CIV3221 Building structures and technology (Clayton and Sunway) Sarah Sapian (29148278)

Semester 2, 2020

Introduction

This exam is an open-book assessment. The answers provided to all questions must be submitted through Moodle. You are allowed to use computational aid (including calculators), and to refer to lecture notes or other materials (that must be properly cited and referenced in order to avoid plagiarism).

Exam duration: 2 hours and 10 mins

Scanning time: 30 mins

QUESTION 1 [10 marks]

- a) Identify differences between first and second order elastic analysis. [5 marks]
- b) What are the reasons that may cause the movement of facade. [5 marks]

QUESTION 2 [10 marks]

For a continuous beam ABC shown in Figure Q2, the following loads are applied:

- External moment at Point A, M = 10 kNm anti-clockwise
- Uniformly distributed load (UDL) between Points A and B, w = 3 kN/m
- Point load at midspan of BC, P = 10 kN

Point A is free (unsupported), Support B is a roller and Support C is fixed.

Given: E = 200,000 MPa, $I_{AB} = 10.8 \times 10^8 \text{mm}^4$, $I_{BC} = 10.8 \times 10^8 \text{mm}^4$, $L_{AB} = 4 \text{ m}$, $L_{BC} = 4 \text{ m}$

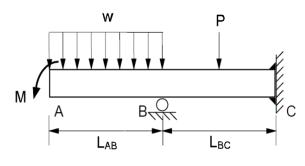


Figure Q2

- a) Using the moment distribution method, calculate the support reactions at B and C. [5 marks]
- b) Plot the bending moment and shear force diagrams. [5 marks]

QUESTION 3 [20 marks]

A simply supported composite slab in a composite floor structure of an office building is given below in Figure Q3. The live load is 3 kPa. The dead load consists of the floor self-weight plus a super-imposed dead load of 1 kPa . Take f'_c = 32 MPa , E_c = 28000 MPa and unit weight of reinforced concrete = 25 kN/mm³ and L = 2580 mm.

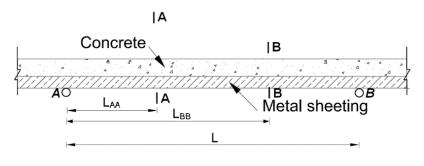


Figure Q3

- a) Check the serviceability limit state condition of this span using the deemed-to-comply span to depth ratio method. Take the overall depth of slab D = 120 mm. [10 marks]
- b) What is the sagging bending moment capacity for the section A-A with a distance of $L_{AA} = 900$ mm from the left support (A), and is it safe there in terms of bending moment capacity? [5 marks]
- c) What is the sagging bending moment capacity for the section B-B with a distance of $L_{BB} = 1880$ mm from the left support (A), and is it safe there in terms of bending moment capacity? [5 marks]

QUESTION 4 [16 marks]

The layout of a reinforced concrete floor is shown in Figure Q4 below for building construction. The overall depth of reinforced concrete slab is 120 mm. 460 UB 67.1 is used as the support steel girder for the secondary composite beam (nominal depth =460 mm, $A_s = 8580 \text{ mm}^2$, $f_{sy} = 300 \text{ MPa}$). All secondary beams are simply supported with a span length L of 8200 mm. The dead load consists of the floor self-weight plus a superimposed dead load of 1 kPa. Take $f'_c = 28 \text{ MPa}$, $E_c = 26,800 \text{ MPa}$ and unit weight of reinforced concrete = 24 kN/m³.

- a) What is the maximum live load that the composite beam can resist? [8 marks]
- b) Calculate the number and spacing of welded shear studs that ensure complete shear connection. Use studs with $d_{bs} = 19 \text{ mm}$ and $f_{uc} = 410 \text{ MPa}$. [8 marks]



QUESTION 5 [30 marks]

A 310UC158 (BHP 300 PLUS) is under combined compression force (N*) and bending moment (M_x *) about its major x-axis. The capacity factor $\phi = 0.9$. The moment ratio $\beta_m = 1.0$.

The applied compression force N^* is 2000 kN. The bending moment M_x^* is the product of N^* and the load eccentricity (e) which is 100 mm. The column length L=3000 mm. The boundary condition of the column can be assumed as fixed at both ends. Section constant $\alpha_b=0$. Assume FLR is provided.

- (a) Calculate the design column member capacity about x-axis (ϕN_{cx}). [5 marks]
- (b) Determine the design in-plane section and member capacities ϕM_{rx} and ϕM_i using the special formulae. Check if the member capacity is adequate. [15 marks]
- (c) Compare the maximum eccentricities (e) can be applied to the member for the given N^* based on the general and special formulae? [10 marks]

QUESTION 6 [14 marks]

Assuming that a typical column rests on a rectangular footing through a $X_c \times Y_c$ (450×400) mm base plate, calculate the maximum design column load N^* the footing can support in terms of bending and punching shear. Assume planar dimensions of the footing to be $X_b \times Y_b$ (1900×1900) mm and its overall depth D=500 mm with a concrete cover thickness of 75 mm. The concrete compressive strength f'_c is 32 MPa and the steel reinforcements (f_v =500 MPa) are placed as shown in Fig. Q6.

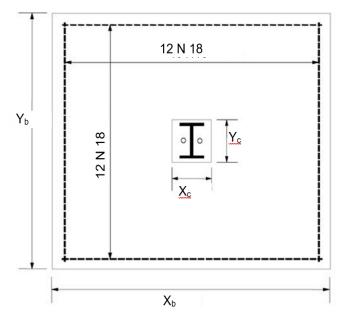


Figure Q6. Plan view of the footing for a single column (not to scale), with steel reinforcements N18 (diameter 18 mm) in each direction

End of exam paper

1 Solution

Step 1: Define coordinate system. This is already provided in ??.

Step 2: The unknown degrees of freedom are:

- Rotation about global y-axis at C (θ_C)
- Rotation about global y-axis at D (θ_D)
- Rotation about global y-axis at F (θ_F)

Due to symmetry of members CD and CF, and no applied point load, the degree of freedom for translation C is known: $\delta_C = 0$. Hence;

$$DOF = \{\theta_C, \theta_D, \theta_F\} \tag{1}$$

Step 3: The known forces corresponding to the unknown DOF are:

$$F = \{-80, 0, 0\} \quad [kNm] \tag{2}$$

Note, the negative sign as per the direction of the double-headed arrow.

Step 4: Apply θ_C positively only.

This causes bending along member DCF, and twisting along member ECG.

Step 5: Get forces at each DOF.

Moment in the direction of θ_C caused by θ_C :

- In Element DC: $M_C = \left(\frac{4EI}{L}\right)\theta_C$
- In Element CF: $M_C = \left(\frac{4EI}{L}\right)\theta_C$
- In Element EC: $M_C = \left(\frac{GJ}{L}\right)\theta_C$
- In Element CG: $M_C = \left(\frac{GJ}{L}\right)\theta_C$

As all member properties are equal, then:

$$M_C = \frac{8EI + 2GJ}{L}\theta_C \tag{3}$$

Moment in the direction of θ_D caused by θ_C :

• In Element DC: $M_D = \left(\frac{2EI}{L}\right)\theta_C$

Moment in the direction of θ_F caused by θ_C :

• In Element CF: $M_F = \left(\frac{2EI}{L}\right)\theta_C$

Step 6: Repeat for each DOF

Apply θ_D positively only and get forces at each DOF.

Moment in the direction of θ_C caused by θ_D :

• In Element DC: $M_C = \left(\frac{2EI}{L}\right) \theta_D$

Moment in the direction of θ_D caused by θ_D :

• In Element DC: $M_D = \left(\frac{4EI}{L}\right)\theta_D$

Moment in the direction of θ_F caused by θ_D is equal to zero ($M_F=0$) as there is no rotation (C is locked). Apply θ_F positively only and get forces at each DOF.

Moment in the direction of θ_C caused by θ_F :

• In Element DC: $M_C = \left(\frac{2EI}{L}\right)\theta_F$

Moment in the direction of θ_D caused by θ_F is equal to zero $(M_D=0)$ as there is no rotation (C is locked). Moment in the direction of θ_F caused by θ_F :

• In Element DC: $M_F = \left(\frac{4EI}{L}\right)\theta_F$

Step 7: Add nodal forces

Total moment in the direction of θ_C :

$$M_C = \frac{8EI + 2GJ}{L}\theta_C + \left(\frac{2EI}{L}\right)\theta_D + \left(\frac{2EI}{L}\right)\theta_F \tag{4}$$

Total moment in the direction of θ_D :

$$M_D = \left(\frac{2EI}{L}\right)\theta_C + \left(\frac{4EI}{L}\right)\theta_D + 0 \tag{5}$$

Total moment in the direction of θ_F :

$$M_F = \left(\frac{2EI}{L}\right)\theta_C + 0\left(\frac{4EI}{L}\right)\theta_F \tag{6}$$

Given:

$$\frac{EI}{L} = \frac{(200 \times 10^3)(37.5 \times 10^{-6})}{(5)} \times 10^{-3} = 1.5 \times 10^3 \text{ kNm}$$
 (7)

$$\frac{GJ}{L} = \frac{(80 \times 10^3) (75 \times 10^{-6})}{(5)} \times 10^{-3} = 1.2 \times 10^3 \text{ kNm}$$
 (8)

The resulting structural stiffness matrix becomes:

$$K = 10^3 \begin{bmatrix} 14.4 & 3 & 3 \\ 3 & 6 & 0 \\ 3 & 0 & 6 \end{bmatrix} \tag{9}$$

Notice, it is symmetrical, giving confidence we have done it correctly.

Step 8: Solve, using Rule of Sarrus and Cramer's Rule to find:

$$\begin{cases}
\theta_C \\
\theta_D \\
\theta_F
\end{cases} = 10^{-3} \begin{bmatrix} 14.4 & 3 & 3 \\ 3 & 6 & 0 \\ 3 & 0 & 6 \end{bmatrix}^{-1} \begin{cases} -80 \\ 0 \\ 0 \end{cases}$$

$$= \frac{10^{-3}}{410} \begin{bmatrix} 36 & -18 & -18 \\ -18 & 77.4 & 9 \\ -18 & 9 & 77.4 \end{bmatrix} \begin{cases} -80 \\ 0 \\ 0 \end{cases}$$

from which:

Step 9: Member forces:

Using the special matrix since there is no vertical force and no vertical displacement for this special case. For Member *CD*:

$$\begin{pmatrix} T_C \\ M_C \\ T_D \\ M_D \end{pmatrix} = 10^3 \begin{bmatrix} 1.2 & 0 & -1.2 & 0 \\ 0 & 6 & 0 & 3 \\ -1.2 & 0 & 1.2 & 0 \\ 0 & 3 & 0 & 6 \end{bmatrix} \begin{pmatrix} 0 \\ -7.018 \\ 0 \\ 3.509 \end{pmatrix} = \begin{pmatrix} 0 \\ -31.579 \\ 0 \\ 0 \end{pmatrix} \text{ [kNm]}$$

For Member CF we consider not using the lower number node as the i node to illustrate the coordinate transform that must be considered. In this case, since the local z-axis and gloabl Y-axis are parallel, positive θ become positive major axis bending in the member's local coordinate system:

For Member *CE*:

And finally, for Member CG, we again break convention and carefully consider the directions of the global displacements as they relate to the local member coordinate system.

$$\begin{cases}
T_G \\
M_G \\
T_C \\
M_C
\end{cases} = 10^3 \begin{bmatrix}
1.2 & 0 & -1.2 & 0 \\
0 & 6 & 0 & 3 \\
-1.2 & 0 & 1.2 & 0 \\
0 & 3 & 0 & 6
\end{bmatrix} \begin{cases}
0 \\
0 \\
-7.018 \\
0
\end{cases} = \begin{cases}
8.421 \\
0 \\
-8.421 \\
0
\end{cases} [kNm]$$

Step 10 is to draw the internal actions diagrams. To do this, the results of the member actions which were derived in the local member coordinate system must now be considered now in the global coordinate system. The easiest way to do this is to draw the directions by carefully interpreting the member force signs against the global axis system. The resulting FBD is shown in Figure 1.

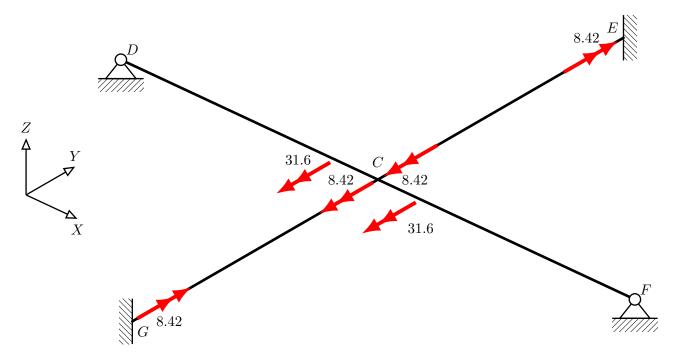


Figure 1: Free body diagram.

Considering the BMD, for each member, to identify the side in tension it can help to visualise the deformation resulting from the forces acting on it indicated in the free body diagram, Figure 1. Since there are no loads acting between the nodes, the BMD is comprised of straight lines between the values at each node. The BMD is shown in Figure 2.

For the TMD, it is not necessary to adopt a strict drawing convention once the relative actions are indicated. For example, the double-headed arrow in Figure 1 indicating the torsion of member CE could be thought

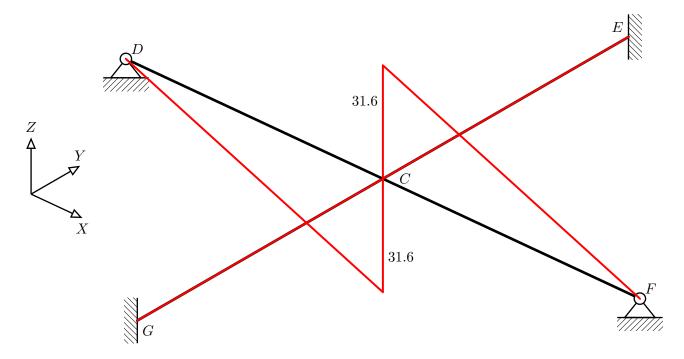


Figure 2: Bending Moment Diagram.

of as an analogous "tension" which we may consider as positive, and so we draw the TMD above the line. Similarly, fr member CG, the double-headed arrows act in the opposite sense to the analogous "tension" and so are analogous to "compression", which we then draw on the bottom of the member, as shown in Figure 3.

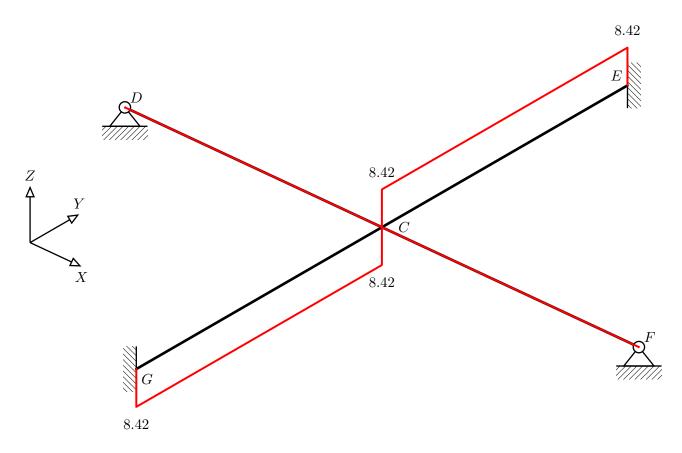


Figure 3: Torsion Moment Diagram.