(d) \cdot \mathbf{v}(+1)] - [\mathbf{v}(d) \cdot \mathbf{v}(-1)])$$

$$= \operatorname{sign}(\mathbf{v}(d) \cdot [\mathbf{v}(+1) - \mathbf{v}(-1)])$$

$$f(\mathbf{x}) = \operatorname{sign}(\mathbf{x} \cdot \mathbf{w}) \qquad w = \mathbf{v}(+1) - \mathbf{v}(-1)$$

$$\mathbf{x} = \mathbf{v}(d)$$

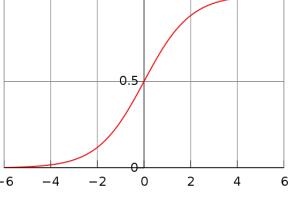
Logistic Regression vs Naïve Bayes

• Naïve Bayes for two classes can also be written as:

$$f(\mathbf{x}) = \operatorname{sign}(\mathbf{x} \cdot \mathbf{w})$$

 Since we can't differentiate sign(x), a convenient variant is a logistic function:

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$





Efficient Logistic Regression with Stochastic Gradient Descent

William Cohen

Learning as optimization for logistic regression

Goal: Learn the parameter w of the classifier

$$P(Y = y|X = \mathbf{x}, \mathbf{w}) = \frac{1}{1 + e^{-\mathbf{x} \cdot \mathbf{w}}}$$

Probability of a single example P(y|x,w) would be

$$P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \frac{1}{1 + e^{-\mathbf{x} \cdot \mathbf{w}}} & \text{if } y = 1\\ 1 - \frac{1}{1 + e^{-\mathbf{x} \cdot \mathbf{w}}} & \text{if } y = 0 \end{cases}$$

• Or with logs:

$$\log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \log p & \text{if } y = 1\\ \log(1 - p) & \text{if } y = 0 \end{cases}$$

$$p \equiv \frac{1}{1 + e^{-\mathbf{x} \cdot \mathbf{w}}} = \frac{1}{1 + \exp(-\sum_{j} x^{j} w^{j})}$$

$$\log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \log p & \text{if } y = 1\\ \log(1 - p) & \text{if } y = 0 \end{cases}$$

$$\frac{\partial}{\partial w^{j}} \log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \frac{1}{p} \underbrace{\frac{\partial}{\partial w^{j}} p}_{1-p} & \text{if } y = 1\\ \frac{1}{1-p} (-\frac{\partial}{\partial w^{j}} p) & \text{if } y = 0 \end{cases}$$

$$(\log f)' = \frac{1}{f} f'$$

$$p \equiv \frac{1}{1 + e^{-\mathbf{x} \cdot \mathbf{w}}} = \frac{1}{1 + \exp(-\sum_{j} x^{j} w^{j})}$$

$$p \equiv \frac{1}{1 + e^{-\mathbf{x} \cdot \mathbf{w}}} = \frac{1}{1 + \exp(-\sum_{j} x^{j} w^{j})}$$

$$1 - p = \frac{1 + \exp(-\sum_{j} x^{j} w^{j})}{1 + \exp(-\sum_{j} x^{j} w^{j})} - \frac{1}{1 + \exp(-\sum_{j} x^{j} w^{j})} = \underbrace{\frac{\exp(-\sum_{j} x^{j} w^{j})}{1 + \exp(-\sum_{j} x^{j} w^{j})}}_{\text{1 + exp}}$$

$$\frac{\partial}{\partial w^{j}} p = \frac{\partial}{\partial w^{j}} (1 + \exp(-\sum_{j} x^{j} w^{j}))^{-1} \qquad (e^{f})' = e^{f} f'$$

$$= (-1)(1 + \exp(-\sum_{j} x^{j} w^{j}))^{-2} \frac{\partial}{\partial w^{j}} \exp(-\sum_{j} x^{j} w^{j})$$

$$= (-1)(1 + \exp(-\sum_{i}^{j} x^{j} w^{j}))^{-2} \exp(-\sum_{i}^{j} x^{j} w^{j})(-x^{j})$$

$$= \underbrace{\frac{1}{1 + \exp(-\sum_{j} x^{j} w^{j})}}_{1 + \exp(-\sum_{j} x^{j} w^{j})} \underbrace{\frac{\exp(-\sum_{j} x^{j} w^{j})}{1 + \exp(-\sum_{j} x^{j} w^{j})}}_{x^{j}}$$

$$(-p)x^{j}$$

$$\log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \log p & \text{if } y = 1\\ \log(1 - p) & \text{if } y = 0 \end{cases}$$

$$\frac{\partial}{\partial w^{j}} \log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \frac{1}{p} \frac{\partial}{\partial w^{j}} p & \text{if } y = 1\\ \frac{1}{1 - p} (-\frac{\partial}{\partial w^{j}} p) & \text{if } y = 0 \end{cases}$$

$$\frac{\partial}{\partial w^{j}} p = p(1 - p) x^{j}$$

$$\frac{\partial}{\partial w^j} \log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \frac{1}{p} p(1 - p) x^j = (1 - p) x^j & \text{if } y = 1\\ \frac{1}{1 - p} (-1) p(1 - p) x^j = -p x^j & \text{if } y = 0 \end{cases}$$

$$\frac{\partial}{\partial w^j} \log P(Y = y | X = \mathbf{x}, \mathbf{w}) = (y - p)x^j$$

$$\mathbf{w}^{(t+1)} = \mathbf{w}^{(t)} + \lambda(y - p)\mathbf{x}$$

Again: Logistic regression

• Start with Rocchio-like linear classifier:

$$\hat{y} = sign(\mathbf{x} \cdot \mathbf{w})$$

- Replace sign(...) with something differentiable:
 - Also scale from 0-1 not-1 to +1

$$\hat{\mathbf{y}} = \sigma(\mathbf{x} \cdot \mathbf{w}) = p$$

$$\sigma(s) = \frac{1}{1 + e^{-s}}$$

$$0.8$$

$$0.5$$

$$0.2$$

$$0.2$$

Define a loss function:

$$L(\mathbf{w} \mid y, \mathbf{x}) = \begin{cases} \log \sigma(\mathbf{w} \cdot \mathbf{x}) & y = 1 \\ \log(1 - \sigma(\mathbf{w} \cdot \mathbf{x})) & y = 0 \end{cases}$$

Differentiate....

$$= \log \left(\sigma(\mathbf{w} \cdot \mathbf{x})^{y} (1 - \sigma(\mathbf{w} \cdot \mathbf{x}))^{1-y} \right)$$

$$\log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \log p & \text{if } y = 1\\ \log(1 - p) & \text{if } y = 0 \end{cases}$$
$$p = \sigma(\mathbf{x} \cdot \mathbf{w})$$

Magically, when we differentiate, we end up with something very simple and elegant.....

$$\frac{\partial}{\partial \mathbf{w}} L(\mathbf{w} \mid y, \mathbf{x}) = (y - p)\mathbf{x}$$
$$\frac{\partial}{\partial w^{j}} L(\mathbf{w} \mid y, \mathbf{x}) = (y - p)x^{j}$$

The update for gradient descent is just:

$$\mathbf{w}^{(t+1)} = \mathbf{w}^{(t)} + \lambda(y - p)\mathbf{x}$$

Logistic regression has a sparse update

An observation: sparsity!

$$\frac{\partial}{\partial w^j} \log P(Y = y | X = \mathbf{x}, \mathbf{w}) = (y - p)x^j$$

Key computational point:

- if $x^{j}=0$ then the gradient of w^{j} is zero
- so when processing an example you only need to update weights for the non-zero features of an example.

Learning as optimization for logistic regression

• The algorithm:

$$\mathbf{w}^{(t+1)} = \mathbf{w}^{(t)} + \lambda(y - p)\mathbf{x}$$

- 1. Initialize a hashtable W
- 2. For t = 1, ..., T
 - For each example \mathbf{x}_i, y_i :

- do this in random order
- Compute the prediction for \mathbf{x}_i :

$$p_{i} = \frac{1}{1 + \exp(-\sum_{j:x_{i}^{j} > 0} x_{i}^{j} w^{j})}$$

- For each non-zero feature of $\mathbf{x_i}$ with index j and value x^j :
 - * If j is not in W, set W[j] = 0.
 - * Set $W[j] = W[j] + \lambda (y_i p_i)x^j$
- 3. Output the hash table W.

Another observation

$$\frac{\partial}{\partial w^j} \log P(Y = y | X = \mathbf{x}, \mathbf{w}) = (y - p)x^j$$

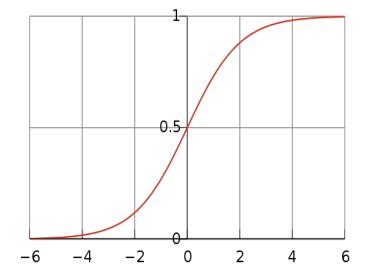
• Consider averaging the gradient over all the examples $D = \{(x_1, y_1), ..., (x_n, y_n)\}$

$$\frac{\partial}{\partial w^j} \log P(D|\mathbf{w}) = \frac{1}{n} \sum_{i} (y_i - p_i) x_i^j = \boxed{\frac{1}{n} \sum_{i:x_i^j = 1} y_i} - \boxed{\frac{1}{n} \sum_{i:x_i^j = 1} p_i}$$

- This will overfit badly with sparse features
 - Consider any word that appears only in positive examples!

Learning as optimization for logistic regression

- Goal: Learn the parameter θ of a classifier
 - Which classifier?
 - We've seen y = sign(x.w) but sign is not continuous...
 - Convenient alternative: replace sign with the logistic function



$$P(Y = y | X = \mathbf{x}, \mathbf{w}) = \frac{1}{1 + e^{\mathbf{x} \cdot \mathbf{w}}}$$

- Practical problem: this overfits badly with sparse features
 - e.g., if w^{j} is only in positive examples, its gradient is always positive!

$$\frac{\partial}{\partial w^j} \log P(D|\mathbf{w}) = \frac{1}{n} \sum_i (y_i - p_i) x_i^j = \frac{1}{n} \sum_{i:x_i^j = 1} y_i - \frac{1}{n} \sum_{i:x_i^j = 1} p_i$$

REGULARIZED LOGISTIC REGRESSION

Regularized logistic regression

Replace LCL

$$\log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \log p & \text{if } y = 1\\ \log(1 - p) & \text{if } y = 0 \end{cases}$$

 with LCL + penalty for large weights, eg

$$LCL - \mu \sum_{j=1}^{d} (w^j)^2$$

So:

$$\frac{\partial}{\partial w^j} \log P(Y = y | X = \mathbf{x}, \mathbf{w}) = (y - p)x^j$$

becomes:

$$\frac{\partial}{\partial w^j} \log P(Y = y | X = \mathbf{x}, \mathbf{w}) - \mu \sum_{j=1}^d (w^j)^2 = (y - p)x^j - 2\mu w^j$$

Regularized logistic regression

Replace LCL

$$\log P(Y = y | X = \mathbf{x}, \mathbf{w}) = \begin{cases} \log p & \text{if } y = 1\\ \log(1 - p) & \text{if } y = 0 \end{cases}$$

 with LCL + penalty for large weights, eg

$$LCL - \mu \sum_{j=1}^{d} (w^j)^2$$

So the update for wj becomes:

$$w^j = w^j + \lambda((y-p)x^j - 2\mu w^j)$$

• Or

$$w^j = w^j + \lambda(y - p)x^j - \lambda 2\mu w^j$$

Learning as optimization for logistic regression

• Algorithm:

$$\mathbf{w}^{(t+1)} = \mathbf{w}^{(t)} + \lambda(y - p)\mathbf{x}$$

- 1. Initialize a hashtable W
- 2. For t = 1, ..., T
 - For each example \mathbf{x}_i, y_i :

- -- do this in random order
- Compute the prediction for \mathbf{x}_i :

$$p_i = \frac{1}{1 + \exp(-\sum_{j:x_i^j > 0} x_i^j w^j)}$$

- For each non-zero feature of $\mathbf{x_i}$ with index j and value x^j :
 - * If j is not in W, set W[j] = 0.
 - * Set $W[j] = W[j] + \lambda (y_i p_i)x^j$
- 3. Output the hash table W.

• Algorithm:

$$w^j = w^j + \lambda(y - p)x^j - \lambda 2\mu w^j$$

- 1. Initialize a hashtable W
- 2. For t = 1, ..., T
 - For each example \mathbf{x}_i, y_i :
 - Compute the prediction for \mathbf{x}_i :

Time goes from O(nT) to O(mVT) where

- n = number of non-zero entries,
- m = number of examples
- V = number of features
- T = number of passes over data

$$p_i = \frac{1}{1 + \exp(-\sum_{j:x_i^j > 0} x_i^j w^j)}$$

- For each non-zero feature of $\mathbf{x_i}$ with index j and value x^j :
 - * If j is not in W, set W[j] = 0.
 - * Set $W[j] = W[j] + \lambda(y-p)x^j \lambda 2\mu w^j$
- 3. Output the hash table W.

This change is very important for large datasets

- We've lost the ability to do sparse updates
- This makes learning much much more expensive
 - $-2*10^6$ examples
 - 2*10⁸ non-zero entries
 - $-2*10^6$ + features
 - -10,000x slower (!)

Time goes from O(nT) to O(mVT) where

- n = number of non-zero entries,
- m = number of examples
- V = number of features
- T = number of passes over data

SPARSE UPDATES FOR REGULARIZED LOGISTIC REGRESSION

- Final algorithm: $w^j = w^j + \lambda(y-p)x^j \lambda 2\mu w^j$
- Initialize hashtable W
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - $p_i = \dots$
 - For each feature *W[j]*

$$-W[j] = W[j] - \lambda 2\mu W[j]$$

 $-If x_i > 0$ then

$$W[j] = W[j] + \lambda (y_i - p^i) x_j$$

- Final algorithm: $w^j = w^j + \lambda (y p) x^j \lambda 2\mu w^j$
- Initialize hashtable W
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - $p_i = ...$
 - For each feature W[j]

$$-W[j] *= (1 - \lambda 2\mu)$$

 $-If x_i^j > 0$ then

$$W[j] = W[j] + \lambda (y_i - p^i) x_j$$

• Final algorithm:

$$w^{j} = w^{j} + \lambda(y - p)x^{j} - \lambda 2\mu w^{j}$$

- Initialize hashtable W
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - $p_i = \dots$
 - For each feature *W[j]*
 - $-\text{If } x_i^j > 0 \text{ then }$

»
$$W[j] *= (1 - \lambda 2\mu)^A$$

$$W[j] = W[j] + \lambda (y_i - p^i) x_j$$

A is number of examples seen since the last time we did an x>0 update on W[j]

• Final algorithm:

$$w^j = w^j + \lambda(y - p)x^j - \lambda 2\mu w^j$$

- Initialize hashtables W, A and set k=0
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - $p_i = ...; k++$
 - For each feature *W[j]*
 - -If x > 0 then

k-A[j] is number of examples seen since the last time we did an x>0 update on W[j]

»
$$W[j] *= (1 - \lambda 2\mu)^{k-A[j]}$$

» $W[j] = W[j] + \lambda (y_i - p^i) x_i$

$$A[j] = k$$

• Final algorithm:

$$w^j = w^j + \lambda(y - p)x^j - \lambda 2\mu w^j$$

- Initialize hashtables W, A and set k=0
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - $p_i = ...; k++$
 - For each feature *W[j]*
 - $-If x \ge 0$ then

$$W[j] *= (1 - \lambda 2\mu)^{k-A[j]}$$

»
$$W[j] = W[j] + \lambda (y_i - p^i) x_i$$

$$A[j] = k$$

- k = "clock" reading
- A[j] = clock reading last time feature j was "active"
- we implement the "weight decay" update using a "lazy" strategy: weights are decayed in one shot when a feature is "active"

• Final algorithm:

$$w^j = w^j + \lambda(y - p)x^j - \lambda 2\mu w^j$$

- Initialize hashtables W, A and set k=0
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - $p_i = ...; k++$
 - For each feature *W[j]*
 - $-If x^{j} > 0$ then

Time goes from O(nT) to O(mVT) where

- n = number of non-zero entries,
- m = number of examples
- V = number of features
- T = number of passes over data

Memory use doubles.

$$W[j] *= (1 - \lambda 2\mu)^{k-A[j]}$$

$$W[j] = W[j] + \lambda (y_i - p^i) x_j$$

$$A[j] = k$$

Comments

- What's happened here:
 - Our update involves a sparse part and a dense part
 - Sparse: empirical loss on this example
 - Dense: regularization loss not affected by the example
 - We remove the dense part of the update
 - Old example update:
 - for each feature { do something example-independent}
 - For each active feature { do something example-dependent}
 - New example update:
 - For each active feature:
 - » {simulate the prior example-independent updates}
 - » {do something example-dependent}

Comments

- Same trick can be applied in other contexts
 - -Other regularizers (eg L1, ...)
 - Conjugate gradient (Langford)
 - -FTRL (Follow the regularized leader)
 - Voted perceptron averaging
 - **—** ...?

BOUNDED-MEMORY LOGISTIC REGRESSION

Question

- In text classification most words are
 - a. rare
 - b. not correlated with any class
 - c. given low weights in the LR classifier
 - d. unlikely to affect classification
 - e. not very interesting

Question

- In text classification most bigrams are
 - a. rare
 - b. not correlated with any class
 - c. given low weights in the LR classifier
 - d. unlikely to affect classification
 - e. not very interesting

Question

- Most of the weights in a classifier are
 - -important
 - not important

How can we exploit this?

- One idea: combine uncommon words together *randomly*
- Examples:
 - replace all occurrances of "humanitarianism" or "biopsy" with "humanitarianismOrBiopsy"
 - replace all occurrances of "schizoid" or "duchy" with "schizoidOrDuchy"
 - replace all occurrances of "gynecologist" or "constrictor" with "gynecologistOrConstrictor"
 - **—** ...
- For Naïve Bayes this breaks independence assumptions
 - it's not obviously a problem for logistic regression, though
- I could combine
 - two low-weight words (won't matter much)
 - a low-weight and a high-weight word (won't matter much)
 - two high-weight words (not very likely to happen)
- How much of this can I get away with?
 - certainly a little
 - is it enough to make a difference? how much memory does it save?

How can we exploit this?

- Another observation:
 - the values in my hash table are *weights*
 - the keys in my hash table are strings for the feature names
 - We need them to avoid collisions
- But maybe we don't care about collisions?
 - Allowing "schizoid" & "duchy" to collide is equivalent to replacing all occurrences of "schizoid" or "duchy" with "schizoidOrDuchy"

Learning as optimization for regularized logistic regression

• Algorithm:

$$w^j = w^j + \lambda(y - p)x^j - \lambda 2\mu w^j$$

- Initialize hashtables W, A and set k=0
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - $p_i = ...$; k++
 - For each feature *j*: $x_i^j > 0$:

»
$$W[j] *= (1 - \lambda 2\mu)^{k-A[j]}$$

$$W[j] = W[j] + \lambda (y_i - p^i) X_i$$

$$A[j] = k$$

Learning as optimization for regularized logistic regression

• Algorithm:

$$w^j = w^j + \lambda(y - p)x^j - \lambda 2\mu w^j$$

- Initialize arrays W, A of size R and set k=0
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - Let V be hash table so that $V[h] = \sum_{i=1}^{n} x_i^{j}$
 - $p_i = ...$; k++

 $j:hash(x_i^J)\%R=h$

• For each hash value *h: V[h]*>0:

»
$$W/h/ *= (1 - \lambda 2\mu)^{k-A[j]}$$

$$W[h] = W[h] + \lambda(y_i - p^i)V[h]$$

$$A[h] = k$$

Learning as optimization for regularized logistic regression

• Algorithm:

$$w^{j} = w^{j} + \lambda(y - p)x^{j} - \lambda 2\mu w^{j}$$

- Initialize arrays W, A of size R and set k=0
- For each iteration t=1,...T
 - For each example (\mathbf{x}_i, y_i)
 - Let V be hash table so that

$$p_i = \dots, k++$$

$$V[h] = \sum_{j:hash(j)\%R==h}^{j} x_i^j$$

$$p \equiv \frac{1}{1 + e^{-\mathbf{x} \cdot \mathbf{w}}} \qquad \qquad p \equiv \frac{1}{1 + e^{-\mathbf{V} \cdot \mathbf{w}}}$$

IMPLEMENTATION DETAILS

Fixes and optimizations

- This is the basic idea but
 - we need to apply "weight decay" to features in an example before we compute the prediction
 - we need to apply "weight decay" before we save the learned classifier
 - -my suggestion:
 - an abstraction for a logistic regression classifier

A possible SGD implementation

class SGDLogistic Regression {

```
/** Predict using current weights **/
 double predict(Map features);
/** Apply weight decay to a single feature and record when in A[]**/
 void regularize(string feature, int currentK);
/** Regularize all features then save to disk **/
void save(string fileName,int currentK);
/** Load a saved classifier **/
static SGDClassifier load(String fileName);
/** Train on one example **/
void train1(Map features, double trueLabel, int k) {
   // regularize each feature
   // predict and apply update
main 'train' program assumes a stream of randomly-ordered examples and
 outputs classifier to disk; main 'test' program prints predictions for each
 test case in input.
```

A possible SGD implementation

```
class SGDLogistic Regression {
     ...
}
// main 'train' program assumes a stream of randomly-ordered
     examples and outputs classifier to disk; main 'test' program prints
     predictions for each test case in input.
<100 lines (in python)</pre>
```

Other mains:

- A "shuffler:"
 - stream thru a training file T times and output instances
 - output is randomly ordered, as much as possible, given a buffer of size B
- Something to collect predictions + true labels and produce error rates, etc.

A possible SGD implementation

- Parameter settings:
 - $-W[j] *= (1 \lambda 2\mu)^{k-A[j]}$
 - $-W[j] = W[j] + \lambda (y_i p^i)x_j$
- I didn't tune especially but used
 - $-\mu = 0.1$
 - $-\lambda = \eta^* E^{-2}$ where *E* is "epoch", $\eta = \frac{1}{2}$
 - epoch: number of times you've iterated over the dataset, starting at E=1

Feature Hashing for Large Scale Multitask Learning

Kilian Weinberger Anirban Dasgupta John Langford Alex Smola Josh Attenberg

Yahoo! Research, 2821 Mission College Blvd., Santa Clara, CA 95051 USA

KILIAN@ YAHOO-INC.COM ANIRBAN@ YAHOO-INC.COM JL@HUNCH.NET ALEX@SMOLA.ORG JOSH@CIS.POLY.EDU

ICML 2009

An interesting example

- Spam filtering for Yahoo mail
 - Lots of examples and lots of users
 - Two options:
 - one filter for everyone—but users disagree
 - one filter for each user—but some users are lazy and don't label anything
 - Third option:
 - classify (msg,user) pairs
 - features of message i are words $w_{i,1},...,w_{i,ki}$
 - feature of user is his/her id u
 - features of **pair** are: $w_{i,1},...,w_{i,ki}$ and $u \cdot w_{i,1},...,u \cdot w_{i,ki}$
 - · based on an idea by Hal Daumé

An example

E.g., this email to wcohen

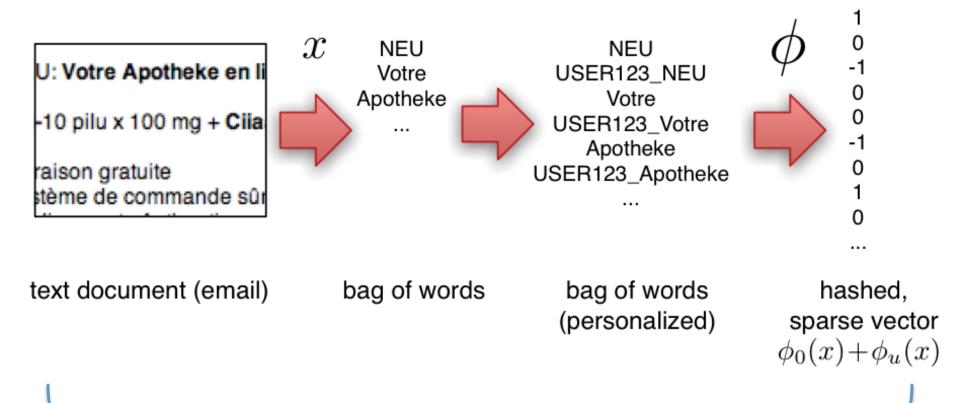
Dear Madam/Sir,

My name is Mohammed Azziz an investment Broker with SouthCoast Plc a company based in London United Kingdom our major activity is in the area of managing customers funds with targetted interest rates through provision and acquisition of loans to interested borrowers with the basic requisite. Our periodic checks on people and Companies located

• features:

- dear, madam, sir,.... investment, broker,..., wcohen•dear, wcohen•madam, wcohen,...,
- idea: the learner will figure out how to personalize my spam filter by using the wcohen•X features

An example



Compute personalized features and multiple hashes on-the-fly: a great opportunity to use several processors and speed up i/o

Experiments

- 3.2M emails
- 40M tokens
- 430k users
- 16T unique features after personalization

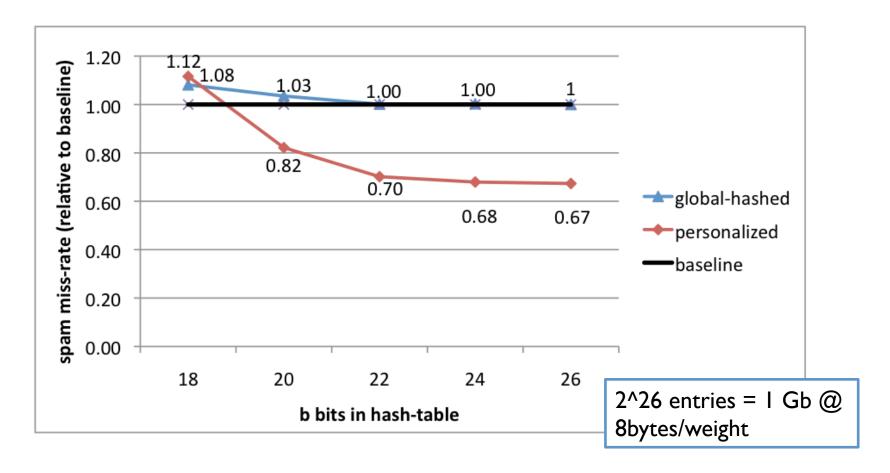


Figure 2. The decrease of uncaught spam over the baseline classifier averaged over all users. The classification threshold was chosen to keep the not-spam misclassification fixed at 1%. The hashed global classifier (global-hashed) converges relatively soon, showing that the distortion error ϵ_d vanishes. The personalized classifier results in an average improvement of up to 30%.

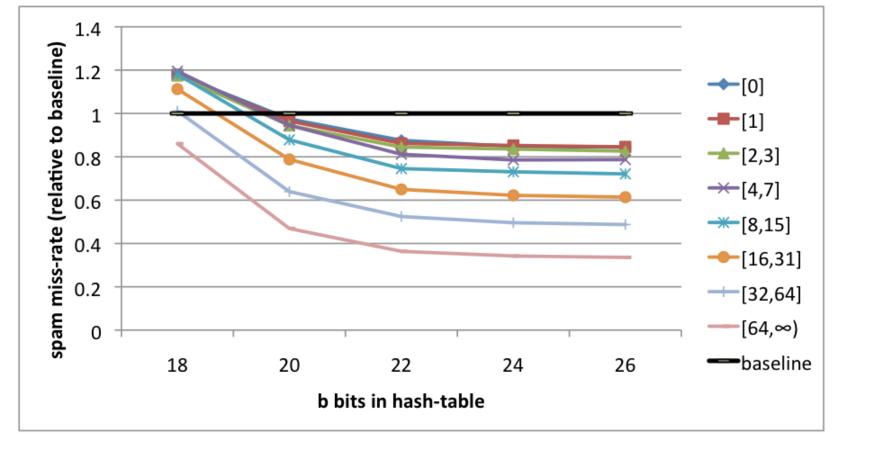


Figure 3. Results for users clustered by training emails. For example, the bucket [8,15] consists of all users with eight to fifteen training emails. Although users in buckets with large amounts of training data do benefit more from the personalized classifier (upto 65% reduction in spam), even users that did not contribute to the training corpus at all obtain almost 20% spam-reduction.