More λ-Calculus Lexical Semantics

LING 571 — Deep Processing Techniques for NLP
October 31st, 2018 ©
Ryan Georgi





Announcements

- We will be dropping lowest assignment.
- EC for HW #4 due tonight





Happy Hall ween!

Emily's costume today:







More \(\lambda\)-Calculus





A Few Clarifications

- We will consider "all" to be semantically equivalent to "every"
- "nobody" = "not a"





Target Representations





W The target representations should have:

Lambdas

Uninstantiated Variables

Constants

Predicates





Common Nouns

- $\lambda x. Restaurant(x) \rightarrow `restaurant'$
 - Somewhat similar to the NNP construction
 - λ var.Predicate(var)
- But common nouns represent relations, rather than constants
 - Meaning of the noun encoded in the predicate
 - Relate the concept of the noun to a particular instance of variable





Scope Ambiguity, Again

- "Every restaurant has a menu"
 - $\forall x \ Restaurant(x) \Rightarrow \exists y \ Menu(y) \land \exists e \ Having(e) \land Haver(e,x) \land HadThing(e,y)$
 - $\exists y \; Menu(y) \; \forall x \; Restaurant(x) \Rightarrow \exists e \; Having(e) \land Haver(e,x) \land HadThing(e,y)$
- For the homework, only need to come up with one.
 - How is this handled in practice?





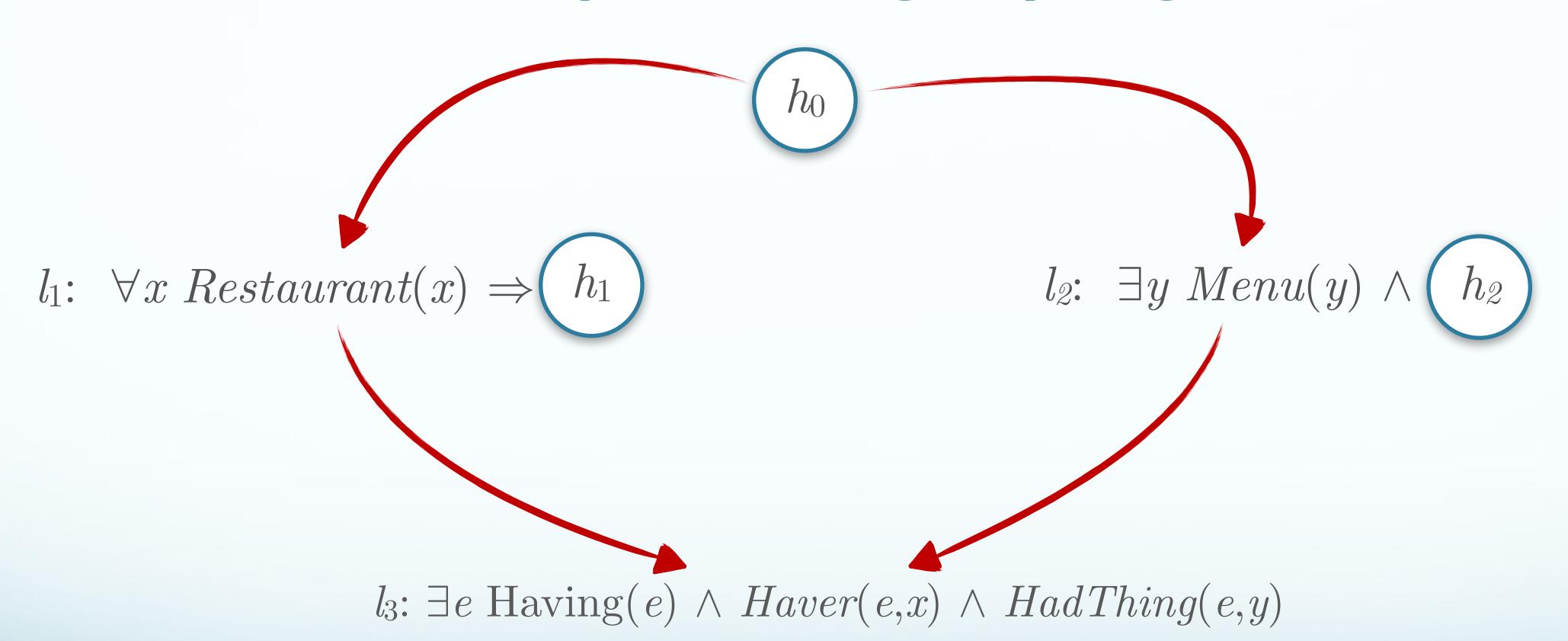
Scope Ambiguity, Again

- "Hole semantics" via Bos, (1996)
 - (h_n) \leftarrow this is a "hole"
- We will use this to stand in for portions of the quantifier statements
- We will then "plug" the "holes" ...why, semanticists, why?
 - Following the rules of dominance constraints
 - ullet An expression with hole h must be filled by a subordinate expression.





Scope Ambiguity, Again







Negation

- "No vegetarian restaurant serves meat."
- "All vegetarian restaurants do not serve meat."
 - $\forall x \ VegetarianRestaurant(x) \Rightarrow Serves(x, Meat)$
- These are semantically equivalent!
 - \neg [IF P, THEN Q] \Leftrightarrow P AND NOT Q
- For NLTK, use the hyphen/minus character: '-'





- Target representation:
 - $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$







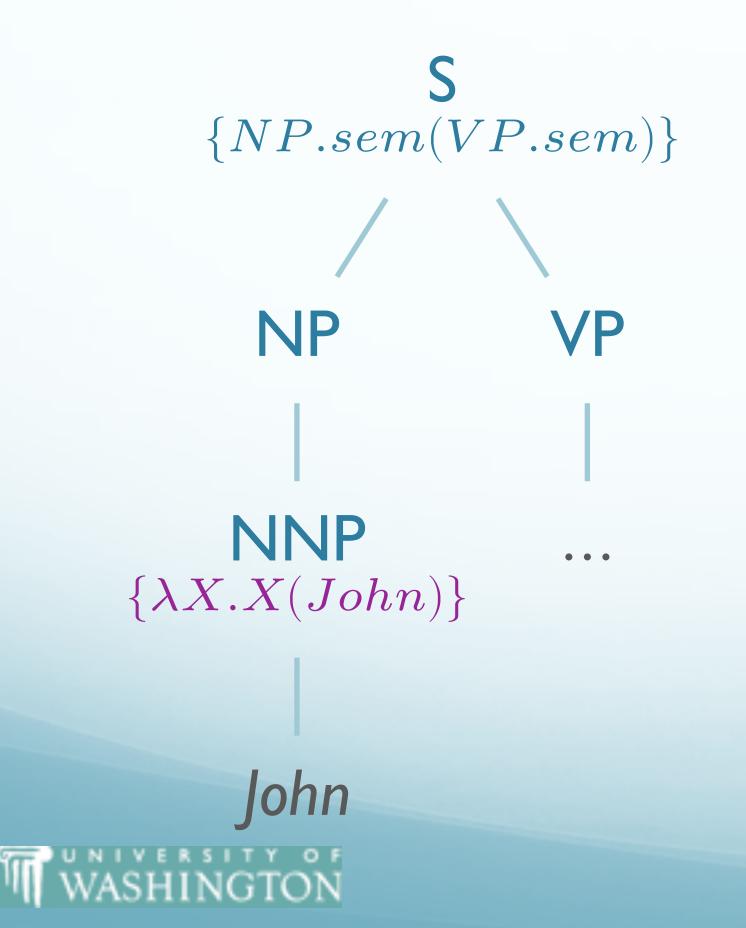


```
\{NP.sem(VP.sem)\}
                                         S \rightarrow NP VP
                                                              \{NP.sem(VP.sem)\}
  NNP
```





• $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$



```
S \rightarrow NP \ VP \{NP.sem(VP.sem)\}

NNP \rightarrow `John` \{\lambda X.X(John)\}

NP \rightarrow NNP \{NNP.sem\}

VP \rightarrow Verb \ NP \{Verb.sem(NP.sem)\}
```

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```
\{\lambda X.X(John)(VP.sem)\}
            NP
           NNP
WASHINGTON
```

$$S \rightarrow NP \ VP$$
 $\{NP.sem(VP.sem)\}$
 $NNP \rightarrow `John'$ $\{\lambda X.X(John)\}$
 $NP \rightarrow NNP$ $\{NNP.sem\}$
 $VP \rightarrow Verb \ NP$ $\{Verb.sem(NP.sem)\}$



```
\{VP.sem(John)\}
          NP
         NNP
WASHINGTON
```

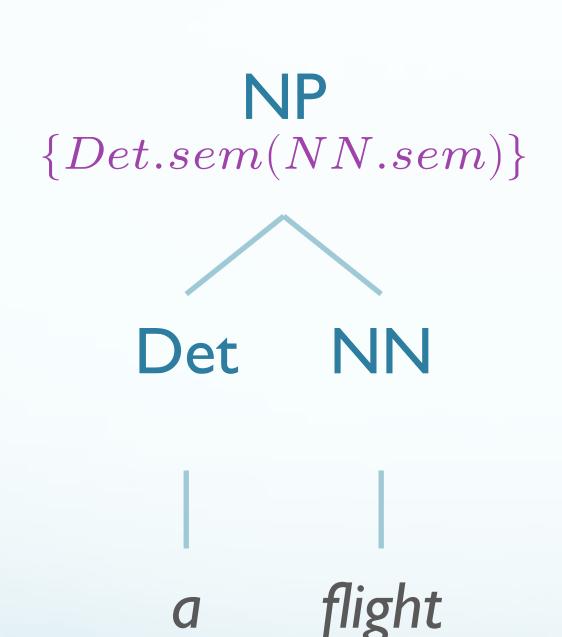
```
S \rightarrow NP \ VP \qquad \{NP.sem(VP.sem)\}

NNP \rightarrow `John' \qquad \{\lambda X.X(John)\}

NP \rightarrow NNP \qquad \{NNP.sem\}

VP \rightarrow Verb \ NP \qquad \{Verb.sem(NP.sem)\}
```

• $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$

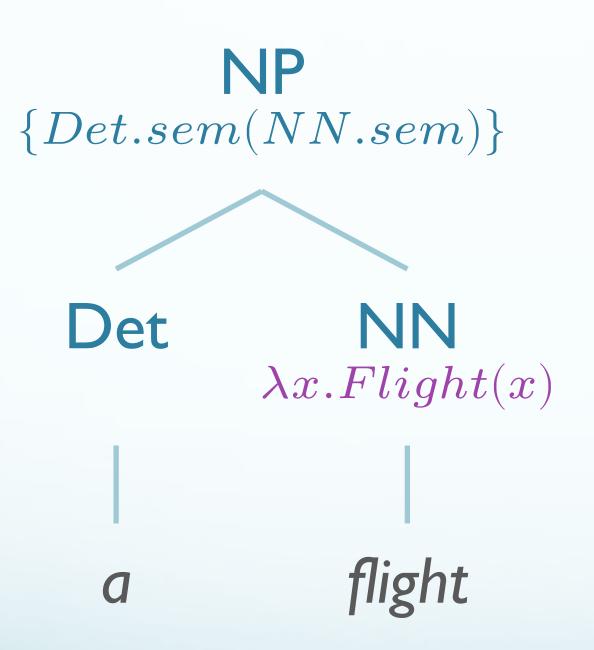


$$NP o Det \ NN$$

 $\{Det.sem(NN.sem)\}$



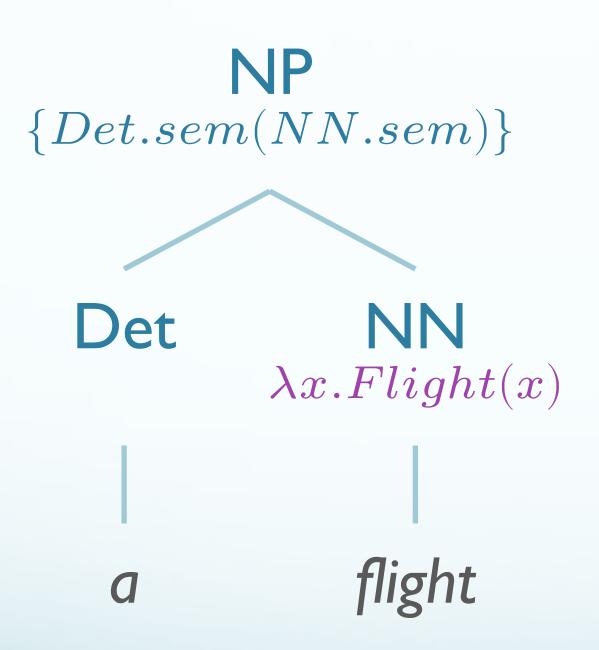




$$NP \rightarrow Det \ NN$$
 $NN \rightarrow 'flight'$

$$\{Det.sem(NN.sem)\}$$

 $\{\lambda x.Flight(x)\}$

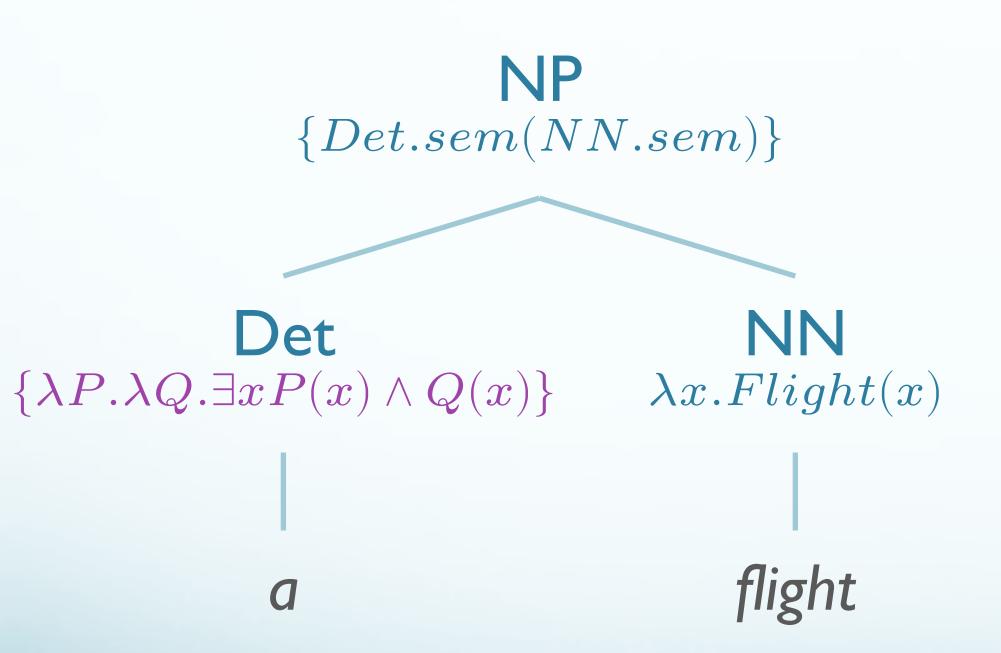


$$NP
ightarrow Det \ NN$$
 $NN
ightarrow ext{'flight'}$
 $Det
ightarrow ext{'a'}$

$$\{Det.sem(NN.sem)\}$$

$$\{\lambda x. Flight(x)\}$$

$$\{\lambda P.\lambda Q. \exists x \ P(x) \land Q(x) \}$$



$$NP
ightarrow Det \ NN$$
 $NN
ightarrow ext{'flight'}$
 $Det
ightarrow ext{'a'}$

$$\{Det.sem(NN.sem)\}$$

$$\{\lambda x.Flight(x)\}$$

$$\{\lambda P.\lambda Q.\exists x\ P(x)\ \land\ Q(x)\ \}$$

$$\begin{array}{c} \textbf{NP} \\ \{Det.sem(NN.sem)\} \end{array}$$

$$NP \rightarrow Det \ NN$$
 { $Det.sem(NN.sem)$ }
$$NN \rightarrow \text{`flight'} \qquad \{\lambda x.Flight(x)\}$$

$$Det \rightarrow \text{`a'} \qquad \{\lambda P.\lambda Q.\exists x \ P(x) \land Q(x) \}$$



• $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$

NP

 $\{Det.sem(NN.sem)\}$ $\{\lambda P.\lambda Q.\exists x P(x) \land Q(x)(\lambda x.Flight(x))\}$

$$NP
ightarrow Det \ NN$$
 $NN
ightarrow ext{'flight'}$
 $Det
ightarrow ext{'a'}$

$$\{Det.sem(NN.sem)\}$$

$$\{\lambda x. Flight(x)\}$$

$$\{\lambda P.\lambda Q. \exists x \ P(x) \land Q(x) \}$$



• $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$

$\begin{array}{c} \mathsf{NP} \\ \{Det.sem(NN.sem)\} \\ \{\lambda P.\lambda Q. \exists x P(x) \land Q(x)(\lambda x. Flight(x))\} \\ \{\lambda Q. \exists x (\lambda x. Flight(x))(x) \land Q(x)\} \end{array}$

$$NP \rightarrow Det \ NN$$
 { $Det.sem(NN.sem)$ }
$$NN \rightarrow \text{`flight'} \qquad \{\lambda x.Flight(x)\}$$

$$Det \rightarrow \text{`a'} \qquad \{\lambda P.\lambda Q.\exists x \ P(x) \land Q(x) \}$$

• $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$

$egin{aligned} \mathsf{NP} \ & \{Det.sem(NN.sem)\} \ & \{\lambda P.\lambda Q.\exists x P(x) \land Q(x)(\lambda x.Flight(x))\} \ & \{\lambda Q.\exists x (\lambda x.Flight(x))(x) \land Q(x)\} \ & \{\lambda Q.\exists x Flight(x) \land Q(x)\} \end{aligned}$

```
NP \rightarrow Det \ NN { Det.sem(NN.sem) } NN \rightarrow \text{`flight'} \qquad \{\lambda x.Flight(x)\} Det \rightarrow \text{`a'} \qquad \{\lambda P.\lambda Q.\exists x \ P(x) \land Q(x) \}
```

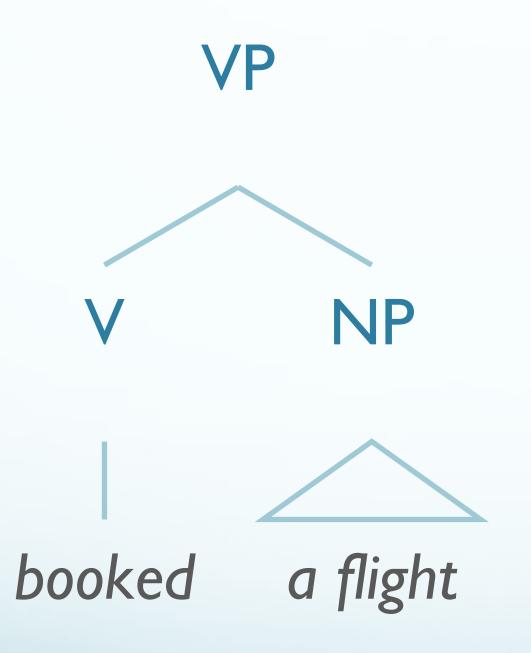
• $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$

```
 \begin{array}{c} \mathsf{NP} \\ \{Det.sem(NN.sem)\} \\ \{\lambda P.\lambda Q.\exists x P(x) \land Q(x)(\lambda x.Flight(x))\} \\ \{\lambda Q.\exists x (\lambda x.Flight(x))(x) \land Q(x)\} \\ \{\lambda Q.\exists x Flight(x) \land Q(x)\} \end{array}
```

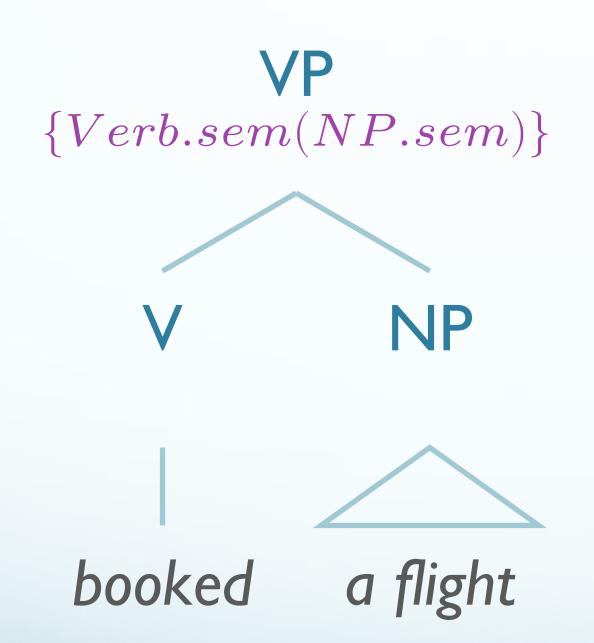
```
NP \rightarrow Det \ NN { Det.sem(NN.sem) } NN \rightarrow 'flight' { \lambda x.Flight(x) } \lambda P.\lambda Q.\exists x \ P(x) \land Q(x) } 'a flight' { \lambda Q.\exists x \ Flight(x) \land Q(x) }
```

WASHINGTON

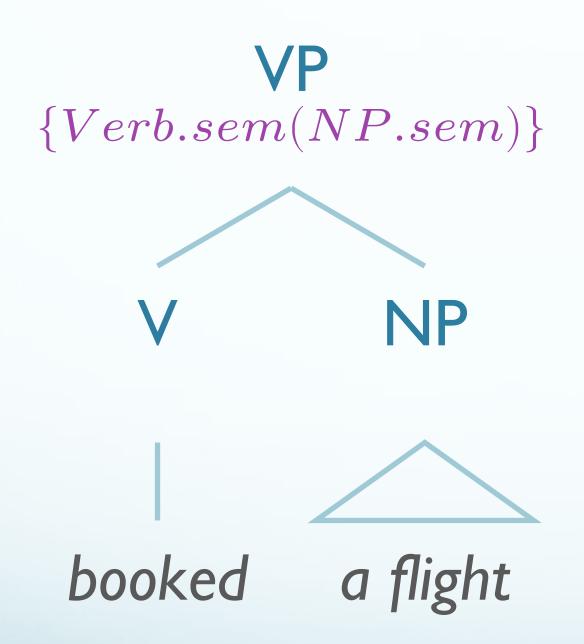




$$VP \rightarrow Verb \ NP \qquad \{ \ Verb.sem(NP.sem) \}$$
 `a flight` \quad \lambda Q.\equiv X \ Flight(x) \lambda Q(x) \ \rangle \quad \ \lambda \equiv \ \lambda \ \quad \ \lambda \ \quad \ \lambda \ \quad \ \quad \ \lambda \ \quad \quad \ \quad \ \quad \quad \ \quad \quad \ \quad \ \quad \quad \ \quad \quad \quad \quad \ \quad \



$$VP \rightarrow Verb \ NP \qquad \{ \ Verb.sem(NP.sem) \}$$
 'a flight'
$$\{ \ \lambda Q. \exists x \ Flight(x) \ \land \ Q(x) \ \}$$



```
Verb 
ightharpoonup 'booked' \{\lambda W.\lambda z. W(\lambda y. \exists eBooked(e) \land Booker(e,z) \land BookedThing(e,y))\} VP 
ightharpoonup Verb NP \qquad \{Verb.sem(NP.sem)\} 'a flight' \{\lambda Q. \exists x \ Flight(x) \land Q(x) \}
```

```
Verb.sem(NP.sem) \\ \lambda W. \lambda z. W(\lambda y. \exists eBooked(e) \land Booker(e,z) \land BookedThing(e,y))(\lambda Q. \exists x \ Flight(x) \land Q(x)) \\ \lambda z. (\lambda Q. \exists x \ Flight(x) \land Q(x))(\lambda y. \exists eBooked(e) \land Booker(e,z) \land BookedThing(e,y)) \\ \lambda z. \exists x \ Flight(x) \land (\lambda y. \exists eBooked(e) \land Booker(e,z) \land BookedThing(e,y))(x) \\ \lambda z. \exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e,z) \land BookedThing(e,x)) \\ \end{pmatrix}
```









• $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$

```
S VP.sem(John) 'booked a flight' \lambda z. \exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e,z) \land BookedThing(e, \boldsymbol{x})
```

 $\lambda z. \exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e,z) \land BookedThing(e,x)(John))$ $\exists x \ Flight(x) \land (\exists eBooked(e) \land Booker(e,John) \land BookedThing(e,x))$





```
\{ \lambda P.\lambda Q. \exists x \ P(x) \land Q(x) \}
Det \rightarrow 'a'
                              \{ \lambda P.\lambda Q. \forall x P(x) \Rightarrow Q(x) \}
Det \rightarrow 'every'
                              \{\lambda x. Flight(x)\}
NN \rightarrow \text{'flight'}
                              \{\lambda W.\lambda z. W(\lambda y. \exists eBooked(e) \land Booker(e,z) \land BookedThing(e,y))\}
Verb \rightarrow booked
                              \{\lambda X.X(John)\}
NNP \rightarrow 'John'
                              \{NNP.sem\}
NP \rightarrow NNP
                              \{Det.sem(NN.sem)\}
NP \rightarrow Det NN
                              \{NP.sem(VP.sem)\}
S \rightarrow NP VP
VP \rightarrow Verb NP
                              \{Verb.sem(NP.sem)\}
```



- $\neg \Box x \ Flight(x) \land (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x))$
- $\forall xFlight(x) \Rightarrow \neg (\exists eBooked(e) \land Booker(e, John) \land BookedThing(e, x)$



```
\{ \lambda P.\lambda Q. \neg \exists x \ P(x) \land Q(x) \mid \lambda P.\lambda Q. \forall x \ P(x) \Rightarrow \neg Q(x) \}
Det \rightarrow `no"
                                 \{ \lambda P.\lambda Q. \exists x \ P(x) \land Q(x) \}
Det \rightarrow 'a'
                                 \{ \lambda P.\lambda Q. \forall x P(x) \Rightarrow Q(x) \}
Det \rightarrow 'every'
                                 \{\lambda x. Flight(x)\}
NN \rightarrow \text{'flight'}
                                 \{\lambda W.\lambda z. W(\lambda y. \exists eBooked(e) \land Booker(e,z) \land BookedThing(e,y))\}
Verb \rightarrow `booked'
NNP \rightarrow 'John'
                                 \{\lambda X.X(John)\}
                                 \{NNP.sem\}
NP \rightarrow NNP
                                 \{Det.sem(NN.sem)\}
NP \rightarrow Det NN
                                 \{NP.sem(VP.sem)\}
S \rightarrow NP VP
                                \{Verb.sem(NP.sem)\}
VP \rightarrow Verb NP
```



What is the purpose of creating a dummy predicate for a lambda expression?

To help compose it with things to the left. 1

To help compose it with things to the right. 2

1 or 2, depending on the position in the tree ³

1 or 2, depending on the needs of the lambda function 4





Other Lambda Calculus





Adjectives

- Similar to nouns, but with an extra conjunction and dummy predicate:
 - "red" = $\lambda P \lambda x (red(x) \wedge P(x))$





Definite Article

- $a = \lambda P.\lambda Q.\exists x (P(x) \land Q(x))$
- $the = \lambda P.\lambda Q.\exists x(\forall y(P(y) \Leftrightarrow x=y \land Q(y)))$
- Roughly:
 - "For everything in the set of things P(y) (y is a thing in the set denoted by P)...
 - ...we are discussing one thing that could be in that set (y)
 - ...and happens to be the thing we are discussing (x)





Definite Article

- $the = \lambda P.\lambda Q.\exists x(\forall y(P(y) \Leftrightarrow x=y \land Q(y)))$
 - Bertrand Russel, "On Denoting" (1905).
 - The definite article isn't exactly the same as a constant (like "John")
 - Rather, it picks out a set of items from a set (the generic NN), and makes a strong assertion:
 - A) The book arrived.
 - B) A book arrived.
 - $A \models B$, but $B \not\models A$
 - Discussion [link]





Lexical Semantics





Lexical Semantics

- Thus far: $POS \rightarrow Word \{sem\}$
 - Can compose larger semantic formulae bottom-up this way
 - ...but we haven't really discussed what a "word" is, semantically.
- Lexical semantics:
 - How do we formally discuss what a "word" is?
 - How do we relate words to one another?
 - How do we differentiate/relate linked senses?





What is a Plant?

- There are more kinds of **plants** and animals in the rainforests than anywhere else on Earth. Over half of the millions of known species of **plants** and animals live in the rainforest. Many are found nowhere else. There are even **plants** and animals in the rainforest that we have not yet discovered.
- The Paulus company was founded in 1938. Since those days the product range has been the subject of constant expansions and is brought up continuously to correspond with the state of the art. We're engineering, manufacturing, and commissioning world-wide ready-to-run **plants** packed with our comprehensive know-how.



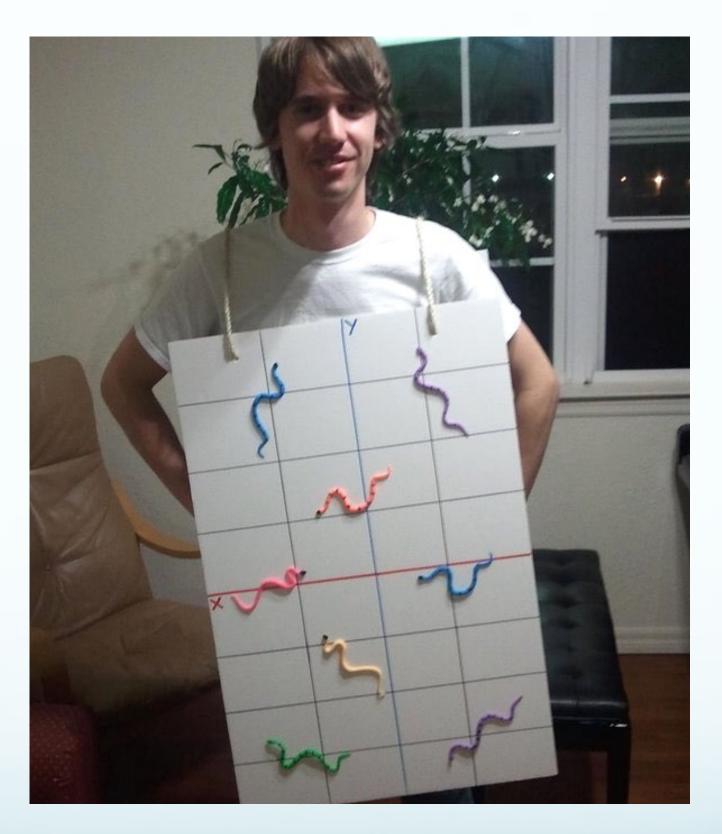


Lexical Semantics

...by way of dad-joke Halloween costumes. O



A Ceiling Fan



Snakes on a Plane





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Sources of Confusion

Homonymy

Polysemy

Synonymy

Antonymy

[Hypo/Hyper]-nymy





Sources of Confusion: Homonymy

- Words have same form but different meanings
 - Generally same POS, but unrelated meaning
 - bank_I (side of river)
 - bank₂ (financial institution)





Sources of Confusion: Homonymy

- Different types of Homonymy:
 - Homophones: same phonology, different orthographic form
 - two
 - to
 - too
 - Homographs: Same orthography, different phonology:
 - "lead" (metal)
 - "lead" (take somewhere)
- Why do we care?
 - Problem for applications: TTS, ASR transcription, IR





Sources of Confusion: Polysemy

- Multiple RELATED senses
 - e.g. bank: money, organ, blood
- Big issue in lexicography
 - Number of senses
 - Relations between senses
 - Differentiation





Sources of Confusion: Polysemy

- Example: [[serve]]
 - serve breakfast
 - serve Philadelphia
 - serve time





Sources of Confusion: Synonymy

- (near) identical meaning
- Substitutability
 - Maintains propositional meaning





Sources of Confusion: Synonymy

- Issues:
- Also has polysemy!
 - Shades of meaning other associations
 - price vs. fare
 - big vs. large
 - water vs. H₂0
- Collocational constraints
 - e.g. babbling brook vs. *babbling river
- Register:
 - social factors: e.g. politeness, formality





Sources of Confusion: Antonymy

- Opposition
- Typically ends of a scale
 - fast vs. slow
 - big vs. little
- Can be hard to distinguish automatically from synonyms





Sources of Confusion: Hyponomy

- instanceOf(x, y) relations:
- More General (hypernym) vs. more specific (hyponym)
 - dog vs. golden retriever
 - fruit vs. mango
- Organize as ontology/taxonomy





Word Sense Disambiguation

- Application of lexical semantics
- Goal: given a word in context, identify the appropriate sense
 - e.g. plants and animals in the rainforest
- Crucial for real syntactic & semantic analysis
 - Correct sense can determine
 - Available syntactic structure
 - Available thematic roles, correct meaning...





Robust Disambiguation

- More to semantics than predicate-argument structure
 - Select sense where predicates underconstrain
- Learning approaches
 - Supervised, bootstrapped, unsupervised
- Knowledge-based approaches
 - Dictionaries, taxonomies
- Contexts for sense selection





There are more kinds of **plants** and animals in the rainforests than anywhere else on Earth. Over half of the millions of known species of **plants** and animals live in the rainforest. Many are found nowhere else. There are even **plants** and animals in the rainforest that we have not yet discovered.

Biological Example

The Paulus company was founded in 1938. Since those days the product range has been the subject of constant expansions and is brought up continuously to correspond with the state of the art. We're engineering, manufacturing and commissioning worldwide ready-to-run **plants** packed with our comprehensive know-how. Our Product Range includes pneumatic conveying systems for carbon, carbide, sand, lime and many others. We use reagent injection in molten metal for the...

Industrial Example

Label the First Use of "Plant"





Roadmap

- Lexical Semantics
 - Motivation & Definitions
 - Word Senses
 - Tasks:
 - Word sense disambiguation
 - Word sense similarity
 - Distributional Similarity





Disambiguation: Features

- Part of Speech
 - Of word and neighbors
- Morphologically simplified form
- Words in neighborhood
 - How big is "neighborhood?"
 - Is there a single optimal size? Why?





Disambiguation: Features

- (Possibly shallow) Syntactic analysis
 - predicate-argument relations
 - modification (complements)
 - phrases
- Collocation
 - words in specific relation
 - Predicate-Argument, or (+/-)1 word index
- Co-occurrence
 - bag of words





Disambiguation: Evaluation

- Ideally, end-to-end evaluation with WSD component
 - Demonstrate real impact of technique in system
 - Difficult, expensive, still application specific
- Typically intrinsic, sense-based
 - Accuracy, precision, recall
 - SENSEVAL/SEMEVAL: all words, lexical sample





WSD Evaluation

- Baseline:
 - Most frequent sense
- Ceiling:
 - Human inter-rater agreement
 - 75-80% fine
 - 90% coarse





Roadmap

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 - Distributional Similarity





Word Sense Similarity

- Synonymy:
 - True propositional substitutability is rare, slippery

- Word similarity (semantic distance)
 - Looser notion, more flexible





Word Sense Similarity

- Appropriate to applications:
 - IR, summarization, MT, essay scoring
 - Don't need binary +/— synonym decision
 - Want terms/documents that have high similarity
- Approaches:
 - Distributional
 - Thesaurus-based





Similarity vs. Relatedness

- Similarity:
 - car, bicycle
 - nickel < coin < currency

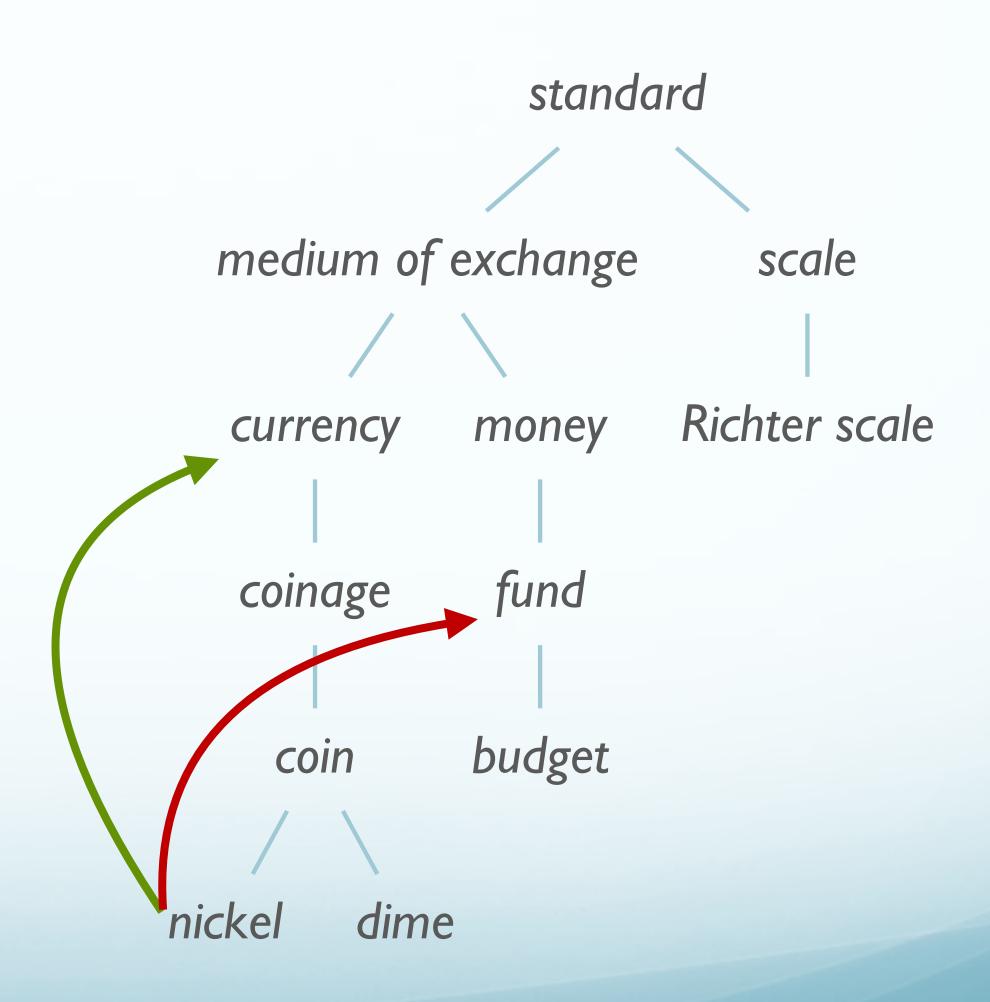
- Related:
 - car, gasoline
 - coin, budget





Thesaurus-Based:

- Build ontology of senses
 - e.g. WordNet
 - Use distance to infer similarity/relatedness:





Roadmap

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 - Word sense similarity
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Distributional Similarity

- "You shall know a word by the company it keeps!" (Firth, 1957)
 - A bottle of tezgüino is on the table.
 - Everybody likes tezgüino.
 - Tezgüino makes you drunk.
 - We make tezgüino from corn.
- Tezguino; corn-based alcoholic beverage. (From Lin, 1998a)





Distributional Similarity

- Represent 'company' of word such that similar words will have similar representations
 - 'Company' = context
- Word represented by context feature vector
 - Many alternatives for vector
- Initial representation:
 - 'Bag of words' binary feature vector
 - Feature vector length N, where N is size of vocabulary
 - $f_i=1$ if $word_i$ within window size w of $word_0$





Context Feature Vector

	arts boil		dat	functio	larg	suga	summariz	wat
			a	n	e	r	ed	er
Apricot	0	l	0	0	l	I	0	I
Pineapple	0	l	0	0	I	I	0	I
Digital	0	0	ı	I	I	0		0
Informatio n	0	0			1	0		0





Distributional Similarity Questions

- What is the right neighborhood?
 - What is the context?
- How should we weight the features?
- How can we compute similarity between vectors?



