

~ I. 1 (14 Bon)

$$A = \begin{pmatrix} 6 & 7 & 3 \\ 3 & 10 & \\ 2 & 2 & 1 \end{pmatrix} \quad B = \begin{pmatrix} 2 & 0 & 5 \\ 4 & -1 & -2 \\ 4 & 3 & 7 \end{pmatrix}$$

$$1) \begin{pmatrix} 52 & 2 & 37 \\ 10 & -1 & 13 \\ 16 & 1 & 13 \end{pmatrix} - \begin{pmatrix} 22 & 24 & 11 \\ 17 & 23 & 10 \\ 47 & 45 & 12 \end{pmatrix} = \begin{pmatrix} 30 & -22 & 26 \\ -7 & -24 & 3 \\ -31 & -44 & -6 \end{pmatrix}$$

$$2) \left(\begin{array}{ccc|ccc} 6 & 7 & 3 & 1 & 0 & 0 \\ 3 & 10 & & 0 & 1 & 0 \\ 2 & 2 & 1 & 0 & 0 & 1 \end{array} \right) \sim \left(\begin{array}{ccc|ccc} 1 & 4 & 2 & 1 & -1 & -1 \\ 3 & 1 & 0 & 0 & 1 & 0 \\ 2 & 2 & 1 & 0 & 0 & 1 \end{array} \right) \sim$$

$$\left(\begin{array}{ccc|ccc} 1 & 4 & 2 & 1 & -1 & -1 \\ 0 & -11 & -6 & -3 & 4 & 3 \\ 0 & -6 & -3 & -2 & 2 & 3 \end{array} \right) \sim \left(\begin{array}{ccc|ccc} 1 & 4 & 2 & 1 & -1 & -1 \\ 0 & 1 & 0 & 1 & 0 & -3 \\ 0 & -6 & -3 & -2 & 2 & 3 \end{array} \right) \sim$$

$$\sim \left(\begin{array}{ccc|ccc} 1 & 4 & 2 & 1 & -1 & -1 \\ 0 & 1 & 0 & 1 & 0 & -3 \\ 0 & 0 & -3 & 4 & 2 & -15 \end{array} \right) \sim \left(\begin{array}{ccc|ccc} 1 & 4 & 2 & 1 & -1 & -1 \\ 0 & 1 & 0 & 1 & 0 & -3 \\ 0 & 0 & 1 & -\frac{4}{3} & -\frac{2}{3} & 5 \end{array} \right) \sim$$

$$\sim \left(\begin{array}{ccc|ccc} 1 & 4 & 0 & \frac{11}{3} & \frac{1}{3} & -11 \\ 0 & 1 & 0 & 1 & 0 & -3 \\ 0 & 0 & 1 & -\frac{4}{3} & -\frac{2}{3} & 5 \end{array} \right) \sim \left(\begin{array}{ccc|ccc} 1 & 0 & 0 & -\frac{1}{3} & \frac{1}{3} & 7 \\ 0 & 1 & 0 & 1 & 0 & -3 \\ 0 & 0 & 1 & -\frac{4}{3} & -\frac{2}{3} & 5 \end{array} \right) \Rightarrow$$

$$\Rightarrow A^{-1} = \begin{pmatrix} -\frac{1}{3} & \frac{1}{3} & 7 \\ 1 & 0 & -3 \\ -\frac{4}{3} & -\frac{2}{3} & 5 \end{pmatrix} \quad A \cdot A^{-1} = E$$

$$3) B = \begin{pmatrix} 2 & 0 & 5 \\ 4 & -1 & -2 \\ 4 & 3 & 7 \end{pmatrix} \quad |B| = 2 \cdot \begin{vmatrix} -1 & -2 \\ 3 & 7 \end{vmatrix} + 5 \cdot \begin{vmatrix} 4 & -1 \\ 4 & 3 \end{vmatrix} = 78$$

$$S^T = \begin{pmatrix} -1 & 15 & 5 \\ -36 & -6 & 24 \\ 16 & -6 & -2 \end{pmatrix}$$

$$\Rightarrow B^{-1} = \frac{1}{|B|} \cdot S^T = \frac{1}{78} \begin{pmatrix} -1 & 15 & 5 \\ -36 & -6 & 24 \\ 16 & -6 & -2 \end{pmatrix} = \begin{pmatrix} -\frac{1}{78} & \frac{5}{26} & \frac{5}{78} \\ -\frac{6}{13} & -\frac{1}{13} & \frac{4}{13} \\ \frac{8}{39} & -\frac{1}{13} & -\frac{1}{39} \end{pmatrix}$$

$$B \cdot B^{-1} = \begin{pmatrix} 2 & 0 & 5 \\ 4 & -1 & -2 \\ 4 & 3 & 7 \end{pmatrix} \cdot \begin{pmatrix} -\frac{1}{78} & \frac{5}{26} & \frac{5}{78} \\ -\frac{6}{13} & -\frac{1}{13} & \frac{4}{13} \\ \frac{8}{39} & -\frac{1}{13} & -\frac{1}{39} \end{pmatrix} = E$$

$$4) f(x) = 2x^2 - 3x + 5$$

$$f(A) = 2 \cdot \begin{pmatrix} 6 & 7 & 3 \\ 3 & 1 & 0 \\ 2 & 2 & 1 \end{pmatrix} - 3 \cdot \begin{pmatrix} 6 & 7 & 3 \\ 3 & 1 & 0 \\ 2 & 2 & 1 \end{pmatrix} +$$

$$+ 5 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} = 2 \cdot \begin{pmatrix} 6 & 7 & 3 \\ 3 & 1 & 0 \\ 2 & 2 & 1 \end{pmatrix} - 3 \cdot \begin{pmatrix} 6 & 7 & 3 \\ 3 & 1 & 0 \\ 2 & 2 & 1 \end{pmatrix} +$$

$$+ 5 \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 12 & 6 & 42 \\ 42 & 44 & 18 \\ 40 & 36 & 74 \end{pmatrix} - \begin{pmatrix} 18 & 21 & 9 \\ 9 & 3 & 0 \\ 6 & 6 & 3 \end{pmatrix} + \begin{pmatrix} 5 & 0 & 0 \\ 0 & 5 & 0 \\ 0 & 0 & 5 \end{pmatrix} =$$

$$= \begin{pmatrix} 113 & 89 & 33 \\ 33 & 46 & 18 \\ 34 & 30 & 16 \end{pmatrix}$$

✓ ii. 7 (14 ban.)

$$1) \begin{vmatrix} 2 & -3 & 7 & 4 \\ 4 & -2 & 2 & 2 \\ 6 & 7 & 8 & 9 \\ 10 & 4 & 6 & 2 \end{vmatrix} = -4 \cdot \begin{vmatrix} -3 & 7 & 4 \\ 7 & 8 & 9 \\ 4 & 6 & 2 \end{vmatrix} - 2 \cdot \begin{vmatrix} 2 & 7 & 4 \\ 6 & 8 & 9 \\ 10 & 6 & 2 \end{vmatrix} -$$

$$-2 \cdot \begin{vmatrix} 2 & -3 & 4 \\ 6 & 7 & 9 \\ 10 & 4 & 2 \end{vmatrix} + 2 \begin{vmatrix} 2 & -3 & 7 \\ 6 & 7 & 8 \\ 10 & 4 & 6 \end{vmatrix} =$$

$$= -4 \left(- \begin{vmatrix} 7 & 4 \\ 6 & 2 \end{vmatrix} + 8 \begin{vmatrix} -3 & 4 \\ 4 & 2 \end{vmatrix} - 9 \begin{vmatrix} -3 & 7 \\ 4 & 6 \end{vmatrix} \right) -$$

$$-2 \left(2 \cdot \begin{vmatrix} 8 & 9 \\ 6 & 2 \end{vmatrix} - \begin{vmatrix} 6 & 9 \\ 10 & 2 \end{vmatrix} + 4 \begin{vmatrix} 6 & 8 \\ 10 & 6 \end{vmatrix} \right) -$$

$$-2 \left(2 \begin{vmatrix} 7 & 9 \\ 4 & 2 \end{vmatrix} + 3 \begin{vmatrix} 6 & 9 \\ 10 & 2 \end{vmatrix} + 4 \begin{vmatrix} 6 & 7 \\ 10 & 4 \end{vmatrix} \right) +$$

$$+ 2 \left(2 \begin{vmatrix} 7 & 8 \\ 4 & 6 \end{vmatrix} + 3 \begin{vmatrix} 6 & 8 \\ 10 & 6 \end{vmatrix} + \begin{vmatrix} 6 & 7 \\ 10 & 4 \end{vmatrix} \right) =$$

$$= -4 \cdot 44 + 2 \cdot 774 + 2 \cdot 246 - 2 \cdot 770 = 324$$

$$2) \begin{vmatrix} 2 & -3 & 7 & 4 \\ 4 & -2 & 2 & 2 \\ 6 & 1 & 8 & 9 \\ 10 & 4 & 6 & 2 \end{vmatrix} = \begin{vmatrix} 4 & -2 & 2 \\ 6 & 1 & 9 \\ 10 & 4 & 2 \end{vmatrix} - 2 \begin{vmatrix} 2 & -3 & 4 \\ 6 & 1 & 9 \\ 10 & 4 & 2 \end{vmatrix} +$$

$$+ 8 \begin{vmatrix} 2 & -3 & 4 \\ 4 & -2 & 2 \\ 10 & 4 & 2 \end{vmatrix} - 6 \begin{vmatrix} 2 & -3 & 4 \\ 4 & -2 & 2 \\ 6 & 1 & 9 \end{vmatrix} =$$

$$= \left(4 \begin{vmatrix} 1 & 0 \\ 4 & 2 \end{vmatrix} + 2 \begin{vmatrix} 6 & 9 \\ 10 & 2 \end{vmatrix} + 2 \begin{vmatrix} 6 & 1 \\ 10 & 4 \end{vmatrix} \right) -$$

$$- 2 \left(2 \cdot \begin{vmatrix} 1 & 0 \\ 4 & 2 \end{vmatrix} + 3 \begin{vmatrix} 6 & 9 \\ 10 & 2 \end{vmatrix} + 4 \begin{vmatrix} 6 & 1 \\ 10 & 4 \end{vmatrix} \right) +$$

$$+ 8 \left(2 \cdot \begin{vmatrix} -2 & 2 \\ 4 & 2 \end{vmatrix} + 3 \begin{vmatrix} 4 & 2 \\ 10 & 2 \end{vmatrix} + 4 \begin{vmatrix} 4 & -2 \\ 10 & 4 \end{vmatrix} \right) -$$

$$- 6 \left(2 \cdot \begin{vmatrix} -2 & 2 \\ 1 & 9 \end{vmatrix} + 3 \begin{vmatrix} 4 & 2 \\ 6 & 9 \end{vmatrix} + 4 \begin{vmatrix} 4 & -2 \\ 6 & 1 \end{vmatrix} \right) =$$

$$= -264 + 2 \cdot 246 + 8 \cdot 84 - 6 \cdot 96 = 324$$

$$3) \begin{vmatrix} 2 & -3 & 7 & 4 \\ 4 & -2 & 2 & 2 \\ 6 & 1 & 8 & 9 \\ 10 & 4 & 6 & 2 \end{vmatrix} = \begin{vmatrix} 2 & -3 & 7 & 4 \\ 0 & 4 & 0 & -6 \\ 0 & 10 & 5 & -3 \\ 0 & 19 & 7 & -18 \end{vmatrix} =$$

$$= \begin{vmatrix} 2 & -3 & 7 & 4 \\ 0 & 4 & 0 & -6 \\ 0 & 0 & 5 & 12 \\ 0 & 0 & 7 & 10,5 \end{vmatrix} = \begin{vmatrix} 2 & -3 & 7 & 4 \\ 0 & 4 & 0 & -6 \\ 0 & 0 & 5 & 12 \\ 0 & 0 & 0 & 8,1 \end{vmatrix} = 2 \cdot 4 \cdot 5 \cdot 8,1 = 324$$

№ 2 (14 вар)

$$\begin{cases} 4x + 2y + z = 1 \\ x + y + z = -2 \\ 2x + y + 3z = 3 \end{cases} \quad \text{записать в матричном виде:}$$

$$\begin{pmatrix} 4 & 2 & 1 & | & 1 \\ 1 & 1 & 1 & | & -2 \\ 2 & 1 & 3 & | & 3 \end{pmatrix}$$

$$1) \begin{pmatrix} 4 & 2 & 1 & | & 1 \\ 1 & 1 & 1 & | & -2 \\ 2 & 1 & 3 & | & 3 \end{pmatrix} \sim \begin{pmatrix} 1 & 1 & 1 & | & -2 \\ 4 & 2 & 1 & | & 1 \\ 2 & 1 & 3 & | & 3 \end{pmatrix} \sim \begin{pmatrix} 1 & 1 & 1 & | & -2 \\ 0 & -2 & -3 & | & 9 \\ 0 & -1 & 1 & | & 7 \end{pmatrix} \sim$$

$$\sim \begin{pmatrix} 1 & 1 & 1 & | & -2 \\ 0 & 1 & -1 & | & -7 \\ 0 & -2 & -3 & | & 9 \end{pmatrix} \sim \begin{pmatrix} 1 & 1 & 1 & | & -2 \\ 0 & 1 & -1 & | & -7 \\ 0 & 0 & -5 & | & -5 \end{pmatrix} \sim$$

$$\sim \begin{pmatrix} 1 & 1 & 0 & | & -3 \\ 0 & 1 & 0 & | & -6 \\ 0 & 0 & 1 & | & 1 \end{pmatrix} \sim \begin{pmatrix} 1 & 0 & 0 & | & 3 \\ 0 & 1 & 0 & | & -6 \\ 0 & 0 & 1 & | & 1 \end{pmatrix} \Rightarrow \begin{cases} x = 3 \\ y = -6 \\ z = 1 \end{cases}$$

$$2) \Delta = \begin{vmatrix} 4 & 2 & 1 \\ 1 & 1 & 1 \\ 2 & 1 & 3 \end{vmatrix} = 4 \begin{vmatrix} 1 & 1 \\ 1 & 3 \end{vmatrix} - 2 \begin{vmatrix} 1 & 1 \\ 2 & 3 \end{vmatrix} + \begin{vmatrix} 1 & 1 \\ 2 & 1 \end{vmatrix} = 5$$

$$\Delta x = \begin{vmatrix} 1 & 2 & 1 \\ -2 & 1 & 1 \\ 3 & 1 & 3 \end{vmatrix} = \begin{vmatrix} 1 & 1 \\ 1 & 3 \end{vmatrix} - 2 \begin{vmatrix} -2 & 1 \\ 3 & 3 \end{vmatrix} + \begin{vmatrix} -2 & 1 \\ 3 & 1 \end{vmatrix} = 15$$

$$\Delta y = \begin{vmatrix} 4 & 1 & 1 \\ 1 & -2 & 1 \\ 2 & 3 & 3 \end{vmatrix} = 4 \begin{vmatrix} -2 & 1 \\ 3 & 3 \end{vmatrix} - \begin{vmatrix} 1 & 1 \\ 2 & 3 \end{vmatrix} + \begin{vmatrix} 1 & -2 \\ 2 & 3 \end{vmatrix} = -30$$

$$\Delta Z = \begin{vmatrix} 4 & 2 & 1 \\ 1 & 1 & -2 \\ 2 & -1 & 3 \end{vmatrix} = 4 \cdot \begin{vmatrix} 1 & -2 \\ 2 & 3 \end{vmatrix} - 2 \cdot \begin{vmatrix} 1 & -2 \\ 2 & 3 \end{vmatrix} + \begin{vmatrix} 1 & 1 \\ 2 & -1 \end{vmatrix} = 5$$

$$\begin{cases} x = \frac{\Delta x}{\Delta} = \frac{15}{5} = 3 \\ y = \frac{\Delta y}{\Delta} = -\frac{30}{5} = -6 \\ z = \frac{\Delta z}{\Delta} = \frac{5}{5} = 1 \end{cases}$$

iii. 7 (14 бар)

Сразу запишем в матричном виде:

$$\begin{pmatrix} 1 & 3 & -1 & 1 & 2 & 6 \\ 2 & -1 & 2 & -1 & -1 & 3 \\ 4 & 1 & -2 & 0 & 1 & -3 \\ 3 & -2 & -1 & -1 & -1 & -9 \\ 2 & 2 & -4 & 1 & 2 & -6 \end{pmatrix} \sim \begin{pmatrix} 1 & 3 & -1 & 1 & 2 & 6 \\ 0 & -7 & 4 & -3 & -5 & -9 \\ 0 & -11 & 2 & -4 & -7 & -27 \\ 0 & -11 & 2 & -4 & -7 & -27 \\ 0 & -4 & -2 & -1 & -2 & -18 \end{pmatrix}$$

$$\sim \begin{pmatrix} 1 & 3 & -1 & 1 & 2 & 6 \\ 0 & -7 & 4 & -3 & -5 & -9 \\ 0 & -4 & -2 & -1 & -2 & -18 \\ 0 & -11 & 2 & -4 & -7 & -27 \\ 0 & -11 & 2 & -4 & -7 & -27 \end{pmatrix} \sim \begin{pmatrix} 1 & 3 & -1 & 1 & 2 & 6 \\ 0 & -7 & 4 & -3 & -5 & -9 \\ 0 & 0 & 30 & -5 & -6 & 90 \\ 0 & 0 & 90 & -15 & -18 & 270 \end{pmatrix}$$

$$\begin{matrix} x_1 & x_2 & x_3 & x_4 & x_5 \\ \sim \begin{pmatrix} 1 & 0 & -25 & 4 & 5 & -75 \\ 0 & 1 & 8 & -7 & -7 & 27 \\ 0 & 0 & 1 & -\frac{1}{6} & -\frac{1}{5} & 3 \end{pmatrix} \sim \begin{pmatrix} 1 & 0 & 0 & -\frac{1}{6} & 0 & 0 \\ 0 & 1 & 0 & \frac{1}{3} & \frac{1}{5} & 3 \\ 0 & 0 & 1 & -\frac{1}{6} & -\frac{1}{5} & 3 \end{pmatrix} \end{matrix}$$

$$\begin{cases} x_1 = \frac{1}{6} x_4 \\ x_2 = 3 - \frac{1}{3} x_4 - \frac{3}{5} x_5 \\ x_3 = 3 + \frac{1}{6} x_4 + \frac{1}{5} x_5 \end{cases}$$

$$\begin{pmatrix} \frac{1}{6} x_4 \\ 3 - \frac{1}{3} x_4 - \frac{3}{5} x_5 \\ 3 + \frac{1}{6} x_4 + \frac{1}{5} x_5 \\ x_4 \\ x_5 \end{pmatrix} = \begin{pmatrix} 0 \\ 3 \\ 3 \\ 0 \\ 0 \end{pmatrix} + x_4 \begin{pmatrix} \frac{1}{6} \\ -\frac{1}{3} \\ \frac{1}{6} \\ 1 \\ 0 \end{pmatrix} + x_5 \begin{pmatrix} 0 \\ -\frac{3}{5} \\ \frac{1}{5} \\ 0 \\ 1 \end{pmatrix}$$

iii. 6 (14 bar)

$$A_1 = (2 \ 1 \ 2 \ 1 \ 2)^T \quad A_2 = (1 \ -1 \ 2 \ 3 \ 3)^T$$

$$B_1 = (-2 \ 3 \ 2 \ -6 \ -4)^T \quad B_2 = (2 \ -1 \ 1 \ 2 \ 0)^T$$

$$B_3 = (-1 \ 1 \ 0 \ -1 \ 1)^T$$

$$\begin{pmatrix} 2 & 1 & 2 & 1 & 2 \\ 1 & -1 & 2 & 3 & 3 \end{pmatrix} \sim \begin{pmatrix} 1 & -1 & 2 & 3 & 3 \\ 0 & 3 & -2 & -5 & -4 \end{pmatrix} \sim$$

$$\sim \begin{pmatrix} 1 & -1 & 2 & 3 & 3 \\ 0 & 1 & -\frac{2}{3} & -\frac{5}{3} & -\frac{4}{3} \end{pmatrix} \sim \begin{pmatrix} 1 & 0 & \frac{4}{3} & \frac{4}{3} & \frac{5}{3} \\ 0 & 1 & -\frac{2}{3} & -\frac{5}{3} & -\frac{4}{3} \end{pmatrix}$$

$\Rightarrow A_1$ u A_2 \Rightarrow bazis $L_1 \Rightarrow$

$$\Rightarrow \dim L_1 = 2$$

$$\begin{pmatrix} -1 & 1 & 0 & -1 & 1 \\ -2 & 3 & 2 & -6 & -4 \\ 2 & -1 & 1 & 2 & 0 \end{pmatrix} \sim \begin{pmatrix} 1 & -1 & 0 & 1 & -1 \\ 0 & 1 & 2 & -4 & -6 \\ 0 & 1 & 1 & 0 & 2 \end{pmatrix} \sim$$

$$\sim \begin{pmatrix} 1 & -1 & 0 & 1 & -1 \\ 0 & 1 & 2 & -4 & -6 \\ 0 & 0 & -1 & 4 & 8 \end{pmatrix} \sim \begin{pmatrix} 1 & -1 & 0 & 1 & -1 \\ 0 & 1 & 0 & 4 & 10 \\ 0 & 0 & 1 & -4 & -8 \end{pmatrix} \sim$$

$$\sim \begin{pmatrix} 1 & 0 & 0 & 5 & 9 \\ 0 & 1 & 0 & 4 & 10 \\ 0 & 0 & 1 & -4 & -8 \end{pmatrix} \Rightarrow B_1, B_2, \text{ u } B_3 \text{ -unm/vez} \Rightarrow$$

$$\Rightarrow \text{dim } L_2 \Rightarrow \dim L_2 = 3$$

$$\begin{pmatrix} 2 & 1 & -2 & 2 & -1 \\ 1 & -1 & 3 & -1 & 1 \\ 2 & 2 & 2 & 1 & 0 \\ 1 & 3 & -6 & 2 & -1 \\ 2 & 3 & -4 & 0 & 1 \end{pmatrix} \sim \begin{pmatrix} 1 & -1 & 3 & -1 & 1 \\ 0 & 3 & -8 & 4 & -3 \\ 0 & 4 & -4 & 3 & -2 \\ 0 & 4 & -9 & 3 & -2 \\ 0 & 5 & -10 & 2 & -1 \end{pmatrix} \sim$$

$$\sim \begin{pmatrix} 1 & -1 & 3 & -1 & 1 \\ 0 & 1 & 4 & -1 & 1 \\ 0 & 3 & -8 & 4 & -3 \\ 0 & 4 & -9 & 3 & -2 \\ 0 & 5 & -10 & 2 & -1 \end{pmatrix} \sim \begin{pmatrix} 1 & -1 & 3 & -1 & 1 \\ 0 & 1 & 4 & -1 & 1 \\ 0 & 0 & -20 & 7 & -6 \\ 0 & 0 & -25 & 7 & -6 \\ 0 & 0 & -30 & 7 & -6 \end{pmatrix} \sim$$

$$\sim \left(\begin{array}{ccccc|c} 1 & -1 & 3 & -1 & 1 & 0 \\ 0 & 1 & 4 & -1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -6 & 0 \\ 0 & 0 & 0 & 1 & -6 & 0 \end{array} \right) \sim \left(\begin{array}{ccccc|c} 1 & -1 & 3 & -1 & 1 & 0 \\ 0 & 1 & 4 & -1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -6 & 0 \\ 0 & 0 & 0 & 1 & -6 & 0 \end{array} \right) \sim$$

$$\sim \left(\begin{array}{ccccc|c} 1 & -1 & 3 & 0 & \frac{1}{7} & 0 \\ 0 & 1 & 4 & 0 & \frac{1}{7} & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -\frac{6}{7} & 0 \\ 0 & 0 & 0 & 1 & -\frac{6}{7} & 0 \end{array} \right) \sim \left(\begin{array}{ccccc|c} 1 & -1 & 0 & 0 & \frac{1}{7} & 0 \\ 0 & 1 & 0 & 0 & \frac{1}{7} & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -\frac{6}{7} & 0 \end{array} \right) \sim$$

$$\sim \left(\begin{array}{ccccc|c} x_1 & x_2 & y_1 & y_2 & y_3 & 0 \\ 1 & 0 & 0 & 0 & \frac{1}{7} & 0 \\ 0 & 1 & 0 & 0 & \frac{1}{7} & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -\frac{6}{7} & 0 \end{array} \right)$$

$\Rightarrow A_1, A_2, B_1, B_2$ none multiples \rightarrow

$$\Rightarrow \dim(L_1 + L_2) = 4$$

$$\text{QCP} \left(\begin{array}{c|c} -\frac{2}{7} & x_1 \\ -\frac{1}{7} & x_2 \\ 0 & y_1 \\ \frac{6}{7} & y_2 \\ 1 & y_3 \end{array} \right)$$

$$(A_1 \ A_2) \cdot \begin{pmatrix} -\frac{2}{7} \\ -\frac{1}{7} \end{pmatrix} = -\frac{2}{7} A_1 - \frac{1}{7} A_2 \Rightarrow$$

$\Rightarrow A_1, A_2$ -daque $L_1 \cap L_2$

$$\Rightarrow \dim(L_1 \cap L_2) = 2$$