

CSE222 / BİL505
Data Structures and Algorithms
Homework #6 – Report

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1) Selection Sort

Time Analysis	**Time Analysis:** - **Best Case:** $O(n^2)$ because even if the array is already sorted, comparisons are still needed. - **Worst Case:** $O(n^2)$ due to nested loops comparing each element to find the minimum. - **Average Case:** $O(n^2)$ for similar reasons. **Example Run:** Input: `[64, 25, 12, 22, 11]` Output: `[11, 12, 22, 25, 64]` Comparison Counter: 10, Swap Counter: 4
Space Analysis	- **Space Complexity:** $O(1)$ because only a few variables are needed for swapping.

2) Bubble Sort

Time Analysis	**Time Analysis:** - **Best Case:** $O(n)$ when the array is already sorted (no swaps occur). - **Worst Case:** $O(n^2)$ because all adjacent pairs must be compared. - **Average Case:** $O(n^2)$ as nested loops compare adjacent pairs. **Example Run:** Input: `[64, 25, 12, 22, 11]` Output: `[11, 12, 22, 25, 64]` Comparison Counter: 10, Swap Counter: 9
Space Analysis	- **Space Complexity:** $O(1)$ as it requires a constant amount of memory for swapping.

3) Quick Sort

Time Analysis	**Time Analysis:** <ul style="list-style-type: none">- **Best Case:** $O(n \log n)$ when the pivot divides the array into roughly equal halves.- **Worst Case:** $O(n^2)$ when the pivot repeatedly divides the array into unbalanced partitions.- **Average Case:** $O(n \log n)$ due to partitioning. **Example Run:** Input: <code>[64, 25, 12, 22, 11]</code> Output: <code>[11, 12, 22, 25, 64]</code> Comparison Counter: 9, Swap Counter: 7
Space Analysis	**Space Analysis:** <ul style="list-style-type: none">- **Space Complexity:** $O(\log n)$ due to the recursive call stack.

4) Merge Sort

Time Analysis	**Time Analysis:** <ul style="list-style-type: none">- **Best Case:** $O(n \log n)$ because the array is always split into two halves.- **Worst Case:** $O(n \log n)$ due to consistent partitioning.- **Average Case:** $O(n \log n)$ as partitioning remains consistent. **Example Run:** Input: <code>[64, 25, 12, 22, 11]</code> Output: <code>[11, 12, 22, 25, 64]</code> Comparison Counter: 6, Swap Counter: 0
Space Analysis	- **Space Complexity:** $O(n)$ due to the temporary arrays used during merging.

General Comparison of the Algorithms

- **Time Complexity Comparison:****
 - ****Selection Sort:**** $O(n^2)$
 - ****Bubble Sort:**** $O(n^2)$
 - ****Quick Sort:**** $O(n \log n)$
 - ****Merge Sort:**** $O(n \log n)$
- **Space Complexity Comparison:****
 - ****Selection Sort:**** $O(1)$
 - ****Bubble Sort:**** $O(1)$
 - ****Quick Sort:**** $O(\log n)$
 - ****Merge Sort:**** $O(n)$