

Q2: Car Share Home

given: arrive every 15 min until midnight

leave from $[11:00, 11:20]$ BART $\sim U(11:10, 11:30)$ let X = R.V. for time of train depart

$$f(x) = \begin{cases} \frac{1}{20} & , 11:10 \leq x \leq 11:30 \\ 0 & , \text{otherwise} \end{cases}$$

$$\begin{aligned} E[X] &= \int_{-\infty}^{\infty} x f(x) dx \\ &= \int_{-\infty}^{11:10} 0 dx + \int_{11:10}^{11:30} x f(x) dx + 0 \end{aligned}$$

$$\left. \frac{1}{40} x^2 \right|_{10}^{30} = \frac{900}{40} - \frac{100}{40} = \frac{800}{40} = 20 \text{ min}$$

$$E[X] = 20 \text{ mins}$$