

# **FORMULATING THE PROBLEM SPACE COMPUTATIONAL MODEL**

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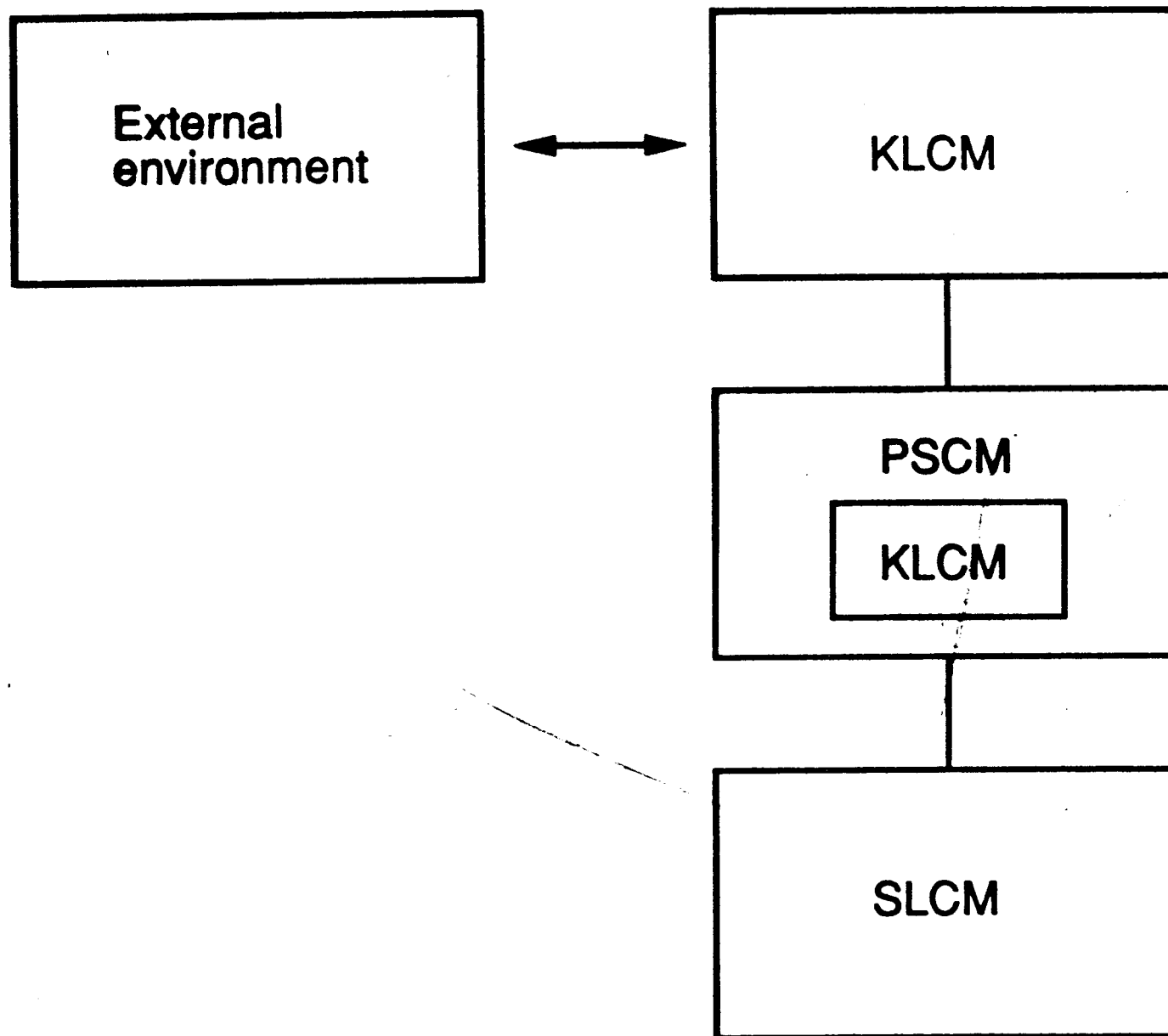
**Transparencies for CMU Soar meeting, 24 May 1990**

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1. Problem spaces. A space of states with a set of operators on states, where a task is formulated as starting at an initial state and searching for a desired state.
2. Logics. A set of clauses that describes the task situation with rules of inference to derive new clauses, where a task is formulated as proving a given theorem from a set of axioms.
3. Constraint satisfaction. A set of variables of given (often discrete) ranges subject to a set of constraints of fixed types, where a task is formulated as finding the values of the variables that satisfy the constraints and (often) optimize various functions of the variables.
4. Schemas. A hierarchical attribute-value structure with values determined by inheritance hierarchies, defaults, constraints, and attached procedures, where a task is formulated as filling out the slots of a given schema.
5. Programs. A programming language, where a task is formulated as synthesizing a program to meet a specification on the inputs, outputs and behavior. The specification is given in some formal language.
6. Plans. A (large) data base of highly abstract variabilized procedures containing subgoals to be obtained by other plans, where a task is formulated as attaining a given partially instantiated plan.
7. The big switch. A (large) data base of programs with a big index on task-relevant features, where a task is formulated by sorting it through the index and applying whatever program is obtained.

Figure 1: Candidate frameworks for formulating tasks.



**Figure 2:** Computational models involved in defining problem spaces.

- E:** An external environment  
 Exists in some state at each time  $t$   
 The agent is an object in the environment

## The agent

- A:** A set of actions  
 Can be evoked at time  $t$   
 May or may not be applicable, depending on state of  $E$   
 Affect state at next time  $t+1$
- P:** A set of perceptual devices  
 Adds knowledge of  $E$  to  $K$  at time  $t$   
 This is the only source of new knowledge
- G:** A goal
- K:** A body of knowledge  
 About the environment, goal, actions, perceptual devices

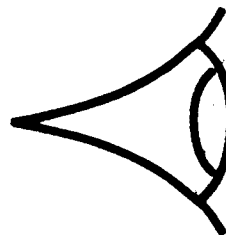
## Principles of Operation

**Rationality:** Take actions that know lead to attaining goal  
 Take  $A_t$  such that  $K_t$  and  $K(G)$  imply will-attain( $A_t$ ,  $G$ )

**Permanence:** Knowledge once acquired is available ever after  
 $P_t:K_t \rightarrow K_{t+1}$ , where  $K_{t+1}$  includes  $K_t$

**Figure 3:** The definition of a knowledge-level (KL) system

**Louie**



**G: Meet us in St. Louis**

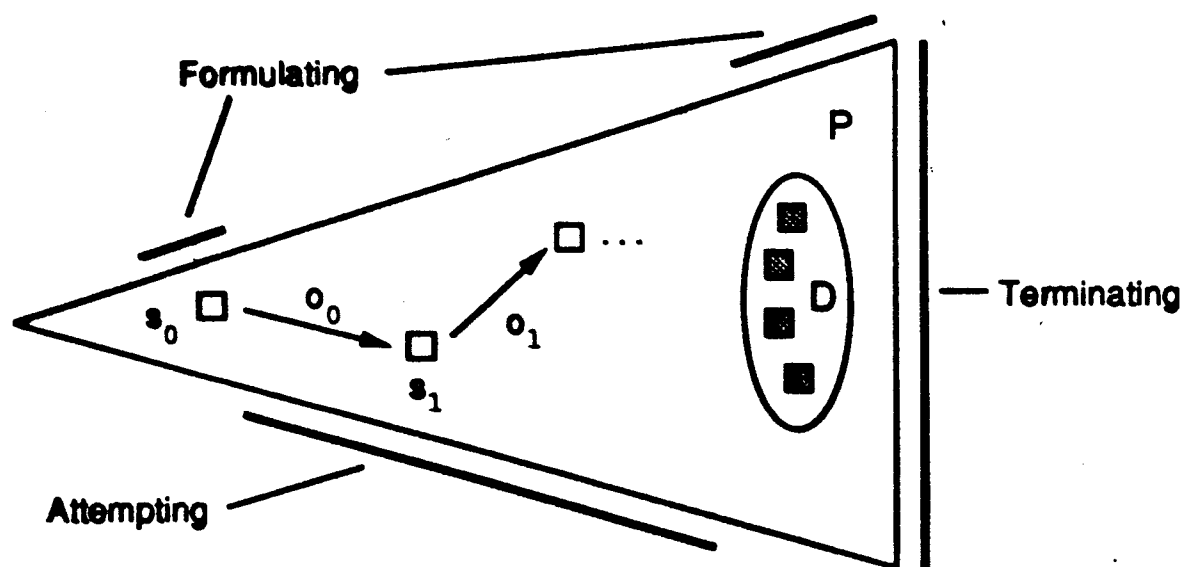
**K: Modes of transport  
Routes to St. Louis**

**...**

**Figure 4: Example KL system: an intelligent system.**

- E:** Personal computer
- G:** Prompt for a query, then respond to it
- K:** A database relating townships, electoral districts, zip codes  
The ability to retrieve on each key
- P:** Strings that represent queries  
Format: "I ; Q"  
Where I is an index, of the form:  
"D = d" or "T = t" or "Z = z"  
Where:  
d is a district number  
t is a township  
z is a zip code  
and Q is a query, of the form:  
"D = ?" or "T = ?" or "Z = ?"
- Examples:**  
Q1: "D = d; Z = ?"  
(Given district number, what are all zip codes in it?)  
Q2: "Z = z; D = ?"  
(Given zip code, what districts is it in?)
- A:** Responses sent to the printer  
Examples (from above):  
R1: List of zip codes  
R2: List of districts

**Figure 5: Example KL system: a design specification.**



A problem space  $P$  is defined by:

- $S$  A set of states
- $O$  A set of operators on  $S$ 
  - Each  $o$  in  $O$  is applicable to a subset  $S_o$  of  $S$
  - Each  $o$  realizes a function:  $o:S_o \rightarrow S$
  - Applying  $o$  to a state in  $S_o$  produces a new state in  $S$

Behavior occurs in problem space  $P$  by consecutive steps:

The step at  $i$  starts with the system at current state  $s_i$

Each step has two phases:

**Selecting:** The current operator  $o_i$  is selected from  $O$

**Applying:** The operator  $o_i$  is applied to  $s_i$   
 If  $o_i$  is applicable, the current state at  $i+1$  is  $o_i(s_i)$   
 If  $o_i$  is not applicable, still remain at  $s_i$

A task is formulated using a problem space by:

**Determining-space:** A problem space  $P$  is adopted

**Goal-setting:** A set of desired states  $D$  is adopted

**Initializing:** The state  $s_0$  becomes the current state

A formulated task is attempted by:

**Solving:** Steps are taken in the space

**Independence principle:** Any operator that can be applied, may be applied

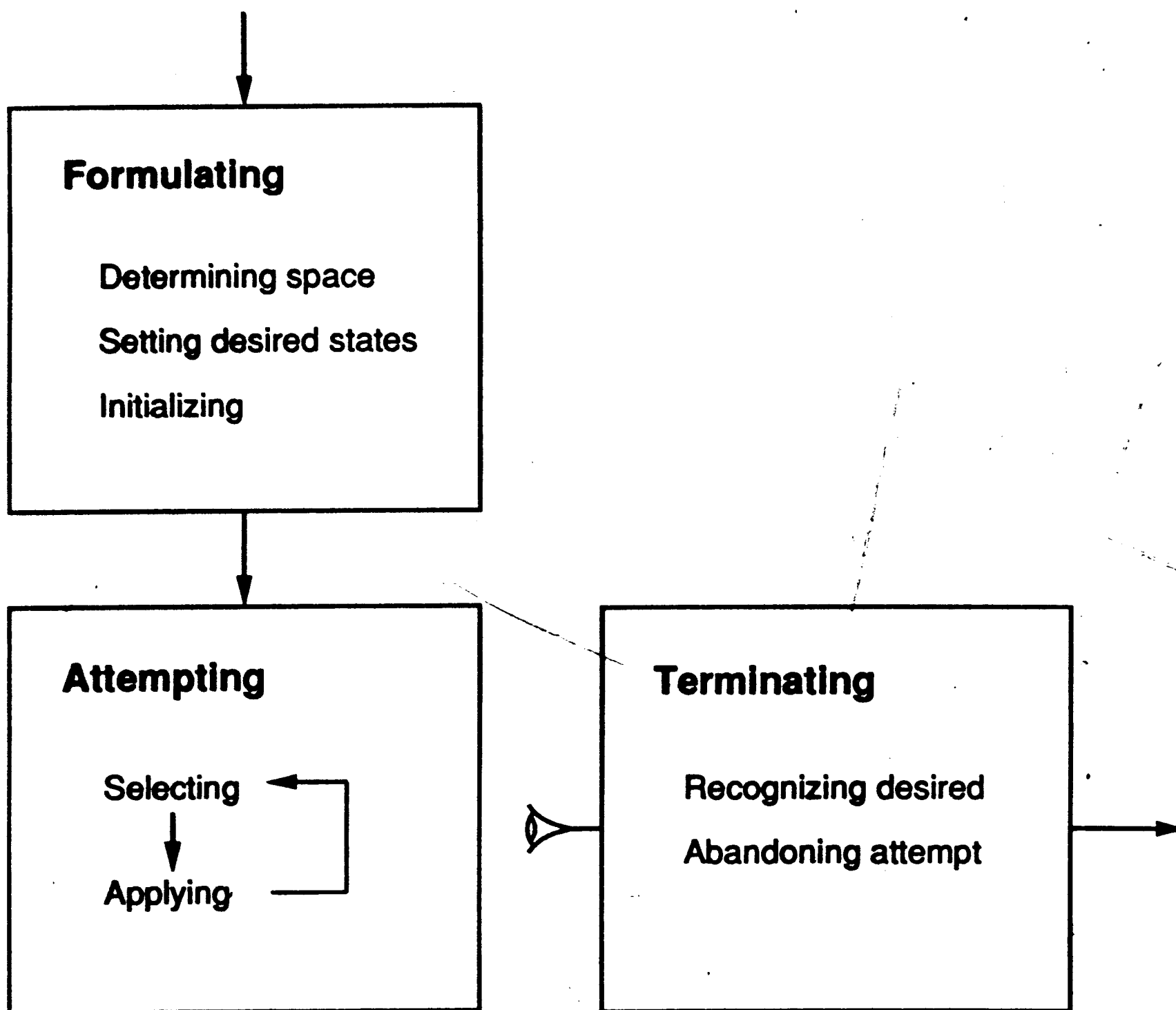
**Terminating:** The task attempt is terminated

If the current state  $s_i$  is in  $D$

If  $s_i$  cannot be brought to be in  $D$

Figure 6: Definition of a problem space





**Figure 7:** Problem space processes.

<b>Environment</b>	The inner computational context of an agent.
<b>Formulate-task</b>	
Goal	To formulate a task by using a problem space
Actions	Produce $P$ (the problem space), $D$ , $s_0$
Perceptions	Of the current context, the impulse situation
Knowledge	About problem spaces, the current context
<b>Select-operator</b>	
Goal	To select $o_i$ to reach a state in $D$
Actions	Produce $o_i$
Perceptions	Of $s_i$
Knowledge	About $P$ , $s_0$ and $D$
<b>Apply-operator</b>	
Goal	To apply $o_i$ to $s_i$
Actions	Produce $o_i(s_i)$
Perceptions	Of $o_i$ and $s_i$
Knowledge	About the conditions of applicability of $o_i$ , the function $o:S \rightarrow S$
<b>Terminate-task</b>	
Goal	To stop attempt if $s_i$ in $D$ or if cannot succeed
Actions	Stop processing
Perceptions	Of $P$ , $D$ , $o_i$ , and $o_i(s_i)$ for the current $i$
Knowledge	About the current context

**Figure 8:** Knowledge-level specification of problem-space components.

**System Specification****Name:** Job-shop-scheduler**State:**

Time slots: 1, 2, 3

Objects: A, B

Schedule: (&lt;object&gt;, &lt;machine&gt;, &lt;timeslot&gt;), ...

**S<sub>0</sub>:**

A: rough, triangular, no holes

B: spherical, no holes, surface undetermined

**D:**

A: cylindrical, polished, size 2 hole

B: cylindrical, polished, no holes

**Operators:****Lathe (what when)**

Preconditions: none

Effects: cylindrical, rough

**Punch (what when size)**

Preconditions: unheated or rectangular

Effects: rough, hole

**Polish (what when)**

Preconditions: unheated or rectangular

Effects: smooth

**Roll (what when)**

Preconditions: none

Effects: cylindrical, hot, surface undetermined

**Operator selection:**

Rule out all unhelpful operators

Those that do not achieve a desired characteristic

Punch before rolling

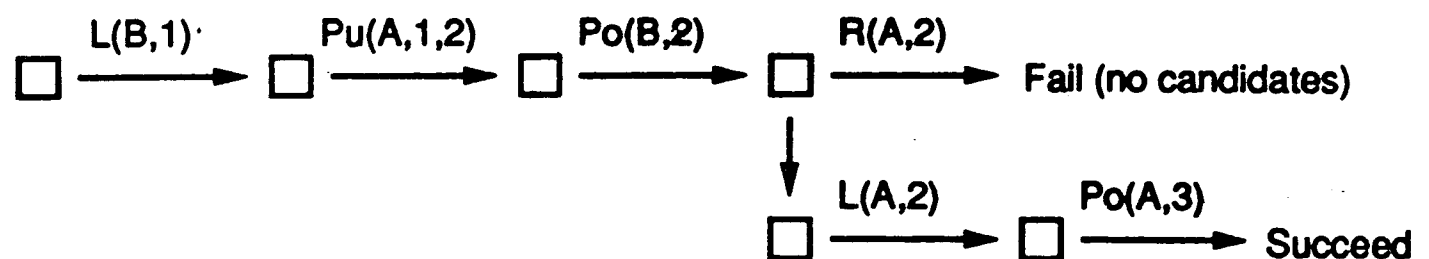
Rolling heats the object so it cannot be punched

Punch or lathe before polishing

Punch and lathe leave an object rough

Try earlier time slots first

Choose randomly among undifferentiated candidates

**Behavior on the task****Figure 9:** Example of a problem-space system.

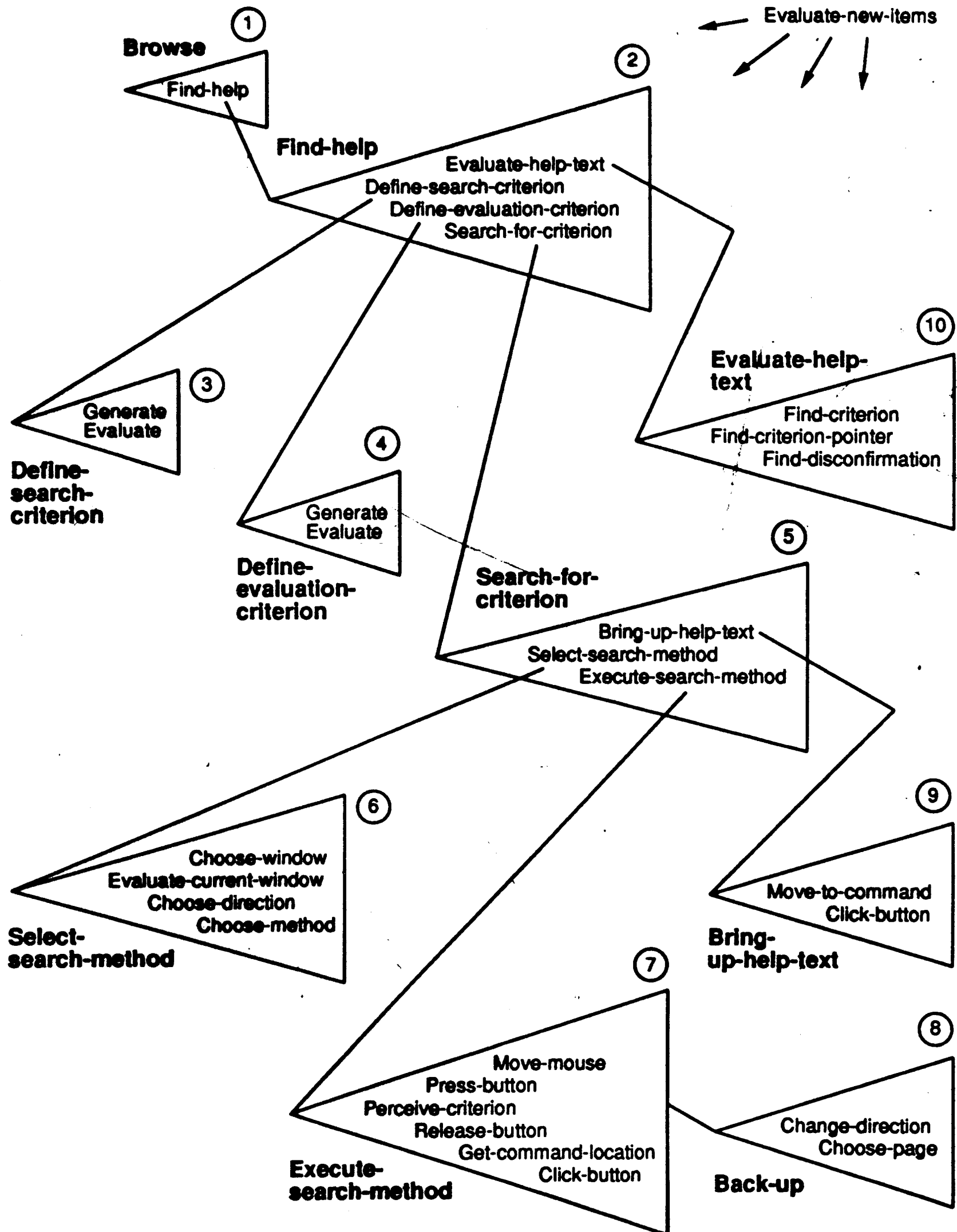
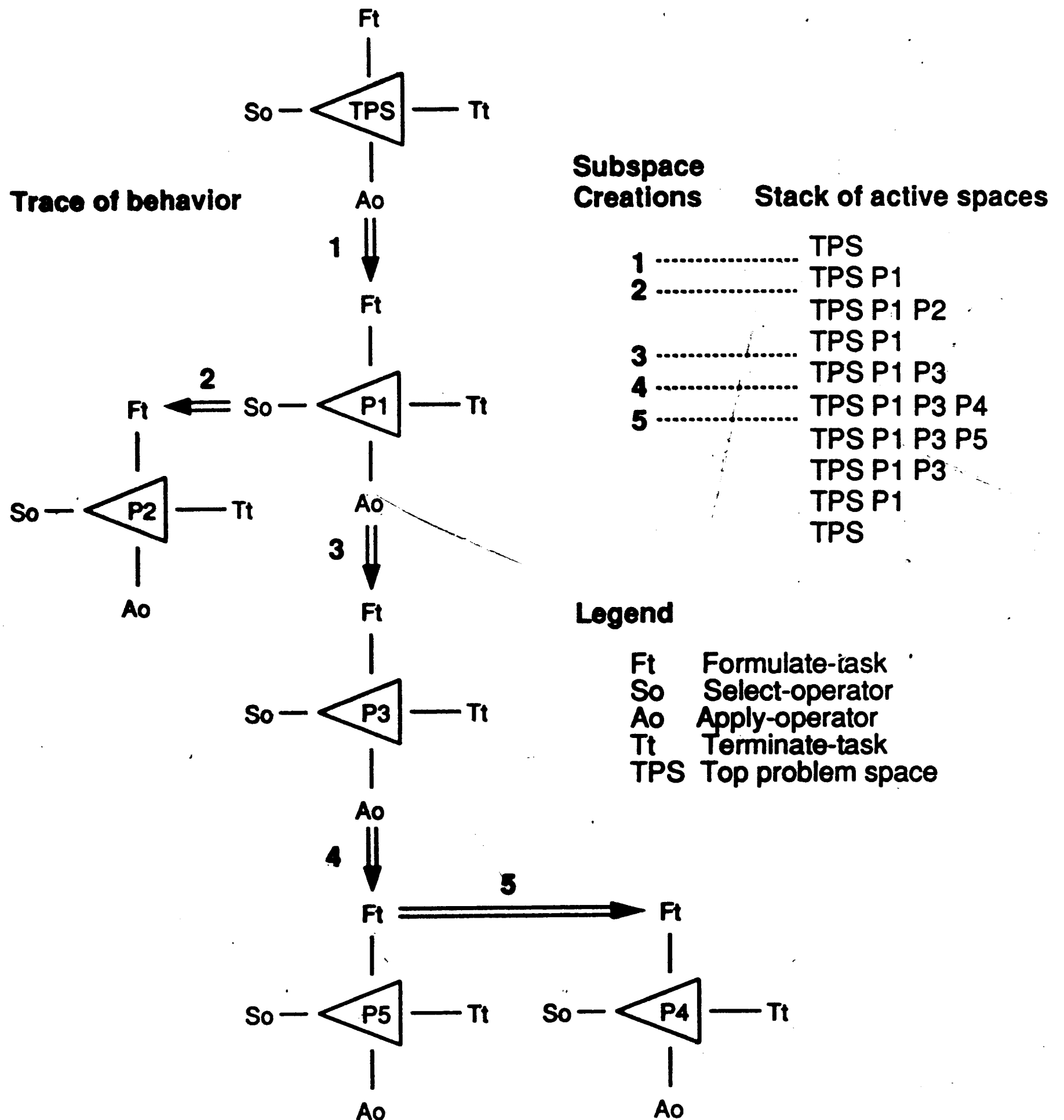


Figure 12: Problem-space trace of Browser-Soar



**Figure 13: Operational details of PSCM operation**

**Instructions:**

1. Read four premises.
2. Then read a statement.
3. If the statement is true say "true".
4. Then stop.

**The specific task:**

5. A plate is left of a knife.
6. A fork is left of the plate.
7. A jug is above the knife.
8. The fork is below a cup.
9. The cup is left of the jug.

**The system should answer:**

10. True.

**Figure 14: Simple instruction-taking (by Soar)**