



3D Reconstruction

Shanchen Jiang

Kazhdan M, Hoppe H. Screened poisson surface reconstruction[J]. ACM Transactions on Graphics (TOG), 2013, 32(3): 29.



Film Industry



3D Camera



Virtual display

Film Industry



Image Landsat / Copernicus

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City Planning

Google Earth

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Taking Photos



Recovery from images

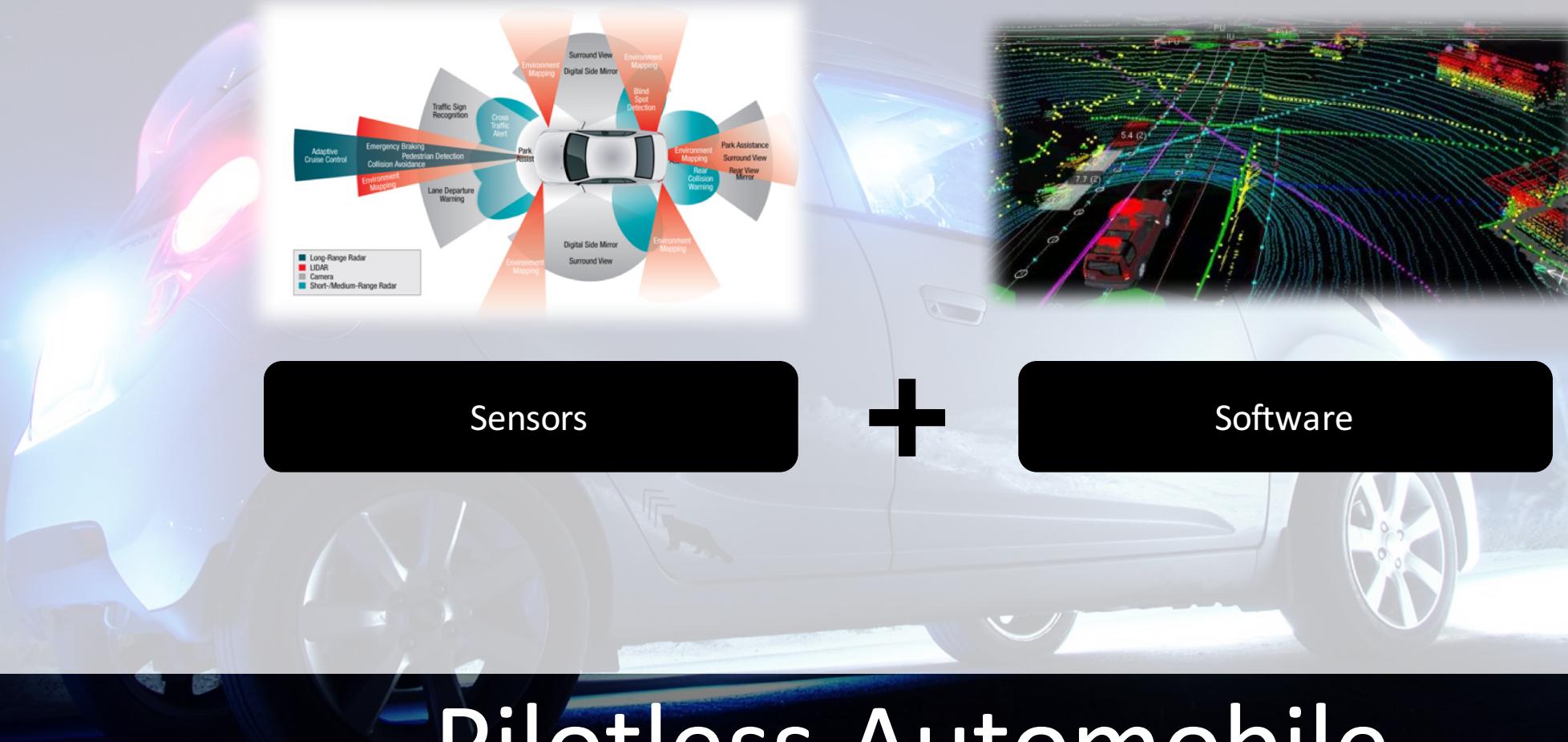
Image Landsat / Copernicus
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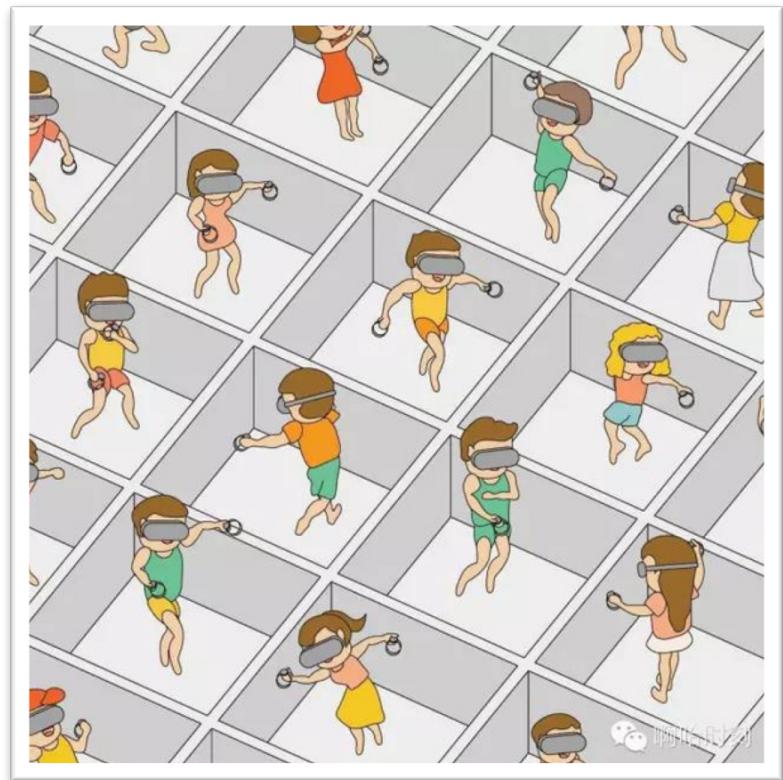
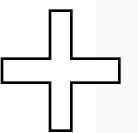
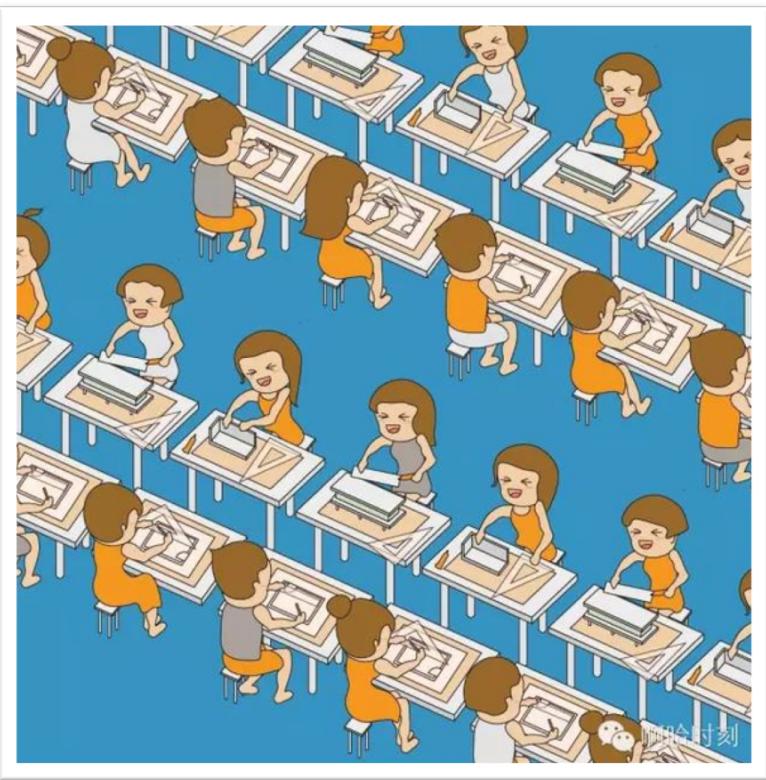
Pilotless Automobile



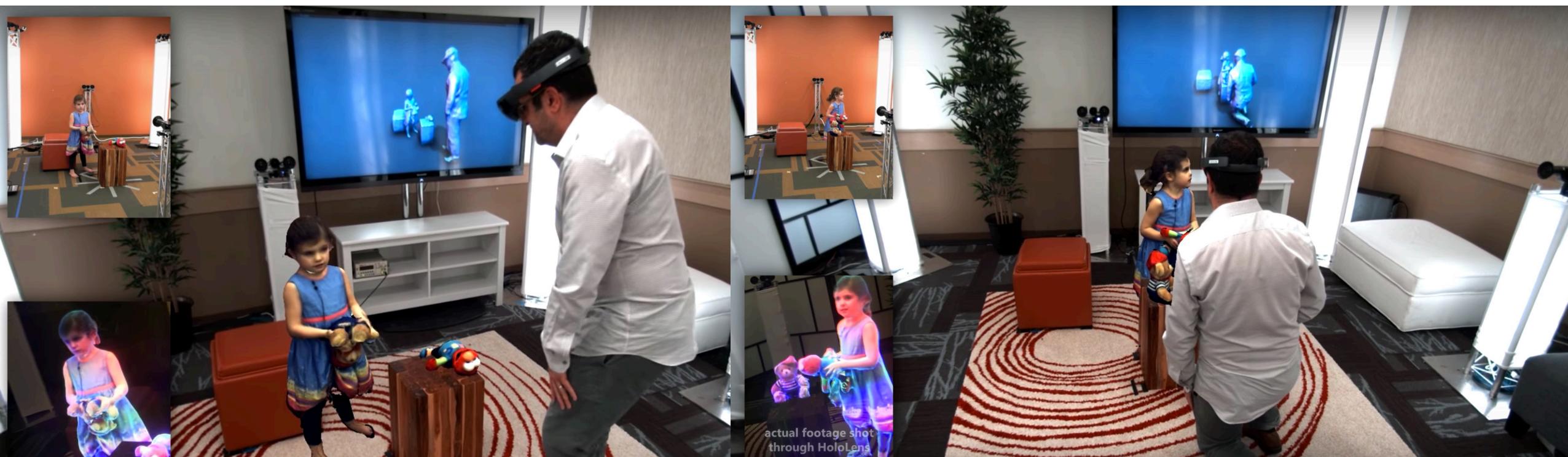
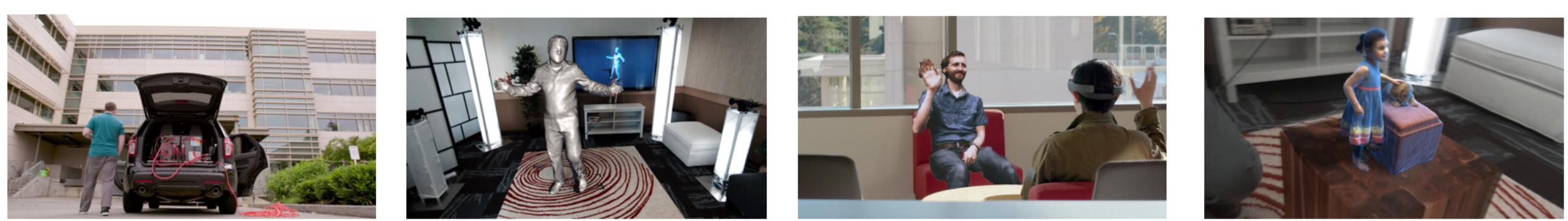


Everything is virtual

Virtual Reality



Virtual Reality



Augmented Reality

Classification

GBM

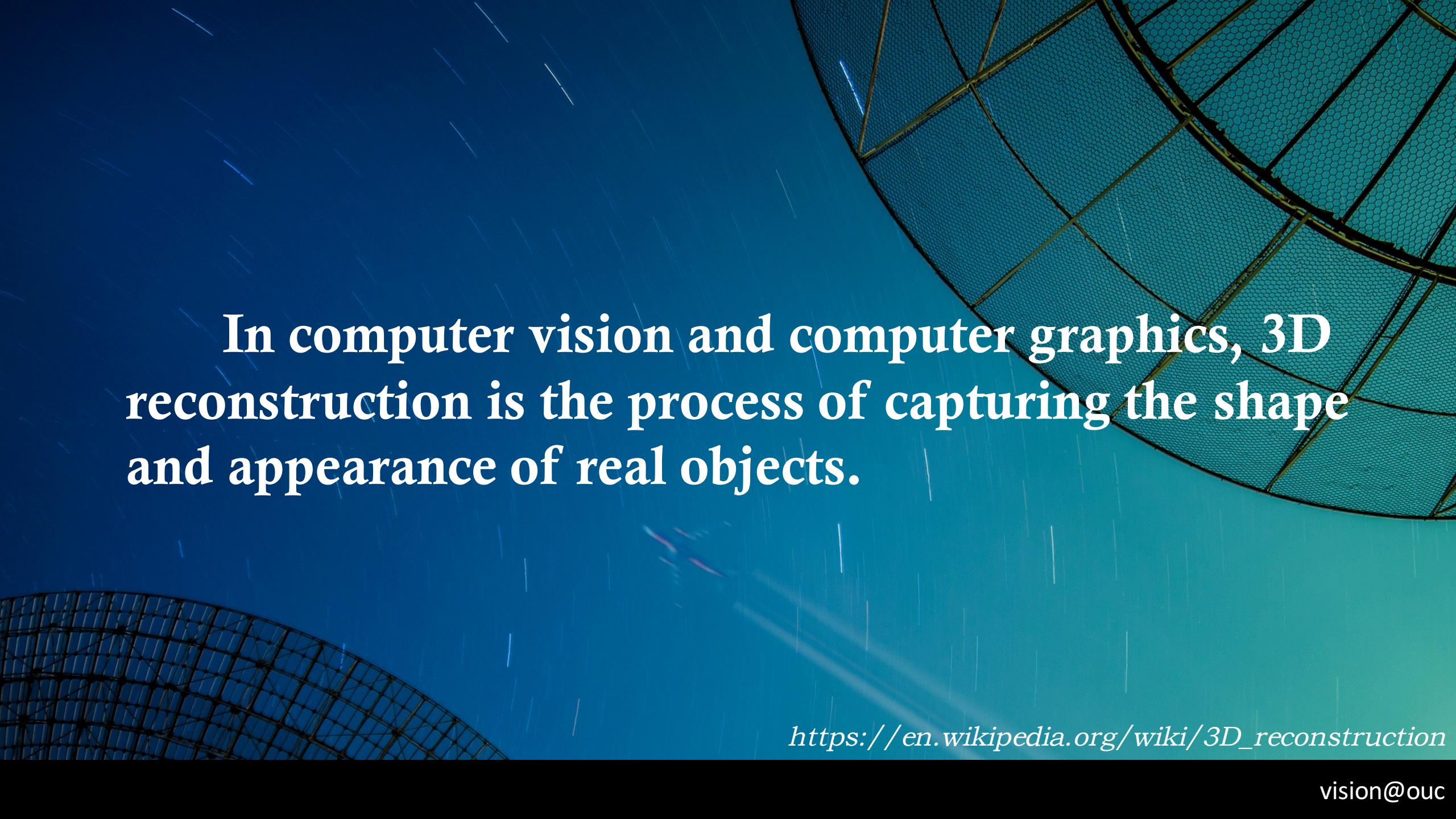
Geometry Based Modeling

DSM

Depth Scanning Modeling

IBM

Image Based Modeling



In computer vision and computer graphics, 3D reconstruction is the process of capturing the shape and appearance of real objects.

https://en.wikipedia.org/wiki/3D_reconstruction

History

1960s Problem Definition

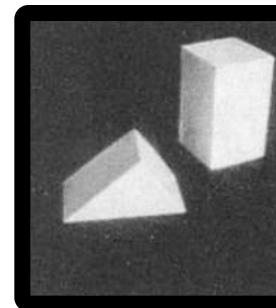
1970s Image Formulation

1980s

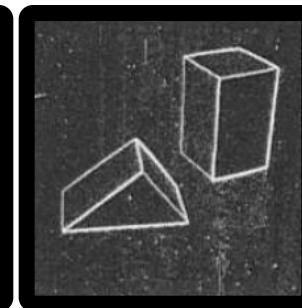
1990s Geometry

2000s Reconstruction

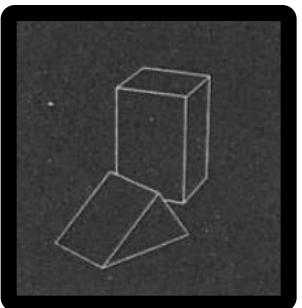
2010s Innovation



Input



Gradient



Output

Roberts L G. Machine perception of three-dimensional soups[D]. Massachusetts Institute of Technology, 1963.

History

- 1960s Problem Definition
- 1970s Image Formulation
- 1980s
- 1990s Geometry
- 2000s Reconstruction
- 2010s Innovation



- (1969) "A theory of cerebellar cortex." *J. Physiol.*, 202:437-470.
- (1970) "A theory for cerebral neocortex." *Proceedings of the Royal Society of London B*, 176:161-234.
- (1971) "Simple memory: a theory for archicortex." *Phil. Trans. Royal Soc. London*, 262:23-81.
- (1974) "The computation of lightness by the primate retina." *Vision Research*, 14:1377-1388.
- (1975) "Approaches to biological information processing." *Science*, 190:875-876.
- (1976) "Early processing of visual information." *Phil. Trans. R. Soc. Lond. B*, 275:483-524.
- (1976) "Cooperative computation of stereo disparity." *Science*, 194:283-287. (with Tomaso Poggio)
- (1976, March) "Artificial intelligence: a personal view." Technical Report AIM 355, MIT AI Laboratory, Cambridge, MA.
- (1977) "Artificial intelligence: A personal view." *Artificial Intelligence* 9(1), 37–48.
- (1977) ***Vision: A computational investigation into the human representation and processing of visual information (ISBN 0-7167-1567-8)***
Neurosciences Res. Prog. Bull., 15:470-488. (with Tomaso Poggio)
- (1978) "Representation and recognition of the spatial organisation of three-dimensional structure." *Proceedings of the Royal Society of London B*, 202:201-220. (with Nishihara)
- (1979) "A computational theory of human stereo vision." *Proceedings of the Royal Society of London B*, 204:301-328. (with Tomaso Poggio)
- (1980) "Theory of edge detection." *Proc. R. Soc. Lond. B*, 207:187-217. (with E. Hildreth)
- (1981) "Artificial intelligence: a personal view." In Haugeland, J., ed., *Mind Design*, chapter 4, pages 129-142. MIT Press, Cambridge, MA.
- (1982) "Representation and recognition of the movements of shapes." *Proceedings of the Royal Society of London B*, 214:501-524. (with L. M. Vaina)
- (1982). *Vision: A Computational Investigation into the Human Representation and Processing of Visual Information*. New York: Freeman.

D. Marr

3D Reconstruction

Gray
Edge

Symbol
Element

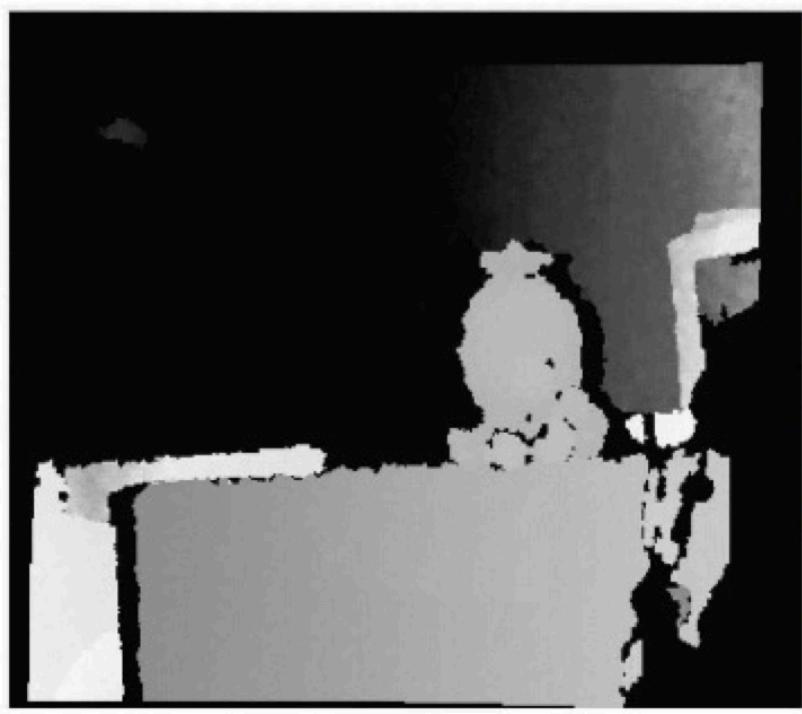
Comprehension

Primary

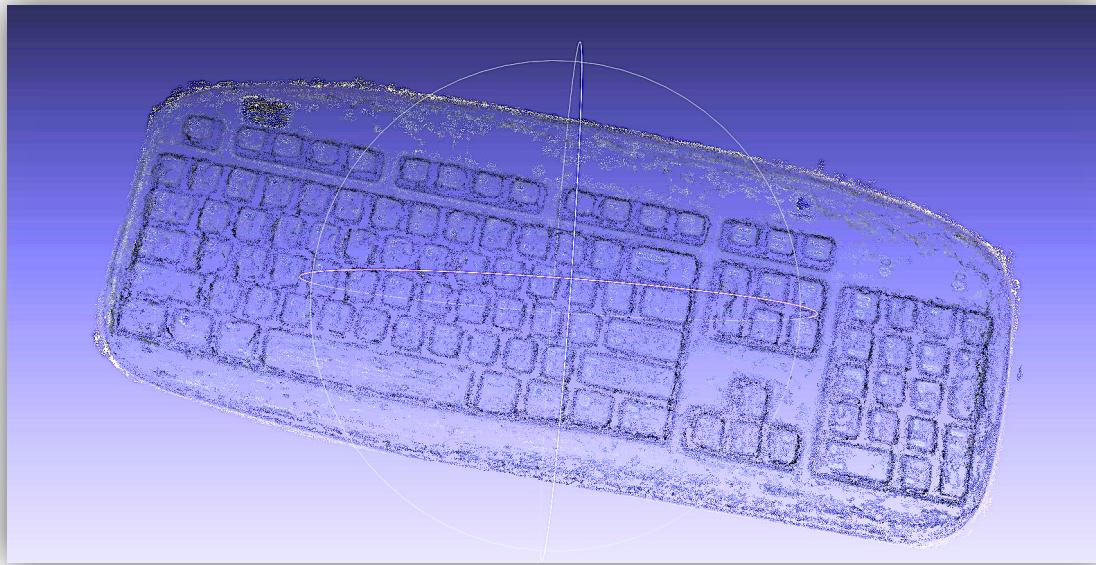
Middle

Advanced

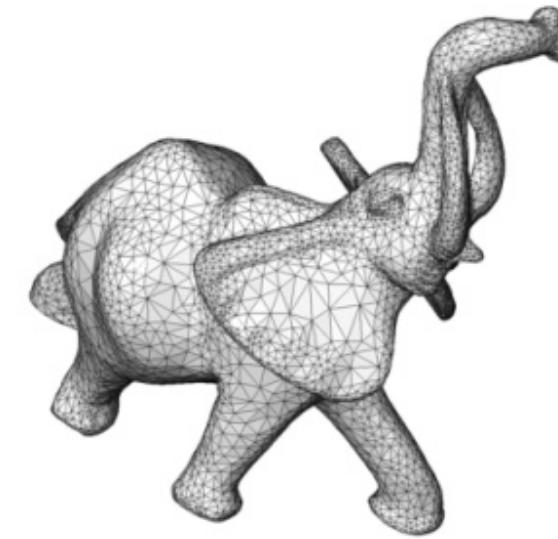
Image Date



2.5 D
information



Point cloud



Grid chart

History

1960s Problem Definition

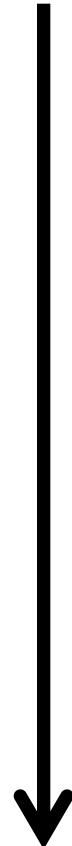
1970s Image Formulation

1980s

1990s **Geometry**

2000s Reconstruction

2010s Innovation



Essential Matrix: $X'_\mu Q_{\mu\nu} X_\nu = 0$

$$X'_\mu Q_{\mu\nu} X_\nu = 0 \quad (11)$$

Dividing equation (11) by $X'_3 X_3$ we arrive at the desired relationship between the image coordinates:

$$x'_\mu Q_{\mu\nu} x_\nu = 0 \quad (12)$$

Longuet-Higgins H C. A computer algorithm for reconstructing a scene from two projections[J].

Readings in Computer Vision: Issues, Problems, Principles, and Paradigms, MA Fischler and O. Firschein, eds, 1987: 61-62.

History

1960s Problem Definition

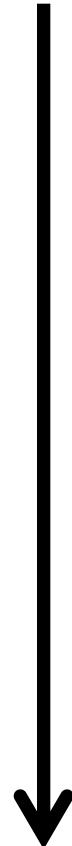
1970s Image Formulation

1980s

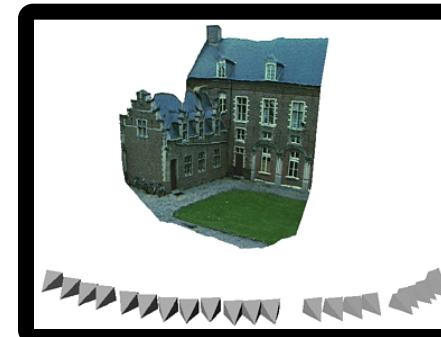
1990s Geometry

2000s **Reconstruction**

2010s Innovation



Structure from Motion



Pollefeys et al

Multi-view Stereo



Furukawa & Ponce

History

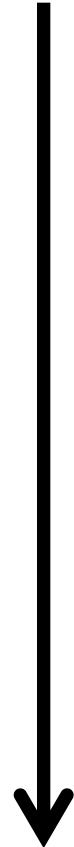
1960s Problem Definition
1970s Image Formulation
1980s
1990s Geometry
2000s Reconstruction
2010s Innovation



Big data
Real time
Deep learning

History

1960s	Problem Definition
1970s	Image Formulation
1980s	
1990s	Geometry
2000s	Reconstruction
2010s	Innovation



Goals of Computer Vision:

- Let machines see
- Let humans see better



basis of 3D reconstruction

DEPTH

Classification

Active methods

Structure light ...

Passive methods

Recover from shadow

Recover from stereoscopic

Structure from motion

Photometric three-dimensional ...

Active methods

Physical means

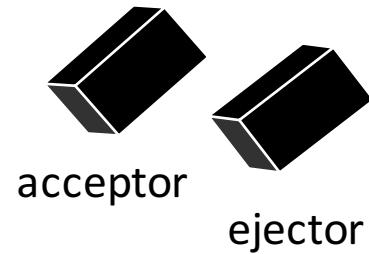
light

acoustic

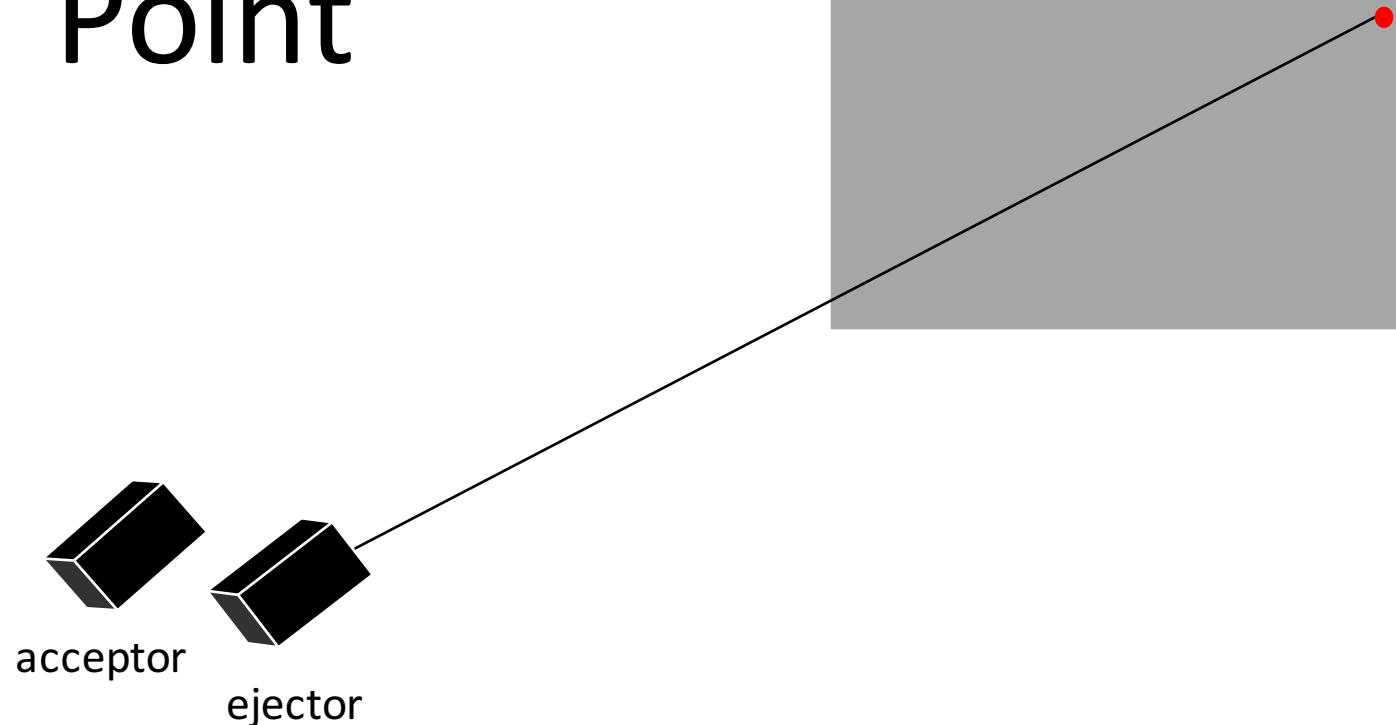
Active methods

Physical means

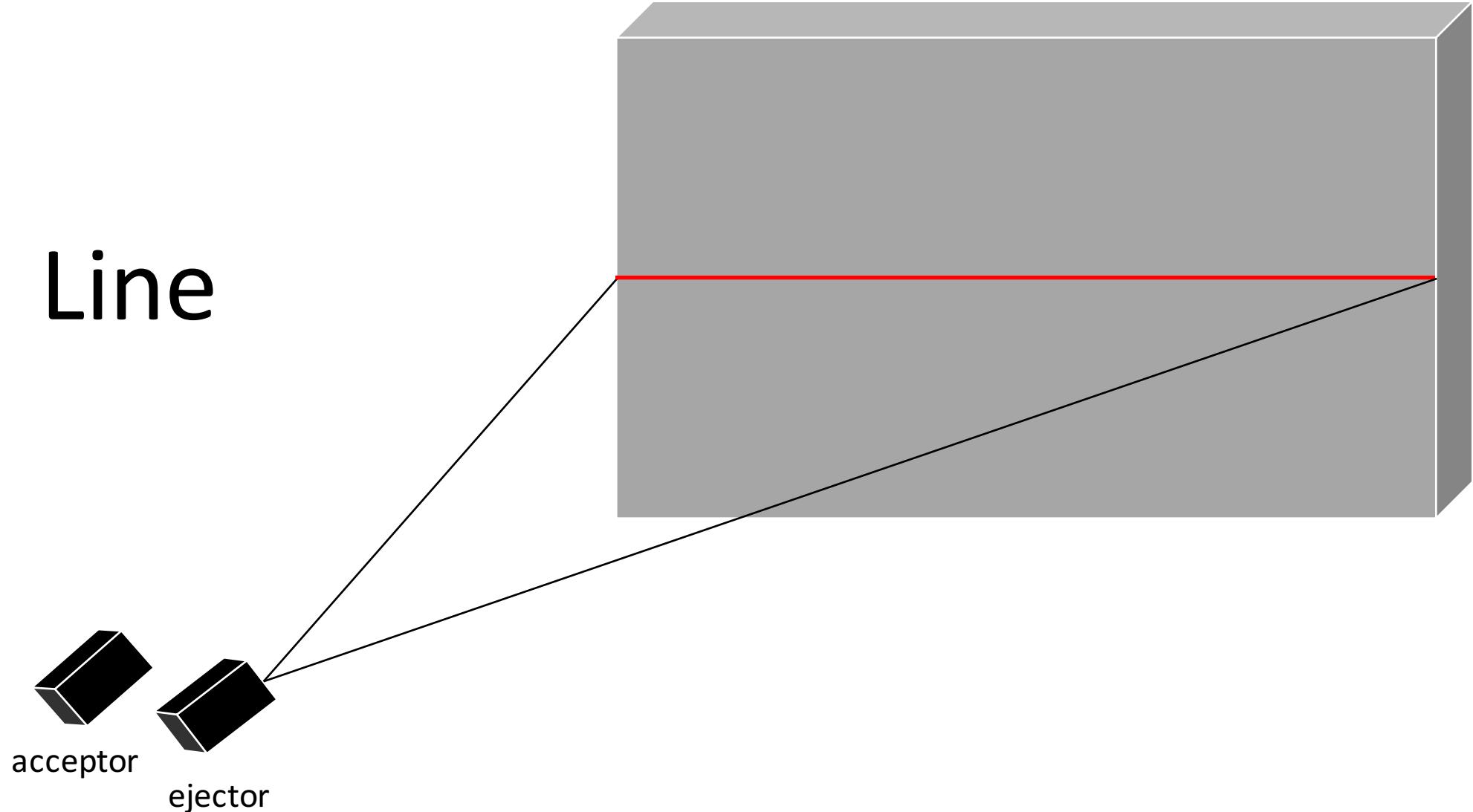
light



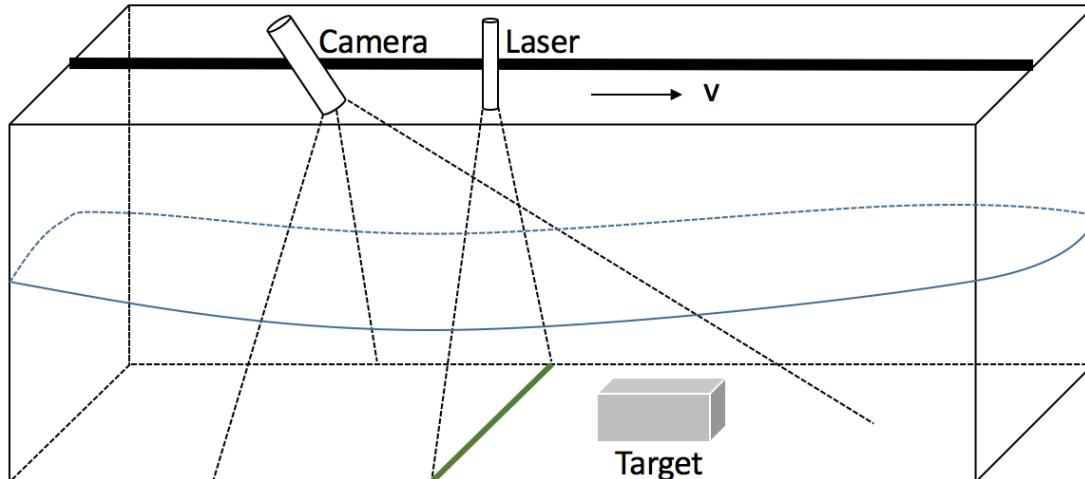
Point



Line



Laser Line Scanning



Calibration

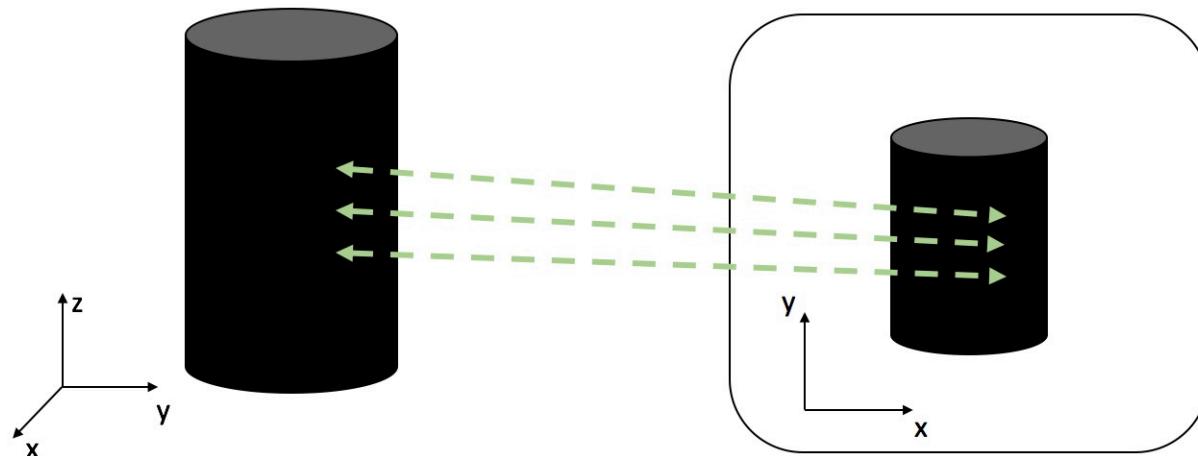
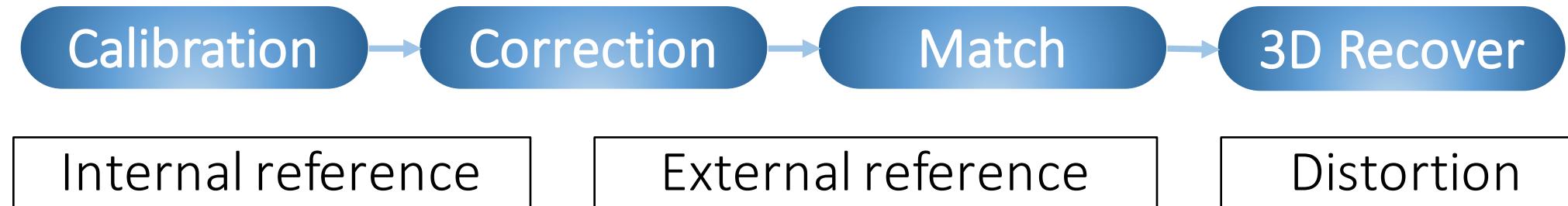
Acquisition

Extraction

Transformation

Modeling

Calibration

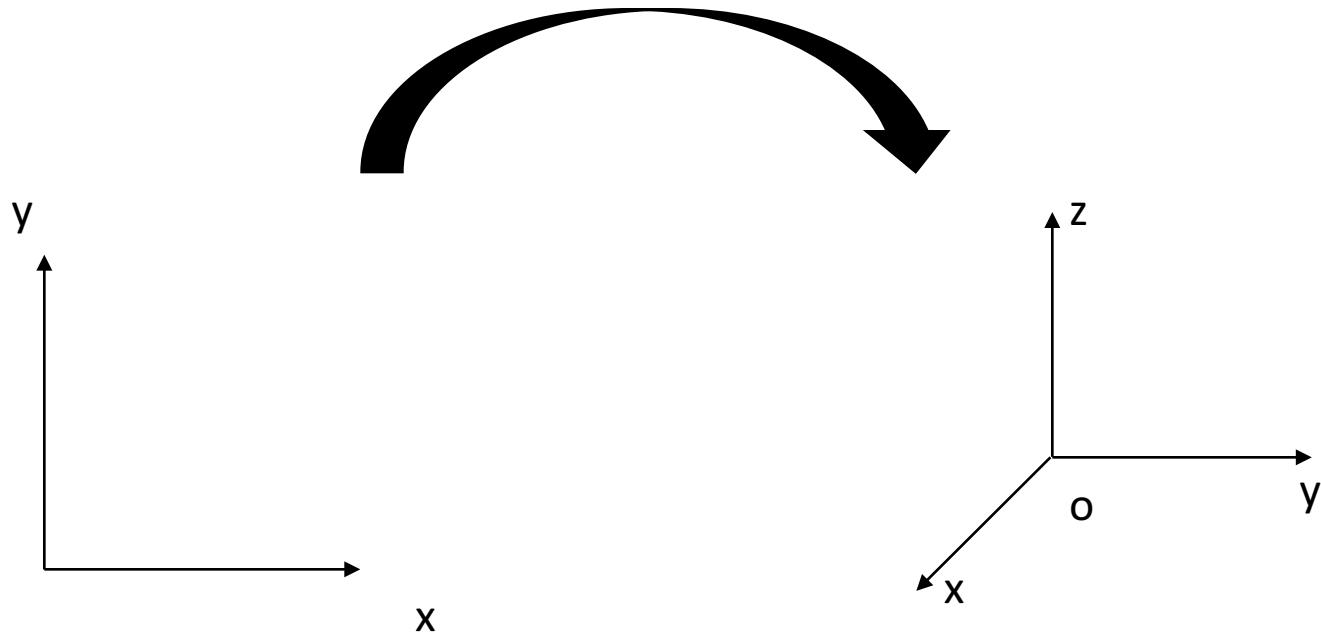


Calibration

$$s\tilde{x} = \textcolor{red}{K}[R \ t]\tilde{X} \quad (1)$$

$$\textcolor{red}{H} = [h_1 \ h_2 \ h_3] = \lambda K[r_1 \ r_2 \ t] \quad (2)$$

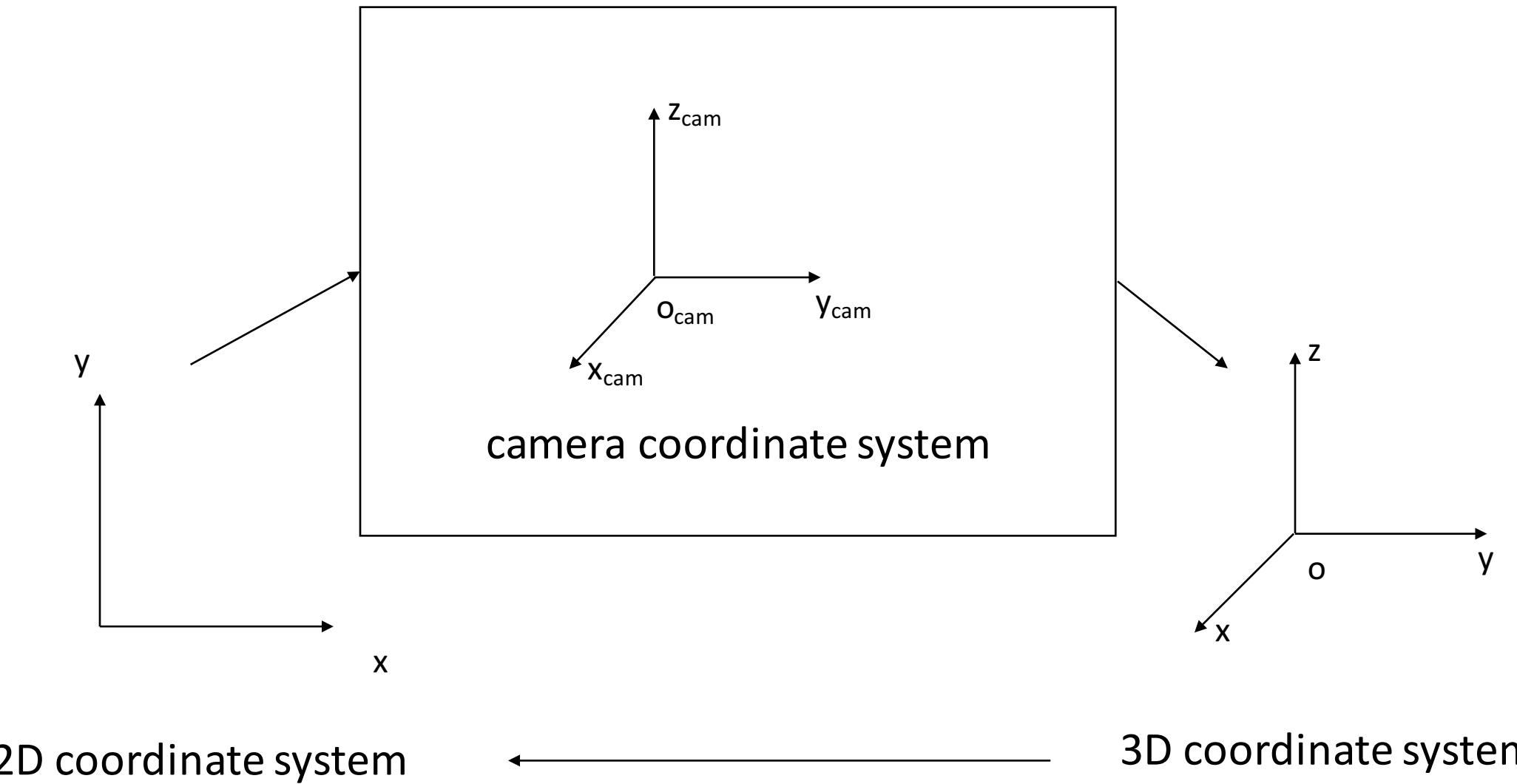
- [1]O. Faugeras. "Three-Dimensional Computer Vision: A Geometric Viewpoint ". MIT Press, 1993.
- [2]Hartley, Richard I. "An algorithm for self calibration from several views." *Cvpr*. Vol. 94. 1994.
- [3] Luong, Q-T. "Self-calibration of a moving camera from point correspondences and fundamental matrices." *International Journal of computer vision* 22.3 (1997): 261-289.



2D coordinate system

3D coordinate system

Jianxiong Xiao



calibration

I am a handsome boy



calibration

I am a 3D Point



calibration

I am a 3D Point

- $$\mathbf{X} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

calibration

I am cool

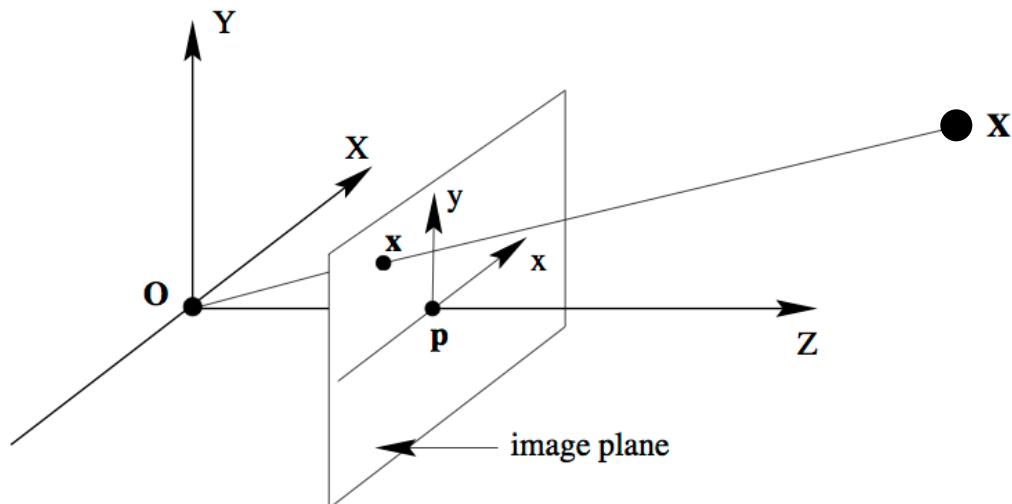
People loves to take picture of me.

$$\bullet \quad \mathbf{X} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

calibration

I am cool

People loves to take picture of me.



$$\mathbf{x} = \begin{bmatrix} x \\ y \end{bmatrix}$$

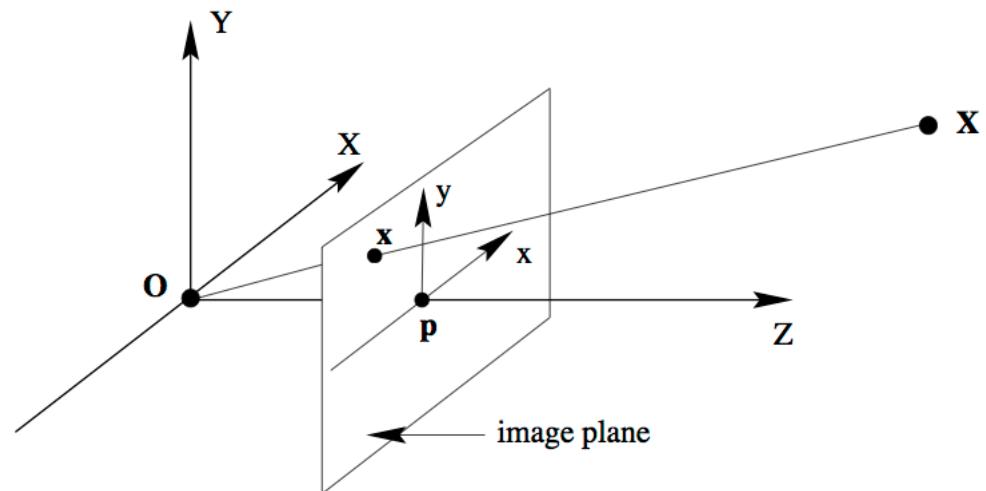
2D

$$\mathbf{X} = \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

3D

calibration

When they take a picture



$$\begin{bmatrix} x \\ y \\ f \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

2D

3D

$$\mathbf{x} = \mathbf{K}[\mathbf{R}|\mathbf{t}] \mathbf{X}$$

calibration

when they take a picture

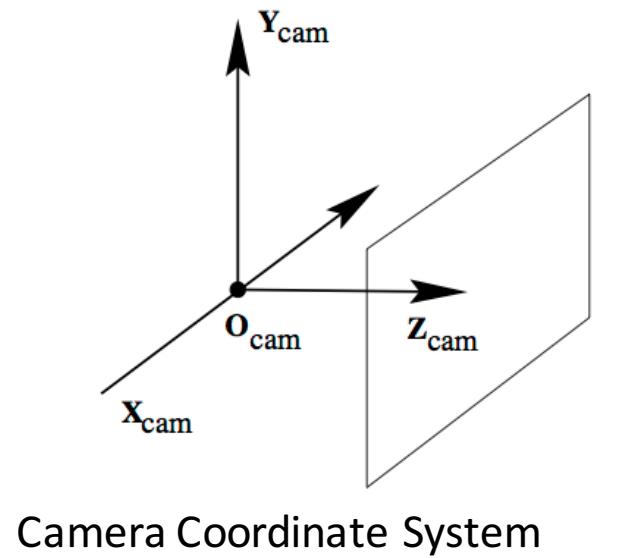
$$\begin{bmatrix} x \\ y \\ f \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} f & 0 & 0 \\ 0 & f & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

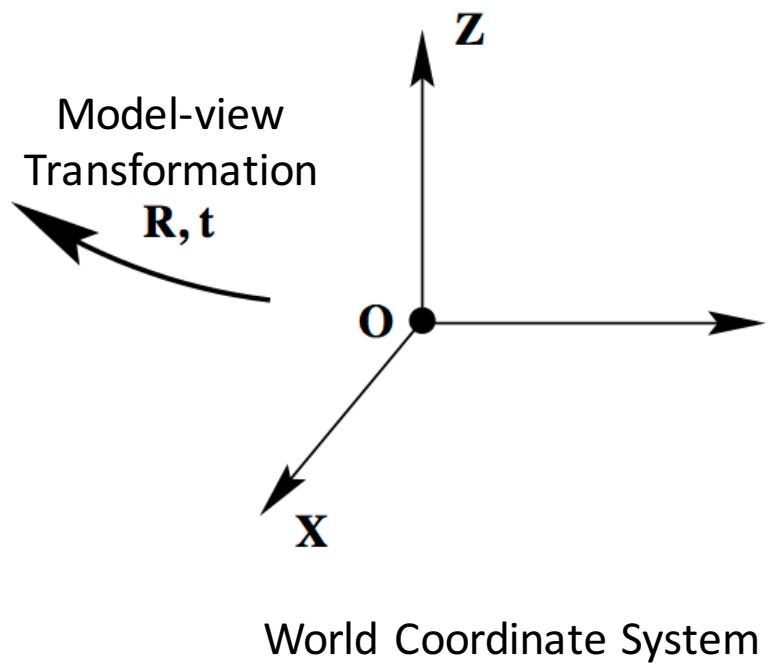
$$\mathbf{x} = \mathbf{K}[\mathbf{R}|\mathbf{t}] \mathbf{X}$$

calibration

I live in a real world



Camera Coordinate System



World Coordinate System

$$\begin{pmatrix} X_{cam} \\ Y_{cam} \\ Z_{cam} \\ 1 \end{pmatrix}_{3D} = \begin{bmatrix} \mathbf{R} & \mathbf{t} \\ \mathbf{0}^T & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}_{3D}$$

$$\mathbf{x} = \mathbf{K}[\mathbf{R}|\mathbf{t}] \mathbf{X}$$

calibration

World Coor. \rightarrow Camera Coor.

$$\boxed{P = K[R|t]}$$

Intrinsic Extrinsic
Camera Parameter
Camera Projection Matrix

$$\begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} f & 0 & 0 \\ 0 & f & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} R & t \\ 0^T & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$
$$P = K[R|t]$$
$$K = \begin{bmatrix} f & 0 & 0 \\ 0 & f & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad x = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \quad x = \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$
$$x = Px$$

calibration

Calibration

Traditional object-based calibration^[1]

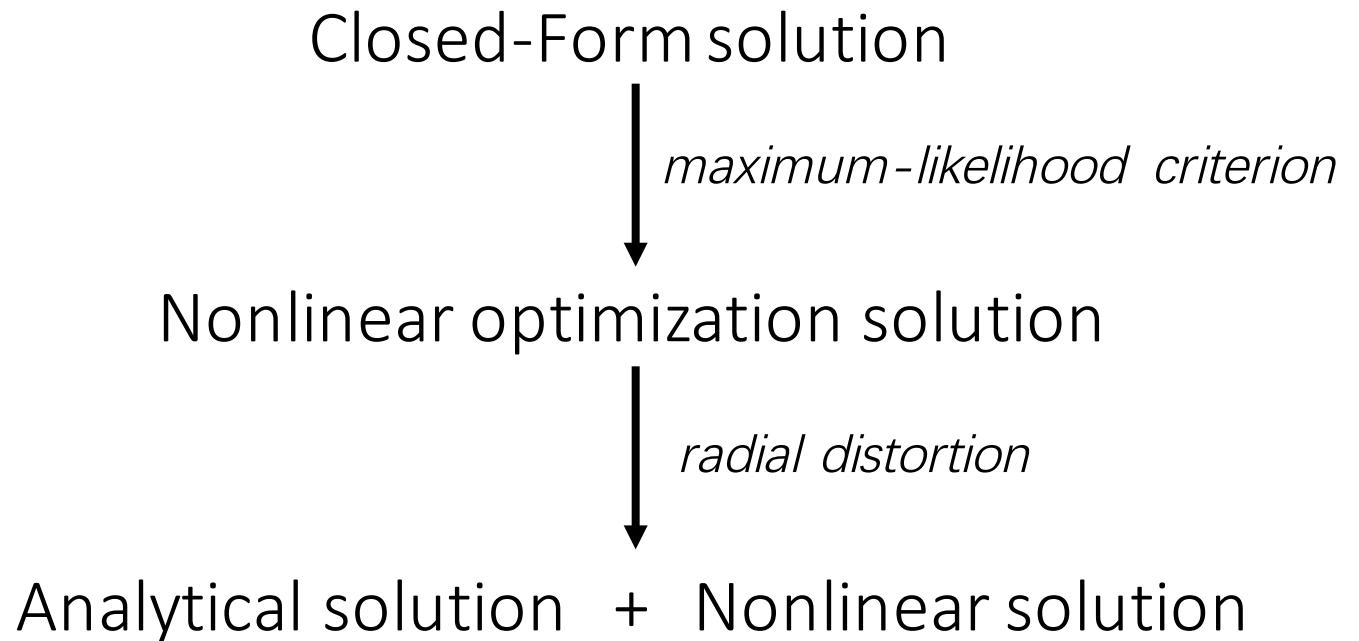
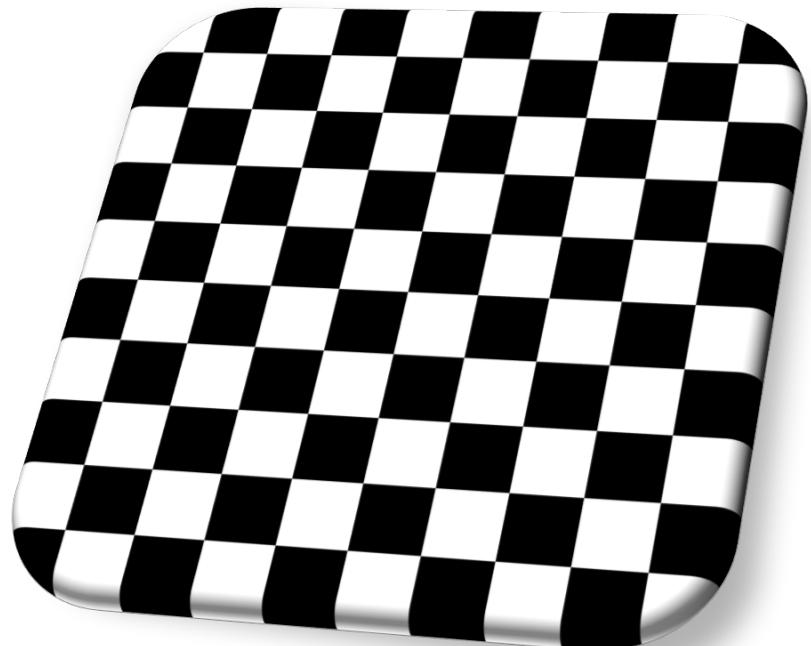
Self-calibration^{[2][3]}

[1]O. Faugeras. "Three-Dimensional Computer Vision: A Geometric Viewpoint ". MIT Press, 1993.

[2]Hartley, Richard I. "An algorithm for self calibration from several views." *Cvpr*. Vol. 94. 1994.

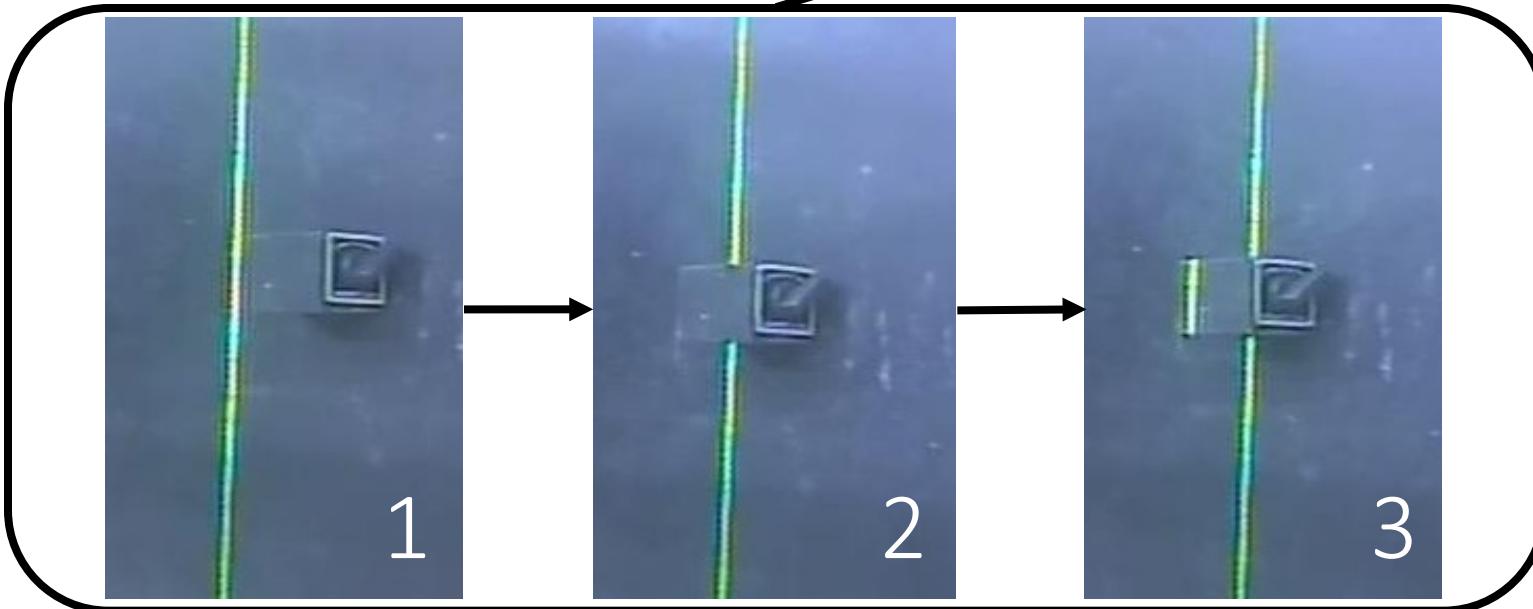
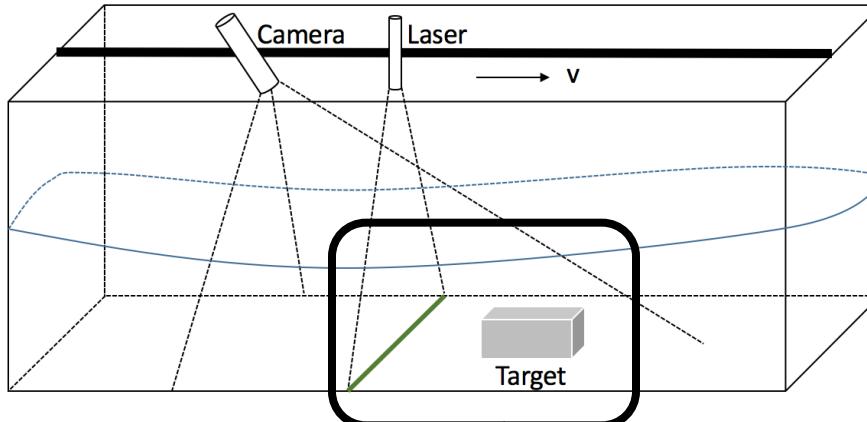
[3] Luong, Q-T. "Self-calibration of a moving camera from point correspondences and fundamental matrices." *International Journal of computer vision* 22.3 (1997): 261-289.

Zhang Zhengyou calibration method

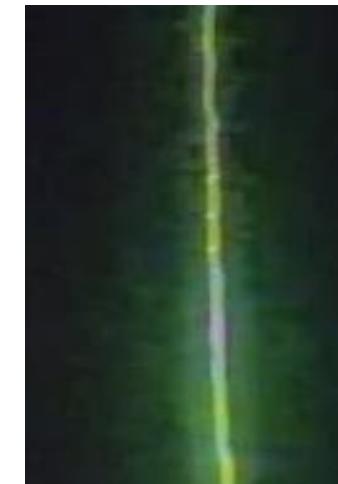
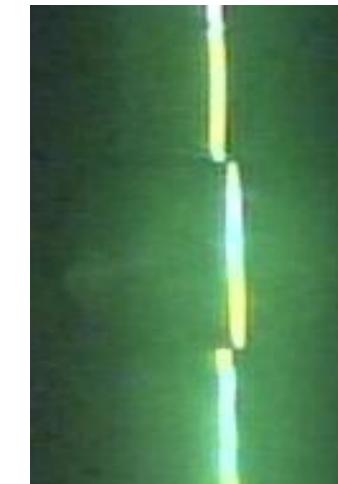
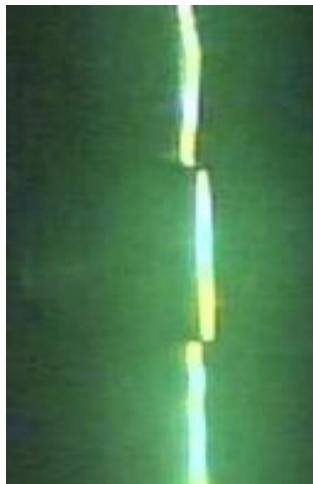
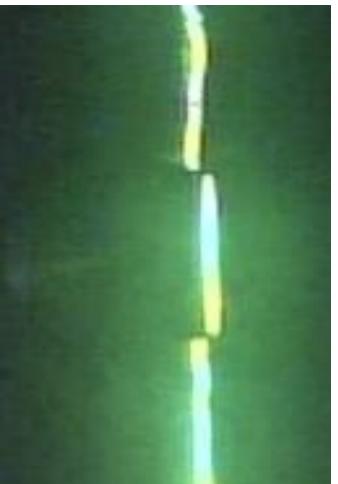


Zhang, Zhengyou. "A flexible new technique for camera calibration."
IEEE Transactions on pattern analysis and machine intelligence 22.11 (2000): 1330-1334.

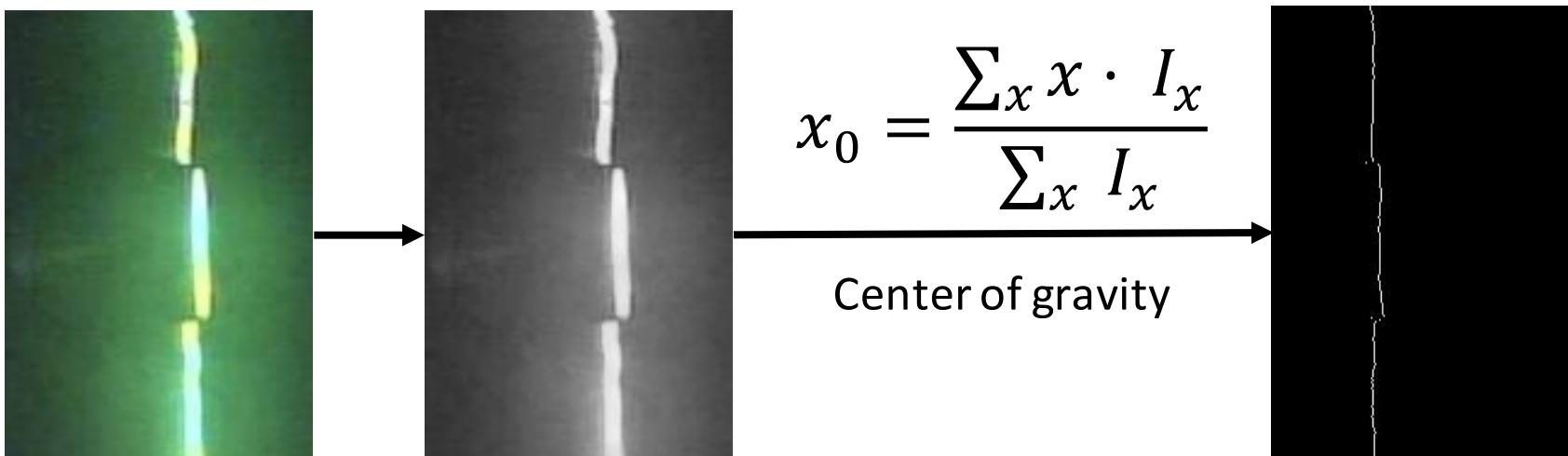
Acquisition

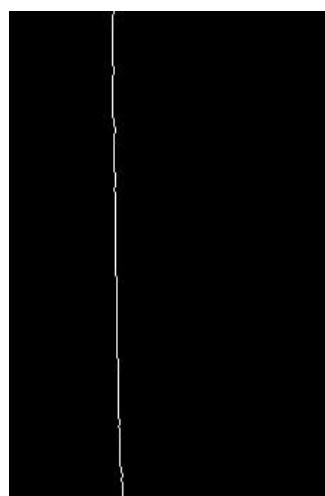
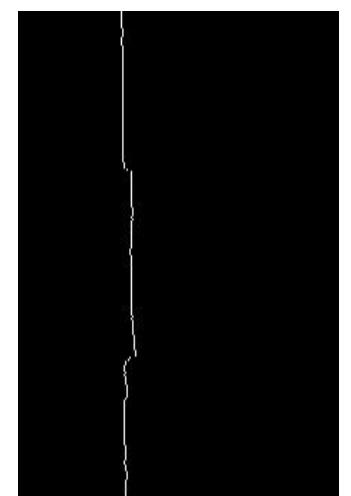
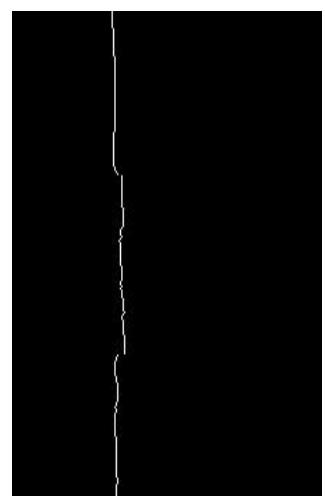
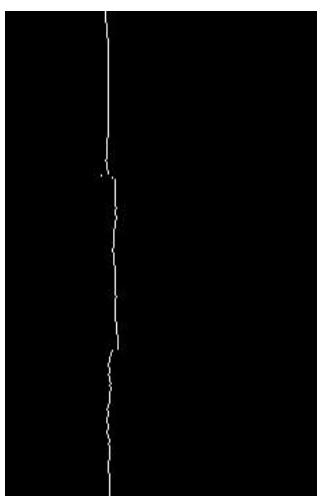
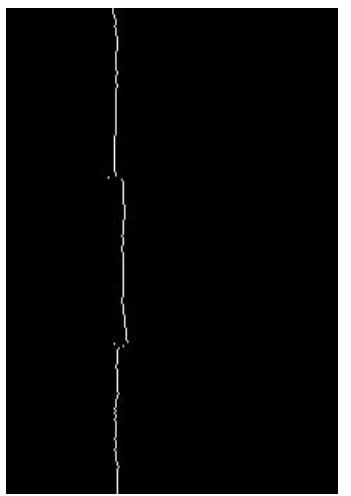
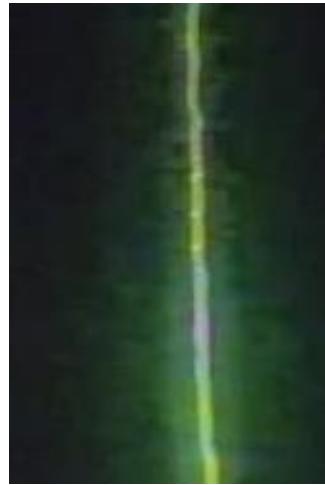
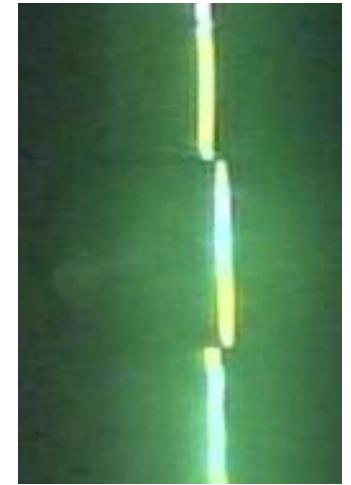
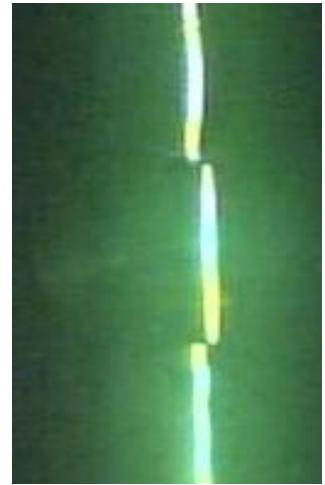
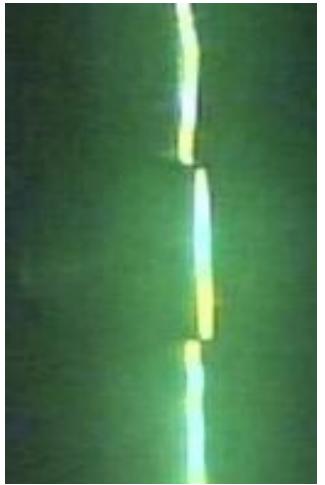
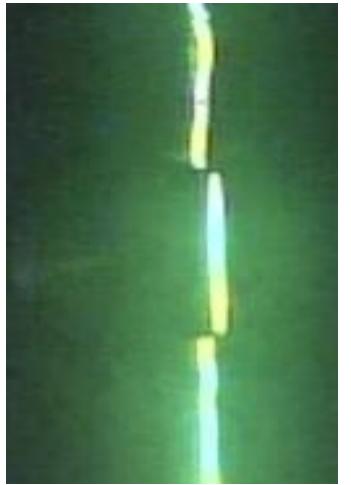


Acquisition

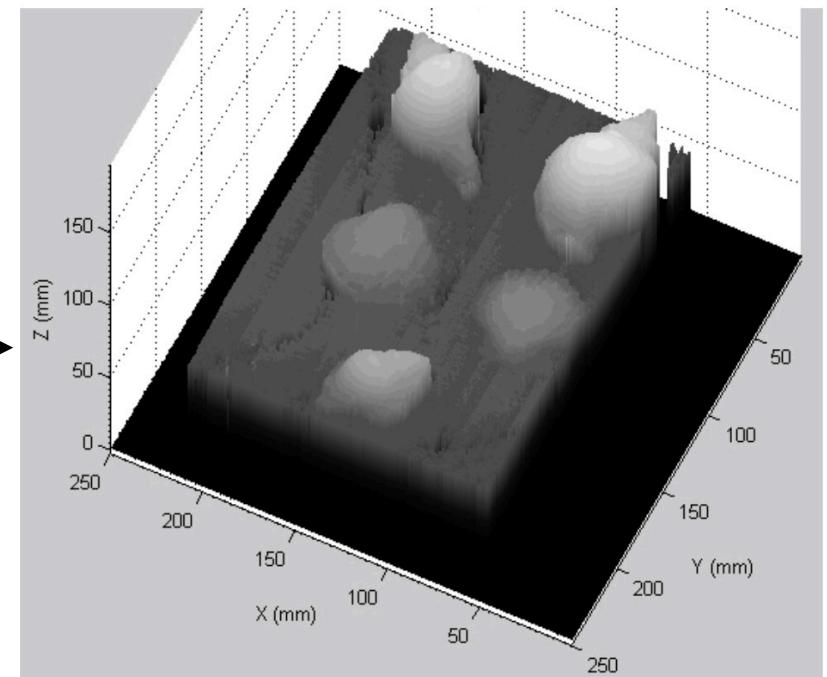
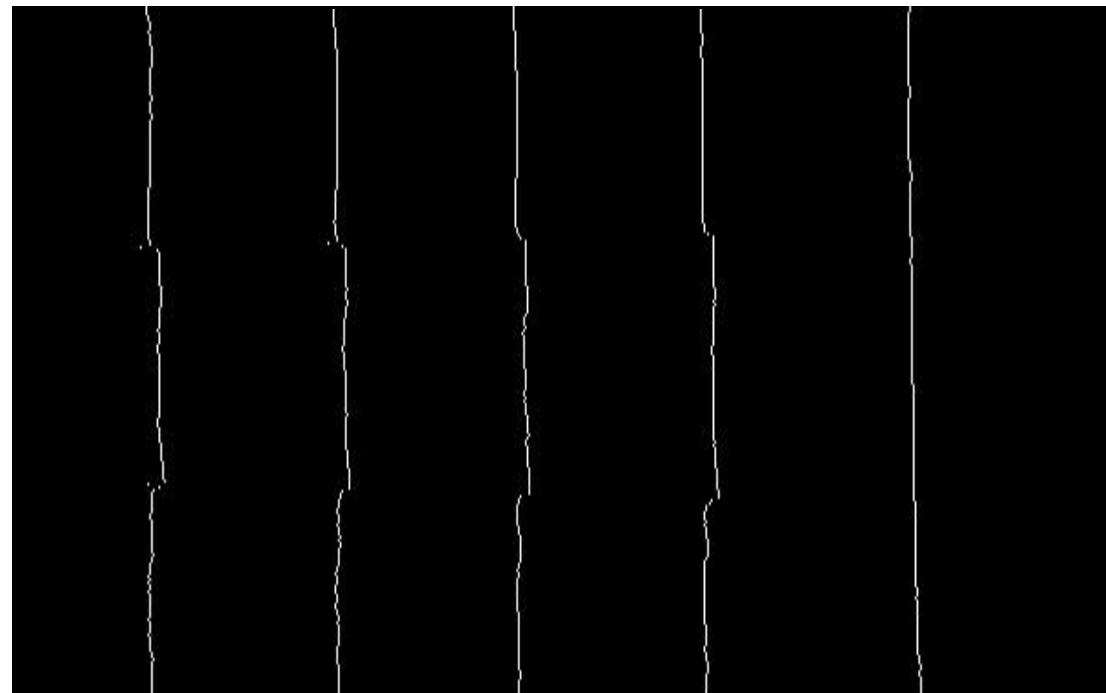


Extraction

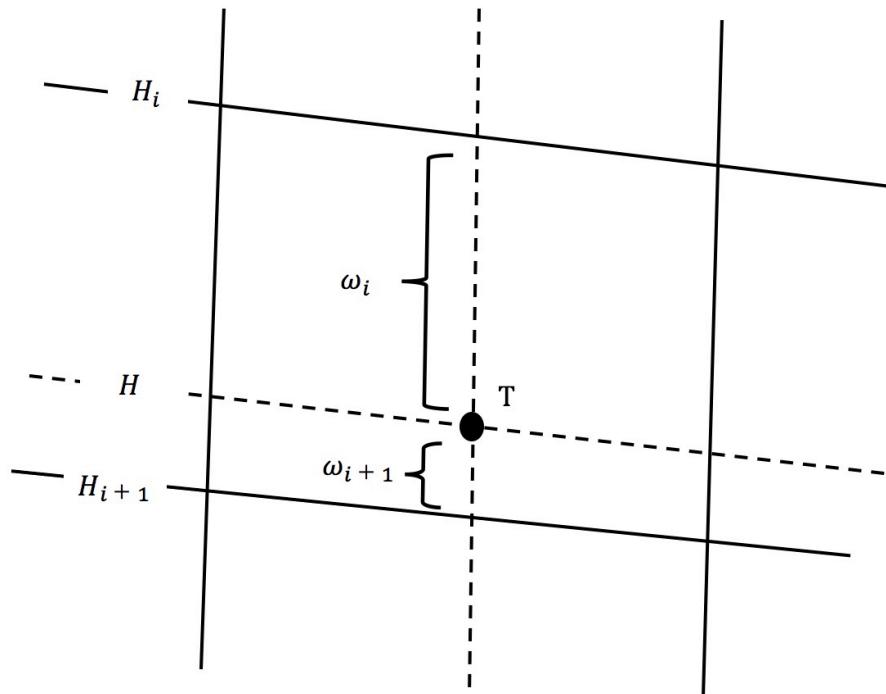




Transformation



Transformation

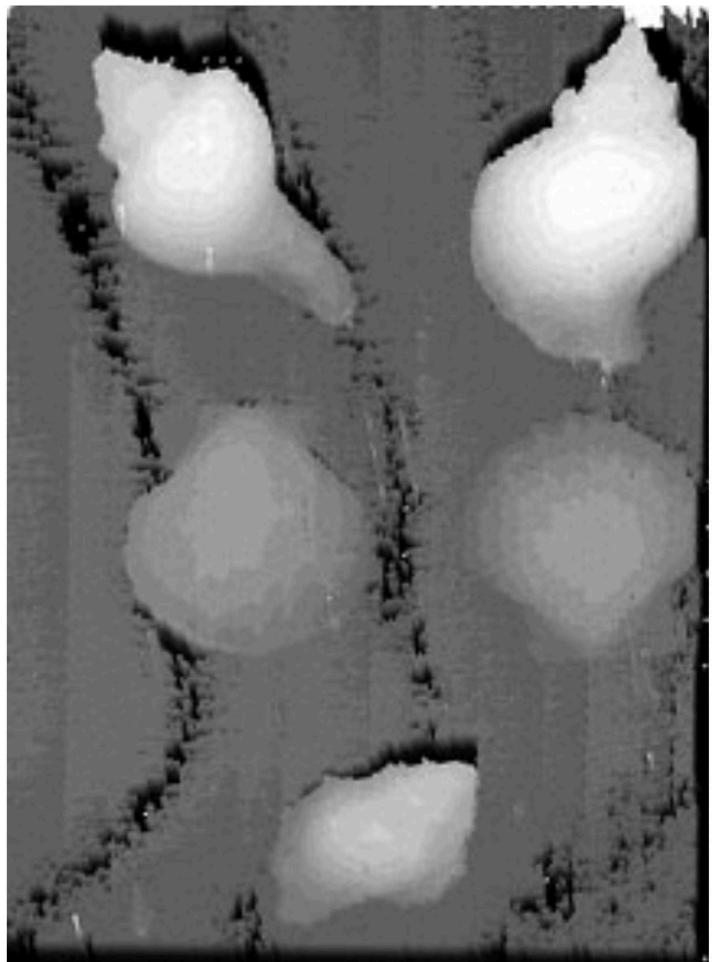


$$\omega_i = \frac{H - H_i}{H_{i+1} - H_i}$$

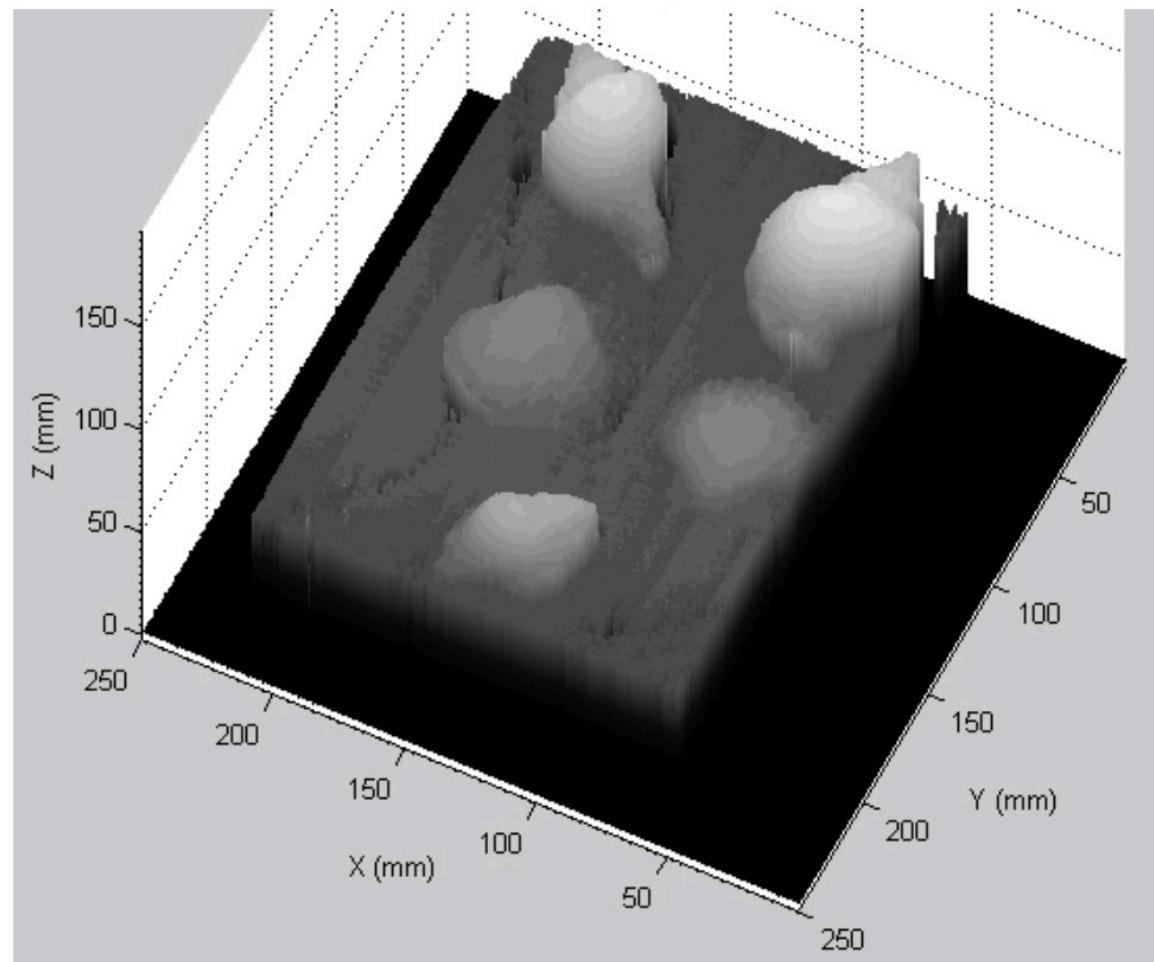
$$\omega_i + \omega_{i+1} = 1$$

$$h = \omega_i H_i + \omega_{i+1} H_{i+1}$$

Wang, Chau-Chang, and Min-Shine Cheng. "Nonmetric camera calibration for underwater laser scanning system." *IEEE Journal of Oceanic Engineering* 32.2 (2007): 383-399.

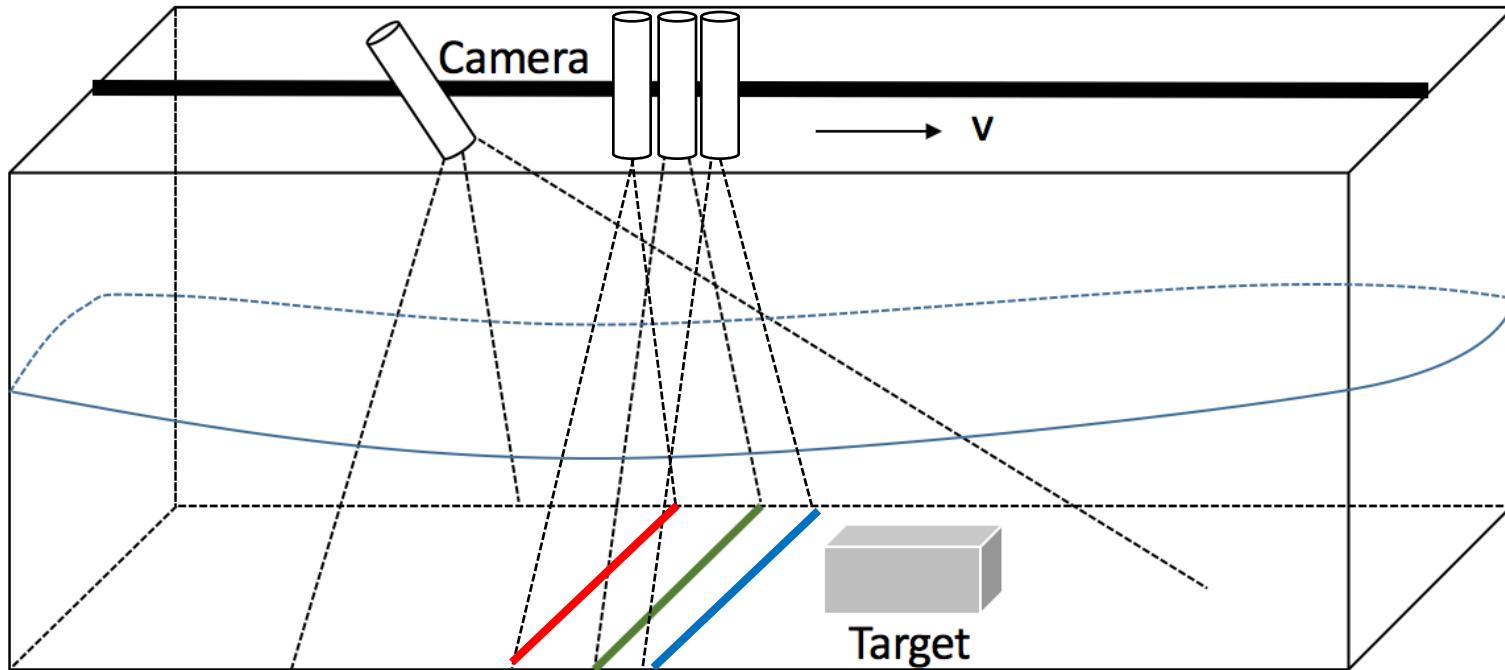


(a)



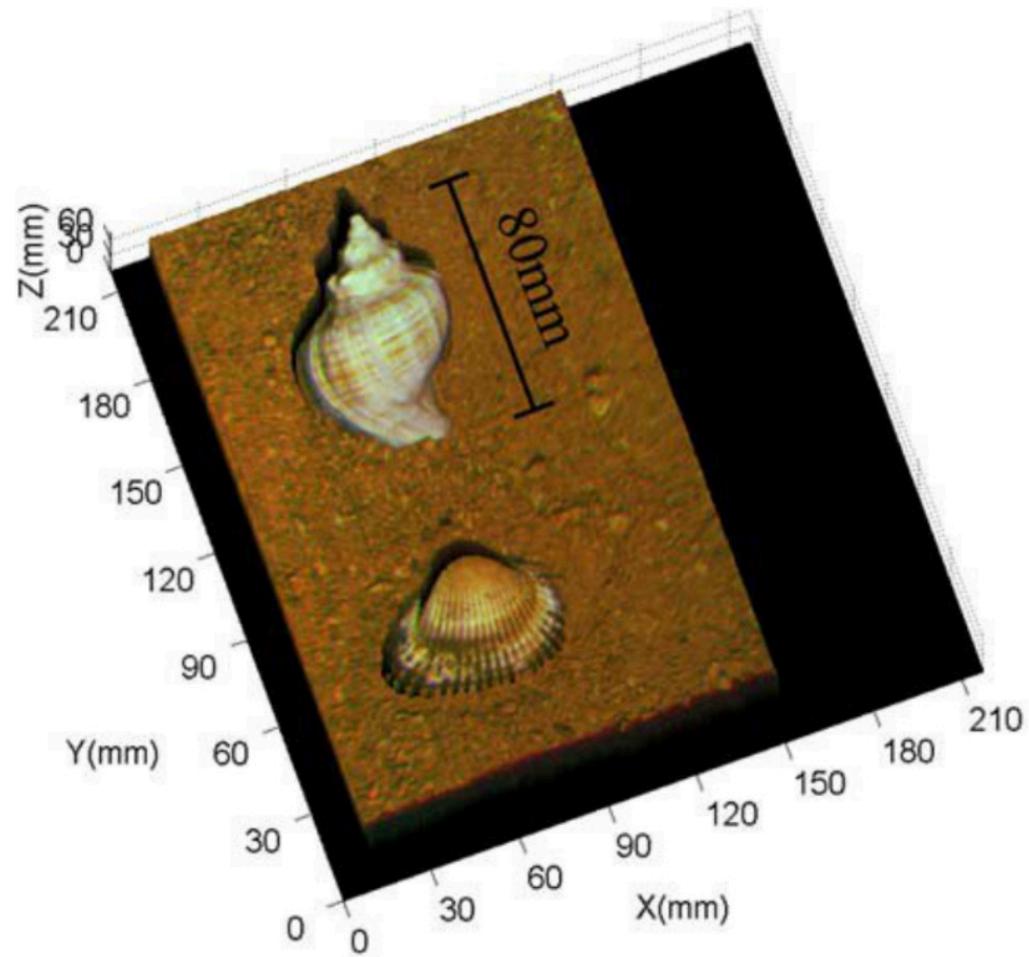
(b)

Yang, Yu, et al. "3D reconstruction for underwater laser line scanning." *OCEANS-Bergen, 2013 MTS/IEEE*. IEEE, 2013.

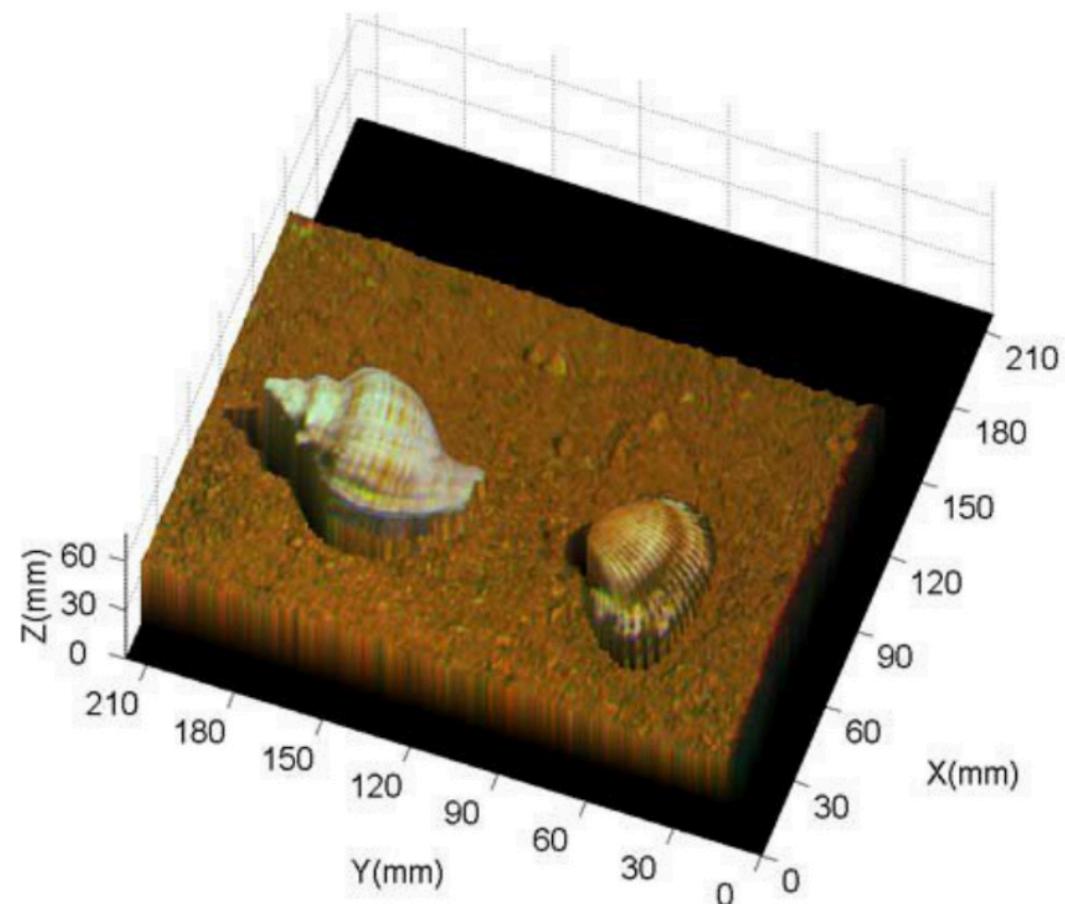


Calibration + Color calibration

Transformation + Color compound



(a)



(b)

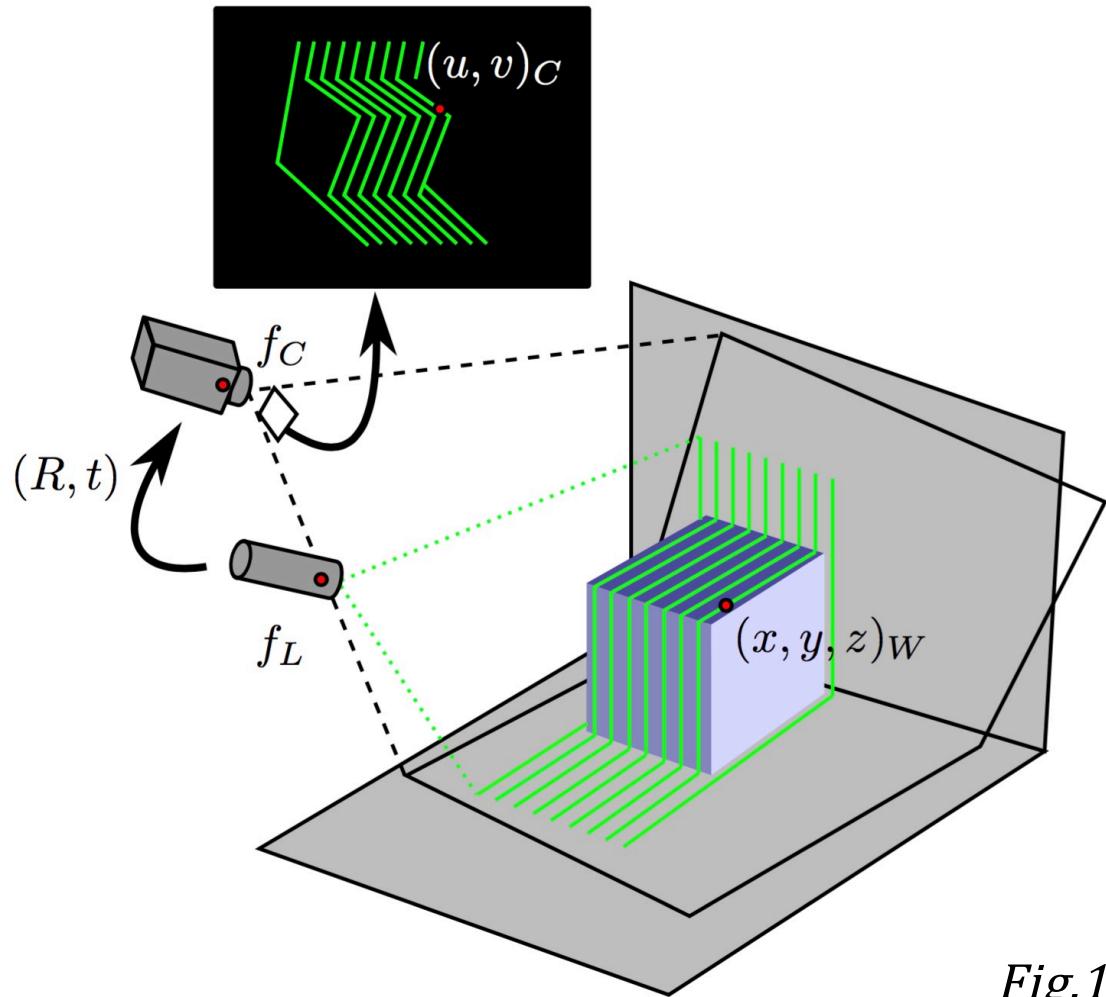
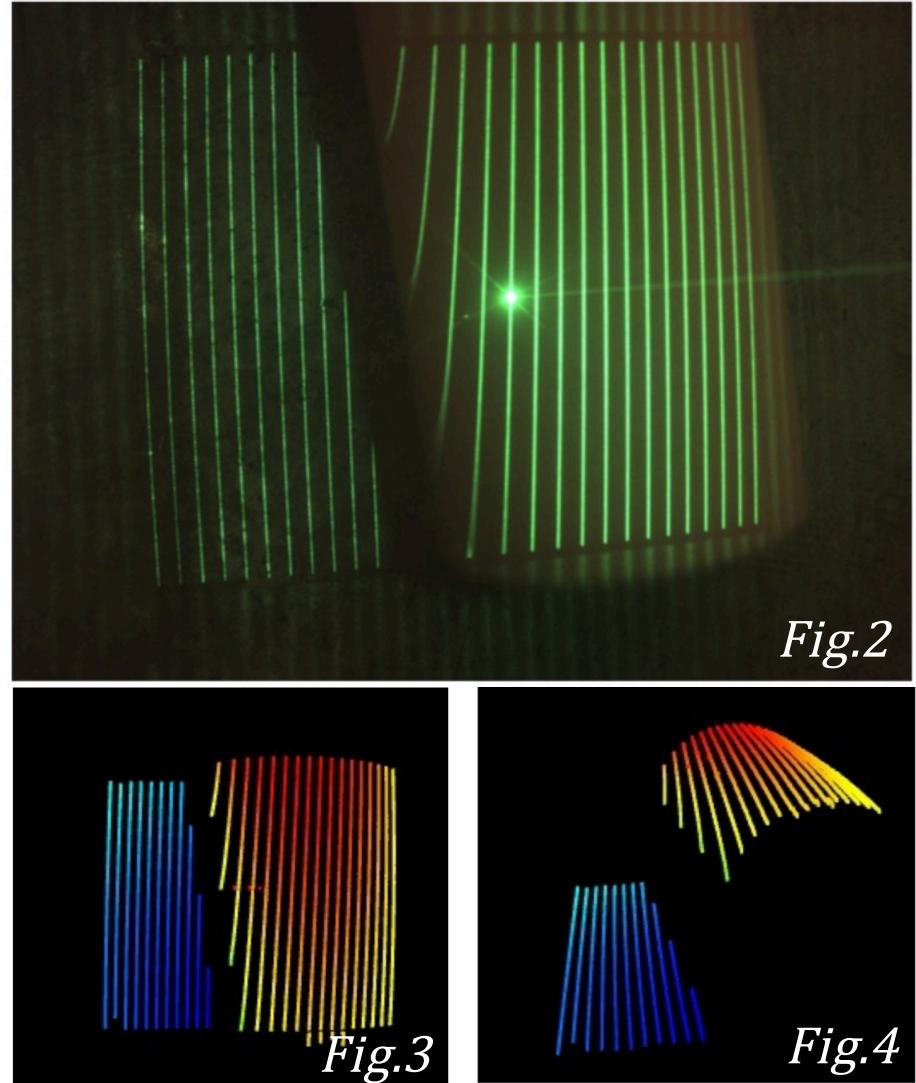
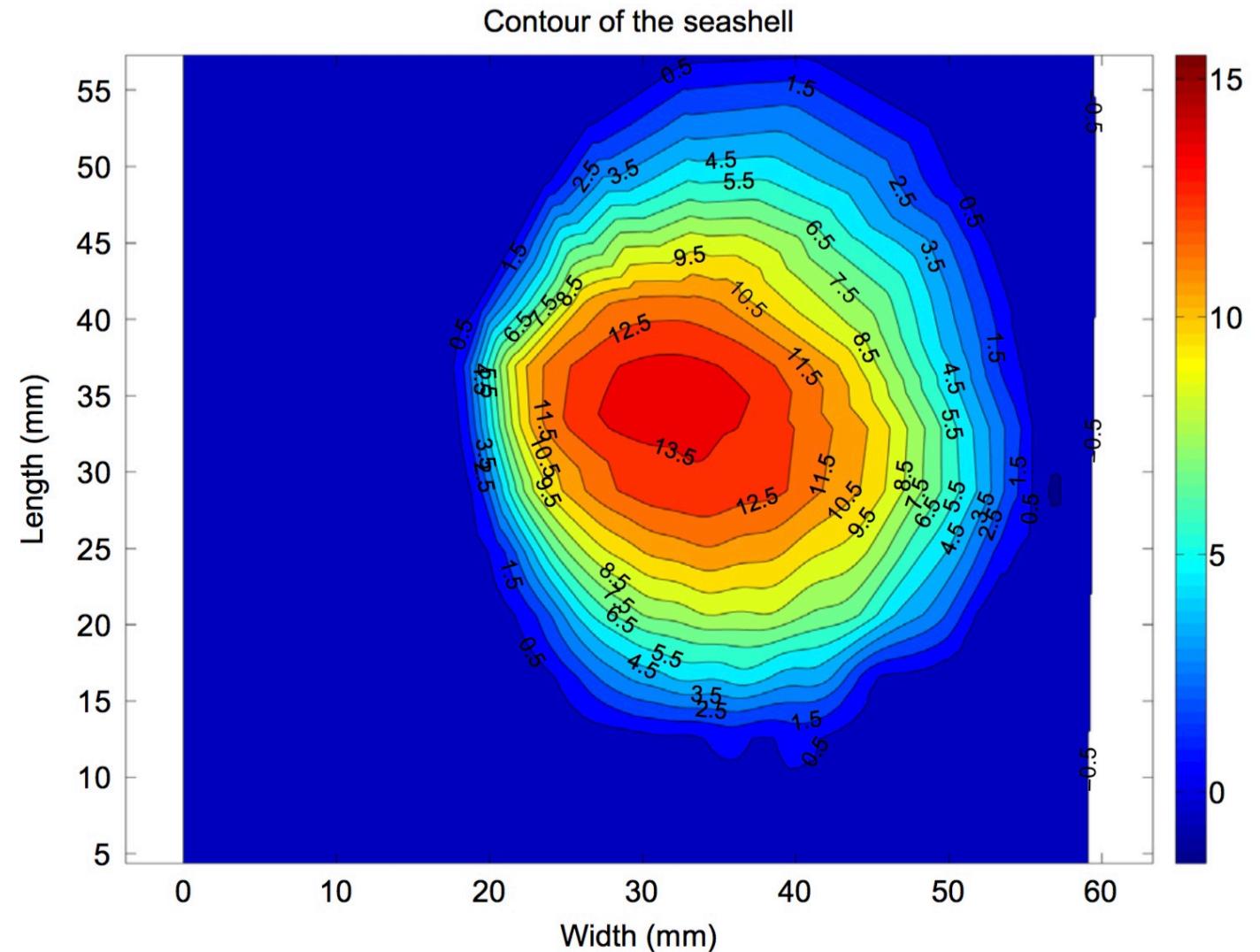
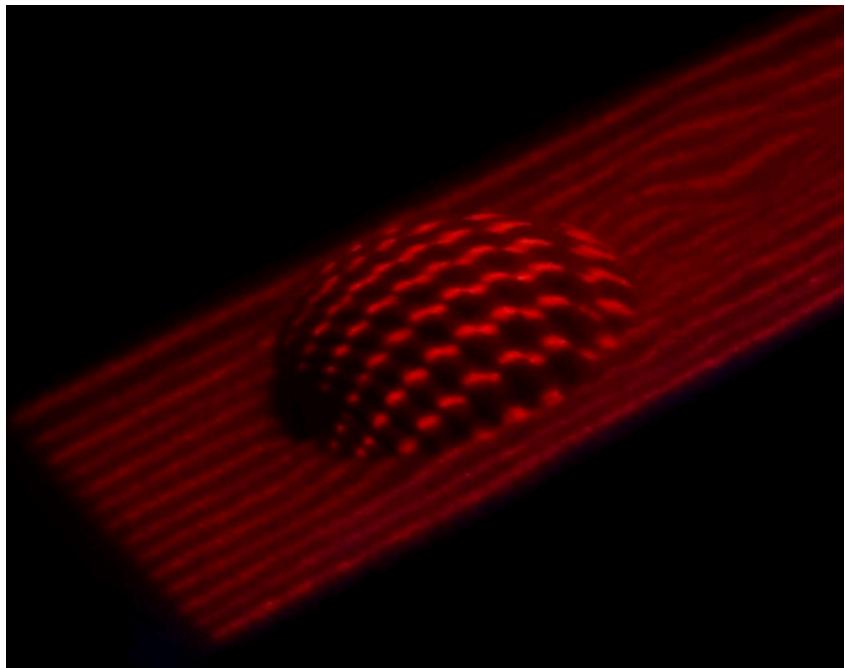


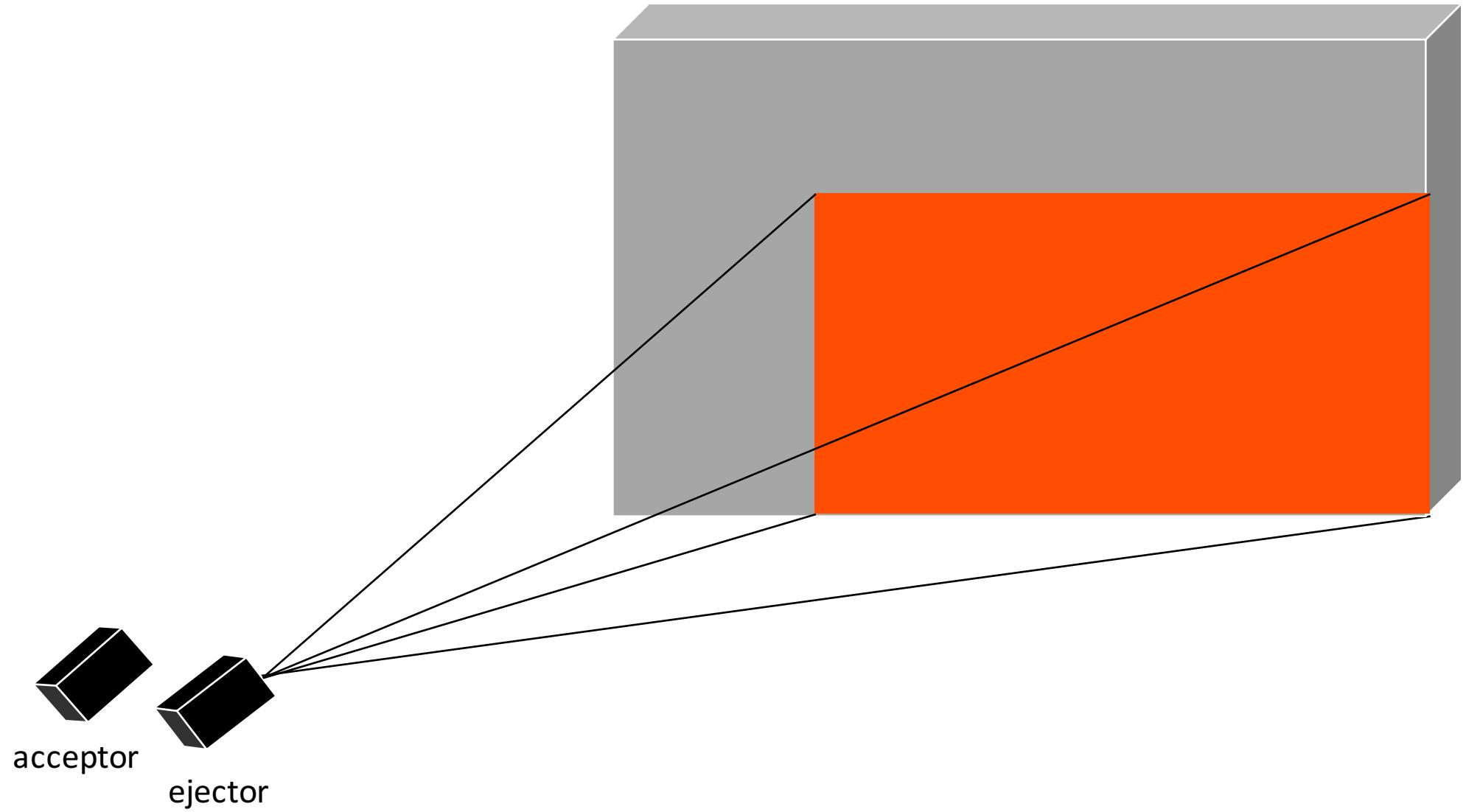
Fig.1



Massot-Campos, Miquel, and Gabriel Oliver-Codina. "One-shot underwater 3D reconstruction." *Emerging Technology and Factory Automation (ETFA), 2014 IEEE*. IEEE, 2014.



Cebrián-Robles, D., and J. Ortega-Casanova. "Low cost 3D underwater surface reconstruction technique by image processing." *Ocean Engineering* 113 (2016): 24-33.



Modified method

Kinect



First generation

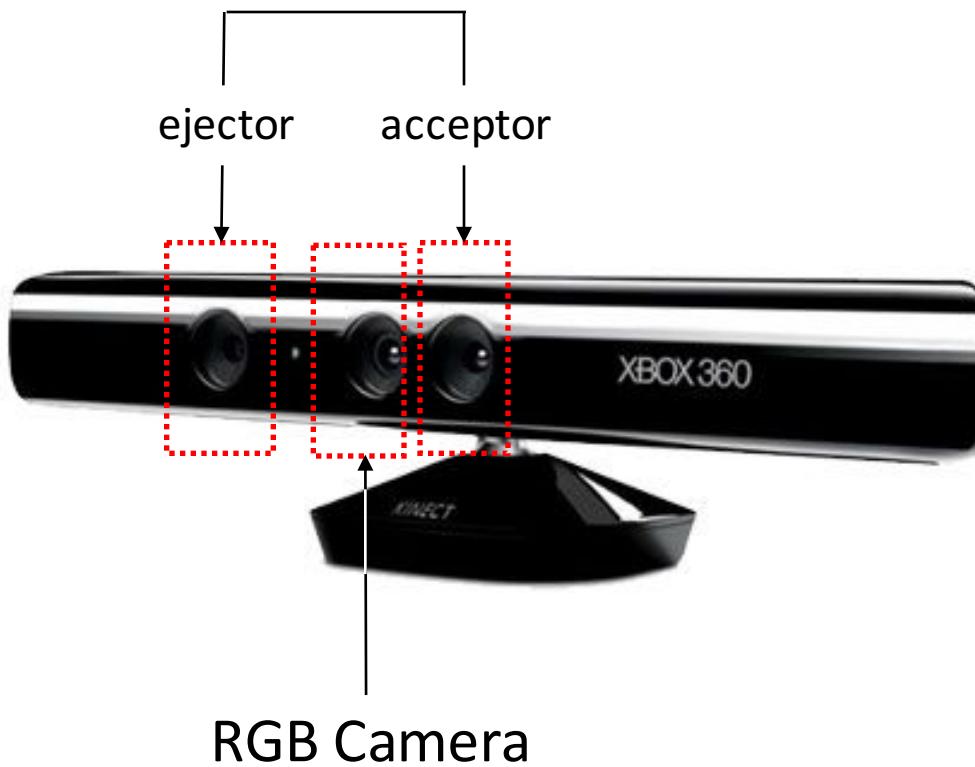


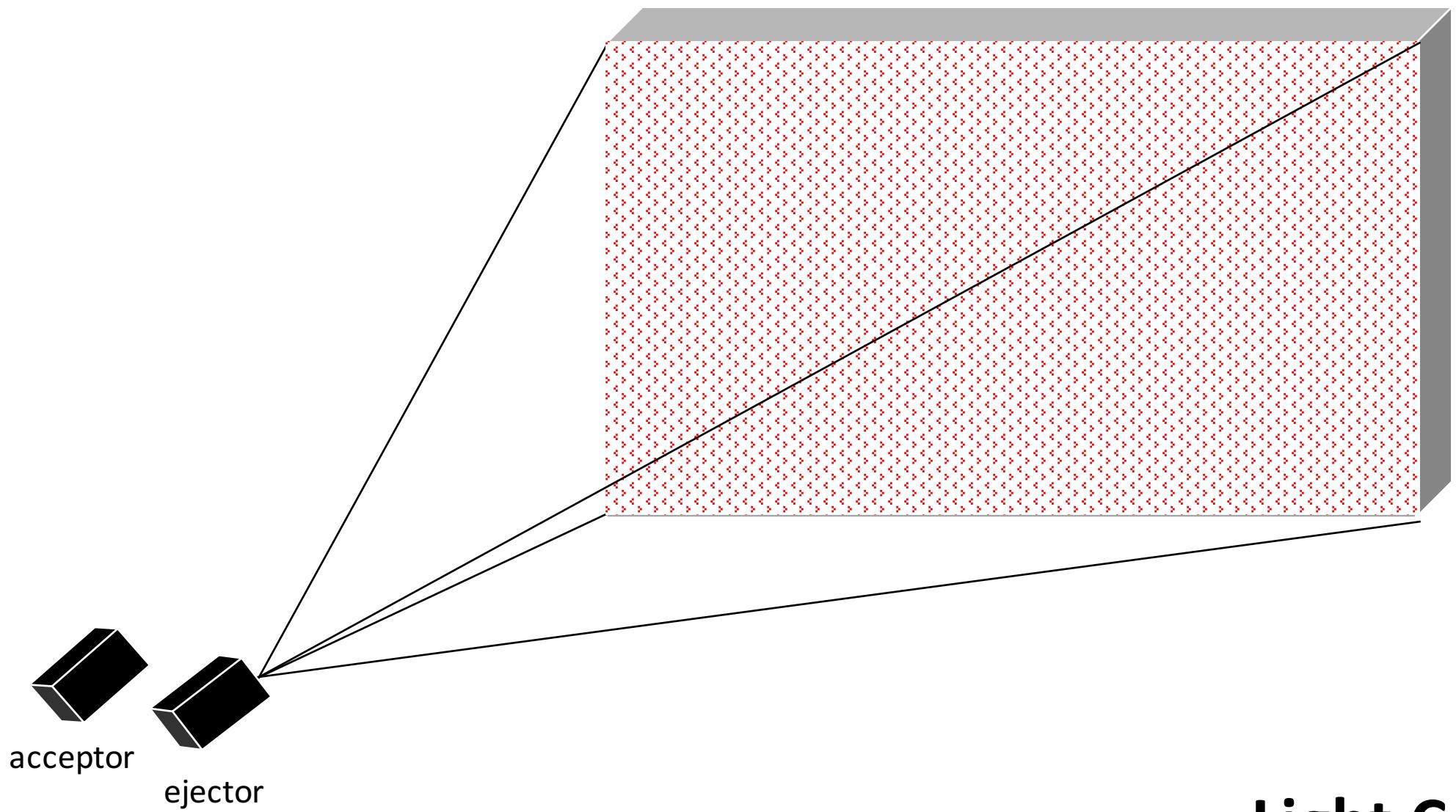
Second generation

Light Coding

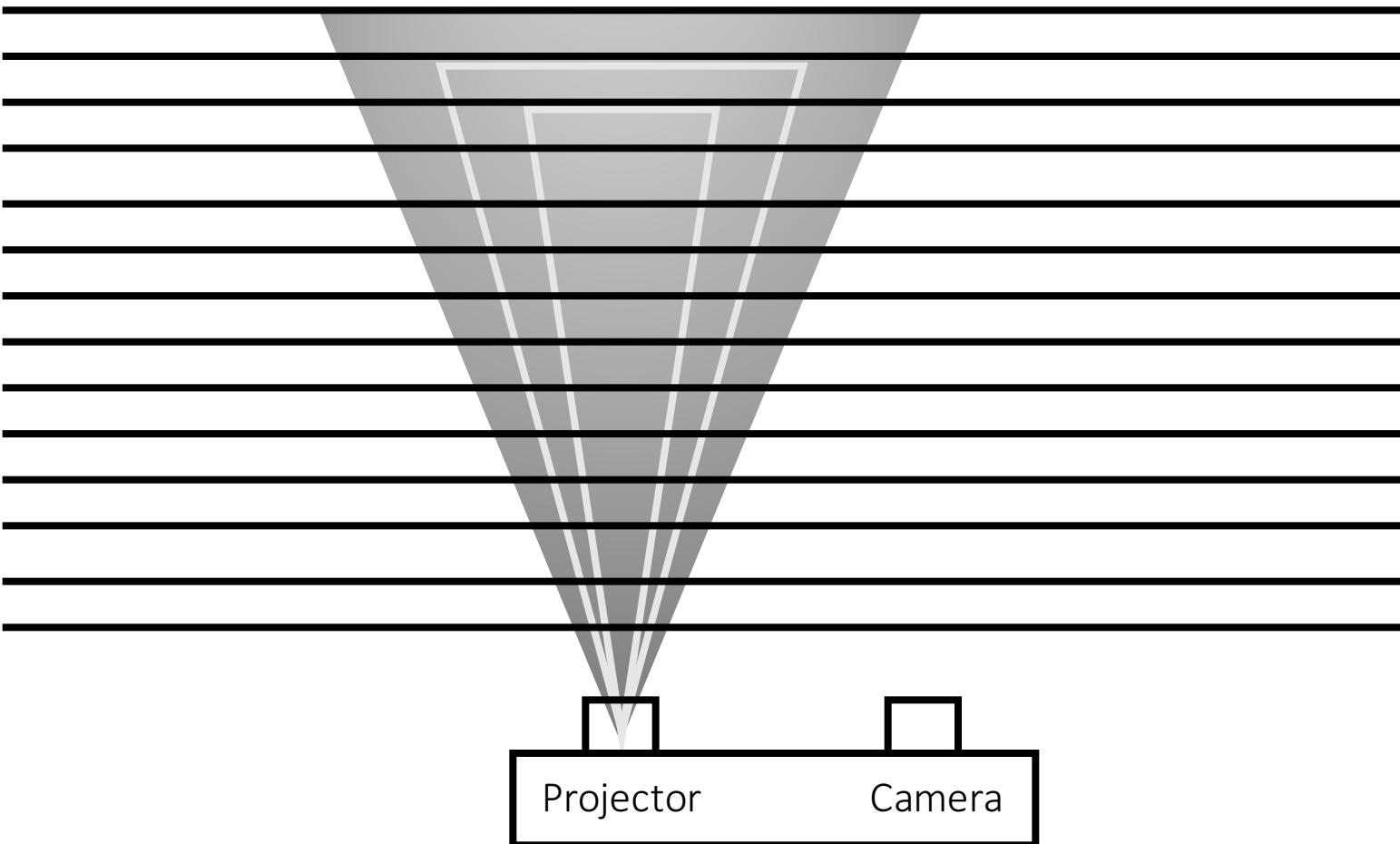
Time of Flight

3D Depth Sensors



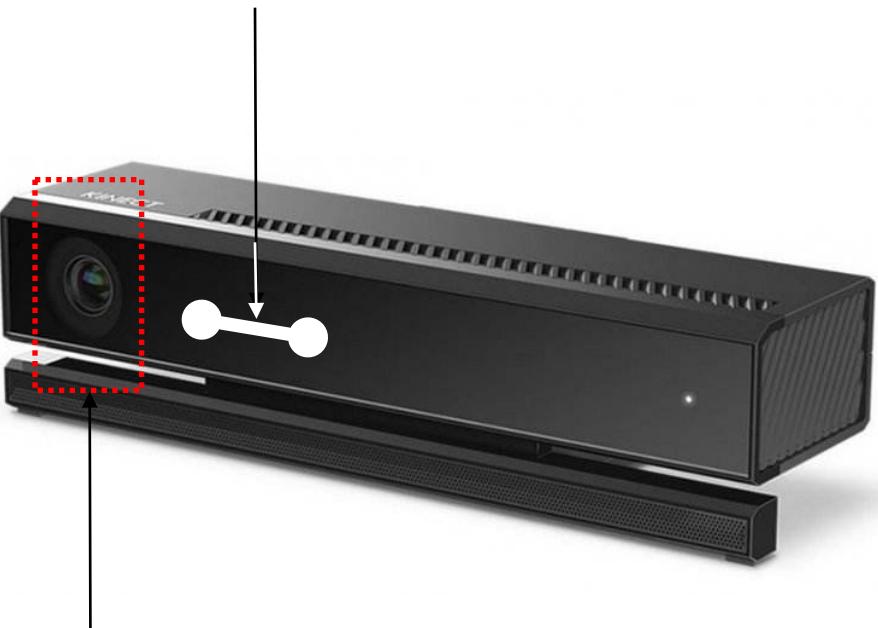


Light Coding



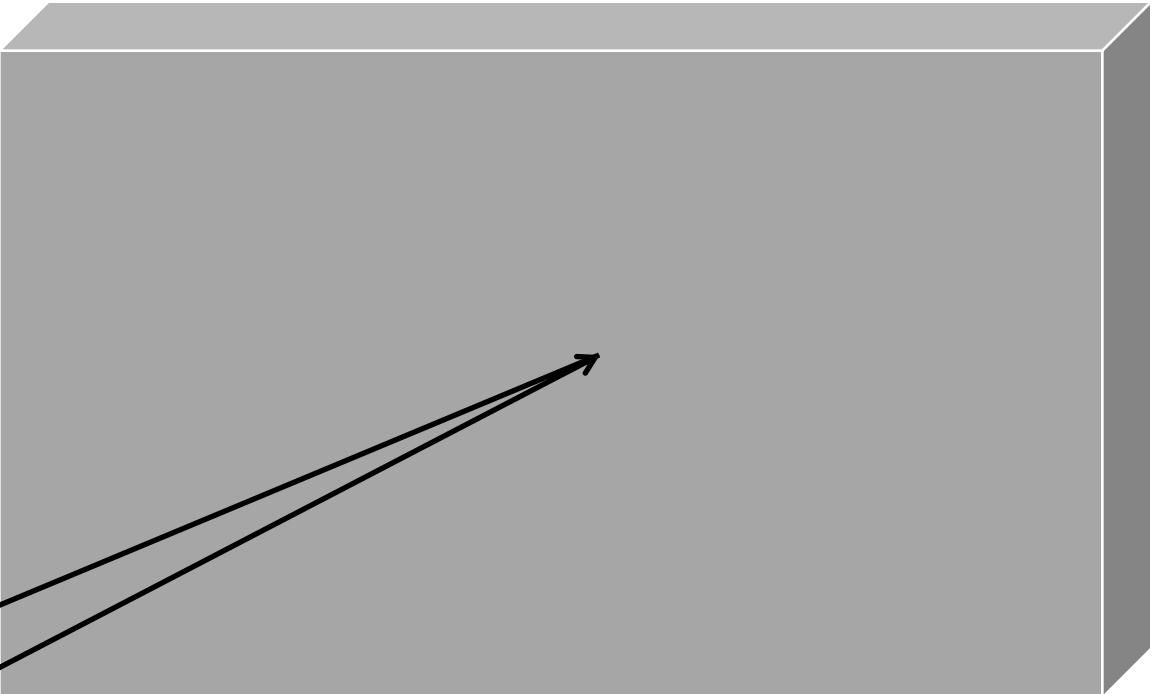
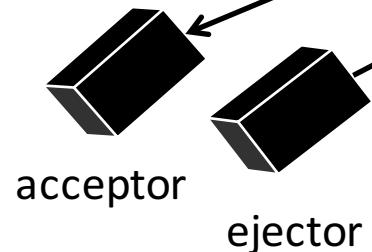
Light Coding

3D Depth Sensors

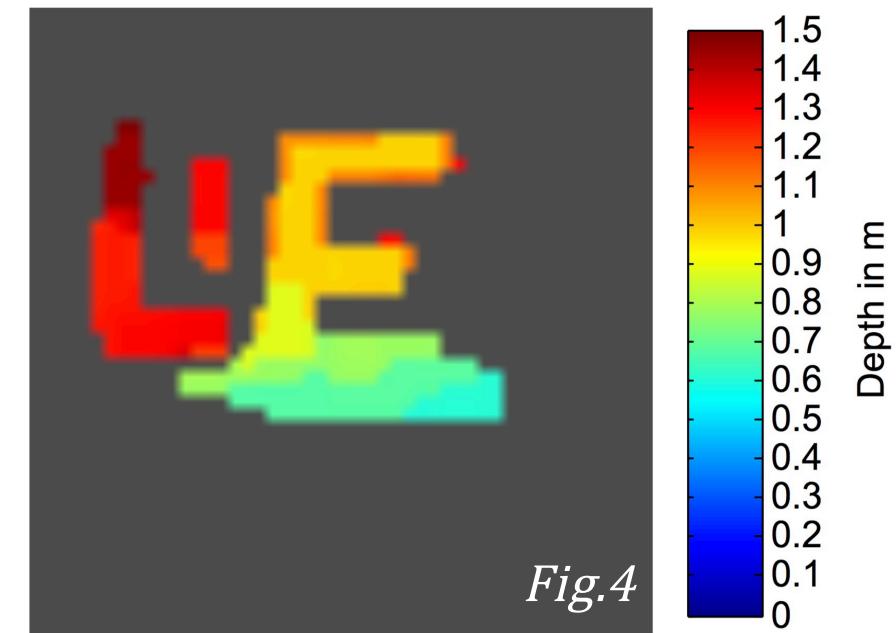
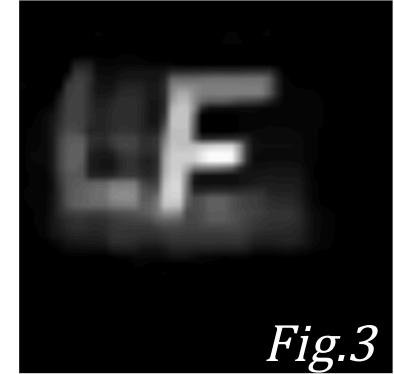
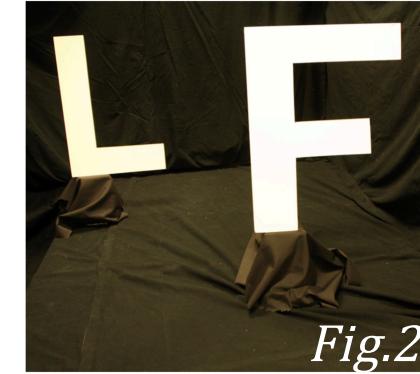
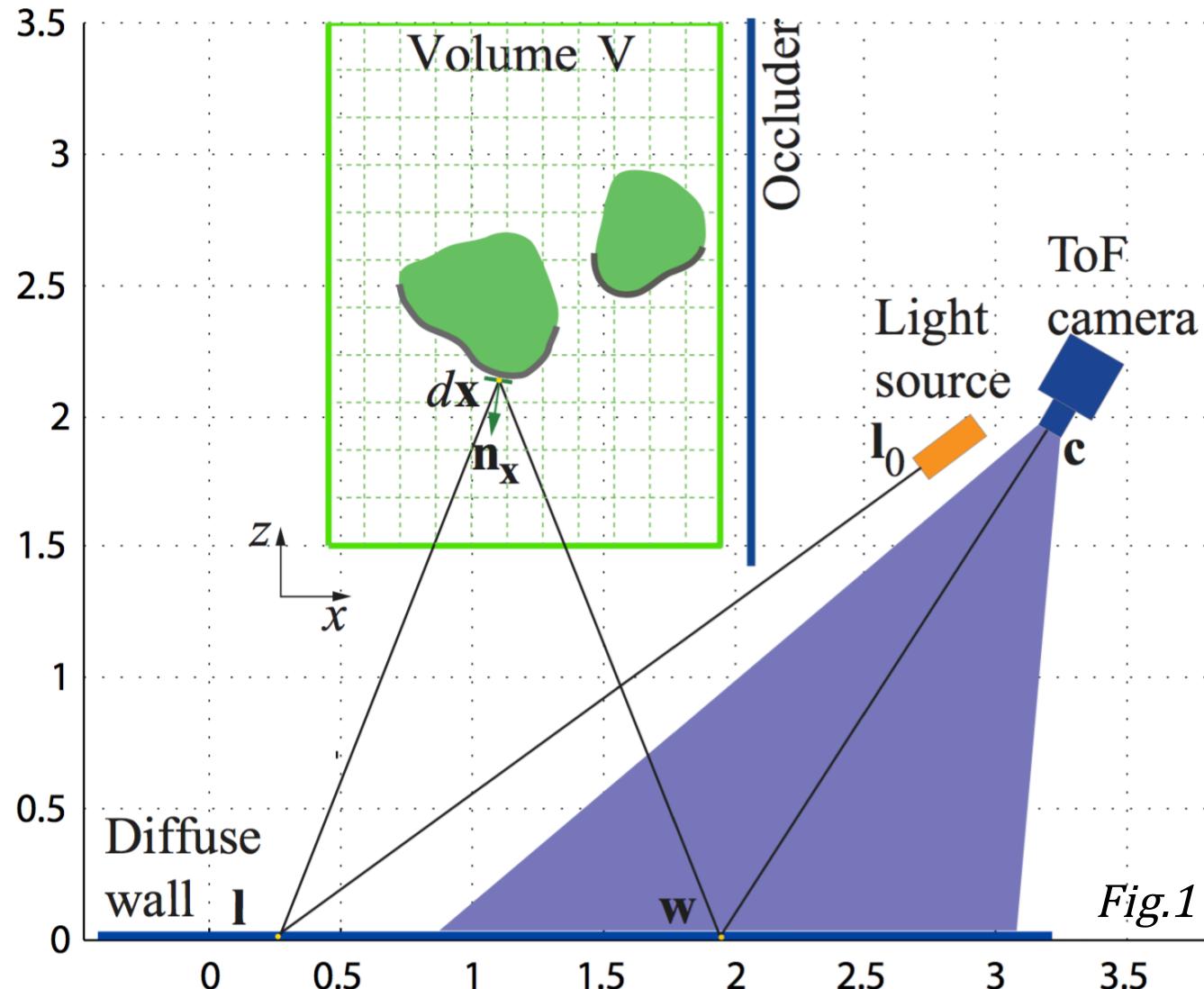


RGB Camera

$$d = \frac{ct}{2}$$



Time of Flight



Heide, Felix, et al. "Diffuse Mirrors: 3D Reconstruction from Diffuse Indirect Illumination Using Inexpensive Time-of-Flight Sensors." *IEEE Conference on Computer Vision and Pattern Recognition* IEEE Computer Society, 2014:3222-3229.

Passive methods

Photos

Monocular vision

One camera

Binocular vision

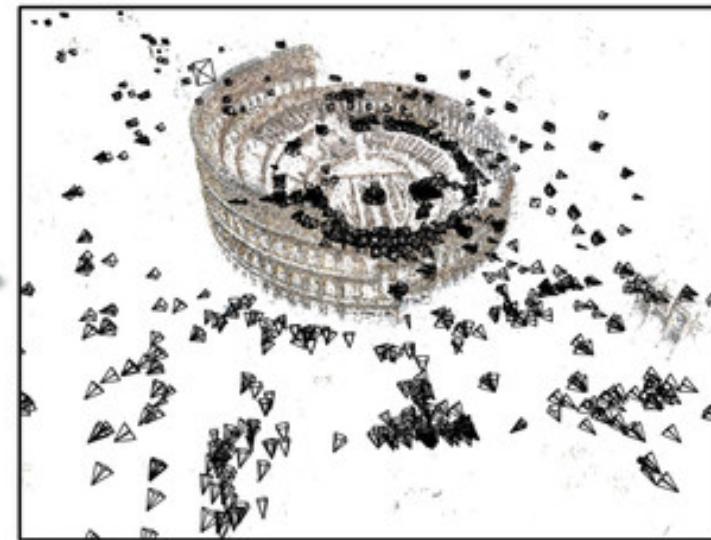
Two parallel camera

Structure from Motion

two-dimensional image sequences



three-dimensional structures



Structure from Motion

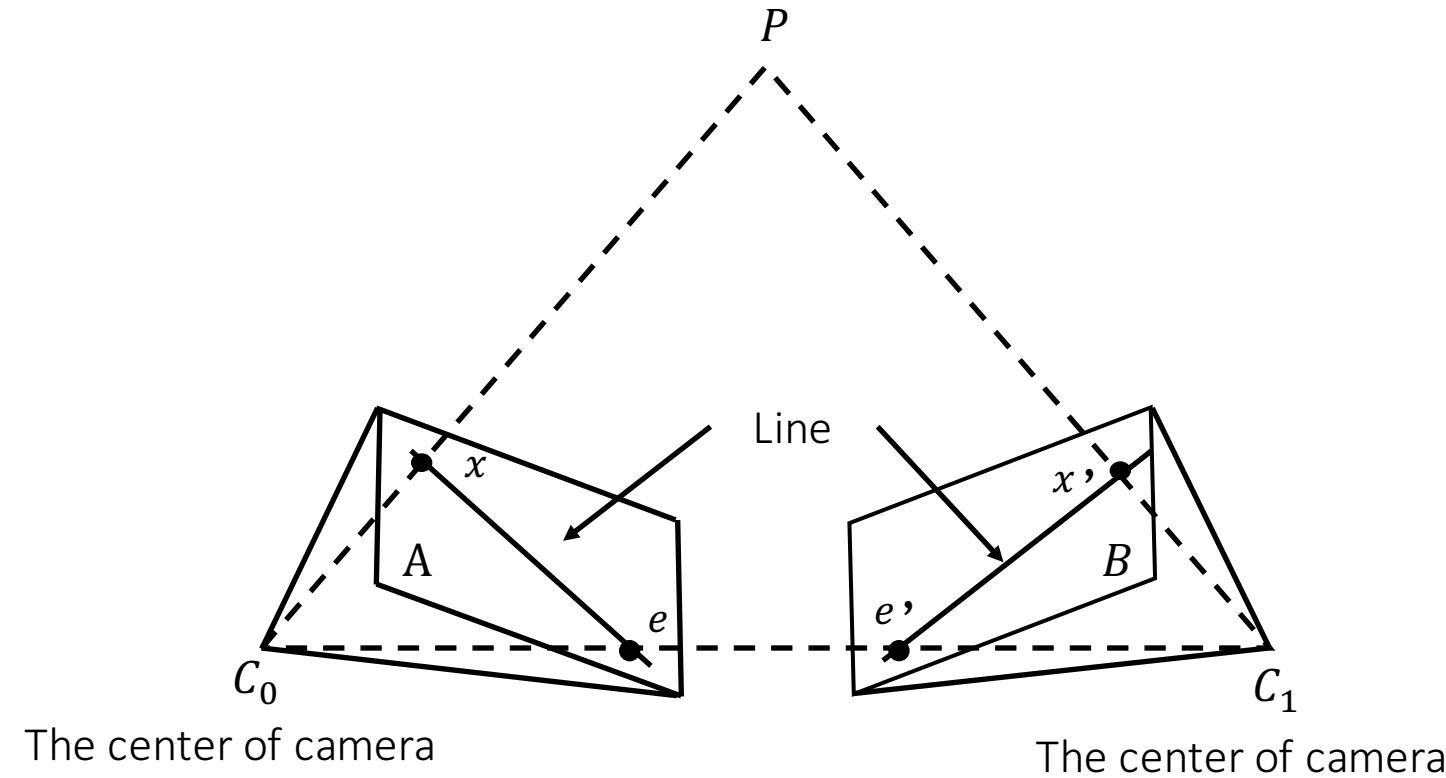
advantage

1. Calibration
2. Acquisition
3. Scene

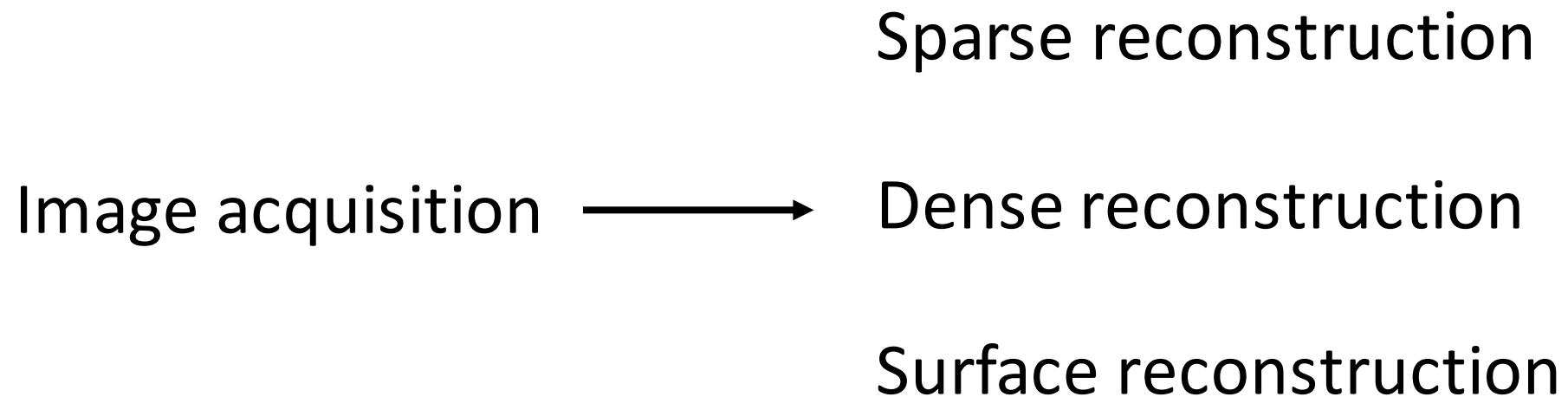
disadvantage

1. Arithmetic
2. Accuracy
3. Time

Introduction



Introduction



Acquisition



UAV



Digital camera



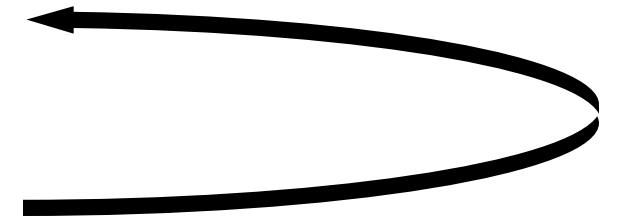
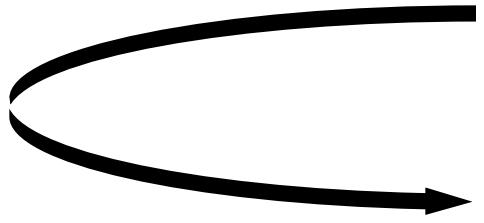
Camera



Street car



Mobile phone



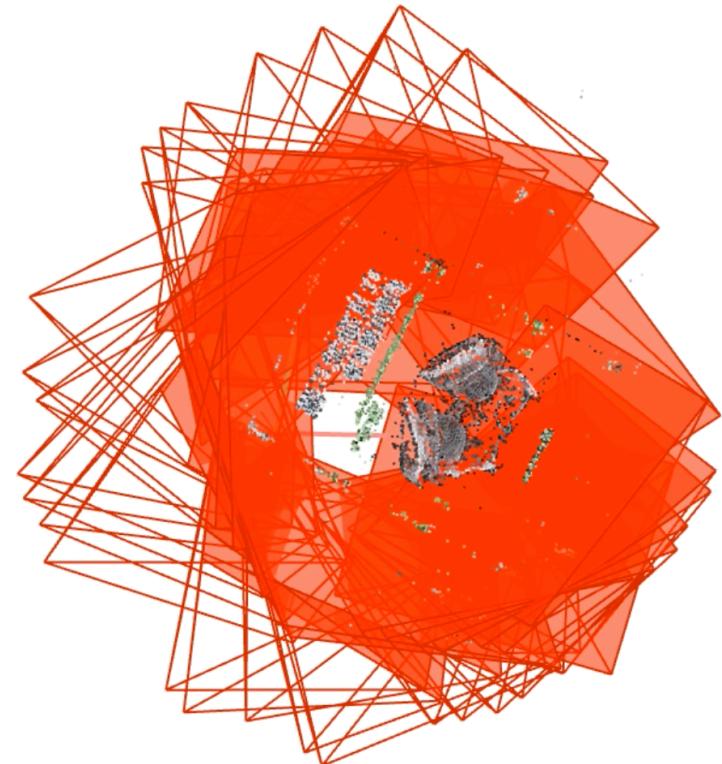
vision@ouc

Sparse reconstruction

Feature point matching

Calculation of camera parameters

Bundle adjustment



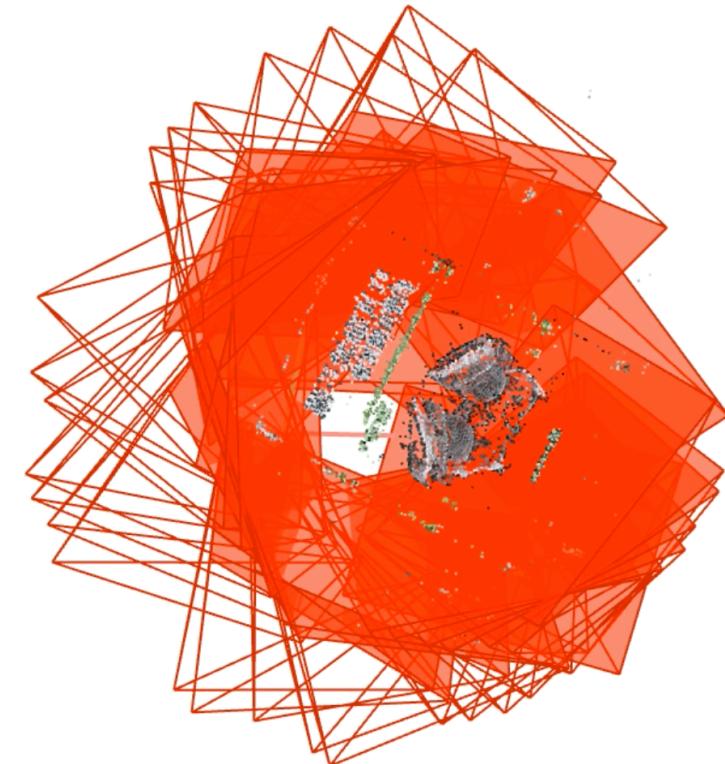
The generated process of Sparse reconstruction

Sparse reconstruction

Feature point matching

Calculation of camera parameters

Bundle adjustment



The generated process of Sparse reconstruction

Feature point matching

Harris corner detection^[1]

SIFT (Scale-invariant feature transform) [2]

SURF (Speeded Up Robust Features) [3]

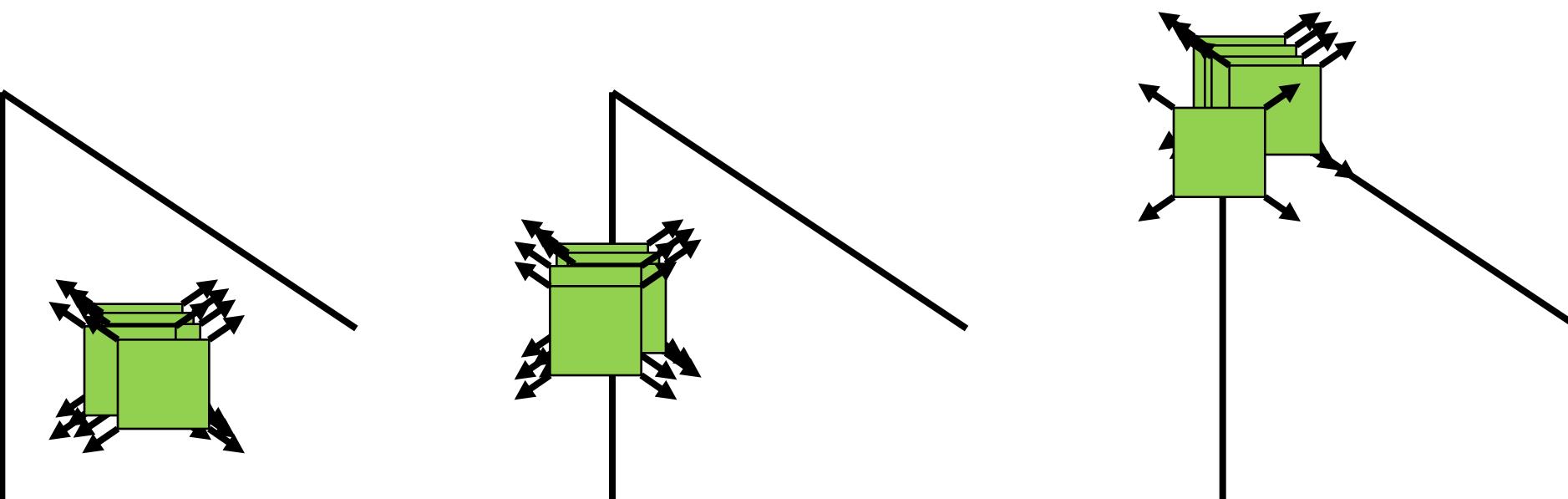
[1] Harris, Chris, and Mike Stephens. "A combined corner and edge detector." *Alvey vision conference*. Vol. 15. No. 50. 1988.

[2] Lowe, David G. "Object recognition from local scale-invariant features." *Computer vision*, 1999.

The proceedings of the seventh IEEE international conference on. Vol. 2. Ieee, 1999.

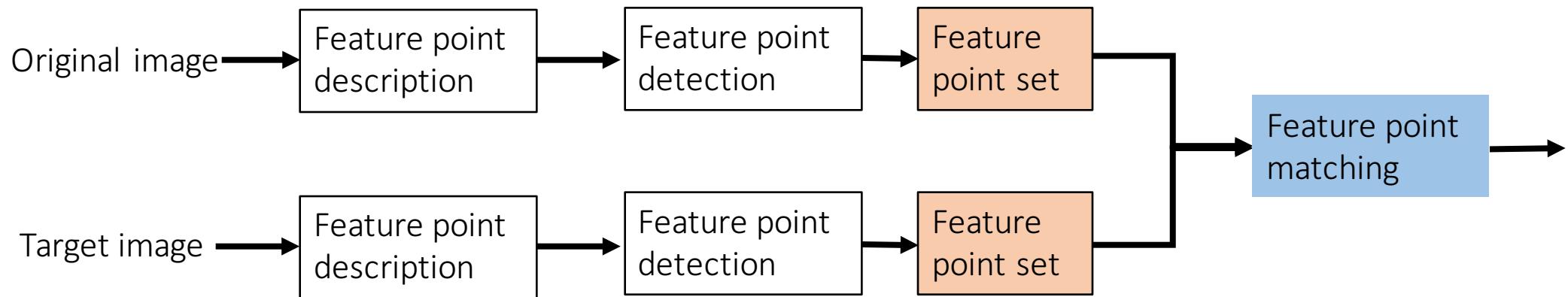
[3] Bay, Herbert, Tinne Tuytelaars, and Luc Van Gool. "Surf: Speeded up robust features." *Computer vision–ECCV 2006* (2006): 404-417.

Harris corner detection



Harris, Chris, and Mike Stephens. "A combined corner and edge detector." *Alvey vision conference*. Vol. 15. No. 50. 1988.

SIFT



Lowe, David G. "Object recognition from local scale-invariant features." *Computer vision*, 1999.
The proceedings of the seventh IEEE international conference on. Vol. 2. Ieee, 1999.

SIFT vs SURF

The establishment of scale space

The extraction of feature points

The generation of feature descriptors

The matching of feature points

similarity

The way of convolution

The detection of feature points

The way of finding direction

The descriptor of feature point

difference

Comparison

Method	Time	Scale	Rotation	Blur	Illumination	Affine
SIFT	common	best	best	best	common	good
PCA-SIFT	good	common	good	common	good	good
SURF	best	good	common	good	best	good

Graffiti dataset

Juan, Luo, and Oubong Gwun. "A comparison of sift, pca-sift and surf." *International Journal of Image Processing (IJIP)* 3.4 (2009): 143-152.

Calculation of camera parameters

3D reconstruction

motion estimation

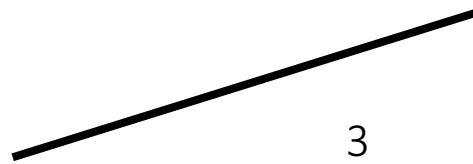
fundamental matrix

self-calibration

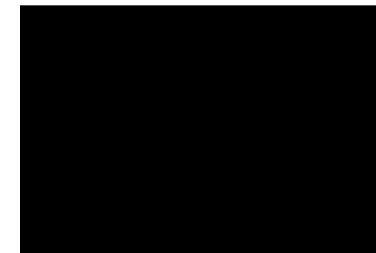
Mapping & tracking

fundamental matrix

The redundancy of feature point



3



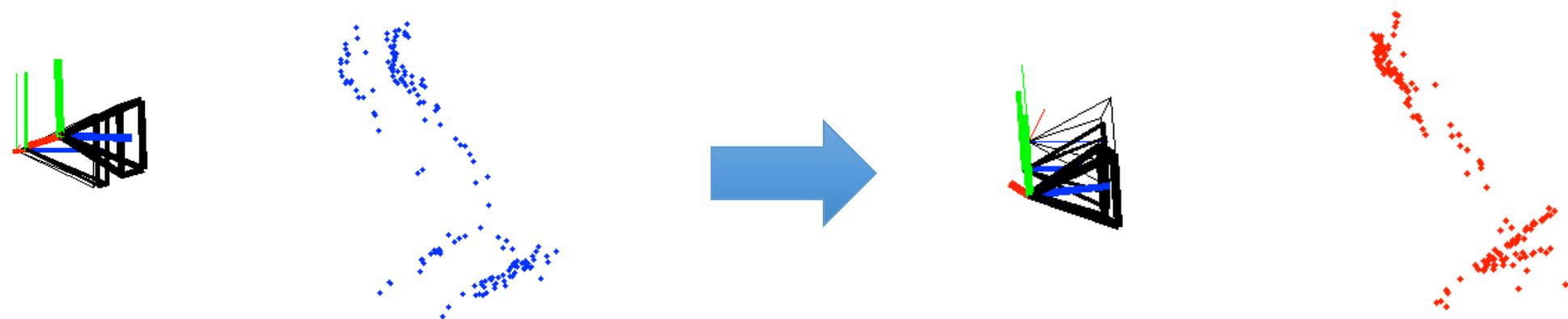
5

[1] Hartley, Richard I. "In defense of the eight-point algorithm." *IEEE Transactions on pattern analysis and machine intelligence* 19.6 (1997): 580-593.

[2] Torr, Philip HS, and David W. Murray. "The development and comparison of robust methods for estimating the fundamental matrix." *International journal of computer vision* 24.3 (1997): 271-300.

Bundle adjustment

parameter optimization iterative optimization nonlinear optimization



Triggs, Bill, et al. "Bundle adjustment—a modern synthesis." *International workshop on vision algorithms*. Springer Berlin Heidelberg, 1999.

Bundler

Noah Snavely



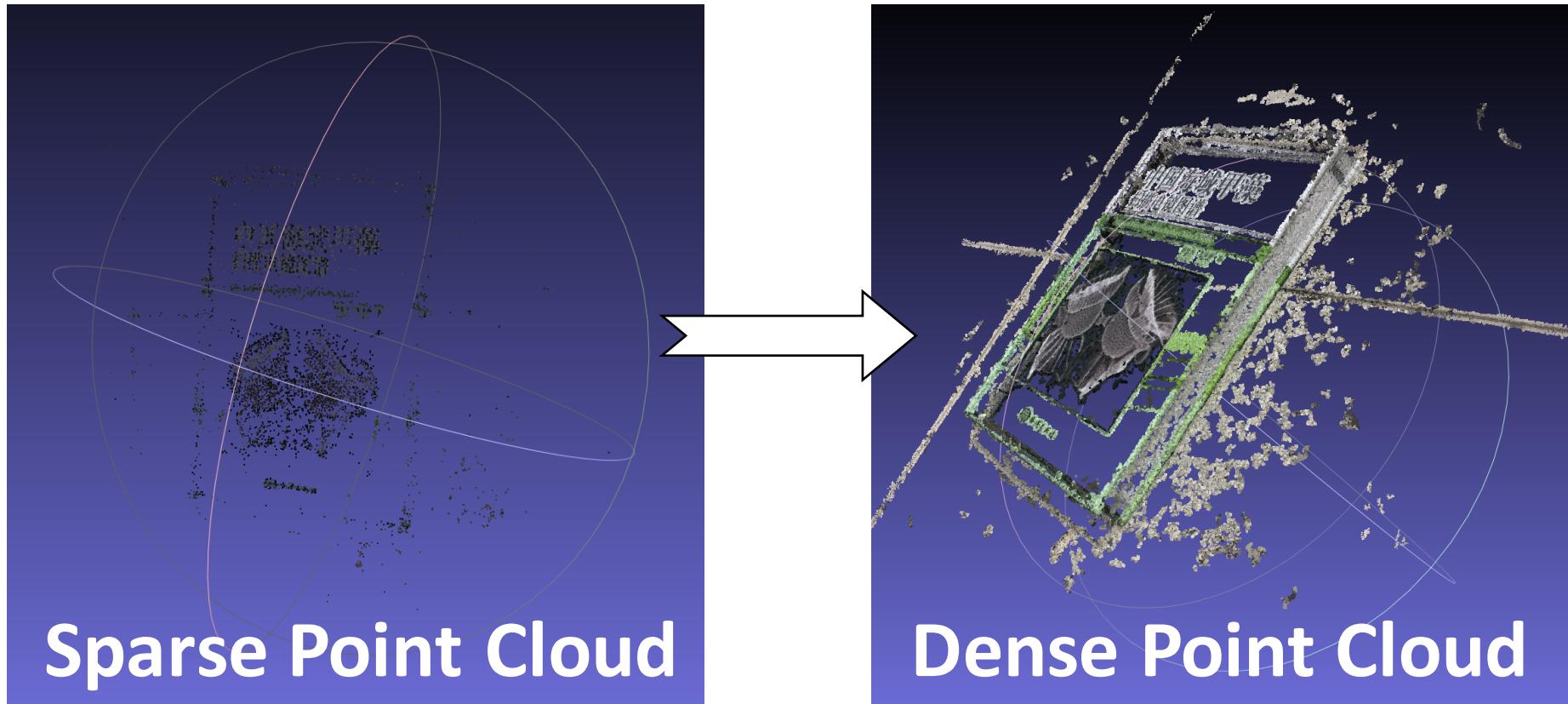
Introduction: <http://www.cs.cornell.edu/%7Esnavely/bundler>

Code: https://github.com/snavely/bundler_sfm

Bundler Noah Snavely

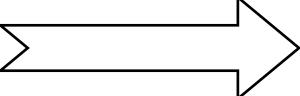
Video

Dense reconstruction



Dense reconstruction

light and shade^[1]

geometry 

surface profile^[2]

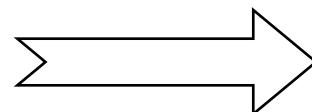
[1]Durou, Jean-Denis, Maurizio Falcone, and Manuela Sagona. "Numerical methods for shape-from-shading: A new survey with benchmarks." *Computer Vision and Image Understanding* 109.1 (2008): 22-43.

[2]Boyer, Edmond, and Jean-Sébastien Franco. "A hybrid approach for computing visual hulls of complex objects." *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*. IEEE Computer Society Press, 2003

PMVS2

Yasutaka Furukawa& Jean Ponce

Sparse point clouds
Camera parameters



Dense point clouds

Introduction & code: <http://www.di.ens.fr/pmv>

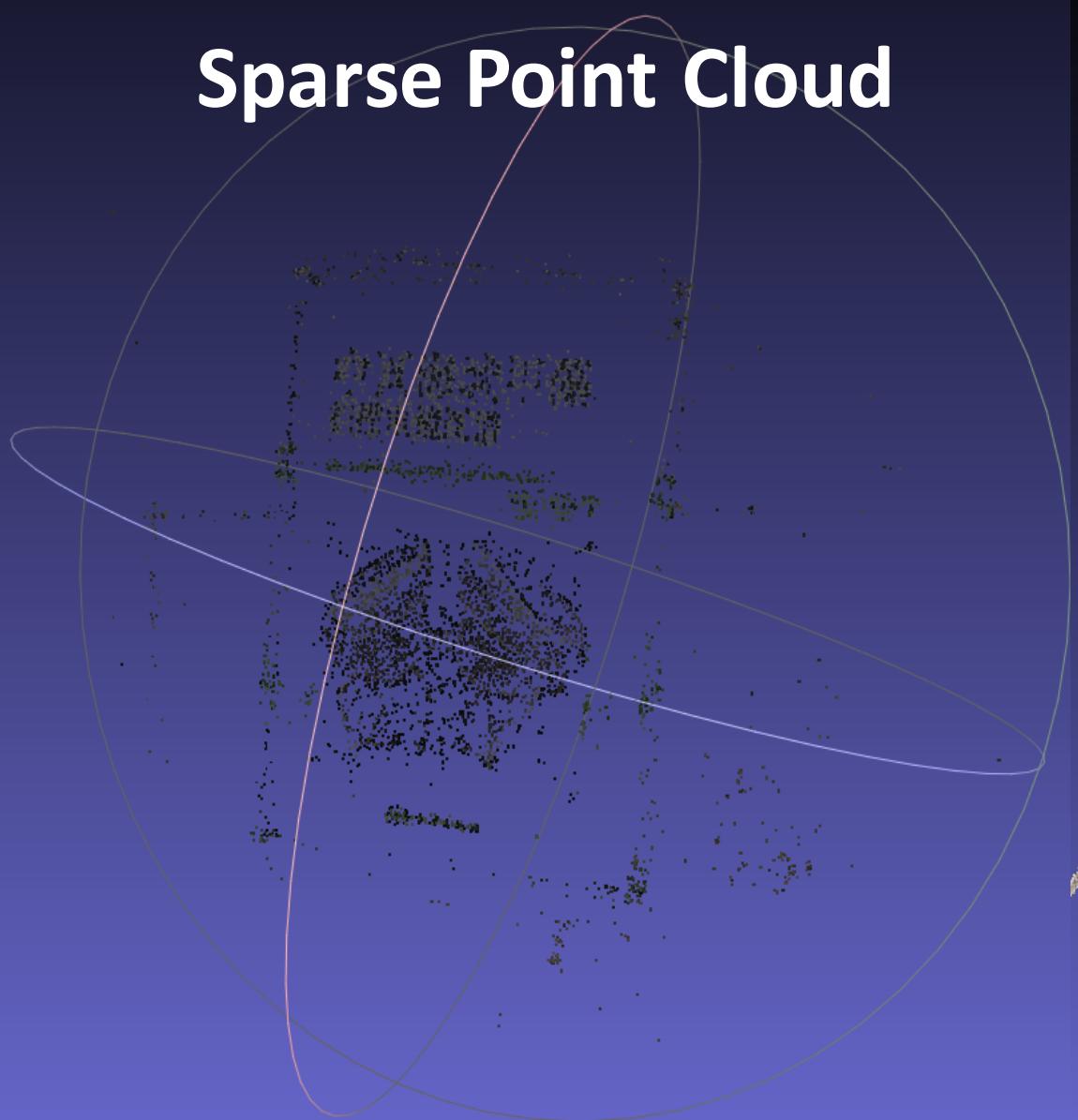
vision@ouc

Open source software 3D reconstruction processing tool

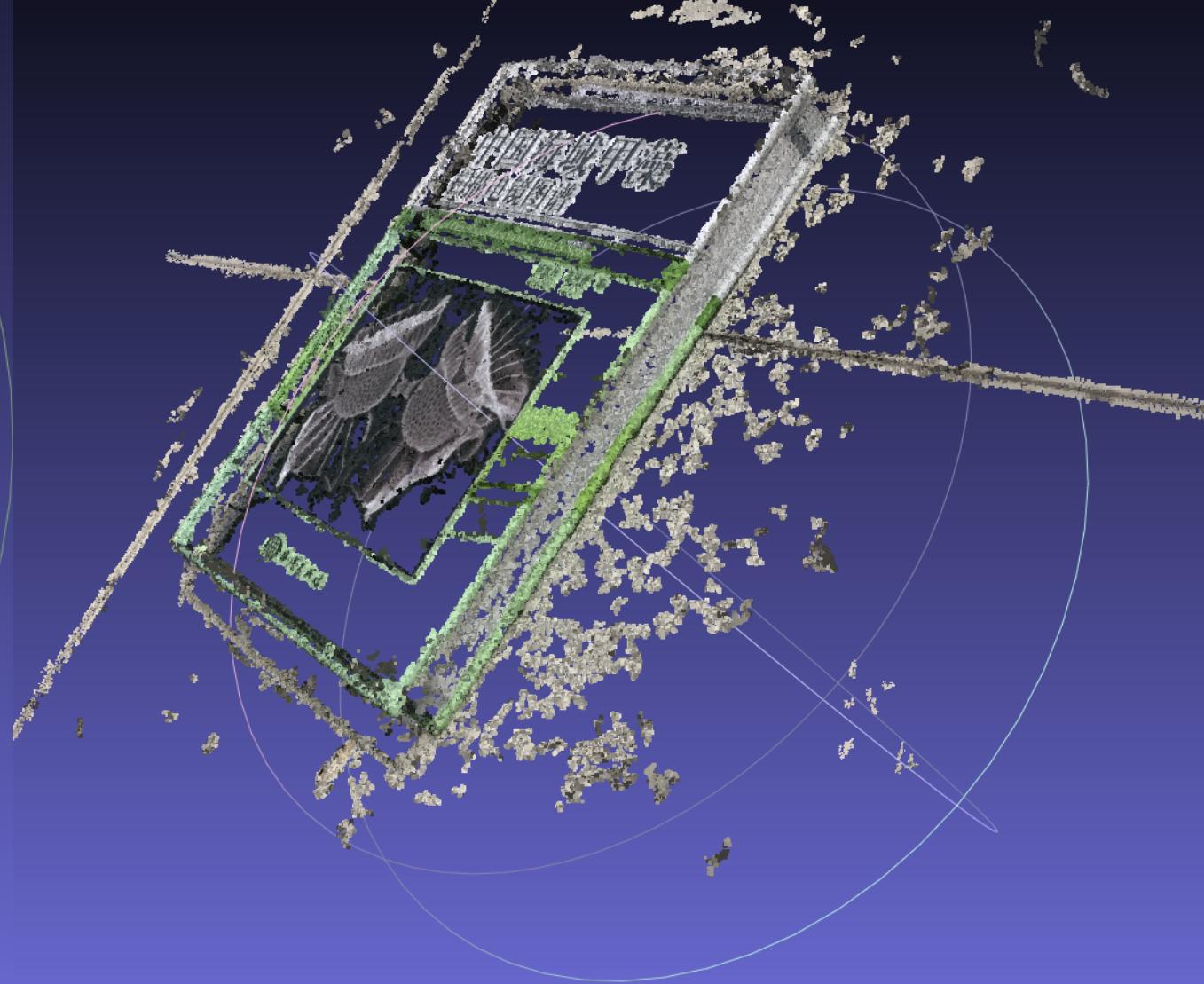
<http://www.meshlab.net>

vision@ouc

Sparse Point Cloud

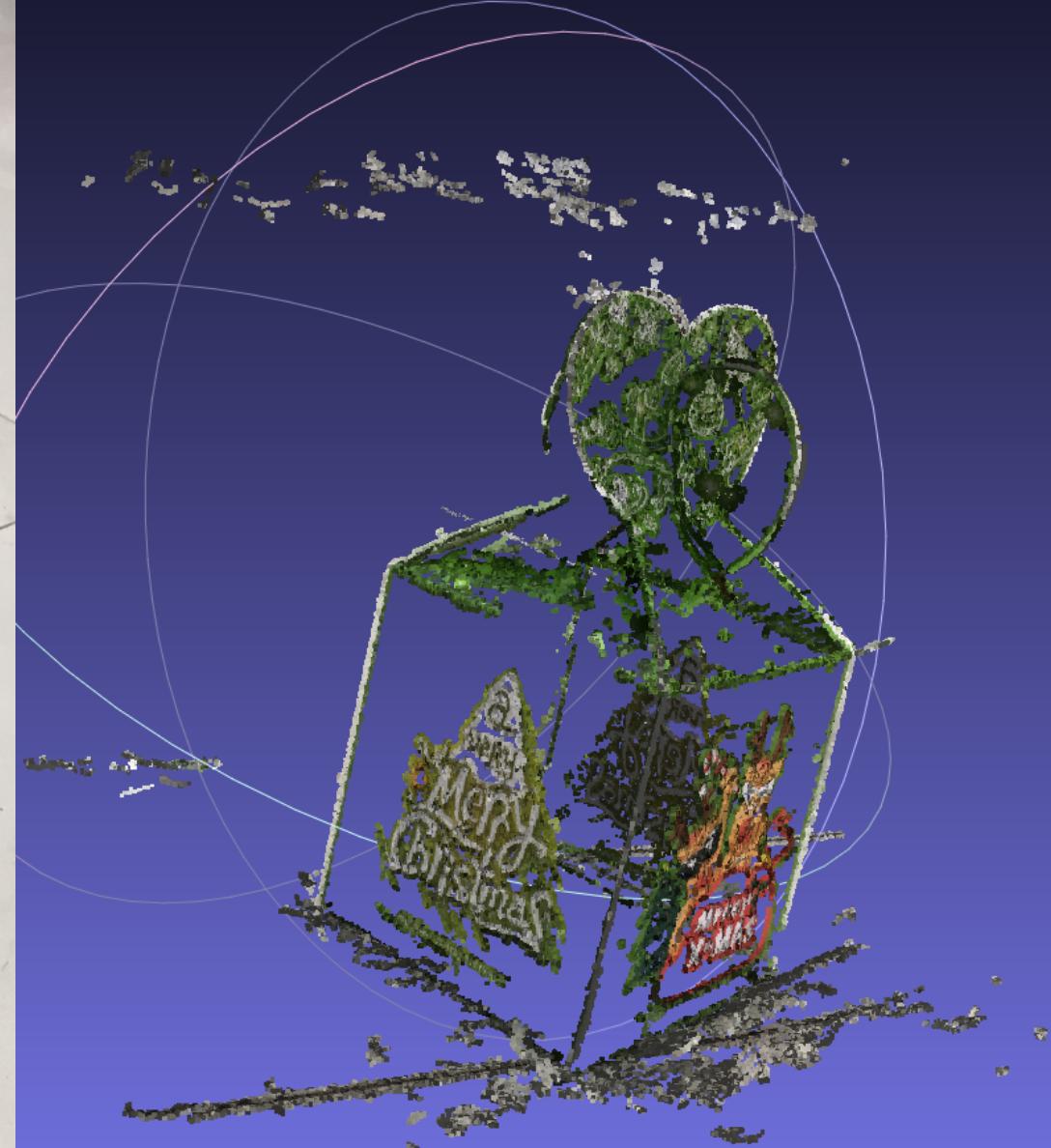


Dense Point Cloud





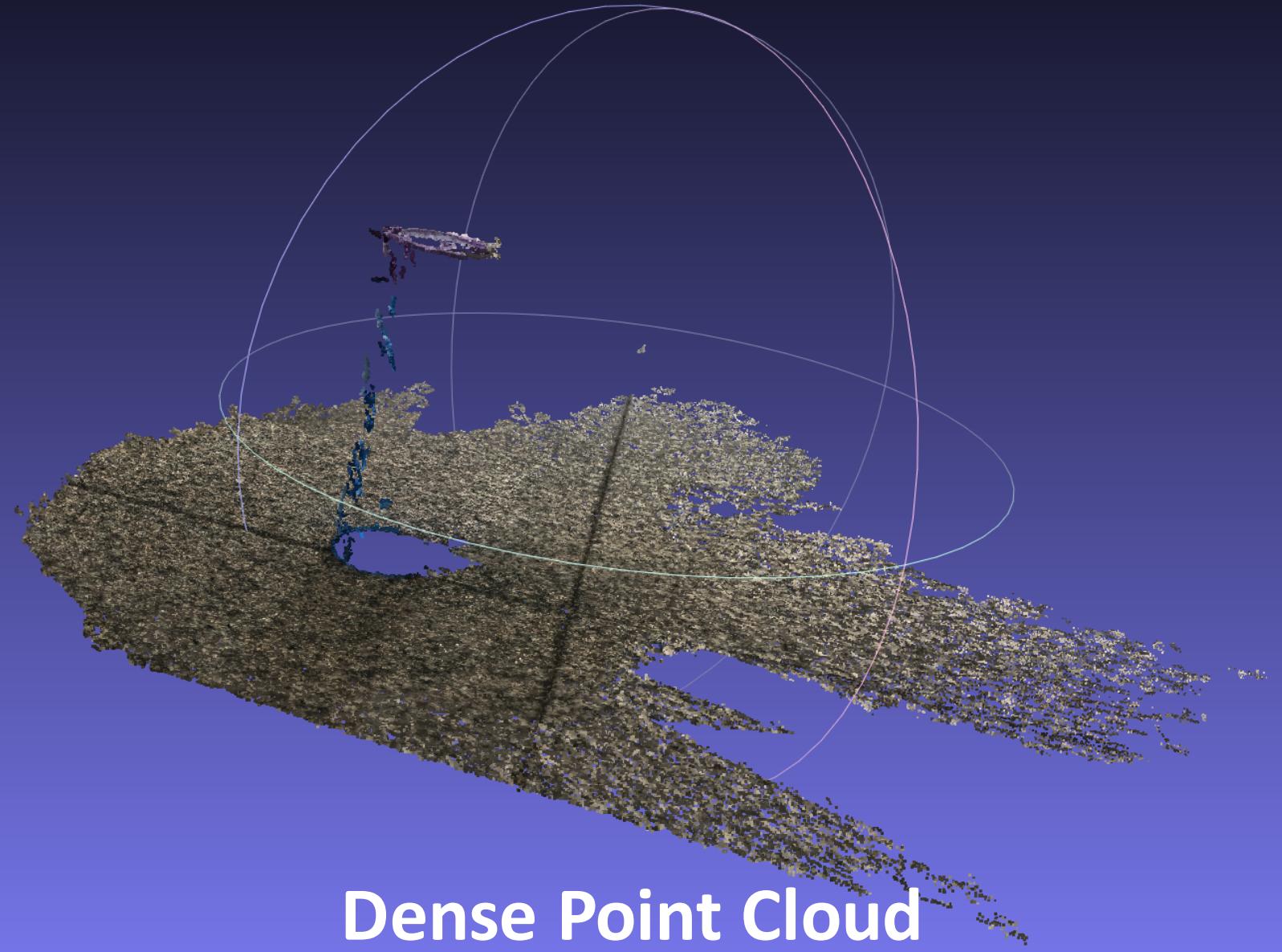
RGB



Dense Point Cloud

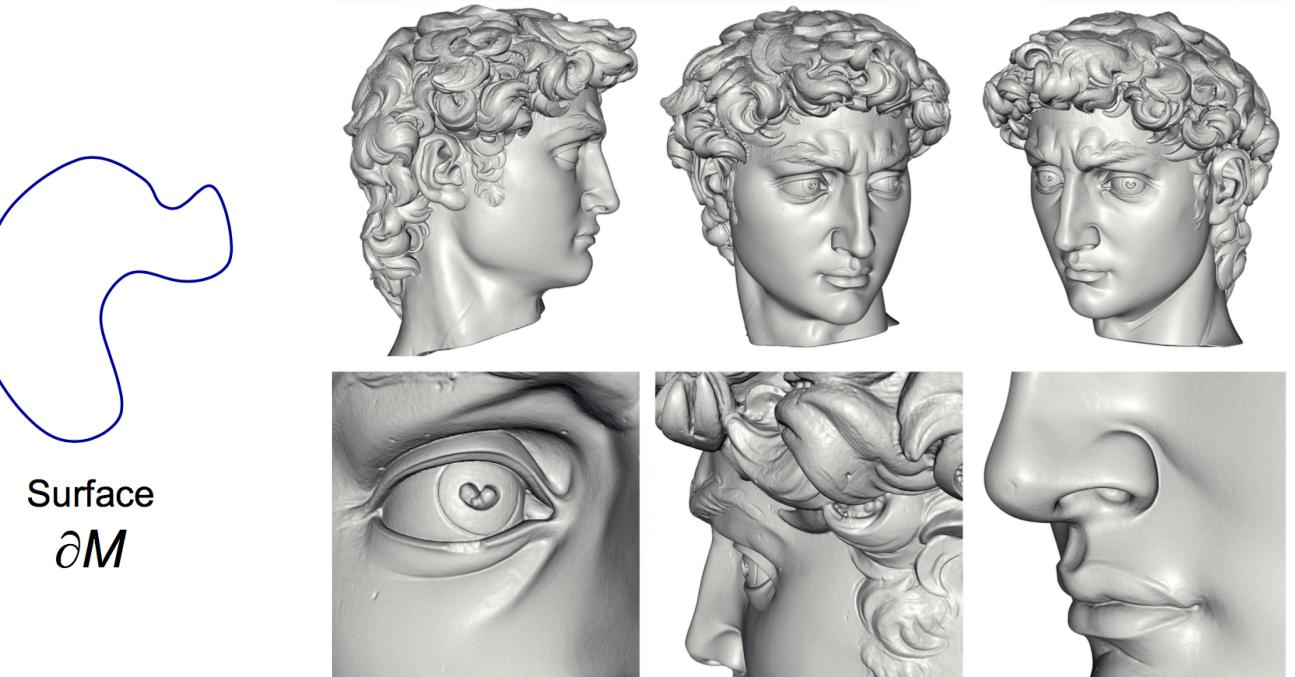
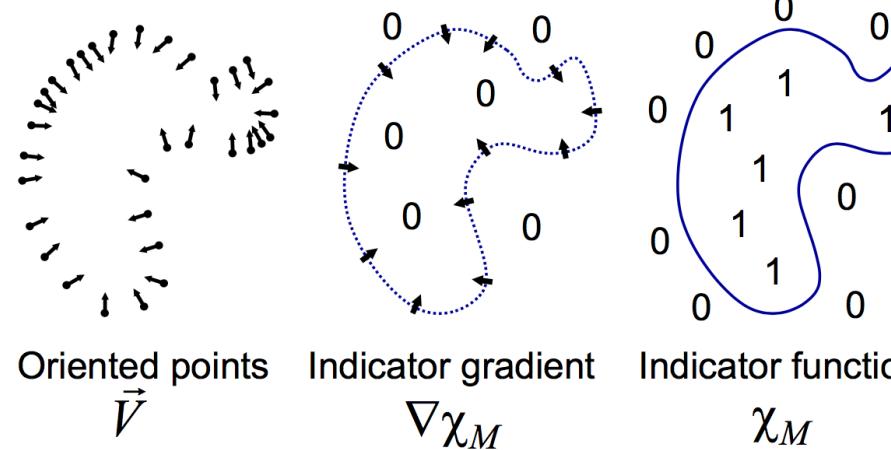


RGB



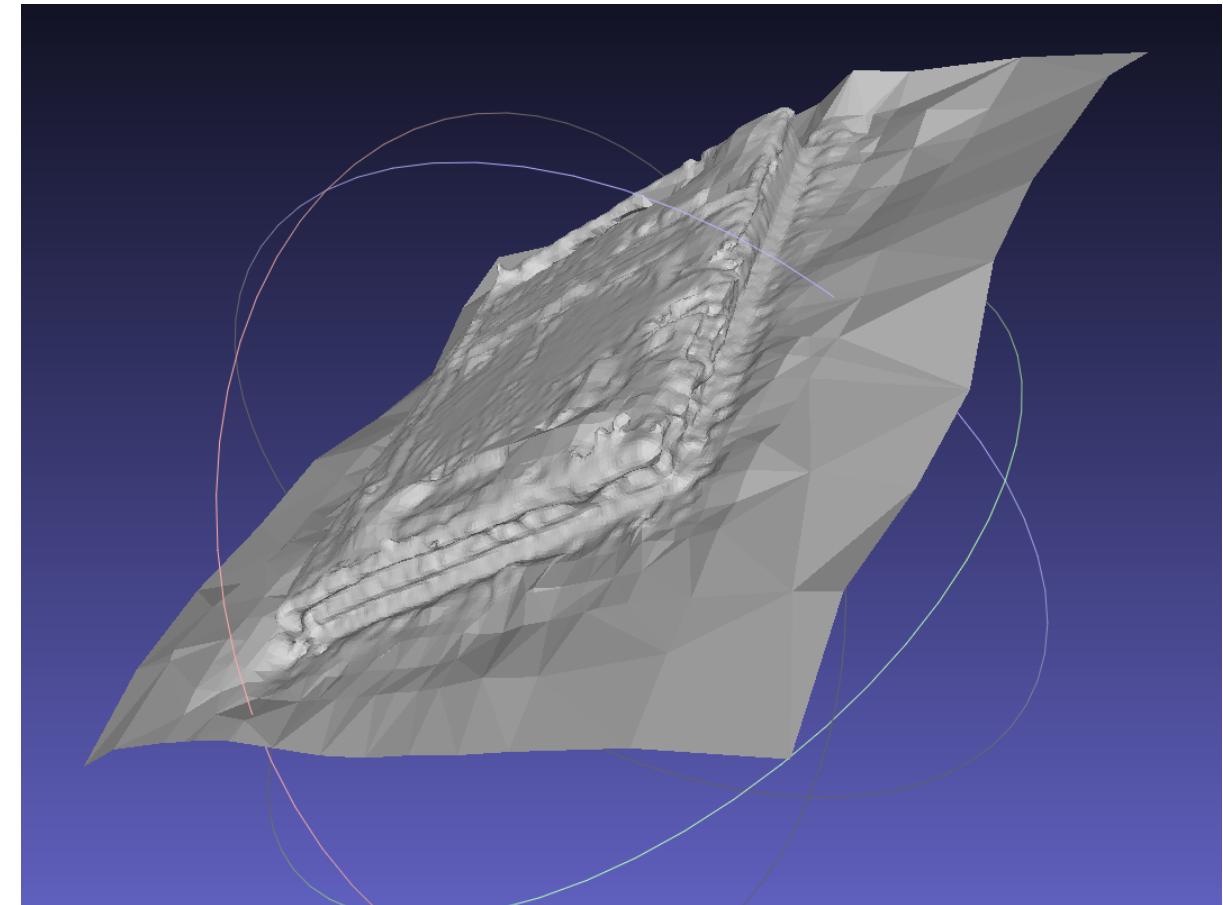
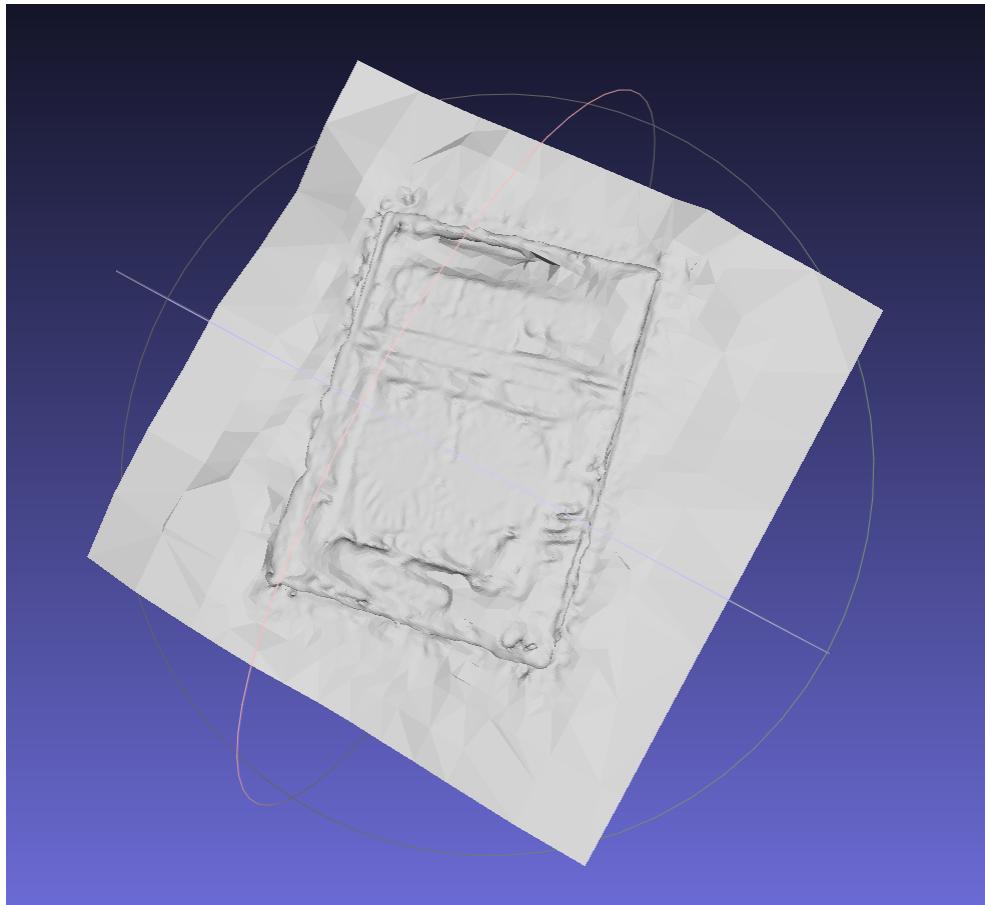
Dense Point Cloud

Poisson Surface Reconstruction

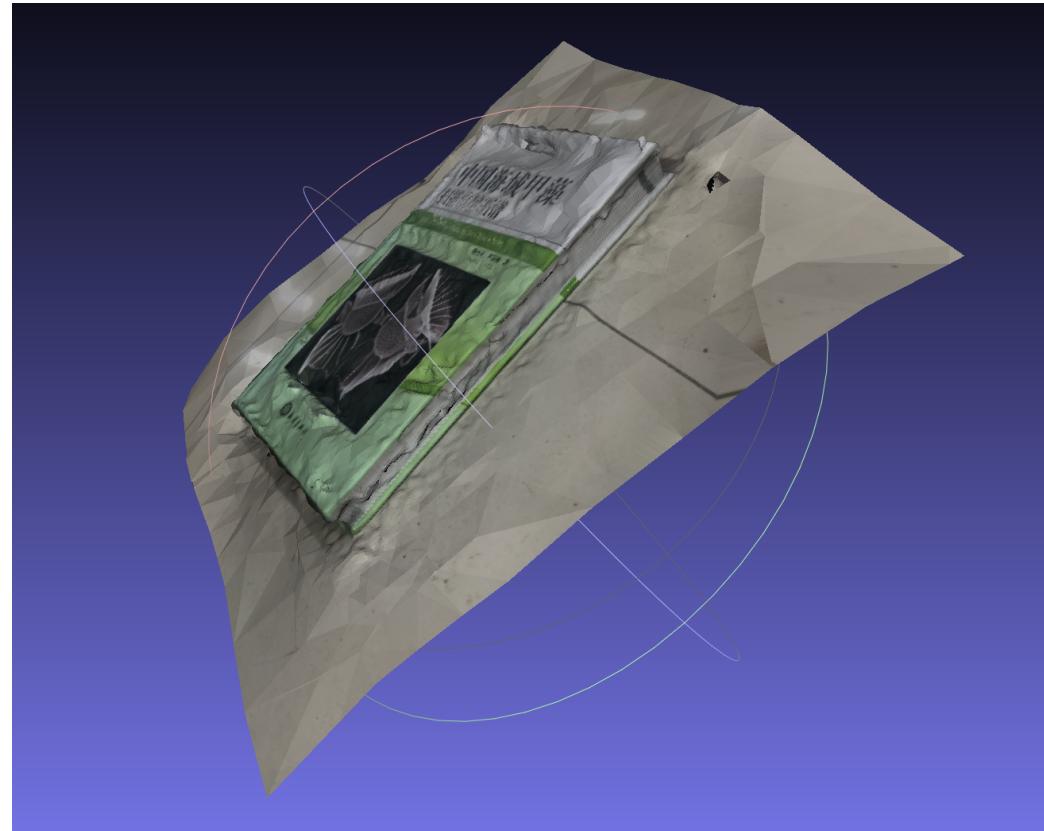
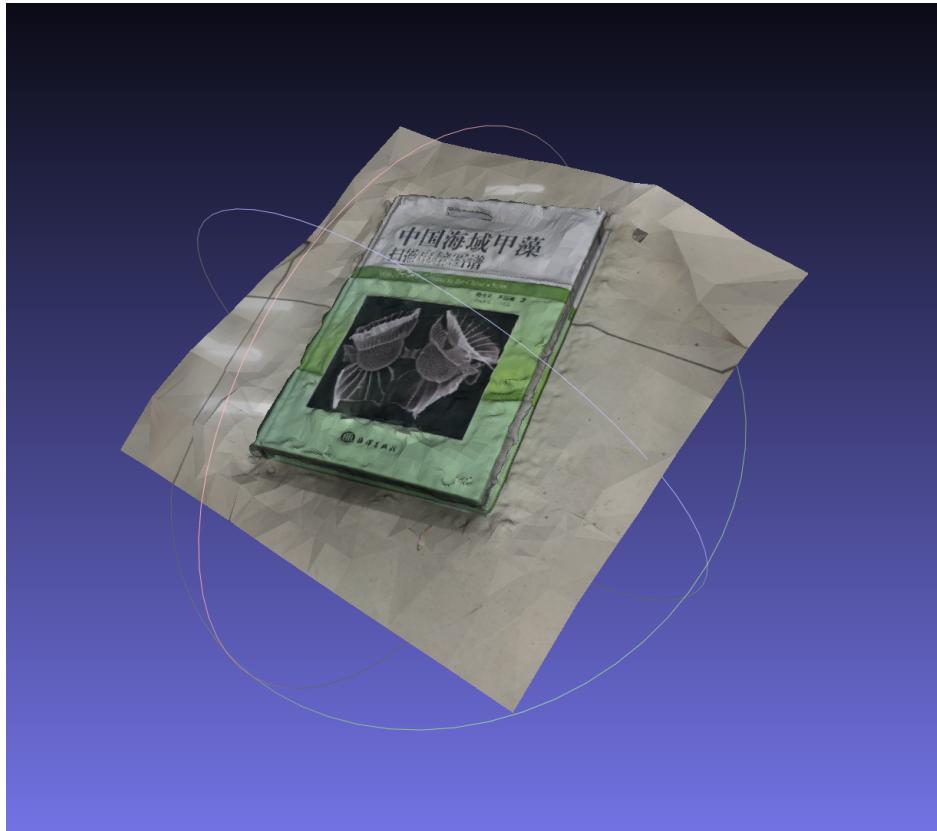


Kazhdan M, Hoppe H. Screened poisson surface reconstruction[J]. ACM Transactions on Graphics (TOG), 2013, 32(3): 29.

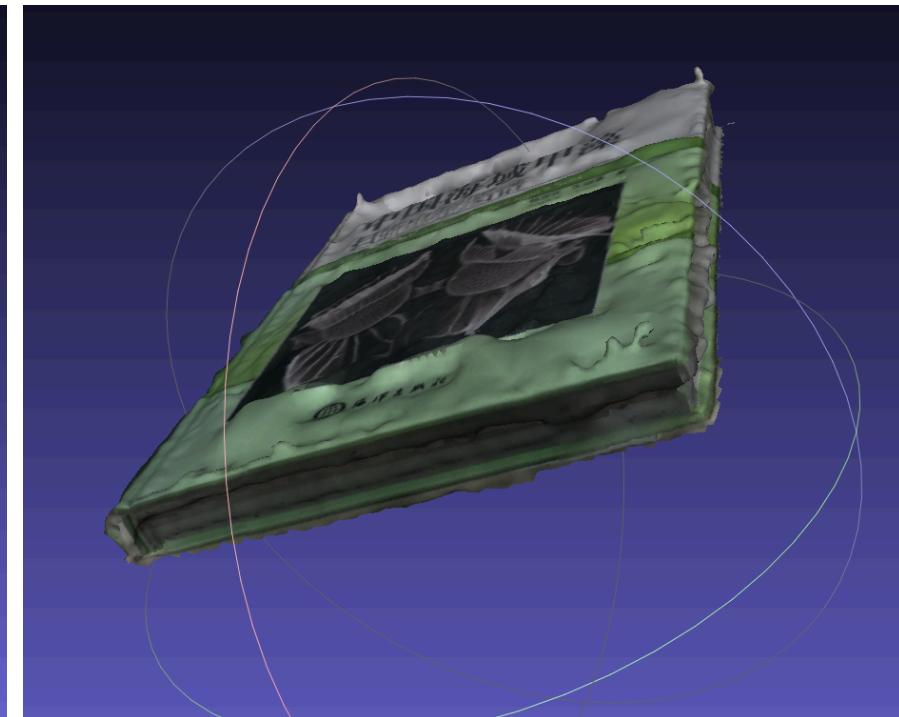
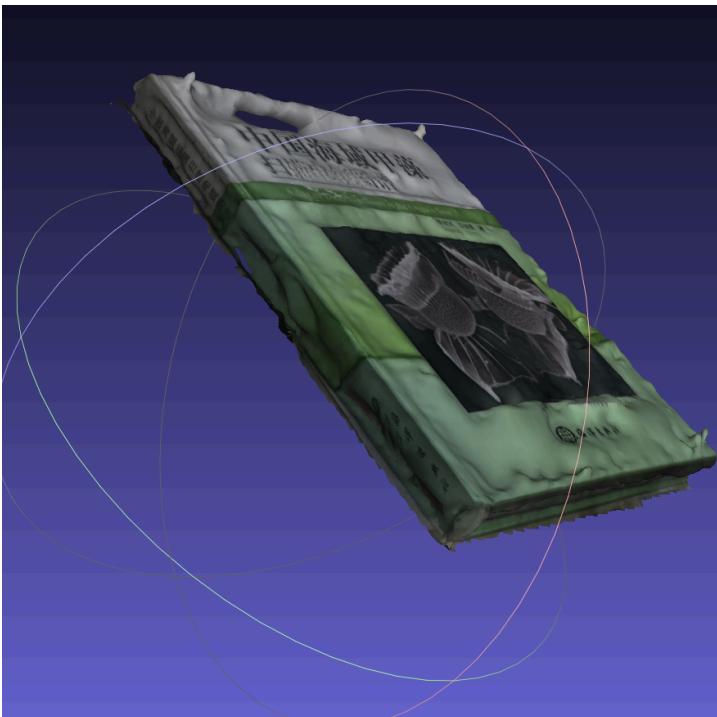
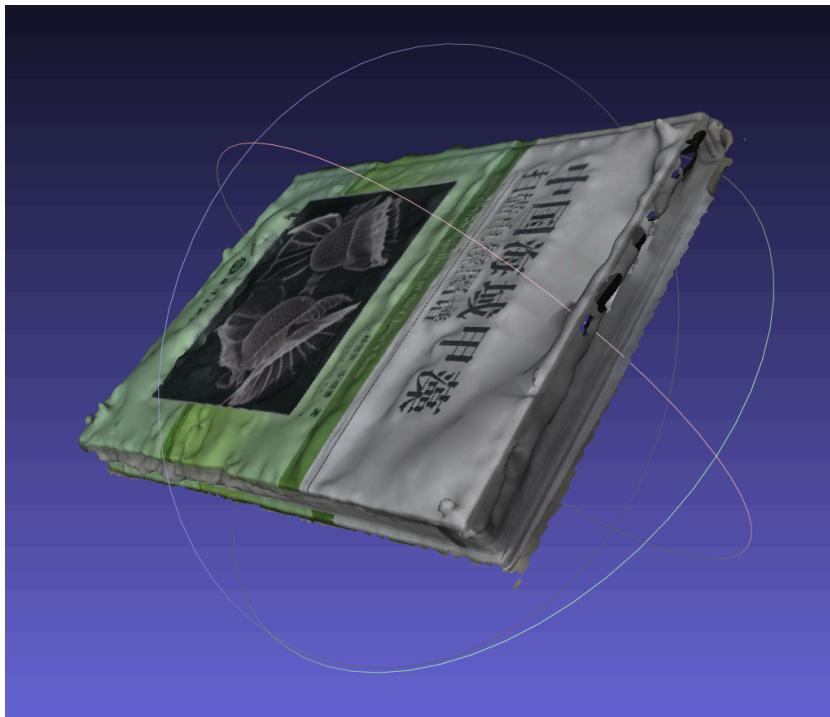
Result

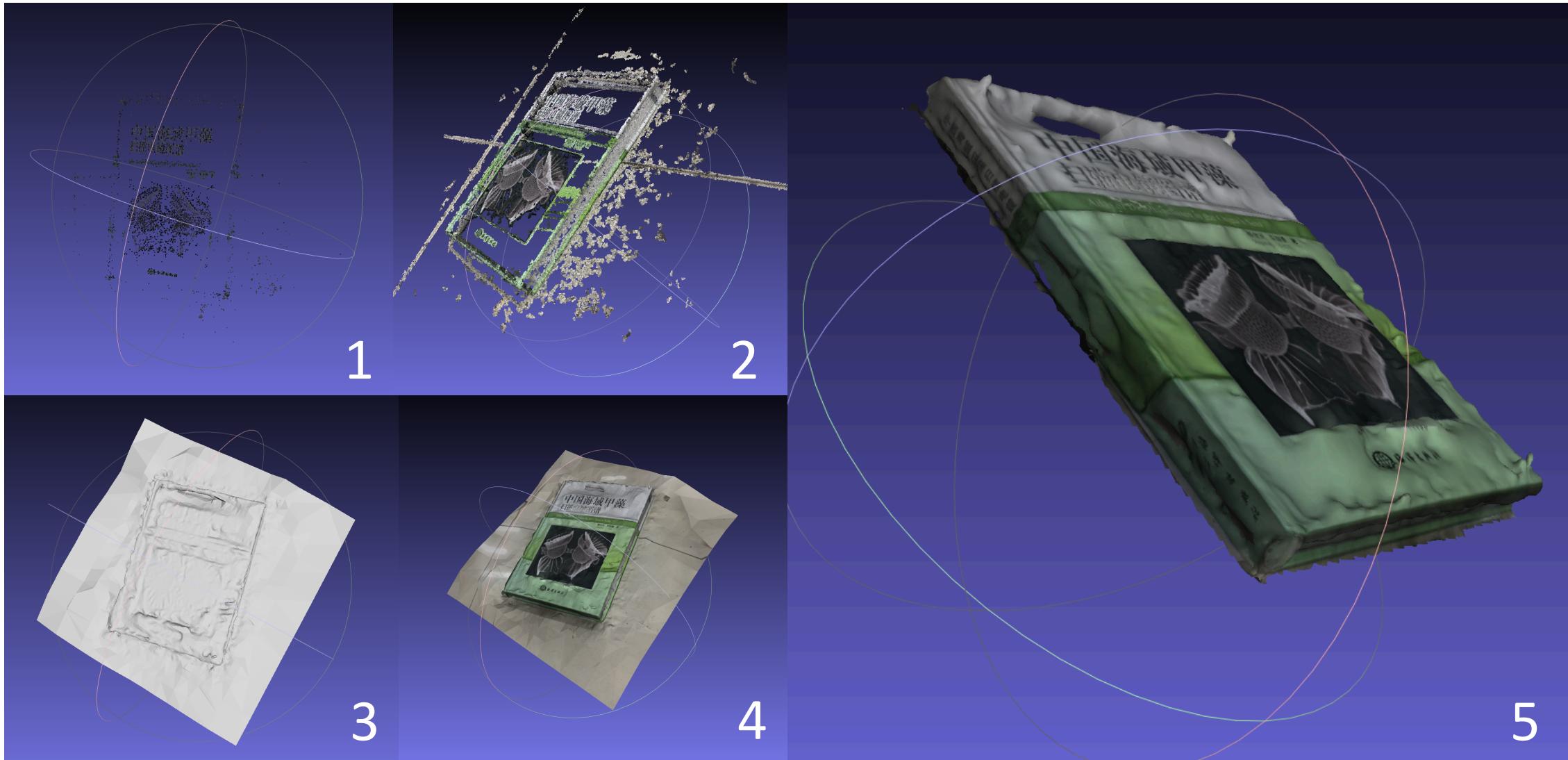


Texture mapping

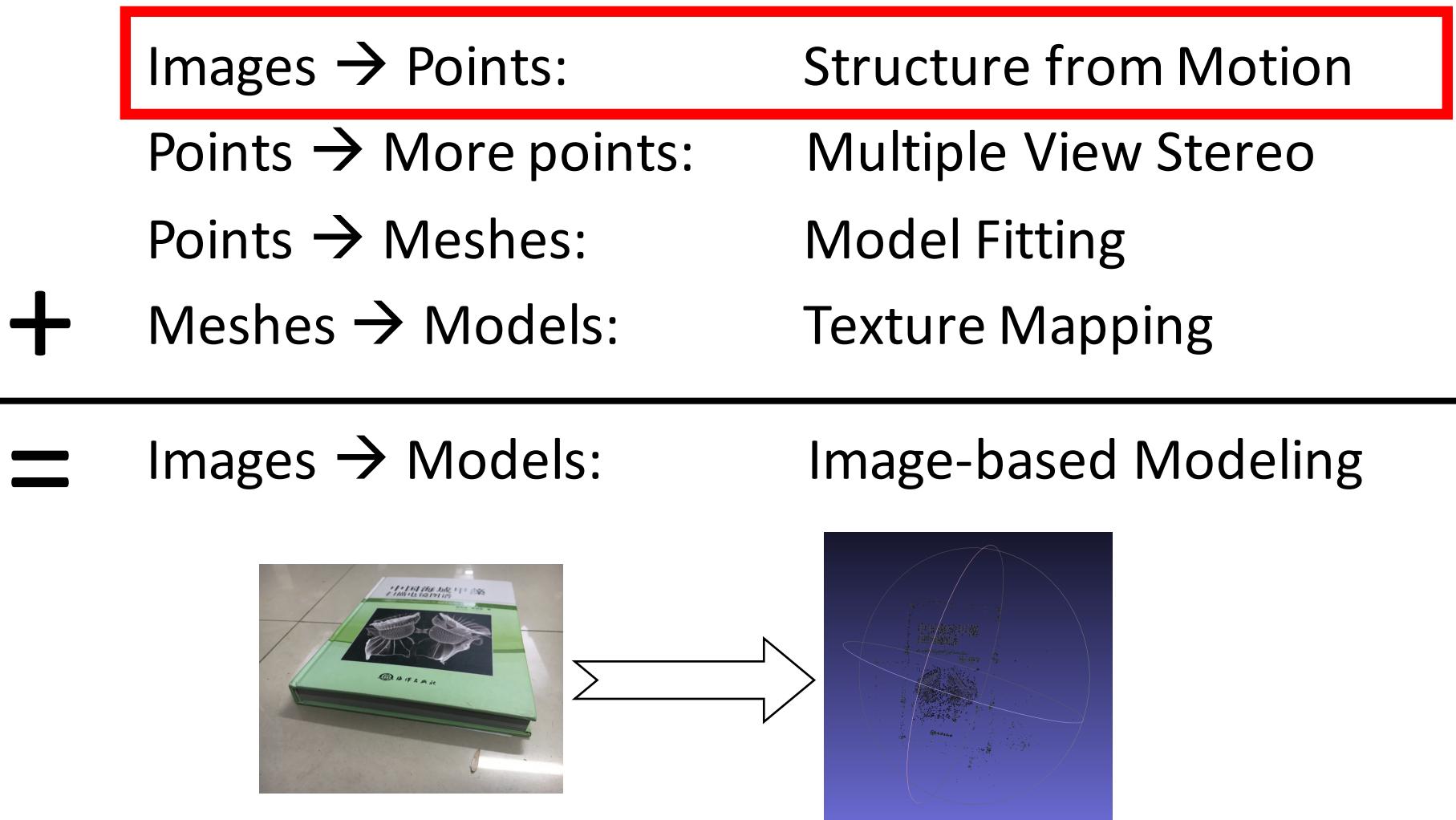


Final result





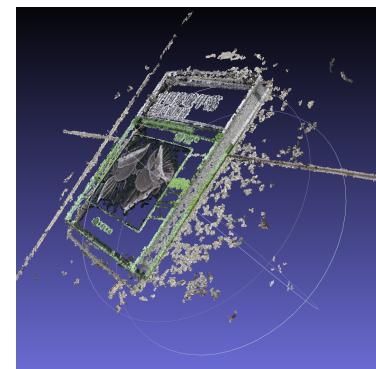
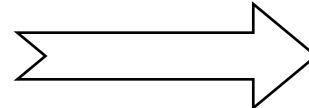
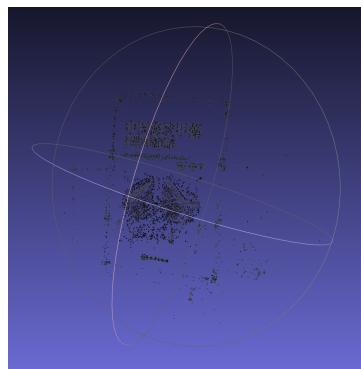
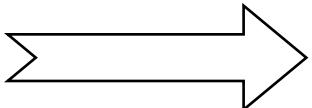
Steps



Steps

Images → Points:	Structure from Motion
Points → More points:	Multiple View Stereo
Points → Meshes:	Model Fitting
+ Meshes → Models:	Texture Mapping

= Images → Models: Image-based Modeling



Steps

Images → Points:

Structure from Motion

Points → More points:

Multiple View Stereo

Points → Meshes:

Model Fitting

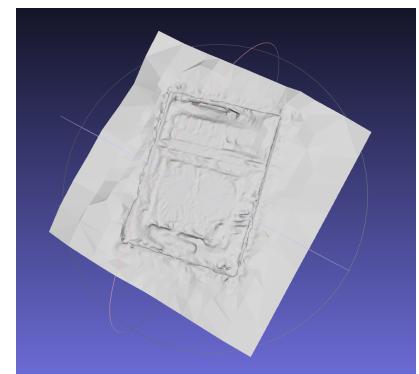
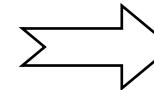
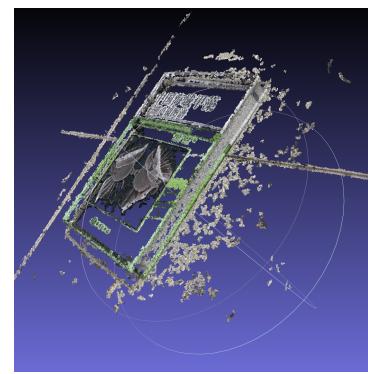
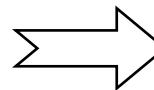
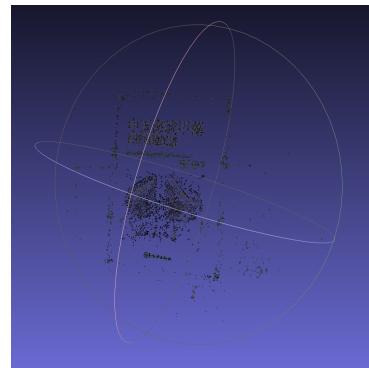
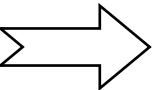
Meshes → Models:

Texture Mapping

2

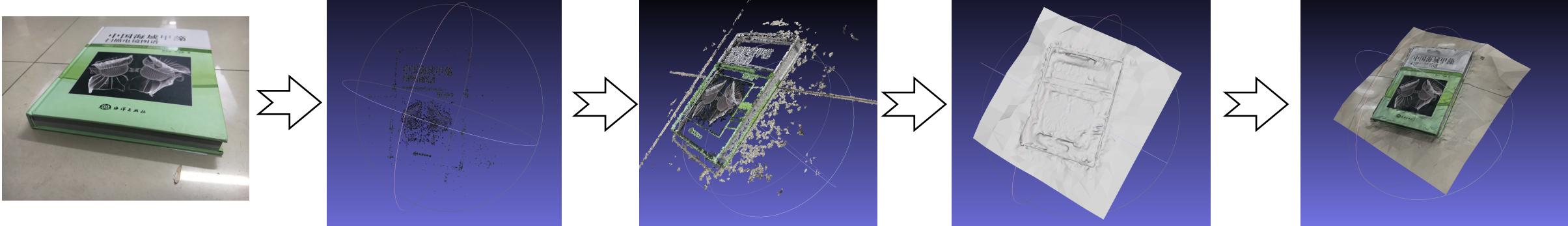
Images → Models:

Image-based Modeling



Steps

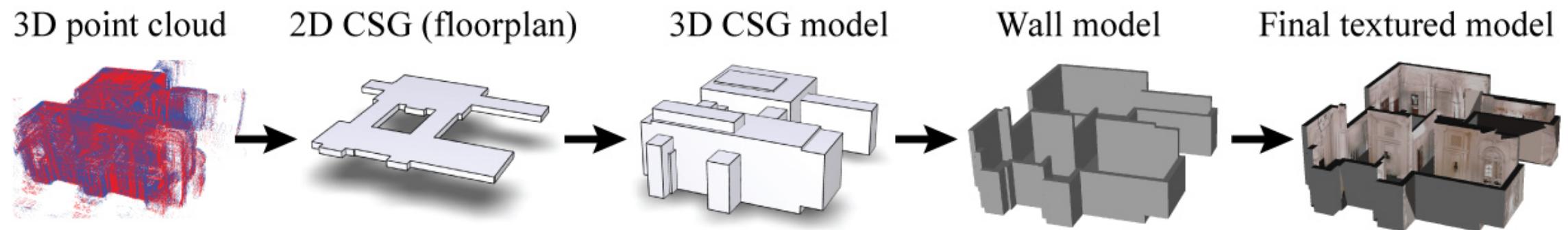
Images → Points:	Structure from Motion
Points → More points:	Multiple View Stereo
Points → Meshes:	Model Fitting
+ Meshes → Models:	Texture Mapping
<hr/>	<hr/>
= Images → Models:	Image-based Modeling



Other tools

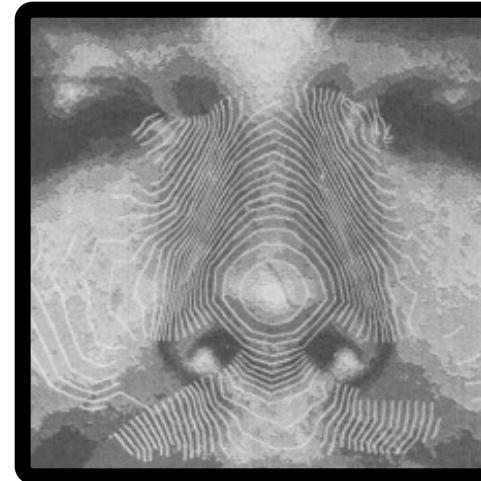
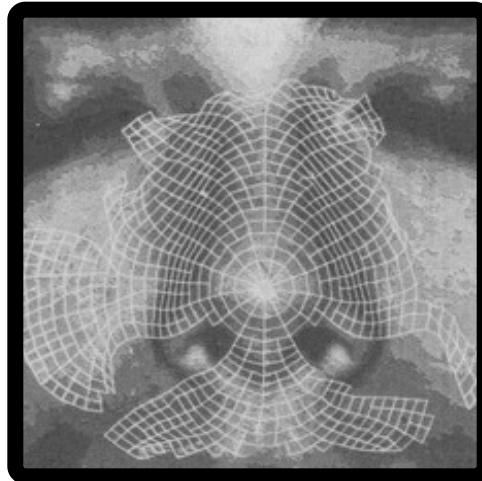
- Surface Reconstruction
 - Marching Cubes: http://en.wikipedia.org/wiki/Marching_cubes
 - Poisson Surface Reconstruction <http://research.microsoft.com/en-us/um/people/hoppe/proj/poissonrecon/>
- Model Fitting
 - RANSAC & J-linkage <http://www.diegm.uniud.it/fusiello/demo/jlk/>
 - InverseCSG
 - GlobFit <http://code.google.com/p/globfit/>
 - Face Model Fitting <http://research.microsoft.com/apps/pubs/default.aspx?id=73211>

Application



Other methods

Shape from Shading

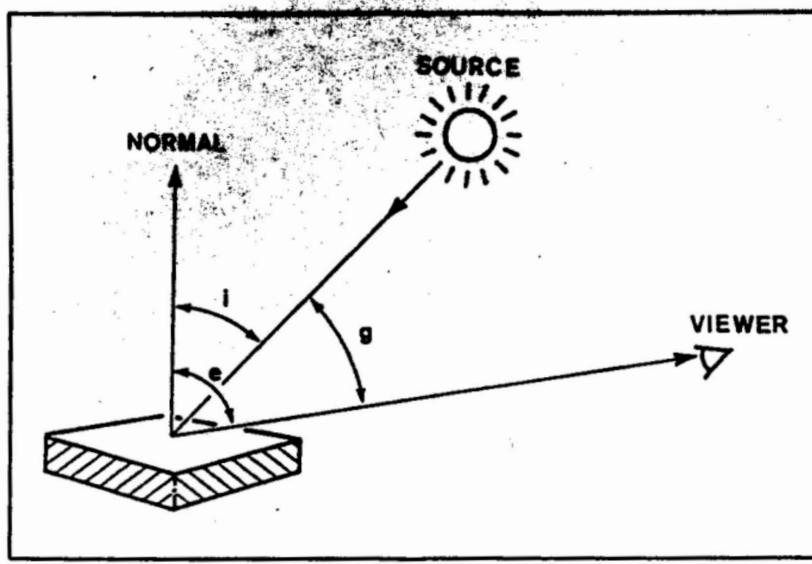


1. Bronte model
2. Infinite point
3. Rectangular projection

Horn, Berthold KP. "Shape from shading: A method for obtaining the shape of a smooth opaque object from one view." (1970).

Other methods

Photometric Stereo

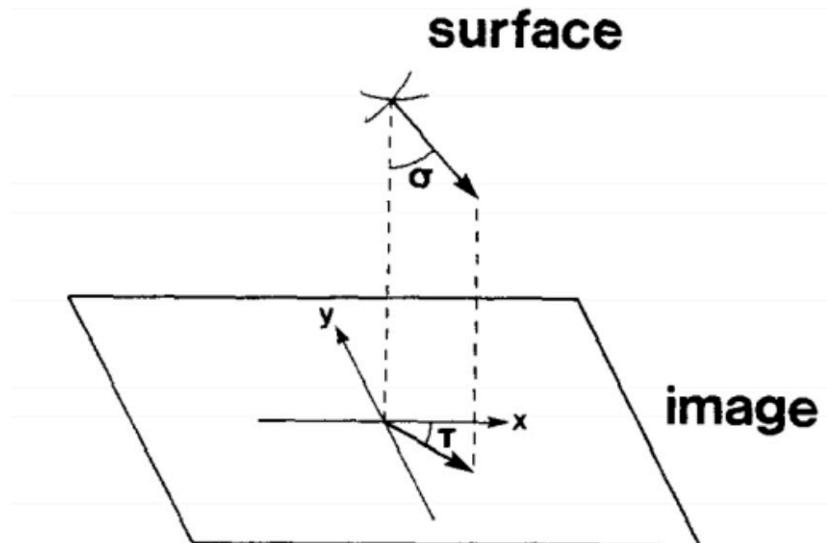


Nonlinearity and Noise Reduction 2003;
Gradient Control Point 2004;
Credibility Passed with Markov Random Field 2005;
Three - dimensional reconstruction of light conditions
under unknown conditions in 2007;
Non - Lambert 2007;
Reconstruction of colored light in 2007;

Woodham, Robert J. "Photometric method for determining surface orientation from multiple images." *Optical engineering* 19.1 (1980): 191139-191139.

Other methods

Shape from Texture

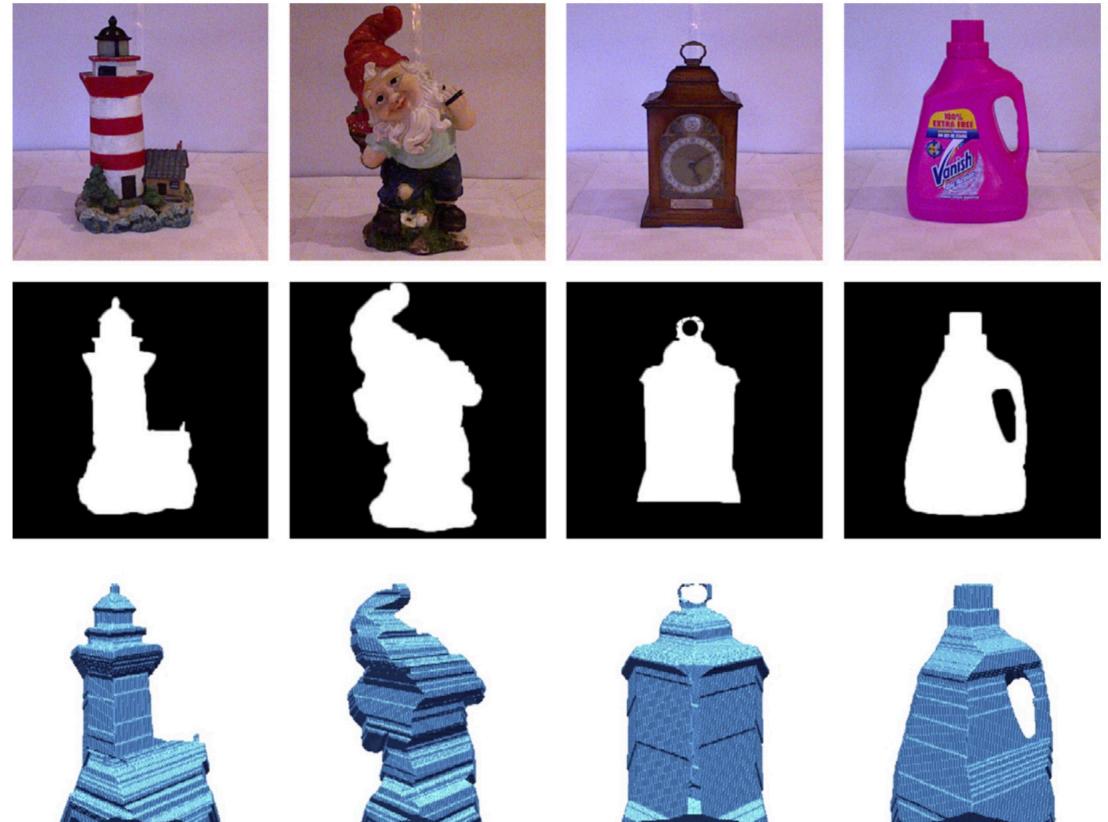


Witkin, Andrew P. "Recovering surface shape and orientation from texture." *Artificial intelligence* 17.1-3 (1981): 17-45.

Other methods

Shape from Silhouettes

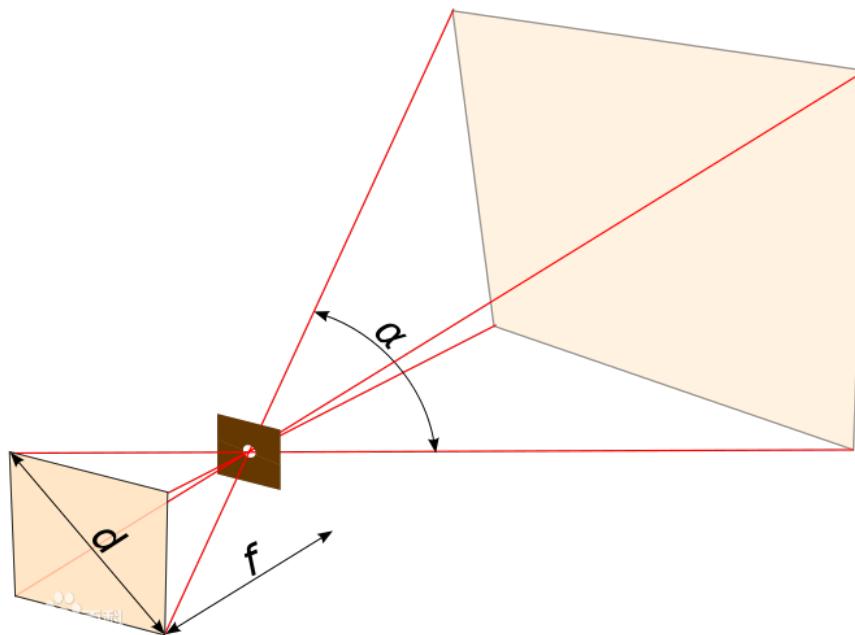
Divide the three-dimensional space into voxels



Martin, Worthy N., and Jagdishkumar Keshoram Aggarwal. "Volumetric descriptions of objects from multiple views." *IEEE transactions on pattern analysis and machine intelligence* 2 (1983): 150-158.

Other methods

Shape from Focus

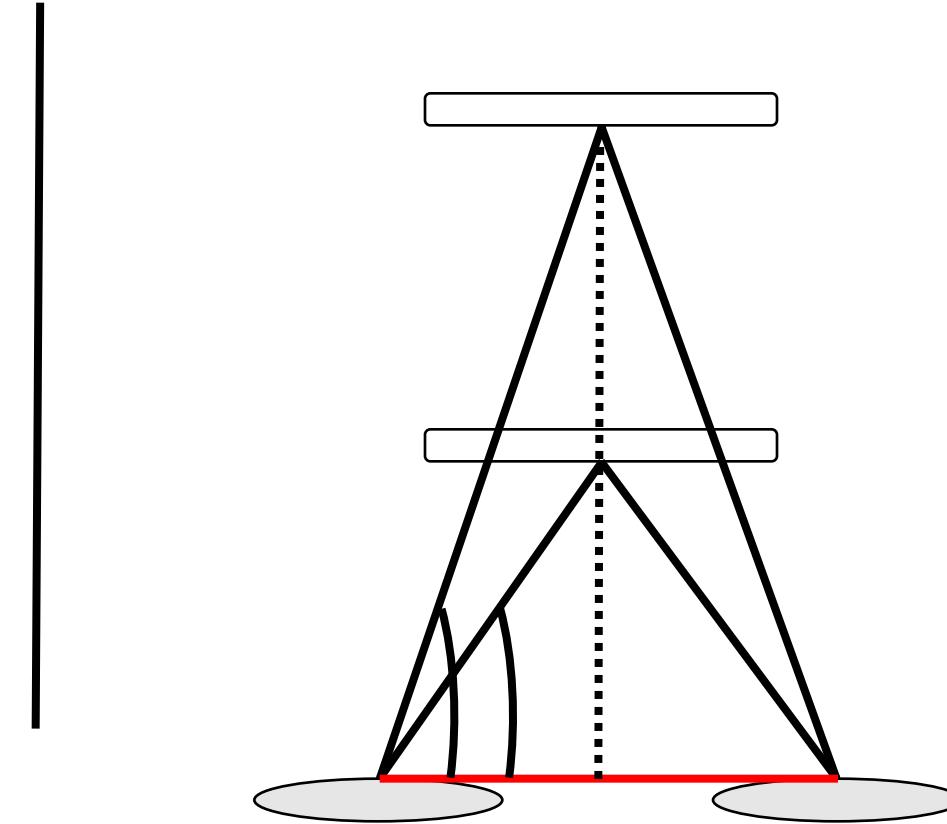


Rajagopalan, A. N., and Subhasis Chaudhuri. "Optimal selection of camera parameters for recovery of depth from defocused images." *Computer Vision and Pattern Recognition, 1997. Proceedings., 1997 IEEE Computer Society Conference on.* IEEE, 1997.

Binocular vision

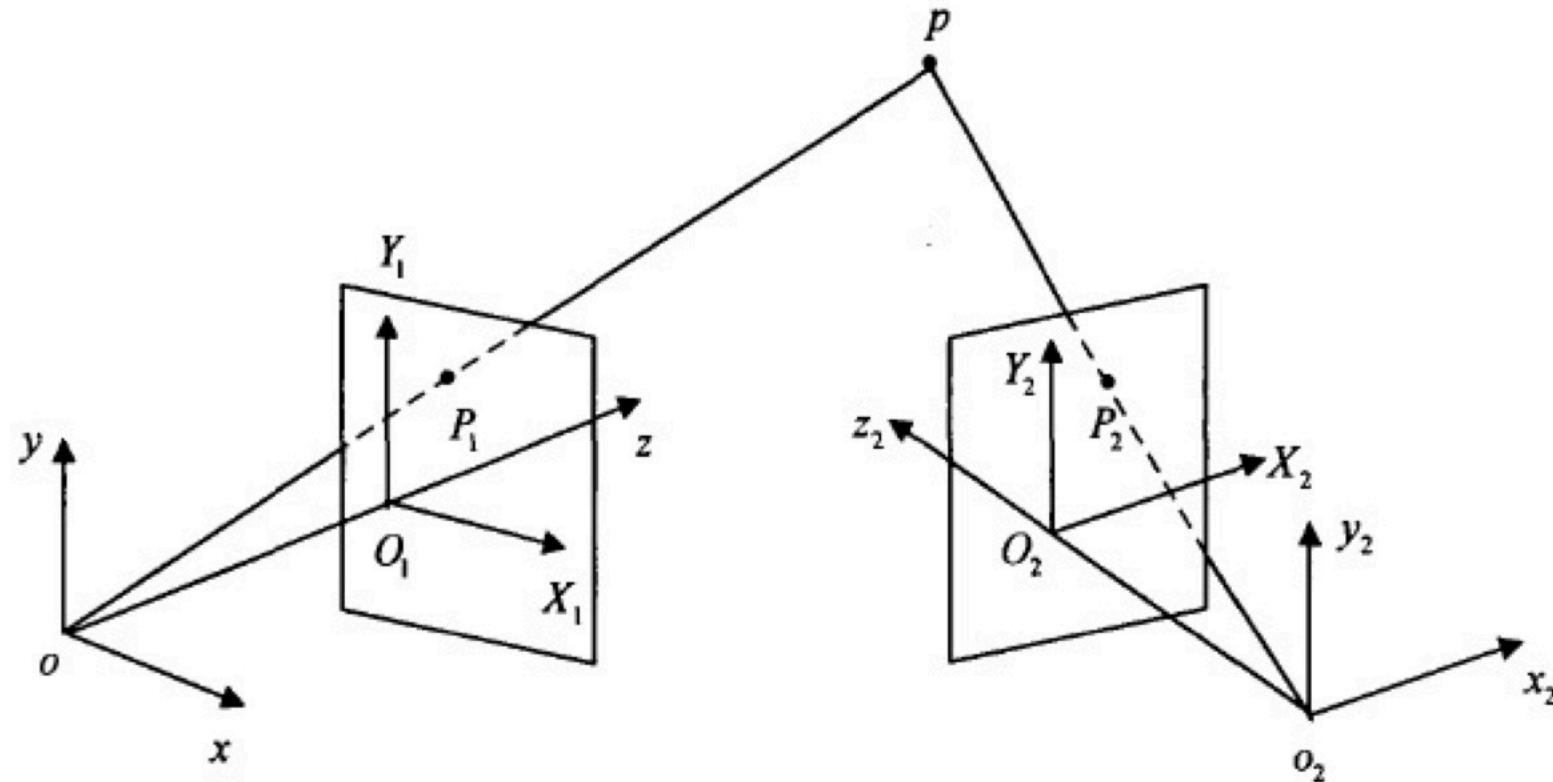


How to work ?

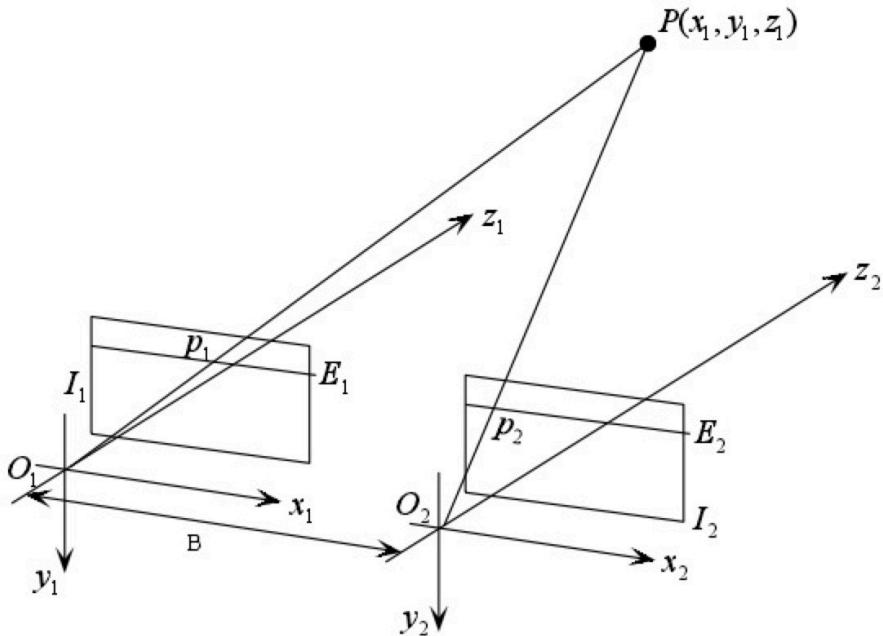


GAME

Binocular vision



Parallel binocular stereo vision model



$$Z = \frac{Bf}{x_1 - x_2}$$

Steps

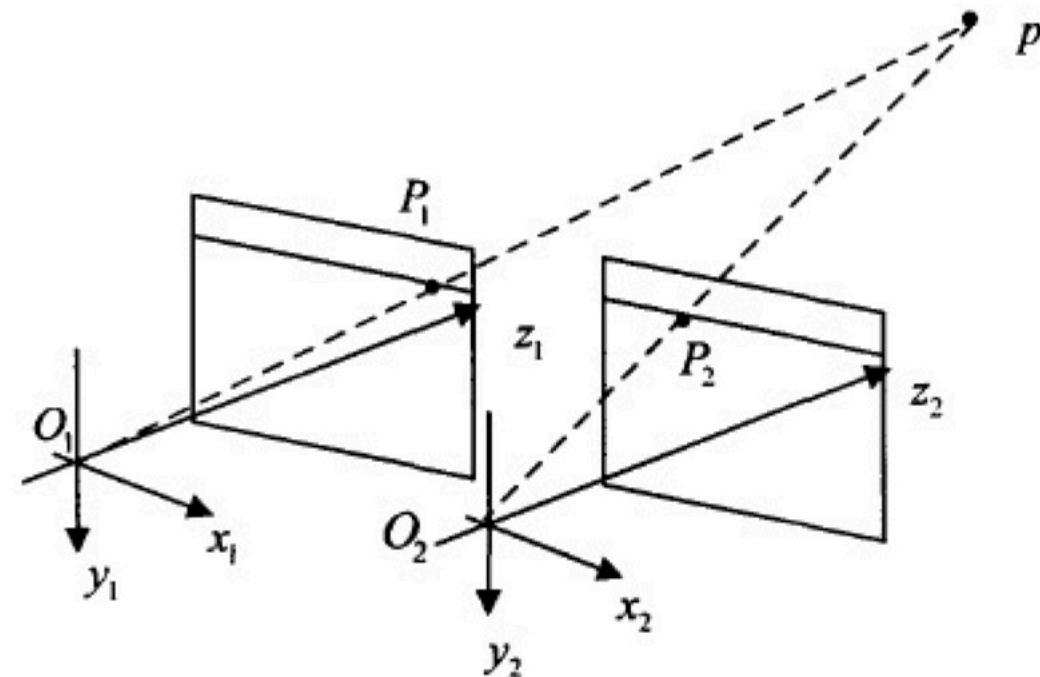
Calibration

Acquisition

Pretreatment

Stereo matching

Recovering



Acquisition & Calibration



Traditional object-based calibration^[1]

Self-calibration^{[2][3]}

[1]O. Faugeras. "Three-Dimensional Computer Vision: A Geometric Viewpoint ". MIT Press, 1993.

[2]Hartley, Richard I. "An algorithm for self calibration from several views." *Cvpr*. Vol. 94. 1994.

[3] Luong, Q-T. "Self-calibration of a moving camera from point correspondences and fundamental matrices."

International Journal of computer vision 22.3 (1997): 261-289.

Pretreatment

Image enhancement

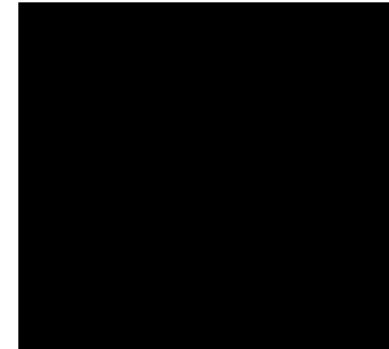
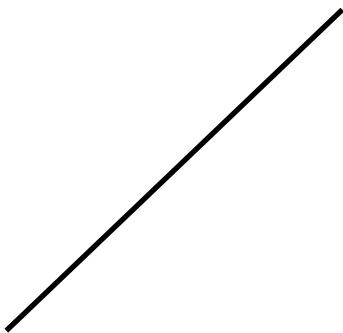
Geometric correction

Smoothing filtering

Image restoration

Stereo matching

element



Gray matching

Feature matching

Phase matching

Constraint condition

uniqueness



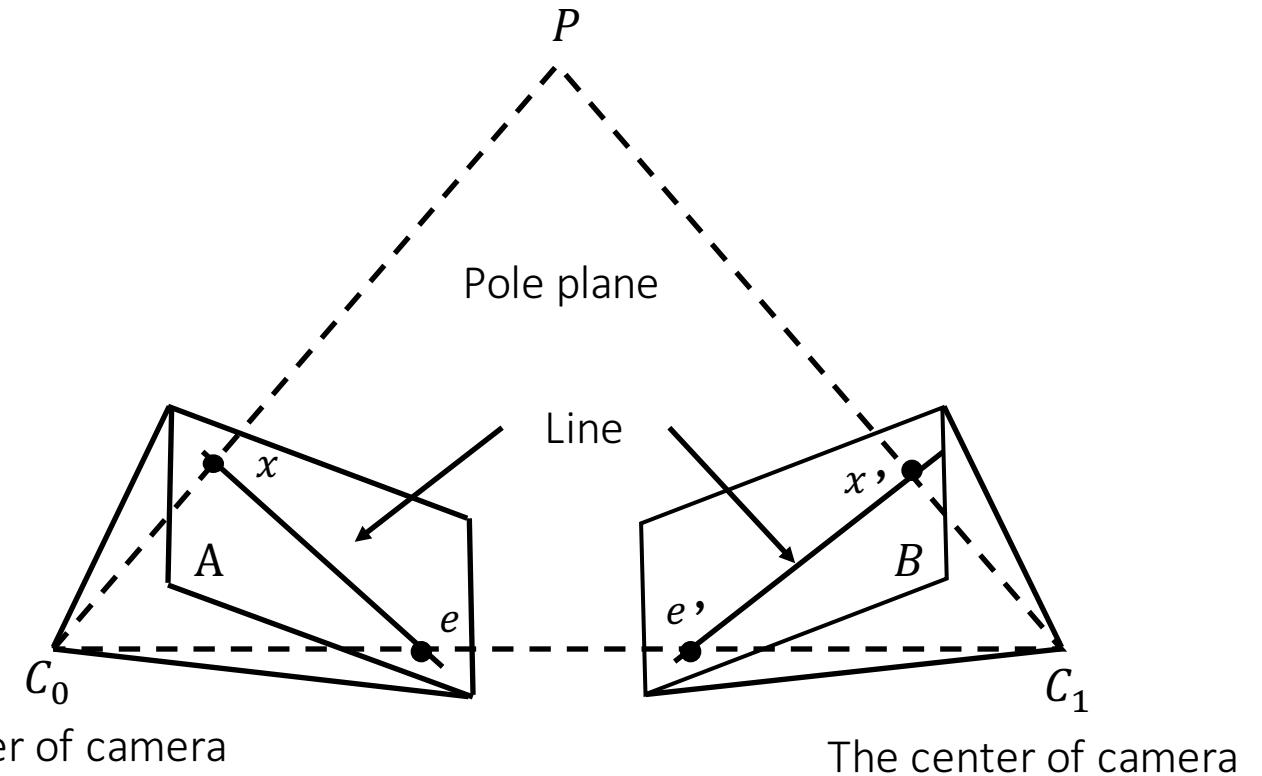
Constraint condition

Continuity



Constraint condition

epipolar constraint



Constraint condition

