#### **CptS 451- Introduction to Database Systems**

## **Relational Algebra**

(ch-4.1 and ch-4.2)

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## **Outline**



- Relational Algebra
  - Basic operations
- Extended Relational Algebra
  - Outerjoins, Grouping/Aggregation

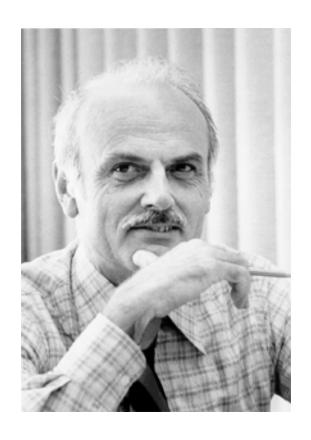
## **Before the Relational Model**



- Database applications were difficult to build and maintain.
- Tight coupling between logical and physical layers.
- You had to (roughly)
   know what queries your
   app would execute before
   you deployed the
   database.

## Relational Model and Relational Algebra

- Proposed in 1970 by Edgar F. Codd.
- Database abstraction to avoid this maintenance.
  - Store database in simple data structures.
  - Access data through high level language.
  - Physical strorage left up to implementation.



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Edgar F. Codd

# What is "Algebra"?



- Mathematical system consisting of:
  - Operands --- variables or values from which new values can be constructed.
  - Operators --- symbols denoting procedures that construct new values from given values.
  - Example: (x-5)/y\*z-3

## What is Relational Algebra?

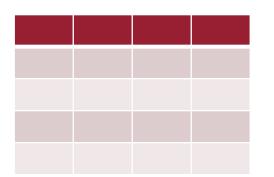


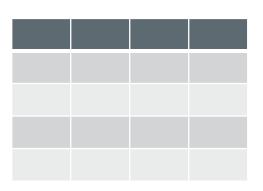
- An algebra whose operands are relations or variables that represent relations.
- Operators are designed to do the most common things that we need to do with relations in a database.
  - Relational algebra is used as a query language for relations.
  - Provides a theoretical foundation for SQL
    - Operations are implemented by the SQL query language

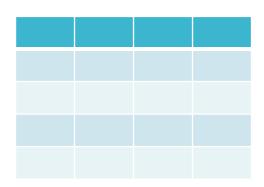


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- Closure
- Compositionality







## **Core Relational Algebra**



- Union, intersection, and difference.
  - Usual set operations, but both operands must have the same relation schema.
- Selection ( $\sigma$ ): picking certain rows.
- Projection( $\Pi$ ): picking certain columns.
- Products (X) and joins ( $\triangleright_{C}$ ): compositions of relations.
- Renaming of relations and attributes.
- We will use the RelaX relational algebra calculator to test relational algebra expressions:
  - https://dbis-uibk.github.io/relax/calc/gist/93fc0fcb193d2ca528edbd2470fce7a1

## Union ∪, Intersection ∩, Difference -



Set operators. Relations must have the same schema.

R(name, dept)

Name	Dept
John	Physics
Tom	EECS

S(name, dept)

Name	Dept
John	Physics
Shira	Math

 $R \cup S$ 

Name	Dept
John	Physics
Tom	EECS
Shira	Math

 $R \cap S$ 

Name	Dept
John	Physics

R-S

Name	Dept
Tom	EECS

## Selection $\sigma$



#### $\sigma_{c}$ (R): return tuples in R that satisfy condition C.

- C is a condition (as in "if" statements) that refers to attributes of R.
- Schema of result is same as that of the input relation R.

Emp (name, dept, salary)

Name	Dept	Salary
Jane	EECS	30K
Jack	Physics	30K
Tom	EECS	75K
Joe	Math	40K
Jack	Math	50K

#### "Employees who earn more than 35K"

or salary>35K (Emp)

Name	Dept	Salary
Tom	EECS	75K
Joe	Math	40K
Jack	Math	50K

#### "EECS Employees who earn less than 40K"

o dept='eecs' and salary<40K (Emp)

Name	Dept	Salary
Jane	EECS	30K

## Projection ∏



 $\Pi_{A1,...,Ak}(R)$ : pick columns of attributes A1,...,Ak of R. eliminate duplicate tuples, if any.

Emp (name, dept, salary)

Name	Dept	Salary
Jane	EECS	30K
Jack	Physics	30K
Tom	EECS	75K
Joe	Math	40K
Jack	Math	50K

"Names and departments of employees"

$$\Pi_{\text{name,dept}}$$
 (Emp)

Name	Dept
Jane	EECS
Jack	Physics
Tom	EECS
Joe	Math
Jack	Math

"Names of employees"

$$\Pi_{\mathsf{name}}$$
 (Emp)

Name	
Jane	
Jack	
Tom	
Joe	

## **Extended Projection**



 $\Pi_{A1,A2+A3->B}(R)$ : the attribute list may contain arbitrary expressions involving attributes:

- 1. Operations on attributes, e.g., A1+A2->B.
- 2. Duplicate occurrences of the same attribute.

#### Grades (ID, Exam1, Exam2)

ID	Exam1	Exam2
1254	80	70
1260	100	90
1275	65	70
1279	71	81

"IDs and average exam grades of students."

$$\Pi_{\text{ID,(Exam1+Exam2)/2->Avg}}$$
(Grades)

ID	Avg
1254	75
1260	95
1275	65
1279	71

The calculated attribute is named 'Avg'

## **Cartesian Product:** ×



#### $\mathbf{R} \times \mathbf{S}$ : pair each tuple $\mathbf{r}$ in $\mathbf{R}$ with each tuple $\mathbf{s}$ in $\mathbf{S}$ .

- Schema of result is the attributes of R and then S, in order.
- If attribute A exists both in R and S then use R.A and S.A.

Emp (name, dept)

Name	Dept	
Jack	Physics	
Tom	EECS	

Contact(name, addr)

Name	Addr
Jack	Pullman
Tom	Moscow
Mary	Colfax

Emp × Contact

Emp.Name	Dept	Contact.Name	Addr
Jack	Physics	Jack	Pullman
Jack	Physics	Tom	Moscow
Jack	Physics	Mary	Colfax
Tom	EECS	Jack	Pullman
Tom	EECS	Tom	Moscow
Tom	EECS	Mary	Colfax

#### Join



$$R \triangleright_{\mathcal{C}} S = \sigma_{\mathbf{c}}(\mathbf{R} \times \mathbf{S})$$

- Take the product **R** X **S**, then apply  $\sigma_c$  to the result.
- Join condition C is of the form:

Each "cond\_i" is of the form A op B, where:

- A is an attribute of R, B is an attribute of S
- op is a comparison operator: =, <, >,  $\geq$ ,  $\leq$ , or  $\neq$ .
- Different types:
  - Theta-join
  - Equi-join
  - Natural join

## **Theta-Join**



$$R \underset{R.A>S.C}{\triangleright \triangleleft} S$$

R(A,B)

Α	В
3	4
5	7

S(C,D)

С	D
2	7
6	8

 $R \times S$ 

Α	В	С	D
3	4	2	7
	1	6	
	_	J	0
5	7	2	7
	7	6	
)	/	U	0

#### Result

Α	В	С	D
3	4	2	7
5	7	2	7

## **Theta-Join**



 $R \longrightarrow S$   $R.A > S.C \text{ and } R.B \neq S.D$ 

R(A,B)

Α	В
3	4
5	7

S(C,D)

С	D
2	7
6	8

 $R \times S$ 

Α	В	С	D
3	4	2	7
_2		C	0
	7	U	O
	7	2	7
)	,		,
	7	6	0
)	1	U	0

#### Result

Α	В	С	D
3	4	2	7

# **Equi-Join**



• Special kind of theta-join: **C** only uses the equality operator.

R(A,B)

Α	В
3	4
5	7

S(C,D)

С	D
2	7
6	8

$$R_{R,B=S,D}$$

R.A	R.B	R.C	R.D
5	7	2	7

#### Natural-Join **⋈**



- Connects two relations by:
  - Equating attributes of the same name (Equi-Join), and
  - Projecting out one copy of each pair of equated attributes.
- Relations R and S. Let L be the union of their attributes.
   And let A1,...,Ak be their common attributes.

$$R \bowtie S = \prod_{L} (R \bowtie S)$$
 $R.A1=S.A1 \text{ and } ..., R.Ak=S.Ak$ 

Emp(name,dept)

Dept	Name
Physics	Jack
EECS	Tom

Contact(name, addr)

Name	Addr
Jack	Pullman
Tom	Moscow
Mary	Colfax

Emp Contact: all employee names, depts, and addresses.

Dept	Name	Addr
Physics	Jack	Pullman
EECS	Tom R	ela <b>MQ\$QQW</b> ra

## Natural Join - Exercise1



 Names and GPAs of <u>students</u> with SAT>1200 who <u>applied</u> to CS and were rejected

$$\Pi_{\text{sName,GPA}}(\sigma_{\text{(SAT>1000) AND (major='CS') AND (decision='R')}}$$
 (Student  $\bowtie$ Apply))

College

Student

**Apply** 

cName	state	enrolment

sID	sName	GPA	SAT

sID	cName	major	decision

Student⊠Apply

sID	sName	GPA	SAT	cName	major	decision

https://dbis-uibk.github.io/relax/calc/gist/b58990c762b4e2e168a57f22a4d0bb51

## Natural Join – Exercise 2



Names and GPAs of students with GPA>3.5 who applied to
 CS at colleges with enrollment>20,000 and were rejected

$$\Pi_{\mathrm{sName,GPA}}(\sigma_{\mathrm{GPA}>3.5~\mathrm{AND~major='CS'~AND~enrollment}>20000~\mathrm{AND~decision='R'}}$$
 ((Student  $\bowtie$ Apply)  $\bowtie$  College))

College

Student

Apply

cName	state	enrolment

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sID	sName	GPA	SAT

sID	cName	major	decision

#### Student ⋈ Apply ⋈ College

	sID	sName	GPA	SAT	cName	major	decision	state	enrollment
1									

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# Renaming $\rho$



- Motivation: disambiguate relation and attribute names.
  - e.g., in R × R, how to differentiate the attributes from the two instances?

$$ho_{\mathsf{S}(\mathsf{B1},\ldots,\mathsf{Bn})}(\mathsf{R})$$

**S** is a relation identical to **R**, with new attributes B1,...,Bn.

$$\rho_{\text{emp1(name1,dept1)}}(\text{Emp})$$

Emp(name,dept)

Name	Dept
Jack	Physics
Tom	EECS

Emp1(name1, addr1)

Name1	Dept1
Jack	Physics
Tom	EECS



# Renaming $\rho$ (cont)

Emp (name, dept)

Name	Dept
Jack	Physics
Tom	EECS
Mary	EECS

"List all employees who work in the same department as Tom."

$$\Pi_{\text{emp1.name}}(\rho_{\text{emp1(name1,dept1)}}(\text{emp}))\bowtie \sigma_{\text{name='Tom'}}(\text{emp}))$$

	Name	
Tom Mary		

## **Schemas of Results - Summary**



#### • Schema of each operation:

- $-\cup$ ,  $\cap$ , —: same as the schema of the two relations (remember that the schema of the operands should be same)
- Selection  $\sigma$ : same as the relation's schema
- Projection  $\Pi$ : attributes in the projection
- Cartesian product X: attributes in two relations, use prefix to avoid confusion
- − Theta Join : same as X
- Natural Join → : union of relations attributes, merge common attributes
- Renaming  $\rho$ : new renamed attributes

# **Building Complex Expressions**



- Three notations (similar to arithmetic):
  - 1. Expressions with several operators
    - Combine operators with parentheses and precedence rules
  - 2. Sequences of assignment statements
  - 3. Expression trees

# 1. Expressions with Several Operators Cotts 45



• Examples:

$$R \bowtie S = \prod_{L} (R \bowtie S)$$

$$R \cap S = R - (R - S)$$

- Precedence of relational operators:
  - 1. () parenthesis
  - 2.  $[\sigma, \pi, \rho]$  (highest).
  - 3. [X, ⋈].
  - **4.** ∩.
  - 5.  $[\cup, -]$

# 2. Sequences of Assignments



- Motivation: expressions can be complicated
- Introduce names for intermediate relations, using the assignment operator "="
- Then a query can be written as a sequential program consisting of a series of assignments
- Example:

$$\prod_{balance} (\sigma_{custssn=ssn}(account \times (\sigma_{name=tom} customer)))$$

R1 = 
$$\sigma_{\text{name=tom}}$$
 (customer)  
R2 =  $\sigma_{\text{custssn=ssn}}$  (account×R1)  
Result =  $\Pi_{\text{balance}}$  (R2)

## **3.Expression Trees**

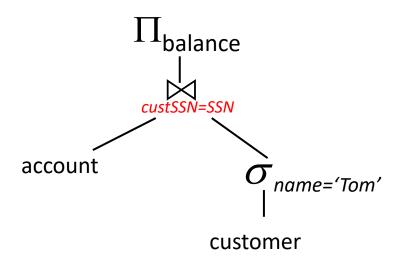


- Leaves are operands --- variables standing for relations.
- Interior nodes are operators, applied to their child or children.

Example: "List account balance of Tom."

customer(SSN, name, city)
account(custSSN, balance)

$$\Pi_{\text{balance}}$$
 (account  $\bowtie \sigma_{\text{name='Tom'}}$  (customer))



# Expression Trees – Example1 (Alternative Solution)

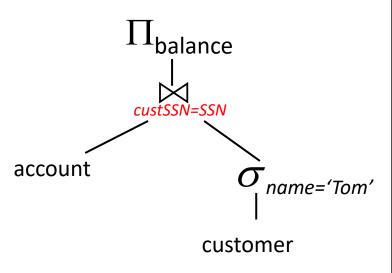


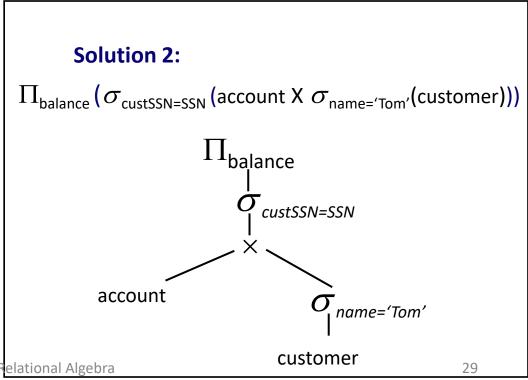
customer(SSN, name, city)
account(custSSN, balance)

•"List account balance of Tom."

#### **Solution 1:**

$$\Pi_{\text{balance}}$$
 (account  $\bowtie \sigma_{\text{name='Tom'}}$  (customer))



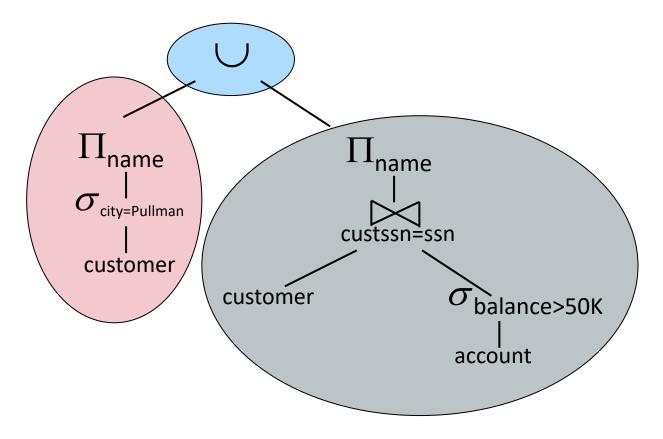


## **Expression Trees – Example 2**



customer(ssn, name, city)
account(custssn, balance)

Find names of customers in
 Pullman or having a balance > 50K.

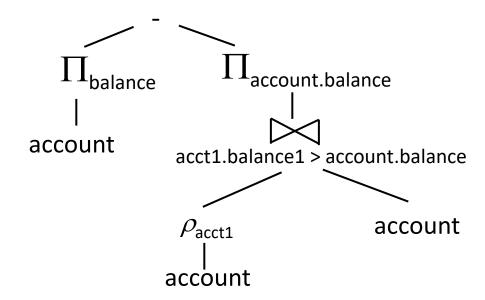


# **Example 3**



customer(ssn, name, city)
account(custssn, balance)

 Find the highest balance among all the customers.



https://dbis-uibk.github.io/relax/calc/gist/528fb4e46355f4b8e9911fdd3376f73d



## **Relational Operations on Bags**

## **Bag Semantics**



- Set semantics: no duplicates
  - {1,2,1,3} is a bag.
  - {1,2,3} is also a bag that happens to be a set.
- Bag semantics: duplicates possible, no order
  - SQL (mostly) uses the bag semantics: a table could have duplicated tuples
  - Reason: efficient processing.
    - Some operations, like projection, are more efficient on bags than sets

R(name, dept)

Name	Dept
Jack	Physics
Tom	EECS
Tom	EECS
	Relational Algebra

A bag



- Bag Union: Combine elements from two relations
  - E.g.,  $\{1,3,7\} \cup \{3,5,6\} = \{1,3,3,5,6,7\}$
- Bag intersection: take the minimum of the number of occurrences in each bag
  - E.g.:  $\{1,1,2,2,3\} \cap \{1,2,2,2,3,4\} = \{1,2,2,3\}$

- Bag difference: proper-subtract the number of occurrences in the two bags
  - E.g.:  $\{1,1,1,2,2,3\}-\{1,2,3,4\}=\{1,1,2\}$



 Selection and projection applies to each tuple independently. Duplicates are not eliminated in the result.

 Products and joins are done on each pair of tuples, regardless of whether it is a duplicate or not. The duplicates are not eliminated in the final result.



#### **Example:** Bag Selection

R(A,B)

Α	В
1	2
5	6
1	2

$$O_{A+B<5}$$
 (R)

Α	В
1	2
1	2

#### **Example: Bag Projection**

R(A,B)

Α	В
1	2
5	6
1	2

$$\Pi_A$$
 (R)

Α	
1	
5	
1	



**Example:** Bag Product

R(A,B)

Α	В
1	2
5	6
1	2

S(B,C)

В	С
2	4
7	8

**RXS** 

R.A	R.B	S.B	S.C
1	2	2	4
1	2	7	8
5	6	2	4
5	6	7	8
1	2	2	4
1	2	7	8
			•

### **Operations on Bags**



**Example:** Bag Natural-Join

R(A,B)

Α	В
1	2
5	6
1	2

S(B,C)

В	С
2	4
7	8

 $R \bowtie S$ 

Α	В	С
1	2	4
1	2	4

**Example:** Bag Theta-Join

R(A,B)

Α	В
1	2
5	6
1	2

S(B,C)

В	С
2	4
7	8

 $R \bowtie_{R,B \leq S,B} S$ 

R.A	R.B	S.B	S.C

### **Laws for Bags**



- Some laws for sets still hold for bags
  - E.g., union and intersection are still commutative and associative
  - $-R \cap S = S \cap R$ ,  $(R \cap S) \cap T = R \cap (S \cap T)$
- Some laws for sets might not hold for bags:
  - 1.  $R \cap (S \cup T) = (R \cap S) \cup (R \cap T)$  is true for sets But it is **not true** for bags. E.g.:
    - R=S=T={1}
    - $R \cap (S \cup T) = \{1\}$
    - $(R \cap S) \cup (R \cap T) = \{1,1\}$
  - 2. S∪S=S is true for setsBut it is **not true** for bags



# **Extended Operators of Relational Algebra**

## **Extended Relational Algebra**



- Basic relational algebra is using the set semantics
- Extended relational algebra and SQL is using bag semantics.
- More operations needed:
  - Duplicate-elimination operator  $\delta$
  - Sorting operator  $\tau$
  - Grouping and aggregation operator  $\gamma$

# Duplicate elimination $\delta$



•  $\delta(R)$  = relation with one copy of each tuple that appears one or more times in R

R

Α	В
1	2
3	4
3	4

 $\delta$  (R)

Α	В
1	2
3	4

# Sorting T



- τ<sub>L</sub>(R) = sort the records in R according to attributes on list L (i.e., L= {A1,A2,..Ak}
  - Sort first on the value of A1, then A2, and so on.

R

Α	В
5	2
3	7
3	4

 $\tau_{A}(R)$ 

Α	В
3	7
3	4
5	2

 $\tau_{A.B}(R)$ 

Α	В
3	4
3	7
5	2

### Aggregation



 Aggregation function takes a collection of values and returns a single value as a result.

avg: average value

– min: minimum value

max: maximum value

sum: sum of values

count: number of values

#### Account

Name	Branch	Balance
Tom	Pullman	10K
Tom	Seattle	20K
Mary	Seattle	5K
Jack	Pullman	20K

COUNT(\*)

4

MAX(Balance)

20K

SUM(Balance)

55K

MIN(Balance)

5K

\* refers to complete list of attributes

AVG(Balance)

13.75K

### Grouping



- Aggregate operation applied to an attribute calculates the value for the entire column.
- Grouping allows to consider the tuples in a relation as groups (corresponding to the value of one or more attributes) and aggregate only within groups.
- Example:

#### Account

Name	Branch	Balance
Tom	Pullman	10K
Tom	Seattle	20K
Mary	Seattle	5K
Jack	Pullman	40K
Mark	Seattle	20K
James	Moscow	15K
Abby	Pullman	45K
Ashley	Moscow	13K

#### Group according to branch

Name	Branch	Balance
Tom	Seattle	20K
Mary	Seattle	5K
Mark	Seattle	20K
Tom	Pullman	10K
Jack	Pullman	40K
Abby	Pullman	45K
James	Moscow	15K
Ashley	Moscow	13K

# Grouping and Aggregation γ



- $\gamma_{L,\theta(A)}(R)$
- Group R according to attributes on list L
- Within each group, do aggregation  $\theta(A)$
- Result has one tuple for each group. It includes:
  - 1. The grouping attributes and
  - Their group's aggregations.

First, group tuples in Accunt according to "Branch."

#### Account

Name	Branch	Balance
Tom	Seattle	20K
Mary	Seattle	5K
Mark	Seattle	20K
Tom	Pullman	10K
Jack	Pullman	40K
Abby	Pullman	45K
James	Moscow	15K
Ashley	Moscow	13K

Then do the aggregation within each group.

 $\gamma_{\text{branch;Count(Name)->NumCust}}(Account)$ 

Branch	NumCust
Pullman	3
Seattle	3
Moscow	2

 $\gamma_{\text{branch;Sum(Balance)->Total}}(Account)$ 

Branch	Total
Pullman	95K
Seattle	45K
Moscow	28K

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R(A,B,C)

Α	В	С
1	2	3
4	5	6
1	2	5

$$\gamma_{A,B;AVG(C)->X}(R) = ??$$

First group R by A and B:

Α	В	С
1	2	3
1	2	5
4	5	6

Then calculate average for C within groups:

Α	В	X
1	2	4
4	5	6

### **Outer Join**



### • Motivation:

R(Dept,Name)

Dept	Name
Physics	Jack
EECS	Tom

S(Name, Addr)

Name	Addr
Jack	Pullman
Mike	Seattle
Mary	Spokane

- Variants of the outerjoin:
  - Full outer join (outer join)
  - Left outer join
  - Right outer join

### **Outer Join**



- An extension of the natural join operation that avoids loss of information.
- Computes the join and then adds ("dangling") tuples form one relation that does not match tuples in the other relation to the result of the join.
- Variants of the outerjoin:
  - Full outer join  $R \bowtie S$  (or just outer join)
  - Left outer join  $R \stackrel{\circ}{\bowtie}_L S$
  - Right outer join  $R \bowtie_R^{\circ} S$

### **Full Outer Join**



- Add dangling tuples from both left and right relations.
- Pad null values for the dangling tuples

### R(Dept, Name)

Dept	Name
Physics	Jack
EECS	Tom

### S(Name, Addr)

Name	Addr	
Jack	Pullman	
Mike	Seattle	
Mary	Spokane	

### R MS

Dept	Name	Addr
Physics	Jack	Pullman

**Natural Join** 

### R ⋈S

Dept	Name	Addr
Physics	Jack	Pullman
EECS	Tom	NULL
NULL	Mike	Seattle
NULL	Mary	Spokane

**Full Outer Join** 

### **Left and Right Outer Join**



- Left Outer Join: Add dangling tuples from left relation.
- Right Outer Join: Add dangling tuples from right relation.
- Pad NULL values for the dangling tuples

### R(Dept,Name)

Dept	Name
Physics	Jack
EECS	Tom

# $R \stackrel{\circ}{\bowtie}_{L} S$

Dept	Name	Addr
Physics	Jack	Pullman
EECS	Tom	NULL

Left Outer Join

### S(Name, Addr)

Name	Addr	
Jack	Pullman	
Mike	Mike Seattle	
Mary	Spokane	

# $R \stackrel{\circ}{\bowtie}_R S$

Dept	Name	Addr
Physics	Jack	Pullman
NULL	Mike	Seattle
NULL	Mary	Spokane

Right Outer Join

## **Limitation of Relational Algebra**



- Some queries cannot be represented
- Example, recursive queries:
  - Table R(Parent, Child)
  - How to find all the ancestors of "Tom"?
  - Impossible to write this query in relational algebra
- More expressive languages needed:
  - E.g., Datalog

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 Consider the following relational schema for a library (assume using bagsemantics). Write the following queries in relational algebra.

Member

**Books** 

Borrowed

member#	name	dob

	isbn	title	authors	publisher
Ī				

member#	isbn	date

#### https://dbis-uibk.github.io/relax/calc/gist/93fc0fcb193d2ca528edbd2470fce7a1

a. Find the names of members who have borrowed any book published by "McGrawHill".

#### Steps:

- 1. Find the books published by McGraw-Hill.
- 2. Find the member# s that borrowed the books in step1. Get the names for those members.

R1 = 
$$\sigma_{\text{publisher='McGraw-Hill'}}$$
(Books)

Result = 
$$\Pi_{\text{name}}$$
 (Member  $\bowtie$  (Borrowed  $\bowtie$  R1))



Member

**Books** 

Borrowed

member#	name	dob

	isbn	title	authors	publisher
Ī				

member#	isbn	date

b. Find the names of members who have borrowed more than five books published by "McGrawHill". A member can borrow the same book more than once.

R1 = 
$$\sigma_{\text{publisher='McGraw-Hill'}}$$
(Books)

R2 = 
$$\sigma_{\text{numBooks}}$$
 ( $\gamma_{\text{member\#,COUNT(isbn)->numBooks}}$  (Borrowed  $\bowtie$  R1))

Result = 
$$\Pi_{\text{name}}$$
 (Member  $\bowtie$  R2)



Member

Books

Borrowed

member#	name	dob

isbn	title	authors	publisher

member#	isbn	date

c. Find the names and membership numbers of members who have borrowed more than one <u>different</u> books published by "McGrawHill". A member can borrow the same book more than once.

R1 := 
$$\sigma_{\text{publisher='McGraw-Hill'}}$$
(Books)

$$R2:=\sigma_{\text{numBooks}}(\gamma_{\text{member\#,COUNT(isbn)->numBooks}}(\delta(\Pi_{\text{member\#,isbn}}(\text{Borrowed}\bowtie R1))))$$

Result:= 
$$\Pi_{\text{name,member#}}$$
 (Member  $\bowtie$  R2)



Member

**Books** 

Borrowed

member#	name	dob

isbn	title	authors	publisher

d. For each publisher, find the name and membership number of members who have borrowed more than one book of that publisher

R1 = 
$$\sigma_{\text{numBooks}>1}$$
 ( $\gamma_{\text{publisher,member\#,COUNT(isbn)->numBooks}}$  (Borrowed  $\bowtie$  Books))  
Result:= $\Pi_{\text{publisher,name,member\#}}$  (Member  $\bowtie$ R1)

WSU CptS 451

Member

**Books** 

Borrowed

member#	name	dob

isbn	title	authors	publisher

member#	isbn	date

e. Find the <u>average number of books</u> borrowed by members. Take into account that if a member does not borrow any books, then that member does not appear in the borrowed relation.

 $\gamma_{\text{COUNT(isbn)}}$  (Borrowed) /  $\gamma_{\text{COUNT(member#)}} \delta(\Pi_{\text{member#}})$  (Borrowed))

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Member

**Books** 

Borrowed

member#	name	dob

isbn	title	authors	publisher

member#	isbn	date

f. Find the members who didn't borrow any 'McGrawHill' books. Give the names and memberNo's of those members.



Member

**Books** 

Borrowed

member#	name	dob

isbn	title	authors	publisher

member# isbn date

g. Find the members who borrowed the most number of books.

h. Find the pair of members who borrowed the same books.