



# Relativized Succinct Arguments in the ROM Do Not Exist

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EPFL



<https://eprint.iacr.org/2024/728>

Succinct non-interactive arguments

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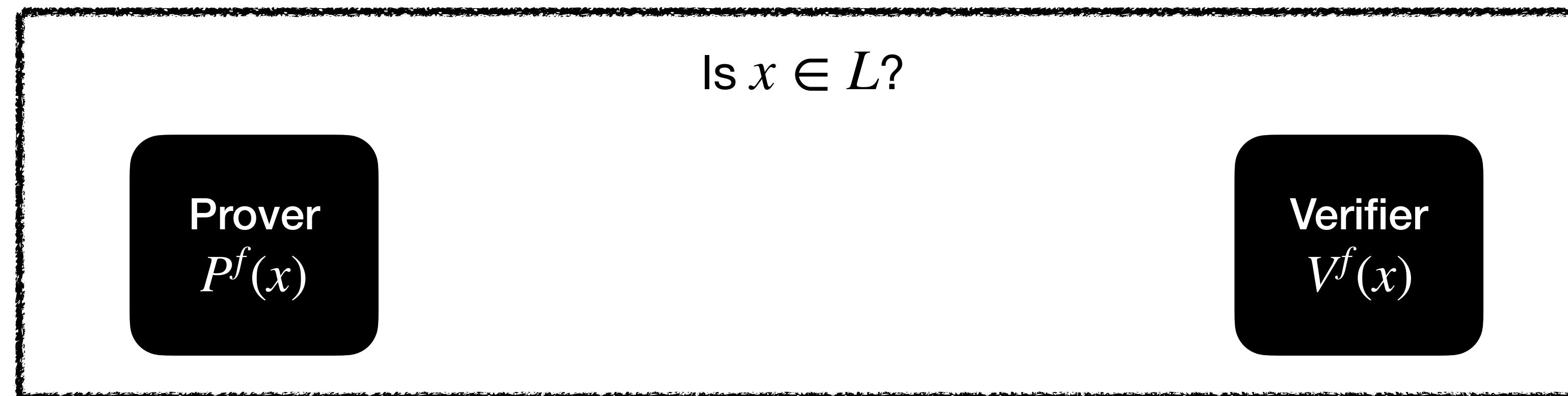


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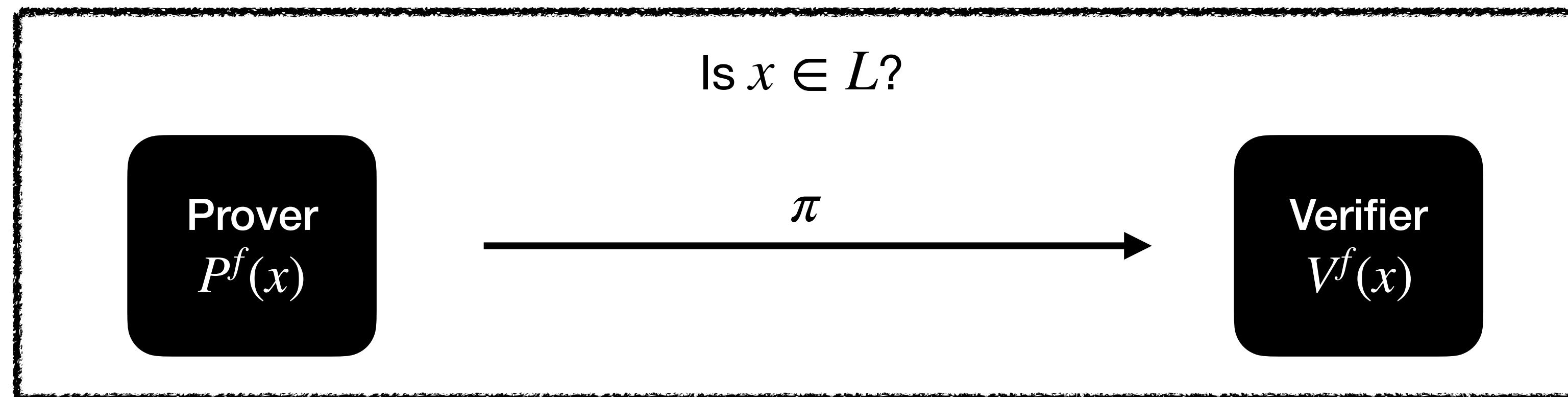


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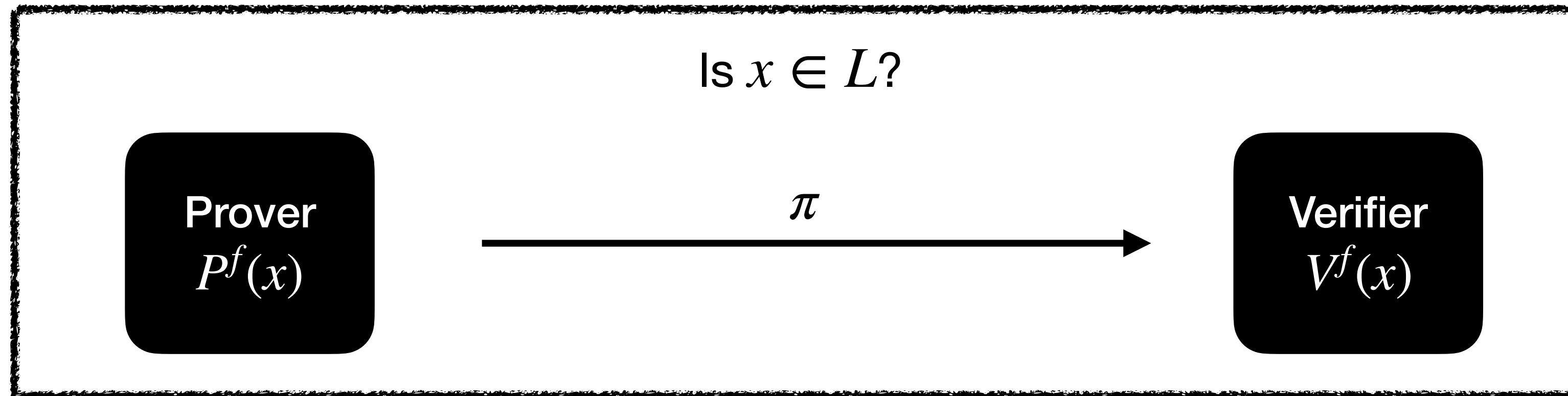


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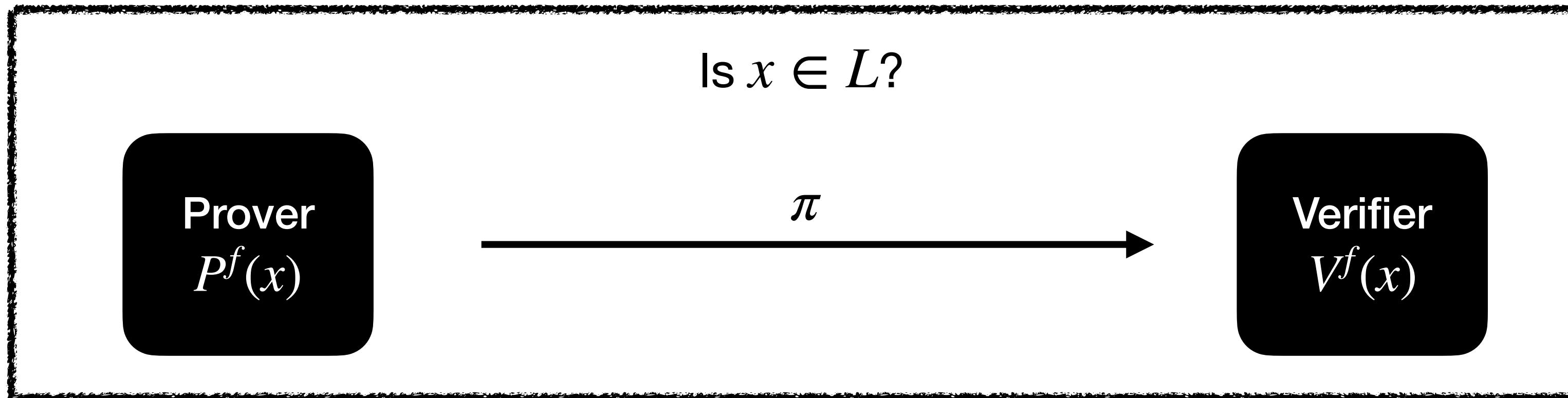
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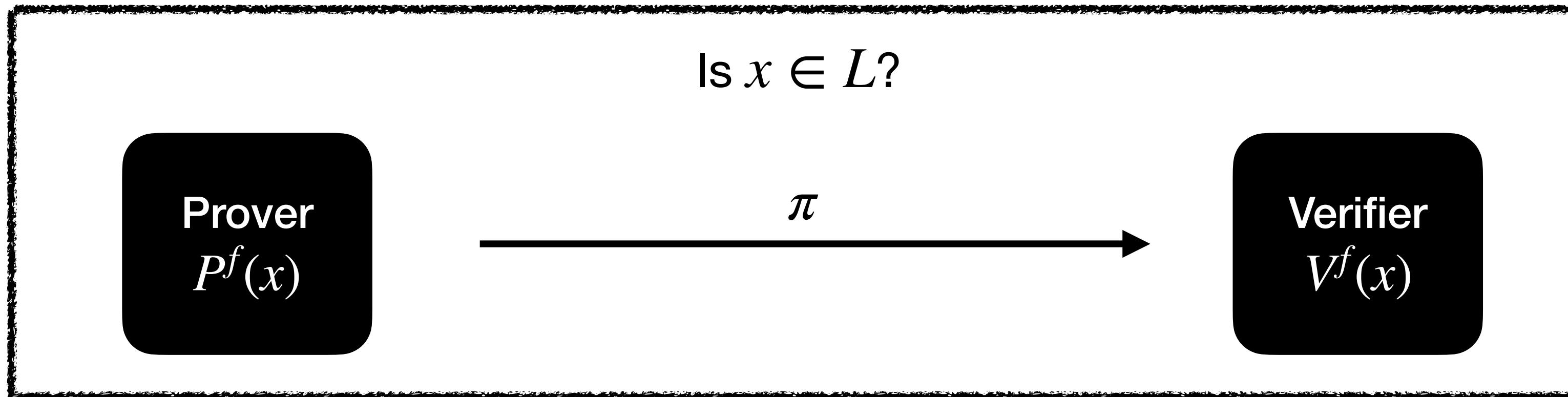
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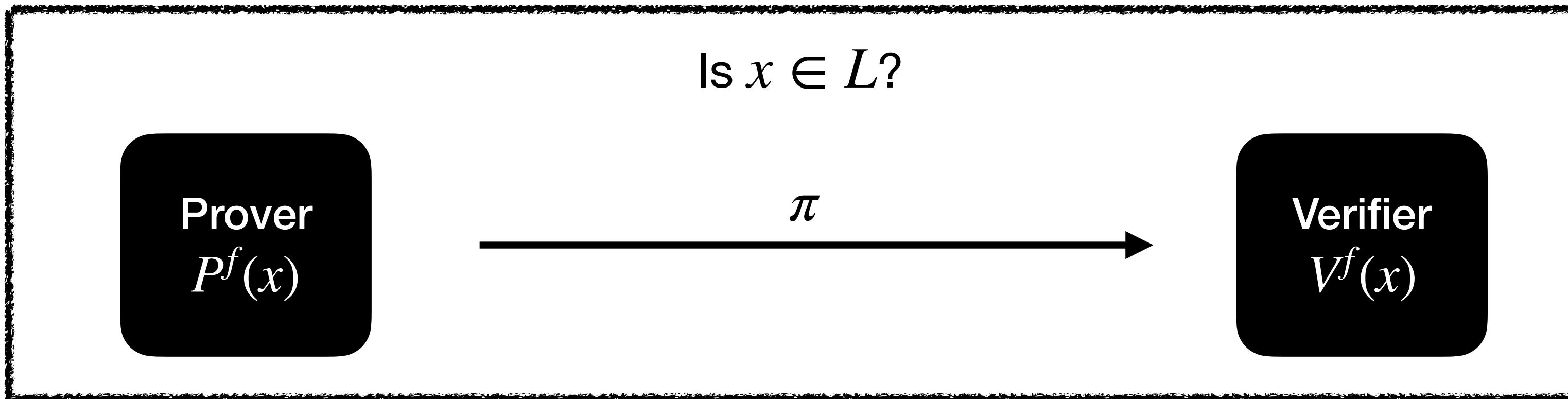
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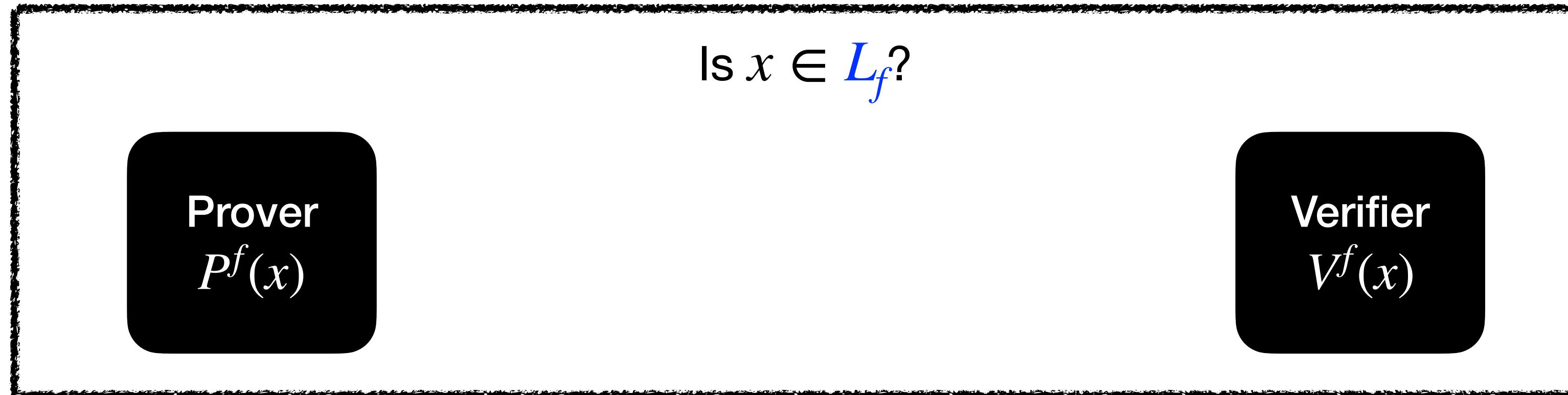


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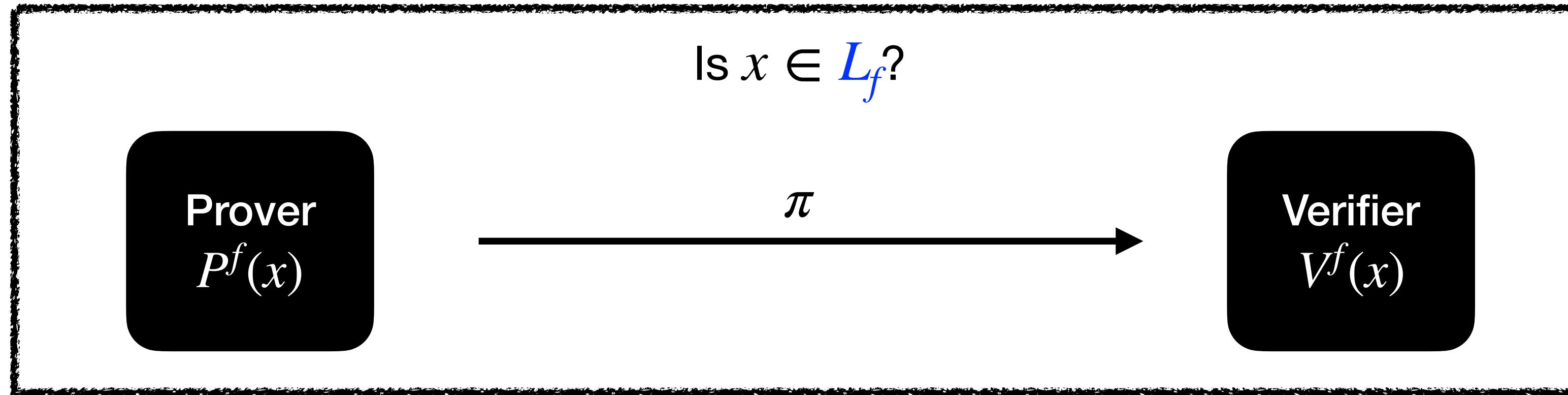


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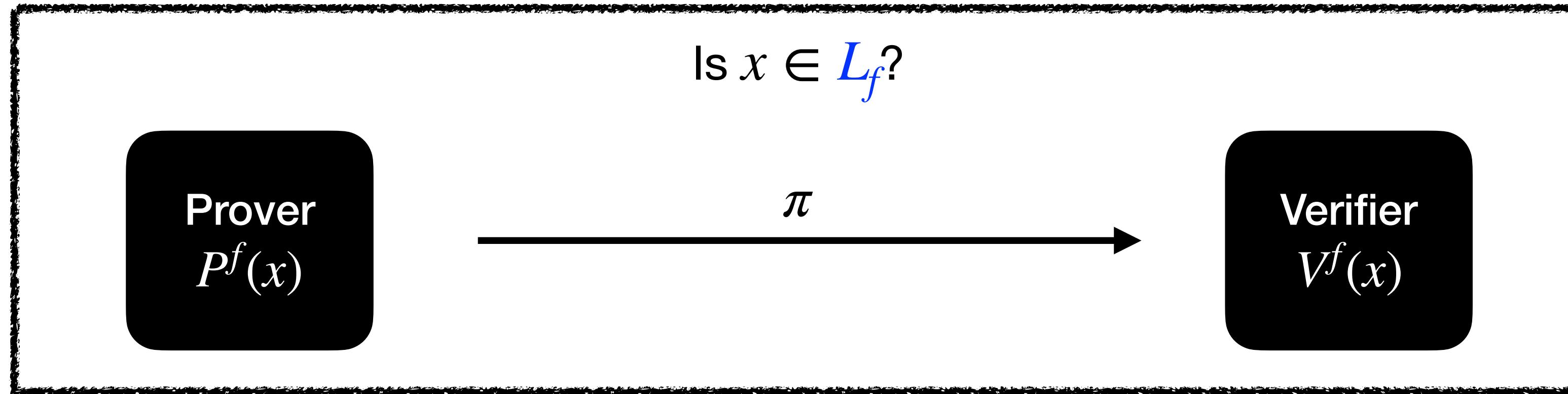


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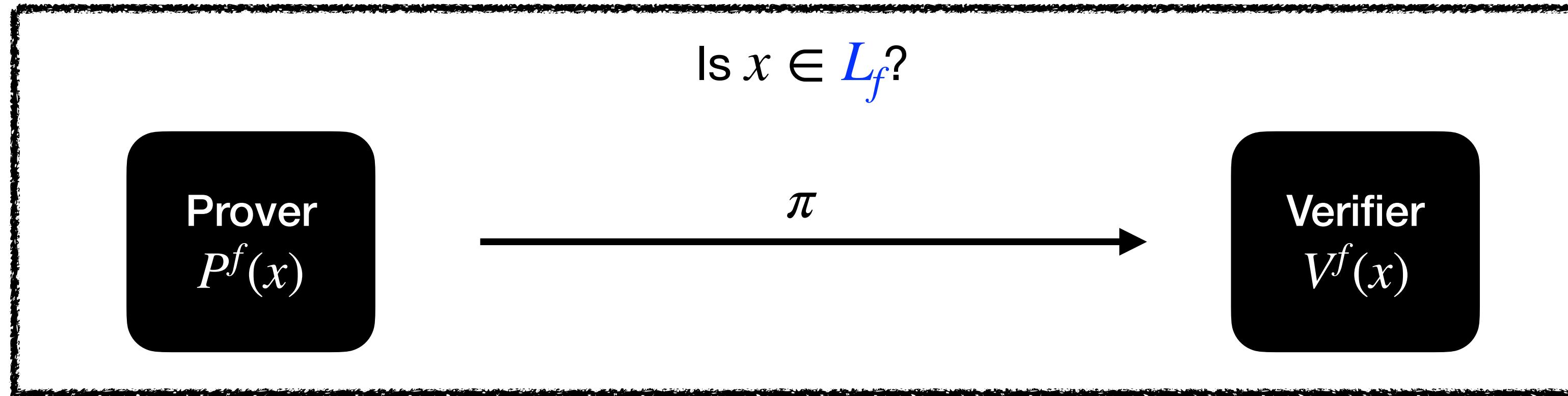
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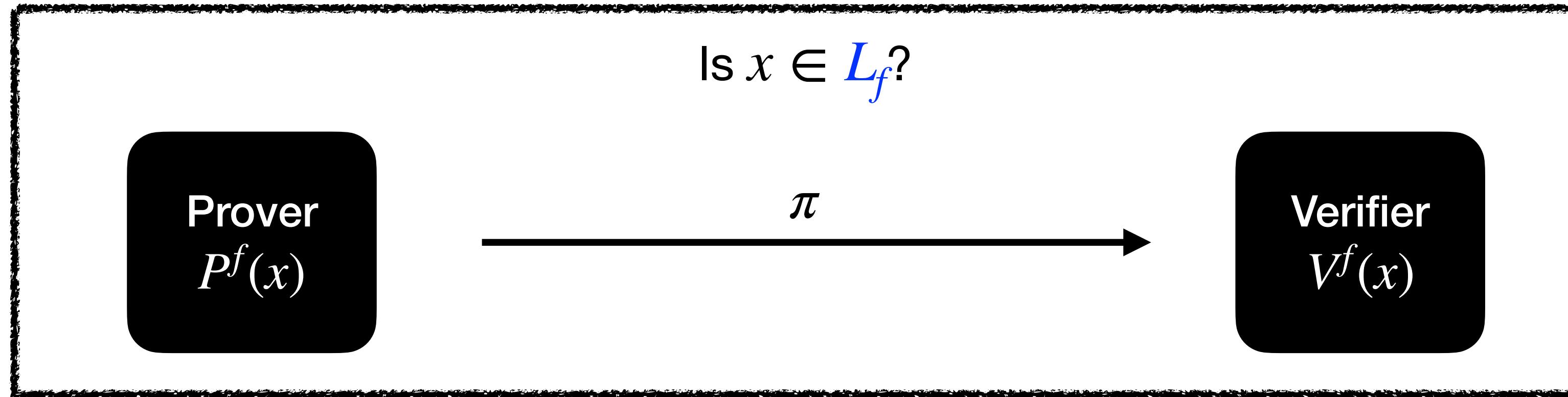
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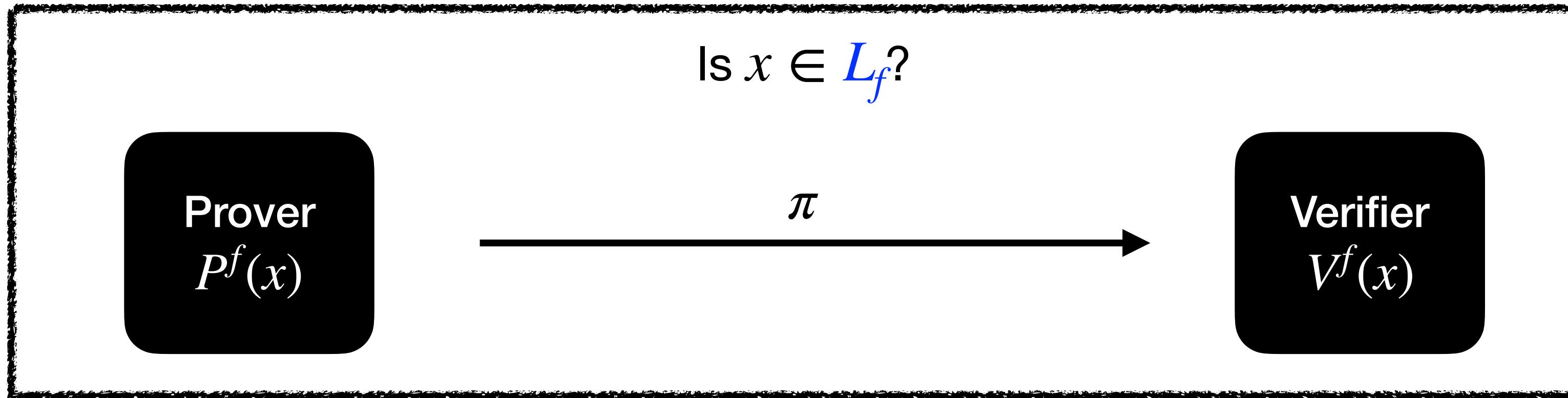
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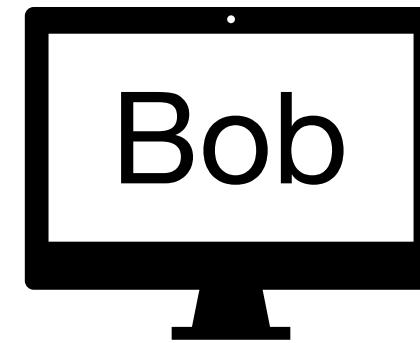
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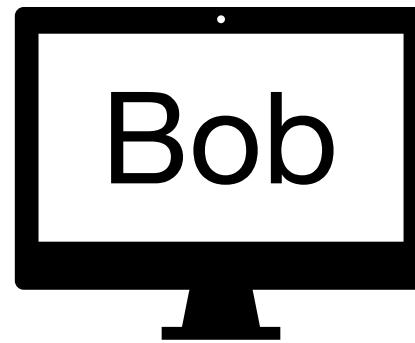
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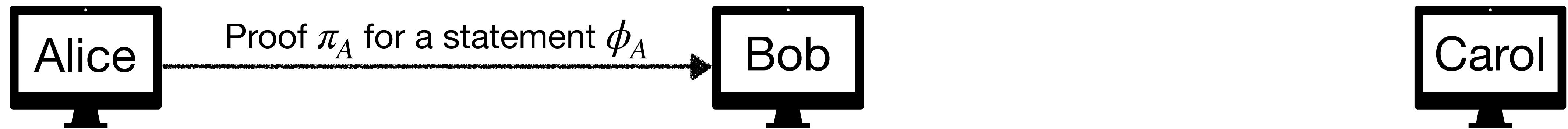
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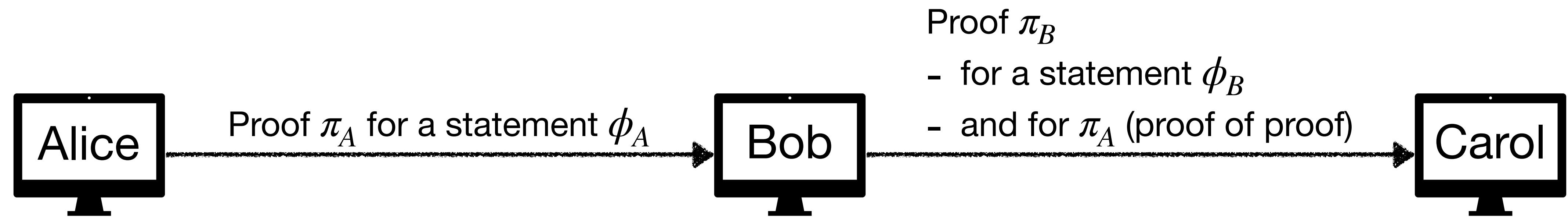
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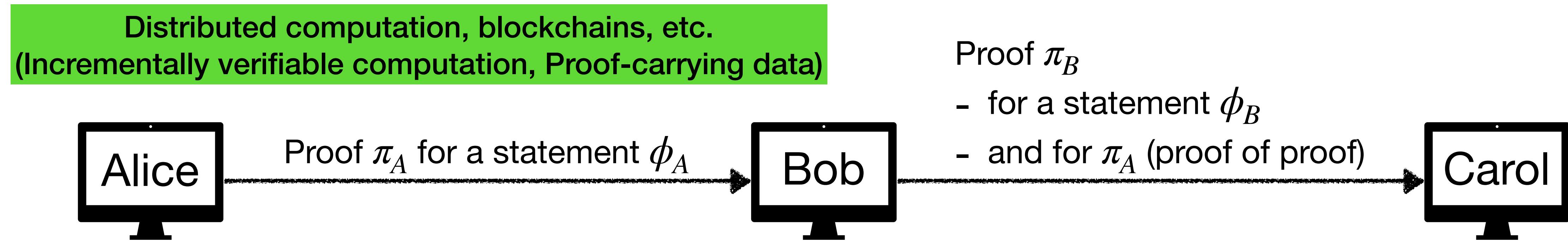
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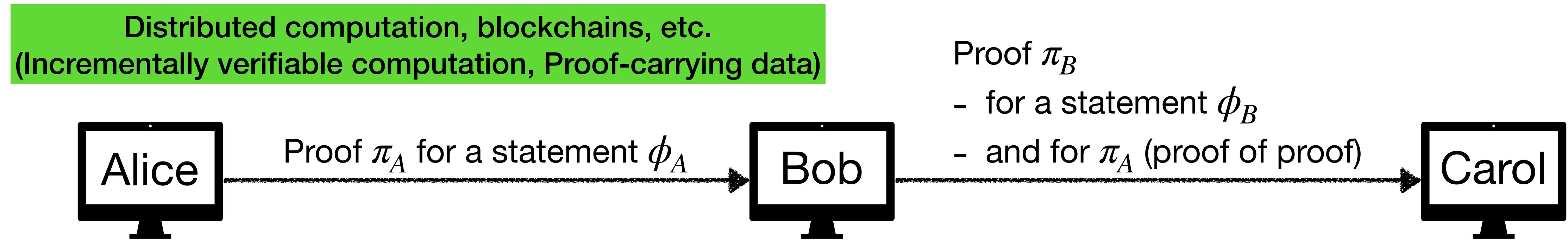
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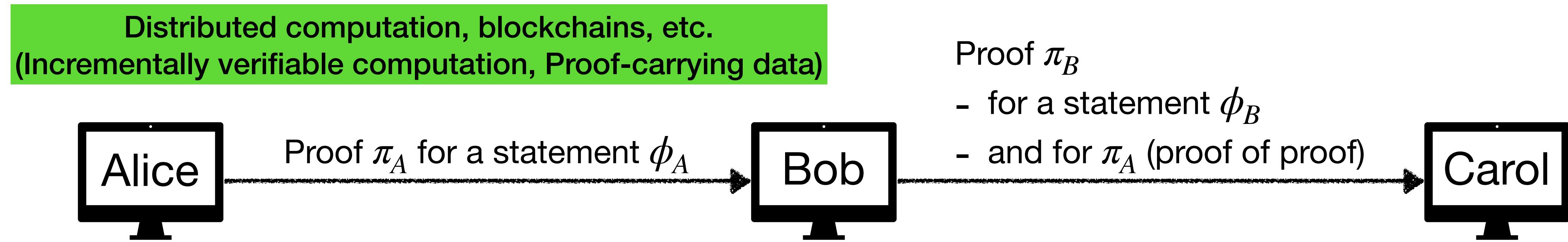
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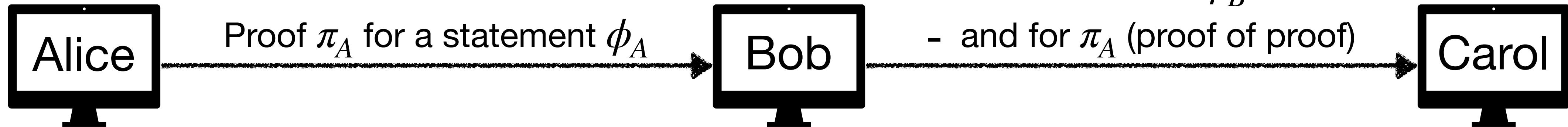
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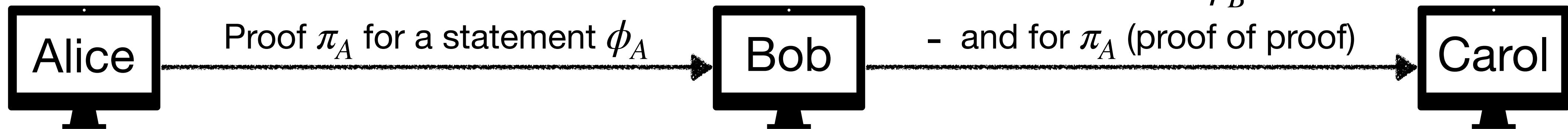
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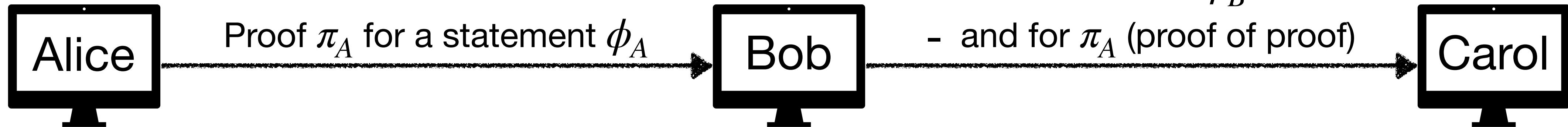
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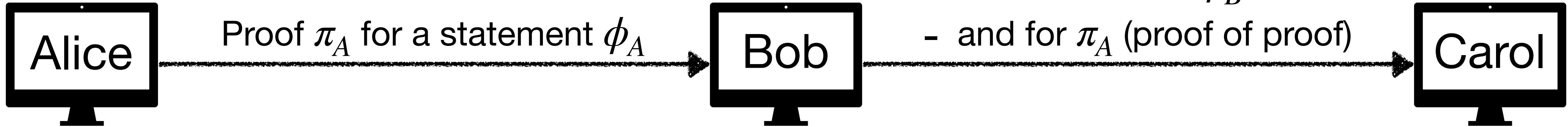
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**Note.**

- The results hold for SNARGs secure against **query-bounded** and **time-bounded** adversaries.
- Similar results hold for interactive arguments.

# **Open problem: Characterization**

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Easy to learn/predict

Hard to learn/predict

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Structured Oracle

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Learn the oracle and use non-relativized SNARGs

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**Open problem.**

Give a sufficient and necessary condition for an oracle that separates DTIME/NTIME and relativized arguments.

# Insights into Fiat-Shamir

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Interactive protocol  
in the standard model

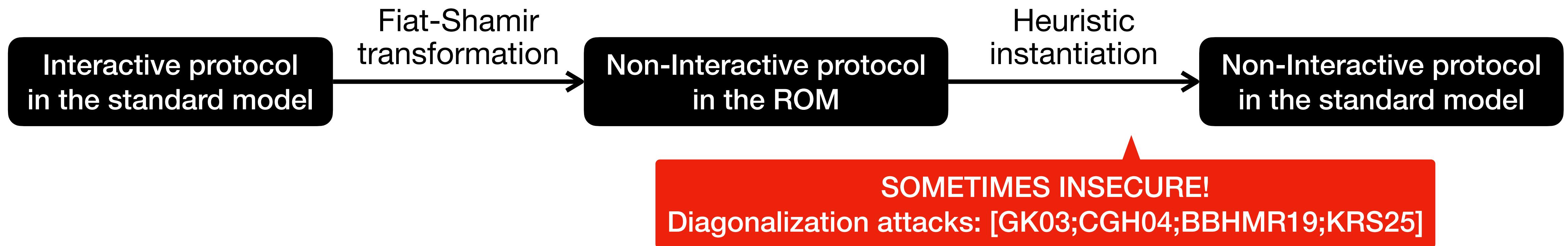
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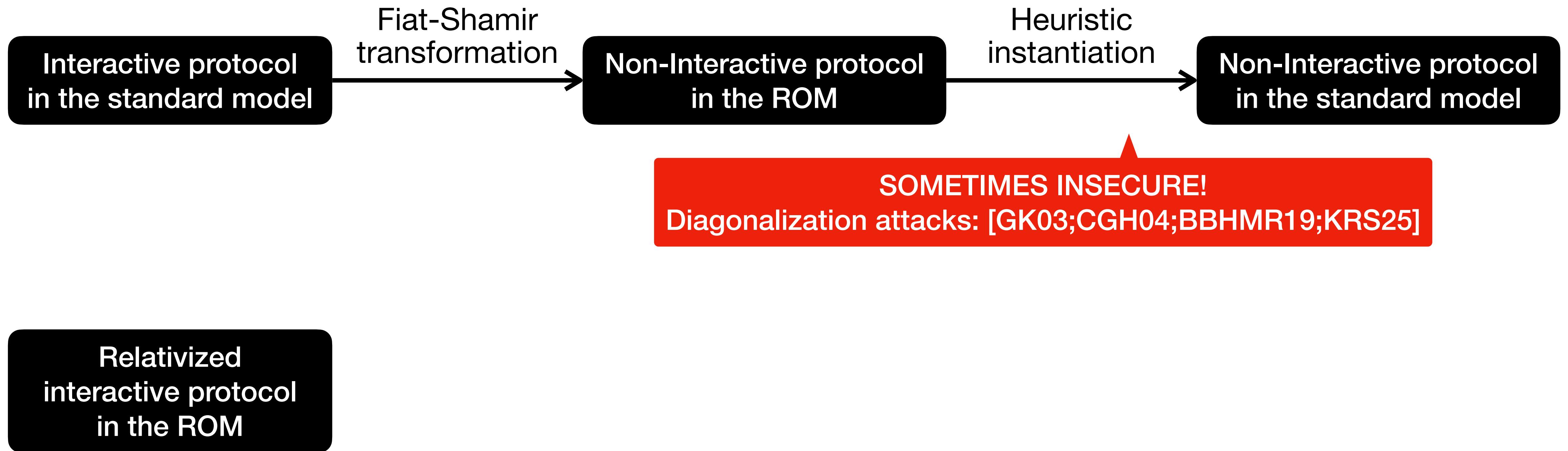
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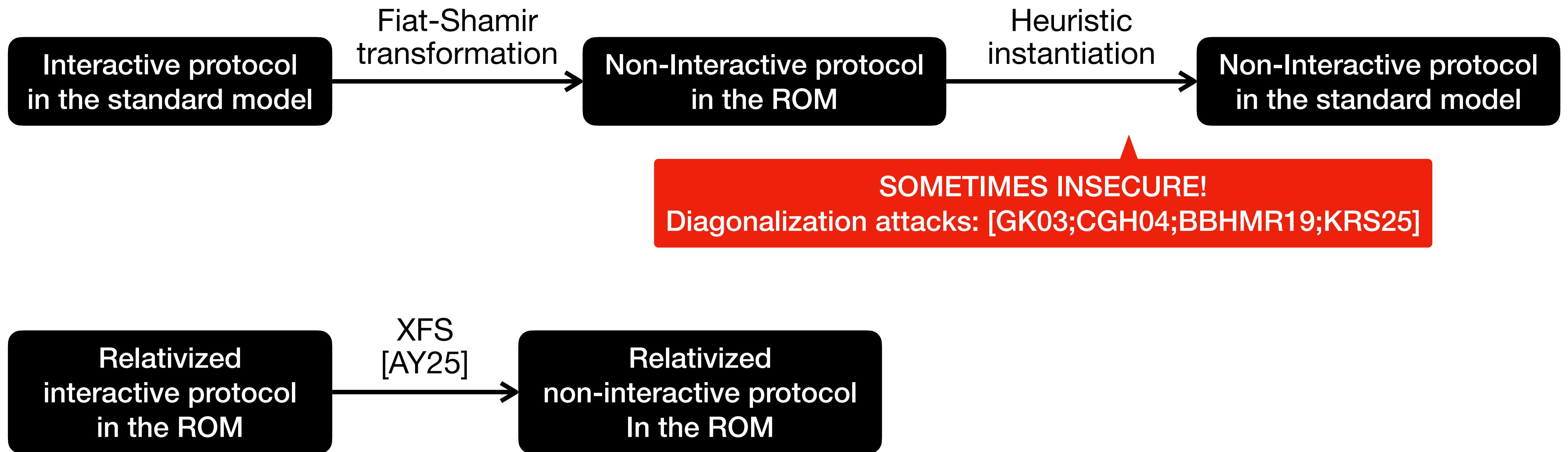
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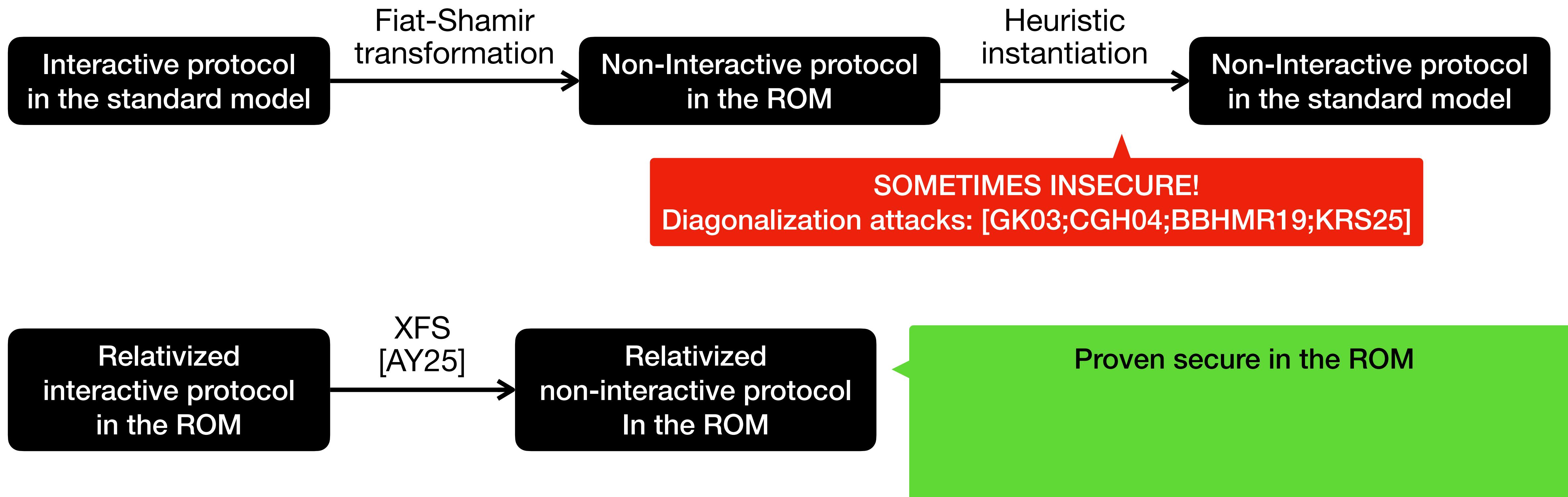
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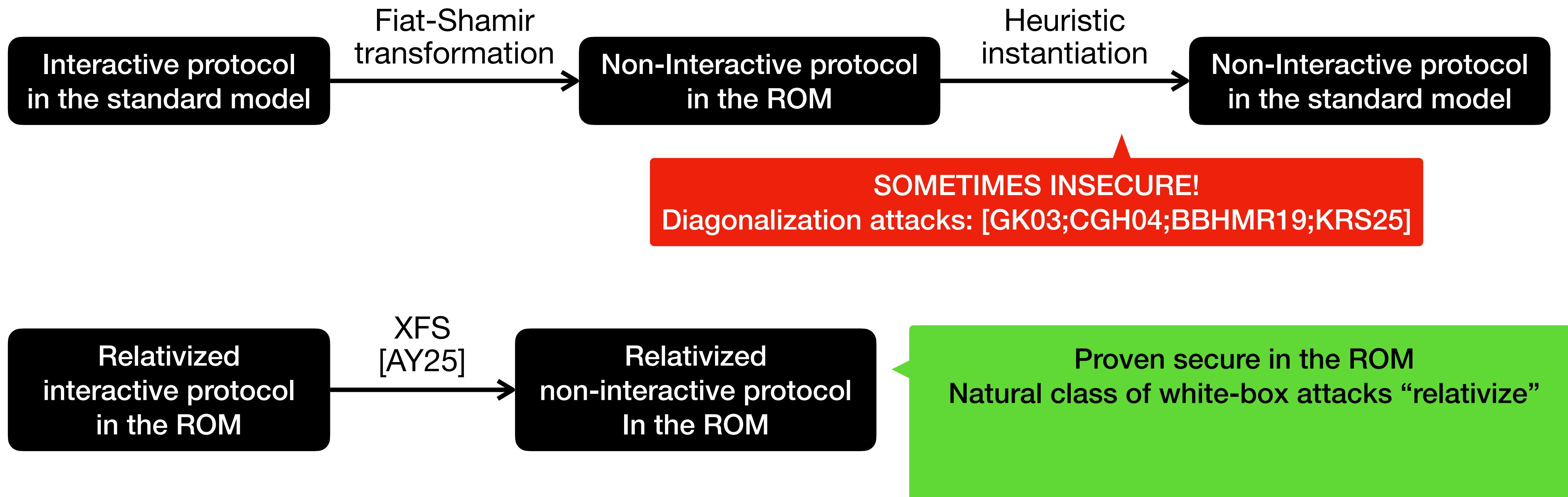
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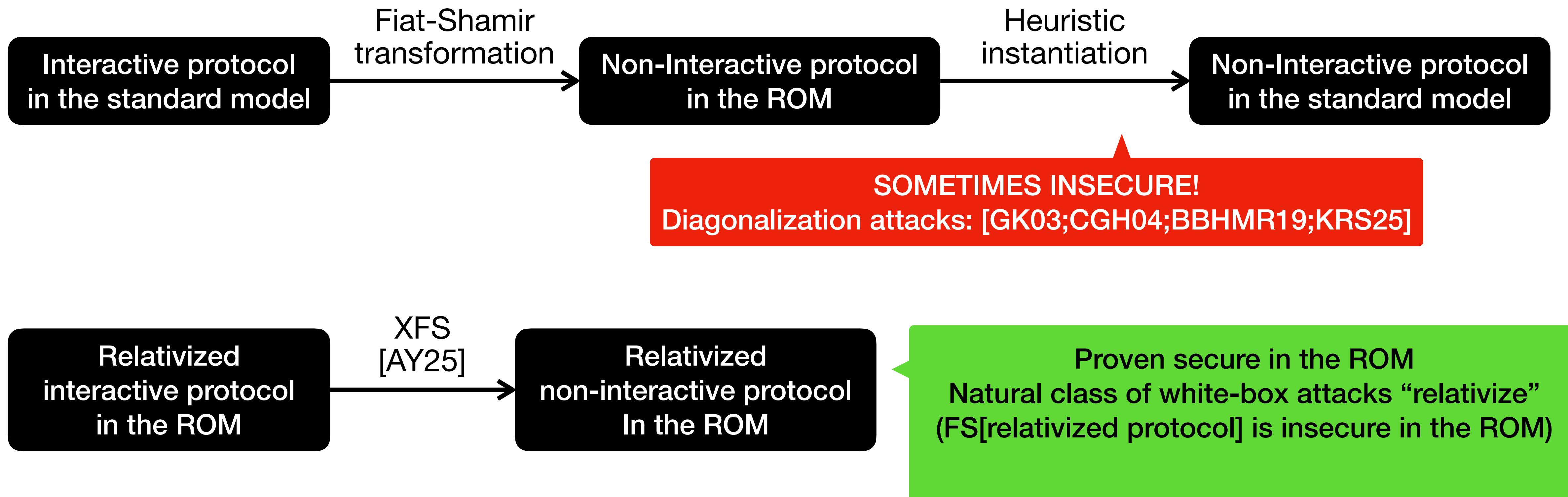
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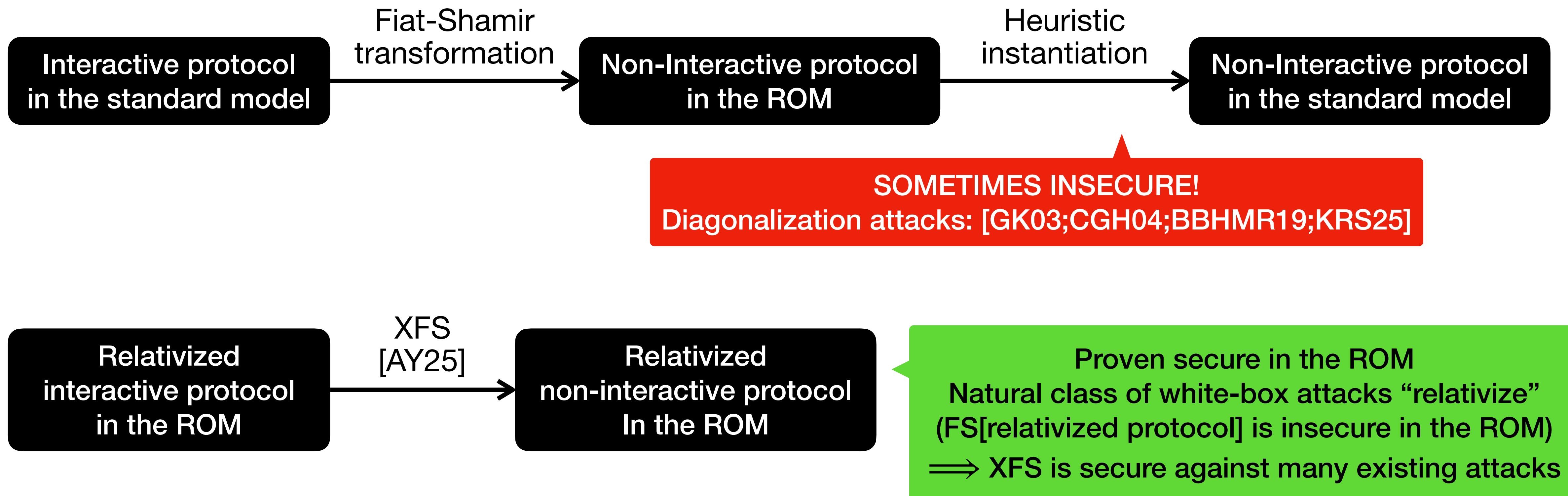
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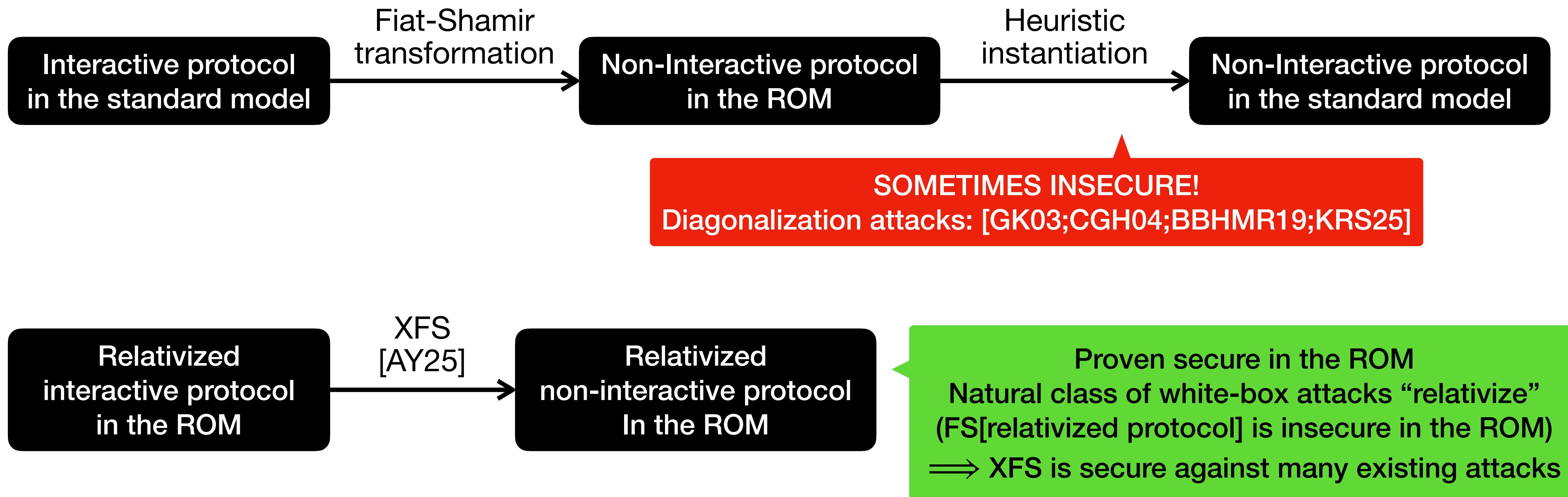
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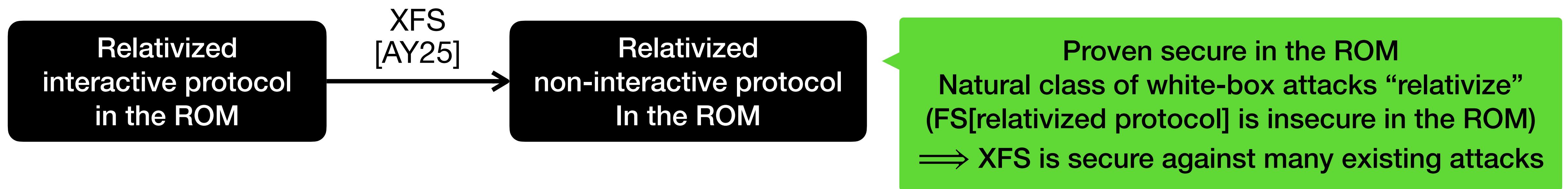


Is Fiat-Shamir transformation secure in other oracle models? LDROM? AROM?

# Insights into Fiat-Shamir



SOMETIMES INSECURE!  
Diagonalization attacks: [GK03;CGH04;BBHMR19;KRS25]



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Thank you!