

Part III

Small network, high performance

Bacteria chemotaxis

based on pioneered works by Howard Berg and others

Week 5-6

Cell chemotaxis

- Chemotaxis (from chemo- + taxis) is movement of an organism in response to a chemical stimulus.
- Is precisely controlled in many developmental and physiological processes
- The underlying biochemical network has been gradually deciphered
- Correlation between biochemical reactions and precise control required systems biology approaches

Examples of chemotaxis

1. Neutrophil: eating bacteria



Examples of chemotaxis

1. Neutrophil: how to find bacteria, fungi

**Chemotactic and phagocytic
response of a micropipette-held
human neutrophil to zymosan**

Heinrich & Lee, *JCS* 2011

Zymosan is a
glucan from the
surface of fungi

Examples of chemotaxis

1. Neutrophil: how to find bacteria, fungi



Neutrophil chasing
bacterium
*Sensing LPS
produced by bacteria*

Examples of chemotaxis

**1. Neutrophil: how to call for reinforcement?
Secreting chemokines that attract other
neutrophils**



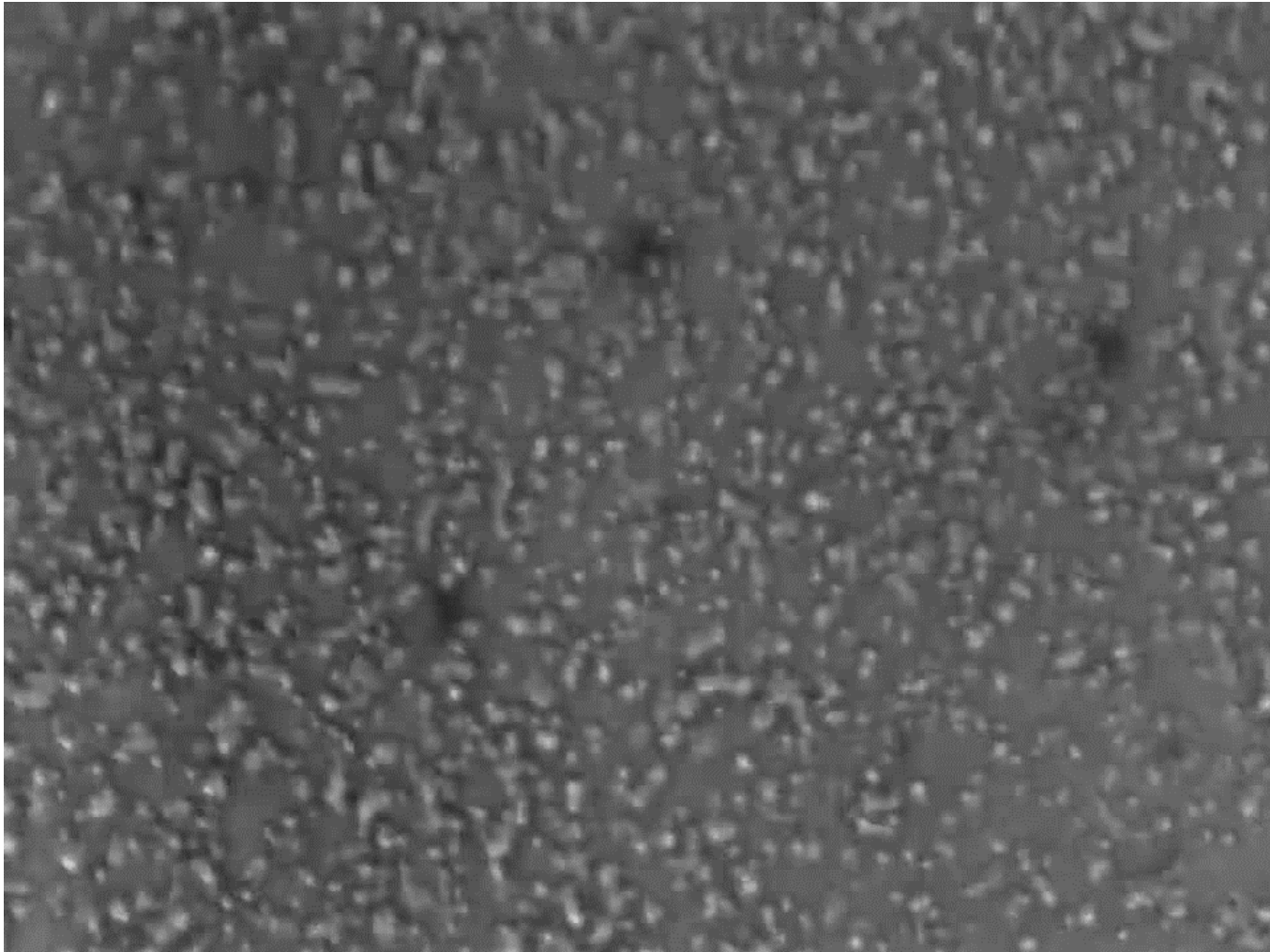
Examples of chemotaxis

2. Dictyostelium: moving towards high concentration of cAMP



Examples of chemotaxis

2. Dictyostelium: what does it for?

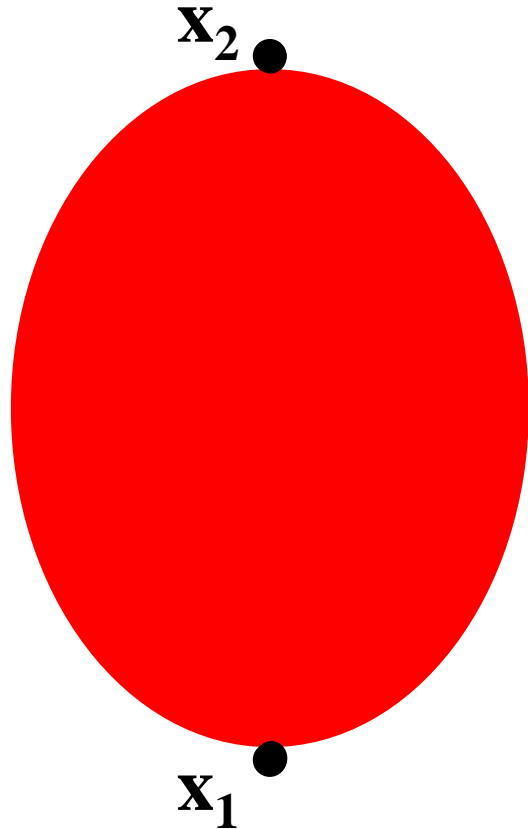


Examples of chemotaxis

2. Dictyostelium: what does it for?



How do they find the direction of high concentration chemoattractants?



Spatial Sensing

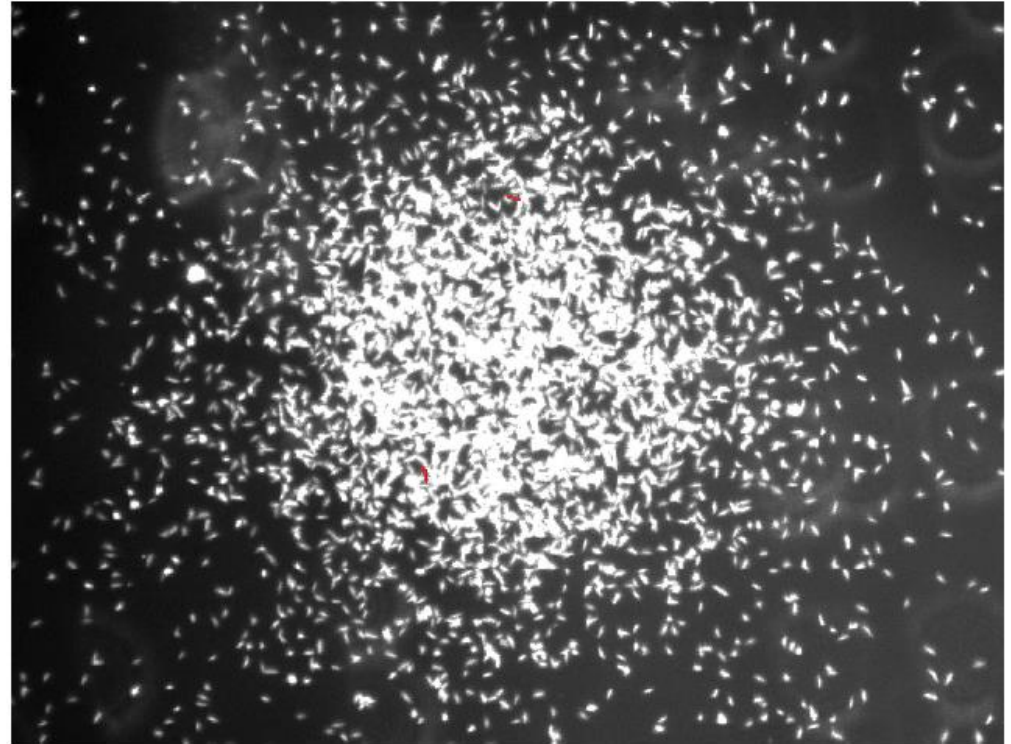
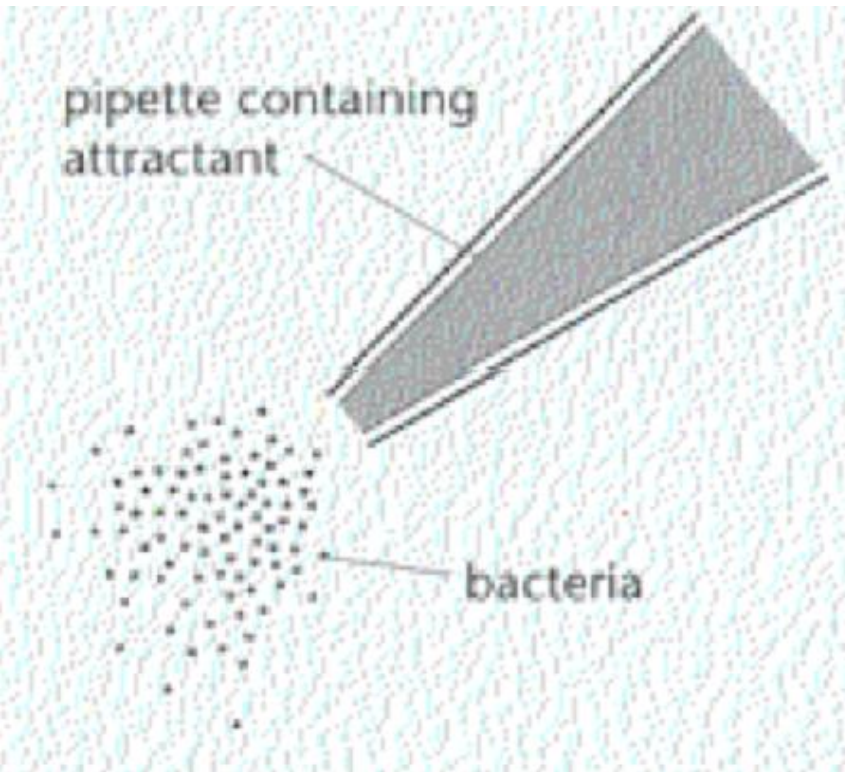
$$\frac{C(x_2) - C(x_1)}{x_2 - x_1} = \frac{dC}{dx}$$

if $\frac{dC(x_2)}{dx} > 0$, shmoo in direction of x_2

Challenge: how to find it in shallow gradient:
~1% difference between front and back?

An biochemically simplest example of chemotaxis

Bacteria finding food (e.g. aspartate, glucose) in the wild



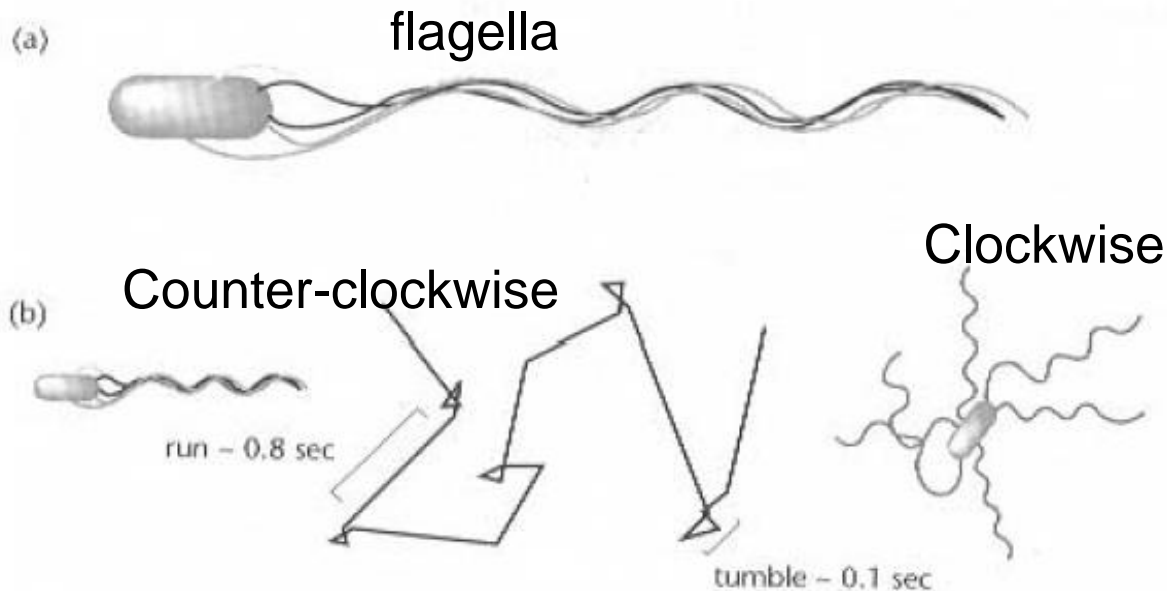
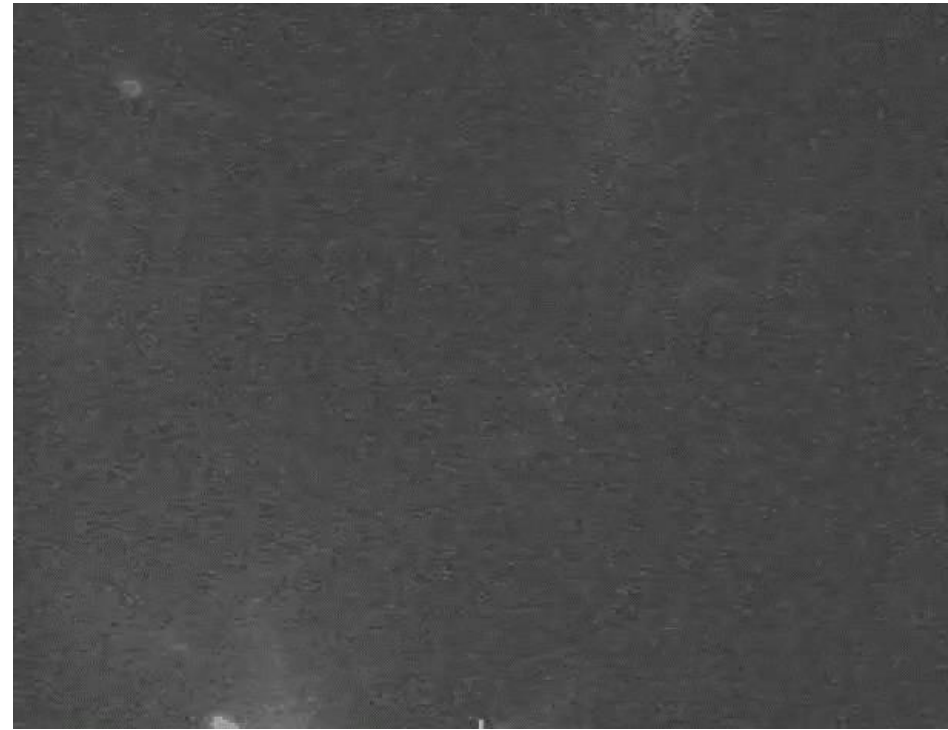
The length of a bacteria ($\sim 1\mu\text{m}$) is much smaller than eukaryotic cell ($\sim 10\mu\text{m}$), spatial sensing of gradient is even harder.

How does it achieve this?

Bacteria movement

When swimming, the cell travels in a straight line for about 1 sec, travels about $30\mu\text{m}$. When tumbling, the cell changes on average by 60 degrees.

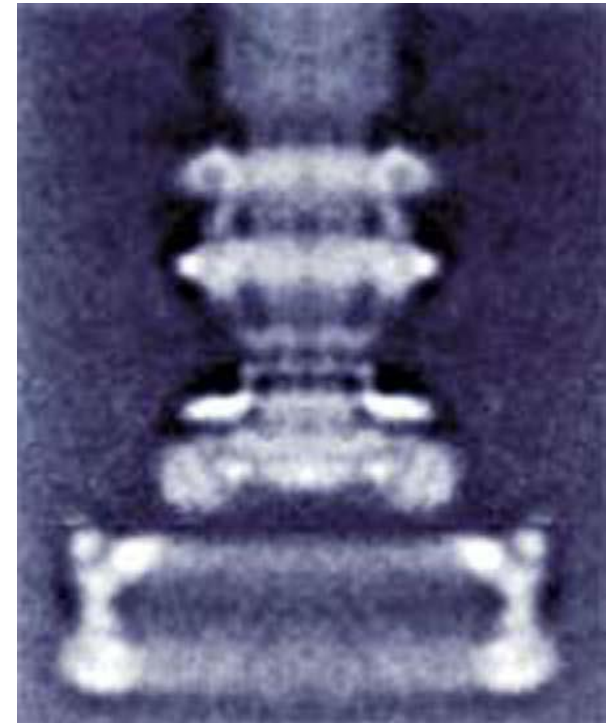
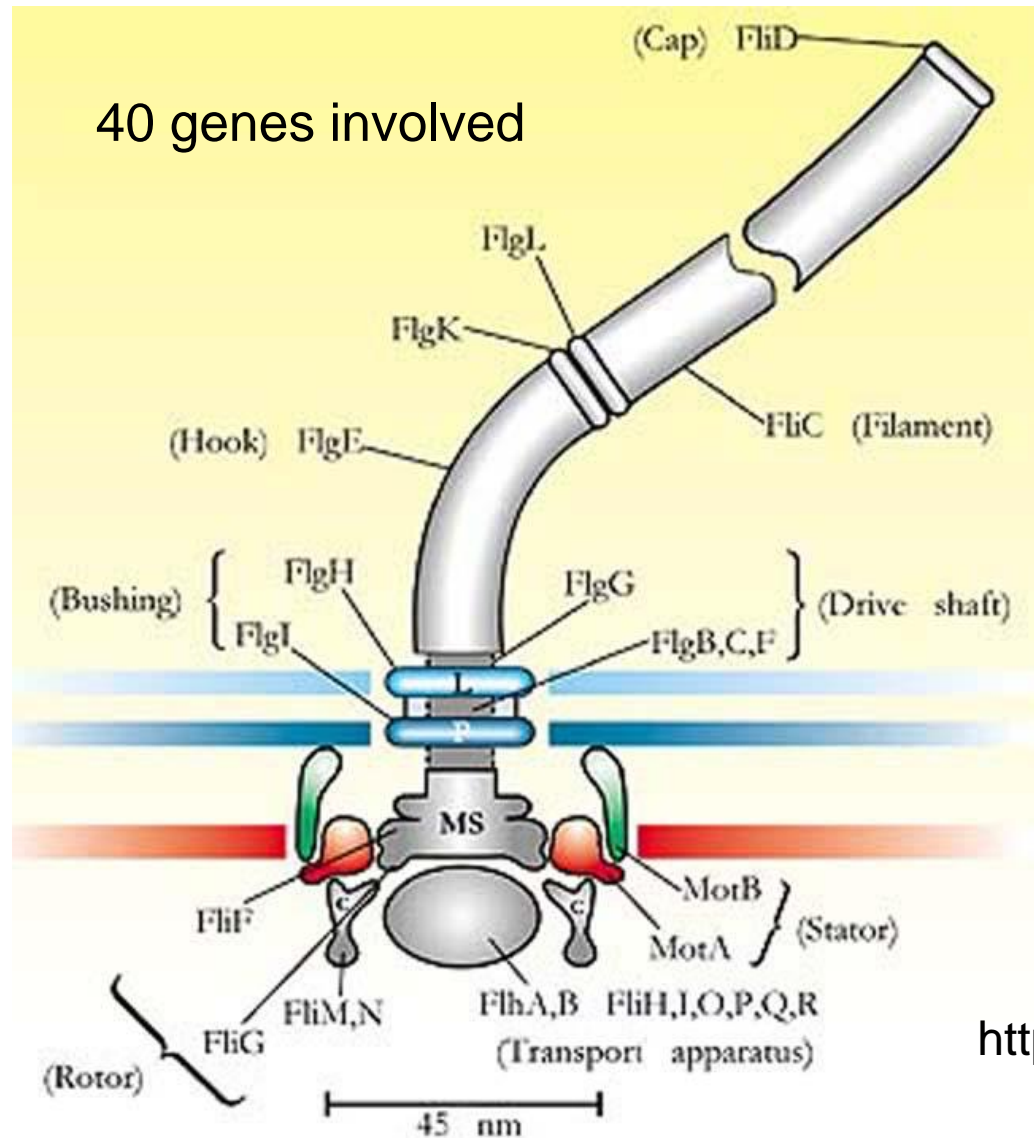
cell length $\sim 3\mu\text{m}$, diameter $\sim 1\mu\text{m}$



Flagella is labeled with conjugated fluorescent dye, and imaged with high speed fluorescent microscopy.

Turner and Berg, 2000

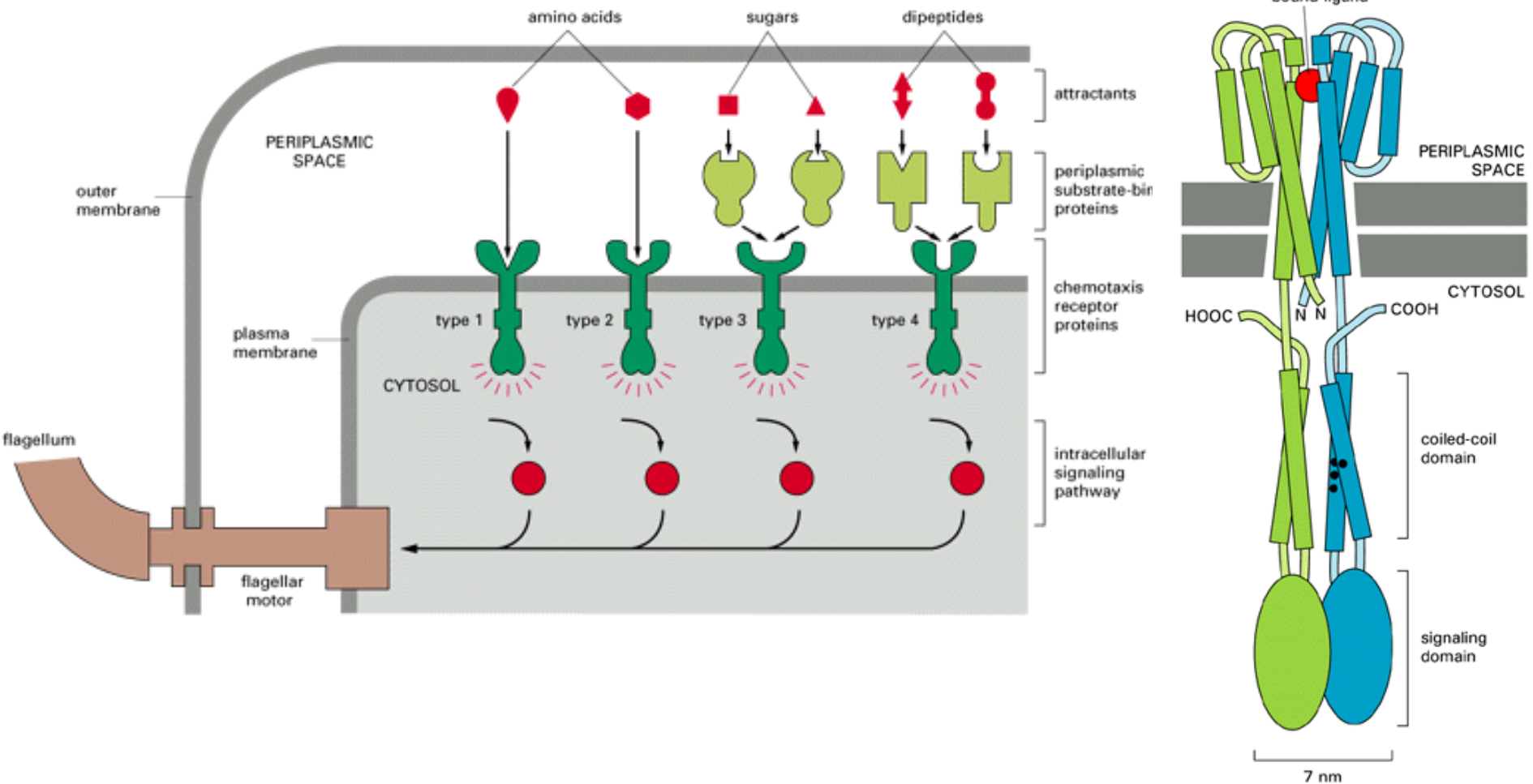
Structure of the flagella machinery



<http://www.aip.org.pt/jan00/berg.htm>

Rotary 8 cylinder motor driven by protonmotive force (400 steps/rev)

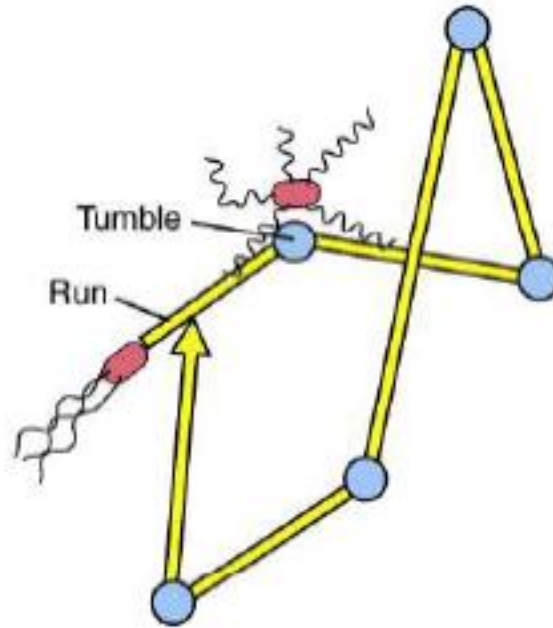
Receptors sensing chemoattractants



Classes of Chemoreceptors

- Originally called methyl-accepting chemotaxis proteins (MCPs)
- Four Types:
 - tsr (MCP I)
 - tar (MCP II) (important, binds aspartate)
 - trg (MCP III)
 - tap (MCP IV)
- Mainly differ in periplasmic domain

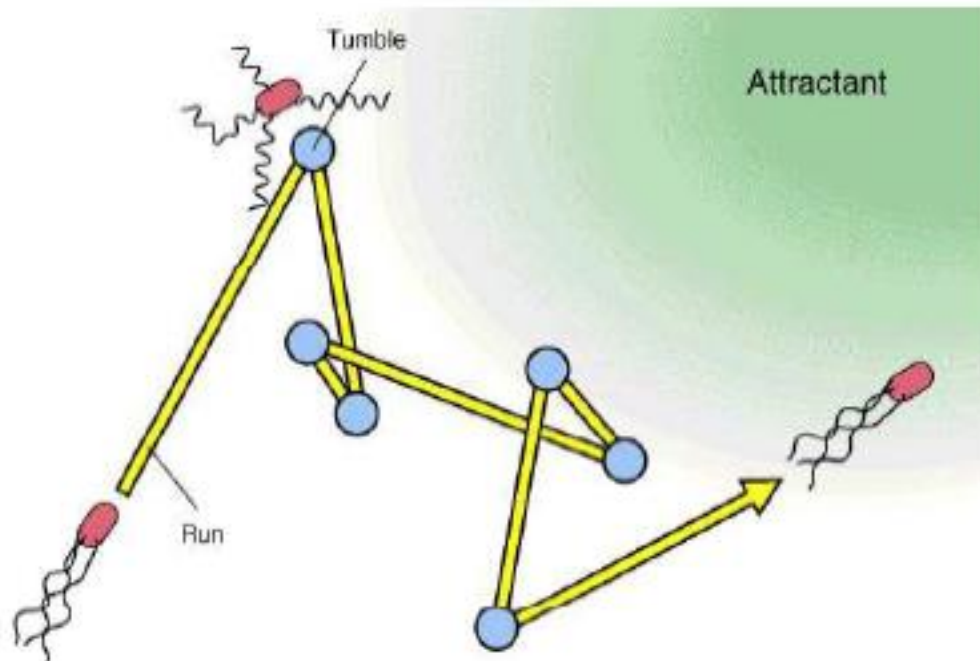
Absence of chemical attractant



Since bacteria cannot move straight and is too small to directly sense the spatial gradient, how does it perform chemotaxis?

The higher the attractant concentration, the lower probability of tumbling.

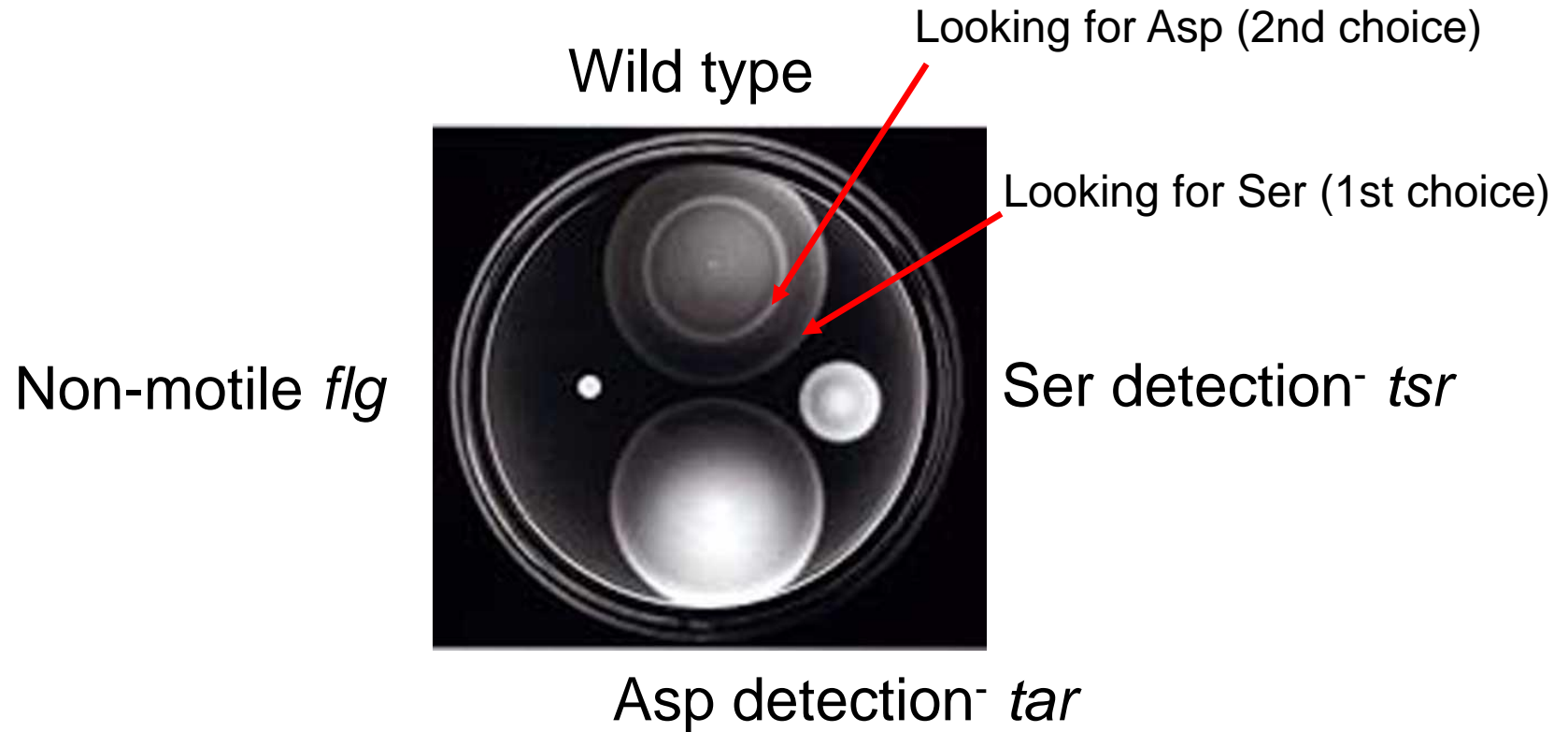
Presence of chemical attractant



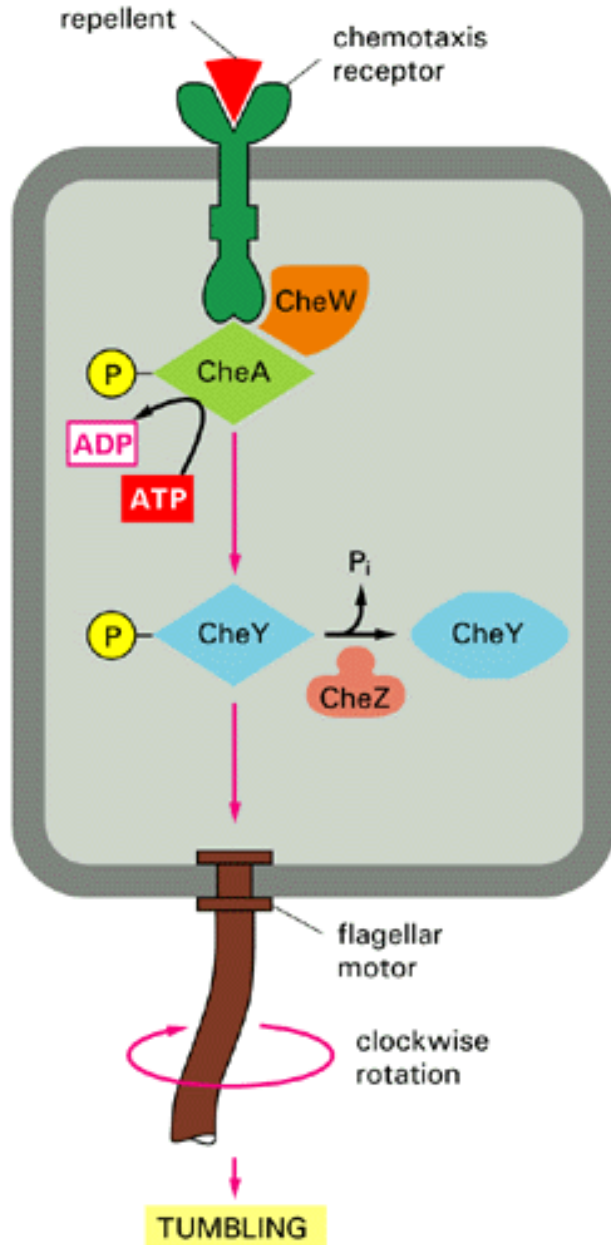
chemical gradient sensed in a temporal manner

Mutational approaches to tease out genes mediating chemotaxis

Plate contains serine and aspartate



The biochemical network performing the task



Counter-Clockwise = straight swim,
bundled flagella

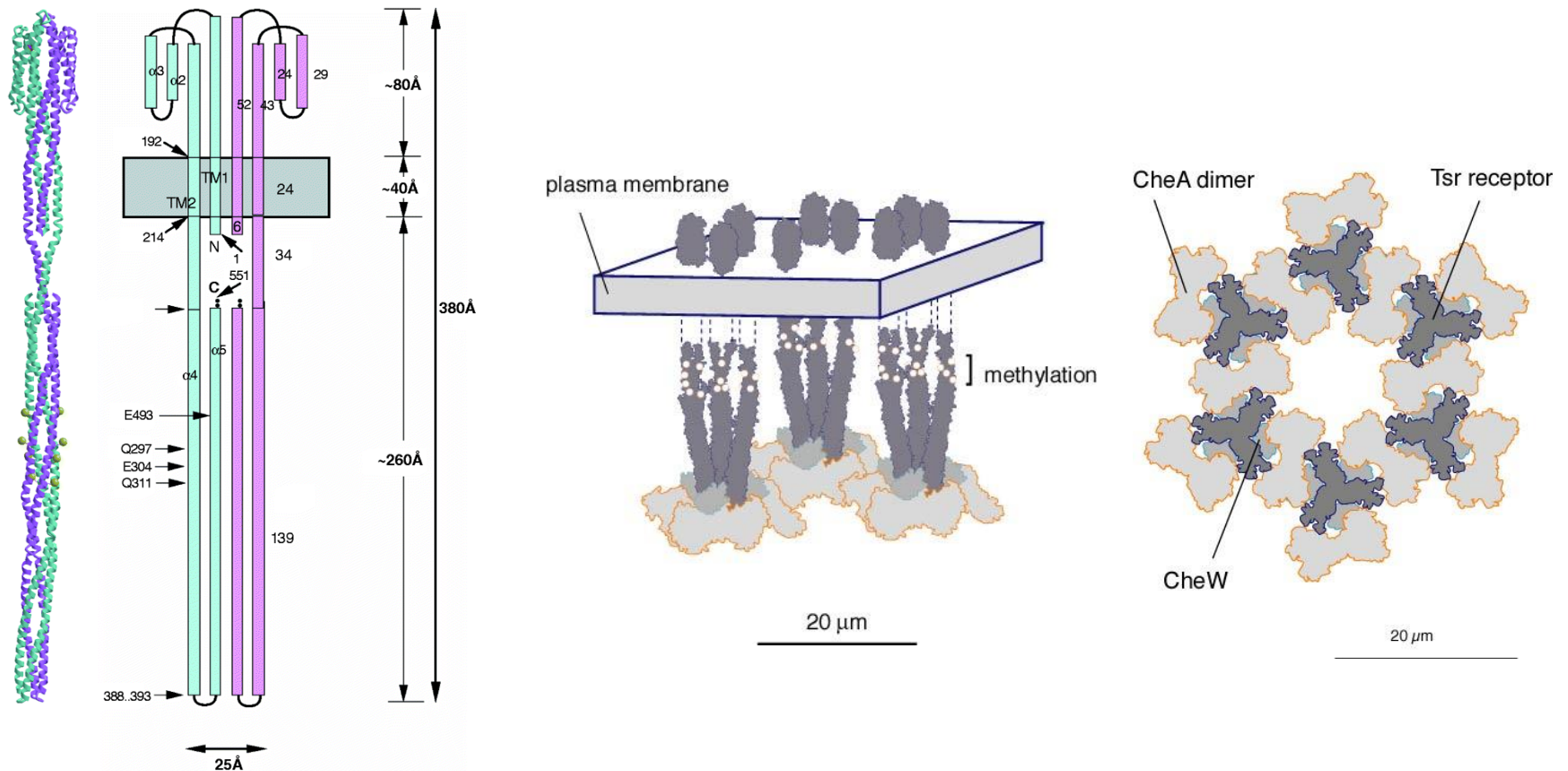
Clockwise = tumble, separate flagella

CheY-P binding to motor → CW rotation

↑ Repellent → ↑ CheA-P → ↑ CheY-P → ↑ CW

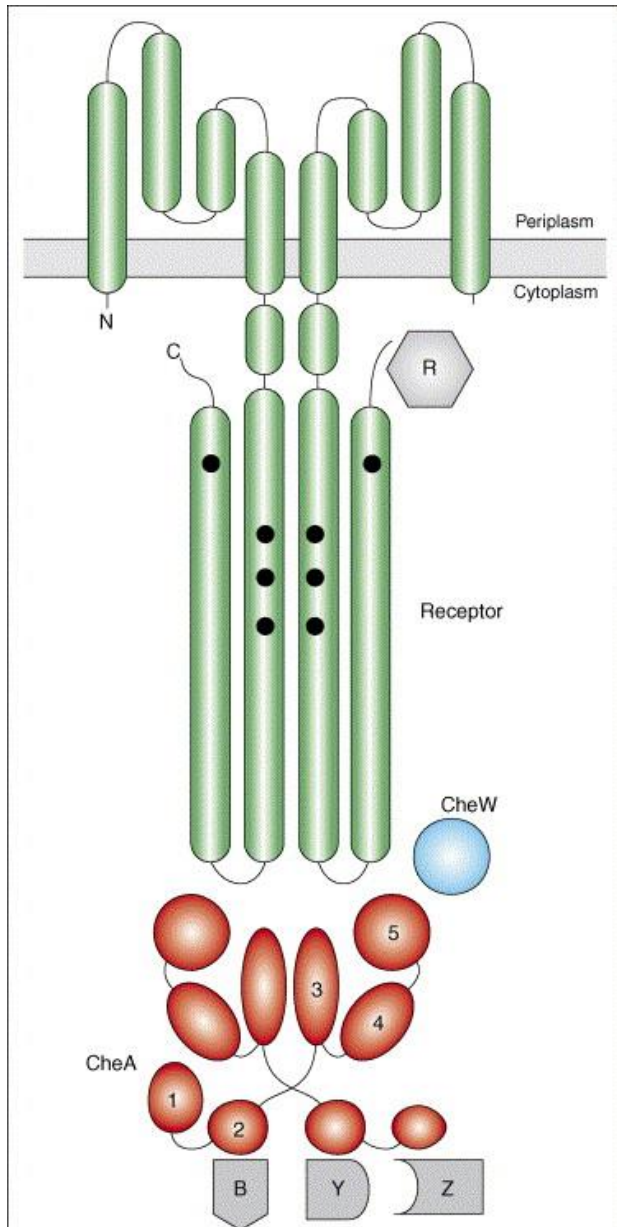
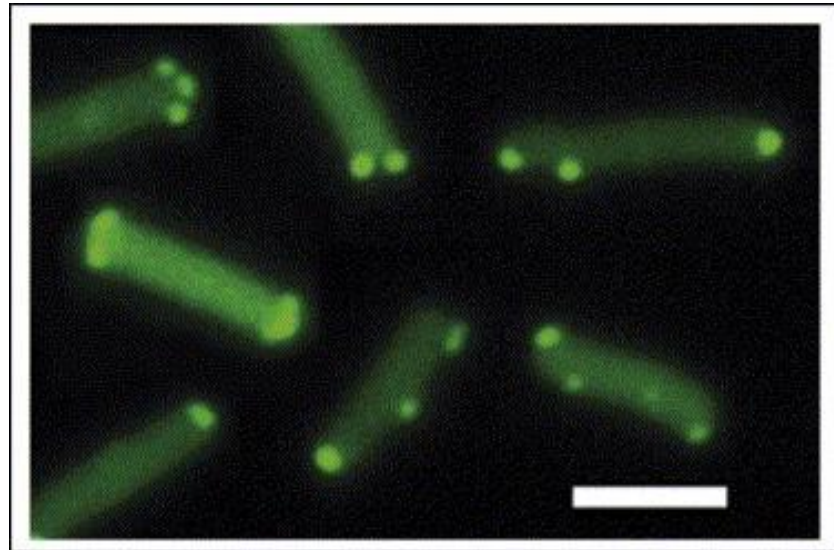
↑ Attractant → ↓ CheA-P → ↓ CheY-P → ↓ CW

The spatial organization of chemotaxis receptors

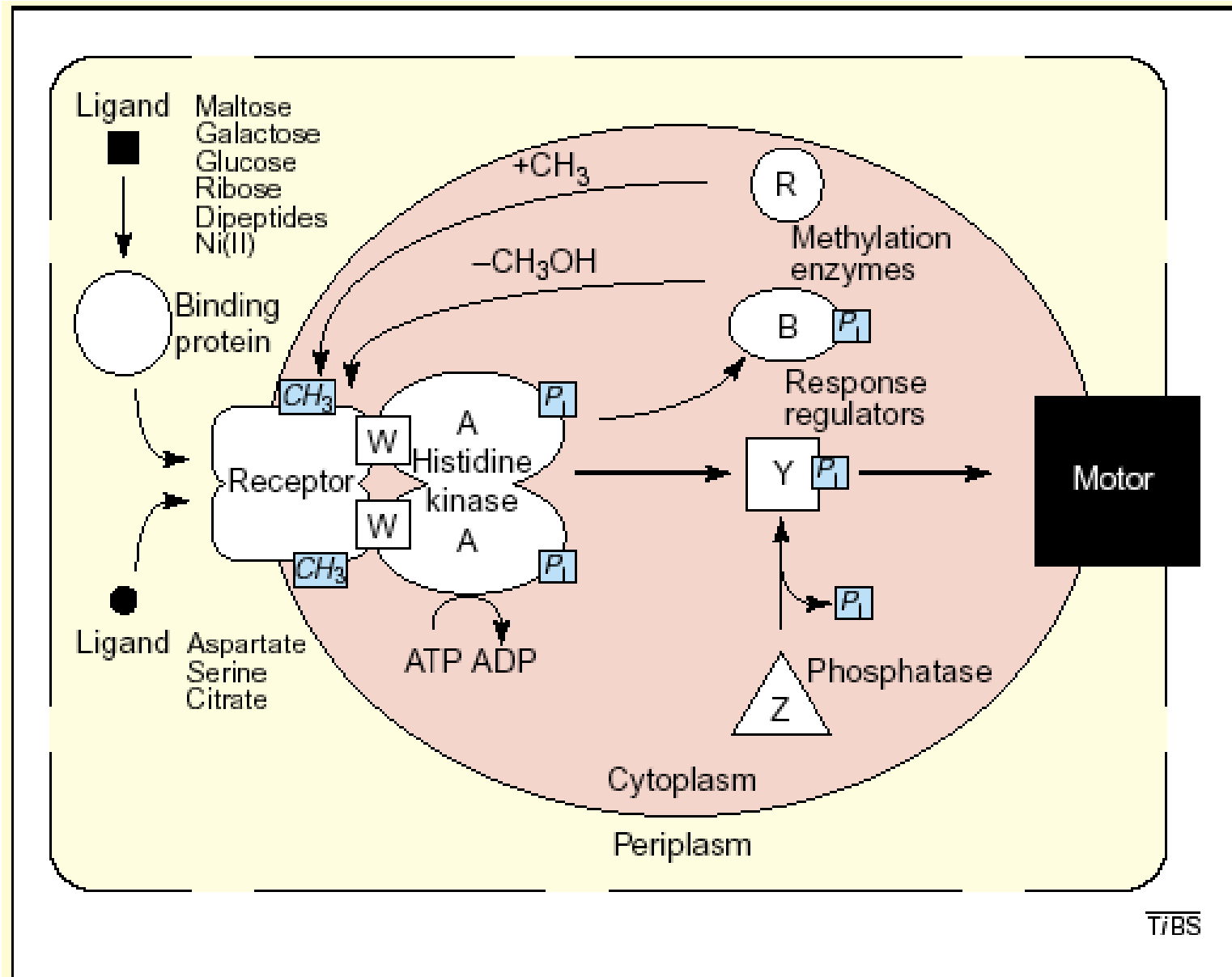


Receptor Localization

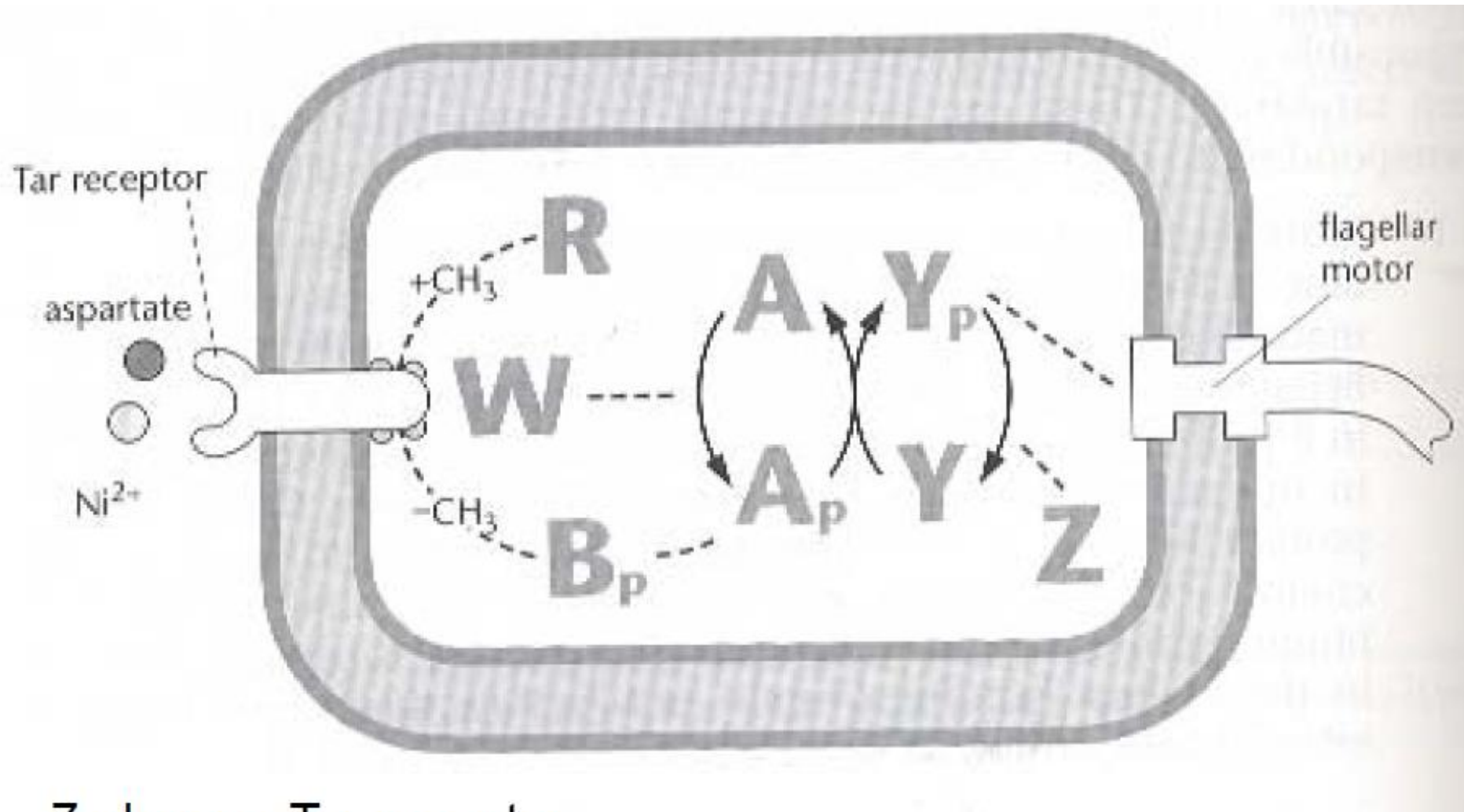
Kentner and Sourjik



The entire chemotactic network



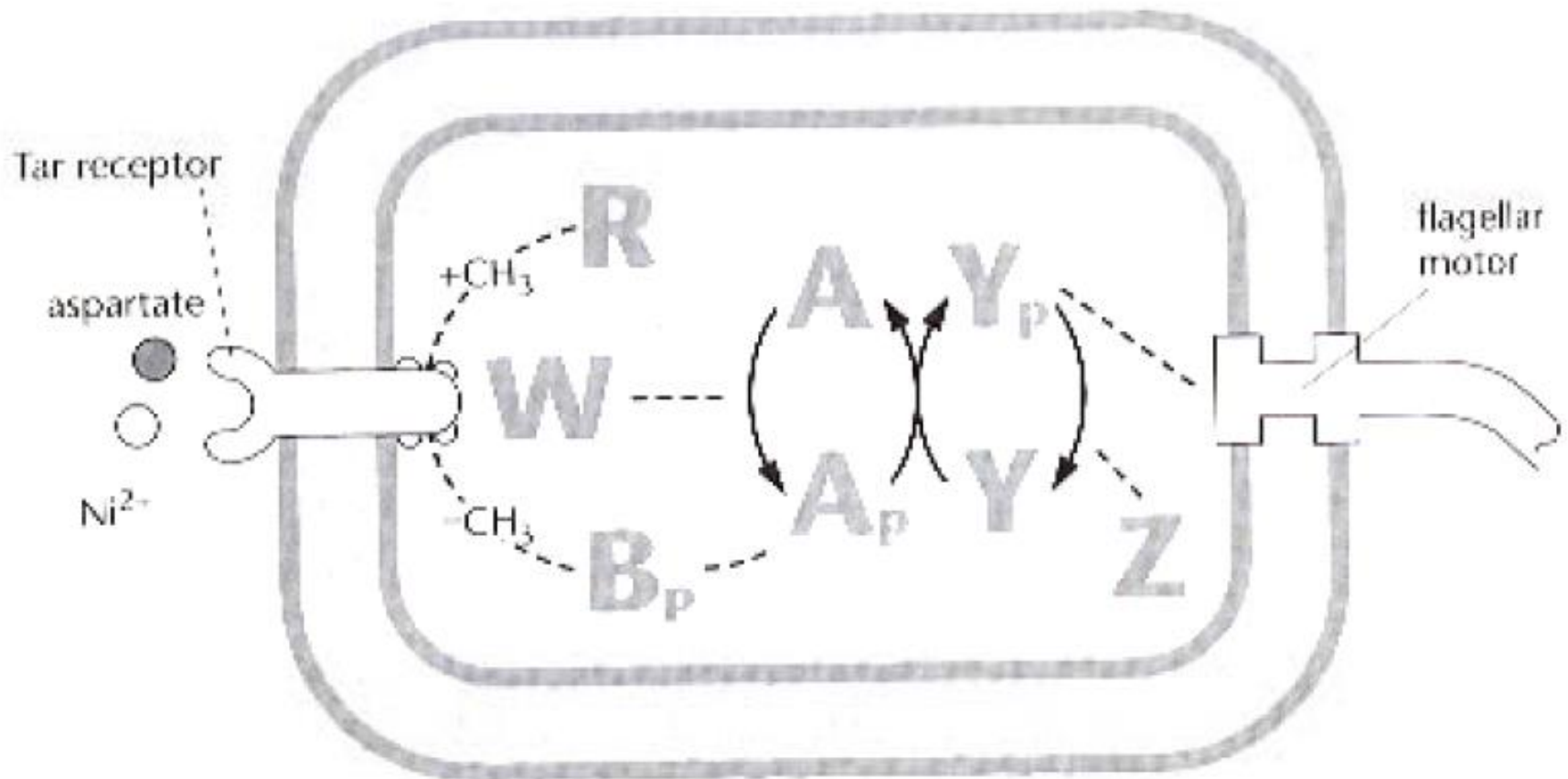
Simplified drawing of the chemotactic network



7 players: Tar receptor,
CheA, CheB, CheR, CheW, CheY, CheZ

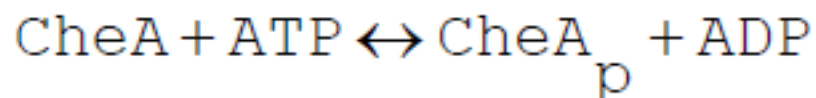
Proteins in the network can be post-translational modified in different ways

- I Phosphorylation (CheA, CheY, CheB)
- II Methylation (Tar receptor)



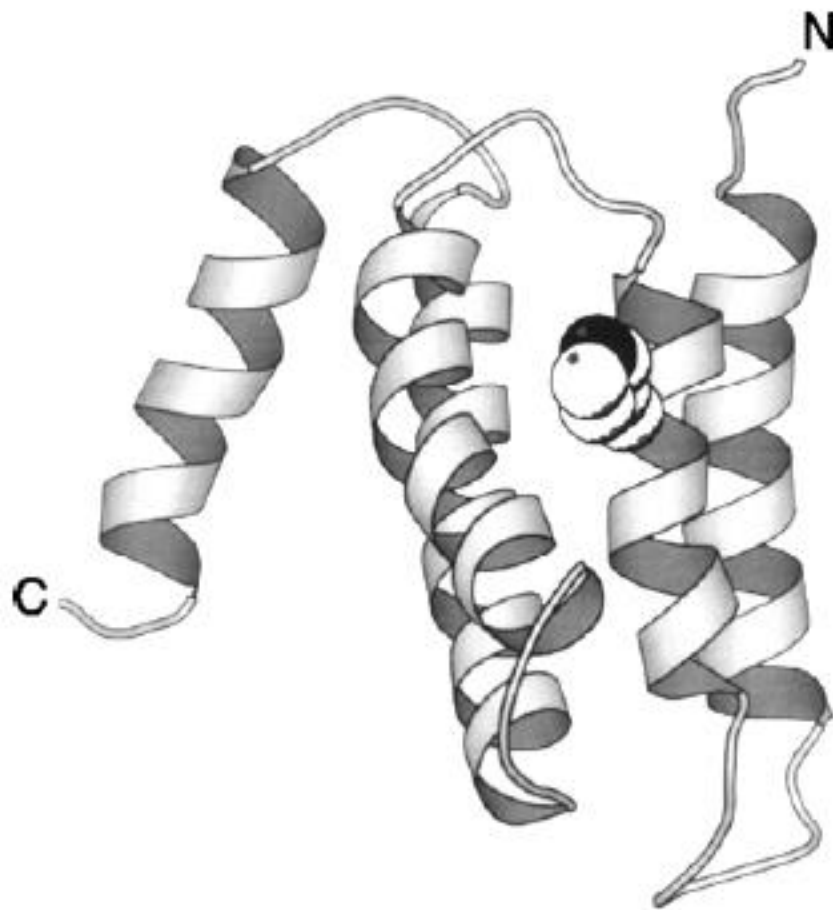
I Phosphorylation (CheA, CheY, CheB)

CheA (protein kinase), uses ATP to phosphorylate one of its histidines.



CheA (CheA_p) is bound to the Tar receptor through an adapter protein **CheW**. **CheW** is not known to have any enzymatic activity. (these proteins are sometimes called 'scaffolding protein')

CheA_p is unstable and transfers its phosphoryl group to CheY (highly soluble, diffuses through the cytoplasm)



CheA
His48

Falke et al. Annu. Rev. Cell Dev. Biol. **13**, 457 (1997)

I **Phosphorylation (CheA, CheY, CheB)**

autophosphorylation: $\text{CheA} + \text{ATP} \leftrightarrow \text{CheA}_p + \text{ADP}$

phosphoryltransfer: $\text{CheA}_p + \text{CheY} \leftrightarrow \text{CheA} + \text{CheY}_p$

CheY_p binds to the motor (FliM),
motor rotates CW (= tumbles)

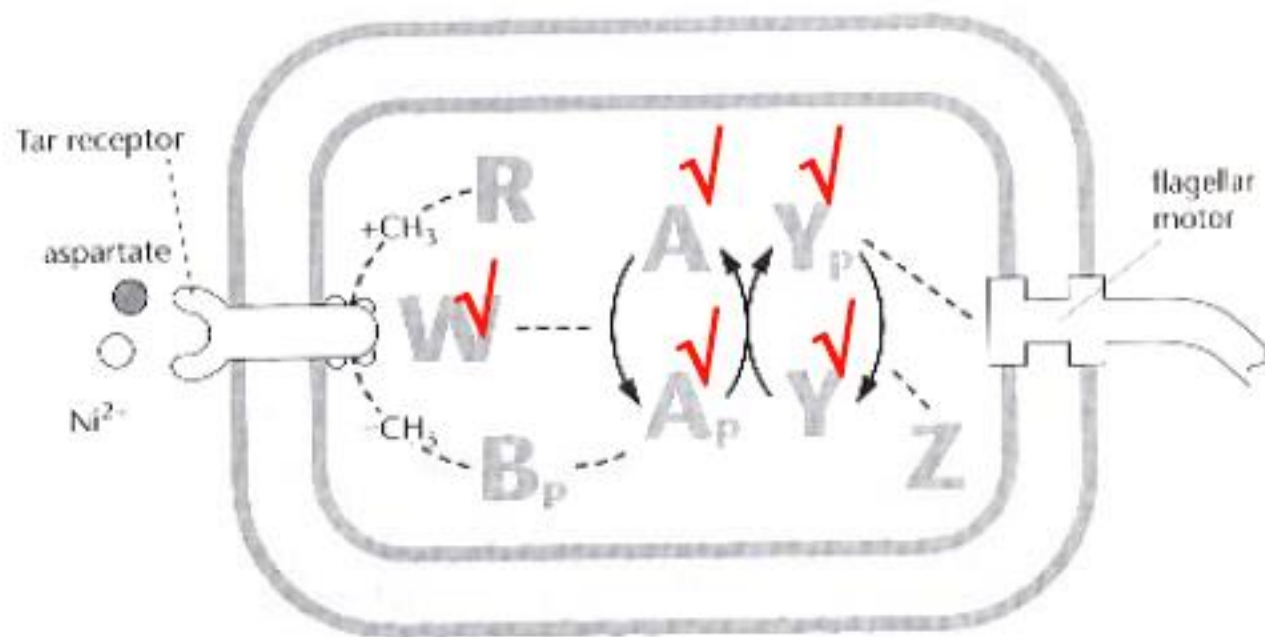
logic:

high levels of CheA_p → high levels of CheY_p

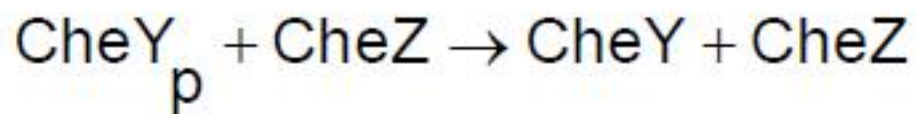
(lots of tumbles)

low levels of CheA_p → low levels of CheY_p

(straight swimming)



CheZ dephosphorylates CheY_p
(phosphatase, opposite function as CheA)

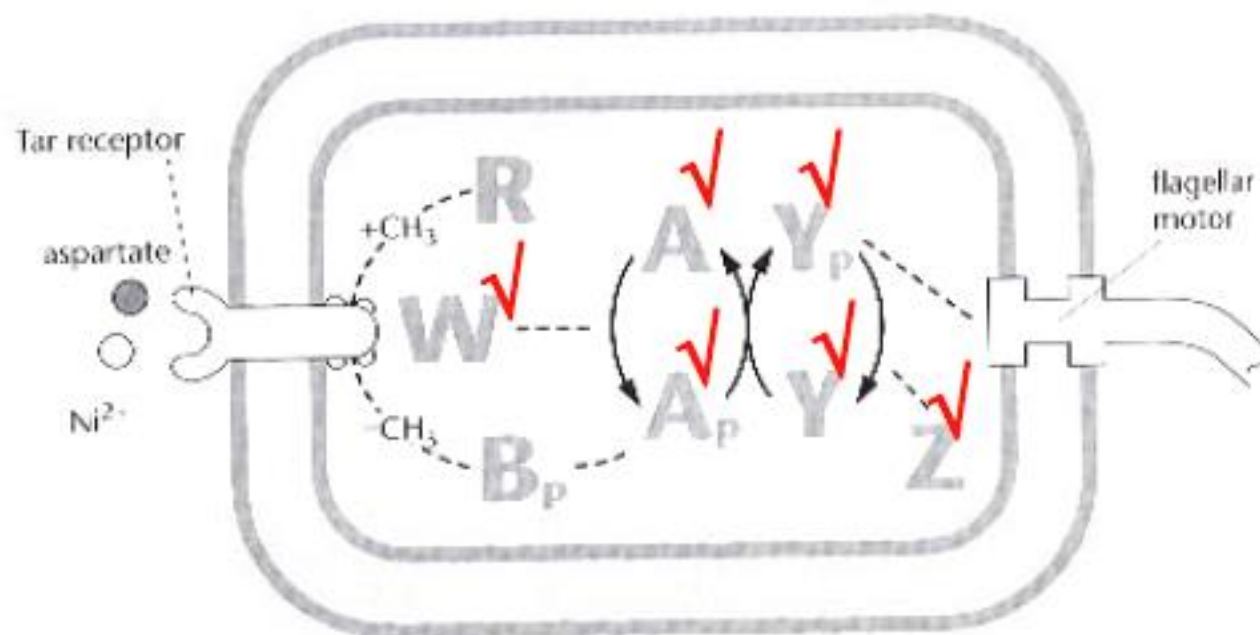


logic:

high levels of CheZ → low levels of CheY_p

(straight swimming)

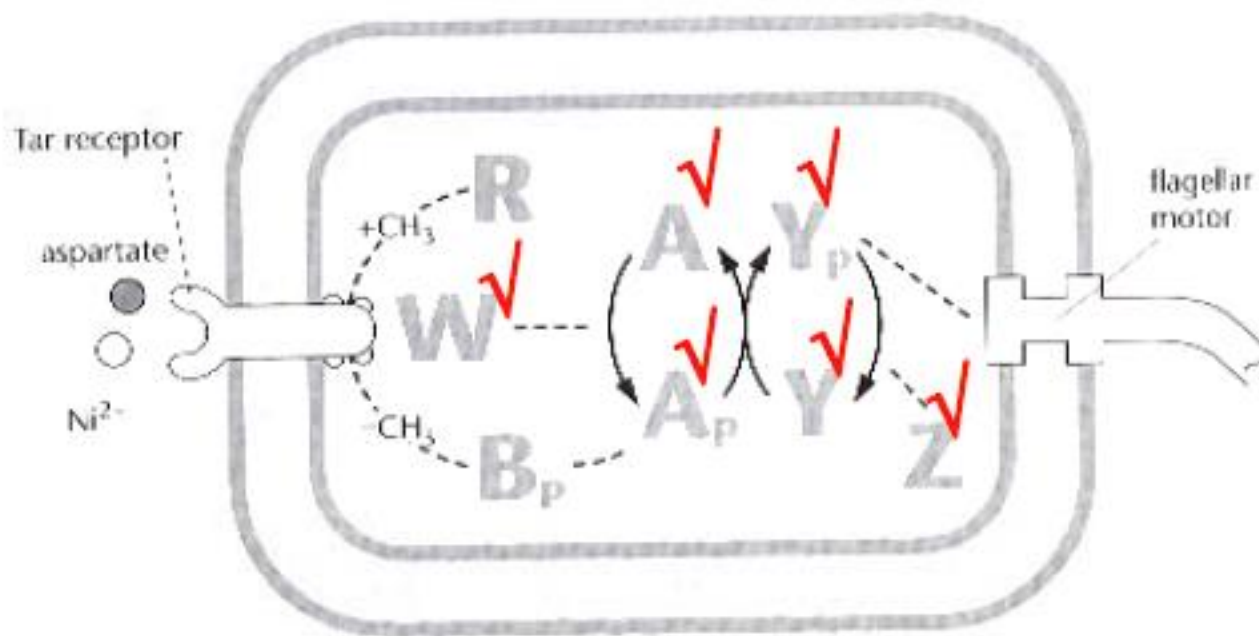
II Methylation (tar receptor)



CheR adds methyl group

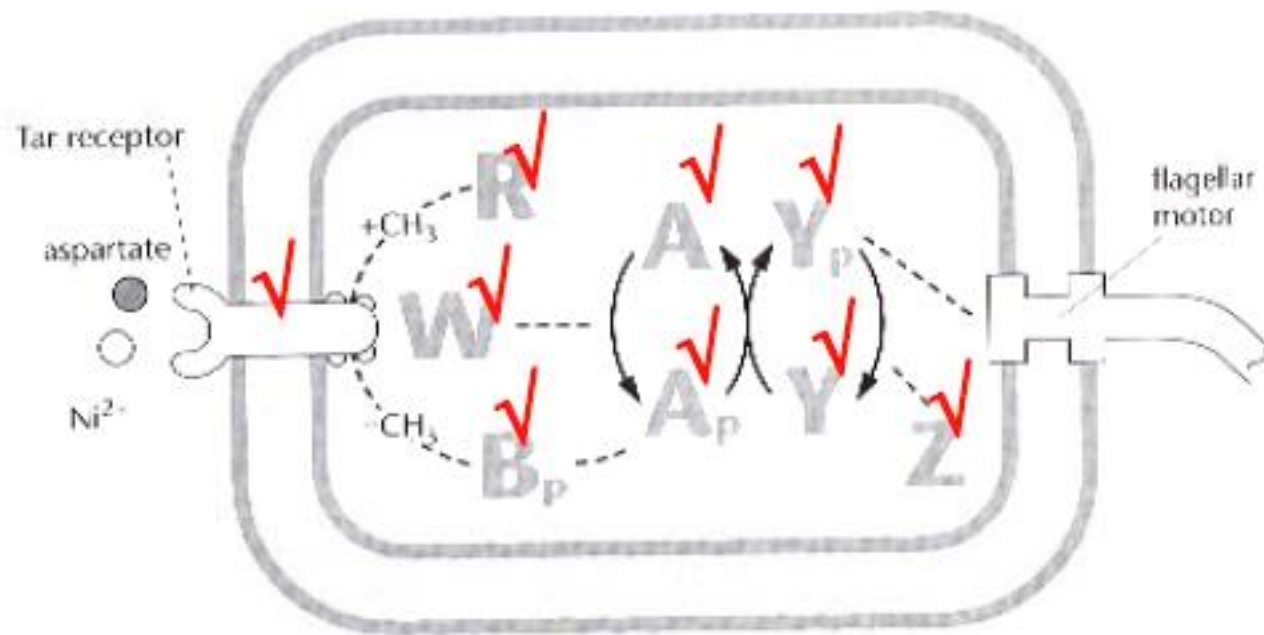
CheB_p removes methyl group

Methylation - Phosphorylation coupling



phosphorylation state of CheB
is controlled by CheA

Role of ligand binding

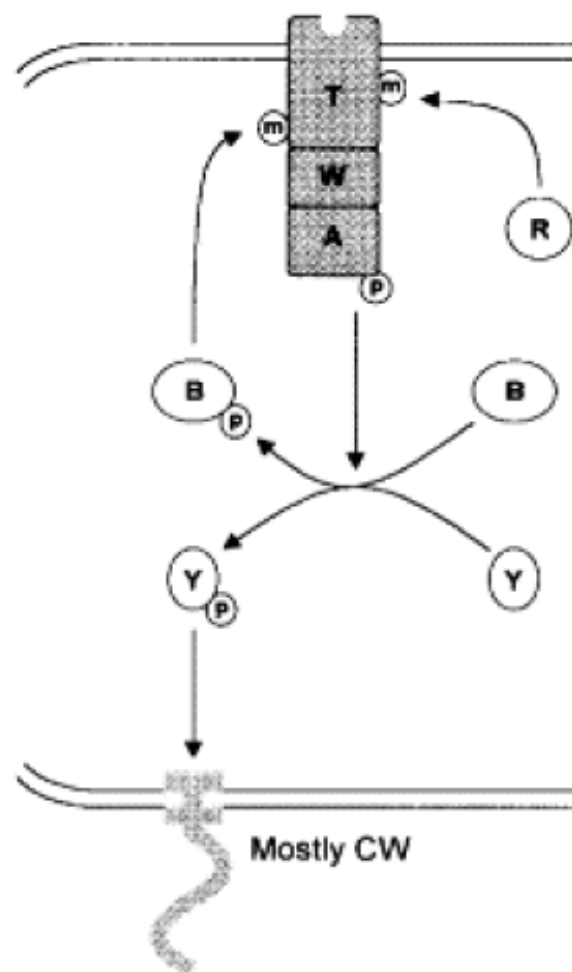


The rate of CheA phosphorylation is stimulated by unoccupied receptors

Competing process of different time scale leads to the critical adaptation

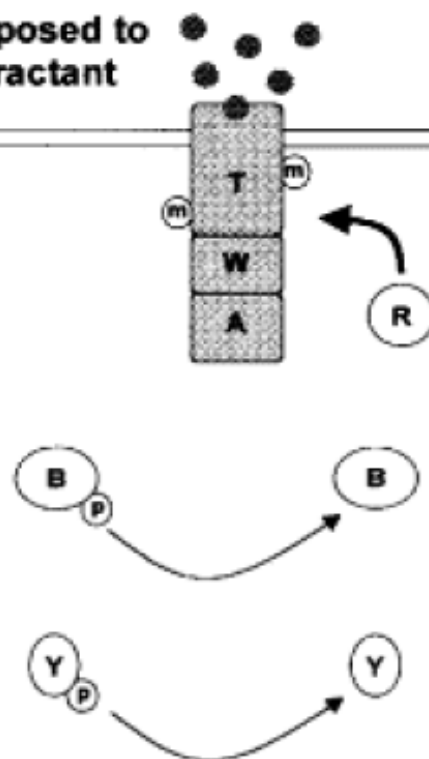
- The attractant/repellant is detected by the chemoreceptors on the cell surface
- Signal is sent to a central processing system
- Central processing system signals the flagellar motor - Excitation (fast)
- The system adapts to the ligand concentration in the environment outside the cell - **Adaptation** (slow)

Unstimulated



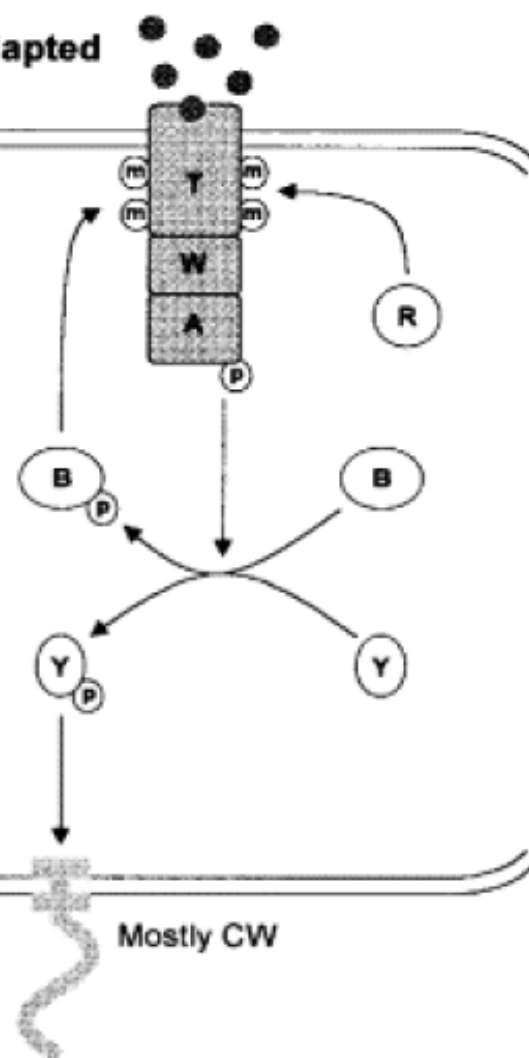
tumble

Exposed to
attractant



tumble
suppression

Adapted



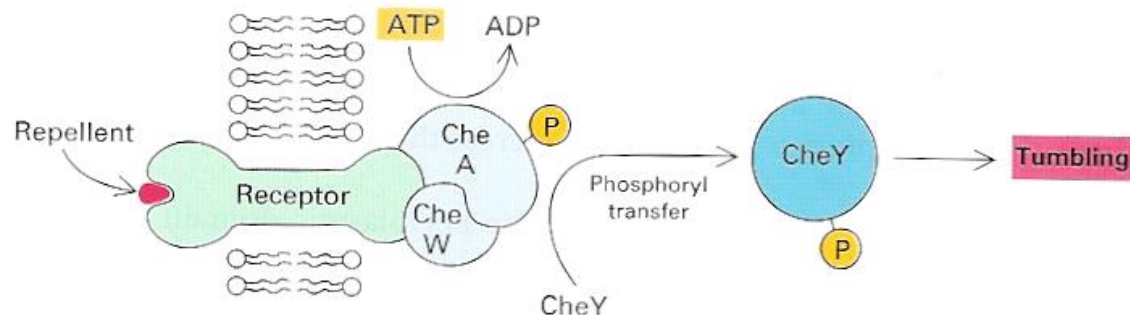
tumble

Fast Response - Excitation

- Normally, CheA autophosphorylates slowly on a histidine residue
 - CheA bound with CheW and receptor
 - Unoccupied receptor or repellant-receptor complex increases autophosphorylation
 - Attractant-receptor complex does not
- A phosphate group can be transferred to an aspartate residue on CheY

Fast Response - Excitation

- CheY ultimately determines direction of rotation
 - Phosphorylated CheY (CheYp) induces tumbling, unphosphorylated CheY does not
 - CheYp is dephosphorylated by the phosphatase CheZ

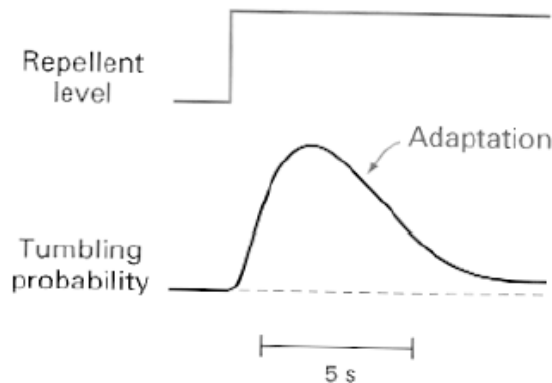


Fast Response - Excitation

- More attractant → less CheAp → less CheYp → less tumbling
- Less attractant/More repellant → more CheAp → more CheYp → more tumbling

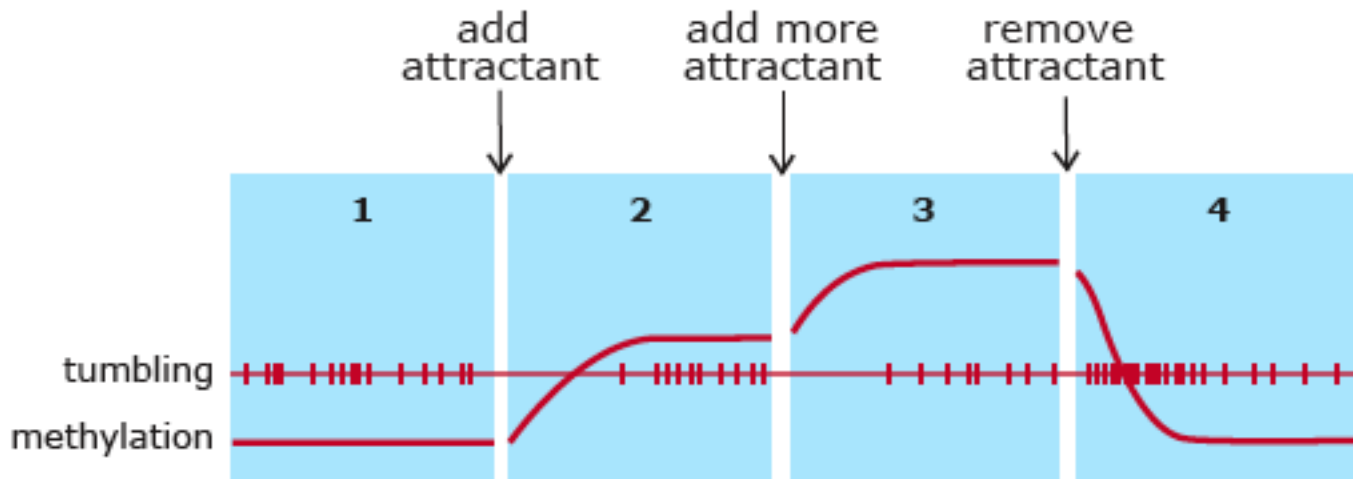
Slow Response - Adaptation

- After an increase in stimuli, system eventually returns to normal tumbling probability
- Adaptation controlled by reversible methylation of chemoreceptors - negative feedback
 - CheR is a methyltransferase (adds methyl)
 - CheB is a methylesterase (removes methyl)



Why does it have to be so
complex?

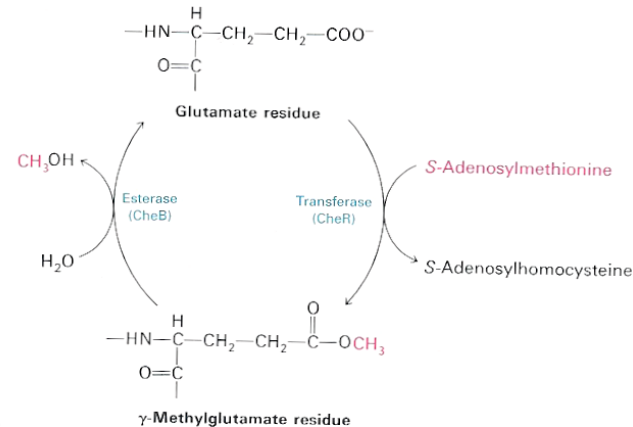
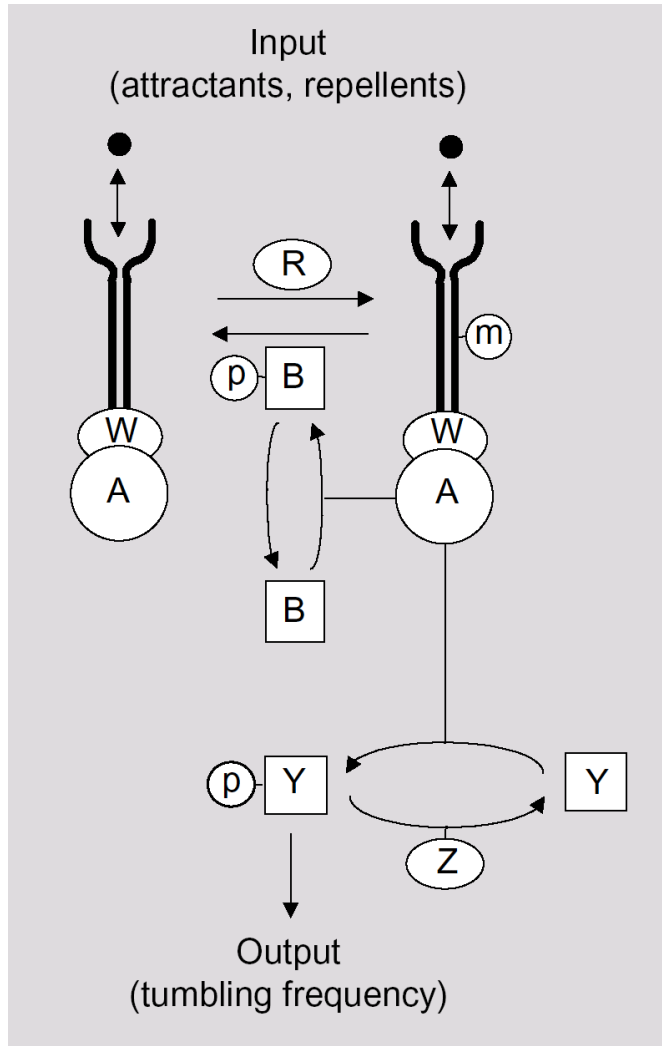
Exact Adaptation and sensitivity



Correlation of Receptor Methylation with Behavioral Response

- Methylation is important for adaptation
- *E. coli* can sense aspartate from **10nM-1mM**
- Sense gradients as shallow as **0.1%**

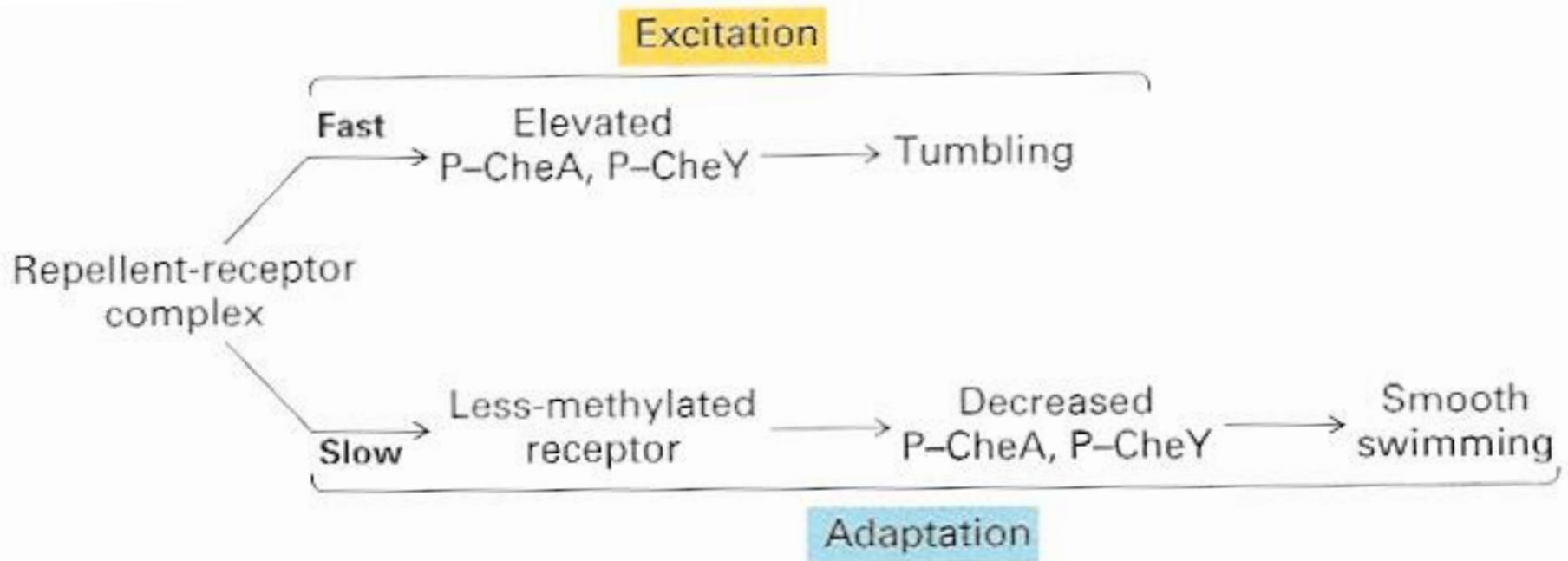
CheB/CheR Methylation and Adaptation



- 1) CheR adds methyl group, CheB removes it
- 2) Attractant/receptor binding \rightarrow methylation up
Repellent/receptor binding \rightarrow methylation down
- 3) Methylation \rightarrow CheA auto-phosphorylation **up**
- 4) CheA a-p \rightarrow CheY phosphorylation up
CheA a-p \rightarrow CheB phosphorylation up
- 5) CheB phosphorylation \rightarrow CheB methylesterase

Excitation and Adaptation are coupled

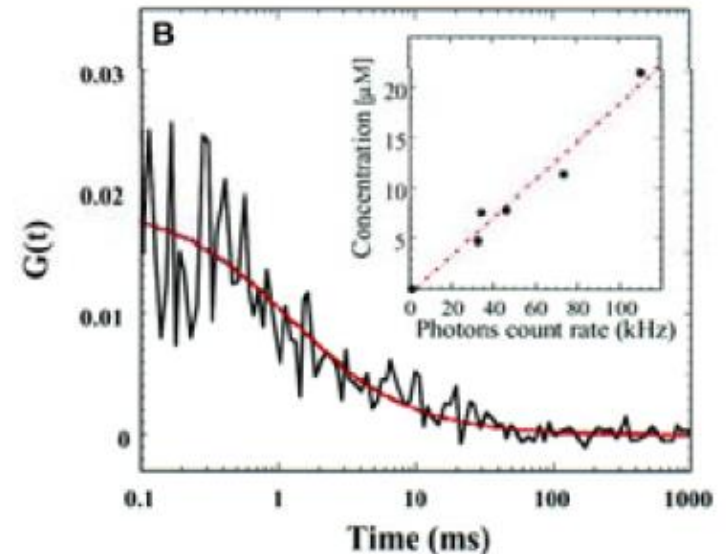
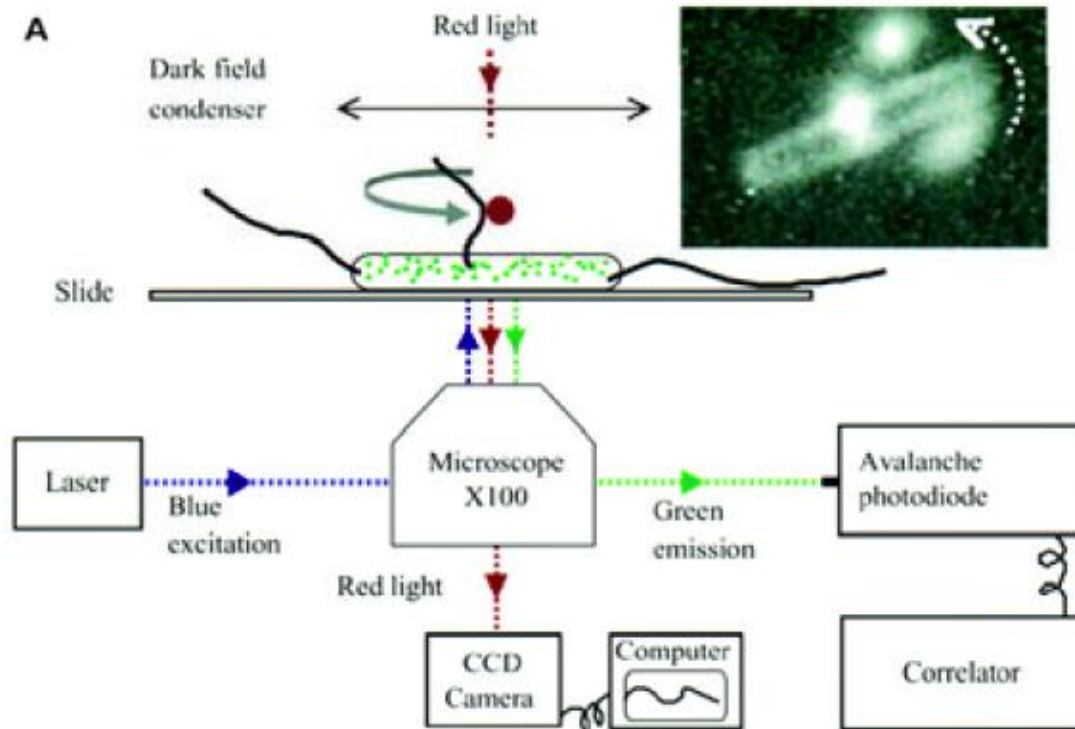
- Functions as a pulse generator
 - Temporary response due to faster kinetics eventually repressed by slower negative feedback system



Before starting with the modeling,
first let's look at some recent experiments

Alon et al. Nature 397,168 (1999)
Cluzel et al. Science **287**, 1652 (2000)
Sourjik et al., PNAS **99**, 123 (2002)
PNAS **99**, 12669 (2002)
Nature **428**, 439 (2004)

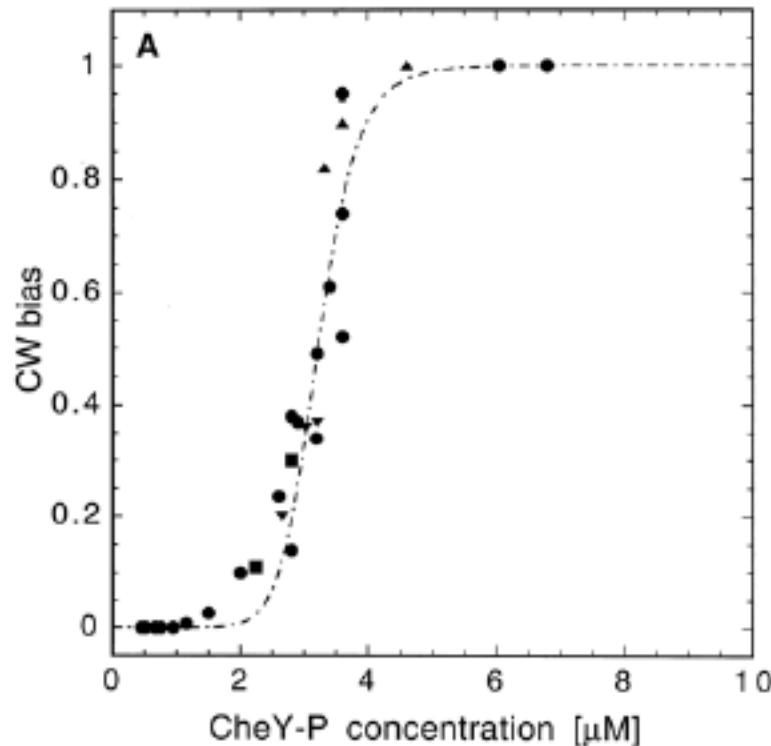
Experimental procedure to analyze flagella rotation directions



Single cell chemotactic analysis

Flagella rotation is very sensitive to cheY phosphorylation

correlation CW bias & CheY-P gene expression



cells have plasmids with CheY-GFP under inducible promoter

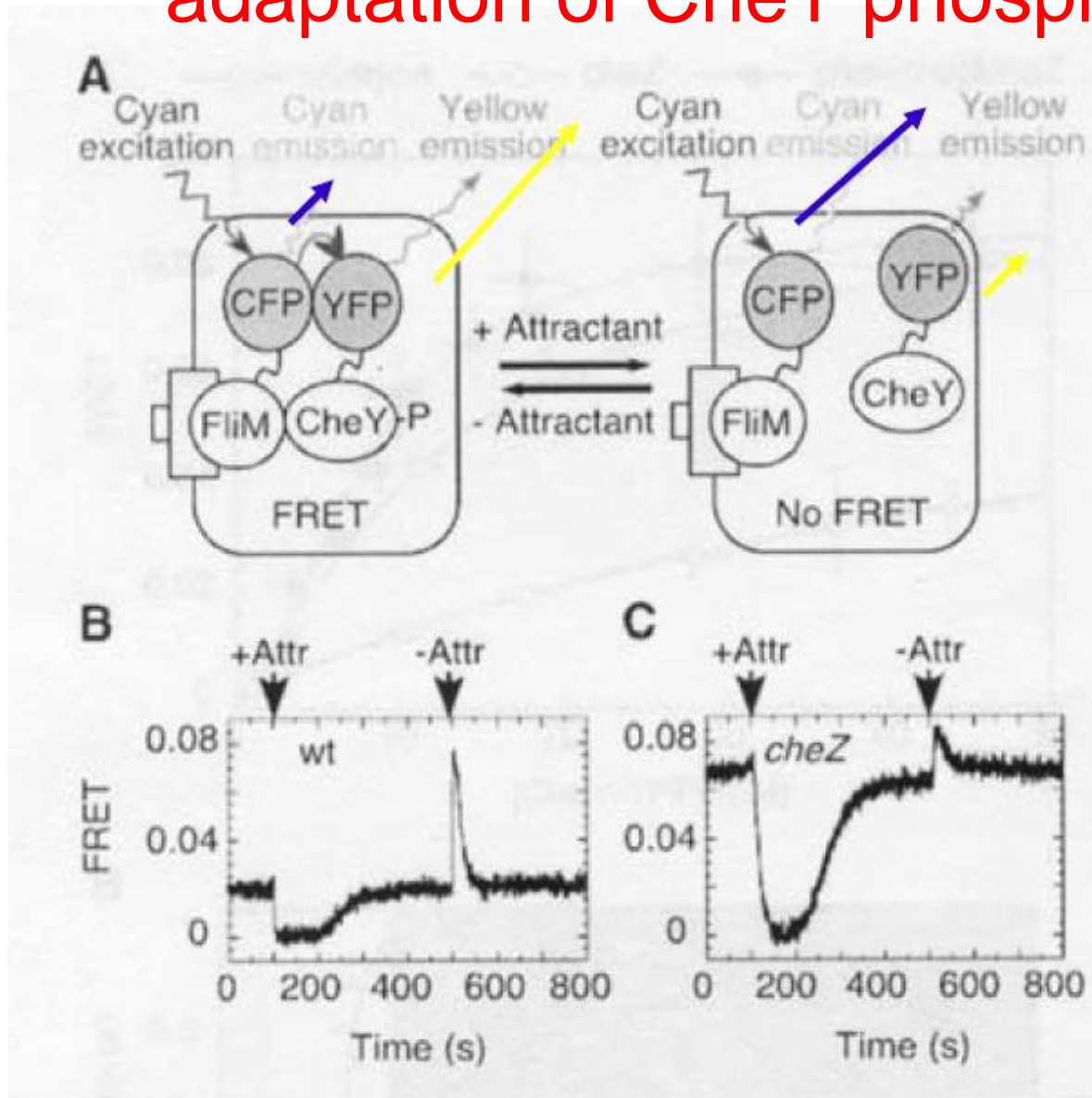
assumption: all CheY is phosphorylated

strain: CheY-, CheZ-, CheB-

Hill #: ~ 10

What about measurement of direct binding of CheY-p to motor?

FRET and cheYp-FliM interaction indicate adaptation of CheY phosphorylation



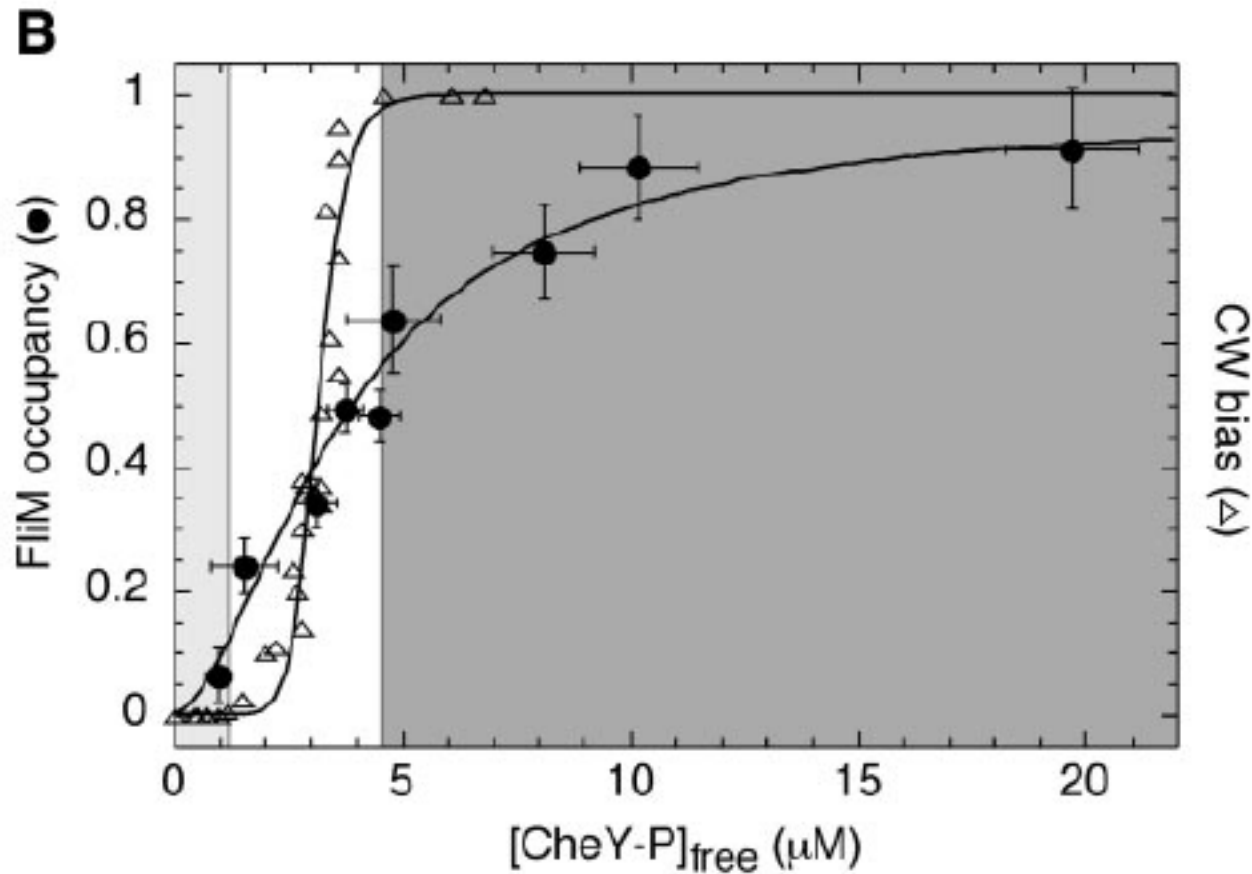
low YFP/CFP:
unbound

high YFP/CFP:
bound

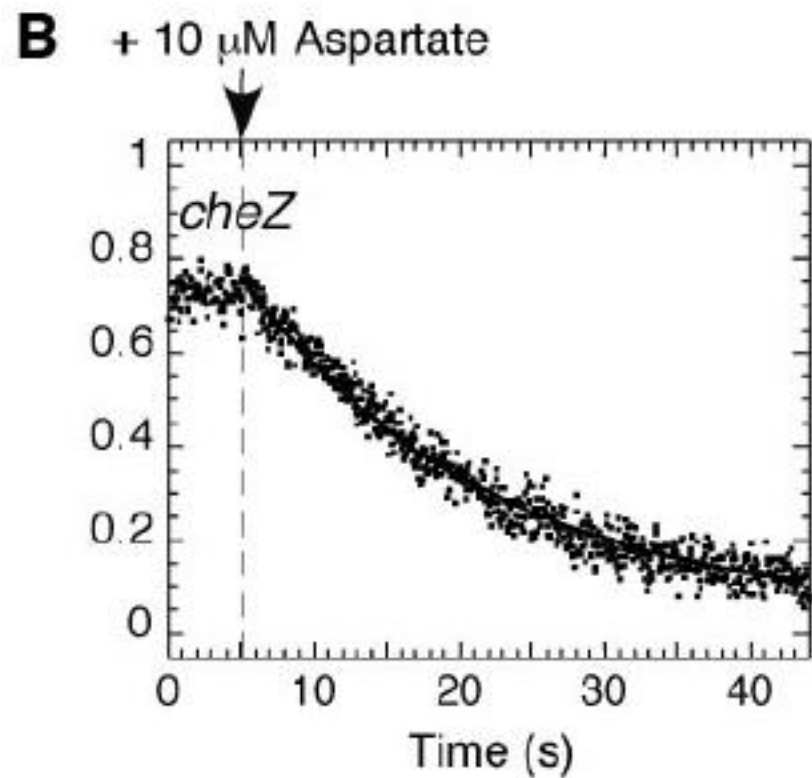
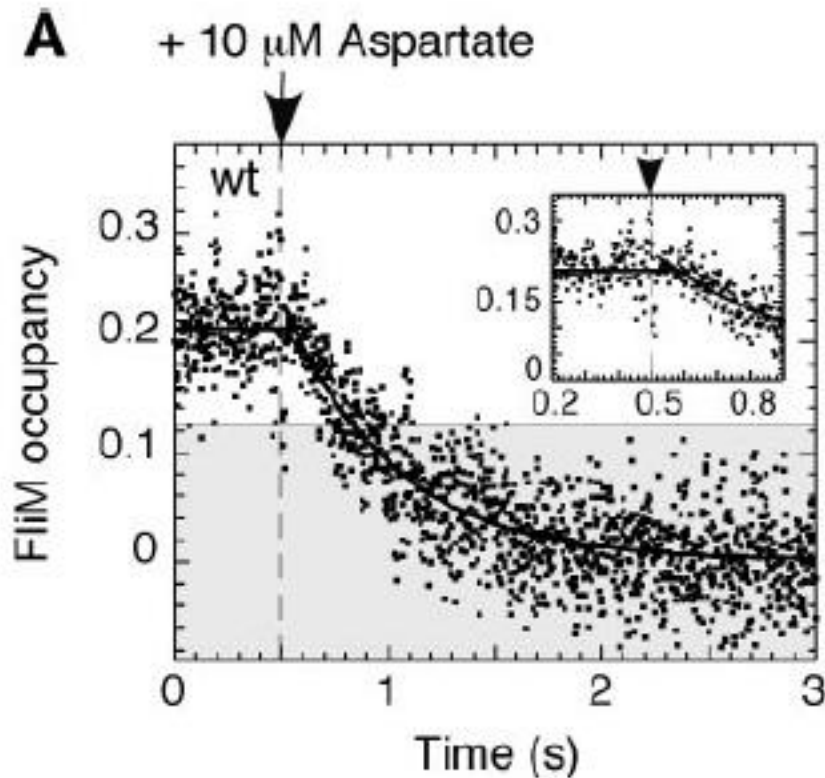
FRET (fluorescence resonant transfer)

Sourjik PNAS 2000

FliM-cheYp interaction is less cooperative than Motor output



cheZ speeds up the FlIM response to Aspartate



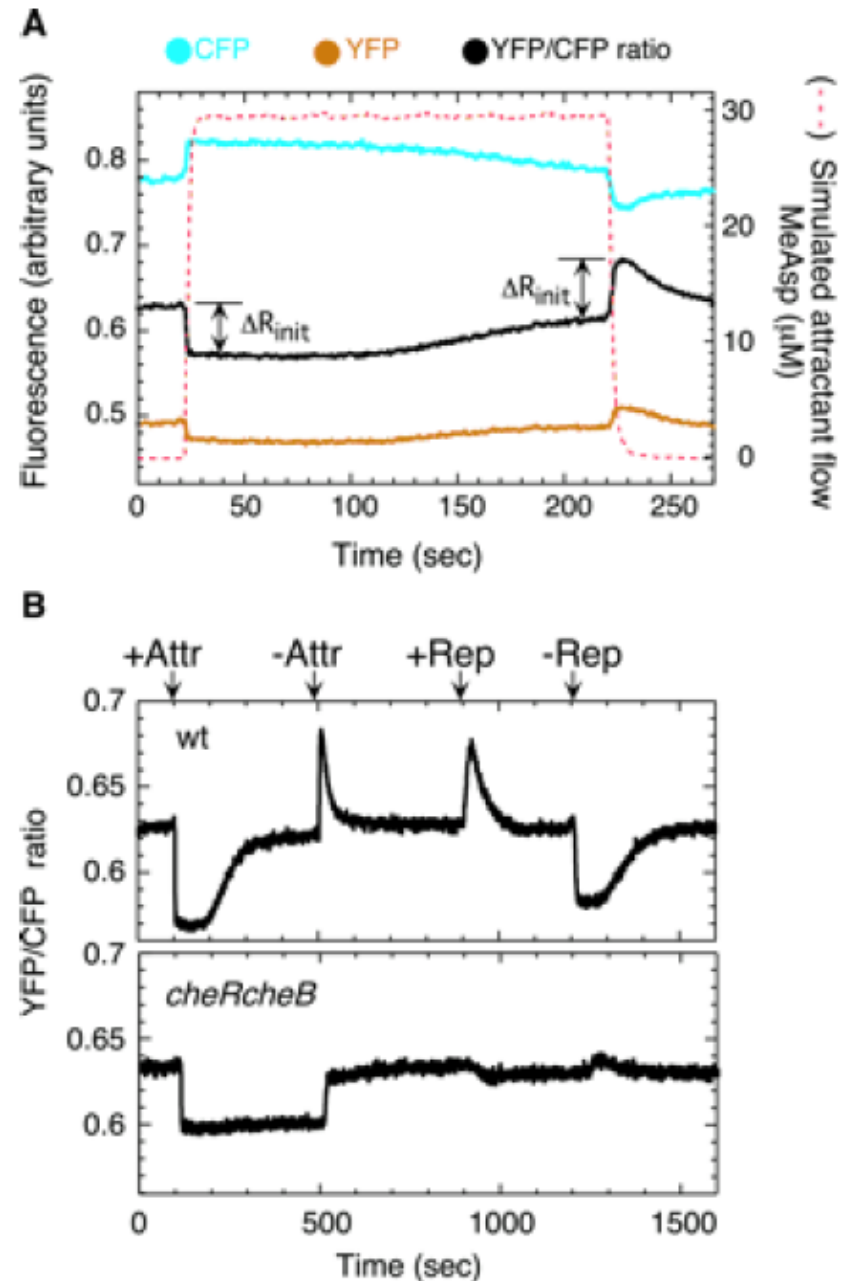
FRET-based adaptation of CheZ-CheYp interaction

CheY-YFP (yellow)
CheZ-CFP (blue)

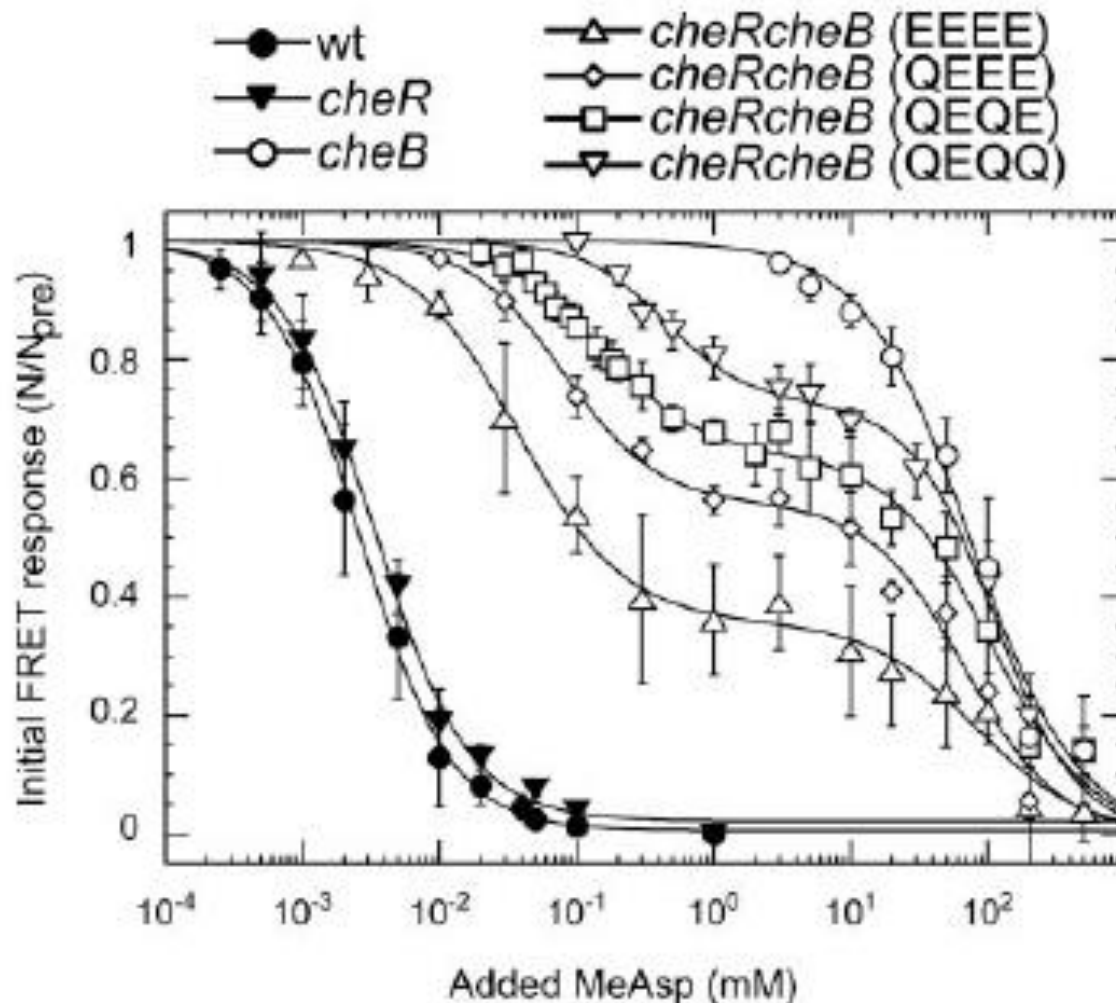
CheZ binds only to
CheYp !!

adding attractant
leads to immediate
lower concentration of
CheY_p-CheZ complex,
lower [CheYp],
less tumbling

Sourjik PNAS 2000



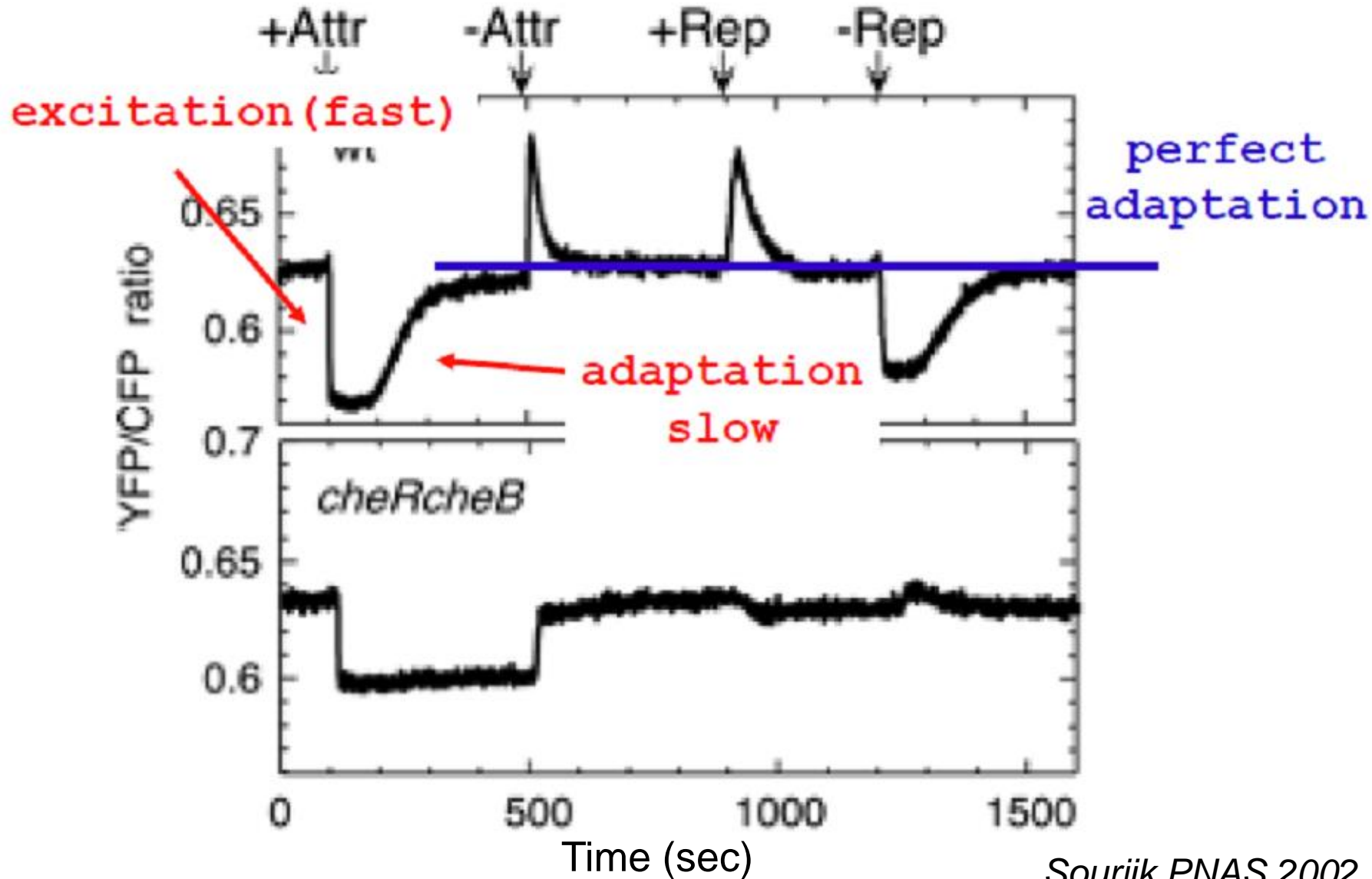
cheR cheB mutants show significantly wide range of sensitivities to Asp and no cooperativity



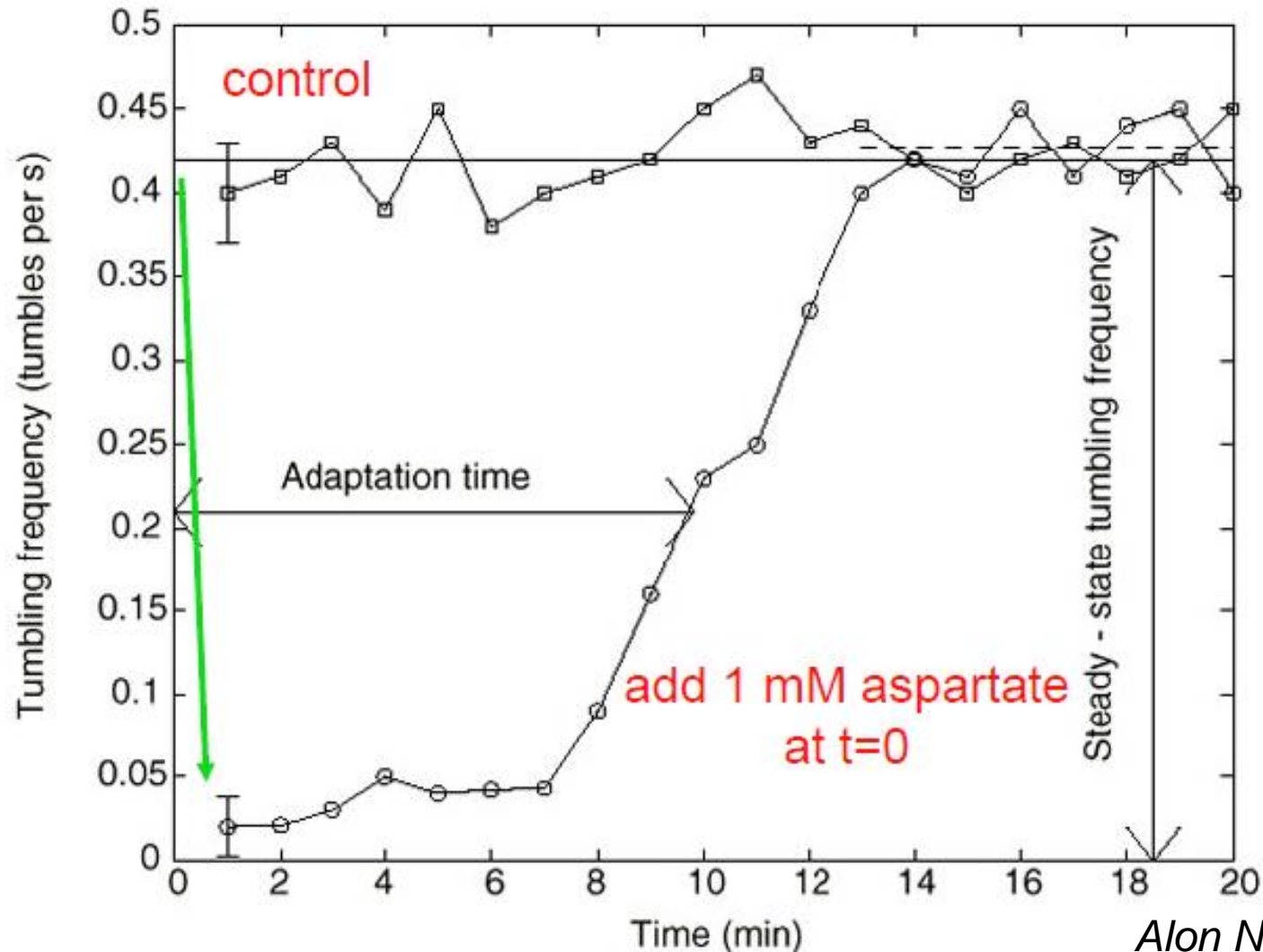
Multistep reactions leads to high amplification

- Amplification between receptors and cheYp: ~35 folds
- Amplification between cheYp and motor: ~10 folds
- cheZ doesn't cause amplification

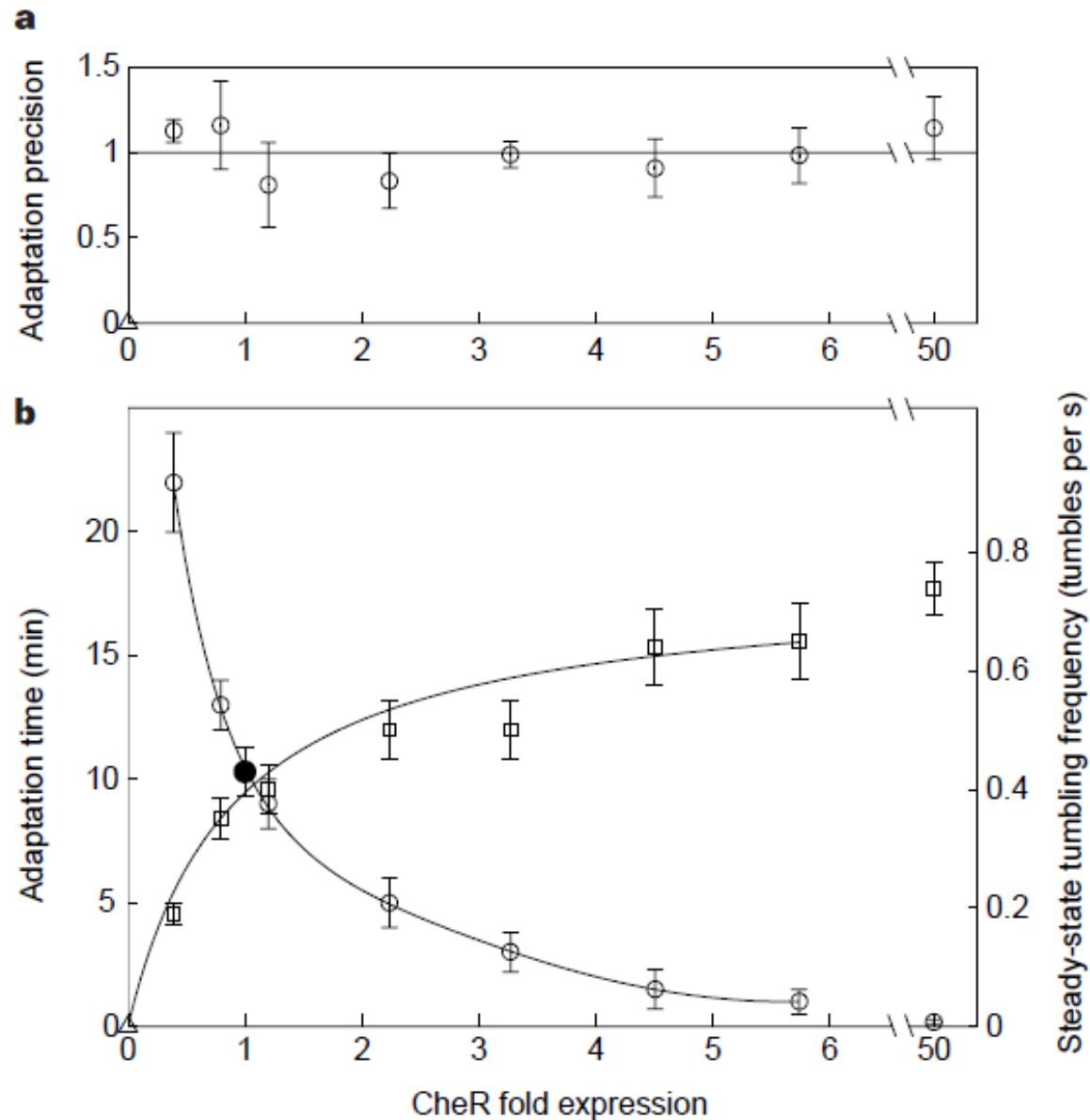
Perfect adaptations



The measurement of adaptation precision and time



Perfect adaptation is robust against changes in cheR expression but not adaptation time.



The goal of the model

- Huge gain
- Sensitivity
- Perfect adaptation

All these are ubiquitous in signal transduction networks in general.

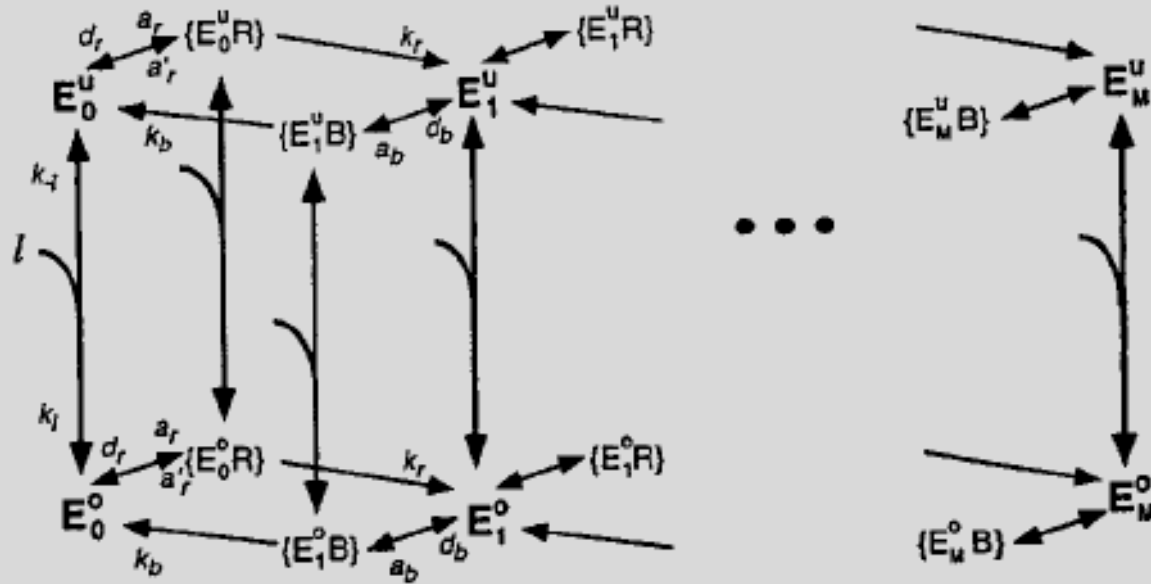
What's the basis for perfect adaptation? Two explanations:

- The kinetic parameters are fine-tuned.
 - E. g.: Spiro et al. *A model of excitation and adaptation in bacterial chemotaxis. PNAS*, 1997
- Perfect adaptation is a robust property of the underlying network.
 - Barkai & Leibler 1997, Nature (Modeling)
 - Alon et al 1999, Nature (Experiment)

Assumptions in Barkai-Leibler model

1. Tar is only receptor type considered. CheW and CheA always bound to Tar.
2. Methylation occurs in specific order
3. Consider only 3 highest methylation states
4. Only cheBp demethylates
5. Phosphorylation of cheA does not affect ligand (un)binding
6. Tar-CheR binding does not affect ligand (un)binding
7. CheZ is not regulated
8. Phosphotransfer from complex to cheY or cheB is not affected by occupancy and methylation state.

A two-state model



The differential equations describing our model can be written in a standard way from the figure. For instance, the kinetic equation for E_m^u is

$$\begin{aligned} \frac{dE_m^u}{dt} = & -k_i E_m^u + k_{-i} E_m^o + \\ & (1 - \delta_{m,0}) [-a_b \alpha_m E_m^u B + d_b \{E_m^u B\} + k_r \{E_{m-1}^u R\}] + \\ & (1 - \delta_{m,M}) [-a_r \alpha_m E_m^u R + a'_r (1 - \alpha_m) E_m^u R + d_b \{E_m^u R\} + k_b \{E_{m+1}^u B\}] \\ & (m = 1, \dots, M) \end{aligned}$$

Testing Robustness

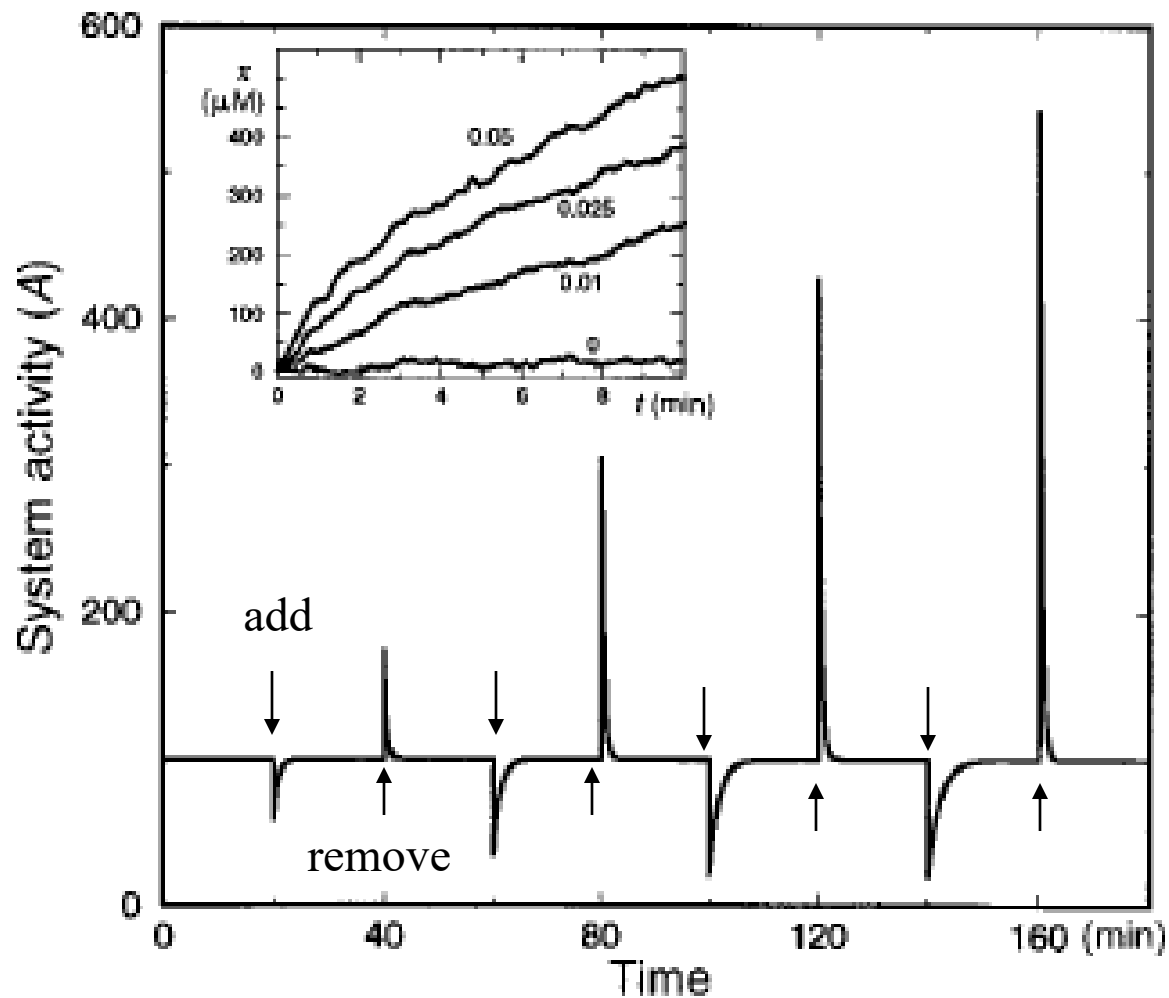
Model has 9 rate constants and 3 enzyme concentrations

In each simulation increase or decrease each parameter 2X randomly

Overall parameter Change = $P_{n,1}/P_{o,1} \times P_{n,2}/P_{o,2} \times \dots$

Do 6000 independent simulations

Examine effects on precision and timing of adaptation



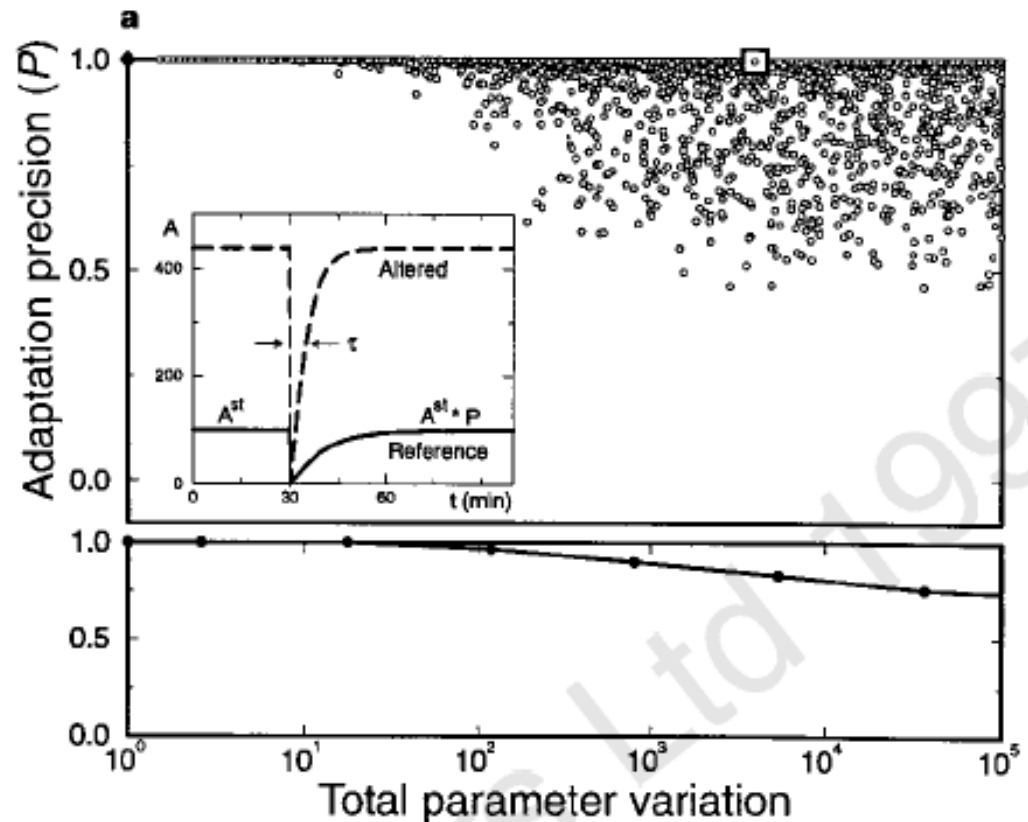
Modeling the effect of successive addition and removal (after 20 min.) of 1, 3, 5 and 7 mM of chemoattractant

Barkai&Leibler 1997 Nature 387, 913

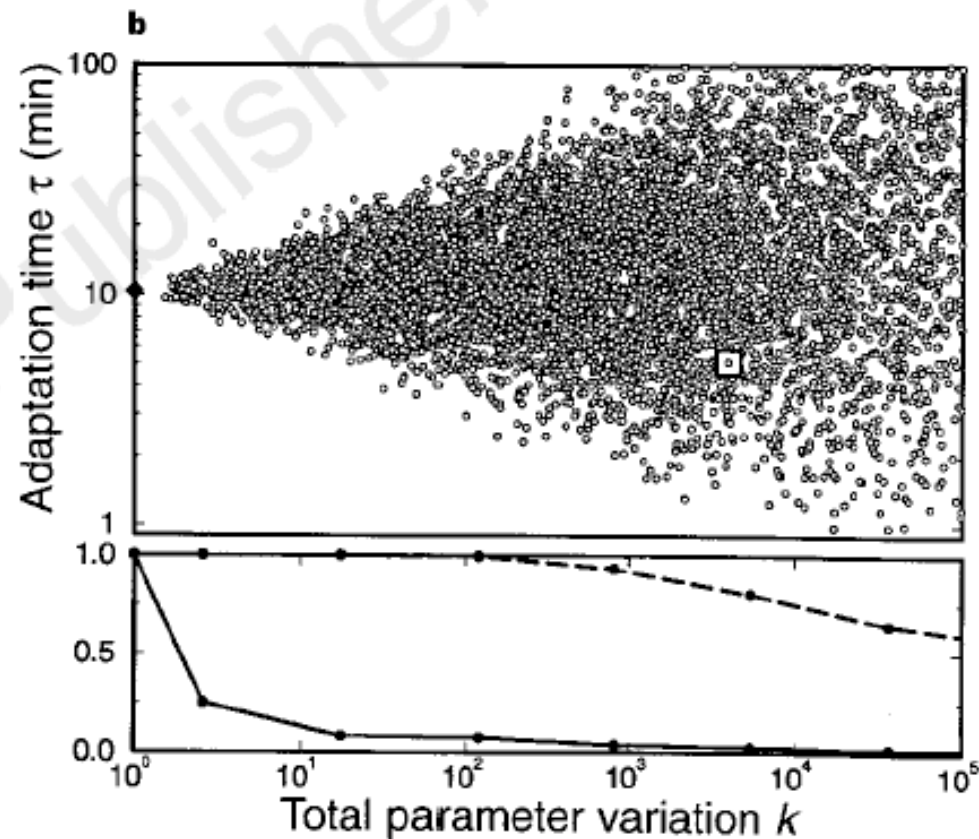
All rate constants in the model can be changed randomly by 2 fold with only a $\sim 15\%$ deviation from perfect adaptation.

A single rate constant can be changed by several orders of magnitude (holding other parameters constant) without significant deviation from perfect adaptation.

Multiple methylation is not necessary for robustness but improves adaptation response time.

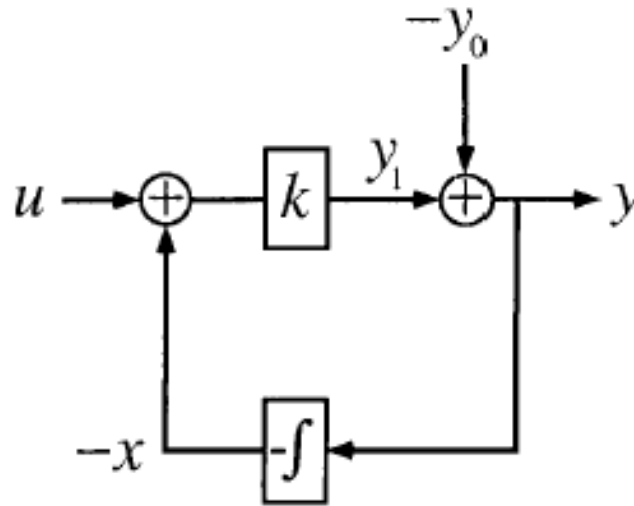


The time required for adaptation varies widely as the rate constants for the model are randomly changed.



Barkai-Leibler Model is a form of Integral Control

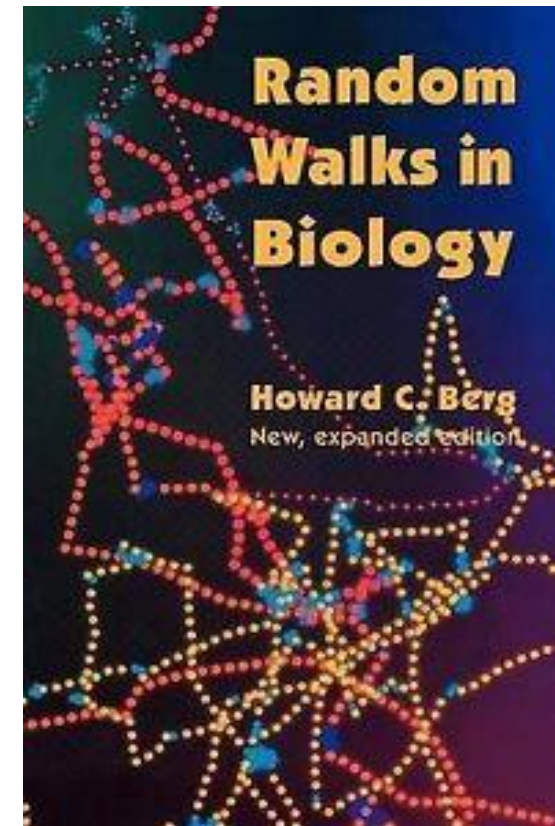
Yi, Huang, Simon&Doyle 2000 PNAS 97, 4649



$\dot{x} = y$	$y(t) \rightarrow 0 \text{ as } t \rightarrow \infty$
$y = y_1 - y_0$	<i>iff</i>
$= k(u - x) - y_0$	$k > 0$

Read the paper if you are interested.

Basic concepts of diffusion and chemotaxis *population vs individual*



Diffusion

- Previously we assumed that the state of a cell at a particular point in time could be described by the concentrations of key components.
- The concentrations could change over time
- We implicitly assumed that within the cell these concentrations do not vary spatially inside the cell
- We considered the cell as a well-stirred biochemical reactor

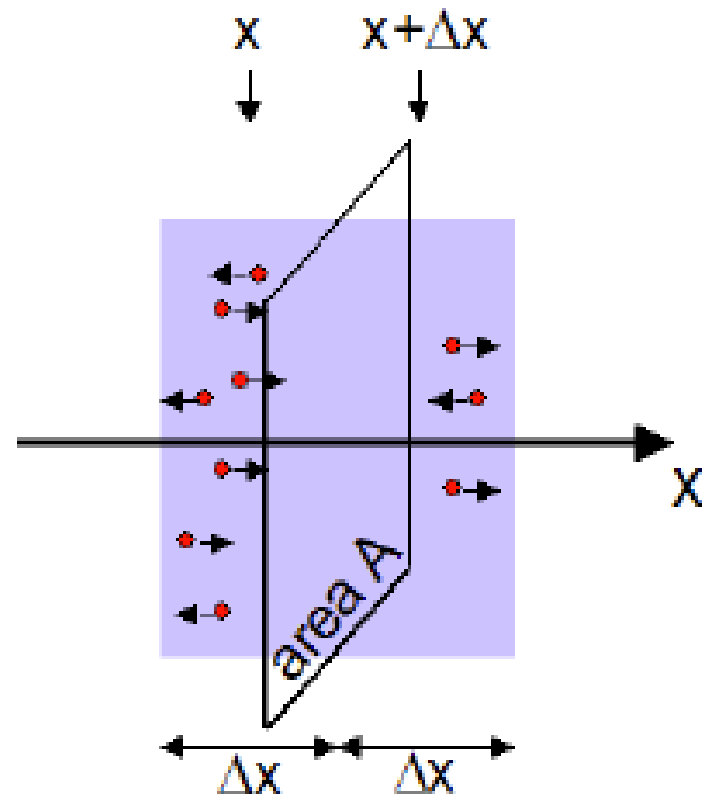
Where does the assumption fail

- For small cells such as E coli this is often a valid assumption
 - Dynamical phenomena:
 - time scale:seconds-minutes.
 - Random mixing by diffusion:
 - time scale $\sim L^2/D \sim 0.1\text{s}$, $L \sim 1\mu\text{m}$, $D \sim 10\mu\text{m}^2/\text{sec}$
- Larger cells such as eukaryotic cells
- Fast process in small cells
- Signal molecules diffusion between cells etc

Fick's first law

To understand the spatial inhomogeneous systems we take a look at Fick's laws

- Considering particles randomly moving along one-dimension crossing an area A .
- Assuming there are $N(x)$ particles on the left of area A and $N(x+\Delta x)$ particles on the right of area A



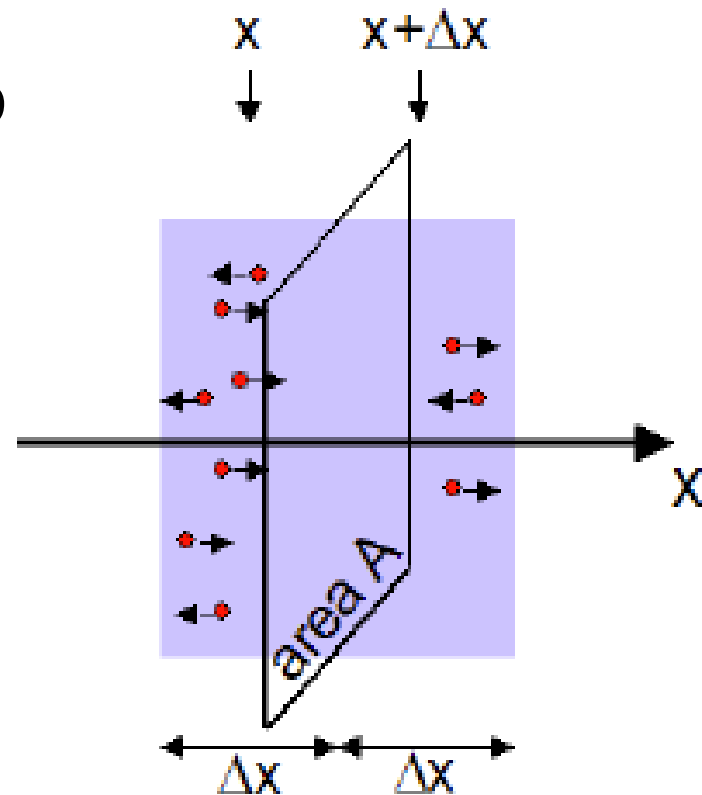
Fick's first law

Probability of traveling to left and right are identical. $0.5N(x)$ will travel to the right cross area A.

However, $0.5N(x+\Delta x)$ will travel to the left cross area A.

Therefore the net number of crossing to the right is:

$$-\frac{1}{2}(N(x + \Delta x) - N(x)).$$



Fick's first law

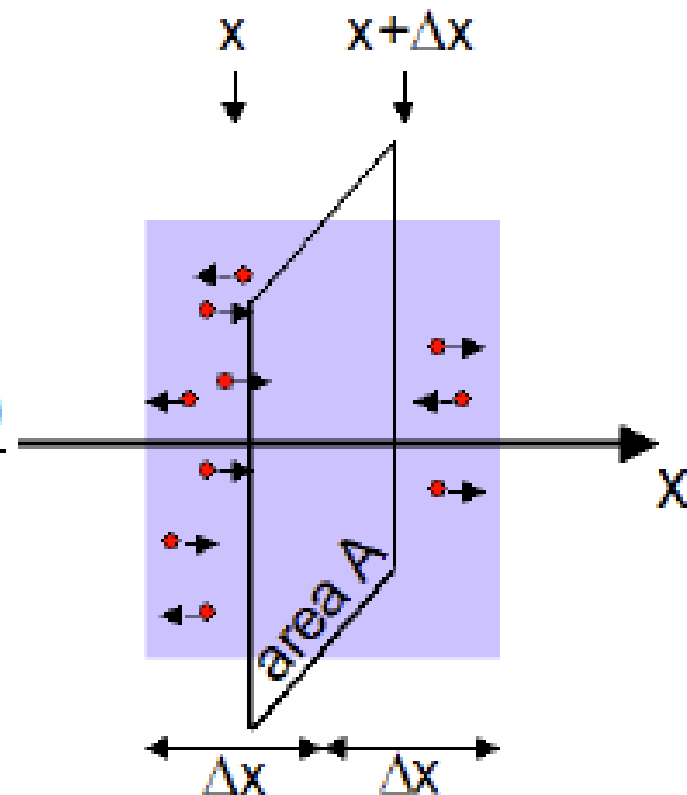
The flux of molecules J through the area A during a short time interval τ is defined as:

$$J = \frac{-\frac{1}{2}(N(x + \Delta x) - N(x))}{A\tau}$$

Defining concentration results in: $C(x) \equiv \frac{N(x)}{A\Delta x}$

$$J = -\frac{(\Delta x)^2}{2\tau} \frac{(C(x + \Delta x) - C(x))}{\Delta x} = -D \frac{\partial C(x)}{\partial x}$$

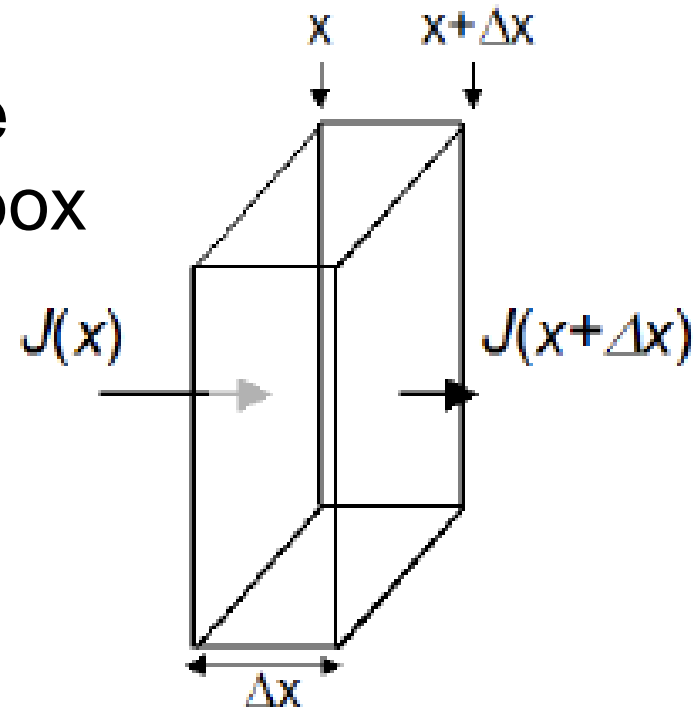
Where D is defined as the diffusion constant.



Fick's second law

Assuming a particle cannot be created or destroyed, consider the volume $A\Delta x$, A flux $J(x)$ enter the box from the left and a flux $J(x+\Delta x)$ leaves the box to the right.

The rate of change of the concentration in the box during a short time τ is given by:



$$\frac{C(t + \tau) - C(t)}{\tau} = \frac{1}{\tau} \frac{(J(x) - J(x + \Delta x))A\tau}{A\Delta x} = - \frac{(J(x + \Delta x) - J(x))}{\Delta x}$$

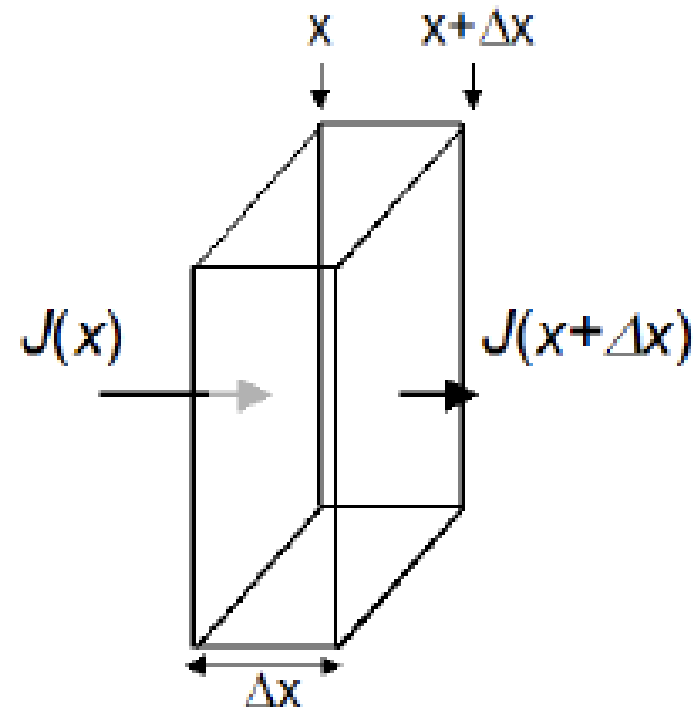
Fick's second law

- Taking the limit $t \rightarrow 0$ and $\Delta x \rightarrow 0$ results in:

$$\frac{\partial C(x)}{\partial t} = - \frac{\partial J(x)}{\partial x}$$

- Combining it with the first law lead to the second law

$$\frac{\partial C(x,t)}{\partial t} = D \frac{\partial^2 C(x,t)}{\partial x^2}$$



Random walks

Let us consider a one-dimensional random walk of N particles. A particle always takes a fixed step size Δx toward the left or right with equal probability.

The position of the particle is denoted by $X_j(n)$, where the subscript denotes which particles and n denotes the number of steps that particle j took.

All particles starts their random walk at $x=0$. The position average of all particles remains zero:

$$\langle x(n) \rangle = \sum_{i=1}^N x_i(n) = \sum_{i=1}^N (x_i(n-1) \pm \Delta x) = \sum_{i=1}^N x_i(n-1) = \sum_{i=1}^N x_i(0) = 0$$

Random walks

However individual particles are spreading in both the positive and negative direction,

A convenient way to quantify the spreading is to calculate the variance of the distribution of positions. The variance is defined as:

$$Var(x(n)) = \langle x^2(n) \rangle - \langle x(n) \rangle^2$$

$$Var(x(n)) = \langle x^2(n) \rangle - 0 = \sum_{i=1}^N x_i^2(n) = \sum_{i=1}^N (x_i(n-1) \pm \Delta x)^2 = \langle x^2(n-1) \rangle + \Delta x^2$$

The variance is non-zero, and it grows by ΔX^2 for each steps, and since the variance is non-zero

$$\langle x^2(n) \rangle = n\Delta x^2$$

Random walks

During one step the particle moves at a constant velocity $v = \Delta x / \tau$. This means that at time t the particle performed $n = t / \tau$ steps, therefore the variance is proportional to t :

$$\langle x^2(n) \rangle = t \frac{\Delta x^2}{\tau} \equiv 2Dt$$

Random walk under external force

- Single particles: Langevin equations

$$m \frac{d^2 x}{dt^2} + \gamma \frac{dx}{dt} = f(x) + \Gamma(t)$$

Inertia
term

Damping
term

deterministic
force

random
force

Random walk of biological cell

Damped Langevin equations

$$\gamma \frac{dx}{dt} = f(x) + \Gamma(t) \qquad \Gamma(t) = \sqrt{D / dt} \, g(t)$$

Damping
term

deterministic
force

random
force

$f(x)$, gravity, chemotaxis etc

A good approximation?

From damped Langevin equation of single cell/molecule, mathematicians derived:

$$\frac{\partial C(x, t)}{\partial t} = D \frac{\partial^2}{\partial x^2} C(x, t) - \frac{\partial}{\partial x} [f(\dots) C(x, t)]$$

In physics and mathematics, this type of equations is called Fokker-Planck Equations.

In finance, the famous Black-Scholes-Merton model for pricing of options is a derivation of this equations. Scholes and Merton won the Nobel prize in Economy in 1997 .



The Sveriges Riksbank Prize in Economic Sciences in Memory of Alfred Nobel 1997

Robert C. Merton, Myron Scholes

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The Sveriges Riksbank Prize in Economic Sciences in Memory of Alfred Nobel 1997



Robert C. Merton
Prize share: 1/2



Myron S. Scholes
Prize share: 1/2

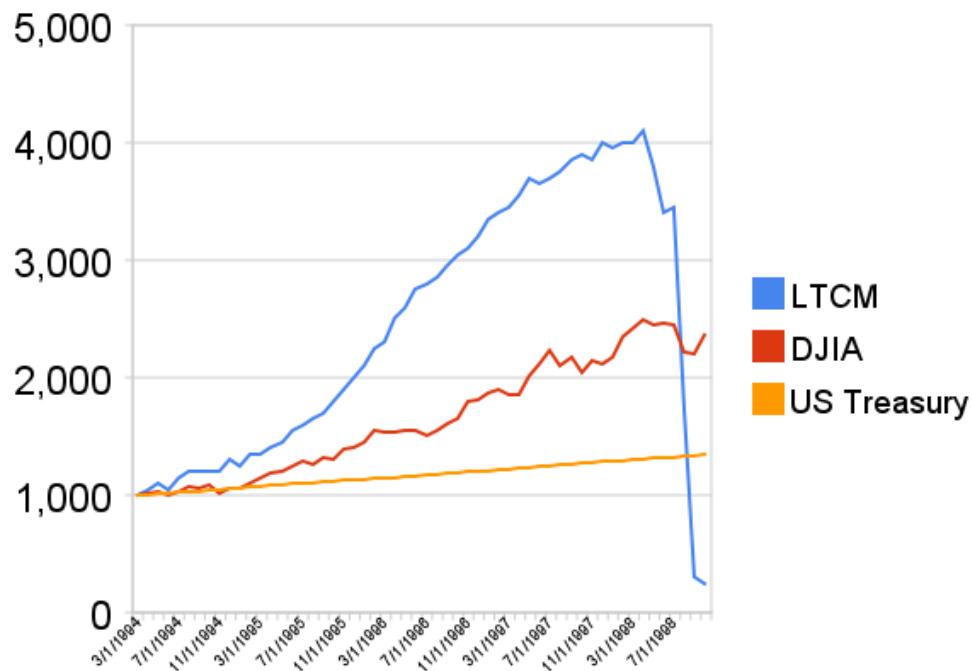
The Sveriges Riksbank Prize in Economic Sciences in Memory of Alfred Nobel 1997 was awarded jointly to Robert C. Merton and Myron S. Scholes "for a new method to determine the value of derivatives"

Photos: Copyright © The Nobel Foundation



Myron S. Scholes (left) and Robert C. Merton were principals at LTCM.

Long Term Capital Management 1994-1998



1998 bailout [\[edit\]](#)

Long-Term Capital Management did business with nearly everyone important on Wall Street. Indeed, much of LTCM's capital was composed of funds from the same financial professionals with whom it traded. As LTCM teetered, Wall Street feared that Long-Term's failure could cause a chain reaction in numerous markets, causing catastrophic losses throughout the financial system.

After LTCM failed to raise more money on its own, it became clear it was running out of options. On September 23, 1998, [Goldman Sachs](#), [AIG](#), and [Berkshire Hathaway](#) offered then to buy out the fund's partners for \$250 million, to inject \$3.75 billion and to operate LTCM within Goldman's own trading division. The offer was stunningly low to LTCM's partners because at the start of the year their firm had been worth \$4.7 billion. [Warren Buffett](#) gave Meriwether less than one hour to accept the deal; the time lapsed before a deal could be worked out.^[24]

Seeing no options left, the [Federal Reserve Bank of New York](#) organized a bailout of \$3.625 billion by the major creditors to avoid a wider collapse in the financial markets.^[25] The principal negotiator for LTCM was general counsel [James G. Rickards](#).^[26] The contributions from the various institutions were as follows:^{[27][28]}

- \$300 million: [Bankers Trust](#), [Barclays](#), [Chase](#), [Credit Suisse First Boston](#), [Deutsche Bank](#), [Goldman Sachs](#), [Merrill Lynch](#), [J.P.Morgan](#), [Morgan Stanley](#), [Salomon Smith Barney](#), [UBS](#)
- \$125 million: [Société Générale](#)
- \$100 million: [Paribas](#), [Credit Agricole](#)^[29]
- [Bear Stearns](#) and [Lehman Brothers](#)^[29] declined to participate.

In return, the participating banks got a 90% share in the fund and a promise that a supervisory board would be established. LTCM's partners received a 10% stake, still worth about \$400 million, but this money was completely consumed by their debts. The partners once had \$1.9 billion of their own money invested in LTCM, all of which was wiped out.^[30]

The fear was that there would be a chain reaction as the company liquidated its securities to cover its debt, leading to a drop in prices, which would force other companies to liquidate their own debt creating a [vicious cycle](#).

The total losses were found to be \$4.6 billion. The losses in the major investment categories were (ordered by magnitude):^[20]

- \$1.6 bn in [swaps](#)
- \$1.3 bn in equity [volatility](#)
- \$430 mn in Russia and other [emerging markets](#)
- \$371 mn in directional trades in [developed countries](#)
- \$286 mn in [Dual-listed company pairs](#) (such as VW, Shell)
- \$215 mn in [yield curve arbitrage](#)
- \$203 mn in [S&P 500](#) stocks
- \$100 mn in [junk bond](#) arbitrage
- no substantial losses in [merger](#) arbitrage



On September 23, 1998, the chiefs of some of the largest investment firms of Wall Street —[Bankers Trust](#), [Bear Stearns](#), [Chase Manhattan](#), [Goldman Sachs](#), [J.P. Morgan](#), [Lehman Brothers](#), [Merrill Lynch](#), [Morgan Stanley Dean Witter](#), and [Salomon Smith Barney](#)—met on the 10th floor conference room of the [Federal Reserve Bank of New York](#) (*pictured*) to rescue LTCM.

Diffusion coefficients of proteins in solution and in cell

VOL. 192, 2010

PROTEIN DIFFUSION IN THE CYTOPLASM OF *E. COLI* 4537

TABLE 1. Diffusion coefficients determined for GFP constructs in the cytoplasm of *E. coli* cells (unless indicated otherwise)^a

Protein ^b	Molecular mass (kDa)	<i>D</i> (μm ² s ⁻¹)	Treatment	Source or reference
GFP in water	27	87		26
GFP	27	7.7 ± 2.5	Induced with 100 μM IPTG ^c	6
GFP	27	3.6 ± 0.7	Induced with 1 mM IPTG	6
EYFP	26.5	7.08 ± 0.3		12
GFP-His ₆	27+	4.0 ± 2.0		6
cMBP-GFP	72	2.5 ± 0.6		6
CheY-GFP	41	4.6 ± 0.8		3
CFP-CheW-YFP	71	1.5 ± 0.05		12
CFP-CheR-YFP	86.2	1.7 ± 0.05		12
torA-GFP	30	9.0 ± 2.1	Cephalexin	18
GFP	27	9.8 ± 3.6	Cephalexin	28
GFP	27	0.4 ± 0.3	After osmotic upshock with NaCl	28
GFP	27	6.3 ± 1.1		25
GFP	27	3.1 ± 1.0	After osmotic shock	25
torA-GFP2 in <i>ΔtatABCDE</i> strain	57	7.5 ± 3.9	Cephalexin, 2% arabinose	This study
GFP2	27	9.1 ± 5.1	Cephalexin	This study
torA-GFP2	57	8.3 ± 4.2	Cephalexin, 500 μM arabinose	This study
torA-GFP3	84	6.3 ± 2.6	Cephalexin, 200 μM arabinose	This study
torA-GFP4	111	5.5 ± 1.9	Cephalexin, 1 mM arabinose	This study
torA-GFP5	138	2.8 ± 1.5	Cephalexin, 800 μM arabinose	This study
AmiA-GFP	58	1.8 ± 0.8	2% arabinose	This study
AmiA-GFP	58	1.8 ± 1.2	Cephalexin, 2% arabinose	This study
AmiA _{noSP} -GFP	58	7.1 ± 3.6	Cephalexin, 2% arabinose	This study
NlpA-GFP	55	2.1 ± 1.4	Cephalexin, 2% arabinose	This study
NlpA _{noLB} -GFP	55	2.7 ± 3.2	Cephalexin, 2% arabinose	This study

^a The techniques used were FRAP and photoactivation of a red-emitting fluorescence state of GFP (6), fluorescence correlation spectroscopy (3), confocal FRAP (12, 18), pulsed FRAP (28), and continuous photobleaching with evanescent illumination (25).

^b EYFP, enhanced yellow fluorescent protein; cMBP, cytoplasmic maltose-binding protein.

^c IPTG, isopropyl-β-D-thiogalactopyranoside.