

I'm currently finishing my undergraduate **CS degree with a minor in English**. Although this is an unusual combination, my English classes have greatly enhanced my ability to communicate difficult technical concepts in writing and in person. My career goals are (1) to further foundational knowledge in CS theory, specifically **complexity theory**, through research and collaborations and (2) to empower others through **teaching and research mentorship**. With these goals in mind, I aim to become a **CS theory professor**.

**Research Interests** I'm fascinated by complexity theory's investigation of inherent limitations, and I'm particularly interested in the **limits of what computational limitations we can prove**. There are several concrete barriers, such as relativization and algebrization, to proving important conjectured class separations and equalities. How to overcome these barriers is an open question. Relativization is a canonical example of limitations in proving lower bounds. We know that any complexity proof must not hold its structure relative to an oracle unless its conclusion holds relative to all oracles. For example, any proof that shows  $P = NP$  or  $P \neq NP$  must not relativize; otherwise, a contradiction would arise since there are oracles  $A$  and  $B$  such that  $P^A = NP^A$  while  $P^B \neq NP^B$  [1]. Further, natural proofs also seem unlikely to prove many important class separations because they imply the nonexistence of one-way functions [2]. Arithmetization overcomes both of these barriers and was successful in proving the major result  $PSPACE \subseteq IP$ . Arithmetization considers Boolean formulas as low-degree polynomials. This gives the verifier in an interactive proof increased power to catch the prover in a lie, enabling an interactive proof to verify the  $PSPACE$ -complete language  $TQBF$  [3]. Unfortunately, this promising technique relativizes with respect to algebraic oracles.  $PSPACE^A \subseteq IP^{\tilde{A}}$  (the algebrized version of  $PSPACE \subseteq IP$  in which  $\tilde{A}$  is the arithmetized version of  $A$ ) holds because we can write an interactive proof for  $TQBF^A$  in a similar manner as before with the addition of the algebraic oracle  $\tilde{A}$ ; even though instances of  $A$  can be embedded in the  $QBF$ , the verifier can evaluate the arithmetized formulas by making calls to its  $\tilde{A}$  oracle. The fact that this proof algebrizes is not a problem in and of itself. However, it indicates that this promising proof technique algebrizes, and for many open questions, their proofs must not algebrize. For example, any proof that  $P = NP$  must not algebrize because there is an algebraic oracle  $\tilde{A}$  such that  $NP^A \not\subseteq P^{\tilde{A}}$ , which would contradict  $NP^A \subseteq P^{\tilde{A}}$ , the algebrized version of  $NP \subseteq P$ . This algebrization barrier extends to many other central questions in complexity theory (including proofs of  $P \neq NP$ ) [4]. In a recent example of proof barriers, R. Williams and Buss quantified the limit of alternation-trading proofs, a commonly used technique in proving time-space lower bounds for many  $NP$ -complete problems [5]. Interestingly, R. Williams first created an automated approach to generating alternation-trading proofs. He then used the fact that the automated approach seemed to converge on a single bound as empirical evidence that this bound is optimal. Later, R. Williams and Buss confirmed this evidence with a formal proof of the limit of alternation-trading proofs. I'm interested in continuing this line of work by looking for alternate approaches to proving time-space lower bounds on  $SAT$ , perhaps using randomized or quantum speed-ups, a tool Dr. R. Williams and his students are currently investigating.

I'm intrigued by these "meta-discoveries" of the limitations of proof techniques, and I hope to develop creative approaches to overcoming them. I'm particularly excited about R. Williams' approach of "**ironic complexity theory**." This approach uses an upper bound for a problem in an algorithmic computational model (specifically, a circuit analysis problem) to prove a lower bound in a circuit model. A remarkable result of this approach is R. Williams' proof that  $NEXP \not\subseteq ACC0$  [6]. To create a connection between the circuit model and the algorithmic model, we consider the circuit analysis problem  $ACC0 - SAT$ , which asks if a given  $ACC0$  circuit accepts any input. First, we prove an upper bound in the algorithmic model. By representing functions in  $ACC0$  in terms of low-degree polynomials, we develop an exponential, but faster-than-brute-force, algorithm solving  $ACC0 - SAT$ . For the sake of contradiction, we assume  $NEXP \subseteq ACC0$ . However, under this assumption our  $ACC0 - SAT$  algorithm can be used to violate the nondeterministic time hierarchy theorem, creating a contradiction. Therefore,  $NEXP \not\subseteq ACC0$ . This technique of "ironic complexity theory" extends to other open questions. For example, for every circuit type  $\mathcal{C}$ , if we can find faster-than-brute-force algorithms for  $\mathcal{C} - SAT$ , then we can prove  $NEXP \not\subseteq \mathcal{C}$ . Further, plausible derandomization assumptions or slightly faster algorithms for problems such as  $EDIT - DISTANCE$  would both also imply circuit lower bounds [7].

More research is necessary to exploit "ironic complexity theory" to prove new circuit lower bounds and to discover the limits of this approach. I hope to be a part of this research. Although I'm particularly interested in complexity theory, and Dr. R. Williams' work specifically, I'm also excited to explore and open to researching other subfields of CS theory pursued across MIT's theory group.

**Preparation** Along with standard theory curriculum, I've taken courses focused on complexity theory and cryptography, and I'll be taking a graduate level course in approximation algorithms next semester. These **theory technical electives** have given me grounding in theoretical literature and experience applying mathematical principles

and proof techniques. I've also developed a deep appreciation for the **collaborative nature of CS theory**; I've enjoyed many Sunday evenings puzzling through complexity problem sets with my classmates. Additionally, I completed a **term paper on Gödel's Proof of Incompleteness**, a proof that every consistent mathematic system has statements which are true but cannot be proven within the system. I condensed Gödel's 36-page proof into an 8-page overview understandable by advanced undergraduate students, demonstrating a firm handle of the mathematical concepts. It took me more hours to read and deeply understand Gödel's proof than there were pages in the paper, and I relished the challenge, finding it engaging and rewarding. My term paper can be seen here: [https://ryan-moreno.github.io/resources/godel\\_incompleteness\\_theorem.pdf](https://ryan-moreno.github.io/resources/godel_incompleteness_theorem.pdf)

My first research experiences were in the **OSU Walker Lab** and the **USC Interaction Lab**, in chemical and mechanical engineering, respectively. They taught me transferrable skills including experimental design, cross-discipline collaboration, and a willingness to ask questions. My current research is in artificial intelligence and natural language processing. I chose this area because USC doesn't have ongoing complexity research. Additionally, I wanted to work in AI and NLP for my **honors undergraduate thesis** because it combines my two areas of study (computer science and English). Last year I developed my thesis proposal for **automated poetry generation using deep learning** based on current techniques in creative image and sound generation. Next semester I will be turning this proposal into my honors undergraduate thesis under the advisement of Dr. Xiang Ren.

I'm also working with Dr. Ren in the **USC Intelligence and Knowledge Lab**, using machine learning to develop a sequence labeling module to recognize named entities in text. Our approach uses trigger phrases that signal named entities (such as the phrase "ate lunch at" signaling an entity of type "restaurant"). We use a small number of manually defined trigger phrases to label named entities in unlabeled corpora. The labels found by the trigger matching module are then used as weakly labeled data to train a separate sequence labeling module. This step is critical because existing approaches to sequence labeling are limited by the expense of human-annotated data, whereas our approach augments a small amount of human-annotated data with a large amount of weakly labeled data. I'm helping to implement the machine learning algorithms and write our manuscript (recently submitted for publication).

Along with research experience, I completed summer **internships at Facebook and Microsoft**. Although I hope to pursue academic research, understanding the engineering practices in the industry sector will help me communicate effectively with industry engineers during potential collaborations. Additionally, having a spectrum of experiences will be beneficial when mentoring my future students.

**Broader Impacts** As a professor, I want to engage students in CS theory. I've seen this field brushed off as academic and inapplicable, which I believe is due to a lack of effective communication. I'm passionate about communicating with students at their level of understanding because feeling like you're already missing background knowledge when learning a difficult subject is discouraging. This discouragement is exacerbated in undergraduate CS courses because some students enter college with years of programming experience while others, particularly underrepresented minorities in the field, enter with none. By promoting **effective communication** in our field, I hope to retain a broader spectrum of students. I've worked as an **undergraduate TA** since sophomore year, specifically helping teach theory courses since junior year. At the end of most discussion sections, I'll have students tell me they appreciated my enthusiasm and methodical approach to teaching problem solving skills. I strive to communicate at a student's level of understanding, so there's nothing more gratifying than hearing from my students that I've done exactly that.

I've also **taught 3rd-12th grade students** through tutoring and classroom assistance. From teaching a 5th grade mini-course on poetry to tutoring high schoolers in pre-calculus, these experiences have all boiled down to the same puzzle of how to effectively communicate in a manner appropriate to the students' experiences and understanding. I've also participated in **STEM outreach** programs such as Robogals, a club dedicated to engaging young women in STEM and empowering them to consider engineering careers. As a future educator, I will continue to participate in STEM outreach programs and will strive to **create inclusive learning and research environments**, which I've learned the importance of firsthand. Last year I participated in **Out 4 Undergrad**, an LGBTQ+ tech conference. The conference theme was "covering," when people feel the need to hide aspects of their identity in work or academic environments. Thinking about my own experiences and hearing others' reminded me that creating an environment in which people are comfortable being their full selves is necessary to maintain an intellectually vibrant community. I learned the importance of having a diverse group of colleagues when building a customer-facing feature at Microsoft. A coworker with experience in foreign languages pointed out that I hadn't accounted for the formatting of right-to-left languages. Someone else suggested ways to make keyboard navigation easier for people with visual impairments. Intellectual diversity is valuable because it allows collaborators to fill in each other's experiential gaps.

I'm excited to become a professor because of the opportunity to teach and share my enthusiasm with students

while collaborating with other researchers to expand fundamental knowledge in complexity theory. I'm eager to make lasting impact to our field through intellectual contributions, student mentorship, and promoting effective communication.

### **References**

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