



## **Dynamics of Mechanical Systems**

### **HW3 - G27**

Excavator 1 - John Deere 60G

Task 1 – Excavate Area 1 (Rectangle Below the Ground Level)

96148 – Álvaro Lopes

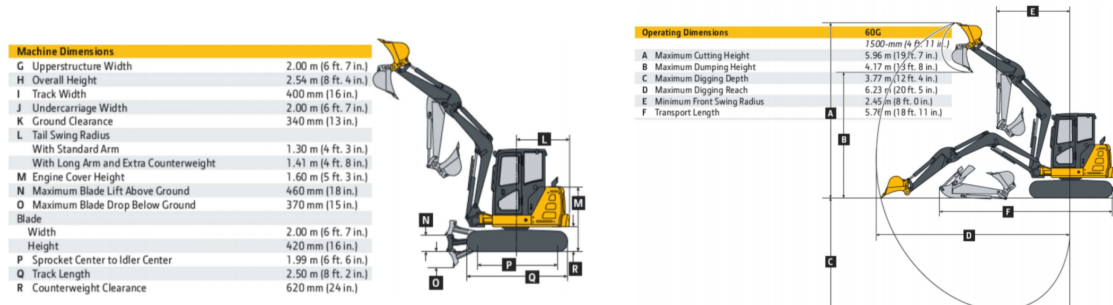
96351 – André Lopes

96455 – Miguel Valverde

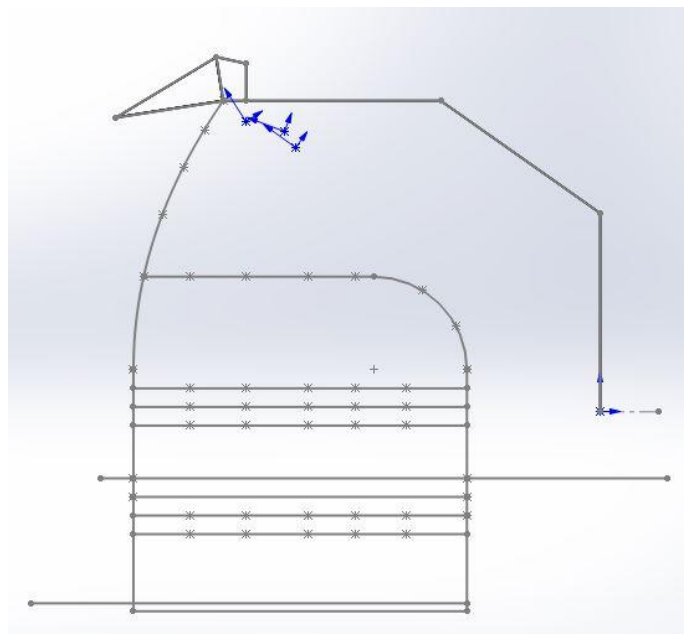
In this homework we had to perform the kinematic analysis of an excavator, more specifically the excavator *John Deer* (excavator 1), using the program *MUBOKAP*. The characteristics of this excavator are the following:

Excavator 1 John Deer 60G

(Bucket Capacity: 0.35 m<sup>3</sup>)






Using this pictures and measurements, a mock-up model of the excavator in *SOLIDWORKS* was created and can be seen below:



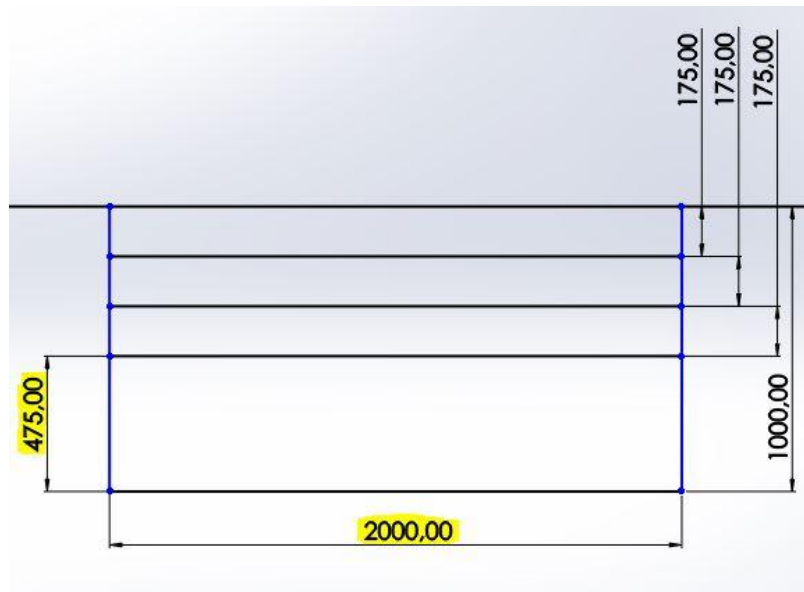
Now we move onto the questions asked:

**(1.1) Build a path (or a sequence of paths) for the bucket to perform the excavation prescribed in your application. Note that for each pass of the bucket there is a limit of material that can be removed. If more than 3 passes are necessary, consider only the first 3 passes and identify the approximate shape of what is left to dig**

First we present the 3 .txt files that serve as an input to *MUBOKAP* as the trajectory to follow. The first one is the x coordinate, the second one the y coordinate and the last one the *theta* angle. For each of these files there are 56 entries and 1 entry corresponds to one second.

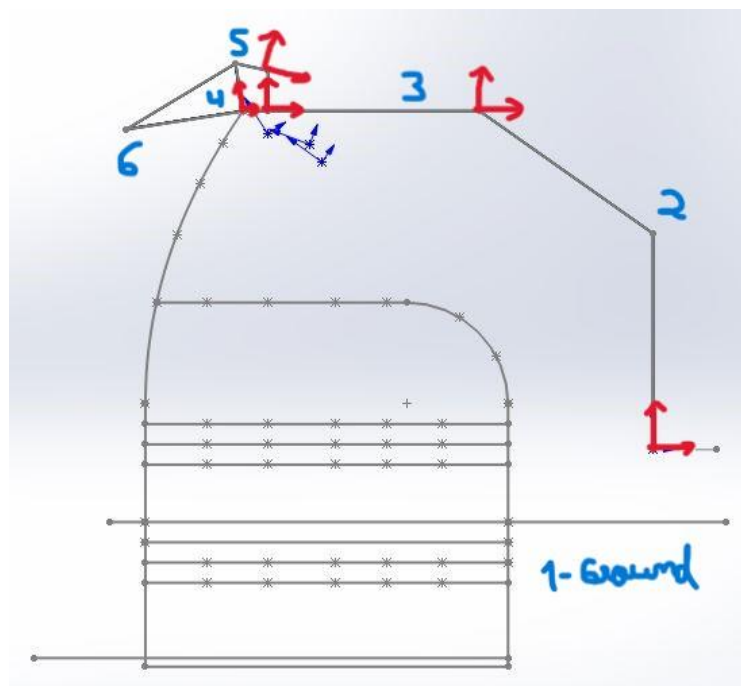
<div>  Driver_001 </div>		<div>  Driver_002 </div>		<div>  Driver_003 </div>	
Ficheiro	Editar	Ficheiro	Editar	Ficheiro	Editar
0 -2826.95		0 2339.01		0 0.1557	
1 -3000		1 2122.31		1 0.43872	
2 -3250		2 1839.04		2 0.72174	
3 -3500		3 1487.7		3 1.00476	
4 -3750		4 1016.44		4 1.28778	
5 -4000		5 316.38		5 1.5708	
6 -4000		6 176.38		6 1.5708	
7 -3666		7 176.38		7 1.5708	
8 -3333		8 176.38		8 1.5708	
9 -3000		9 176.38		9 1.5708	
10 -2666		10 176.38		10 1.5708	
11 -2333		11 176.38		11 1.5708	
12 -2000		12 176.38		12 1.5708	
13 -2000		13 316.38		13 1.5708	
14 -2100		14 646.72		14 2.09412469282041	
15 -2400		15 912.12		15 2.61681469282041	
16 -2700		16 1016.44		16 3.14181469282041	
17 -3000		17 1016.44		17 2.66381469282041	
18 -3300		18 1016.44		18 2.18581469282041	
19 -3550		19 1016.44		19 1.70781469282041	
20 -3800		20 1016.44		20 1.22911469282041	
21 -4000		21 316.38		21 1.57079469282041	
22 -4000		22 36.38		22 1.57079469282041	
23 -3666		23 36.38		23 1.57079469282041	
24 -3333		24 36.38		24 1.57079469282041	
25 -3000		25 36.38		25 1.57079469282041	
26 -2666		26 36.38		26 1.57079469282041	
27 -2333		27 36.38		27 1.57079469282041	
28 -2000		28 36.38		28 1.57079469282041	
29 -2000		29 316.38		29 1.57079469282041	
30 -2100		30 646.72		30 2.09412469282041	
31 -2400		31 912.12		31 2.61681469282041	
32 -2700		32 1016.44		32 3.14181469282041	
33 -3000		33 1016.44		33 2.66381469282041	
34 -3300		34 1016.44		34 2.18581469282041	
35 -3550		35 1016.44		35 1.70781469282041	
36 -3800		36 1016.44		36 1.22911469282041	
37 -4000		37 316.38		37 1.57079469282041	
38 -4000		38 -103.62		38 1.57079469282041	
39 -3666		39 -103.62		39 1.57079469282041	
40 -3333		40 -103.62		40 1.57079469282041	
41 -3000		41 -103.62		41 1.57079469282041	
42 -2666		42 -103.62		42 1.57079469282041	
43 -2333		43 -103.62		43 1.57079469282041	
44 -2000		44 -103.62		44 1.57079469282041	
45 -2000		45 316.38		45 1.57079469282041	
46 -2100		46 646.72		46 2.09412469282041	
47 -2400		47 912.12		47 2.61681469282041	
48 -2700		48 1016.44		48 3.14181469282041	
49 -3000		49 1016.44		49 2.66381469282041	
50 -3300		50 1016.44		50 2.18581469282041	
51 -3200		51 1016.44		51 1.70781469282041	
52 -3100		52 1016.44		52 1.22911469282041	
53 -3000		53 1487.7		53 1.43404469282041	
54 -2900		54 1839.04		54 0.549114692820414	
55 -2850		55 2122.31		55 0.209114692820414	
56 -2826.95		56 2339.01		56 0.1557	

Since our bucket had an area of  $0.35\text{m}^2$  and the area to dig is 2 square meters ( $2\text{m} \times 1\text{m}$ ), more than 3 passes were necessary ( $3 \times 0.35 = 1.05\text{m}^2$ ). As such, the area left to dig is equal to  $0.95\text{ m}^2$  ( $0.475 \times 2$ ). The image below shows all the measures mentioned.



**(1.2) Guide the bucket position and orientation with the position drivers directly applied to the bucket body and, obtain the history of the positions of the points to which the hydraulic actuators are connected.**

As for the model which was built, we decided to divide the excavator into 6 different bodies. In total there are 6 joints, all of them revolution joints. The bodies, their numbers and their local reference frames are depicted in the picture below



In addition to this, there are 3 conditions for the ground and 3 driver constraints as this model has 3 degrees of freedom. If we check:

$$6*3 - 6*2 - 3*1 = 3 \text{ degrees of freedom}$$

The model information and its respective input file can be seen here:

```

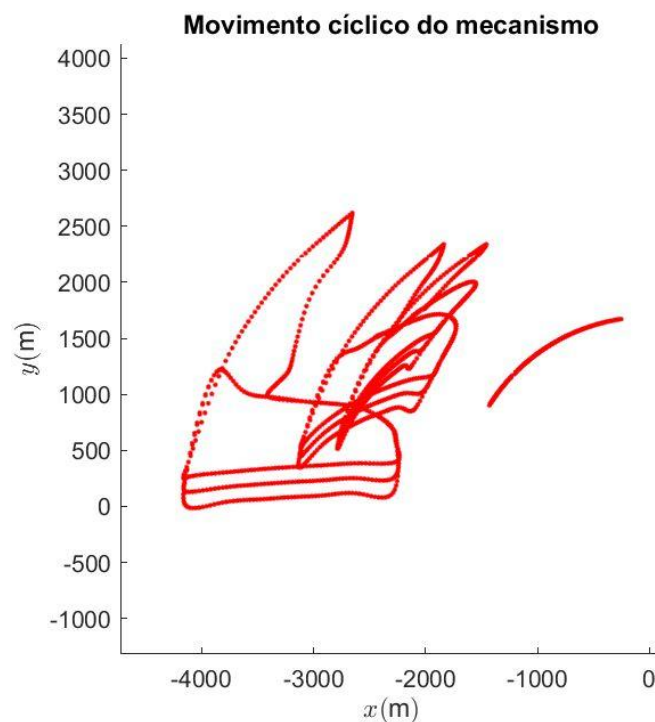
model_excavator
Ficheiro  Editar  Ver

6 6 0 0 0 0 0 3 3 4
0 0 0
0 0 0
-1195.69 2339.01 0
-2653.95 2339.01 0
-2653.95 2619.35 6.0683
-2826.95 2339.01 0.1557
1 2 0 0 0
2 3 -1195.69 2339.01 0 0
3 4 -1458.26 0 0 0
3 6 -1631.26 0 0 0
4 5 0 280.34 0 0
5 6 -230 0 0 333.4
1 1 0
1 2 0
1 3 0
3 6 1 0 0.000 0.000 0.000 0.000 4 1
3 6 2 0 0.000 0.000 0.000 0.000 4 2
3 6 3 0 0.000 0.000 0.000 0.000 4 3
3 0 0
4 0 0
5 0 0
6 -816.38 0
12 0.000001
0 0.1 56

```

Now we are ready to see the results. They are presented below as well:

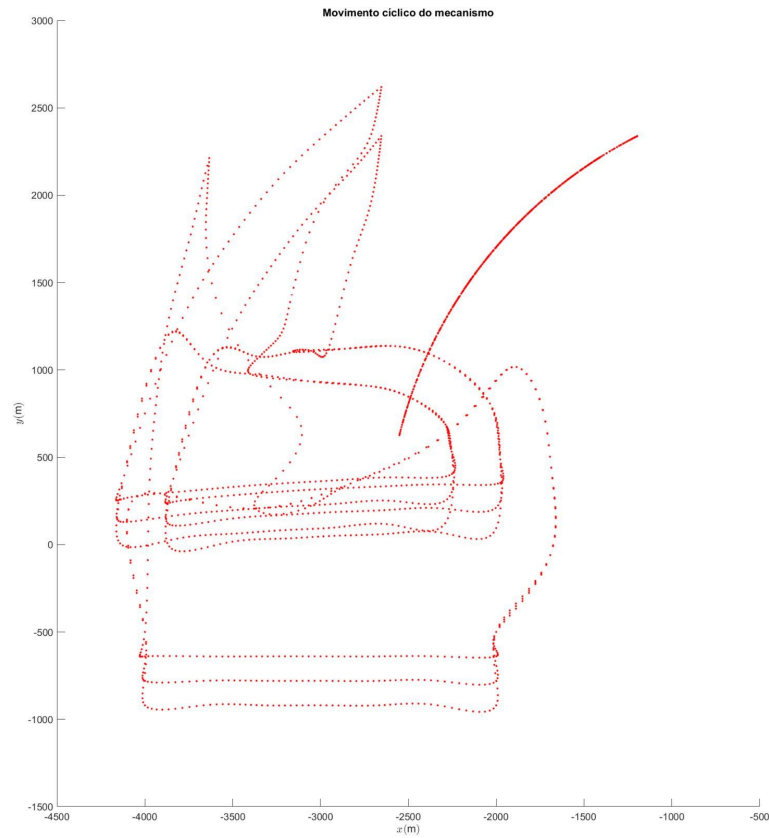
### History of the positions of the points to which the hydraulic actuators are connected



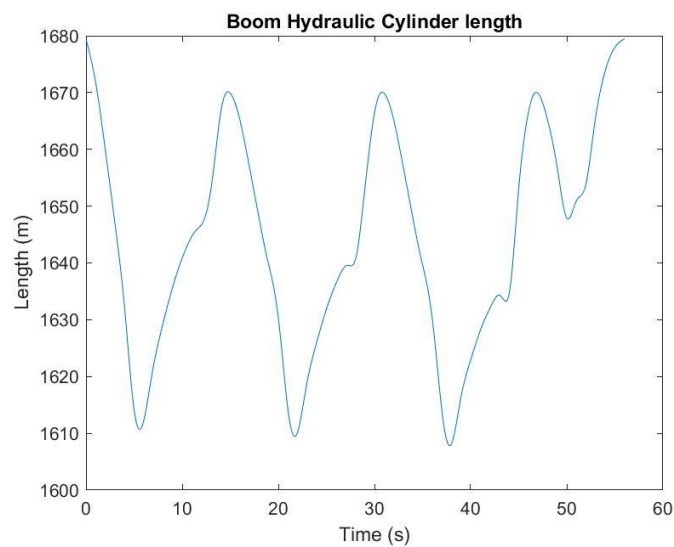
**(1.3) Plot the trajectories of the bucket, obtained with the kinematic simulation, and the length of each one of the hydraulic actuators as functions of time**

For the final question, some other plots were made:

### **Trajectory of the bucket and other joint points**

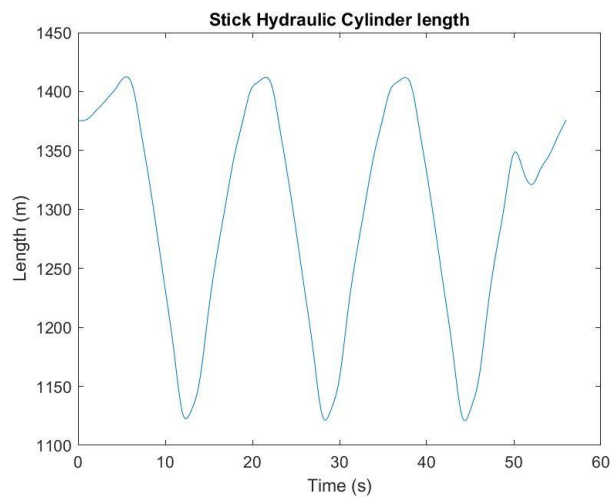


### **Length of hydraulic actuator number 1 as a function of time**

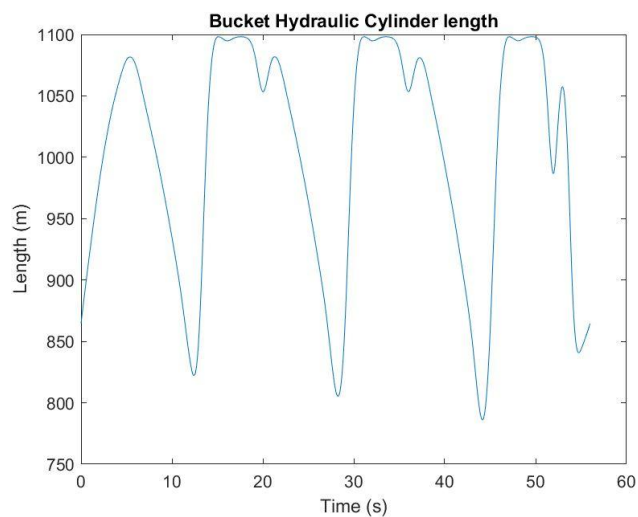




### Length of hydraulic actuator number 2 as a function of time



### Length of hydraulic actuator number 3 as a function of time



This was the code used to obtain these lengths:

```
for i = 1:length(t)
    distance_hydraulic1(i) = sqrt((Pts.Int(1).q(1,i)-Pts.Int(2).q(1,i))^2 + ...
    (Pts.Int(1).q(2,i)-Pts.Int(2).q(2,i))^2);
    distance_hydraulic2(i) = sqrt((Pts.Int(3).q(1,i)-Pts.Int(2).q(1,i))^2 + ...
    (Pts.Int(3).q(2,i)-Pts.Int(2).q(2,i))^2);
    distance_hydraulic3(i) = sqrt((Pts.Int(5).q(1,i)-Pts.Int(4).q(1,i))^2 + ...
    (Pts.Int(5).q(2,i)-Pts.Int(4).q(2,i))^2);
end
```

(2.1) Instead of driving the bucket of the excavator, drive the hydraulic actuators with point2point drivers so that the end kinematics of the bucket is that one prescribed in phase 1. Plot the bucket trajectory and orientation obtained with the new drivers together with the trajectory obtained in phase 1 (driving the bucket directly)

The driver files were made by extracting the previously calculated length of actuators as a function of time. This is the used input file and the various driver files:

```

model_excavator3.txt - Notepad
File Edit Format View Help
6 6 0 0 0 0 0 3 3 4
0 0 0
0 0 0
-1195.69 2339.01 0
-2653.95 2339.01 0
-2653.95 2619.35 6.0683
-2826.95 2339.01 0.1557
1 2 0 0 0 0
2 3 -1195.69 2339.01 0 0
3 4 -1458.26 0 0 0
3 6 -1631.26 0 0 0
4 5 0 280.34 0 0
5 6 -230 0 0 333.4
1 1 0
1 2 0
1 3 0
5 1 0 2 -100.000 0.000 -253.06 1672.45 4 4
5 2 0 3 -253.06 1672.45 -260.7 0.000 4 5
5 3 0 5 -640.43 0.000 0.000 0.000 4 6
2 -253.06 1672.45
3 -260.7 0
3 -640.43 0
5 0 0
12 0.000001
0 0.1 56

```

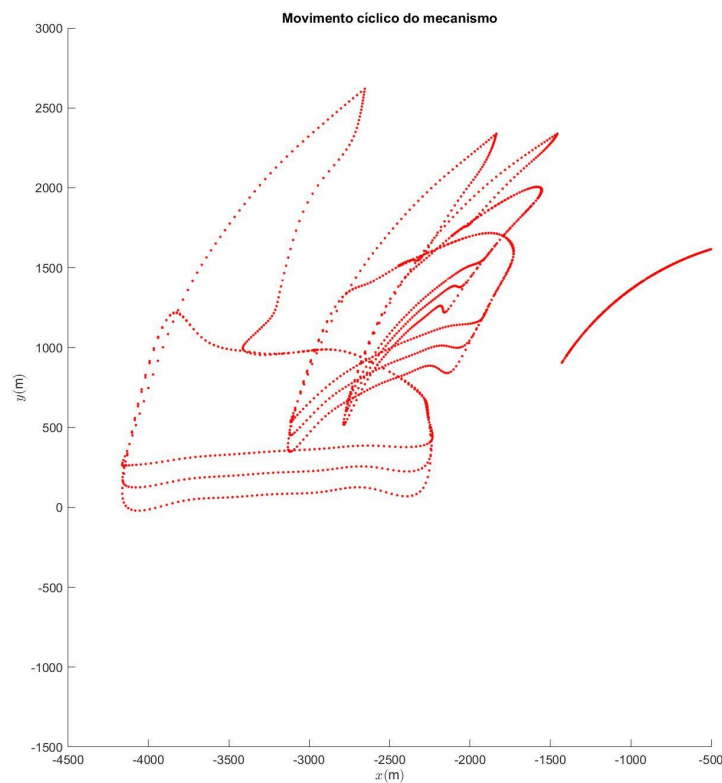


Driver_004.txt - Notepad					
File	Edit	Format	View	Help	
0		1679.43930110618			
1		1671.76722047773			
2		1659.98698923614			
3		1647.06811756293			
4		1632.30467027290			
5		1614.12282959128			
6		1612.19385650855			
7		1621.70972877355			
8		1629.30426647259			
9		1635.65162154001			
10		1640.84781477987			
11		1644.68688294431			
12		1646.71284843712			
13		1653.07587520142			
14		1666.39674576522			
15		1669.88320958969			
16		1665.20518286329			
17		1656.84432165199			
18		1647.86074402468			
19		1639.65431029230			
20		1630.29552038134			
21		1614.12282959128			
22		1610.17790962896			
23		1619.06587103417			
24		1626.09780768283			
25		1631.85865594554			
26		1636.39306608882			
27		1639.44701622775			
28		1640.49205904452			
29		1653.07587520142			
30		1666.39674576522			
31		1669.88320958969			
32		1665.20518286329			
33		1656.84432165199			
34		1647.86074402468			
35		1639.65431029230			
36		1630.29552038134			
37		1614.12282959128			
38		1608.10769785886			
39		1616.40156245357			
40		1622.89190371607			
41		1628.09035484238			
42		1631.99920505612			
43		1634.33052635033			
44		1634.51571537349			
45		1653.07587520142			
46		1666.39674576522			
47		1669.88320958969			
48		1665.20518286329			
49		1656.84432165199			
50		1647.86074402468			
51		1650.94055226238			
52		1653.93110298006			
53		1665.68436652120			
54		1673.82226805436			
55		1677.93765062438			
56		1679.43930110618			

Driver_005.txt - Notepad					
File	Edit	Format	View	Help	
0		1375.61089065913			
1		1376.29742415199			
2		1383.33202257236			
3		1391.03113874480			
4		1399.44927440932			
5		1410.04596822571			
6		1409.45351934844			
7		1375.74410944999			
8		1331.78789435077			
9		1283.24098890387			
10		1232.11748489449			
11		1179.88238880511			
12		1127.04143203156			
13		1129.77607486289			
14		1157.27966238386			
15		1215.80884425855			
16		1265.01687948026			
17		1307.34756308003			
18		1347.71720151556			
19		1378.44272004423			
20		1403.88508556018			
21		1410.04596822571			
22		1409.19054372718			
23		1375.25059020815			
24		1331.15970398502			
25		1282.49462939400			
26		1231.24827307016			
27		1178.87231071797			
28		1125.85308916423			
29		1129.77607486289			
30		1157.27966238386			
31		1215.80884425855			
32		1265.01687948026			
33		1307.34756308003			
34		1347.71720151556			
35		1378.44272004423			
36		1403.88508556018			
37		1410.04596822571			
38		1409.27411308984			
39		1375.40676714600			
40		1331.35841144467			
41		1282.73069650805			
42		1231.52321046771			
43		1179.19185476705			
44		1126.22915047937			
45		1129.77607486289			
46		1157.27966238386			
47		1215.80884425855			
48		1265.01687948026			
49		1307.34756308003			
50		1347.71720151556			
51		1334.57609921103			
52		1321.09632653158			
53		1333.32584085132			
54		1345.13024949685			
55		1361.04588660294			
56		1375.61089065913			

Driver_006.txt - Notepad					
File	Edit	Format	View	He	
0		864.531705060689			
1		924.736181389900			
2		979.523300561191			
3		1023.92154591698			
4		1056.60980238723			
5		1079.32548674141			
6		1075.34095185830			
7		1044.77583547230			
8		1011.62682093648			
9		975.359303667027			
10		934.887936390792			
11		888.786172462142			
12		833.934554575618			
13		858.508102568305			
14		1040.99787738334			
15		1097.97495531173			
16		1094.86735538030			
17		1097.61508512529			
18		1097.82053774101			
19		1086.84917769285			
20		1053.26371702354			
21		1079.32501773428			
22		1071.39989669368			
23		1038.30815455795			
24		1002.72211910249			
25		963.778432115932			
26		920.152396951264			
27		870.163941125090			
28		810.309762791239			
29		858.506491535307			
30		1040.99787738334			
31		1097.97495531173			
32		1094.86735538030			
33		1097.61508512529			
34		1097.82053774101			
35		1086.84917769285			
36		1053.26371702354			
37		1079.32501773428			
38		1067.62231772664			
39		1032.04640315424			
40		994.085469815455			
41		952.562359767402			
42		905.944930486335			
43		852.369122982359			
44		788.130462673188			
45		858.506491535307			
46		1040.99787738334			
47		1097.97495531173			
48		1094.86735538030			
49		1097.61508512529			
50		1097.82053774101			
51		1072.47130394799			
52		986.949250003113			
53		1057.41105775795			
54		901.742738829434			
55		843.612163457227			
56		864.531705060689			

The obtained trajectory plot resembles the one done with type 3 drivers:



**(2.2) Compare the angular velocities and accelerations of the arm and boom using the two types of drivers (the driven bucket in phase 1 and the point2point drivers in phase 2)**

The angular velocities and accelerations obtained in phase 1 are in blue and the ones from phase 2 are in red. As we can see, and as expected, they are extremely similar:

