

2. In each circuit in Fig. 1, either the value of v or i is not known

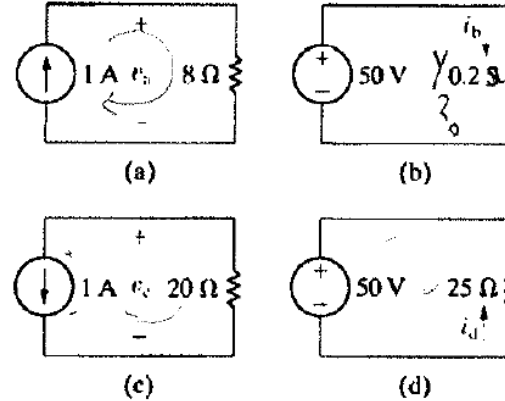


Figure 1

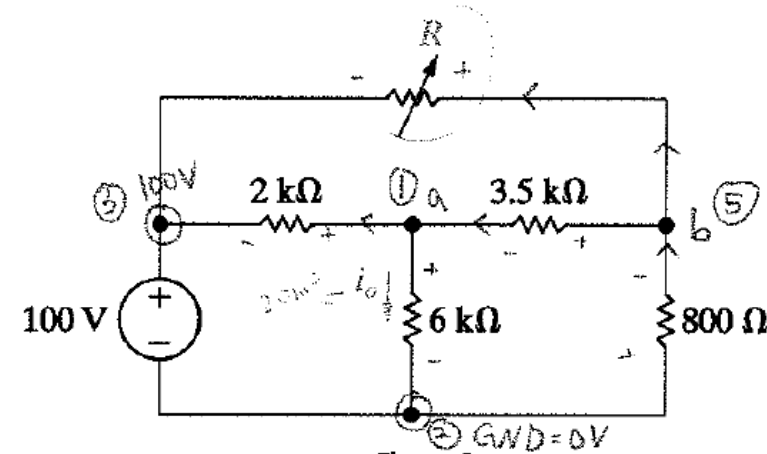
a) Calculate the values of v_a , i_b , v_c , and i_d . Units are important for all questions.

<p>0.5</p> <p>Answer:</p>	$V_a = 1 \times 8 = 8V$ $I_b = \frac{50}{0.2} = 10A$ $V_c = -1 \times 20 = -20V$ $I_d = \frac{-50}{25} = -2A$
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b) Determine the power dissipated in each resistor. $P = \frac{V^2}{R}$ or $P = I^2 R$

<p>0.5</p> <p>Answer:</p>	$(a) V_a \times I = 8 \times 1 = 8W$ $(b) 50 \times \frac{50}{10} = 500W$ $(c) -1 \times -20 = 20W$ $(d) -2 \times -50 = 100W$
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7. The variable resistor R in the circuit in Fig. 6 is adjusted until i_0 equals 20 mA Find the value of R .



④ Set polarity

Figure 6

Answer:

$$\textcircled{4} \bar{i}_0 = 20\text{mA} = \frac{(a-0)}{6\text{k}} \Rightarrow a = 120\text{V}$$

⑤

⑥ KCL at a

$$\frac{a-100}{2\text{k}} + \bar{i}_0 = \frac{b-a}{3.5\text{k}} \Rightarrow b = 225\text{V}$$

$$\textcircled{7} \text{KCL at } b \quad \frac{b-100}{R} + \frac{b-a}{3.5\text{k}} = \frac{0-225}{800}$$

$$R \approx -2401.92 \Omega$$

an active component

8. Find (a) i_o (b) i_1 , and (c) i_2 in the circuit in Fig.7

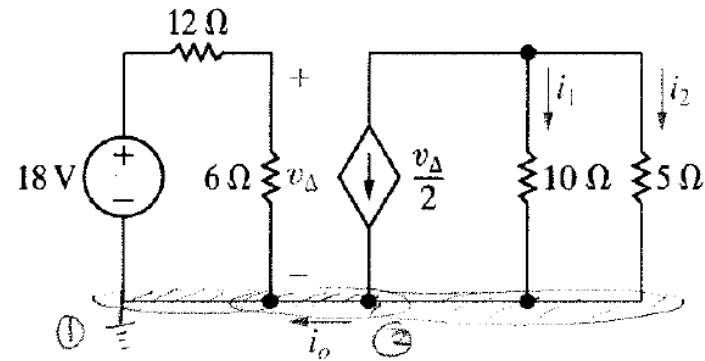


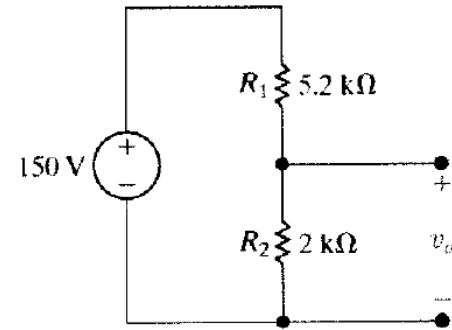
Figure 7

0.3
(a)
Answer $i_o = 0A$, \therefore no current can exist in a single node.

0.3
(b)
Answer

① $i_1 = \frac{18V}{(12+6)\Omega} = 1A$
 ② $V_\Delta = 18 \times \frac{6}{12+6} = 6V$
 ③ $\diamond \frac{V_\Delta}{2} = 3A$
 ⑥ KVL at X loop.
 $5i_2 = 10i_1$
 ⑦ KCL at ⑤ node
 $6 \cdot \frac{-2V_\Delta}{2} + i_1 + i_2 = 0 \therefore i_1 = -1A$
 $i_2 = -2A$

4. Refer to the following circuit to answer following questions



a) Calculate the output voltage v_o for the voltage divider circuit

0.4	$V_o = 150 \times \frac{2k}{(5.2+2)k} = 41.66V$
Answer:	

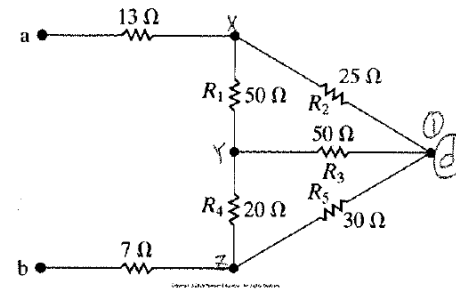
b) Calculate the net current flowing through the circuit

0.3	$\bar{I} = \frac{150V}{(5200+2000)} = 20.8mA = 0.0208A$
Answer:	

c) Calculate the total power of this circuit in the absence of R_1 , if the existing voltage source is replaced by a similar source of 100V.

0.3	$P = VI = \frac{V^2}{R} = \frac{(100)^2}{2000} = 5W$
Answer:	

5-6. Refer to the following circuit to answer following questions



5. Find the equivalent resistance R_{ab} in the circuit by using a Y-to-Δ transformation involving the resistors R_2 , R_3 , and R_5 .

②

[Note that R_1 , R_4 are not considered in this calculation]

③ $R_a = \frac{(25 \times 50 + 50 \times 20) + (20 \times 25)}{25} = 116.6 \Omega$

④ $R_b = \frac{350}{50} = 7 \Omega$

⑤ $R_c = \frac{2750}{25} = 110 \Omega$

Answer:

⑥

⑦ $R_1 \parallel R_4 = 50 \parallel 116.6$

⑧ $R_4 \parallel R_c = 20 \parallel 110$

⑨ $(11 + 8) \parallel R_b = 30 \Omega$

⑩ $R_{ab} = 13 + 30 + 7 = 50 \Omega$

6. Repeat (a) using a Δ-to-Y transformation involving resistors R_3 , R_4 , and R_5 .

① Find Δ

② $R_{xc} = \frac{50 \times 20}{50 + 20 + 30} = 10 \Omega$

$R_y = \frac{50 \times 30}{100} = 15 \Omega$

$R_z = \frac{20 \times 30}{100} = 6 \Omega$

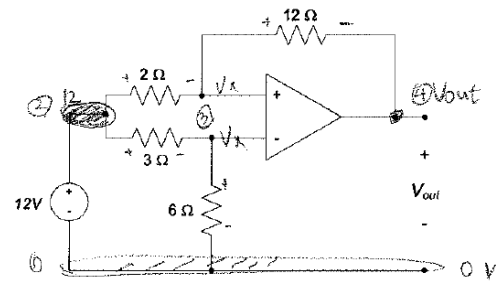
Answer:

③

④ $60 \parallel 40 = 24 \Omega$

⑤ $R_{ab} = 13 + 24 + 6 + 7 = 50 \Omega$

1. For the circuit shown, find V_{out} .



⑤ KCL at $V^- \rightarrow 0$

$$\frac{12 - V_x}{3} = \frac{V_x}{6}$$

$$24 - 2V_x = V_x$$

$$3V_x = 24$$

$$V_x = 8V$$

⑥ KCL at V^+

$$\frac{12 - V_x}{2} = \frac{V_x - V_{out}}{12}$$

$$Z = \frac{8 - V_{out}}{12}$$

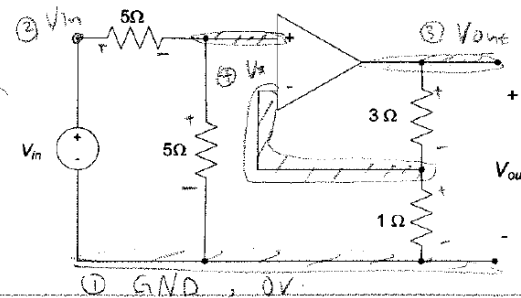
$$-V_{out} = 24 - 8$$

$$= 16$$

$$V_{out} = -16V$$

Answer:

2. For the circuit shown, find the relationship between V_{out} and V_{in} .



⑤ KCL at V^+

$$\frac{V_{in} - V_x}{5} = \frac{V_x}{5}$$

$$2V_x = V_{in}$$

$$V_x = \frac{1}{2} V_{in}$$

⑥ Voltage divider at V^-

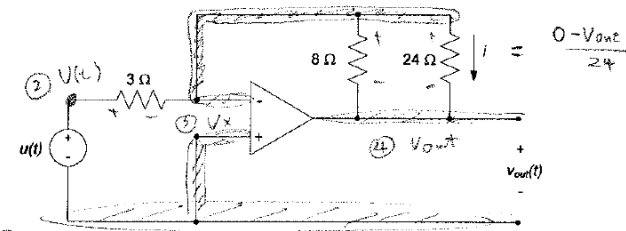
$$V_x = V_{out} \cdot \frac{1}{3+1}$$

Answer:

$$\frac{1}{4} V_{out} = \frac{1}{2} V_{in}$$

$$\textcircled{7} V_{out} = 2V_{in}$$

3. For the circuit below, determine:



a) The current i and voltage v_{out} if $u(t) = 4V$

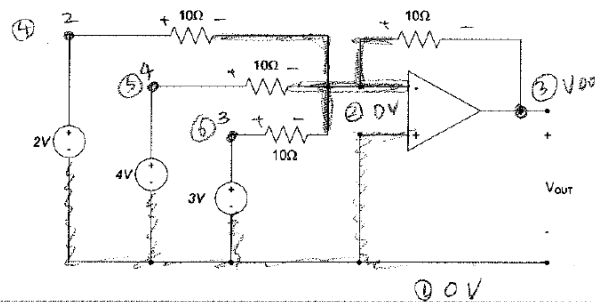
① $GND = 0V$

Answer:	<p>④ at $V^+ = 0V$ $\therefore V^- = 0 = V_x$</p> <p>⑤ KCL at $V^+ = 0$</p> <p>$\frac{u(t) - 0}{3} = \frac{0 - v_{out}}{8} + \frac{0 - v_{out}}{24}$</p> <p>$8u(t) = -3v_{out} - v_{out}$ $2u(t) = -v_{out}$ if $u(t) = 4V$ $v_{out} = -8V$ $i = \frac{-v_{out}}{24} = \frac{8}{24} = \frac{1}{3}A$</p>
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b) The current, i , and voltage v_{out} if $u(t) = 2\cos(5t)$

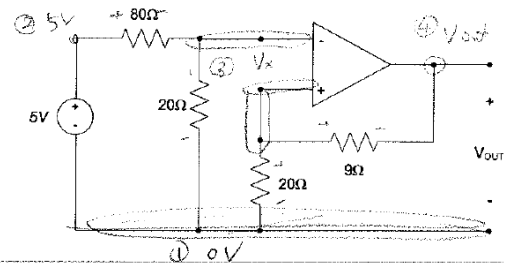
Answer:	<p>$v_{out} = -2u(t) = -4\cos(5t) [V]$ $i = \frac{-(-4\cos(5t))}{24} = \frac{1}{6}\cos(5t) [A]$</p>
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4. For the circuit shown, find V_{out} .



Answer:	<p>① KCL at V^-</p> <p>$\frac{2-0}{10} + \frac{4-0}{10} + \frac{3-0}{10} = \frac{0-v_{out}}{10}$</p> <p>$-v_{out} = 2+4+3 = 9$ $v_{out} = -9 [V]$</p>
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5. For the circuit shown, find V_{out} .



⑤ at V^-

$$\frac{5 - V_x}{80} = \frac{V_x}{20}$$

$$5 - V_x = 4V_x$$

$$5V_x = 5$$

$$V_x = 1$$

⑥ at V^+

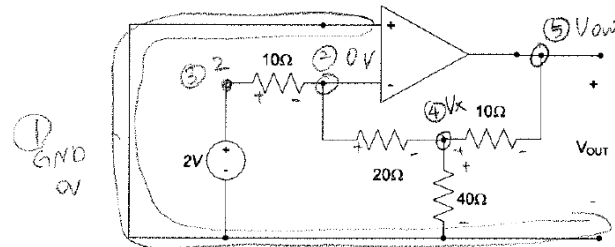
$$V_x = 1 = \frac{V_{out} \times 20}{20 + 9} = \frac{20}{29} V_{out}$$

$$V_{out} = \frac{29}{20} [V]$$

$$= 1.45 \text{ V}$$

Answer:

6. For the circuit shown, find V_{out} .



⑥ KCL at V^-

$$\frac{2 - 0}{10} = \frac{0 - V_x}{20}$$

$$4 = -V_x$$

$$V_x = -4 [V]$$

⑦ KCL at V_x



Answer:

$$\frac{0 - V_x}{20} = \frac{V_x - V_{out}}{10} + \frac{V_x}{40}$$

$$\frac{-(-4)}{20} = \frac{-4 - V_{out}}{10} + \frac{-4}{40}$$

$$\left(\frac{1}{5} = \frac{-4 - V_{out}}{10} + \frac{-1}{10} \right) 10$$

$$2 = -4 - V_{out} - 1$$

$$V_{out} = -4 - 1 - 2 = -7 [V]$$