

**HW 7    Due: 13 oct 2017**

1. Let  $|x|_a$  be the number of occurrences of the symbol  $a$  in the string  $x$ .
  - Define a context-free grammar for the language  $L = \{w \in \{0,1\}^* : |w|_0 = |w|_1\}$ .
  - Give a formal proof that your grammar does indeed generate  $L$ . 100
2. Define a NPDA for the language  $L = \{a^n b^m : m, n \in \mathbb{N}, m \leq n \leq 2m\}$ . 50
3. Define a NPDA for the language  $L = \{uv \in \{0,1\}^* : |u| = |v| \wedge u \neq v^R\}$ . 50