

# Variance Reduction for Multi-physics Analysis of Moving Systems

Chelsea D'Angelo

Preliminary Exam

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**WISCONSIN**  
UNIVERSITY OF WISCONSIN-MADISON

## 1 Motivation

## 2 Literature Review

- SDR Analysis

- MC VR Techniques

- GT-CADIS Demonstration

- Moving Geometries and Sources

## 3 Proposal

- TGT-CADIS: VR for SDR Analysis of Moving Systems

## 4 Implementation Plan

- Software

- TGT-CADIS Workflow

## 5 Experiment

## 6 Progress

- Stepwise geometry tool

- DAGMCNP update

## 7 Final Thoughts

# Motivation

- Fusion Energy Systems (FES)
  - Burning plasma, D-T fusion
  - ${}^2_1\text{H} + {}^3_1\text{H} \rightarrow {}^4_2\text{He} + {}^1_0\text{n}$
- Neutrons penetrate deeply into system components, causing activation
- Radioisotopes persist long after shutdown
- Important to quantify the dose caused by decay photons

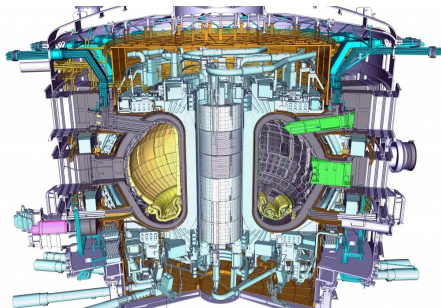


Figure 1 : Cutaway view of ITER drawing.

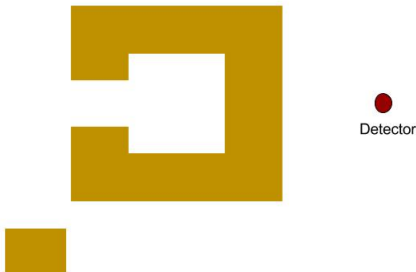
- FES are designed with modular components
  - Can move during maintenance procedure
- Interested in SDR at a particular location
- SDR will change as a function of the activated component's position over time



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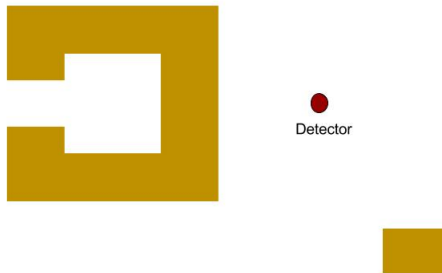


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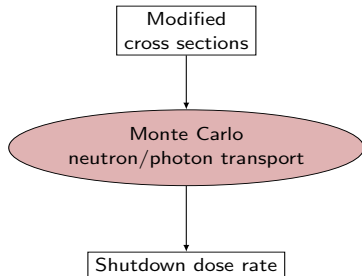




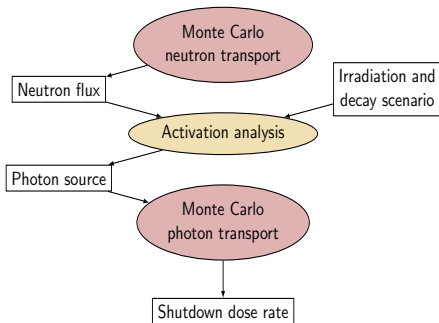
**Optimize** the calculation of the **shutdown dose rate** when activated components are **moving** around the facility.

## Literature Review

## Direct 1-Step Method (D1S) [1]



## Rigorous 2-Step Method (R2S) [2]



- Monte Carlo (MC) method [3]:
  - Stochastic method
  - Simulate random particle walks through phase space
  - Score quantities of interest in discrete regions of phase space
  - Accurate for large, complex models
  - Challenged in highly attenuated regions
    - Results scored in regions that have low particle flux, have higher statistical uncertainty

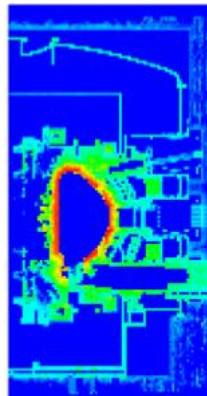


Figure 2 : Photon source in ITER tokamak building.

- Uncertainty in MC calculations:

$$\Re = \frac{\sigma_{\bar{x}}}{\bar{x}} \quad (1)$$

$$\sigma_{\bar{x}} \propto \frac{1}{\sqrt{N}}$$

- Efficiency in MC calculations:

$$FOM = \frac{1}{\Re^2 t_{proc}} \quad (2)$$

- To decrease uncertainty:
  - Increase number of histories,  $N$
  - Use variance reduction (VR) techniques



- Techniques to modify particle behavior
  - **Goal:** preferentially sample events that will contribute to results of interest
- Adjust statistical weight of particles to keep playing a fair game
- Types
  - **Modified Sampling:** source biasing
  - **Population Control:** splitting/rouletteing

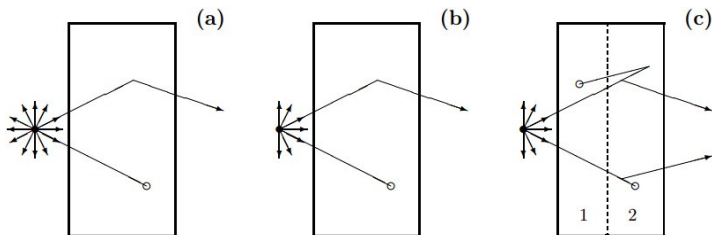


Figure 3 : a) analog b) source biasing c) splitting/rouletteing [4]

- Use **deterministic** estimate of the adjoint flux,  $\Psi^+$ , to generate **Monte Carlo** VR parameters
- Adjoint flux can define the importance of regions of phase space to the detector response
- Define adjoint source to be detector response function

**Forward:**

$$H\Psi(\vec{r}, E, \hat{\Omega}) = q(\vec{r}, E, \hat{\Omega}) \quad (3)$$

$$H = \hat{\Omega} \cdot \nabla + \sigma_t(\vec{r}, E) - \int_0^\infty dE' \int_{4\pi} d\Omega' \sigma_s(\vec{r}, E' \rightarrow E, \hat{\Omega}' \rightarrow \hat{\Omega})$$

**Adjoint:**

$$\langle \Psi^+, H\Psi \rangle = \langle \Psi, H^+\Psi^+ \rangle \quad (4)$$

$$H^+\Psi^+(\vec{r}, E, \hat{\Omega}) = q^+(\vec{r}, E, \hat{\Omega}) \quad (5)$$

$$H^+ = -\hat{\Omega} \cdot \nabla + \sigma_t(\vec{r}, E) - \int_0^\infty dE' \int_{4\pi} d\Omega' \sigma_s(\vec{r}, E \rightarrow E', \hat{\Omega} \rightarrow \hat{\Omega}')$$



## Consistent **A**djoint **D**riven **I**mportance **S**ampling (CADIS)

- Use the adjoint flux,  $\Psi^+$ , to generate MC source and transport biasing parameters
- Biased source:

$$\hat{q}(\vec{r}, E, \hat{\Omega}) = \frac{\Psi^+(\vec{r}, E, \hat{\Omega}) q(\vec{r}, E, \hat{\Omega})}{R} \quad (6)$$

- Weight window lower bounds:

$$w_l(\vec{r}, E, \hat{\Omega}) = \frac{R}{\Psi^+(\vec{r}, E, \hat{\Omega})^{\left(\frac{\alpha+1}{2}\right)}} \quad (7)$$



## VR for **photon** transport

- **Straightforward**
- Can use CADIS method to direct photons towards detector
  - Flux-to-dose-rate conversion factors define adjoint source

## VR for **neutron** transport

- More **complicated**
- Biasing function needs to capture
  - ① Potential of regions to become activated
  - ② Potential to produce photons that will contribute to the SDR
- Can use CADIS if we can construct adjoint source that will fulfill these criteria



## Multi-Step (MS)-CADIS [6]

- VR method to optimize the initial radiation transport step of a coupled, multi-step process
- When applied to SDR analysis, MS-CADIS will optimize the neutron transport step of R2S

- System of coupled, multi-physics:

$$\textit{Primary} : H\phi(u) = q(u) \quad (8)$$

$$\textit{Secondary} : L\psi(v) = b(v) \quad (9)$$

$$b(v) = f(\phi(u))$$

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- Adjoint identities:

$$\langle \phi^+, q \rangle = \langle \phi, q^+ \rangle \quad (10)$$

$$\langle \psi^+, b \rangle = \langle \psi, b^+ \rangle \quad (11)$$



- Response to secondary physics:

$$R_{final} = \langle \omega_R(v), \psi(v) \rangle \quad (12)$$



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- $\phi_R^+$  represents importance function for  $R_{final}$
- Solving for  $q^+$  requires this unique relationship:

$$b(v) = \langle \sigma_b(u, v), \phi(u) \rangle \quad (15)$$

- Substitute Eq. 15 and set primary response equal to secondary :

$$R_{final} = \langle q^+(u), \phi(u) \rangle = \langle \langle \sigma_b(u, v), \phi(u) \rangle, \psi_R^+(v) \rangle \quad (16)$$

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- Switch the order of integration

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- MS-CADIS adjoint primary source:

$$q^+(u) \equiv \langle \sigma_b(u, v), \psi_R^+(v) \rangle \quad (18)$$

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$$q^+(u) \equiv \langle \sigma_b(u, \nu), \psi_R^+(\nu) \rangle \quad (19)$$

- Apply to coupled neutron-photon physics:

- $q^+(u) \equiv q_n^+(E_n)$
- $\psi^+(\nu) \equiv \phi_\gamma^+(E_\gamma)$
- Prompt photon production:  $\sigma_b(u, \nu) \equiv \sigma_{n,\gamma}(E_n, E_\gamma)$
- Delayed photon production:  $\sigma_b(u, \nu) \equiv T_{n,\gamma}(E_n, E_\gamma)$

## Groupwise Transmutation (GT)-CADIS [7]

- Implementation of MS-CADIS specifically for SDR analysis
- Provides method to calculate optimal adjoint neutron source,  $q_n^+$ :

$$q_n^+(E_n) = \langle T(E_n, E_\gamma), \phi_\gamma^+(E_\gamma) \rangle \quad (20)$$

- $T(E_n, E_\gamma)$ 
  - Approximation of the transmutation process
  - Solution exits when SNILB criteria are met
  - Defined by this relationship:

$$q_\gamma(E_\gamma) = \langle T(E_n, E_\gamma), \phi_n(E_n) \rangle \quad (21)$$

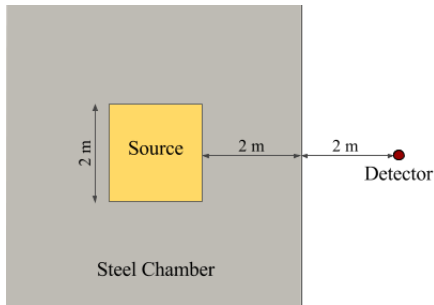


## Groupwise Transmutation (GT)-CADIS [7]

- Calculate T:
  - ① Irradiate each material with neutrons from a single energy group,  $g$
  - ② Record resulting photon emission in each energy group,  $h$

$$T_{g,h} = \frac{q_{\gamma,h}(\phi_{n,g})}{\phi_{n,g}} \quad (22)$$

- Geometry
  - Steel chamber
  - $2\text{m} \times 2\text{m} \times 2\text{m}$  central cavity
- Source
  - Uniform volume source in central cavity
  - 13.8-14.2 MeV neutrons
- Detector
  - Calculate SDR
  - 2m away from chamber



# GT-CADIS Demonstration: Adjoint Photon Transport

## GT-CADIS workflow

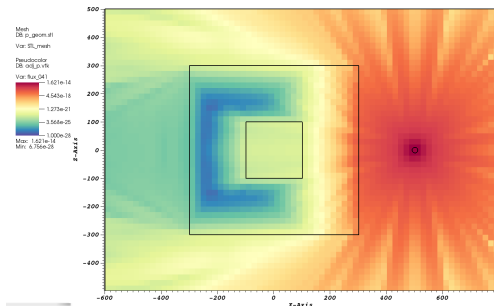
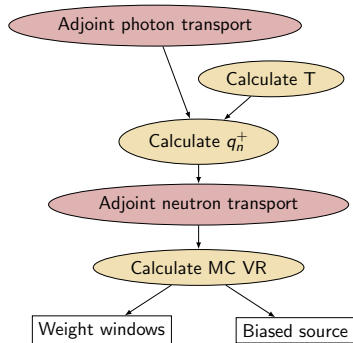


Figure 4 : Adjoint photon flux

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## GT-CADIS workflow

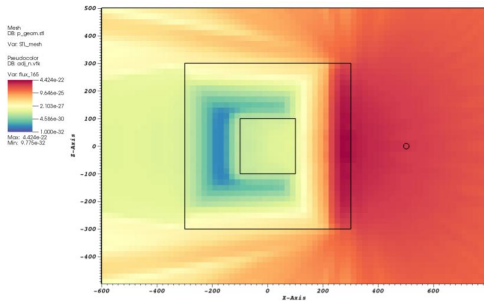
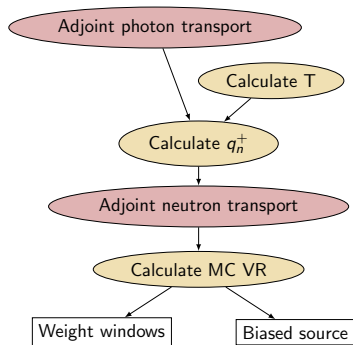


Figure 5 : GT-CADIS adjoint neutron flux. Functions as importance map.

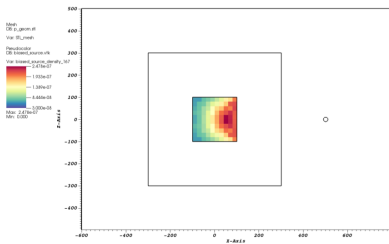


Figure 6 : Biased neutron source generated with GT-CADIS method.

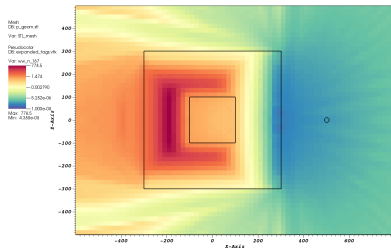


Figure 7 : Weight window mesh generated with GT-CADIS method.

- VR parameters produced by GT-CADIS method result in much faster convergence of the neutron transport flux in comparison to analog and FW-CADIS methods

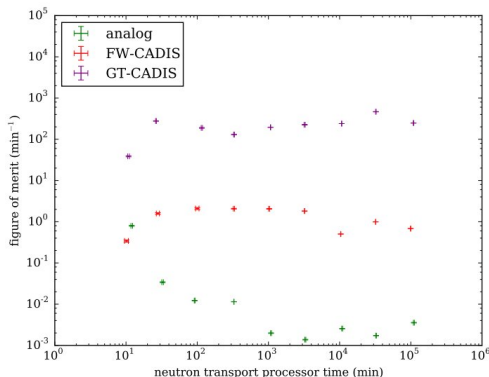


Figure 8 : FOM as function of neutron transport processor time. [8]

GT-CADIS importance map is **insufficient** for moving systems.



Figure 9 : Demo model.

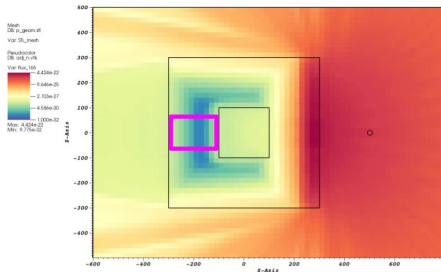


Figure 10 : GT-CADIS adjoint neutron flux. Functions as importance map.

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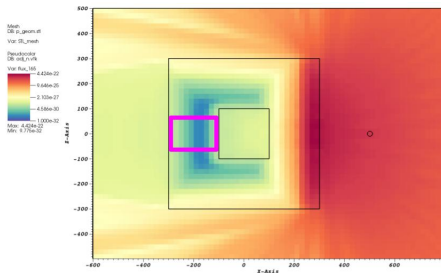


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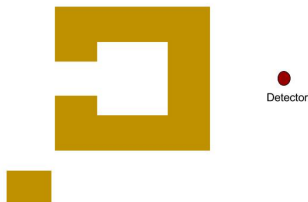


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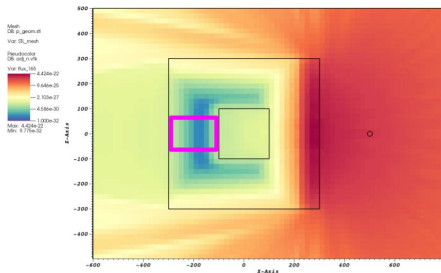


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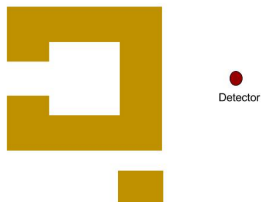


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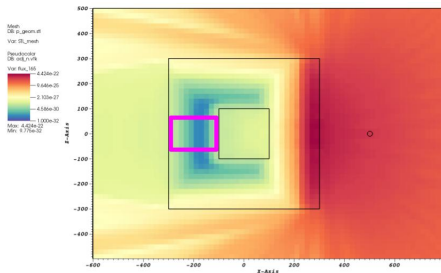


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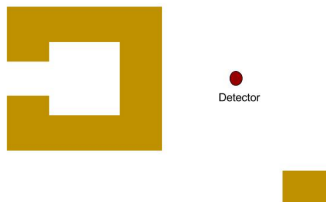


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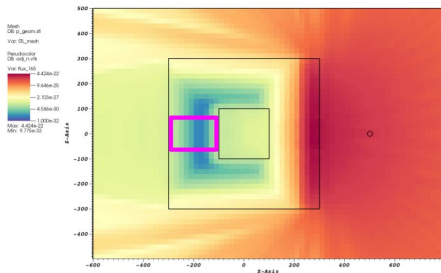


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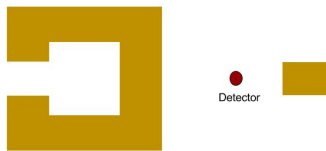


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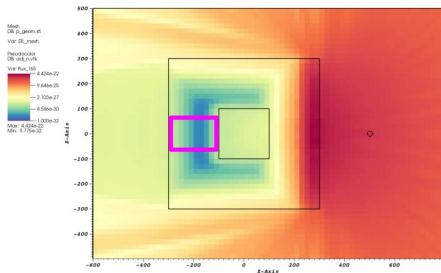


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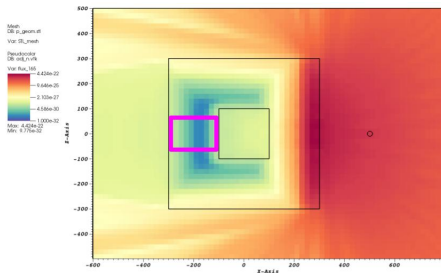


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## MCNP6 Moving Objects [9], [10]

- Update in future version of MCNP6
- Allows movement of objects, sources, delayed particles during single simulation
- Available for native MCNP geometry descriptions (not mesh)



## Mesh Coupled R2S (MCR2S)[11]

- Capability that allows components to move before photon transport step
- Transformations are applied to copies of moving components
- Original component still in original location, set to void material



- MC method is most accurate way to obtain detailed particle flux distributions
  - Use MC codes for both neutron and photon transport steps of R2S
  - Need to use VR methods to optimize the transport calculations
- GT-CADIS has proven to optimize the neutron transport step of R2S
- MCNP6 and MCR2S have developed some capabilities for performing transport on moving geometries
- No automated VR for optimizing neutron transport in systems that move after shutdown



# Proposal

- GT-CADIS optimizes neutron transport step in static systems

$$q_n^+(E_n) = \langle T(E_n, E_\gamma), \phi_\gamma^+(E_\gamma) \rangle$$

- Movement after shutdown, during photon transport:

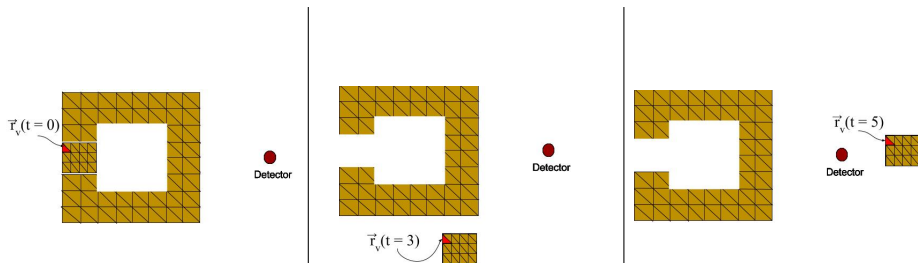
**Need time-integrated adjoint neutron source**

# Time-integrated Adjoint Neutron Source



- Score adjoint photon flux in discrete volume elements at each time step
  - Adjoint flux in volume element  $v$  at time  $t$ :  $\phi_{\gamma}^{+}(\vec{r}_v(t), t)$
  - Position of volume element  $v$  at time  $t$ :  $\vec{r}_v(t)$
- Combine with  $T$  and integrate over time

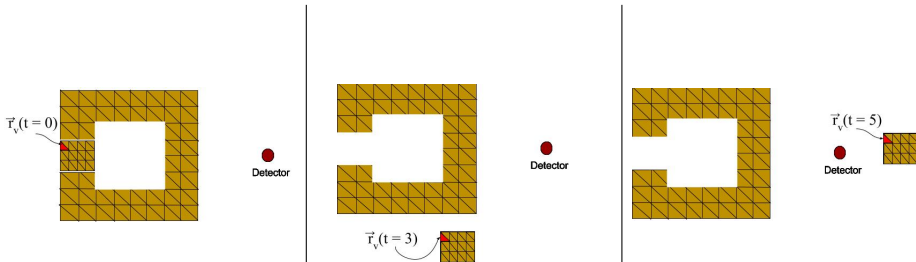
$$q_n^{+} = \frac{\int_t \phi_{\gamma}^{+}(\vec{r}_v(t), t) T_v(t) dt}{\int_t dt} \quad (23)$$



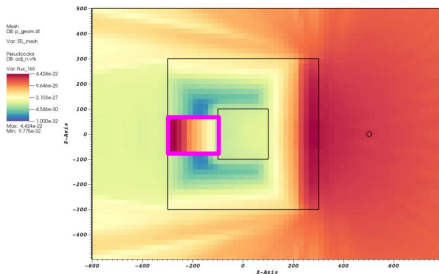
- Discrete form:

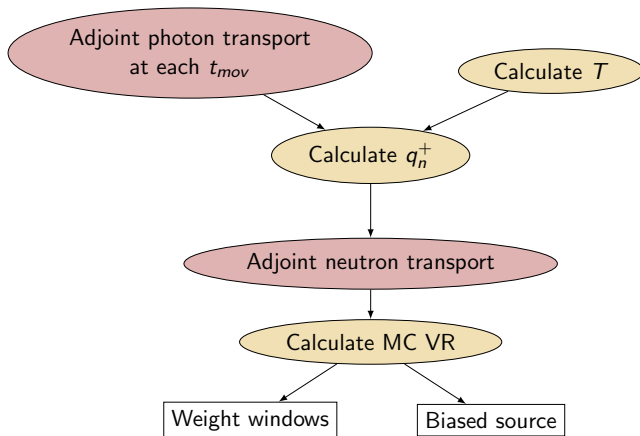
- $t_{mov}$  is the time step
- $\Delta t_{mov}$  is the duration of the time step
- $t_{tot}$  is the total number of time steps

$$q_{n,v,g}^+ = \frac{\sum_{t_{mov}} \left( \sum_h T_{v,g,h} \phi_{\gamma,v,h,t_{mov}}^+ \right) \Delta t_{mov}}{t_{tot}} \quad (24)$$



- Perform deterministic adjoint neutron transport using the time-integrated source
- Resultant adjoint neutron flux should look something like this:

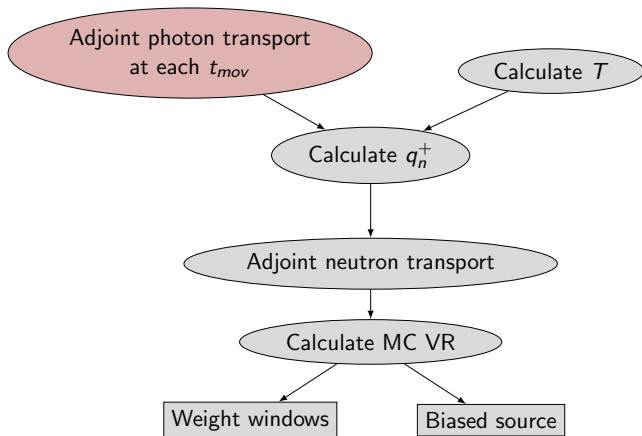




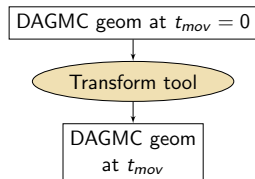
## Implementation Plan

- **PARTISN: PARallel, TIme-Dependent SN** [12]
  - Deterministic adjoint transport
- **DAGMC: Direct Accelerated Geometry** [13], **Monte Carlo, MCNP: Monte Carlo N Particle** [3]
  - Forward MC transport on CAD geometry
- **ALARA: Analytic and Laplacian Adaptive Radioactivity Analysis** [14]
  - Activation analysis
- **PyNE: Python for Nuclear Engineering** [15]
  - Tools to support transport
- **MOAB: Mesh-Oriented datABase** [16]
  - Moving geometries

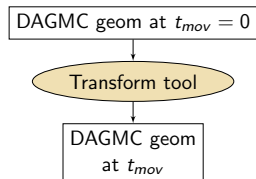




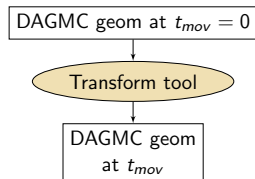
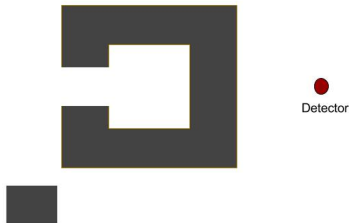
- Generate geometry files at each time step of movement after shutdown



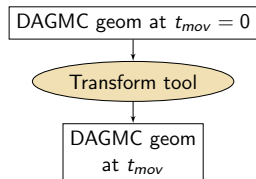
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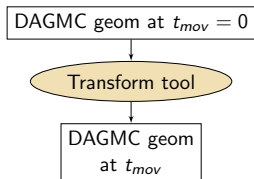
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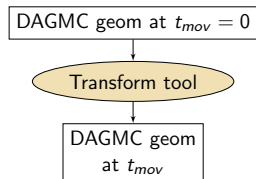
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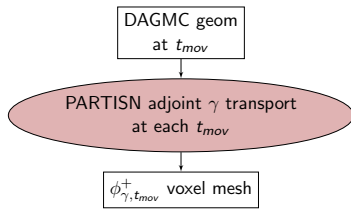
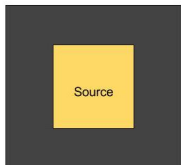
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- Generate geometry files at each time step of movement after shutdown

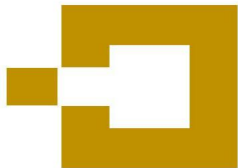


- Perform adjoint photon transport at each time step

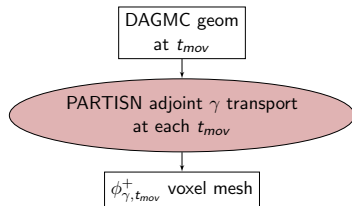




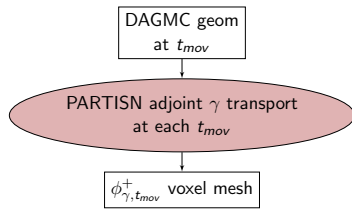
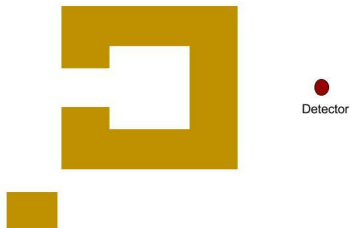
- Perform adjoint photon transport at each time step



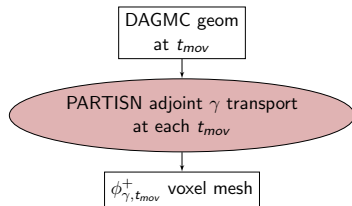
Detector



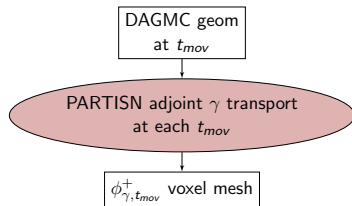
- Perform adjoint photon transport at each time step



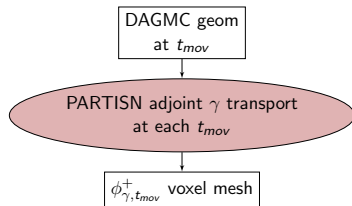
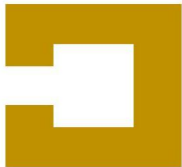
- Perform adjoint photon transport at each time step

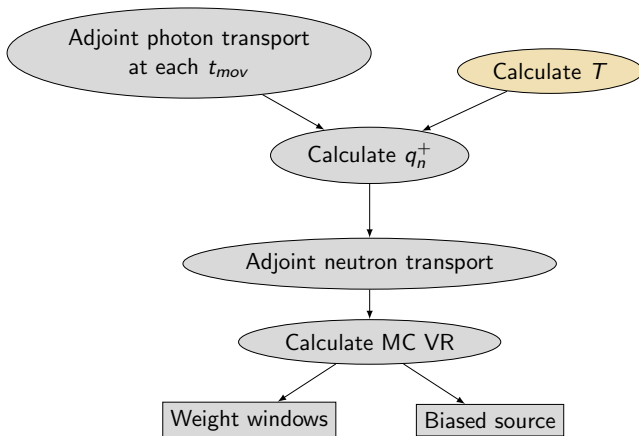


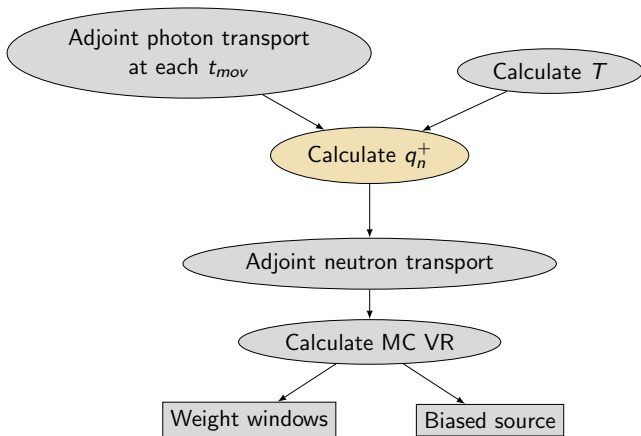
- Perform adjoint photon transport at each time step



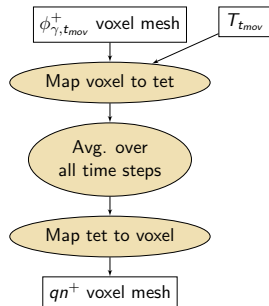
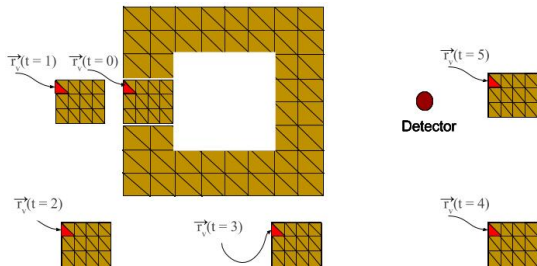
- Perform adjoint photon transport at each time step



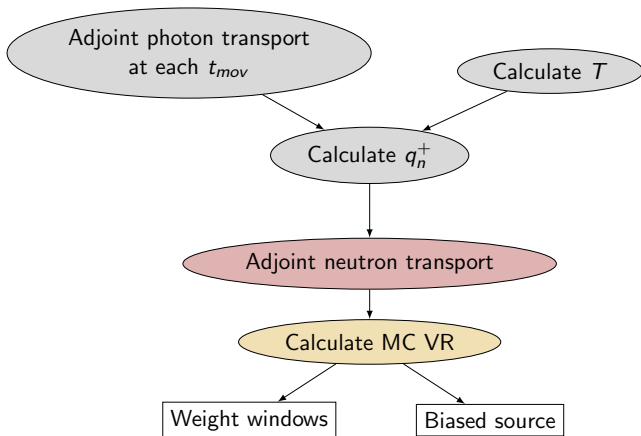




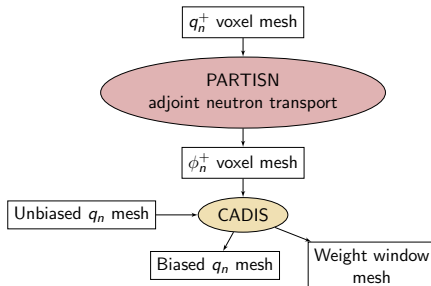
- Map the structured (voxel) mesh to a tetrahedral mesh
- Combine  $\phi_{\gamma,t_{mov}}^+$  and  $T_{t_{mov}}$  and average over time







- Perform adjoint neutron transport
- Generate biased source and weight window mesh via CADIS methodology



# Experiment

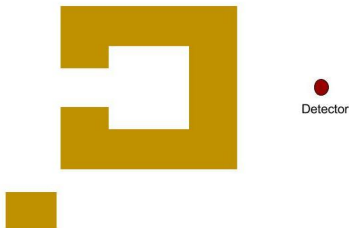
- Assess efficiency of TGT-CADIS
  - Steel chamber with moving component
  - Incrementally add optimization
  - Calculate figure of merit (FOM)



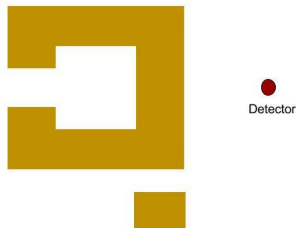
- Assess efficiency of TGT-CADIS
  - Steel chamber with moving component
  - Incrementally add optimization
  - Calculate figure of merit (FOM)



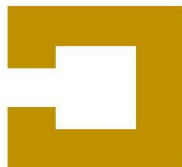
- Assess efficiency of TGT-CADIS
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- Assess efficiency of TGT-CADIS
  - Steel chamber with moving component
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  - Calculate figure of merit (FOM)



- Assess efficiency of TGT-CADIS
  - Steel chamber with moving component
  - Incrementally add optimization
  - Calculate figure of merit (FOM)



•  
Detector



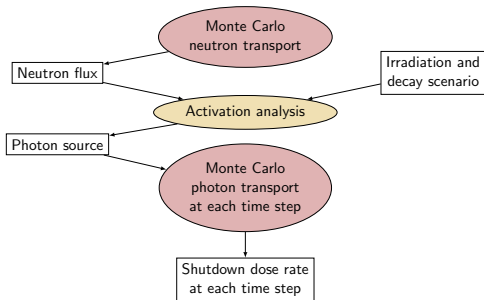


- Assess efficiency of TGT-CADIS
  - Steel chamber with moving component
  - Incrementally add optimization
  - Calculate figure of merit (FOM)



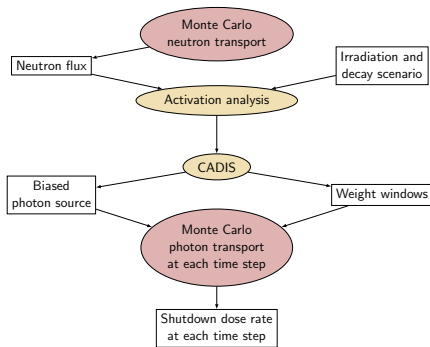
## Experimental Steps:

### 1 No VR



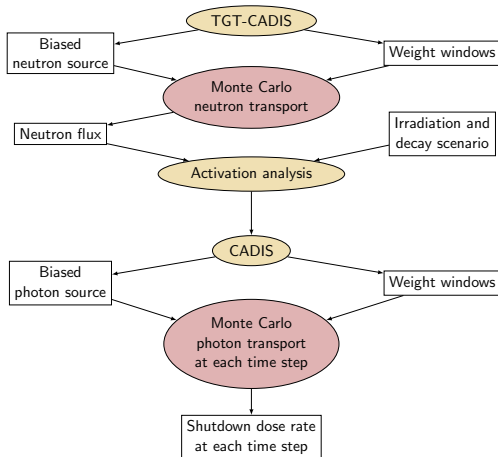
## Experimental Steps:

- 1 No VR
- 2 Photon VR:  
CADIS



## Experimental Steps:

- 1 No VR
- 2 Photon VR:  
CADIS
- 3 Neutron and  
Photon VR:  
TGT-CADIS,  
CADIS



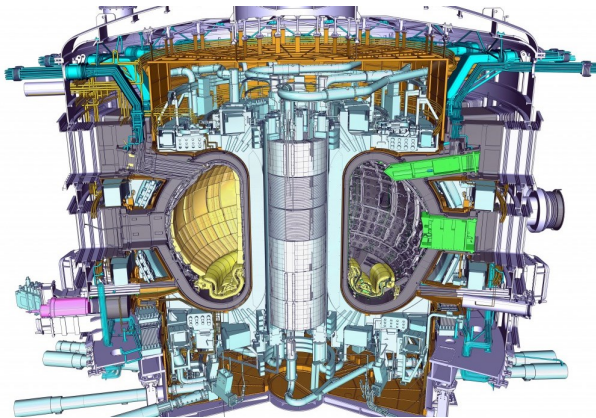
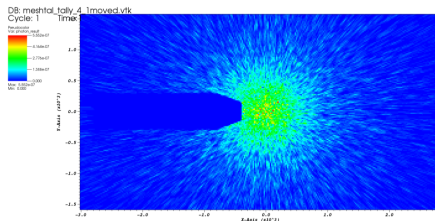


Figure 11 : Cutaway view of ITER drawing.

## Progress

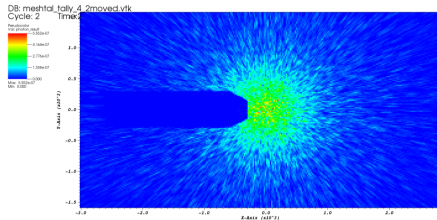
- Capabilities to update position of geometry based on user-defined motion data
  - ① Production of step-wise geometry files
  - ② DAGMCNP update
- Common functionality:
  - Read tag data that specifies type of transformation
  - Identify starting position of each component
  - Update position according to transformation

- Tool to generate new geometry file at each time step
- Motion data:
  - Time-dependent:
    - Translation or rotation vector
    - Duration of time
    - Number of time steps
  - Relocation:
    - Translation or rotation distance

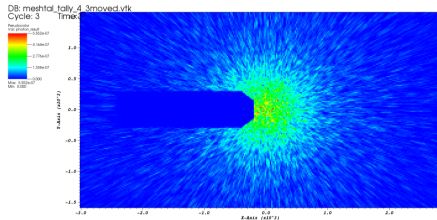




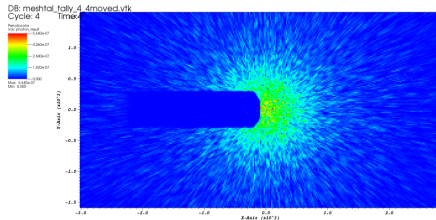
- Tool to generate new geometry file at each time step
- Motion data:
  - Time-dependent:
    - Translation or rotation vector
    - Duration of time
    - Number of time steps
  - Relocation:
    - Translation or rotation distance



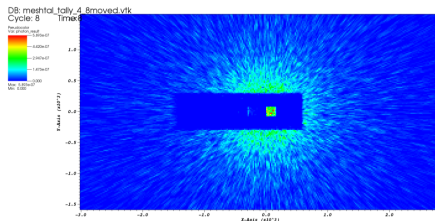
- Tool to generate new geometry file at each time step
- Motion data:
  - Time-dependent:
    - Translation or rotation vector
    - Duration of time
    - Number of time steps
  - Relocation:
    - Translation or rotation distance



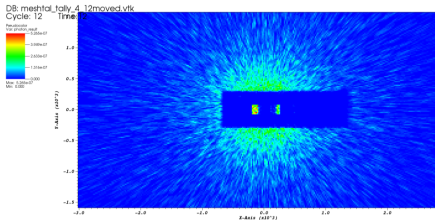
- Tool to generate new geometry file at each time step
- Motion data:
  - Time-dependent:
    - Translation or rotation vector
    - Duration of time
    - Number of time steps
  - Relocation:
    - Translation or rotation distance



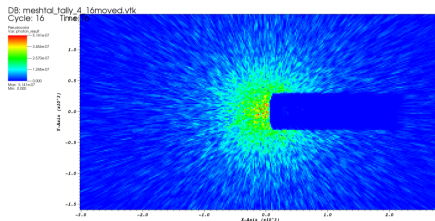
- Time-dependent:
  - Translation or rotation vector
  - Duration of time
  - Number of time steps
- Relocation:
  - Translation or rotation distance



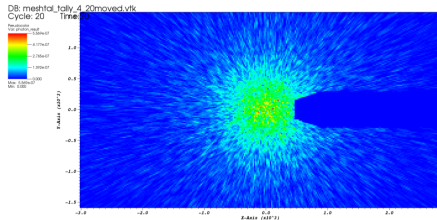
- Tool to generate new geometry file at each time step
- Motion data:
  - Time-dependent:
    - Translation or rotation vector
    - Duration of time
    - Number of time steps
  - Relocation:
    - Translation or rotation distance



- Tool to generate new geometry file at each time step
- Motion data:
  - Time-dependent:
    - Translation or rotation vector
    - Duration of time
    - Number of time steps
  - Relocation:
    - Translation or rotation distance



- Tool to generate new geometry file at each time step
- Motion data:
  - Time-dependent:
    - Translation or rotation vector
    - Duration of time
    - Number of time steps
  - Relocation:
    - Translation or rotation distance





- Functionality to apply MCNP TR(n) card data to DAGMC geometry
- Motion data:
  - Transformation distance
- Separate input file containing transformations for each time step of geometry movement



## Final Thoughts

- Photon transport occurs much faster than geometry movement  $\therefore$  reasonable to do quasi-static simulation
- Period of geometry movement is short enough that the photon source will not change appreciably  $\therefore$  can use same photon source for all time steps of geometry movement



- Geometry movement tools do not treat object kinetics
  - User must be careful to not cause overlap in components
- Can only move components that do not share a surface with any other components

- Depending on complexity of model and fidelity of time resolution, can amass large number of CAD geometry files, volume mesh tally files
- Need to optimize this workflow in order to keep file storage at minimum

- Accurate quantification of the SDR during maintenance procedures is crucial to the design and operation of FES
- GT-CADIS has proven to optimize SDR analysis in static FES
- **TGT-CADIS** aims to provide the capabilities necessary to **optimize** the calculation of the **SDR** during operations that involve activated components **moving** around the facility

Questions?



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