

#### 4.4 MODELING, OPTIMIZATION

(61)

MAXIMUMS OR MINIMUMS OCCUR  
AT ENDPOINTS OR WHEN  $\frac{dy}{dx} = 0$

STRATEGIES FOR SOLVING MAX-MIN PROBLEMS  
BOTTOM OF p. 208. (SUGGESTIONS)

EXAMPLE

$$X + Y = 20 \quad \text{MAXIMIZE } X \cdot Y$$

$\rightarrow Y = 20 - X$

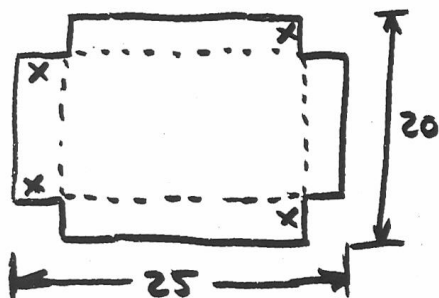
$$\text{PRODUCT} = P = X \cdot Y = X(20 - X)$$

$$P = 20X - X^2 \quad \frac{dP}{dX} = 20 - 2X \quad 20 - 2X = 0$$

$$Y = 20 - X = 20 - 10 \quad \boxed{Y = 10} \quad \boxed{X = 10}$$

EXAMPLE 1 p. 206

OPEN TOP BOX CUT OUT OF  $20 \times 25$  SHEET  
MAXIMIZE THE VOLUME.



$$V = lwh$$

$$V = (25 - 2x)(20 - 2x)x$$

$$V = 4x^3 - 90x^2 + 500x$$

$$\frac{dV}{dx} = 12x^2 - 180x + 500$$

OVER  $\rightarrow$

Solve  $(12x^2 - 180x + 500 = 0, x)$  TI-89 OR (62)

$Y1 = 12x^2 - 180x + 500$  QUADRATIC FORMULA OR  
GRAPH MORE MATH ROOT  $x = 3.681$   $x = 11.319$   
DOMAIN  $0 < x < 10$  MAXIMUM IMPOSSIBLE

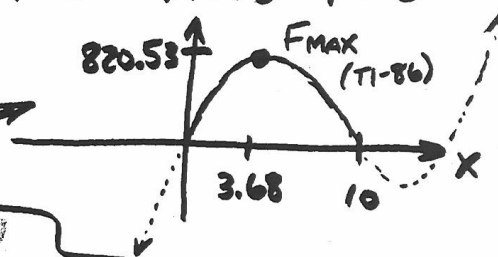
BECAUSE  $x$  IS HEIGHT &  $20 - 2x$  IS WIDTH

$$V = (25 - 2 \cdot 3.681)(20 - 2 \cdot 3.681) 3.681 = \underline{820.53}$$

AT END POINTS  $x = 0$   $V = 0$   $x = 10$   $V = 0$

So MAX  $V = 820.53$

$$Y = 4x^3 - 90x^2 + 500x$$



EXAMPLE p. 217 #32a

$$S = kwd^2 \quad w^2 + d^2 = 12^2 \Rightarrow d^2 = 144 - w^2$$

$$S = kw(144 - w^2) \Rightarrow S = 144kw - kw^3$$

$$\frac{dS}{dw} = 144k - 3kw^2 \quad 144k - 3kw^2 = 0$$

$$3k(48 - w^2) = 0 \quad 48 - w^2 = 0 \quad w = \sqrt{48}$$

$$d^2 = 144 - w^2 = 144 - (\sqrt{48})^2 = 96 \quad d = \sqrt{96}$$

DIMENSIONS  $\sqrt{48} \times \sqrt{96}$  STRONGEST BEAM

HOMEWORK p. 214-217  $\rightarrow$  1-33 ODD

1 a only    23 ab only  
33 a only

AB OMIT  
23, 25, 27