

1. (1 point)

Evaluate the integral

$$\int \frac{-6\sqrt{x}}{1+x^3} dx$$

Answer: _____ + C

[Click for a hint](#)

2. (1 point)

Evaluate the indefinite integral

$$\int \frac{1}{4\cos x + 3\sin x + 1} dx$$

Answer: _____ + C

3. (1 point)

Evaluate the indefinite integral

$$\int x^2 \sin(4x+2) dx$$

Answer: _____ + C

4. (1 point)

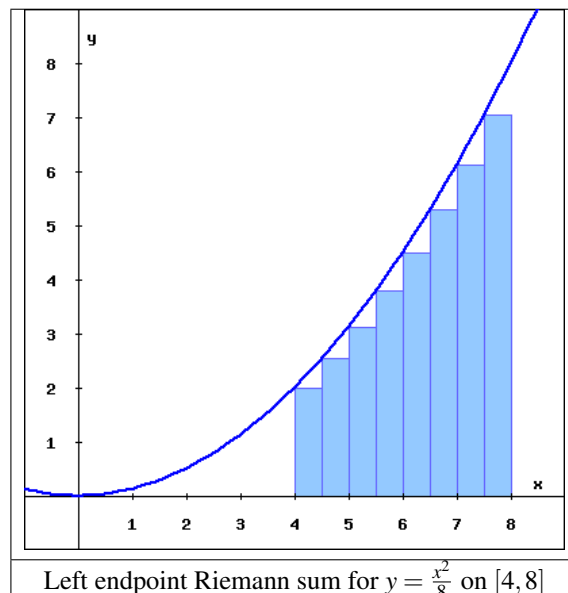
Evaluate the indefinite integral

$$\int x \tan^{-1}(3x) dx$$

Answer: _____ + C

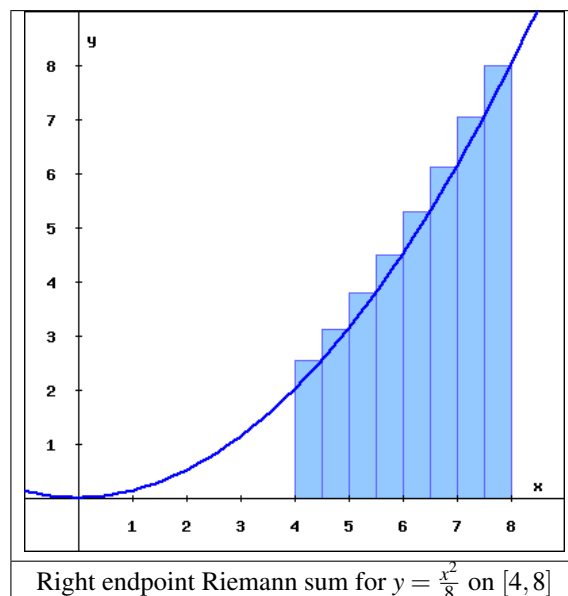
5. (1 point) a) The rectangles in the graph below illustrate a "left endpoint" Riemann sum for $f(x) = \frac{x^2}{8}$ on the interval $[4, 8]$.

The value of this Riemann sum is _____, and this Riemann sum is an the area of the region enclosed by $y = f(x)$, the x-axis, and the vertical lines $x = 4$ and $x = 8$.



b) The rectangles in the graph below illustrate a "right endpoint" Riemann sum for $f(x) = \frac{x^2}{8}$ on the interval $[4, 8]$.

The value of this Riemann sum is _____, and this Riemann sum is an the area of the region enclosed by $y = f(x)$, the x-axis, and the vertical lines $x = 4$ and $x = 8$.



6. (1 point)

Evaluate the definite integral:

$$\int_{-1}^6 |x - 4x^2| dx = \underline{\hspace{2cm}}$$

7. (1 point)

Evaluate the following integral:

$$\int_1^2 \frac{-5 \ln(x)}{x^2} dx$$

8. (1 point)

Evaluate the integral

$$\int_0^{\pi/2} \frac{9 \cos t}{\sqrt{1 + \sin^2(t)}} dt$$

9. (1 point)

Evaluate the integral

$$\int_{-1}^2 (-1x - 3|x|) dx$$

Integral =

10. (1 point) Use the Fundamental Theorem of Calculus to find the derivative $\frac{dy}{dx}$, where:

$$y = \int_9^{\sqrt{x}} \frac{\cos t}{t^{13}} dt, \quad x > 0.$$

$$\frac{dy}{dx} = \underline{\hspace{2cm}}$$

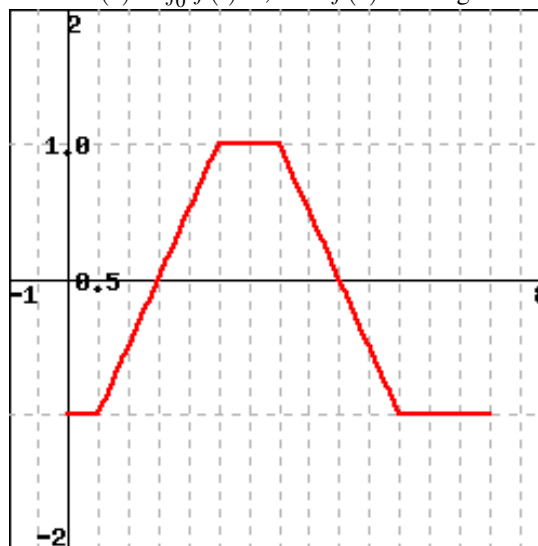
11. (1 point) Find a function f and a number a such that

$$2 + \int_a^x \frac{f(t)}{t^2} dt = 3x^{-3}$$

$$f(x) = \underline{\hspace{2cm}}$$
$$a = \underline{\hspace{2cm}}$$

12. (1 point)

Let $A(x) = \int_0^x f(t) dt$, with $f(x)$ as in figure.



$A(x)$ has a local minimum on $(0, 7)$ at $x = \underline{\hspace{2cm}}$

$A(x)$ has a local maximum on $(0, 7)$ at $x = \underline{\hspace{2cm}}$

13. (1 point)

Let $I_n = \int_0^{\pi/2} \sin^n x dx$, for $n \geq 0$.

It is known that the following reduction formula holds for some constants A and B :

$$I_n = \frac{n+A}{n+B} I_{n-2} \quad \text{for } n \geq 2.$$

Find the values of A and B .

$$A = \underline{\hspace{2cm}}$$

$$B = \underline{\hspace{2cm}}$$

Click for a hint

Hence, evaluate I_{10} .

$$I_{10} = \underline{\hspace{2cm}}$$

14. (1 point) Determine whether the integral is divergent or convergent. If it is convergent, evaluate it. If not, enter *div*

$$\int_4^{+\infty} x e^{-3x} dx$$

Answer:

15. (1 point) Evaluate the improper integral.

$$\int_2^4 \frac{dx}{\sqrt{4x - x^2}}$$

Hint: Use the technique of completing the square.