2023年2月23日 10:03

3.3 pd. A workhow f. y -> X of shower over Steps. iso to a scheme $\frac{1}{\sqrt{1}}$ $\frac{1}{\sqrt{1}}$ \$9. From sch 4 20p. then to Chp. $\underline{Q,1},\underline{D}f.$ $\underline{Q,1},\underline{Q,1},\underline{D}f.$ $\underline{Q,1},\underline{Q,1},\underline{D}f.$ $\underline{Q,1},\underline{Q,1},\underline{D}f.$ $\underline{Q,1},\underline{Q,1},\underline{Q,1},\underline{D}f.$ $\underline{Q,1},\underline{Q,$ A rep. mor of share over Start $\frac{Y \longrightarrow X}{\forall U \in Schys}, \quad \text{for all } x \in X(U),$ $\frac{Y \times U \longrightarrow U}{\langle X \times U \longrightarrow U \times Sch \times V \times V}$ sole > (x U -> U & sole (2) X & Shu (Sfift, Set) is an algebraic space over S. If (a), the diag. X > X x x rep.

(b) > surj et mov. U > X with Ue suh's. (by (0) (3.4) this is onto outo my. hence moles sense the cat of alg. spars is denoted by Esps. (3). Let Y => X nor of algoricic space over Sport. A chart for f is a comm. diag obtained by this way.

with 1/-> 4 in Sche.

with V -> U in Solys. (4) Let P = E4, sm, suij. Y -> X in Exprs. has P it = chart of f s.t. V-> U has P. Cet P = Ed, 80 sm, Surj. (5) A rep- mor of stacks over Start has P if "Sho (Sief, Eapl) φ φ $\gamma \in \chi(u)$, $u \in S_ch/S$, $y \times u \rightarrow u$ hous φ . X e shu (staf. epd) à our debrine stack. <u>(6)</u> . (or Artin stack) (vesp. Deligno - Munford stack)

over S if (a) the diag $X \longrightarrow X_{\overline{s}}X$ is rep (by dg. spans) (b) $\overline{\Rightarrow}$ sur). Sm (vesp. $\underline{\epsilon}(1)$ mor $U \longrightarrow X$ with $U \in S_{c}b_{S_{c}}$ Remoted the & (2,1) - car of alg. stacks over S by

(7). Let $y \xrightarrow{f} \chi$ mor in the /s, a chart of f $V \xrightarrow{sm,sn_i} y_{\chi} U \rightarrow U$ $y \xrightarrow{sm_i,sn_i} \chi U$ $y \xrightarrow{sm_i,sn_i} \chi U$ $y \xrightarrow{sm_i,sn_i} \chi U$

(8). Let P z 21, Sm, Sm). Y -> X in Chers. hors P. if I a chart of f s.t. V-> U hous P.

4.2. Essemples of aley spaces / stacks N). BG: (Suh/s) of capd. where G a a (lossifying stack sm S-gy sdove. More generally, $X \in 20 p/s$, G - sm S-gp solu.outing on X. define quotient stack [X/G]: (Selys) of - end. T (n:Z -> XT) Where Z E Tovs (T, CoT), 2 - CoT - equivarant

morphism of Shu(Tfm).

• Pry z-Yoneda, $U \rightarrow [X_G]$ amounts to

71 Z -> Xu Z C Tovs (U, Gu).

• Fact: $[X_G] \in Chp_S$ $X \longrightarrow [X_G] \longleftrightarrow P: G_X \longrightarrow X$ $X \longrightarrow [X_G] \longleftrightarrow P: G_X \longrightarrow X$

• In particular. BG = BsG = [S/G]

· Similarly, more simple.

action in free. ($G \times X \longrightarrow X \times X$)

Then $X_G := (T \longrightarrow X(T)_G)^{\#} \in Sep_S$.

called quotion space. with $X \longrightarrow X_G$ at as.

(2). Mg; (9ch/s) of Epd.

Times (CAT on proper with geo. fiber)

courr. genus g curre.

is a DM stack.

U Ø -> W

cation χ . Ohjor $u \xrightarrow{u} \chi \leftarrow u \in \chi(u)$.

covering; {U; -> U}. is Ed (figt) containing when viewed on scheme over S.

(gmall & , lis- 24.)

 $\frac{5.2}{\Gamma(\chi_{\overline{\tau}, -})} = \frac{21}{fpf}, \quad \lim_{\xi \to \infty} \frac{5.2}{fpf}, \quad \lim_{\xi$

5.). Functoriality. $y \rightarrow \chi$ nor. of stable. over S.

s. adj. Shu(y_{τ}) $\xrightarrow{f_{\pi}}$ Shu(χ_{τ})

and.

 $\frac{5.4}{1}$. Rule. For $X \in Sde/S$, this agrees with big $\frac{5.4}{1}$ for $\frac{5$

5.5 Det (Crovbos). Let e be a site.

A stack y ∈ Shu (C, epd). is gente onon ∈ if
 - (locally nonempty) ∀ U ∈ C, ∃ cov. & U; → U} st.
 _ (bocally commerted)

Y(U;) ≠ Ø, ∀i'.

 $\frac{d}{d}$ $\frac{d}{d}$

* $\tau \in \{\&, frof \}$ $\uparrow \in Shr(S_{\tau}, epd)$ we have $H^{2}_{\tau}(\tau, ef) \cong Crowls(\tau, ef)/eg-equil.$

5.6 Cohomological descent Let XC Chys. and $X \longrightarrow X$ an atlax $\beta \in Ab(X_{\epsilon})$. $X. ? \Delta^{op} \longrightarrow \underbrace{\text{Sup} / s}_{X \times X - \cdot - X} \longrightarrow \text{NOT adms.} \text{ be Each vario.}$ Then $E_{i}^{pq} = H_{r}^{q}(\underbrace{X_{p}, P|_{X_{p}}}) \Longrightarrow H_{r}^{pqq}(X, P)$ whose Ed Ez-page is $E_{2}^{pq} = H^{r}(X/\chi, \mathcal{H}_{r}^{q}(\mathcal{F})) \Rightarrow H_{1}^{pq}(\chi,\mathcal{F})$ the preshort $U \longrightarrow H^{9}(U, F|_{U})$ XXC X Solum X (X/G) 1 gg orhum Xp = X x G x G ... x 9 GXT-3G T-S-X