Determining the domain in \mathbb{R}^2

$$f(x,y) = 5xy + 3y$$

2.
$$f(x,y) = \sqrt{9 - x^2 - y^2}$$

3.
$$f(x,y) = \sqrt{x^2/4 + y^2/25 - 1}$$

4.
$$f(x,y) = \ln(-x^2 + 4 - y)$$

5.
$$f(x,y) = \frac{\sqrt{25 - x^2 - y^2}}{xy}$$

6.
$$f(x,y) = \frac{1}{\ln(x+y-5)}$$

Solution

1.

$$D(f) = \mathbb{R}$$

2.

$$9 - x^2 - y^2 \ge 0$$
$$9 \ge x^2 + y^2$$

$$D(f) = \{(x, y) \in \mathbb{R}^2 \mid 9 \ge x^2 + y^2\}$$

3.

$$x^{2}/4 + y^{2}/25 - 1 \ge 0$$

$$x^{2}/4 + y^{2}/25 \ge 1$$

$$D(f) = \{(x, y) \in \mathbb{R}^{2} \mid x^{2}/4 + y^{2}/25 \ge 1\}$$

4.

$$-x^2 + 4 - y > 0$$

$$4 > y + x^2$$

$$D(f) = \{(x, y) \in \mathbb{R}^2 \mid 4 > y + x^2\}$$

5.

$$x \neq 0$$
$$y \neq 0$$
$$25 - x^2 - y^2 \ge 0$$

$$25 \ge x^2 + y^2$$

$$D(f) = \{(x,y) \in \mathbb{R}^2 \mid (25 \ge x^2 + y^2) \land (x \ne 0 \land \ne 0)\}$$

6.

$$x + y - 5 > 0$$
$$x + y > 5$$

$$x + y - 5 \neq 1$$

$$D(f) = \{(x,y) \in \mathbb{R}^2 \mid (x+y > 5) \land (x+y-5 \neq 1)\}$$