

ELECTRIC CIRCUITS

Ohm's Law

$$V = I \cdot R \text{ (Some books use } E = I \cdot R \text{)}$$

where: V = voltage (volts or V)

I = current (amperes or amps or A)

R = resistance (ohms or Ω)

Equivalent Resistance

Series Resistance:

Given resistors $R_1, R_2, R_3, \dots, R_N$; connected in series.

The equivalent resistance is given by the formula:

$$R_{EQ} = R_1 + R_2 + R_3 + \dots + R_N$$

Parallel Resistance:

Given resistors $R_1, R_2, R_3, \dots, R_N$; connected in parallel.

The equivalent resistance is given by the formula:

$$1 / R_{EQ} = 1 / R_1 + 1 / R_2 + 1 / R_3 + \dots + 1 / R_N$$

$$\frac{1}{R_{EQ}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_N}$$

For the “special” case (or short cut) of two resistors (R_1 and R_2) connected in parallel, the formula becomes:

$$R_{EQ} = (R_1 \cdot R_2) / (R_1 + R_2)$$

$$R_{EQ} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

Voltage Law

The voltage changes around any closed loop in an electric circuit must sum to zero.

Voltage Divider Rule

For a circuit with two resistors, R1 and R2, in series, the voltage drop across each resistor equals the resistance times the total voltage, divided by the sum of the two resistors.

$$V_1 = \frac{V_s \cdot R1}{(R1 + R2)}$$

$$V_2 = \frac{V_s \cdot R2}{(R1 + R2)}$$

Current Law

The electric current which flows into any junction in an electric circuit is equal to the current which flows out.

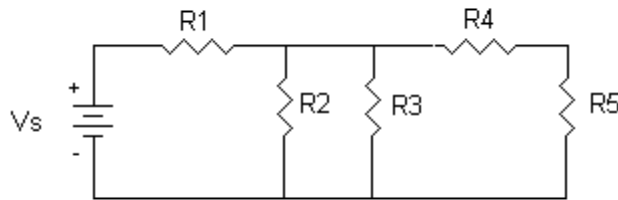
Current Divider Rule

For two parallel resistors, R1 and R2, the current through the branch equals the resistance of the opposite branch times the input current divided by the sum of the two resistors.

$$I_1 = \frac{I \cdot R_2}{(R_1 + R_2)}$$

$$I_2 = \frac{I \cdot R_1}{(R_1 + R_2)}$$

Circuit Example



If $R_1 = 24 \, \Omega$, $R_2 = 24 \, \Omega$, $R_3 = 12 \, \Omega$, $R_4 = 12 \, \Omega$, $R_5 = 12 \, \Omega$ and $V_s = 12$ Volts, determine the circuit equivalent resistance (R_{EQ}) and the circuit current (I). Also calculate the branch currents through R_2 , R_3 , R_4 , and R_5 , and the voltage drops across R_1 , R_2 , R_3 , R_4 and R_5 .

Solution

Calculate R_{45} (Series Resistance)

$$R_{45} = R_4 + R_5 = 12 + 12$$

$$R_{45} = 24 \, \Omega$$

Calculate R_{345} (Parallel Resistance)

$$1/R_{345} = 1/R_3 + 1/R_{45} = 1/12 + 1/24 = 2/24 + 1/24 = 3/24$$

$$\text{Therefore, } R_{345} = 8 \, \Omega$$

Calculate R_{2345} (Parallel Resistance)

$$1/R_{2345} = 1/R_2 + 1/R_{345} = 1/24 + 1/8 = 1/24 + 3/24 = 4/24$$

$$\text{Therefore, } R_{2345} = 6 \, \Omega$$

Calculate R_{EQ} (Series Resistance)

$$R_{EQ} = R_1 + R_{2345} = 24 \, \Omega + 6 \, \Omega$$

$$R_{EQ} = 30 \, \Omega$$

Calculate the circuit current. Use Ohm's Law $V = I \cdot R$

$$12 \text{ V} = I \cdot 30 \Omega$$

$$\text{Therefore, } I = 12/30$$

$$\mathbf{I = 0.4 \text{ A}}$$

Calculate the voltage drop across R1

$$V_1 = I \cdot R_1 = 0.4 \text{ A} \cdot 24 \Omega$$

$$\mathbf{V_1 = 9.6 \text{ V}}$$

Calculate the voltage drops across R2 and R3

$$V_2 = V_3 = 12 \text{ V} - 9.6 \text{ V}$$

$$\mathbf{V_2 = V_3 = 2.4 \text{ V}}$$

Calculate the current through R2

$$I_2 = V_2 / R_2 = 2.4 \text{ V} / 24 \Omega$$

$$\mathbf{I_2 = 0.1 \text{ A}}$$

Calculate the current through R3

$$I_3 = V_3 / R_3 = 2.4 \text{ V} / 12 \Omega$$

$$\mathbf{I_3 = 0.2 \text{ A}}$$

Calculate the current through R4 and R5

$$\text{The voltage drop across } R_{45} = V_2 = V_3 = 2.4 \text{ V}$$

$$\text{Therefore } I_4 = I_5 = V_{45} / R_{45} = 2.4 \text{ V} / 24 \Omega$$

$$\mathbf{I_4 = I_5 = 0.1 \text{ A}}$$

Finally, calculate the voltage drops across R4 and R5

$$V_4 = I_4 \cdot R_4 = 0.1 \text{ A} \cdot 12 \Omega$$

$$\mathbf{V_4 = 1.2 \text{ V}}$$

$$V_5 = I_5 \cdot R_5 = 0.1 \text{ A} \cdot 12 \Omega$$

$$\mathbf{V_5 = 1.2 \text{ V}}$$