CAAP Statistics - Lec07 R Session3

Jul 15, 2022

Review

- Normal Distribution
 - Standard Normal Distribution and Z-score
 - How to get normal probabilities?
 - How to get normal percentile?
- Bernoulli distribution
- Binomial distribution

Learning Objectives

- Binomial distribution(continued)
- Calculate the normal probabilities in R
- Calculate the normal percentile in R
- Simulate Bernoulli random variable
- Normal approximation of binomial distribution

Normal Probabilities and Percentiles

Load packages

```
library(openintro)
library(tidyverse)
library(ggplot2)
```

Load the data

Body girth measurements and skeletal diameter measurements, as well as age, weight, height and gender, are given for 507 physically active individuals - 247 men and 260 women.

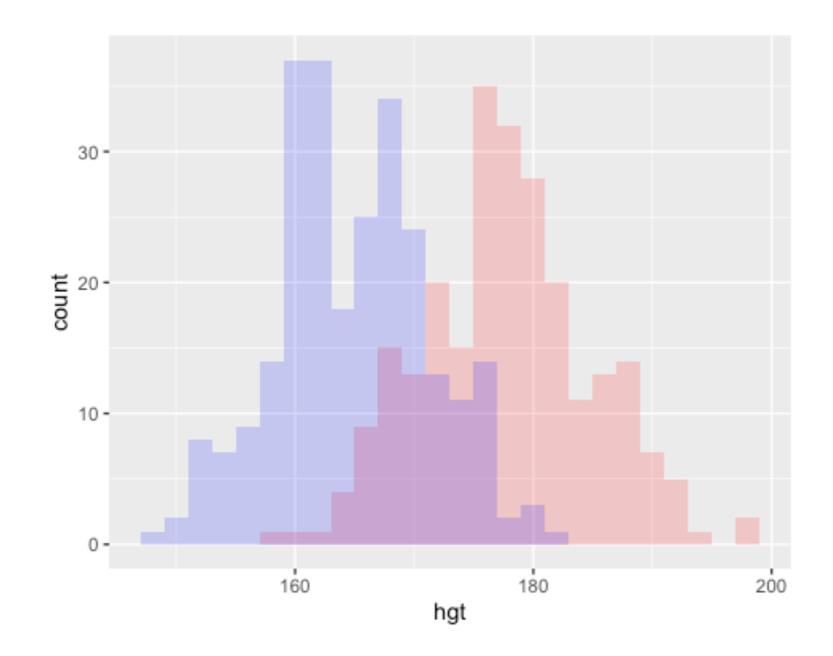
```
head(bdims)
## # A tibble: 6 × 25
    bia_di bii_di bit_di che_de che_di elb_di wri_di kne_di ank_di sho_gi che_gi
##
##
    <dbl>
                     17.7
## 1
    42.9
         26 31.5
                            28
                                  13.1
                                       10.4
                                             18.8 14.1
                                                         106.
                                                              89.5
## 2
    43.7 28.5 33.5
                     16.9
                           30.8
                                       11.8
                                             20.6 15.1
                                                        110.
                                  14
                                                             97
    40.1 28.2 33.3
                     20.9 31.7
## 3
                                 13.9
                                       10.9
                                             19.7 14.1
                                                        115. 97.5
    44.3 29.9 34 18.4 28.2
## 4
                                 13.9
                                       11.2
                                             20.9 15
                                                        104.
                                                             97
## 5
         29.9
               34 21.5 29.4
                                 15.2
    42.5
                                       11.6
                                             20.7 14.9
                                                        108.
                                                             97.5
## 6
     43.3
                 31.5
                      19.6
                            31.3
                                       11.5
                                             18.8
                                                   13.9
                                                         120.
                                                              99.9
           27
                                  14
## # ... with 14 more variables: wai gi <dbl>, nav gi <dbl>, hip gi <dbl>,
## #
     thi gi <dbl>, bic gi <dbl>, for gi <dbl>, kne gi <dbl>, cal gi <dbl>,
## #
     ank gi <dbl>, wri gi <dbl>, age <int>, wgt <dbl>, hgt <dbl>, sex <int>
```

Filter out the data

```
male = bdims %>%
  filter(sex == 1) # Male
female = bdims %>%
  filter(sex ==0) # Female
```

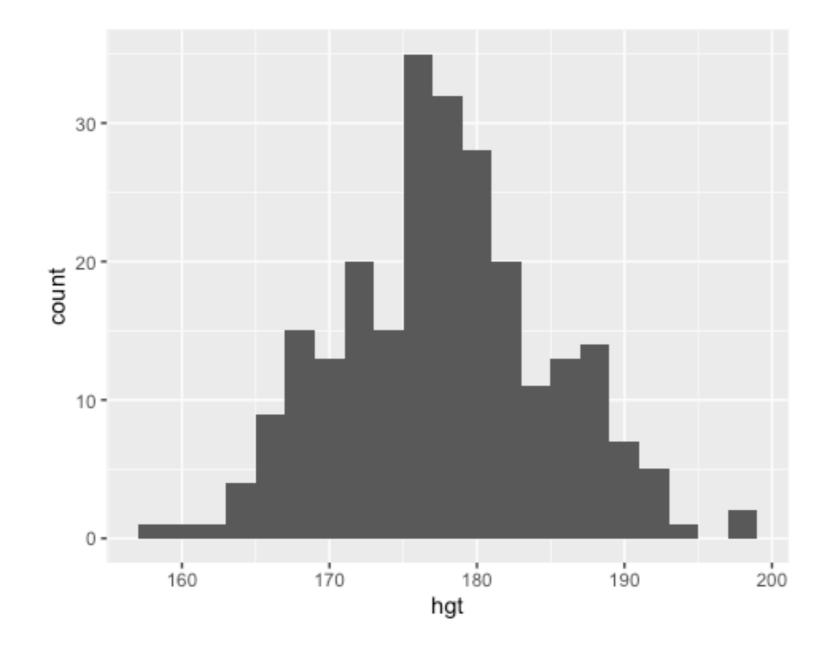
Visualize the distribution of hgt

```
ggplot(bdims,aes(x=hgt)) +
    geom_histogram(data=subset(bdims,sex == 1),fill = "red", alpha = 0.2, binwidth = 2) +
    geom_histogram(data=subset(bdims,sex == 0),fill = "blue", alpha = 0.2, binwidth = 2)
```



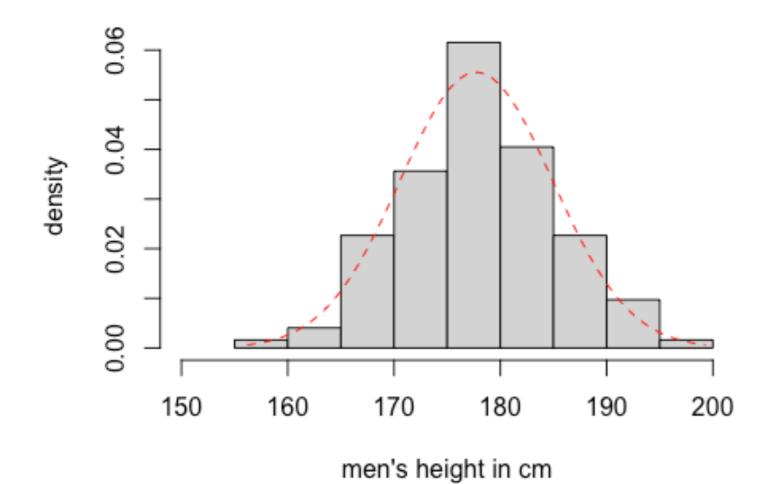
Let's focus on male data

```
ggplot(male, aes(x = hgt))+
  geom_histogram(binwidth = 2)
```



Normal Distribution

Histogram of Male Height



Normal Probabilities

What is the probabilities of the male height being less than 175 cm?

```
(zscore = (175-mu)/sigma)
## [1] -0.3821668
pnorm(175, mean = mu, sd = sigma)
## [1] 0.3511688
pnorm(zscore)
## [1] 0.3511688
```

Normal Probabilities

What is the probabilities of the male height being taller than 185 cm?

```
(zscore = (185-mu)/sigma)
## [1] 1.009887
1-pnorm(185, mean = mu, sd = sigma)
## [1] 0.1562746
1-pnorm(zscore)
## [1] 0.1562746
```

Normal Percentile

The n-th percentile is defined as the value where n percent of the data are below its value. What is the 97% percentile of this distribution?

```
qnorm(0.97, mean = mu, sd = sigma)
## [1] 191.2563
qnorm(0.97)*sigma + mu
## [1] 191.2563
quantile(male$hgt, 0.97)
## 97%
## 191.43
```

Bernoulli Trial

Recall the Milgram experiment.

```
p = 0.35 #probability of success
outcome = c(1,0) # success or failure
sample(outcome, size = 1, prob = c(p, 1-p))
## [1] 0
nexp = 1000
set.seed(1004)
result ber = matrix(0, nrow = nexp, ncol = 1)
for (i in 1:nexp){
  result ber[i,] = sample(outcome, size = 1, prob = c(p,1-p))
}
table(result ber)
## result ber
## 0 1
## 675 325
```

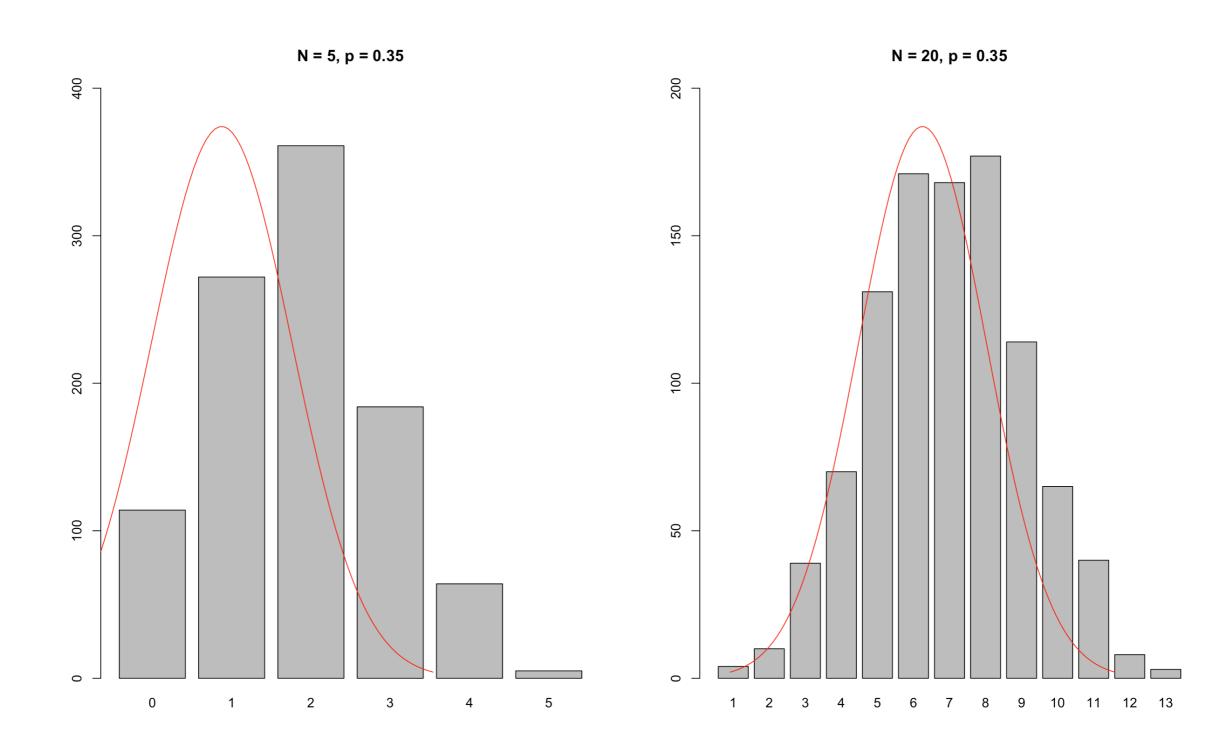
Binomial Trial - Normal Approximation

```
n_small = 5
n_large = 20
set.seed(1004)
result_bin_sm = matrix(0, nrow = nexp, ncol = n_small)
result_bin_lg = matrix(0, nrow = nexp, ncol = n_large)
for (i in 1:nexp){
   result_bin_sm[i,] = sample(outcome, size = n_small, prob = c(p,1-p), replace = TRUE)
   result_bin_lg[i,] = sample(outcome, size = n_large, prob = c(p,1-p), replace = TRUE)
}
```

Binomial - Normal Approximation(Code)

```
bin_dist_sm = table(rowSums(result_bin_sm))
bin_dist_large = table(rowSums(result_bin_lg))
par(mfrow=c(1,2))
barplot(bin_dist_sm, main = "N = 5, p = 0.35", ylim = c(0,400))
lines(x*sqrt(5*0.35*0.65)+5*0.35,
dnorm(x*sqrt(5*0.35*0.65)+5*0.35, 5*0.35,
sqrt(5*0.35*0.65))*nexp,col="red")
barplot(bin_dist_large, main = "N = 20, p = 0.35", ylim = c(0,200))
lines(x*sqrt(20*0.35*0.65)+20*0.35,
dnorm(x*sqrt(20*0.35*0.65)+20*0.35,
sqrt(20*0.35*0.65))*nexp,col="red")
```

Binomial - Normal Approximation(Plot)



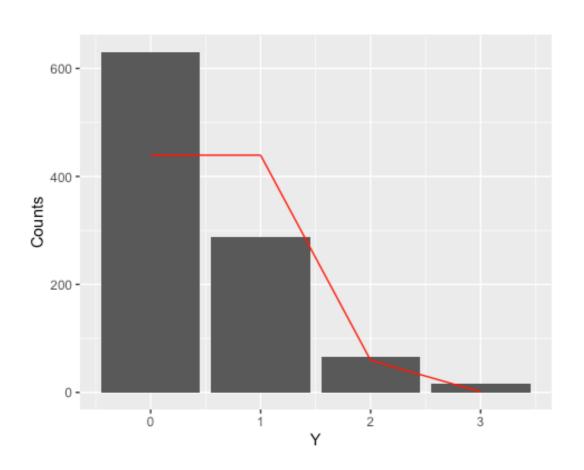
Poisson - Normal Approximation(Code)

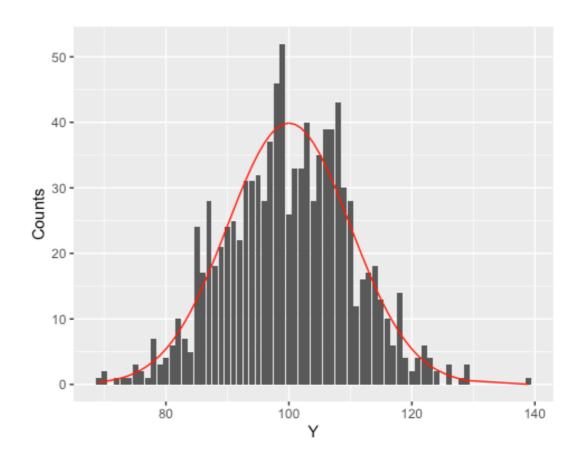
```
lambda_small = 0.5
lambda_large = 100
set.seed(1004)
result_poi_sm = data.frame(Y = rpois(nexp, lambda_small))
result_poi_lg = data.frame(Y = rpois(nexp, lambda_large))

result_poi_sm %>%
    ggplot()+
    geom_bar(aes(x=Y))+
    geom_line(aes(x = Y, dnorm(Y, mean = lambda_small, sd = sqrt(lambda_small))*nexp), color="red")+
    ylab("Counts")

result_poi_lg %>%
    ggplot()+
    geom_bar(aes(x=Y))+
    geom_bar(aes(x=Y))+
    geom_line(aes(x = Y, dnorm(Y, mean = lambda_large, sd = sqrt(lambda_large))*nexp), color="red")+
    ylab("Counts")
```

Poisson - Normal Approximation(Plot)





First Quiz on Thursday

Quiz

- OpenIntro Chapter 1-4
- Lecture 1-9
- Code from R sessions will be on the exam.
 You need to know the meaning of each code
 - eg: what does sample(1:6, size
 =2) do?
- Office hour from <u>7pm</u> via Zoom.