

CKY Parsing

LING 571 — Deep Processing Techniques for NLP

October 8, 2018

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Start recording!

Misc. & Announcements

HW #2

- Due tonight, 11:00pm Pacific
- Grammar output format:
 1. Terminals quoted (single or double)
 2. One production per line
 - *Optionally*, RHS alternates with vertical bar/pipe character: |
 3. Start symbol is first nonterminal encountered in file

Indigenous Peoples' Day

- Seattle/Sealth
- For those of you taking 550:
 - The Lushootseed spelling [IPA] of Chief Seattle/Sealth:
 - siʔaɫ [ˈsiʔa:ɫ]
- Duwamish — Dx^wdəwʔabš [dx^wdəwʔabʃ]



Indigenous Peoples' Day

- Studying non-English languages gives more holistic insight for NLP tasks
 - Many interesting phenomena in non-Indo-European languages
- Lushootseed exhibits debatable distinction between verbs and nouns
 - **?uǰ^w** ti **sbiaw**
goes that-which **is-a-coyote**
"The/a coyote goes"
 - **sbiaw** ti **?uǰ^w**
is-a-coyote that-which **goes**
"The one who goes is a coyote" via [Beck, 2013](#)
- (Translation distinction provided for clarity — semantically equivalent)

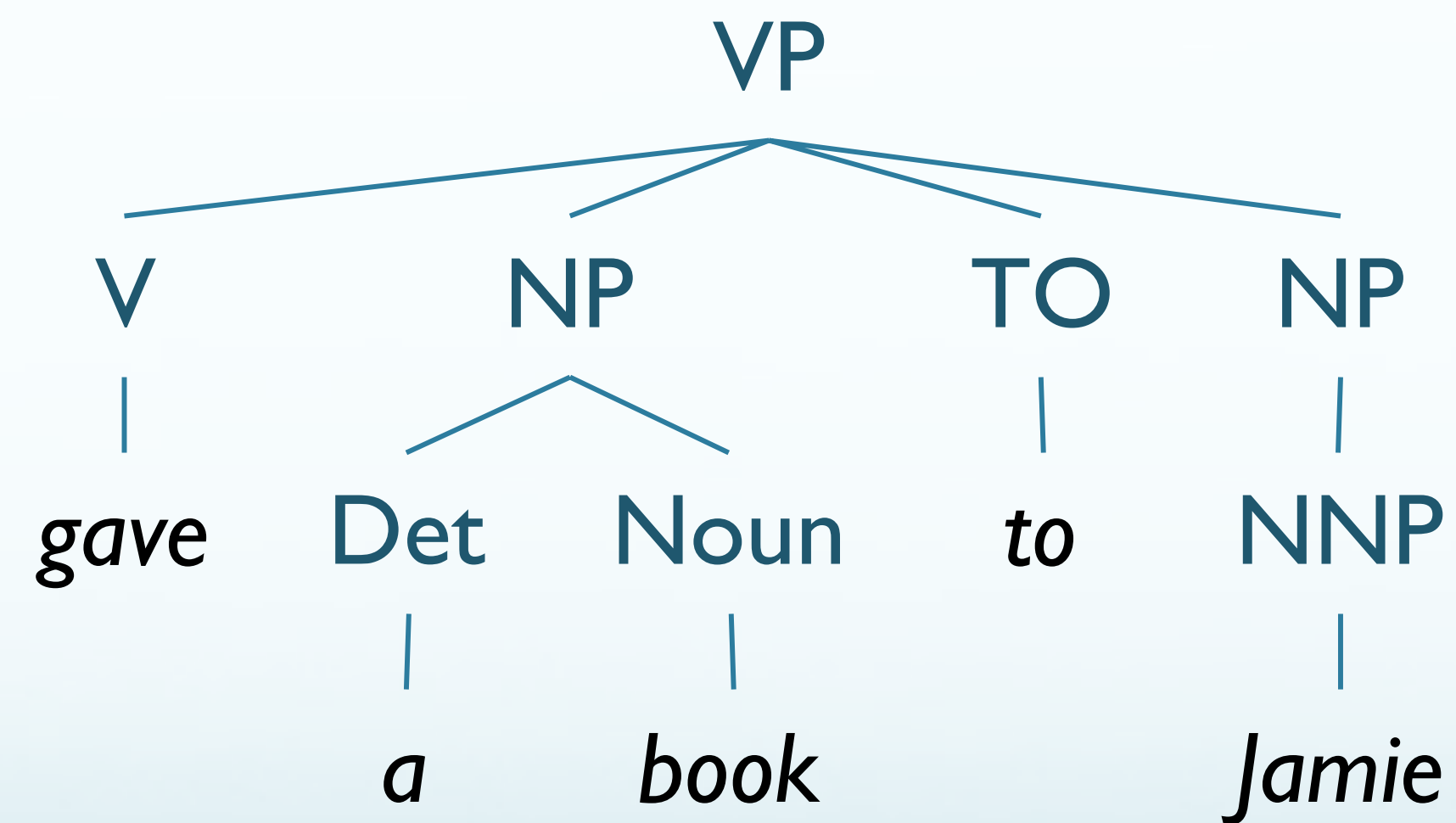
Indigenous Peoples' Day

- UW American Indian Studies Courses
- (Sometimes including language courses, e.g. Southern Lushootseed)

Variation in CNF: Binarization

Original Rule

$VP \rightarrow V NP TO NP$



Variation in CNF: Binarization

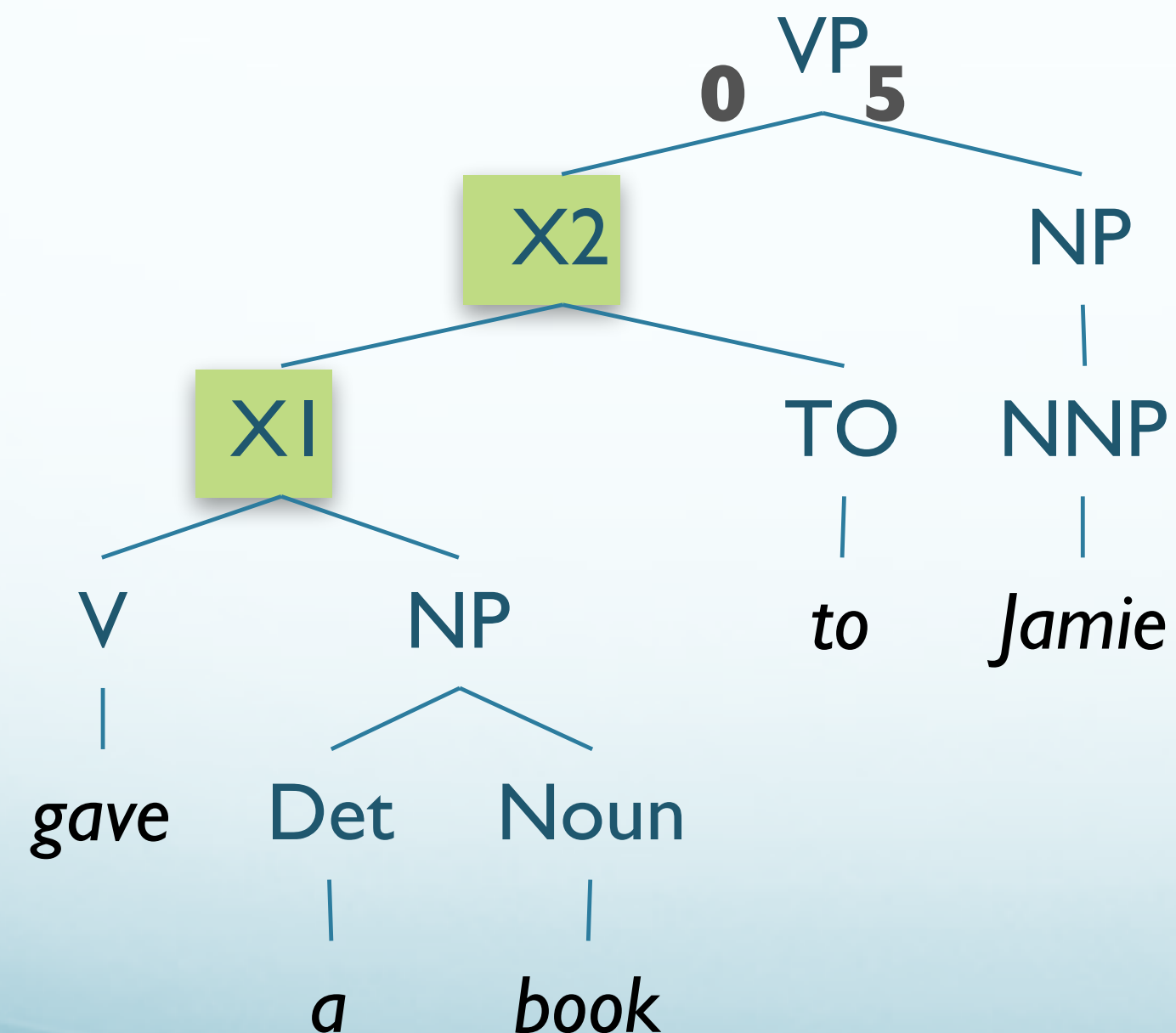
Original Rule

$VP \rightarrow V NP TO NP$

Left to Right Reduction

$VP \rightarrow X1 TO NP$ $X1 \rightarrow V NP$

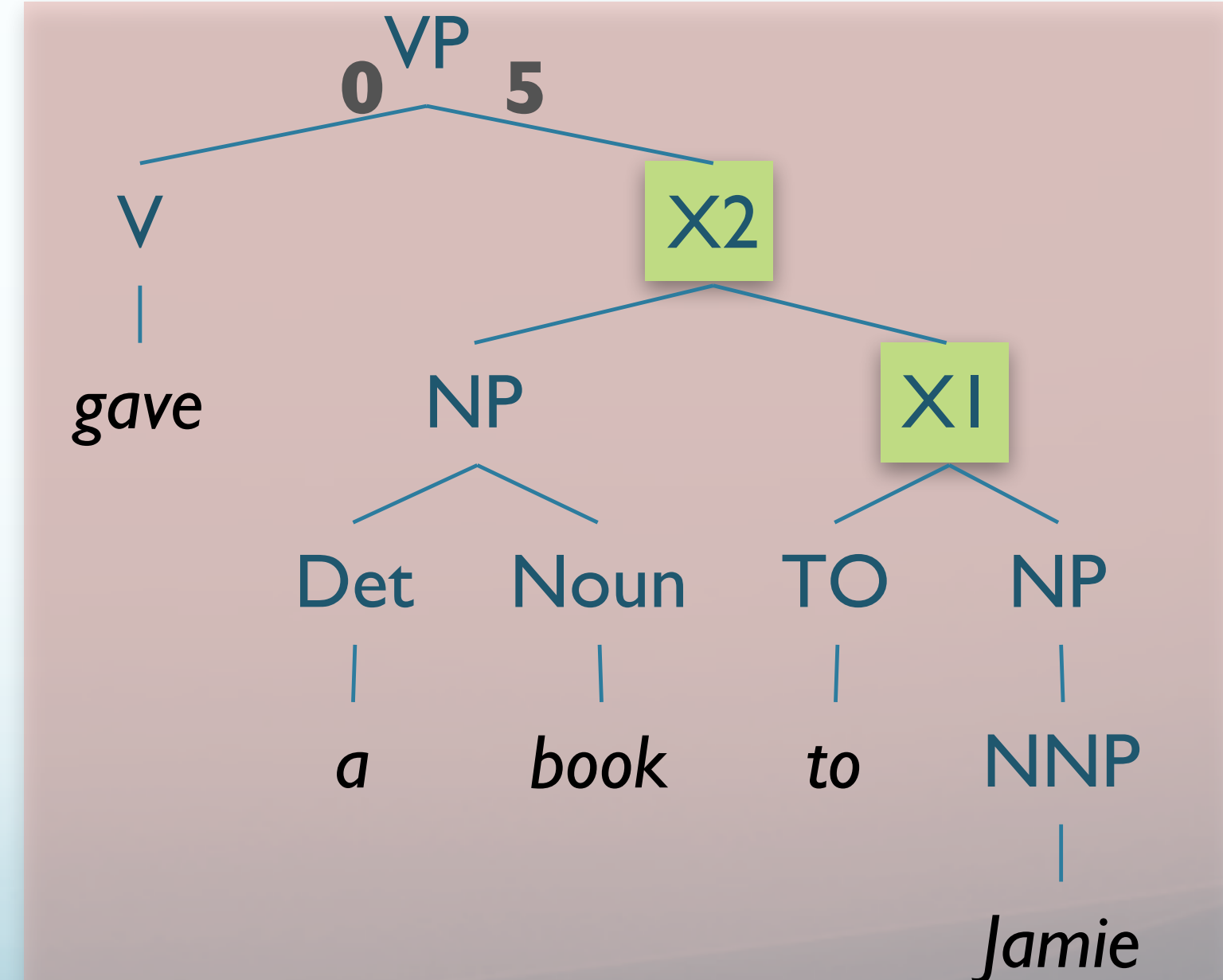
$VP \rightarrow X2 NP$ $X2 \rightarrow X1 TO$



Right to Left Reduction

$VP \rightarrow V NP X1$ $X1 \rightarrow TO NP$

$VP \rightarrow V X2$ $X2 \rightarrow NP X1$



Roadmap

- CKY Parsing Algorithm
 - Dynamic programming structure
 - Algorithm and example
 - Analysis & Discussion
- Probabilistic CFGs
 - Motivation: Ambiguity
 - Augmenting CFGs with probabilities

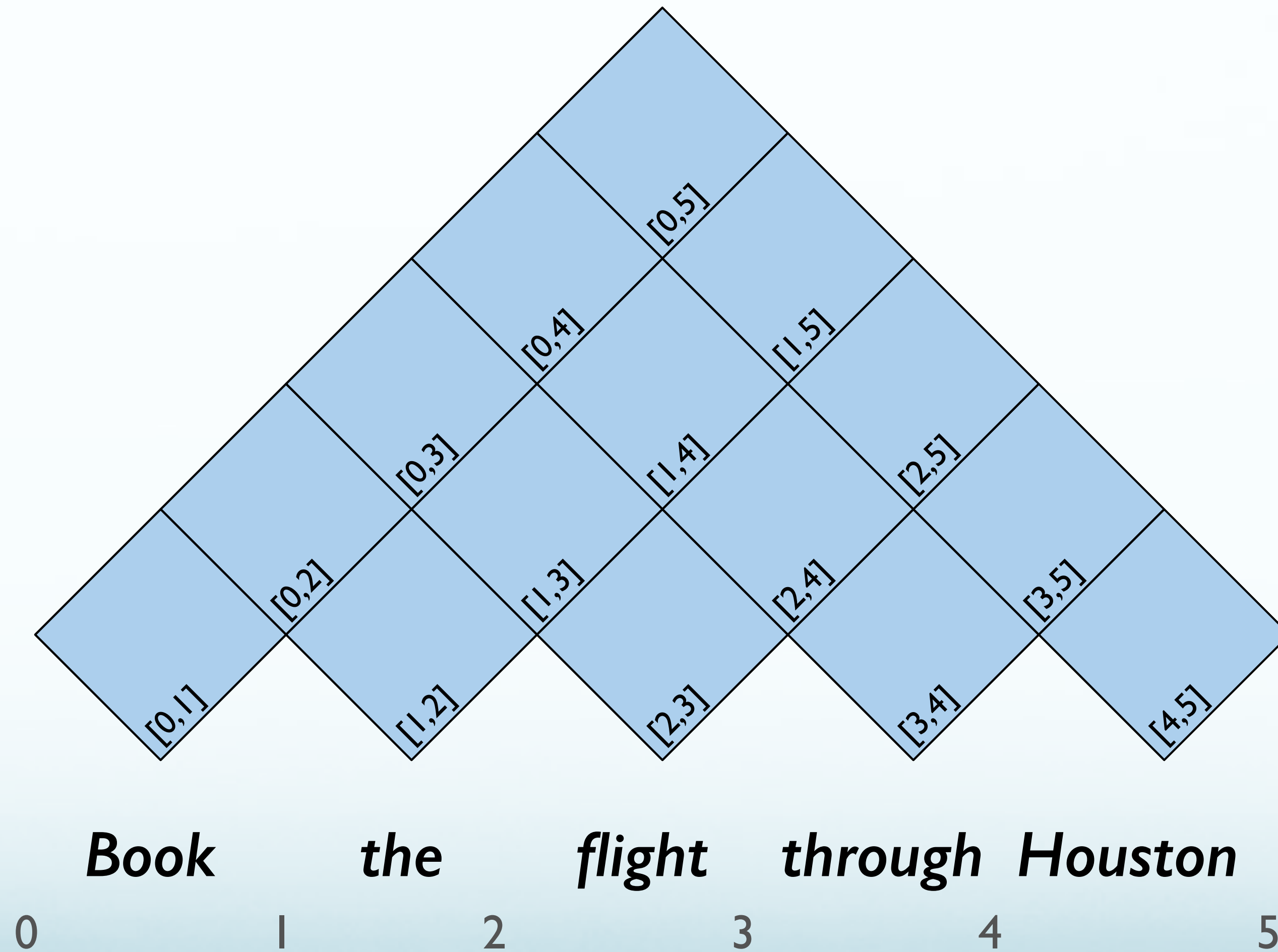
CKY

- Given an input string S of length n
- Build table $(n + 1) \times (n + 1)$
 - Indexes correspond to inter-word positions
 - $_0$ Book $_1$ that $_2$ flight $_3$
- Each cell $[i, j]$ contains SETS $\{ \}$ of non-terminals with derivations spanning i, j
 - $[j - 1, j]$ contains pre-terminals
 - if $[0, n]$ contains the start symbol, the sentence is **accepted**

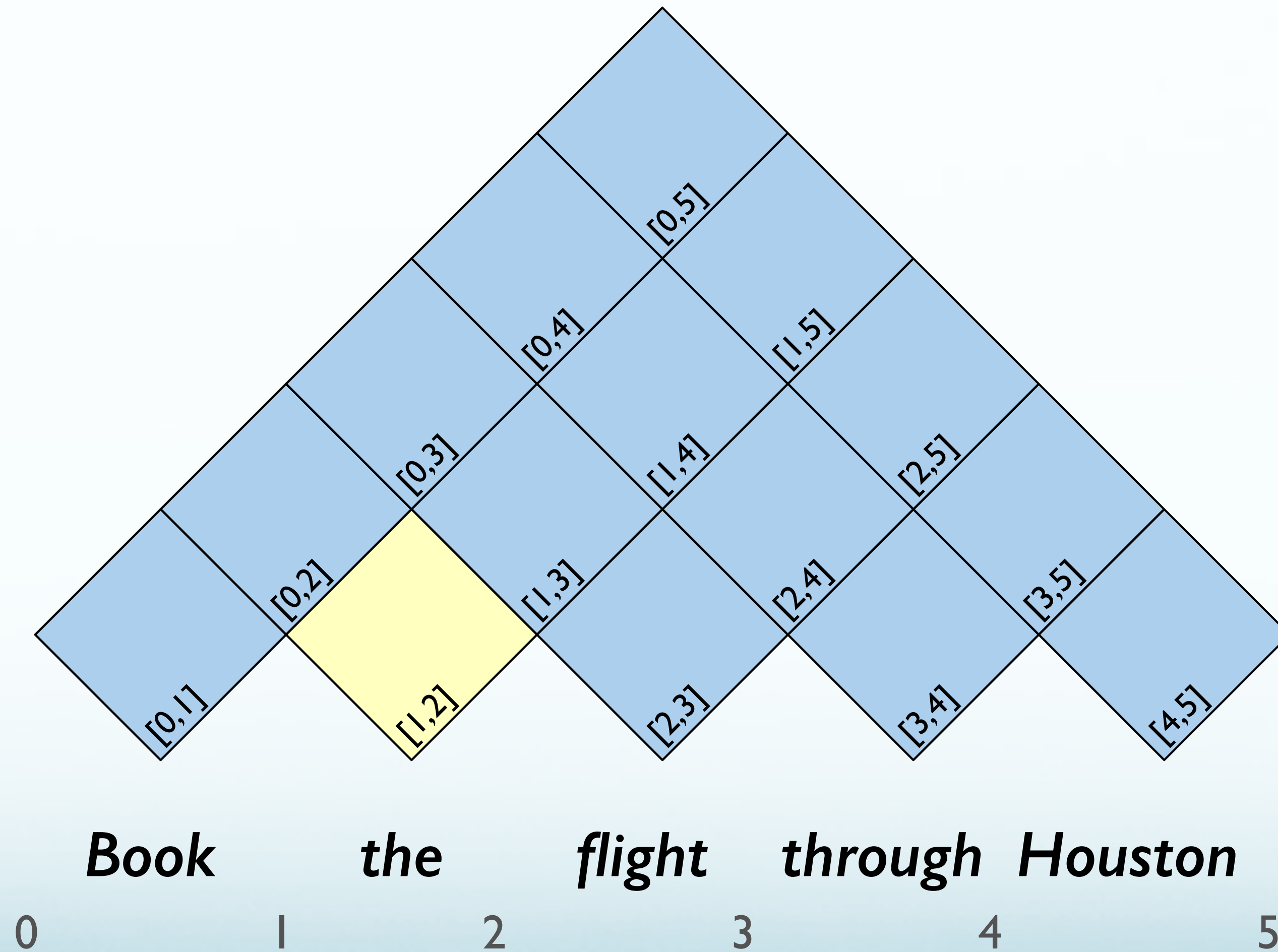
CKY Matrix

<i>Book</i>	<i>the</i>	<i>flight</i>	<i>through</i>	<i>Houston</i>
[0,1]	[0,2]	[0,3]	[0,4]	[0,5]
	[1,2]	[1,3]	[1,4]	[1,5]
		[2,3]	[2,4]	[2,5]
			[3,4]	[3,5]
				[4,5]

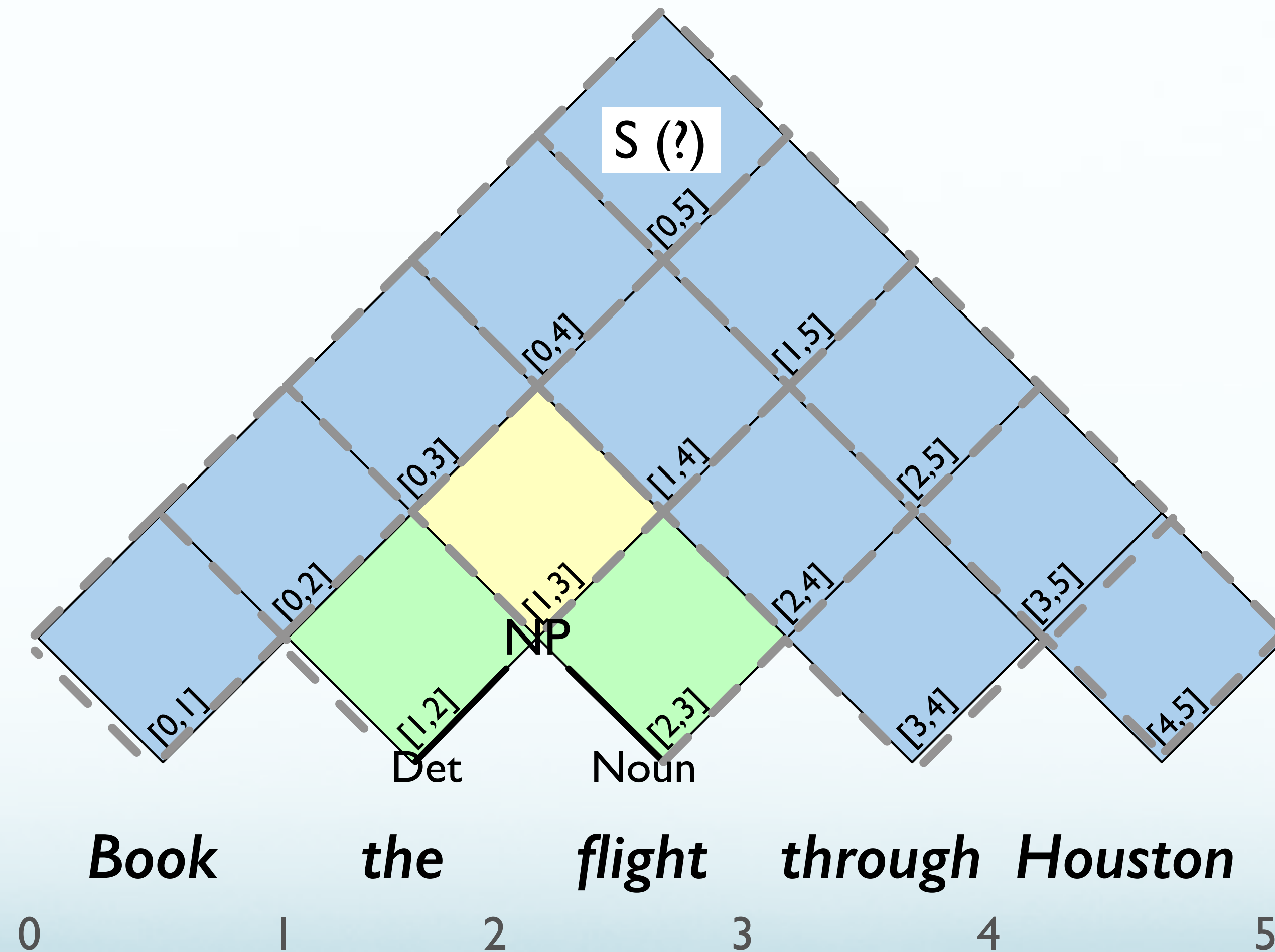
CKY Matrix



CKY Matrix



CKY Matrix

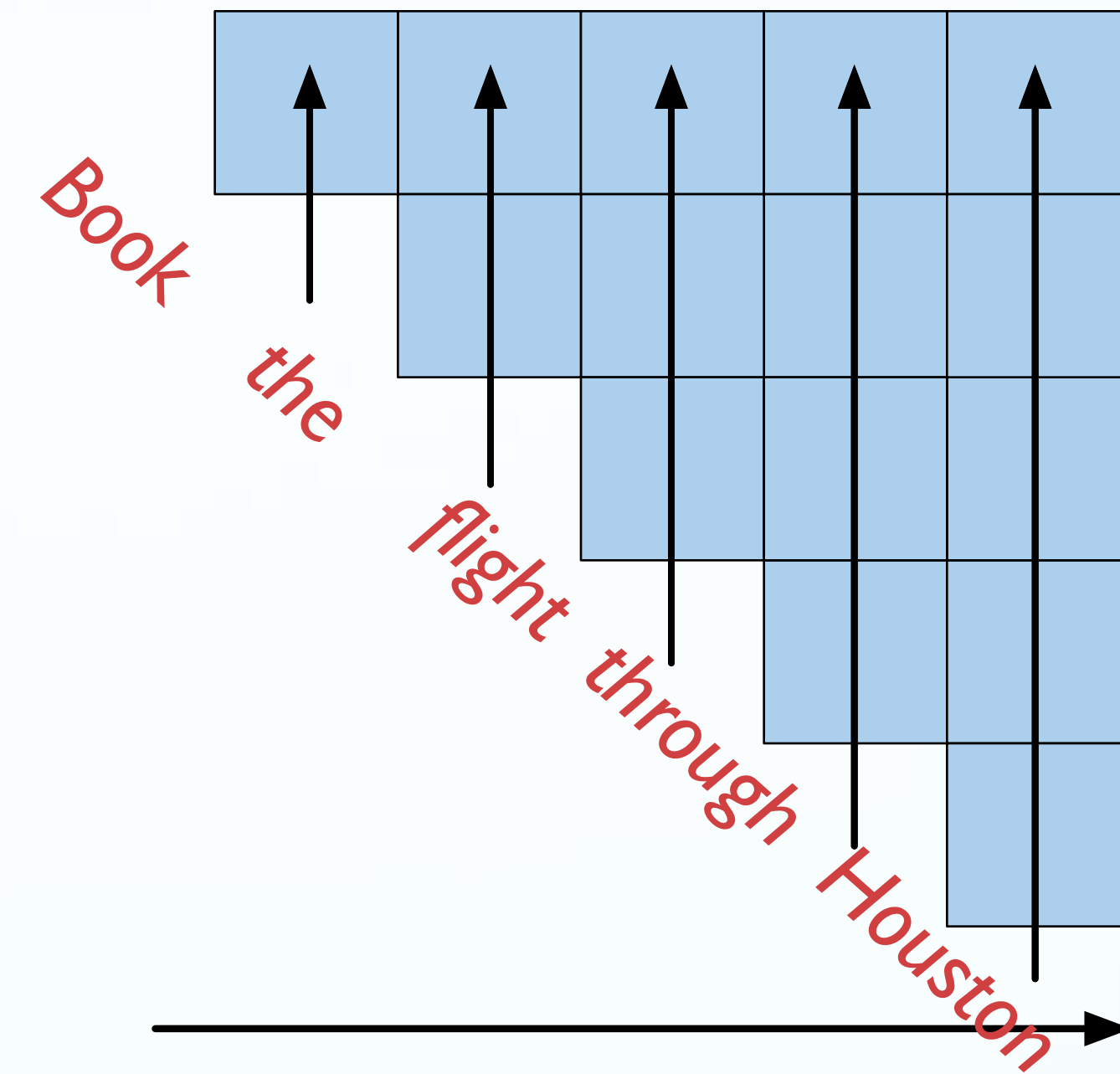


Dynamic Programming in CKY

- Key idea:
 - for $i < k < j$
 - ...and a parse spanning substring $[i, j]$
 - $\exists k$ such that there are parses spanning $[i, k]$ and $[k, j]$
 - We can construct parses for whole sentences by building from these partial parses
- So to have a rule $A \rightarrow B C$ in $[i, j]$
 - Must have B in $[i, j]$ and C in $[k, j]$ for some $i < k < j$
 - CNF forces this for all $j > i + 1$

CKY

- Table fills:
 - Column-by-column, left-to-right
 - bottom-to-top
- Why?
 - To fill each cell, must have access to all sub-spans
 - For cell $[i, j]$, must be able to access all cells $[i, k]$ and $[k, j]$ where $i < k < j$
 - Allows online sentence analysis
 - Works across input string as it arrives



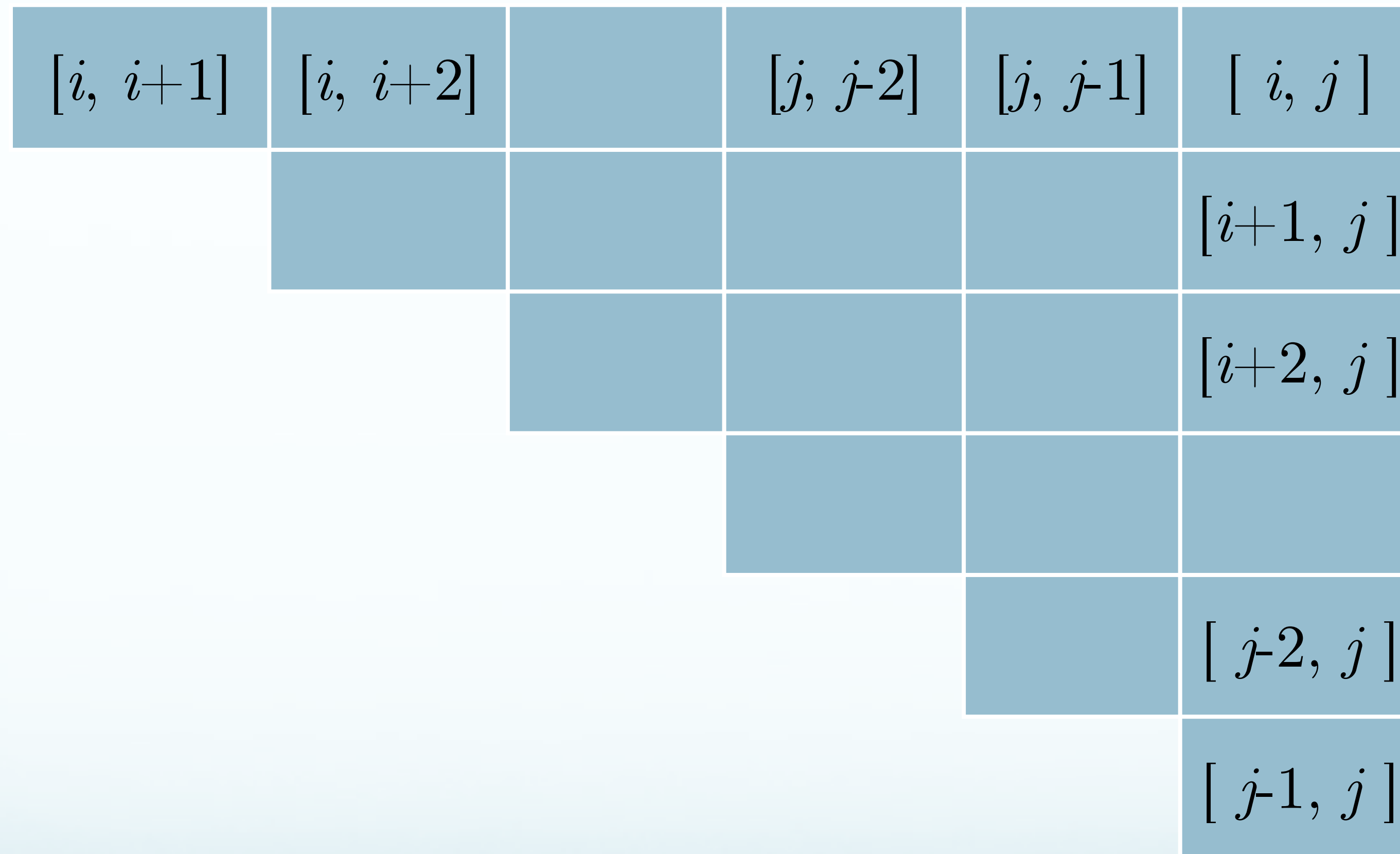
CKY Algorithm

```
function CKY-PARSE(words, grammar) returns table
for j ← from 1 to LENGTH(words) do
  table[ j - 1, j ] ← { A | A → words[ j ] ∈ grammar }
  for i ← from j - 2 downto 0 do
    for k ← i + 1 to j - 1 do
      table[ i, j ] ← table[ i, j ] ∪
        { A | A → BC ∈ grammar
          B ∈ table[ i, k ],
          C ∈ table[ k, j ] }
```

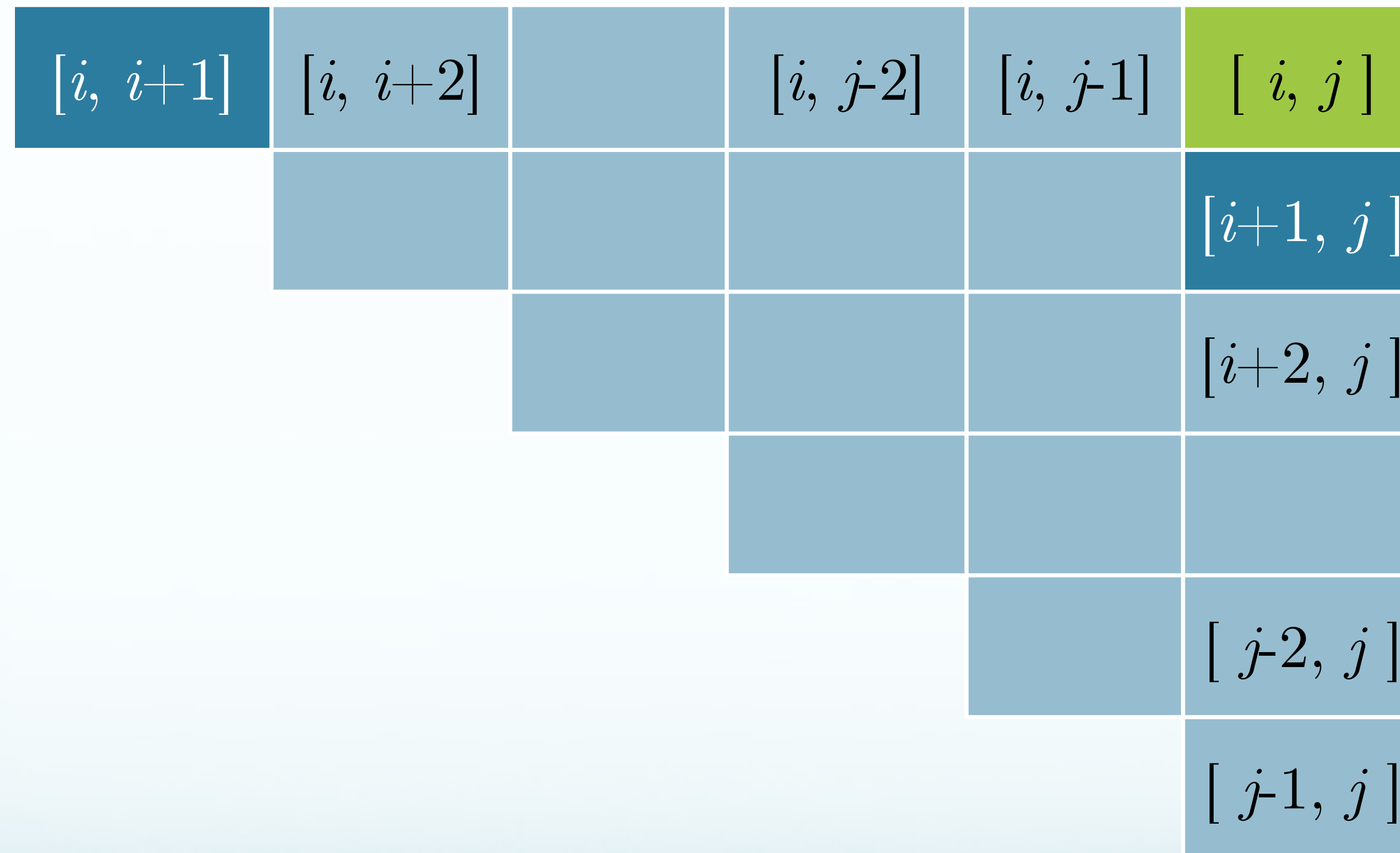
- Left-to-right, bottom-to-top
- Sliding *k* as the pivot for child nodes
- Filling the cell with set of applicable rules

Filling Cell $[i, j]$

For cell $[i, j]$, find rule spanning cells $[i, k]$ and $[k, j]$ where $i < k < j$

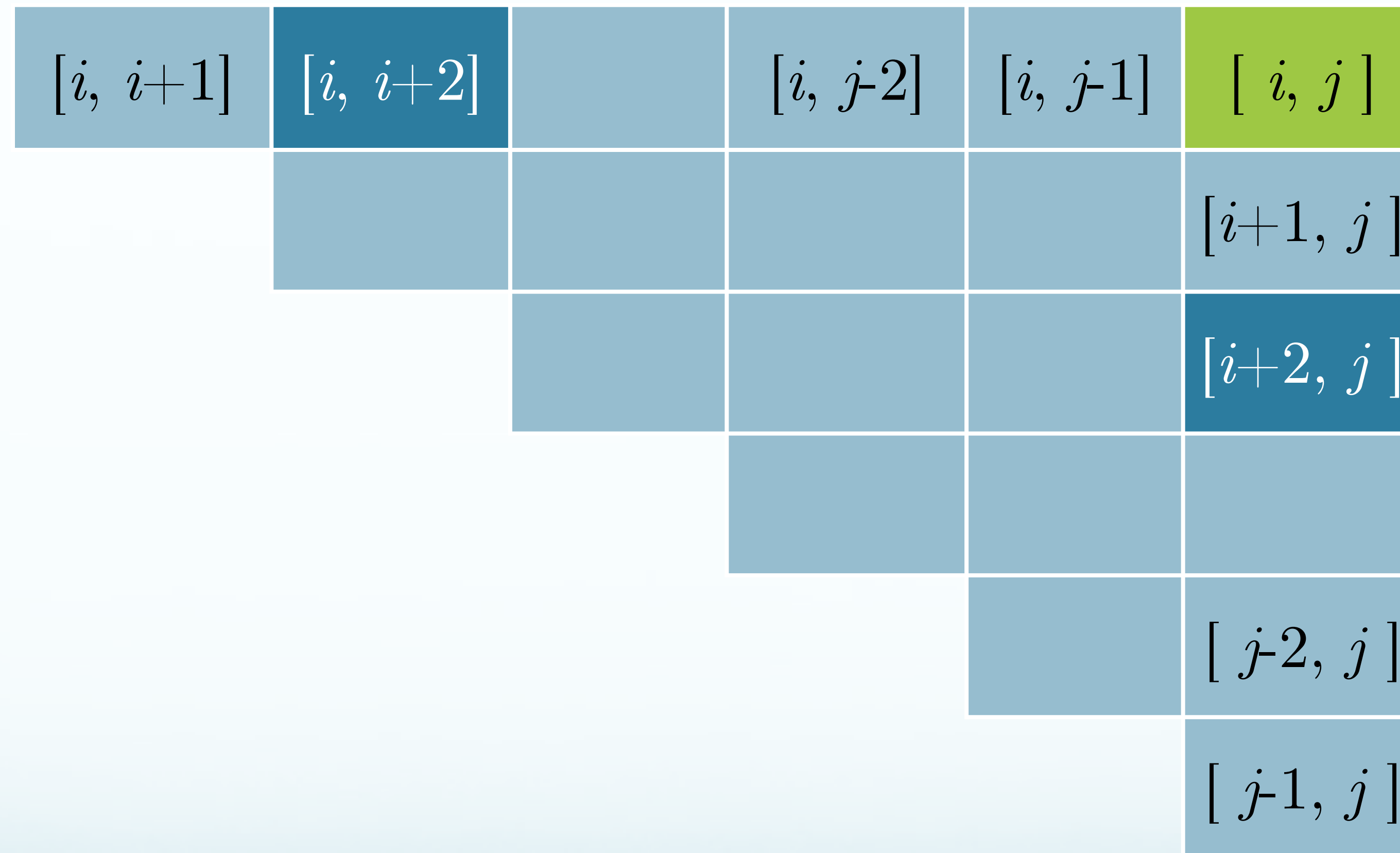


Filling Cell $[i, j]$



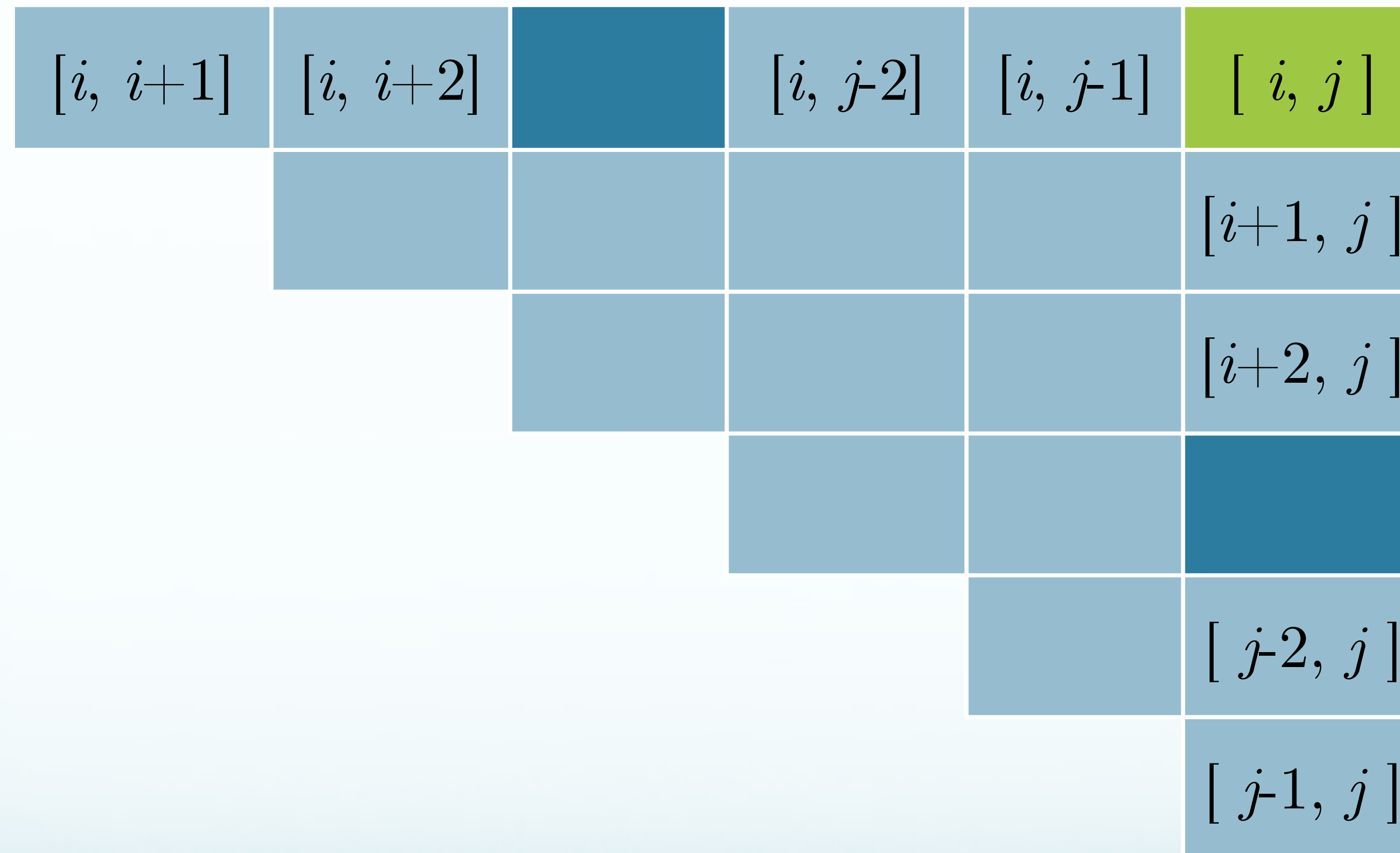
For cell $[i, j]$, find rule spanning cells $[i, k]$ and $[k, j]$ where $i < k < j$

Filling Cell $[i, j]$



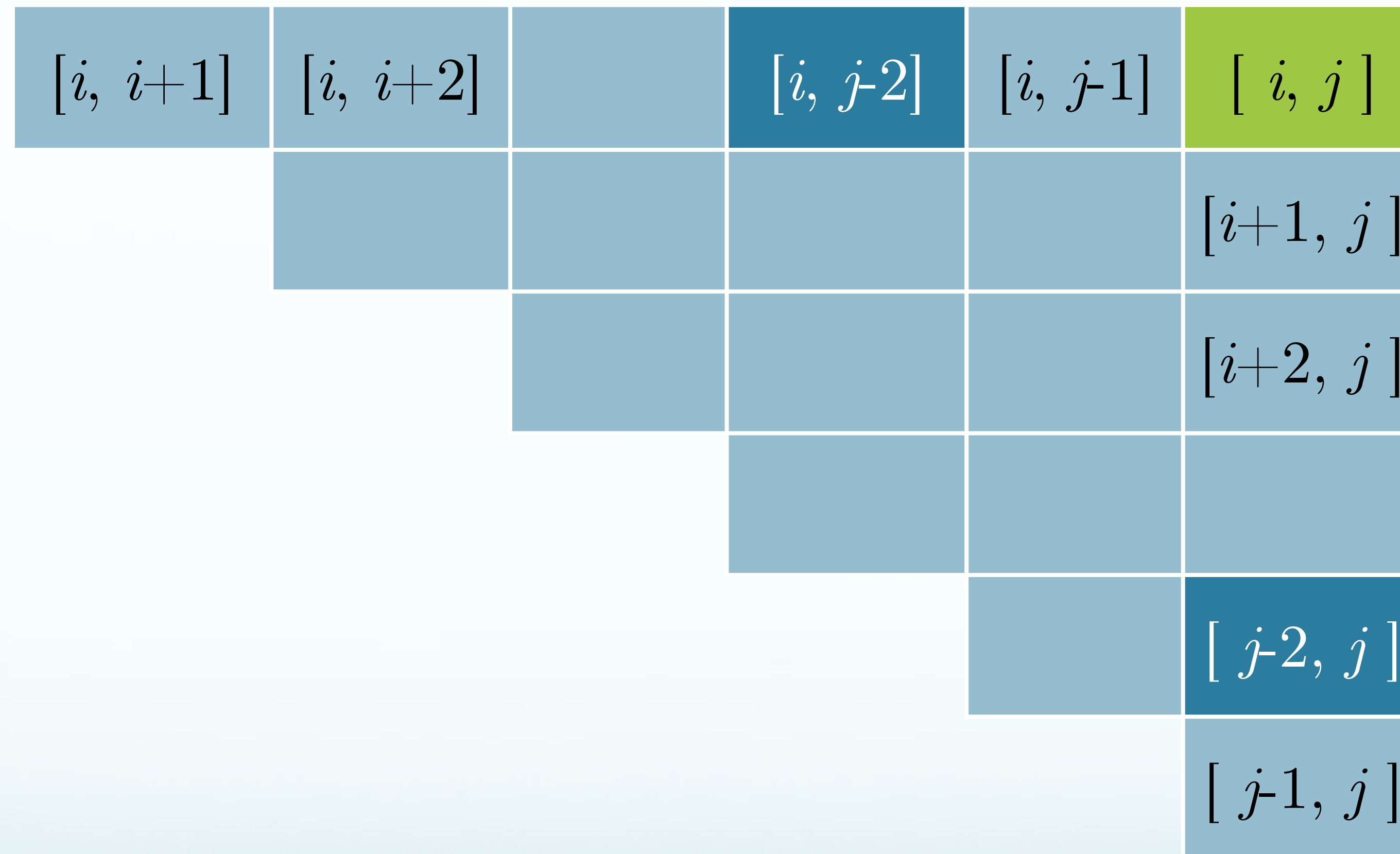
For cell $[i, j]$, find rule spanning cells $[i, k]$ and $[k, j]$ where $i < k < j$

Filling Cell $[i, j]$



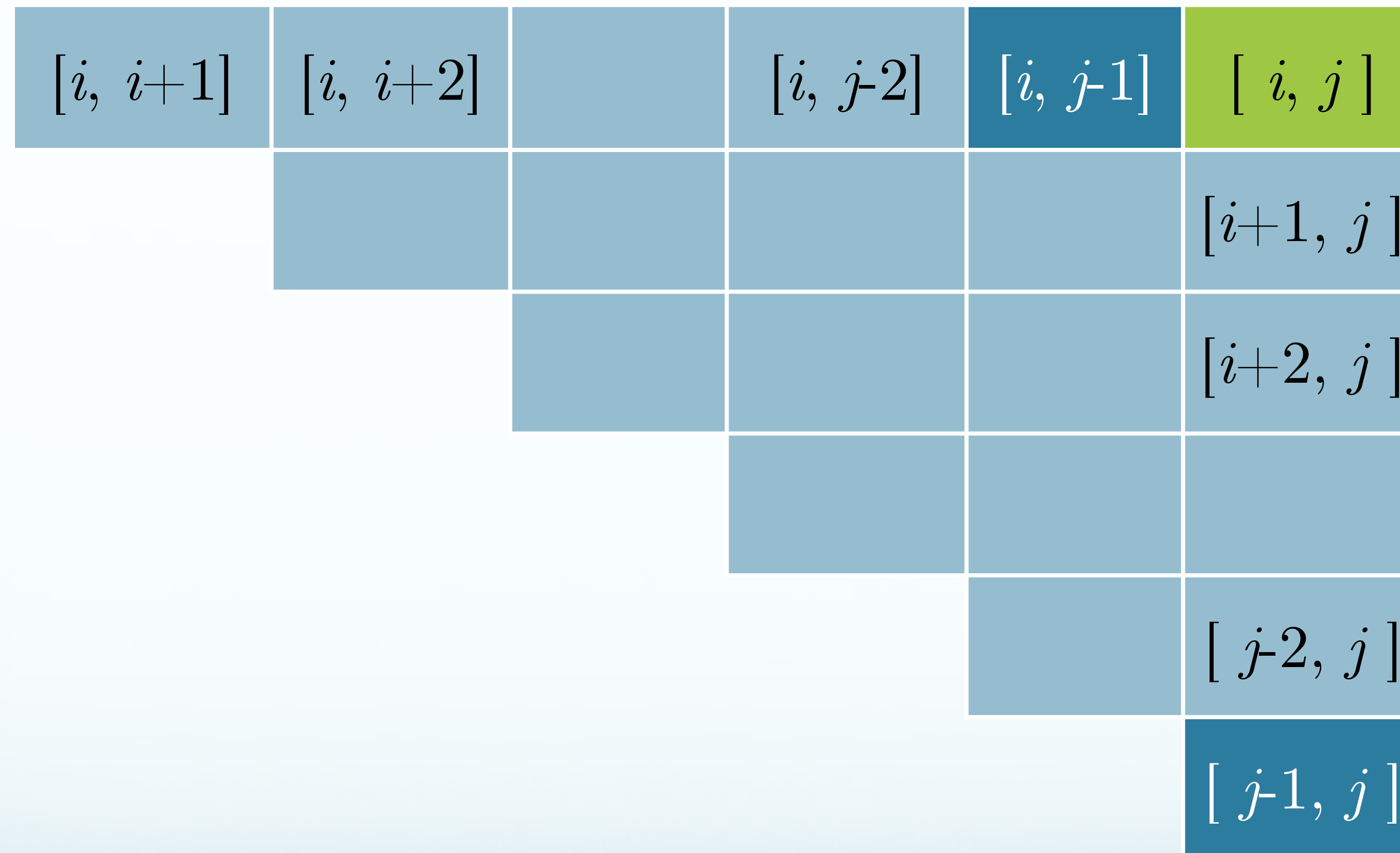
For cell $[i, j]$, find rule spanning cells $[i, k]$ and $[k, j]$ where $i < k < j$

Filling Cell $[i, j]$



For cell $[i, j]$, find rule spanning cells $[i, k]$ and $[k, j]$ where $i < k < j$

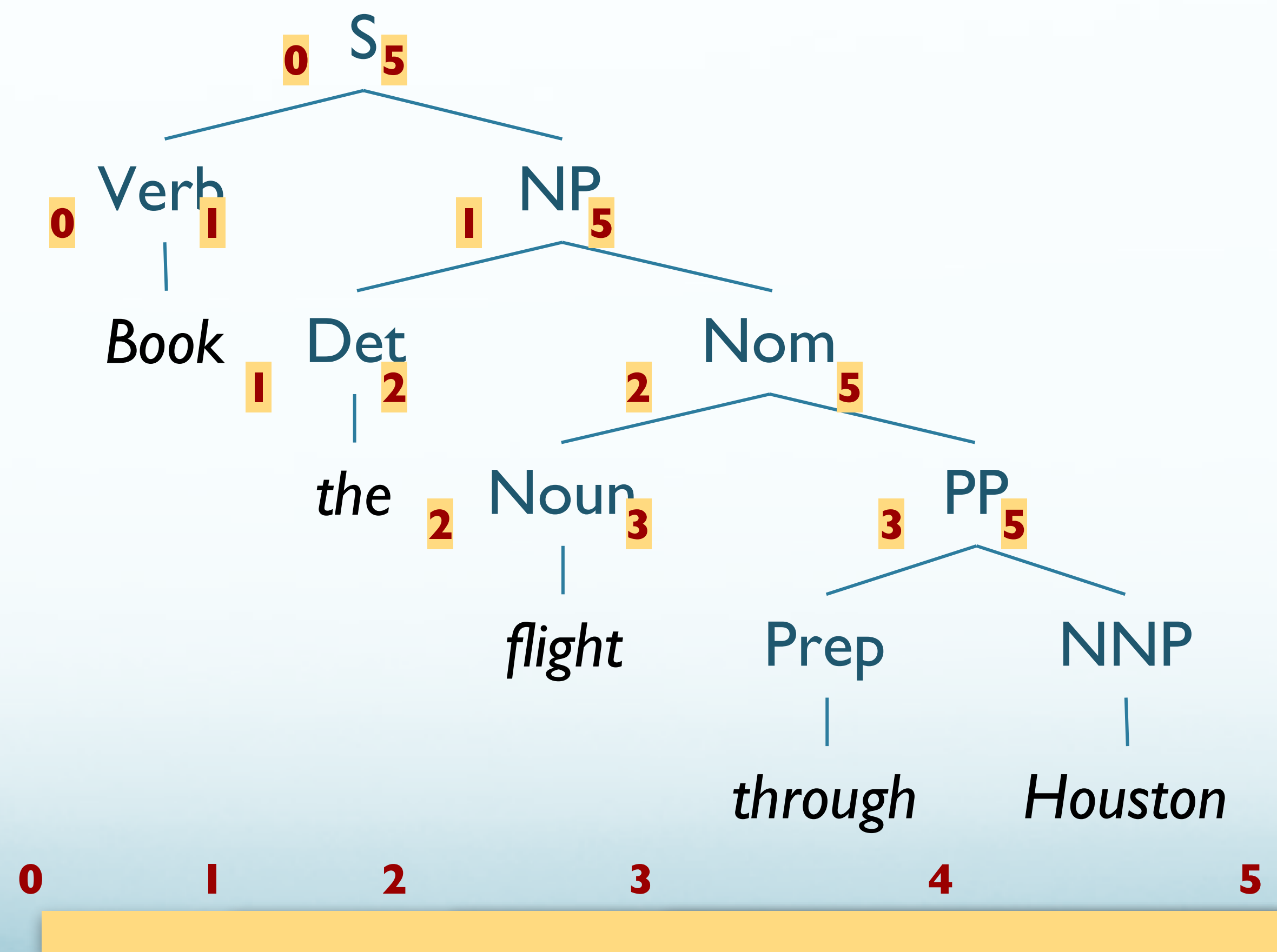
Filling Cell $[i, j]$



For cell $[i, j]$, find rule spanning cells $[i, k]$ and $[k, j]$ where $i < k < j$

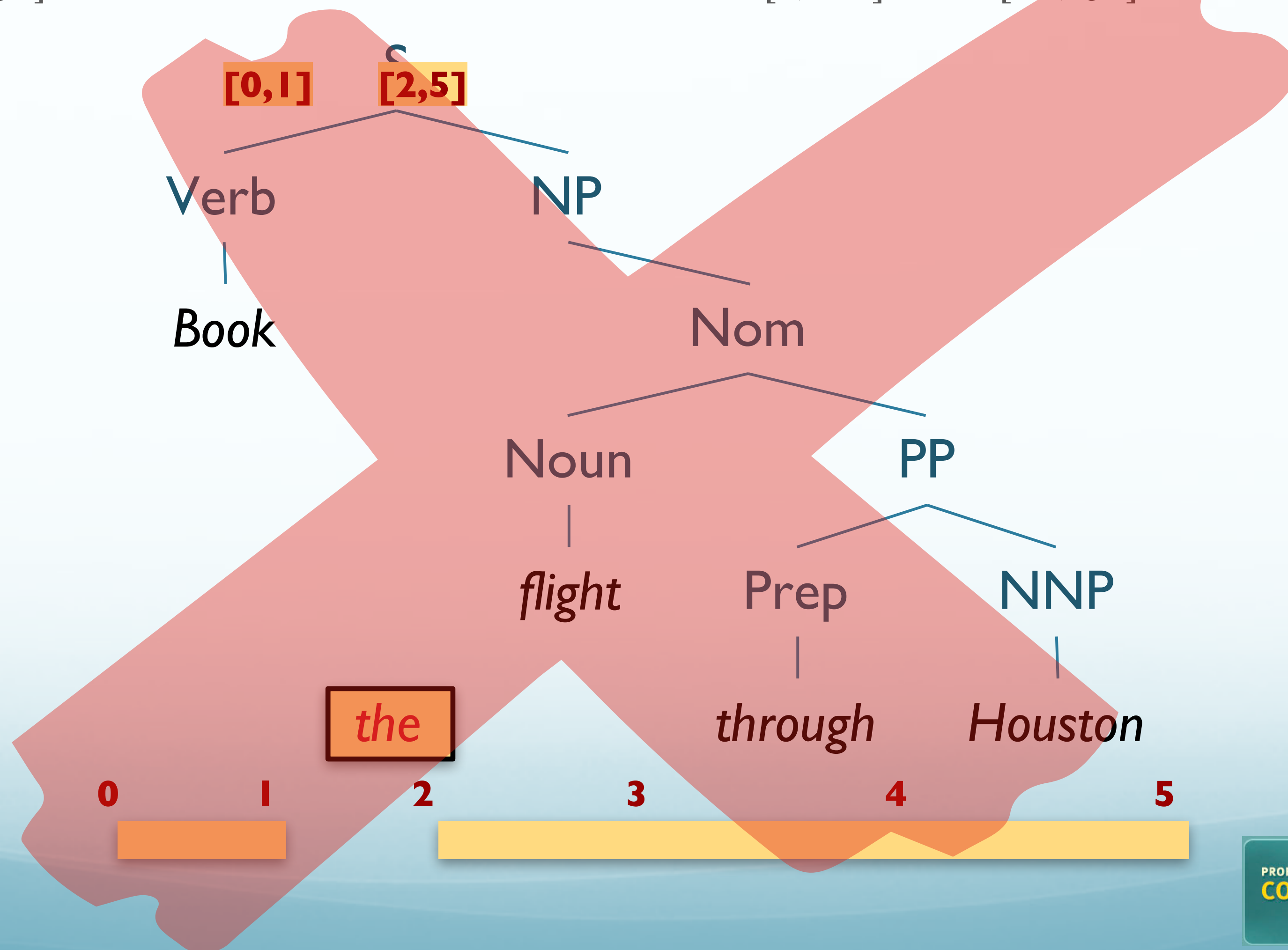
Why fill cells this way?

- For cell $[i, j]$, must be able to access all cells $[i, k]$ and $[k, j]$ where $i < k < j$



Why fill cells this way?

- For cell $[i, j]$, must be able to access all cells $[i, k]$ and $[k, j]$ where $i < k < j$



CKY Parsing Example

\mathcal{L}_1 Grammar

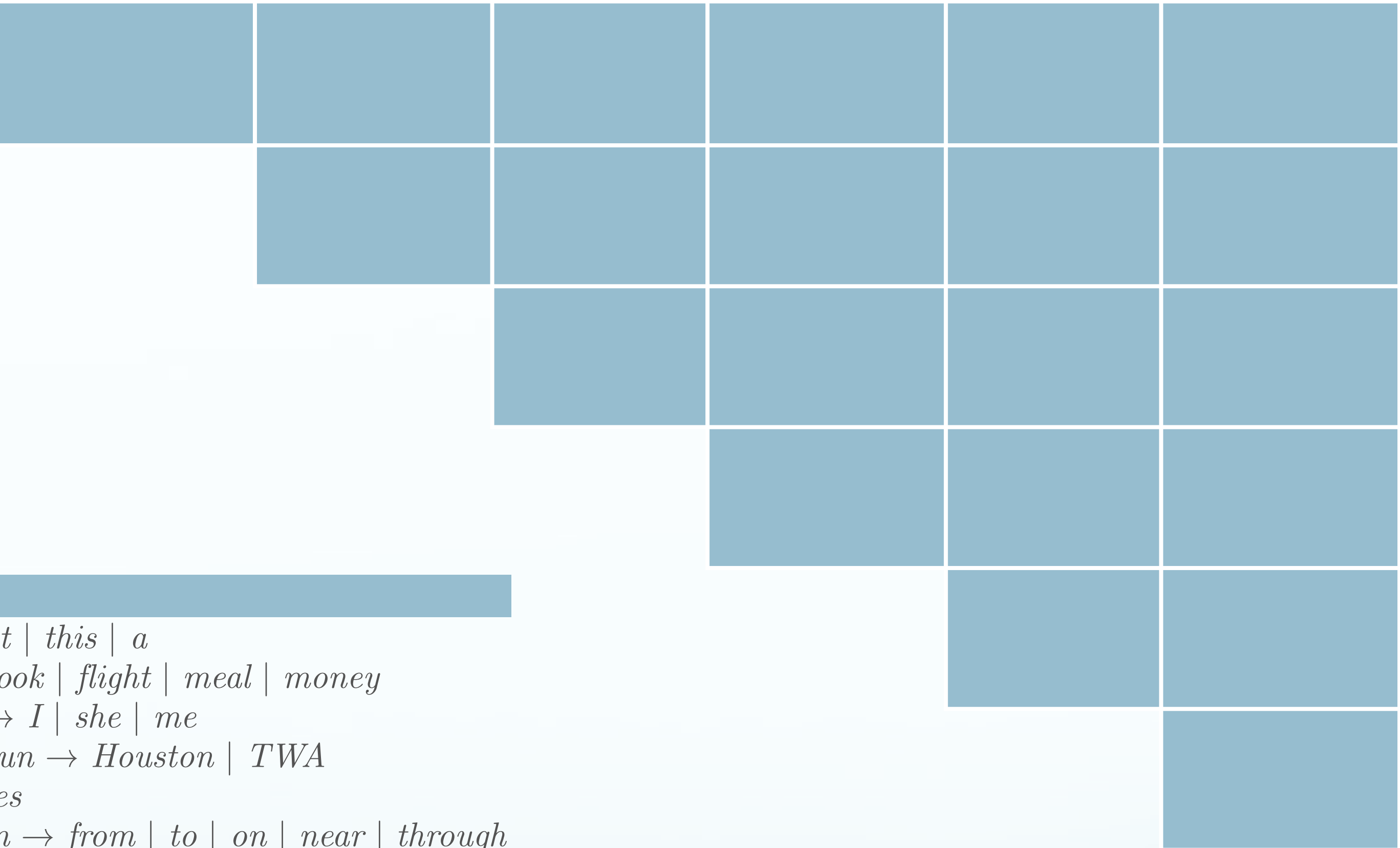
$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$
 $Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$
 $PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$



0 1 2 3 4 5 6

I *prefer* *a* *flight* *on* *TWA*

\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

NP

I

 / she / me

NP \rightarrow TWA / Houston

NP \rightarrow Det Nominal

Nominal \rightarrow book / flight / meal / money

Nominal \rightarrow Nominal Noun

Nominal \rightarrow Nominal PP

VP \rightarrow book / include / prefer

VP \rightarrow Verb NP

VP \rightarrow X2 PP

X2 \rightarrow Verb NP

VP \rightarrow Verb PP

VP \rightarrow VP PP

PP \rightarrow Preposition NP

Lexicon

Det \rightarrow that | this | a

Noun \rightarrow book | flight | meal | money

Pronoun \rightarrow I | she | me

Proper-Noun \rightarrow Houston | TWA

Aux \rightarrow does

Preposition \rightarrow from | to | on | near | through

Verb \rightarrow book | include | prefer



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$$S \rightarrow X1 \quad VP$$
$$X1 \rightarrow Aux NP$$

$S \rightarrow book / include / prefer$

$$S \rightarrow Verb\ NP$$
$$S \rightarrow X2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP \ PP$$

$NP \rightarrow I \mid she \mid me$

NP → TWA / Houston

$$NP \rightarrow Det \textit{ Nominal}$$

Nominal \rightarrow *book* / *flight* / *meal* / *money*

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow *Nominal PP*

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X_2 PP$$
$$X2 \rightarrow Verb\ NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP PP$$

$PP \rightarrow \textit{Preposition NP}$

**NP,
Pronoun**
[0,1]

Lexicon

$$Det \rightarrow that \mid this \mid a$$

Noun → book | flight | meal | money

<i>Pronoun</i>	→	<i>I</i>		<i>she</i>		<i>me</i>
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Proper-Noun \rightarrow *Houston* | *TWA*

Aux \rightarrow *does*

Preposition → *from* | *to* | *on* | *near* | *through*

Verb → *book* | *include* | *prefer*



prefer

a

flight

on

TWA

\mathcal{L}_1 Grammar

$$S \rightarrow NP VP$$
$$S \rightarrow X1 \text{ VP}$$

$X1 \rightarrow Aux NP$

$S \rightarrow \text{book} / \text{include} / \text{prefer}$

$$S \rightarrow \textit{Verb NP}$$
$$S \rightarrow X2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP \ PP$$

$NP \rightarrow I \mid she \mid me$

NP → TWA / Houston

$$NP \rightarrow Det \textit{ Nominal}$$

Nominal \rightarrow *book* / *flight* / *meal* / *money*

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow Nominal PP

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X^2 PP$$
$$X2 \rightarrow Verb\ NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP \ PP$$

$PP \rightarrow Preposition\ NP$

NP, Pronoun [0,1]

Verb, VP, S

[1,2]

Lexicon

$$Det \rightarrow that \mid this \mid a$$

Noun \rightarrow *book* | *flight* | *meal* | *money*

$$Pronoun \rightarrow I \mid she \mid me$$

Proper-Noun \rightarrow *Houston* | *TWA*

Aux → *does*

Preposition → from | to | on | near | through

Verb \rightarrow book | include | prefer

A diagram illustrating a preference range. A horizontal axis is marked with 0, 1, and 2. A green bar is positioned above the axis, starting at 1 and extending to 2. Below the axis, the word "prefer" is written in a stylized font, also starting at 1 and extending to 2.

prefer

a

flight

on

TWA

\mathcal{L}_1 Grammar

$$S \rightarrow NP VP$$
$$S \rightarrow X1 \quad VP$$
$$X1 \rightarrow Aux NP$$

$S \rightarrow book / include / prefer$

$$S \rightarrow Verb\ NP$$
$$S \rightarrow X^2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP \ PP$$

$NP \rightarrow I / she / me$

NP → *TWA* / *Houston*

$$NP \rightarrow Det \textit{ Nominal}$$

Nominal \rightarrow *book* / *flight* / *meal* / *money*

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow *Nominal PP*

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X^2 PP$$
$$X2 \rightarrow Verb NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP \ PP$$
$$PP \rightarrow \textit{Preposition NP}$$

**NP, NP,
Pronoun**
[0,1]

[0,2]

Werth, WP, S

[1,2]

Lexicon

Det \rightarrow *that* | *this* | *a*

Noun \rightarrow *book* | *flight* | *meal* | *money*

Pronoun \rightarrow *I* | *she* | *me*

Proper-Noun \rightarrow *Houston* | *TWA*

Aux \rightarrow *does*

Preposition → *from* | *to* | *on* | *near* | *through*

Verb \rightarrow *book* | *include* | *prefer*

1

prefer

a

flight

on

TWA

0

1

2

3

4

5

6

\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$$S \rightarrow X1 \quad VP$$
$$X1 \rightarrow Aux NP$$

$S \rightarrow book / include / prefer$

$$S \rightarrow Verb\ NP$$
$$S \rightarrow X2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP \ PP$$

$NP \rightarrow I \mid she \mid me$

NP → TWA / Houston

NP \rightarrow *Det Nominal*

Nominal \rightarrow *book* / *flight* / *meal* / *money*

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Nominal \rightarrow *Nominal PP*

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X_2 PP$$
$$X2 \rightarrow Verb\ NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP PP$$

$PP \rightarrow \textit{Preposition NP}$

NP, NP,
Pronoun
[0,1]

$[0,2]$

Verb, VP, S
[1,2]

Lexicon

$$Det \rightarrow that \mid this \mid a$$

Noun \rightarrow *book* | *flight* | *meal* | *money*

<i>Pronoun</i>	\rightarrow	<i>I</i>	<i>she</i>	<i>me</i>
----------------	---------------	----------	------------	-----------

Proper-Noun \rightarrow *Houston* | *TWA*

Aux → *does*

Preposition → *from* | *to* | *on* | *near* | *through*

Verb \rightarrow *book* | *include* | *prefer*

A diagram illustrating a 3-point Likert scale for the statement "I prefer". The scale is represented by a horizontal bar with three segments, labeled 0, 1, and 2. The segment labeled 0 is red, the segment labeled 1 is blue, and the segment labeled 2 is green. The statement "I prefer" is written above the bar, with the "I" positioned above the red segment and "prefer" positioned above the blue and green segments.

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A diagram illustrating a 3-point Likert scale. At the top, a long green bar represents the statement "I prefer". Below this bar, the word "I" is positioned above the number "0" and the word "prefer" is positioned above the number "2". The scale is represented by three colored boxes: a red box on the left, a blue box in the middle, and a green box on the right. The numbers 0, 1, and 2 are placed below the boxes, indicating the scale points.

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\mathcal{L}_1 Grammar

$$S \rightarrow NP VP$$
$$S \rightarrow X1 \text{ VP}$$
$$X1 \rightarrow Aux NP$$

$S \rightarrow book / include / prefer$

$$S \rightarrow Verb\ NP$$
$$S \rightarrow X2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP \ PP$$
$$NP \rightarrow I \mid she \mid me$$

NP → TWA / Houston

$$NP \rightarrow Det \textit{ Nominal}$$

Nominal \rightarrow *book* / *flight* / *meal* / *money*

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow *Nominal PP*

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X^2 PP$$
$$X2 \rightarrow Verb\ NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP \ PP$$

$PP \rightarrow \textit{Preposition NP}$

NP, NP,
Pro
Pro
[0, I]

$[0,2]$

Wertb, VP, S
[1,2]

Lexicon

$$Det \rightarrow that \mid this \mid a$$

Noun \rightarrow *book* | *flight* | *meal* | *money*

Pronoun \rightarrow *I* | *she* | *me*

Proper-Noun \rightarrow *Houston* | *TWA*

Aux → *does*

Preposition → *from* | *to* | *on* | *near* | *through*

Verb \rightarrow *book* | *include* | *prefer*

A diagram illustrating a 3-point Likert scale for the statement "I prefer". The scale is represented by a horizontal bar with three segments. The first segment is red and labeled "0". The second segment is blue and labeled "1". The third segment is green and labeled "2". The statement "I prefer" is written above the bar, centered over the second and third segments.

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\mathcal{L}_1 Grammar

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$

 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$

 $Nominal \rightarrow book \mid flight \mid meal \mid money$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$

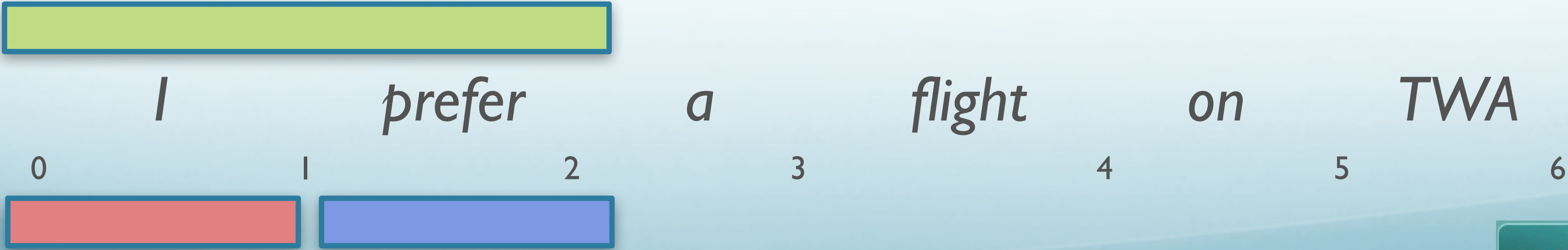
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$

 $PP \rightarrow Preposition NP$

Lexicon

$Det \rightarrow that \mid this \mid a$
 $Noun \rightarrow book \mid flight \mid meal \mid money$
 $Pronoun \rightarrow I \mid she \mid me$
 $Proper-Noun \rightarrow Houston \mid TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from \mid to \mid on \mid near \mid through$
 $Verb \rightarrow book \mid include \mid prefer$

NP, NP, Pronoun [0,1]	S S [0,2]				
	Verb, VP, S [1,2]				



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

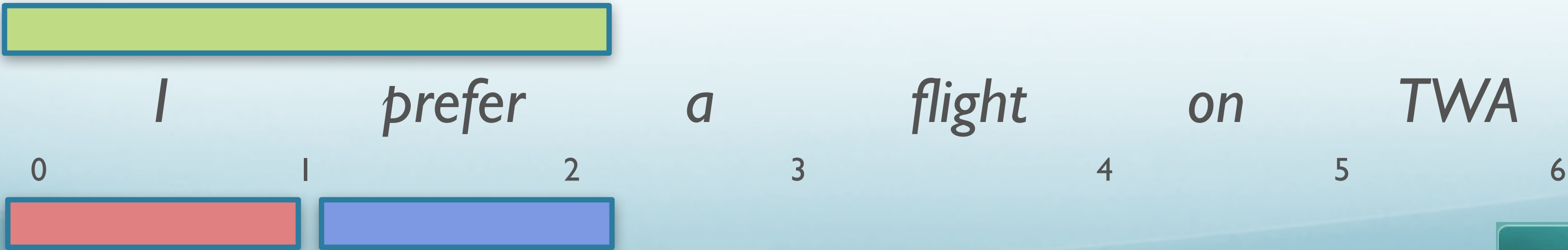
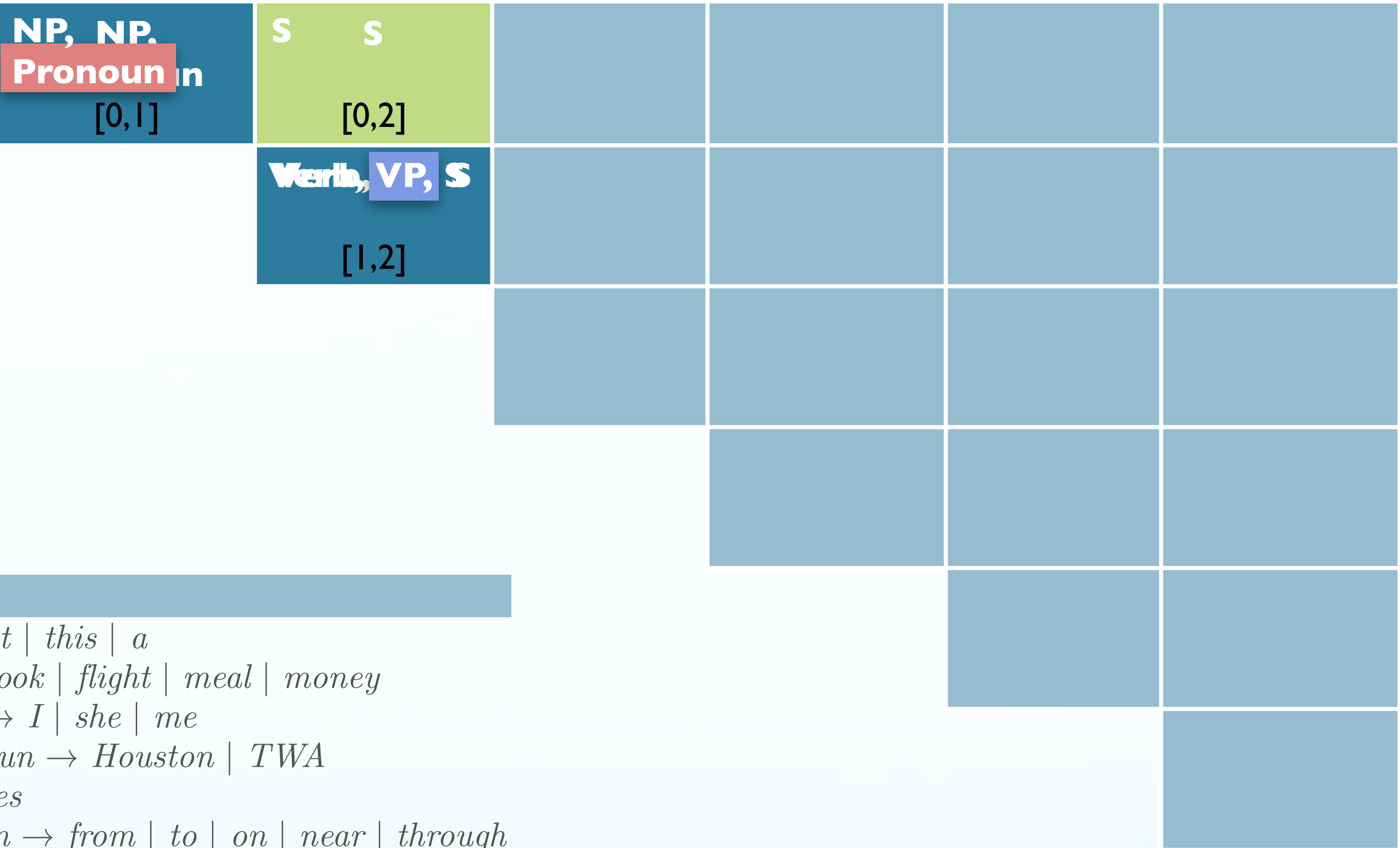
$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$



\mathcal{L}_1 Grammar

$$S \rightarrow NP VP$$
$$S \rightarrow X1 \quad VP$$
$$X1 \rightarrow Aux NP$$

$S \rightarrow book / include / prefer$

$$S \rightarrow Verb \ NP$$
$$S \rightarrow X^2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP \ PP$$

$NP \rightarrow I \mid she \mid me$

NP → *TWA* / *Houston*

$$NP \rightarrow Det \textit{ Nominal}$$

Nominal \rightarrow *book* / *flight* / *meal* / *money*

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow *Nominal PP*

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X^2 PP$$
$$X2 \rightarrow Verb NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP \ PP$$

$$PP \rightarrow \textit{Preposition NP}$$

NP, NP,
Pronoun
[0,1]

S S
[0,2

Verb, VP, S

[1,2]

Lexicon

Det \rightarrow *that* | *this* | *a*

Noun \rightarrow *book* | *flight* | *meal* | *money*

Pronoun \rightarrow *I* | *she* | *me*

Proper-Noun \rightarrow *Houston* | *TWA*

Aux \rightarrow *does*

Preposition → *from* | *to* | *on* | *near* | *through*

Verb \rightarrow *book* | *include* | *prefer*

1

prefer

a

flight

on

TWA

0

1

2

3

4

5

6

\mathcal{L}_1 Grammar

$$S \rightarrow NP VP$$
$$S \rightarrow X1 \text{ VP}$$
$$X1 \rightarrow Aux NP$$

$S \rightarrow book / include / prefer$

$$S \rightarrow Verb\ NP$$
$$S \rightarrow X2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP \ PP$$
$$NP \rightarrow I \mid she \mid me$$

NP → TWA / Houston

$$NP \rightarrow Det \textit{ Nominal}$$

Nominal \rightarrow *book* / *flight* / *meal* / *money*

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow *Nominal PP*

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X^2 PP$$
$$X2 \rightarrow Verb NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP \ PP$$

$PP \rightarrow \textit{Preposition NP}$

NP, Pronoun [0, 1]

S

[0,2]

[0,2]

Verb, VP, S

[1,2]

[1,2]

Det

[2,3]

[2,3]

Lexicon

Det → *that* | *this* | *a*

Noun → *book* | *flight* | *meal* | *money*

$$Pronoun \rightarrow I \mid she \mid me$$

Proper-Noun \rightarrow *Houston* | *TWA*

Aux \rightarrow *does*

Preposition → *from* | *to* | *on* | *near* | *through*

Verb \rightarrow *book* | *include* | *prefer*

Response	Percentage
U.S. should take more action	78%
U.S. should take no more action	19%

prefer

Diagram illustrating a 2D array structure with 2 rows and 3 columns. The first row is highlighted in green. The element at row 1, column 2 is highlighted in orange and labeled 'a'.

flight

4 5

on

TWA

$PP \rightarrow \textit{Preposition NP}$

Verb \rightarrow *book* | *include* | *prefer*

Page 10 of 10

$$PP \rightarrow \textit{Preposition NP}$$

Verb \rightarrow *book* | *include* | *prefer*

TWA

6

\mathcal{L}_1 Grammar

$$S \rightarrow NP VP$$
$$S \rightarrow X1 \quad VP$$
$$X1 \rightarrow Aux NP$$

$S \rightarrow book / include / prefer$

$$S \rightarrow Verb\ NP$$
$$S \rightarrow X^2 PP$$
$$S \rightarrow Verb PP$$
$$S \rightarrow VP \ PP$$

$NP \rightarrow I / she / me$

NP → *TWA* / *Houston*

$$NP \rightarrow Det \textit{ Nominal}$$

Nominal \rightarrow *book* / *flight* / *meal* / *money*

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow *Nominal PP*

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X^2 PP$$
$$X2 \rightarrow Verb NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP \ PP$$
$$PP \rightarrow \textit{Preposition NP}$$

Lexicon

Det \rightarrow *that* | *this* | *a*

Noun \rightarrow *book* | *flight* | *meal* | *money*

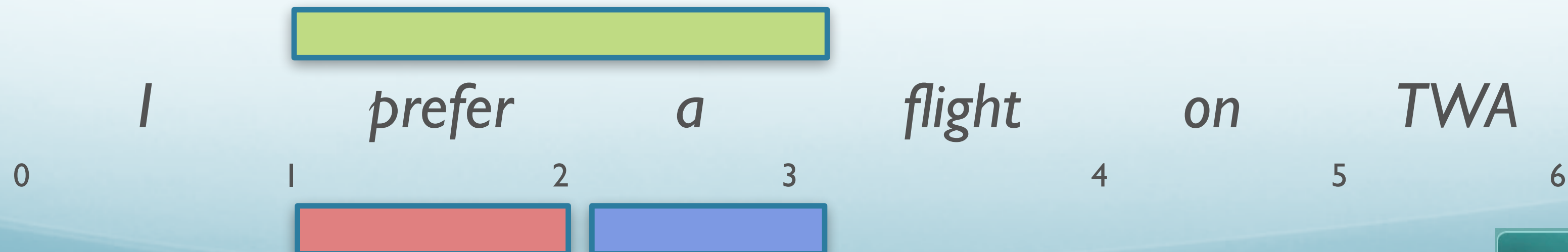
Pronoun \rightarrow *I* | *she* | *me*

Proper-Noun \rightarrow *Houston* | *TWA*

Aux \rightarrow *does*

Preposition → *from* | *to* | *on* | *near* | *through*

Verb \rightarrow *book* | *include* | *prefer*



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

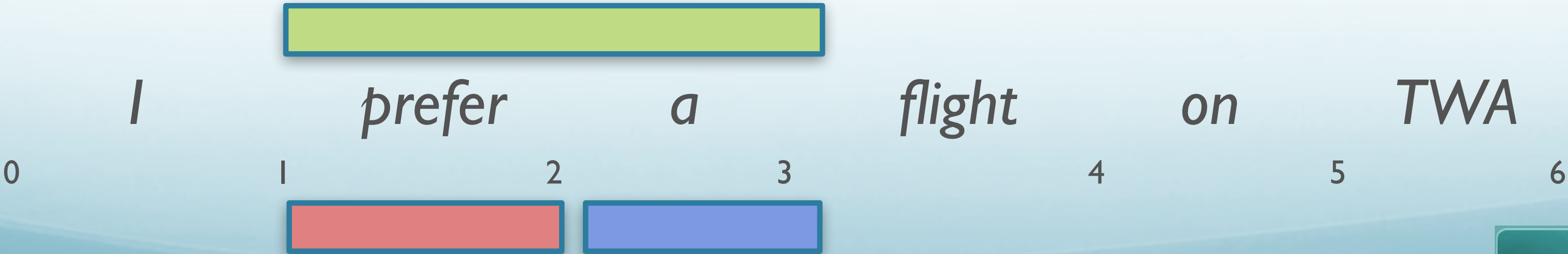
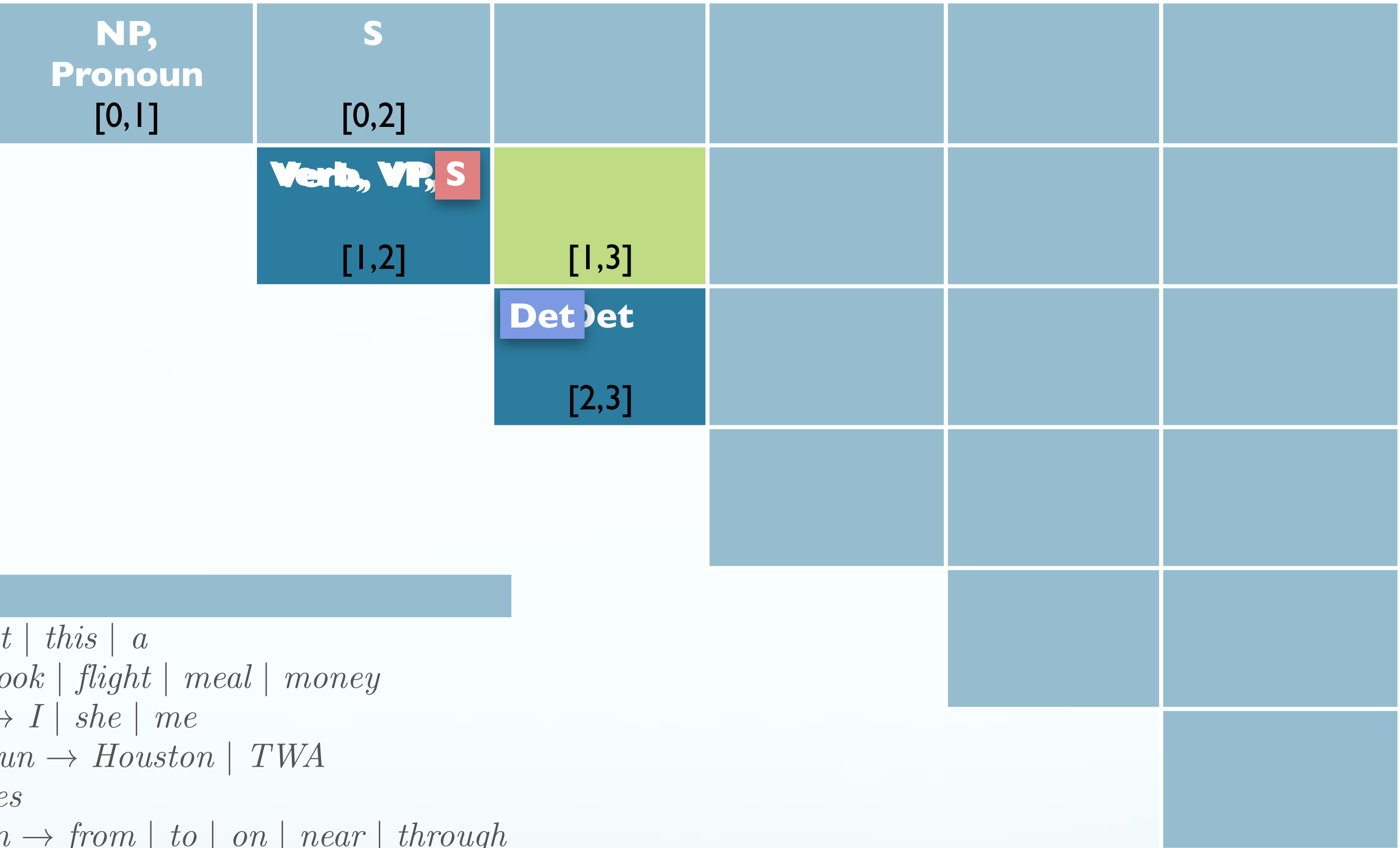
$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

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 $Verb \rightarrow book\ /\ include\ /\ prefer$



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

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$S \rightarrow book / include / prefer$

$$S \rightarrow Verb\ NP$$
$$S \rightarrow X2 PP$$
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NP → TWA / Houston

$$NP \rightarrow Det \textit{ Nominal}$$

Nominal \rightarrow *book* / *flight* / *meal* / *money*

Nominal \rightarrow *Nominal Noun*

Nominal \rightarrow *Nominal PP*

$VP \rightarrow book / include / prefer$

$$VP \rightarrow Verb\ NP$$
$$VP \rightarrow X^2 PP$$
$$X2 \rightarrow Verb\ NP$$
$$VP \rightarrow Verb PP$$
$$VP \rightarrow VP \ PP$$

$PP \rightarrow \textit{Preposition NP}$

Lexicon

$$Det \rightarrow that \mid this \mid a$$

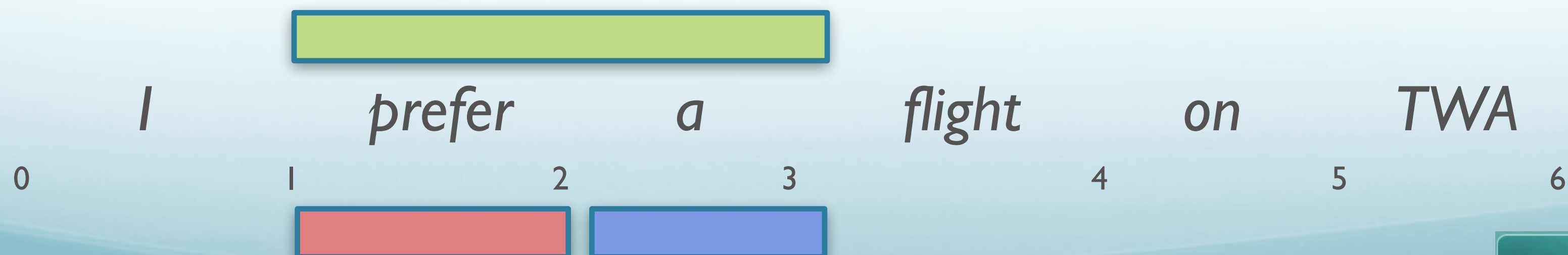
Noun \rightarrow *book* | *flight* | *meal* | *money*

<i>Pronoun</i> → <i>I</i>	<i>she</i>	<i>me</i>
---------------------------	------------	-----------

$$Proper-Noun \rightarrow Houston \mid TWA$$

Aux \rightarrow *does*

Preposition → *from* | *to* | *on* | *near* | *through*

$$Verb \rightarrow book \mid include \mid prefer$$


\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

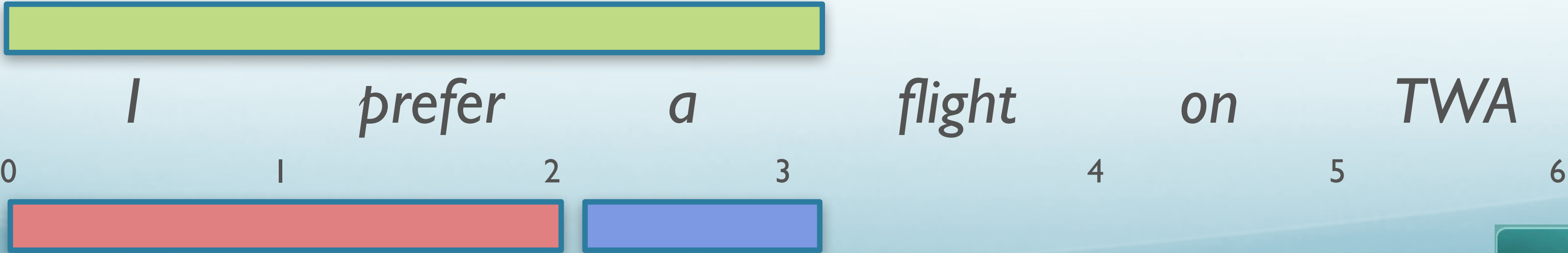
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]			
		Det [2,3]			



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

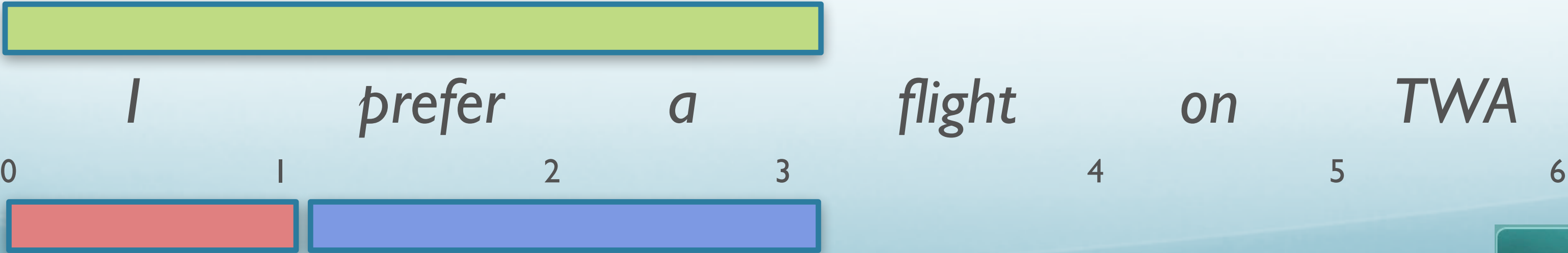
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]			
		Det Det [2,3]			



$PP \rightarrow \textit{Preposition NP}$

[3,4]

Verb \rightarrow *book* | *include* | *prefer*

48

\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

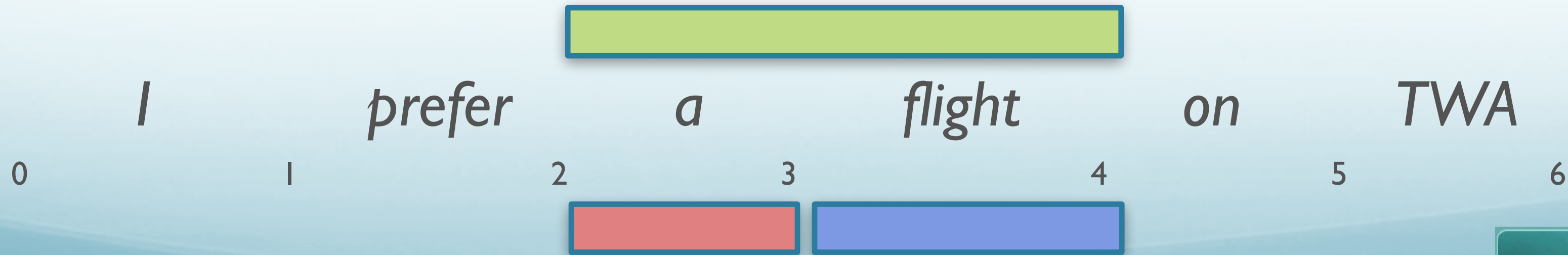
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]			
	Det [2,3]	[2,4]			
		Noun, Nom [3,4]			

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

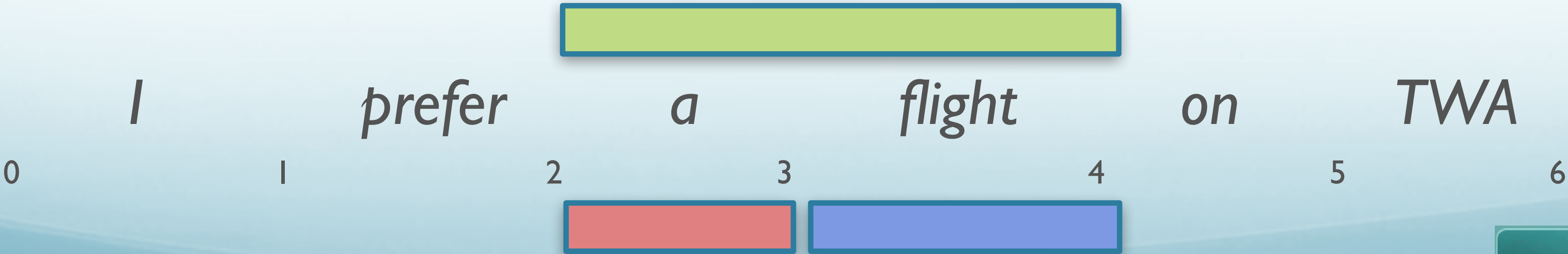
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]			
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

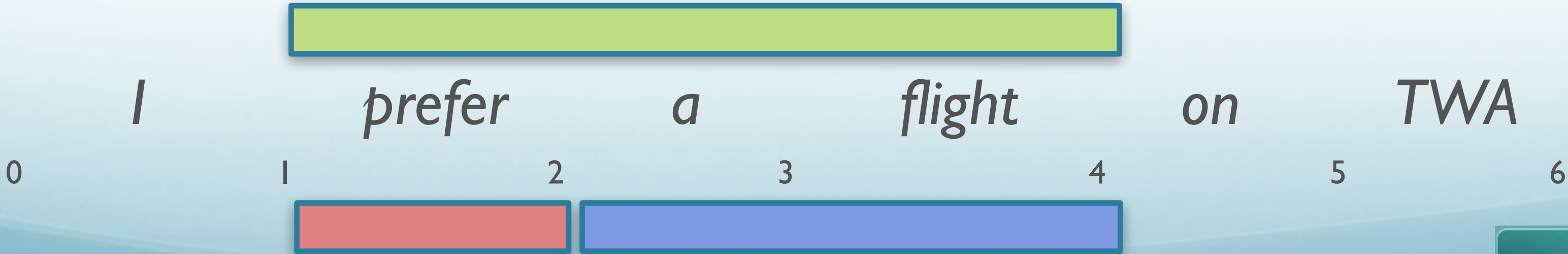
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

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 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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 $Proper-Noun \rightarrow Houston\ /\ TWA$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]	[1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

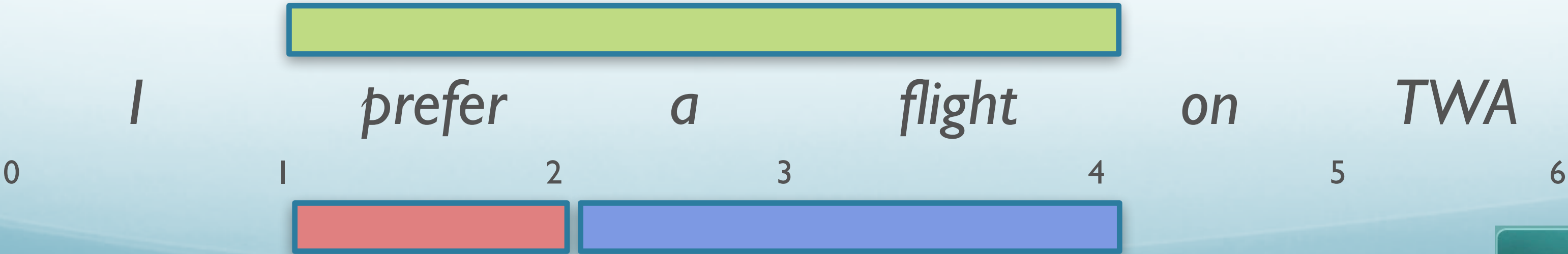
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]	VP [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
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 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
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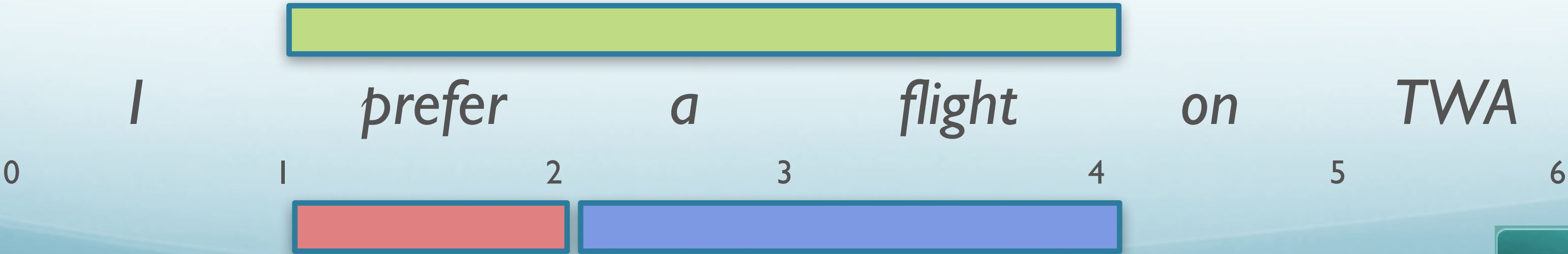
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

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Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
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 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]	VP, X2 [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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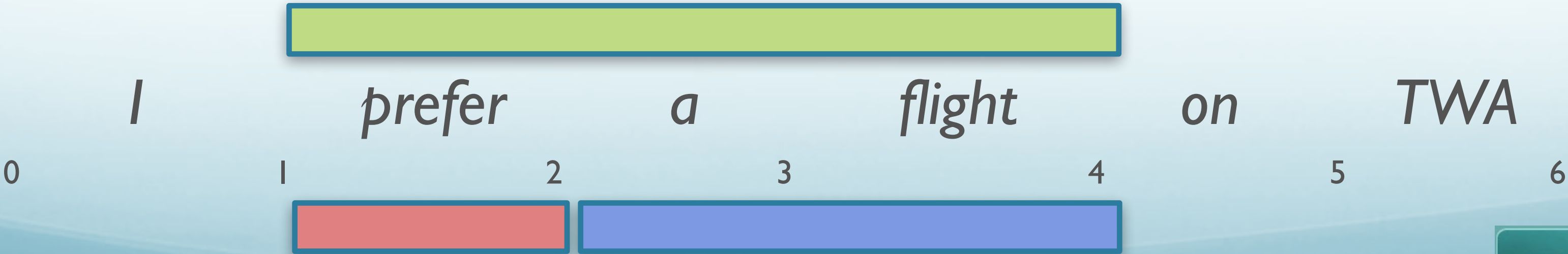
$VP \rightarrow book / include / prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

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NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

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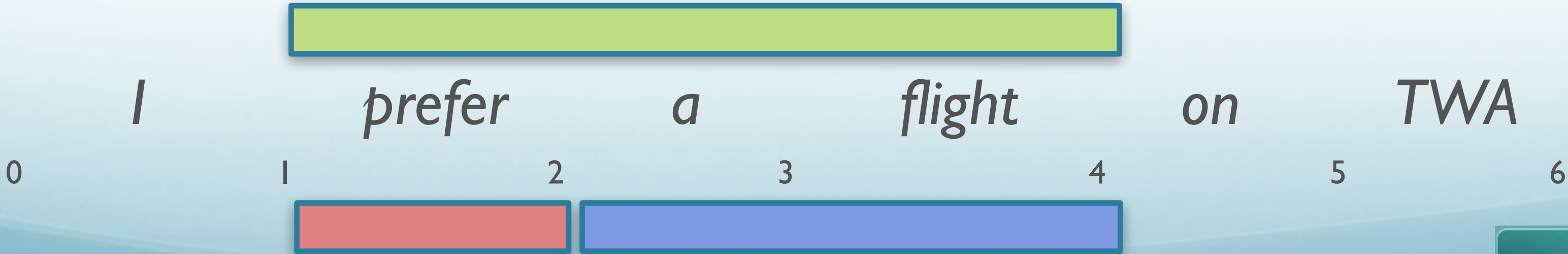
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

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 $Proper-Noun \rightarrow Houston\ /\ TWA$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
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$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

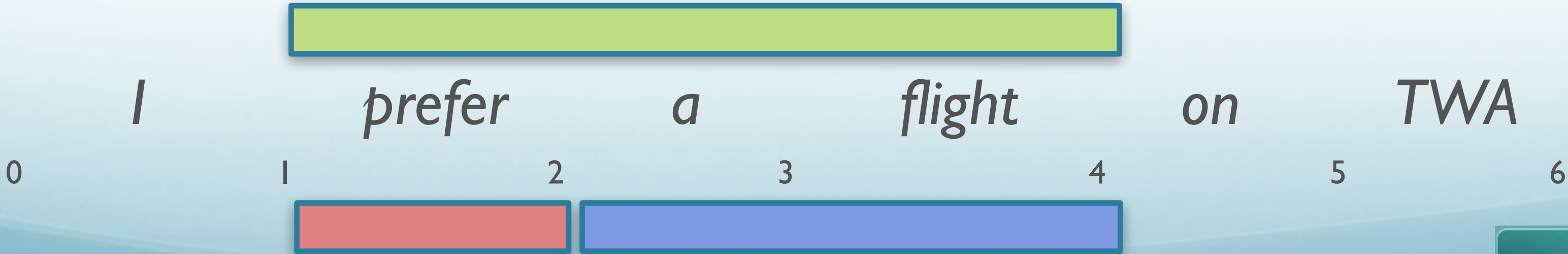
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

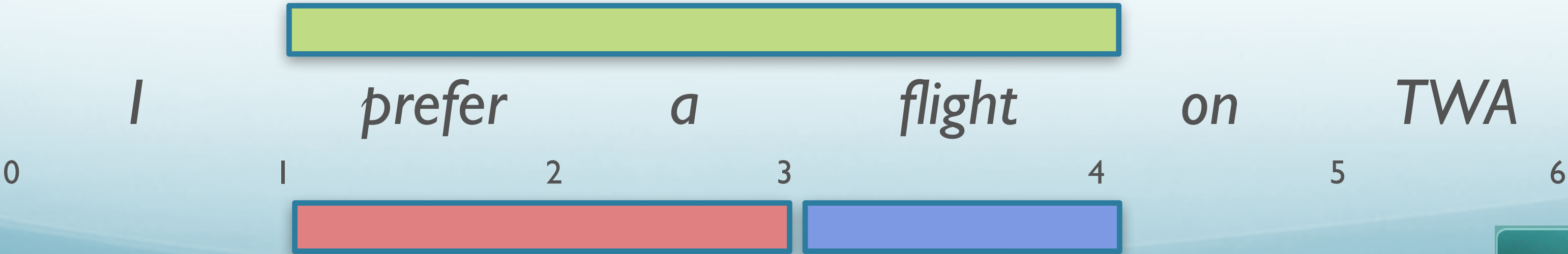
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$

$S \rightarrow X1\ VP$

$X1 \rightarrow Aux\ NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb\ NP$

$S \rightarrow X2\ PP$

$S \rightarrow Verb\ PP$

$S \rightarrow VP\ PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal\ Noun$

$Nominal \rightarrow Nominal\ PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb\ NP$

$VP \rightarrow X2\ PP$

$X2 \rightarrow Verb\ NP$

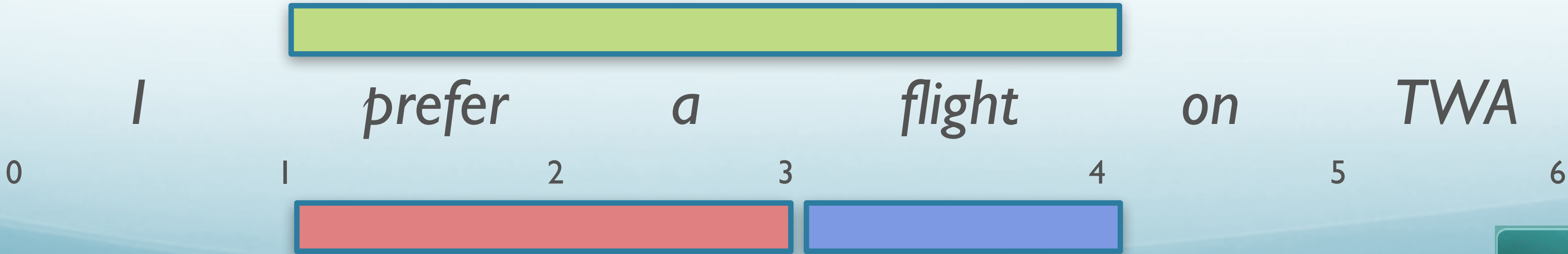
$VP \rightarrow Verb\ PP$

$VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon
$Det \rightarrow that\ /\ this\ /\ a$
$Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]			
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

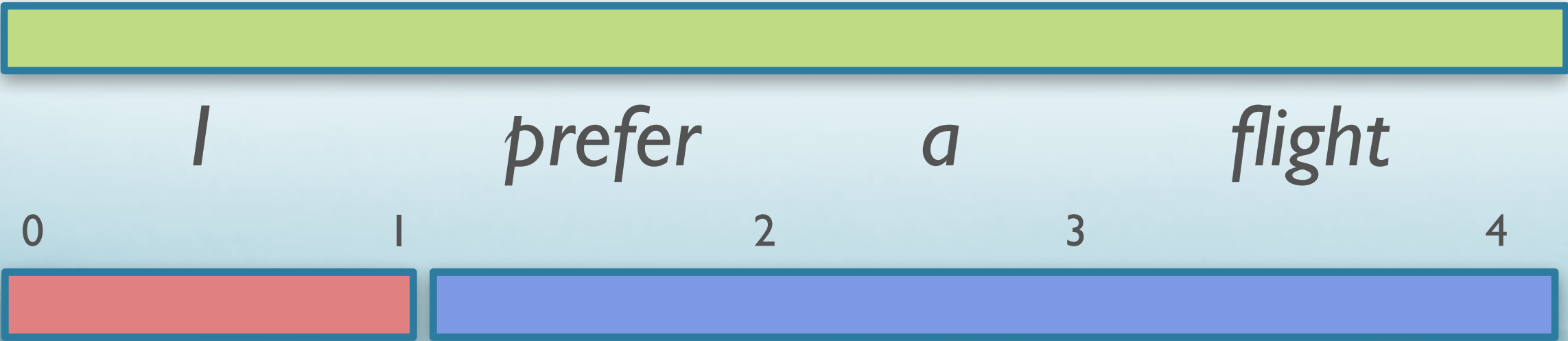
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	[0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$
 $S \rightarrow X1 VP$
 $X1 \rightarrow Aux NP$
 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb NP$
 $S \rightarrow X2 PP$
 $S \rightarrow Verb PP$
 $S \rightarrow VP PP$

 $NP \rightarrow I \mid she \mid me$
 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det Nominal$

 $Nominal \rightarrow book \mid flight \mid meal \mid money$
 $Nominal \rightarrow Nominal Noun$
 $Nominal \rightarrow Nominal PP$

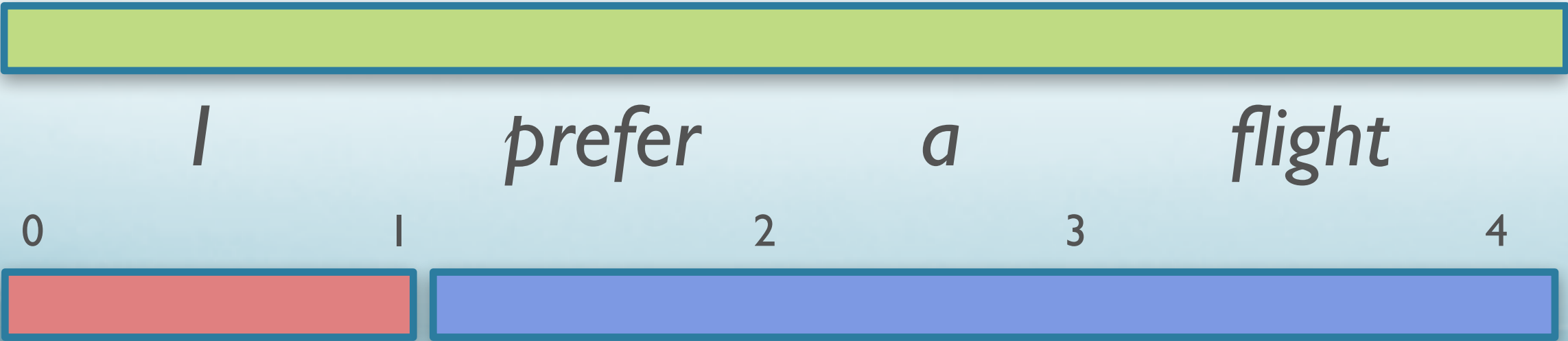
 $VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb NP$
 $VP \rightarrow X2 PP$
 $X2 \rightarrow Verb NP$
 $VP \rightarrow Verb PP$
 $VP \rightarrow VP PP$

 $PP \rightarrow Preposition NP$

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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
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 $S \rightarrow book\ /\ include\ /\ prefer$
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 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
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 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

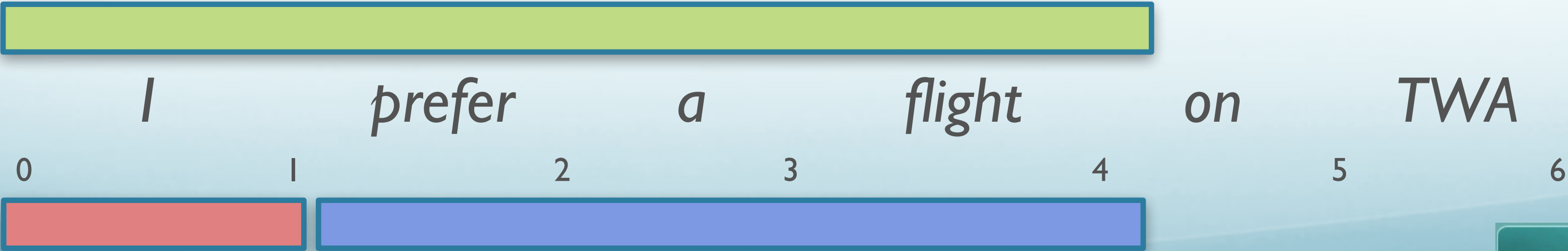
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
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 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



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$S \rightarrow NP\ VP$
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$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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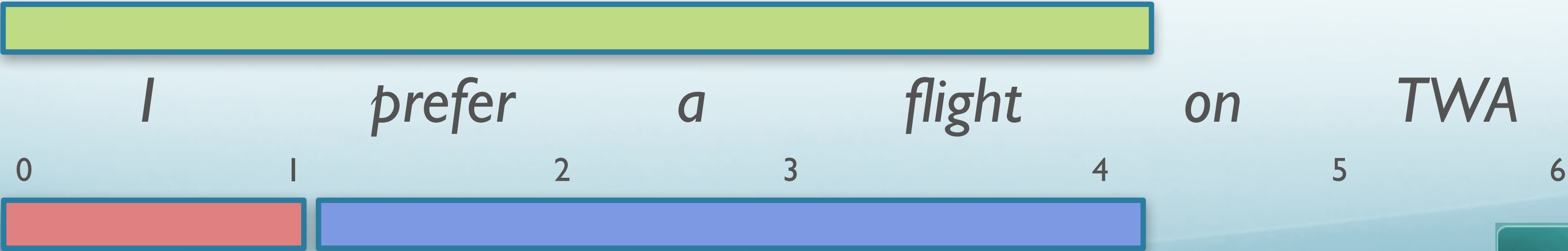
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
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$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
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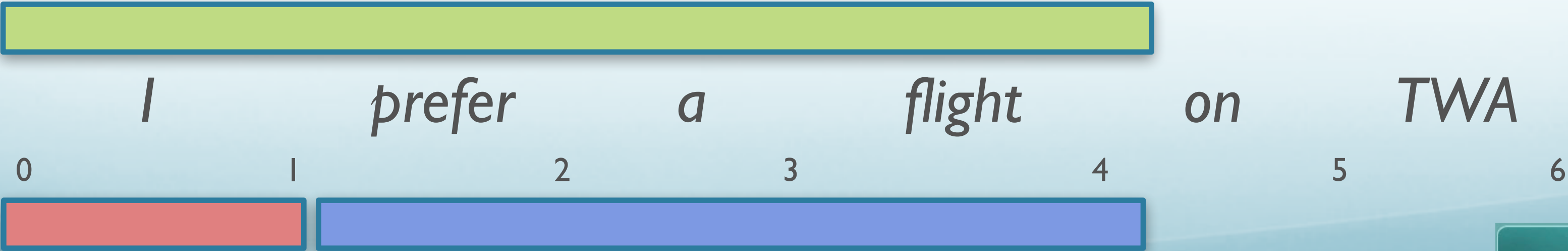
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $X1 \rightarrow Aux\ NP$
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 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
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 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

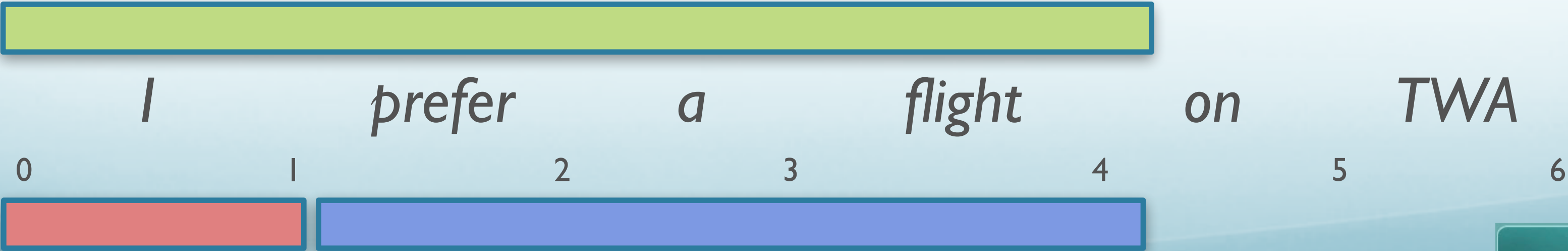
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
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 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



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$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

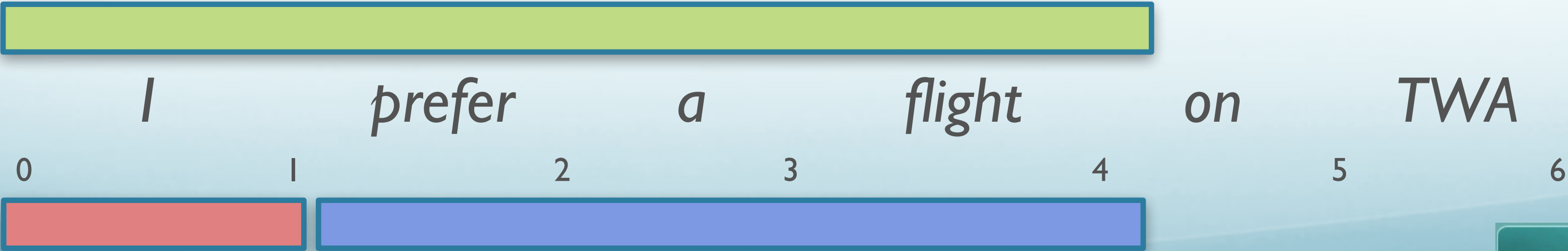
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

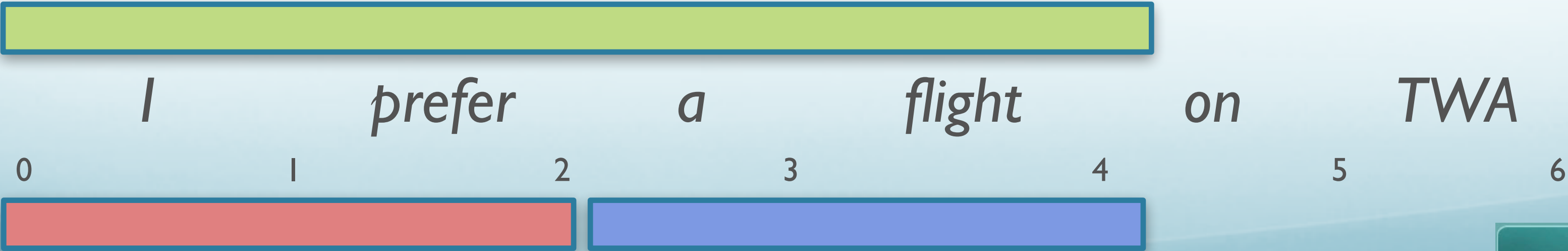
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	<div>S</div> <div>[0,2]</div>	[0,3]	<div>S</div> <div>[0,4]</div>		
	<div>Verb, VP, S</div> <div>[1,2]</div>	[1,3]	<div>VP, X2, S</div> <div>[1,4]</div>		
		<div>Det</div> <div>[2,3]</div>	<div>NP</div> <div>[2,4]</div>		
			<div>Noun, Nom</div> <div>[3,4]</div>		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

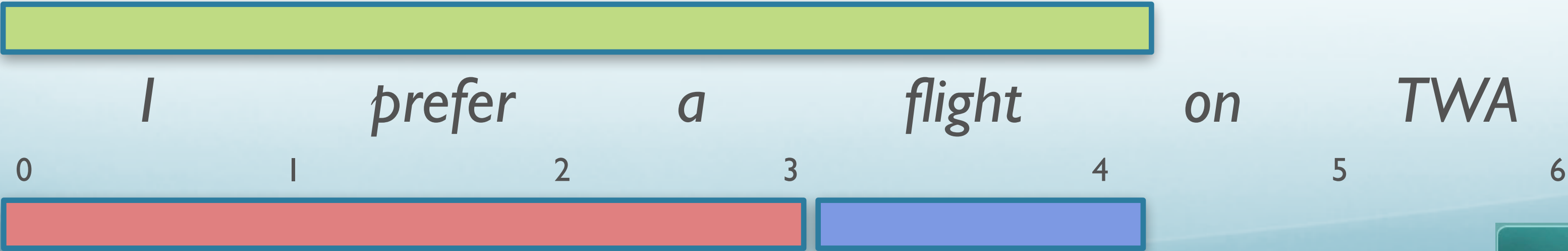
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

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 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$

$S \rightarrow X1\ VP$

$X1 \rightarrow Aux\ NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb\ NP$

$S \rightarrow X2\ PP$

$S \rightarrow Verb\ PP$

$S \rightarrow VP\ PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal\ Noun$

$Nominal \rightarrow Nominal\ PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb\ NP$

$VP \rightarrow X2\ PP$

$X2 \rightarrow Verb\ NP$

$VP \rightarrow Verb\ PP$

$VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

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$Aux \rightarrow does$
$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
$Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		
				Prep [4,5]	



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

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 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

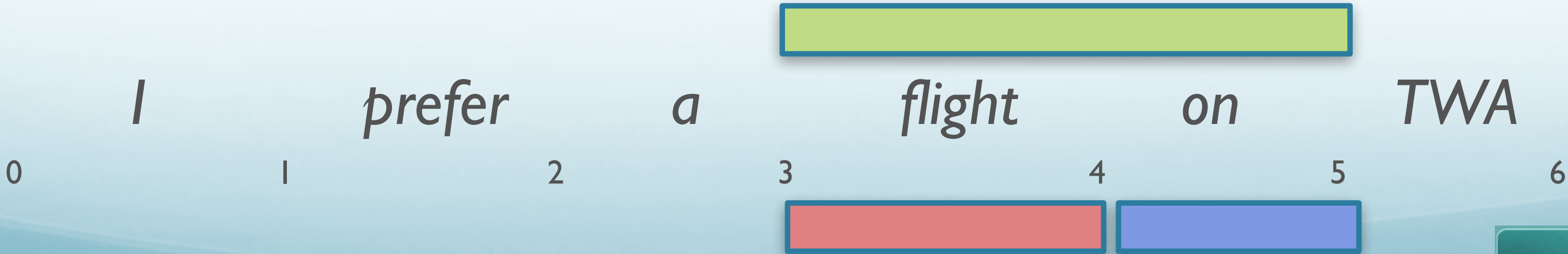
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]	[3,5]	
				Prep [4,5]	



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
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 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

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 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
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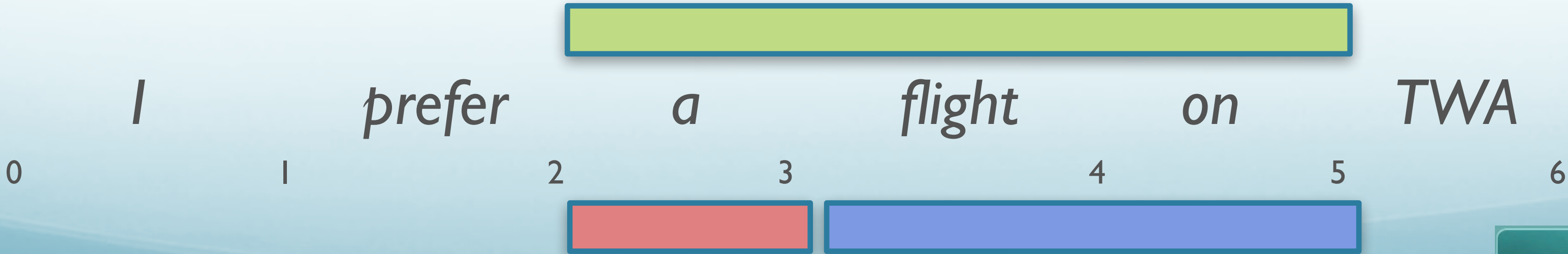
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 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

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 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		
				Prep [4,5]	



\mathcal{L}_1 Grammar

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 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

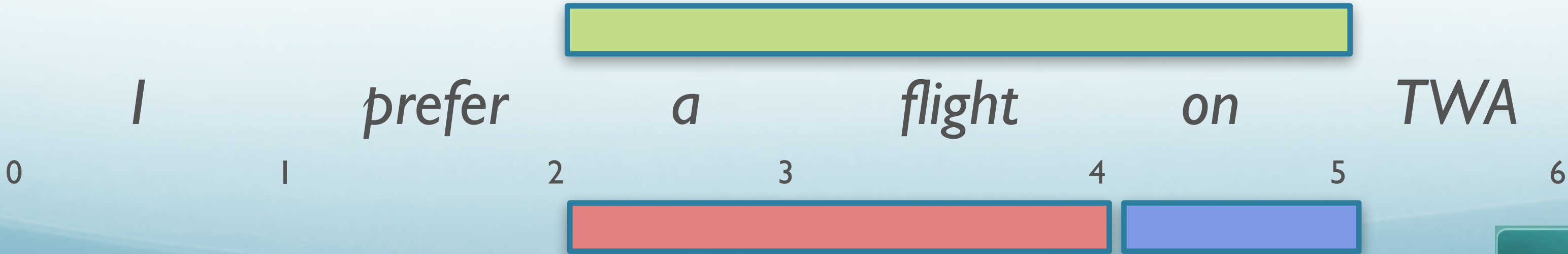
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		
				Prep [4,5]	



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

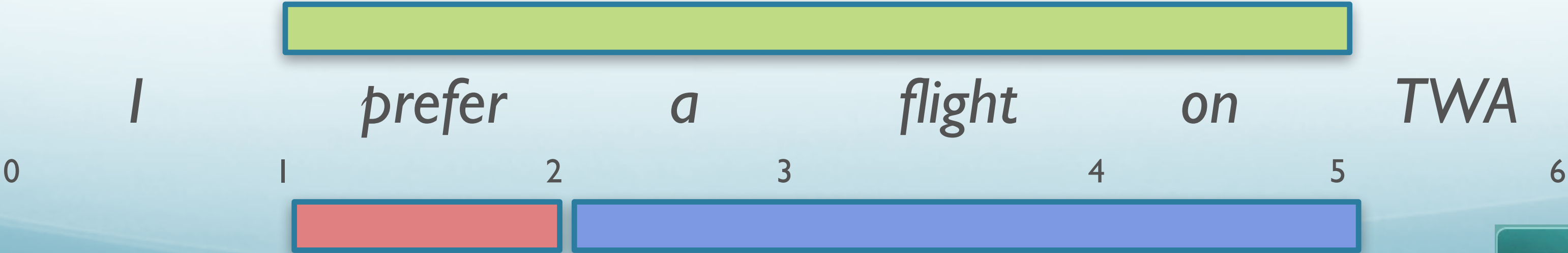
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
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NP, Pronoun [0,1]	S [0,2]		S [0,4]		
	Verb, VP, S [1,2]		VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		
				Prep [4,5]	



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $S \rightarrow book\ /\ include\ /\ prefer$
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 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

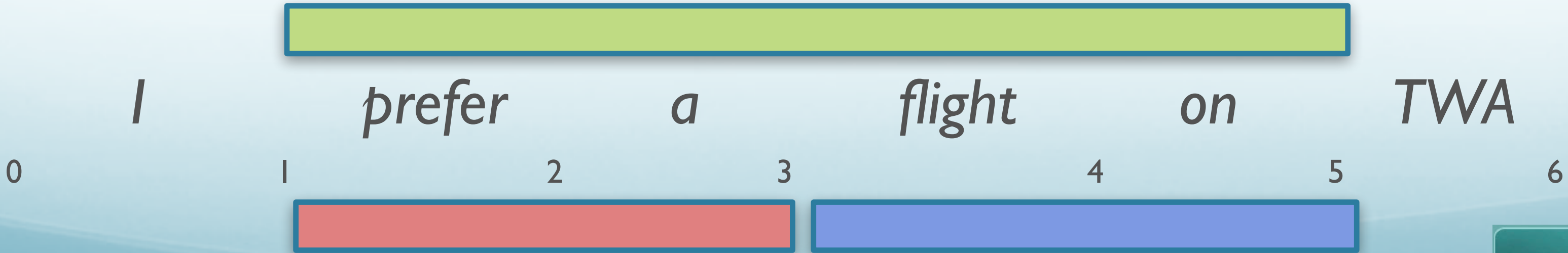
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]	[3,5]	
				Prep [4,5]	



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$S \rightarrow NP\ VP$
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 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
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 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

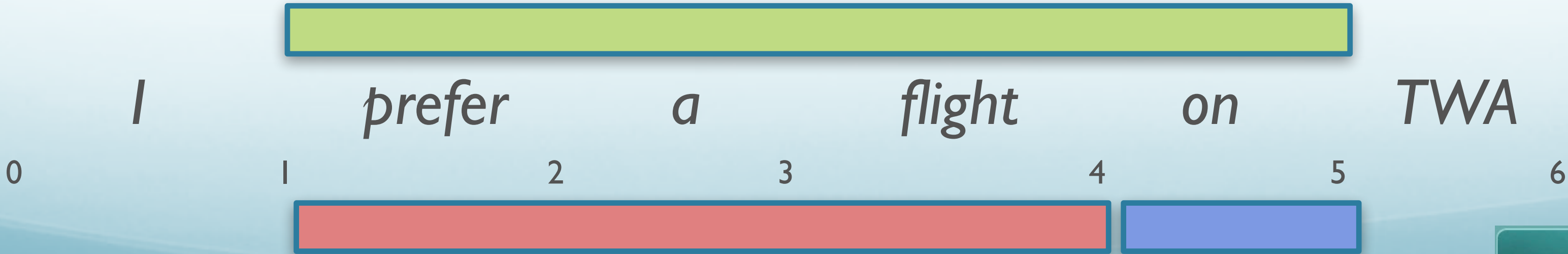
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]		
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]		
		Det [2,3]	NP [2,4]		
			Noun, Nom [3,4]		
				Prep [4,5]	



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$S \rightarrow NP\ VP$
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 $S \rightarrow book\ /\ include\ /\ prefer$
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 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
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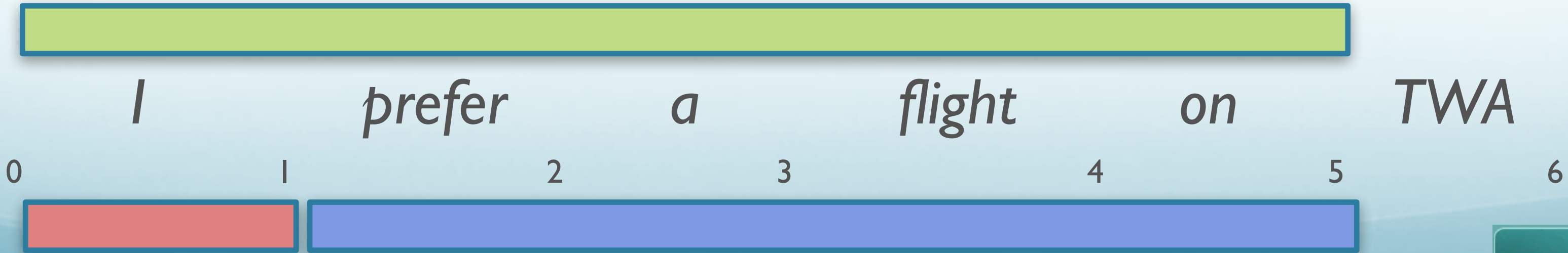
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	
			Noun, Nom [3,4]	[3,5]	
				Prep [4,5]	



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

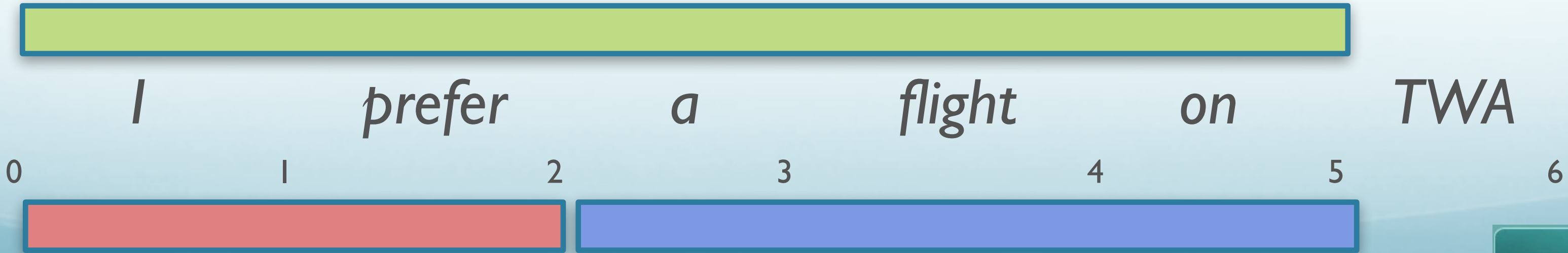
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	
			Noun, Nom [3,4]	[3,5]	
				Prep [4,5]	



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$S \rightarrow NP\ VP$
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 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
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 $S \rightarrow X2\ PP$
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$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

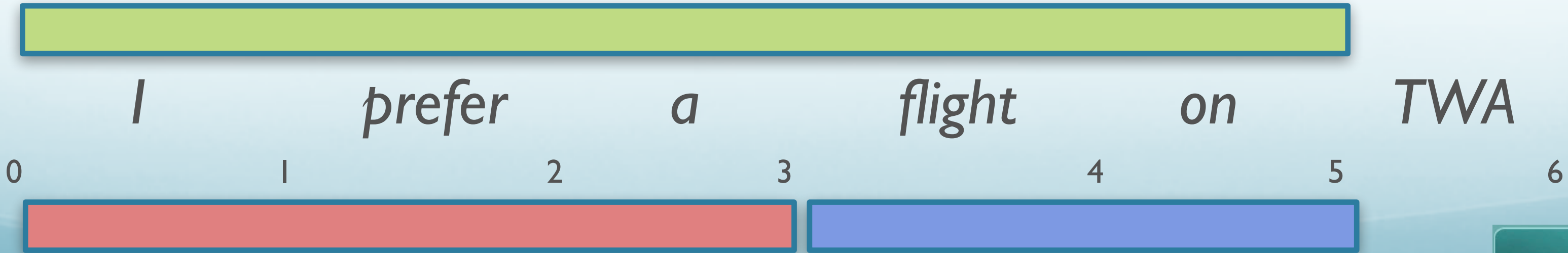
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

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 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	
			Noun, Nom [3,4]	[3,5]	
				Prep [4,5]	



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
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 $S \rightarrow book\ /\ include\ /\ prefer$
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 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

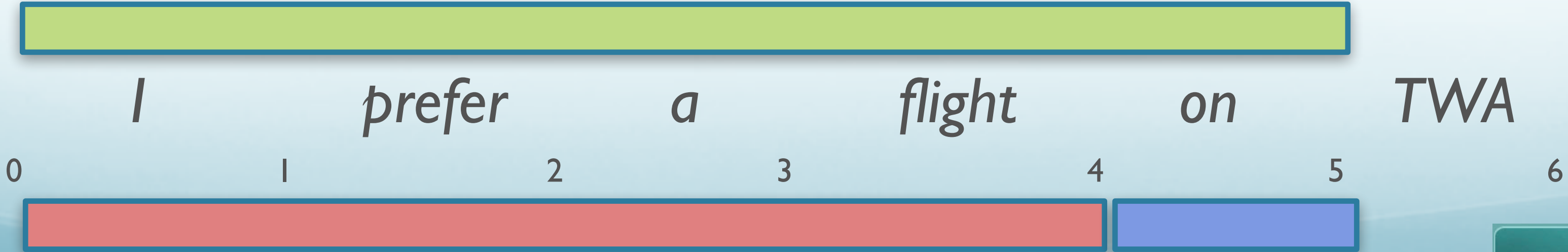
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

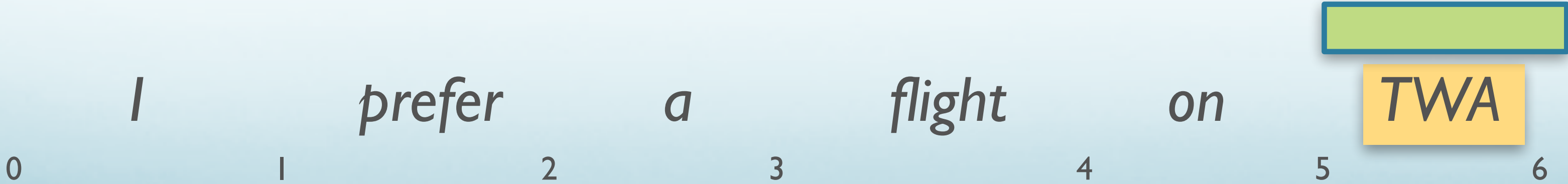
NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	
			Noun, Nom [3,4]	[3,5]	
				Prep [4,5]	



\mathcal{L}_1 Grammar	
$S \rightarrow NP\ VP$	
$S \rightarrow X1\ VP$	
$X1 \rightarrow Aux\ NP$	
$S \rightarrow book\ /\ include\ /\ prefer$	
$S \rightarrow Verb\ NP$	
$S \rightarrow X2\ PP$	
$S \rightarrow Verb\ PP$	
$S \rightarrow VP\ PP$	
<hr/>	
$NP \rightarrow I\ /\ she\ /\ me$	
$NP \rightarrow TWA\ /\ Houston$	
$NP \rightarrow Det\ Nominal$	
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$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$	
$Nominal \rightarrow Nominal\ Noun$	
$Nominal \rightarrow Nominal\ PP$	
<hr/>	
$VP \rightarrow book\ /\ include\ /\ prefer$	
$VP \rightarrow Verb\ NP$	
$VP \rightarrow X2\ PP$	
$X2 \rightarrow Verb\ NP$	
$VP \rightarrow Verb\ PP$	
$VP \rightarrow VP\ PP$	
<hr/>	
$PP \rightarrow Preposition\ NP$	
<hr/>	

Lexicon	
$Det \rightarrow that\ /\ this\ /\ a$	
$Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$	
$Pronoun \rightarrow I\ /\ she\ /\ me$	
$Proper-Noun \rightarrow Houston\ /\ TWA$	
$Aux \rightarrow does$	
$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$	
$Verb \rightarrow book\ /\ include\ /\ prefer$	

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	
			Noun, Nom [3,4]	[3,5]	
				Prep [4,5]	
					NNP, NP [5,6]



\mathcal{L}_1 Grammar	
$S \rightarrow NP\ VP$	
$S \rightarrow X1\ VP$	
$X1 \rightarrow Aux\ NP$	
$S \rightarrow book\ /\ include\ /\ prefer$	
$S \rightarrow Verb\ NP$	
$S \rightarrow X2\ PP$	
$S \rightarrow Verb\ PP$	
$S \rightarrow VP\ PP$	
$NP \rightarrow I\ /\ she\ /\ me$	
$NP \rightarrow TWA\ /\ Houston$	
$NP \rightarrow Det\ Nominal$	
$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$	
$Nominal \rightarrow Nominal\ Noun$	
$Nominal \rightarrow Nominal\ PP$	
$VP \rightarrow book\ /\ include\ /\ prefer$	
$VP \rightarrow Verb\ NP$	
$VP \rightarrow X2\ PP$	
$X2 \rightarrow Verb\ NP$	
$VP \rightarrow Verb\ PP$	
$VP \rightarrow VP\ PP$	
$PP \rightarrow$	$Preposition\ NP$

Lexicon	
$Det \rightarrow that\ /\ this\ /\ a$	
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$Pronoun \rightarrow I\ /\ she\ /\ me$	
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$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$	
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	
			Noun, Nom [3,4]	[3,5]	
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar	
$S \rightarrow NP\ VP$	
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$S \rightarrow Verb\ PP$	
$S \rightarrow VP\ PP$	
<hr/>	
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$NP \rightarrow Det\ Nominal$	
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$Nominal \rightarrow Nominal\ Noun$	
$Nominal \rightarrow Nominal\ PP$	
<hr/>	
$VP \rightarrow book\ /\ include\ /\ prefer$	
$VP \rightarrow Verb\ NP$	
$VP \rightarrow X2\ PP$	
$X2 \rightarrow Verb\ NP$	
$VP \rightarrow Verb\ PP$	
$VP \rightarrow VP\ PP$	
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$PP \rightarrow Preposition\ NP$	
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$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$	
$Verb \rightarrow book\ /\ include\ /\ prefer$	

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

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$Aux \rightarrow does$
$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

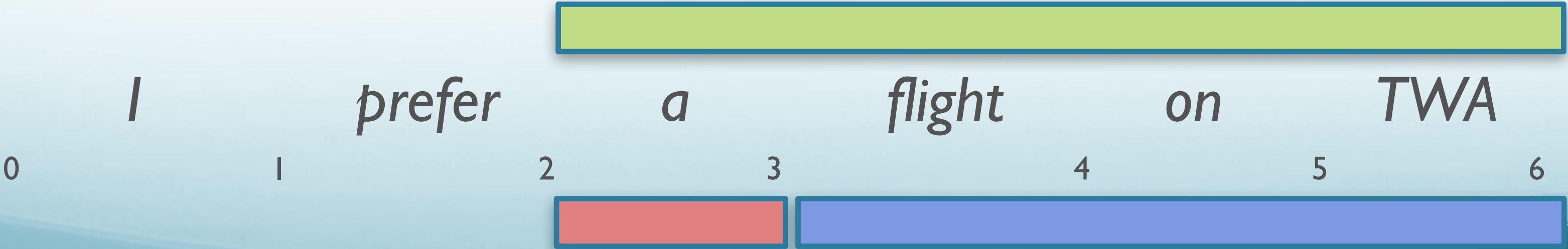
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 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

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 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

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$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

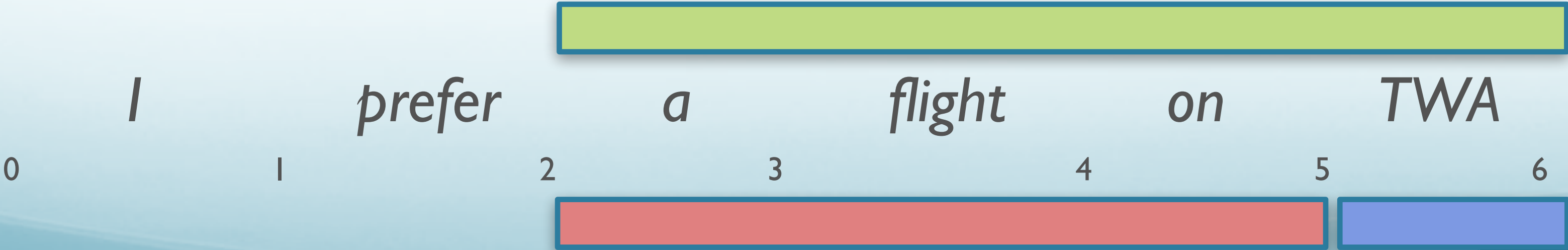
$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

Lexicon
$Det \rightarrow that \mid this \mid a$
$Noun \rightarrow book \mid flight \mid meal \mid money$
$Pronoun \rightarrow I \mid she \mid me$
$Proper-Noun \rightarrow Houston \mid TWA$
$Aux \rightarrow does$
$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

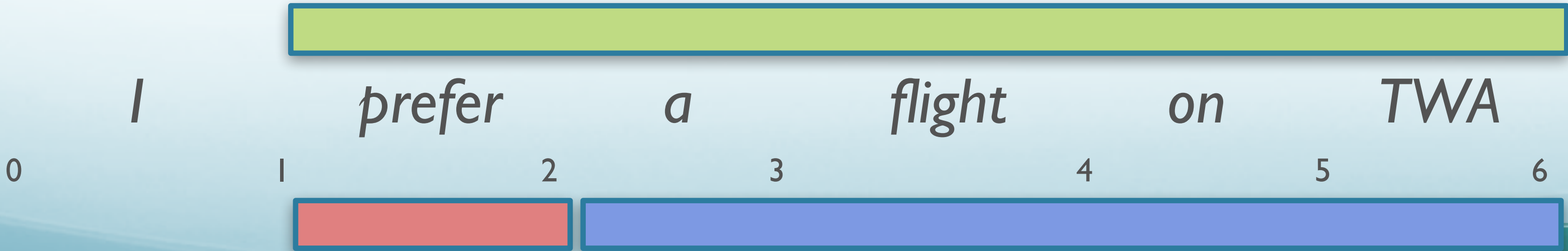
$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

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$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	[1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

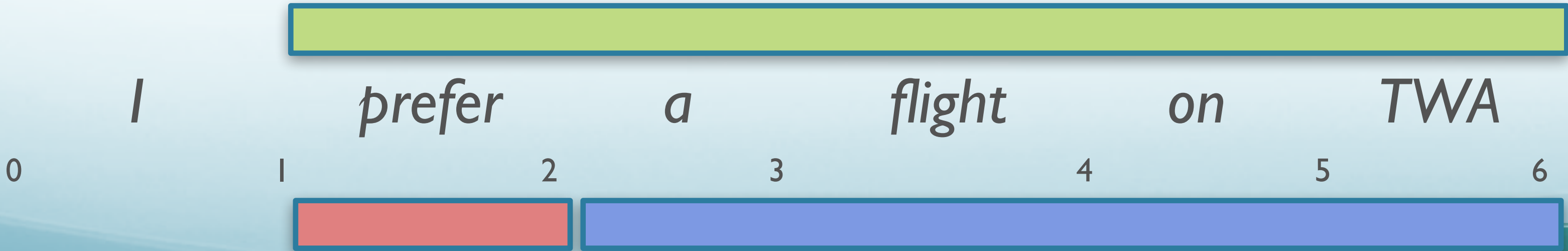
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]

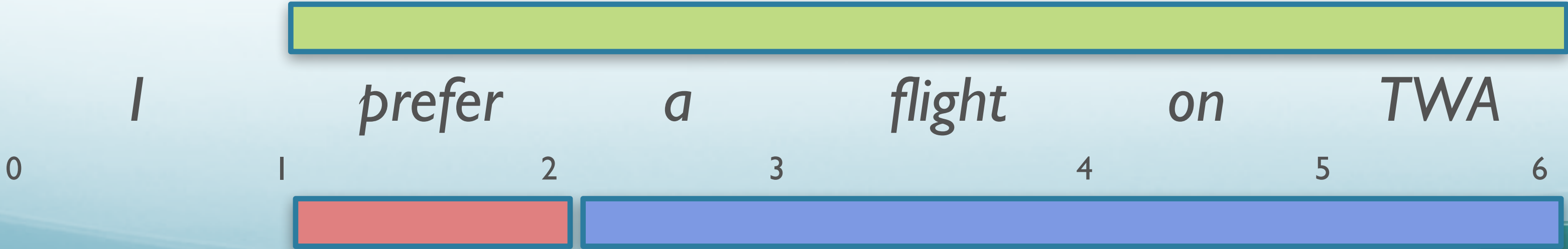


\mathcal{L}_1 Grammar	
$S \rightarrow NP\ VP$	
$S \rightarrow X1\ VP$	
$X1 \rightarrow Aux\ NP$	
$S \rightarrow book\ /\ include\ /\ prefer$	
$S \rightarrow Verb\ NP$	
$S \rightarrow X2\ PP$	
$S \rightarrow Verb\ PP$	
$S \rightarrow VP\ PP$	
<hr/>	
$NP \rightarrow I\ /\ she\ /\ me$	
$NP \rightarrow TWA\ /\ Houston$	
$NP \rightarrow Det\ Nominal$	
<hr/>	
$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$	
$Nominal \rightarrow Nominal\ Noun$	
$Nominal \rightarrow Nominal\ PP$	
<hr/>	
$VP \rightarrow book\ /\ include\ /\ prefer$	
$VP \rightarrow Verb\ NP$	
$VP \rightarrow X2\ PP$	
$X2 \rightarrow Verb\ NP$	
$VP \rightarrow Verb\ PP$	
$VP \rightarrow VP\ PP$	
<hr/>	
$PP \rightarrow Preposition\ NP$	
<hr/>	

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$Det \rightarrow that\ /\ this\ /\ a$	
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$Aux \rightarrow does$	
$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$	
$Verb \rightarrow book\ /\ include\ /\ prefer$	

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2 [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

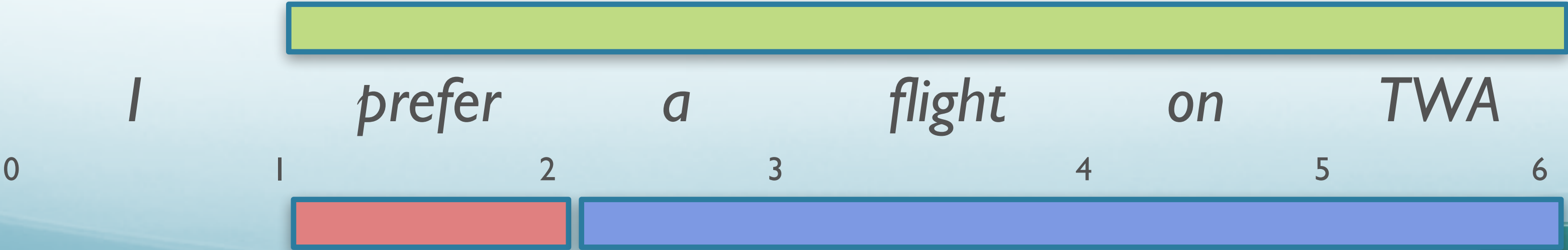
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ |\ include\ |\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ |\ she\ |\ me$
 $NP \rightarrow TWA\ |\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ |\ flight\ |\ meal\ |\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

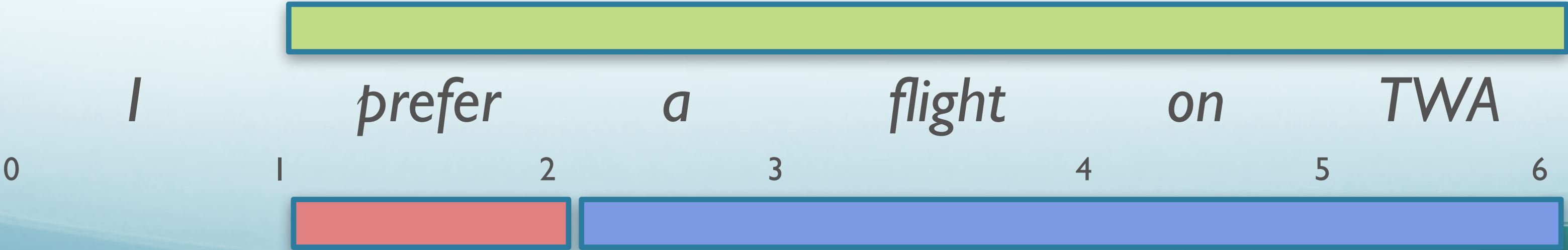
$VP \rightarrow book\ |\ include\ |\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ |\ this\ |\ a$
 $Noun \rightarrow book\ |\ flight\ |\ meal\ |\ money$
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 $Preposition \rightarrow from\ |\ to\ |\ on\ |\ near\ |\ through$
 $Verb \rightarrow book\ |\ include\ |\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP , S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]		NP [2,6]
			Noun, Nom [3,4]		Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

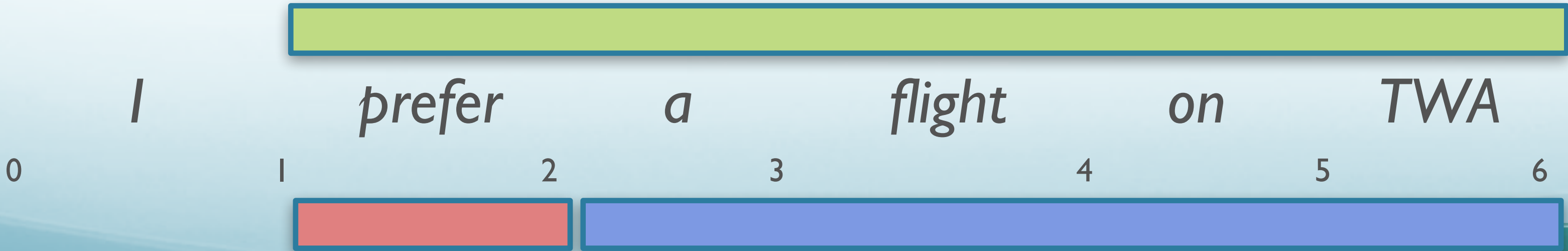
$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

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$Aux \rightarrow does$
$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]		S [0,4]		
	Verb, VP, S [1,2]		VP, X2, S [1,4]		VP, X2, S [1,6]
		Det [2,3]	NP [2,4]		NP [2,6]
			Noun, Nom [3,4]		Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



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$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

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$Aux \rightarrow does$
$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]		S [0,4]		
	Verb, VP, S [1,2]		VP, X2, S [1,4]		VP, X2, S [1,6]
		Det [2,3]	NP [2,4]		NP [2,6]
			Noun, Nom [3,4]		Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
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 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
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 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

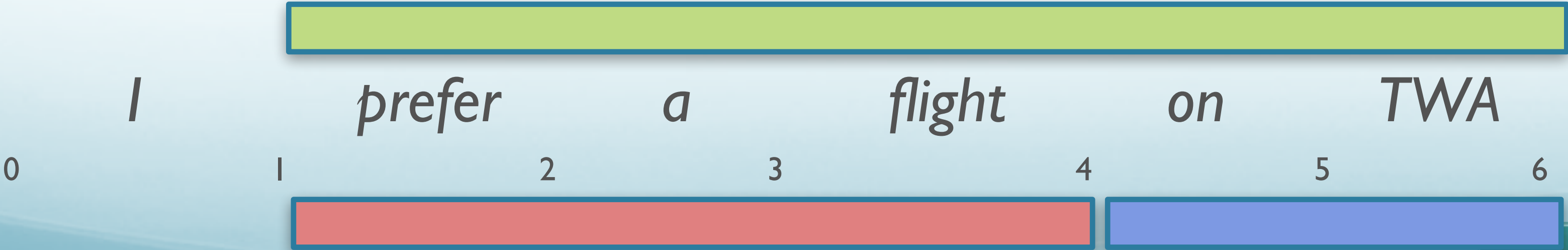
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $S \rightarrow book \mid include \mid prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$

$S \rightarrow VP\ PP$

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 $NP \rightarrow TWA \mid Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

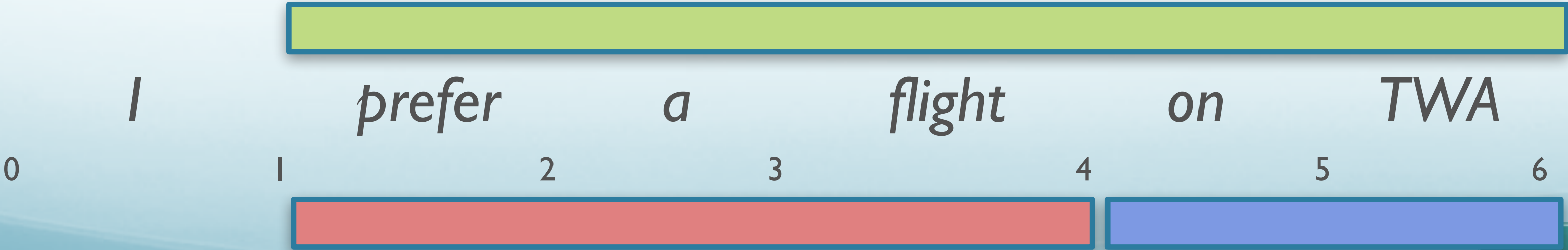
$VP \rightarrow book \mid include \mid prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

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 $Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]

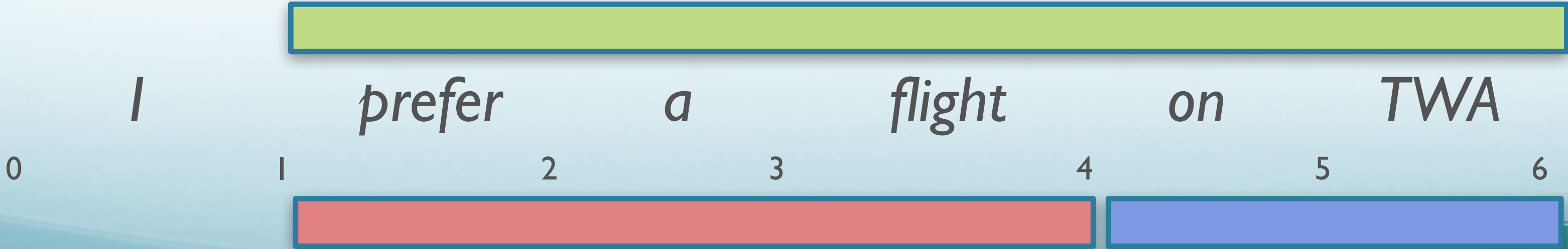


\mathcal{L}_1 Grammar	
$S \rightarrow NP\ VP$	
$S \rightarrow X1\ VP$	
$X1 \rightarrow Aux\ NP$	
$S \rightarrow book\ /\ include\ /\ prefer$	
$S \rightarrow Verb\ NP$	
$S \rightarrow X2\ PP$	
$S \rightarrow Verb\ PP$	
$S \rightarrow VP\ PP$	
<hr/>	
$NP \rightarrow I\ /\ she\ /\ me$	
$NP \rightarrow TWA\ /\ Houston$	
$NP \rightarrow Det\ Nominal$	
<hr/>	
$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$	
$Nominal \rightarrow Nominal\ Noun$	
$Nominal \rightarrow Nominal\ PP$	
<hr/>	
$VP \rightarrow book\ /\ include\ /\ prefer$	
$VP \rightarrow Verb\ NP$	
$VP \rightarrow X2\ PP$	
$X2 \rightarrow Verb\ NP$	
$VP \rightarrow Verb\ PP$	
$VP \rightarrow VP\ PP$	
<hr/>	
$PP \rightarrow Preposition\ NP$	
<hr/>	

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$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$	
$Verb \rightarrow book\ /\ include\ /\ prefer$	

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$

$S \rightarrow X1\ VP$

$X1 \rightarrow Aux\ NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb\ NP$

$S \rightarrow X2\ PP$

$S \rightarrow Verb\ PP$

$S \rightarrow VP\ PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal\ Noun$

$Nominal \rightarrow Nominal\ PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb\ NP$

$VP \rightarrow X2\ PP$

$X2 \rightarrow Verb\ NP$

$VP \rightarrow Verb\ PP$

$VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

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$Aux \rightarrow does$
$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
$Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

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$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

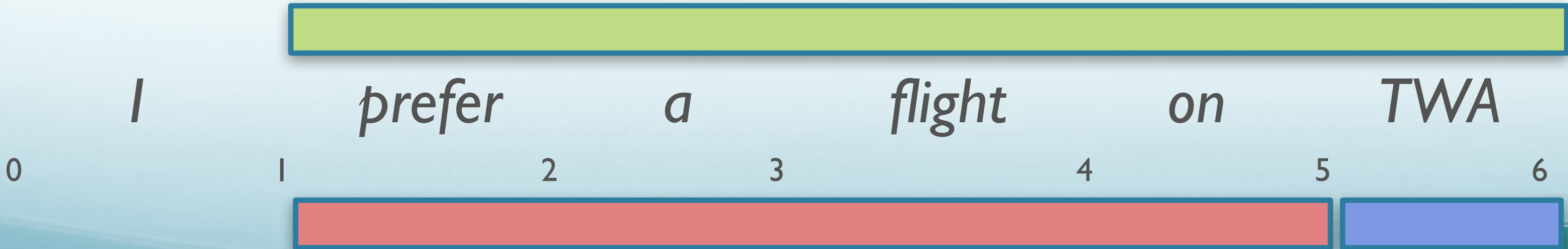
$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

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$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]		S [0,4]		
	Verb, VP, S [1,2]		VP, X2, S [1,4]		VP, X2, S [1,6]
		Det [2,3]	NP [2,4]		NP [2,6]
			Noun, Nom [3,4]		Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

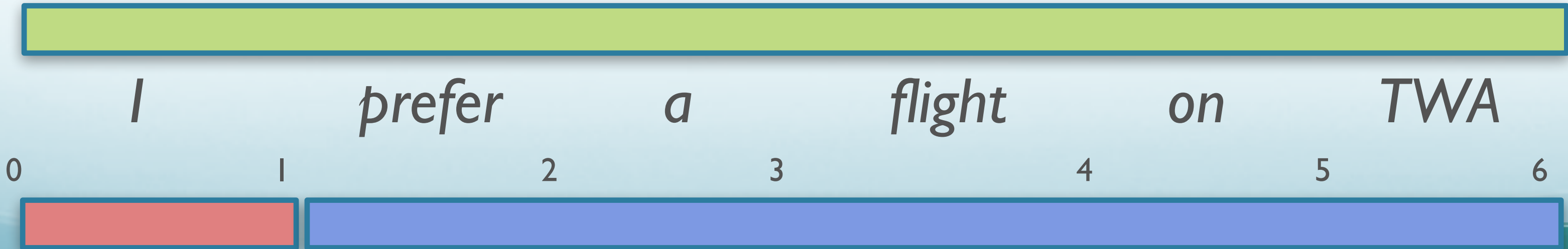
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
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 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	[0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

Lexicon

$Det \rightarrow that \mid this \mid a$

$Noun \rightarrow book \mid flight \mid meal \mid money$

$Pronoun \rightarrow I \mid she \mid me$

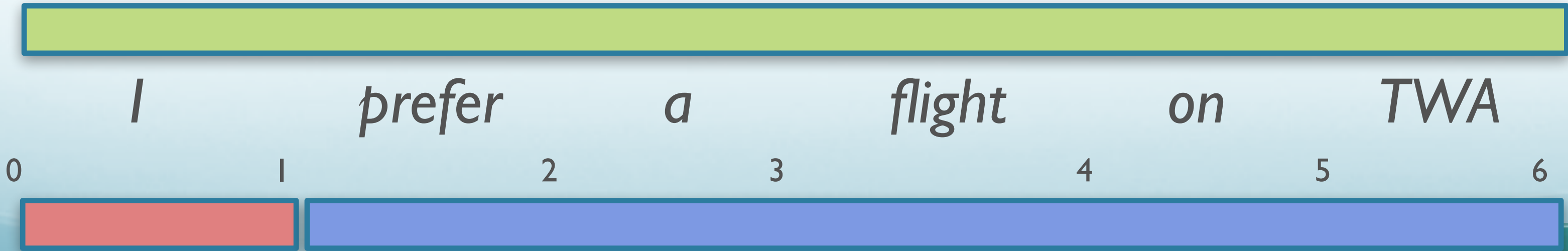
$Proper-Noun \rightarrow Houston \mid TWA$

$Aux \rightarrow does$

$Preposition \rightarrow from \mid to \mid on \mid near \mid through$

$Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
 $S \rightarrow X1\ VP$
 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

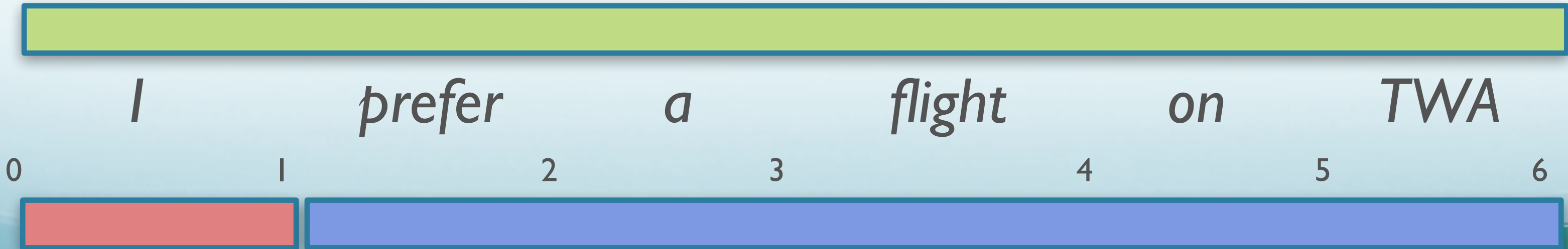
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
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NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]		NP [2,6]
			Noun, Nom [3,4]		Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

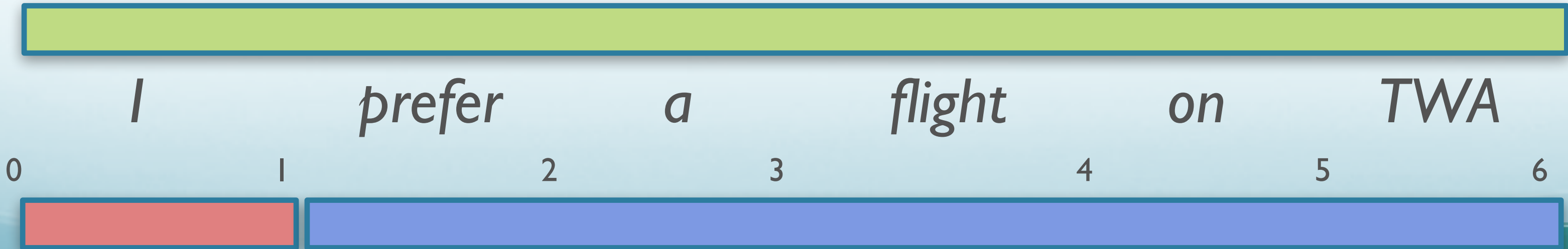
$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

Lexicon
$Det \rightarrow that \mid this \mid a$
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$Aux \rightarrow does$
$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]		S [0,4]		S [0,6]
	Verb, VP, S [1,2]		VP, X2, S [1,4]		VP, X2, S [1,6]
		Det [2,3]	NP [2,4]		NP [2,6]
			Noun, Nom [3,4]		Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP\ VP$
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 $X1 \rightarrow Aux\ NP$
 $S \rightarrow book\ /\ include\ /\ prefer$
 $S \rightarrow Verb\ NP$
 $S \rightarrow X2\ PP$
 $S \rightarrow Verb\ PP$
 $S \rightarrow VP\ PP$

$NP \rightarrow I\ /\ she\ /\ me$
 $NP \rightarrow TWA\ /\ Houston$
 $NP \rightarrow Det\ Nominal$

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 $Nominal \rightarrow Nominal\ Noun$
 $Nominal \rightarrow Nominal\ PP$

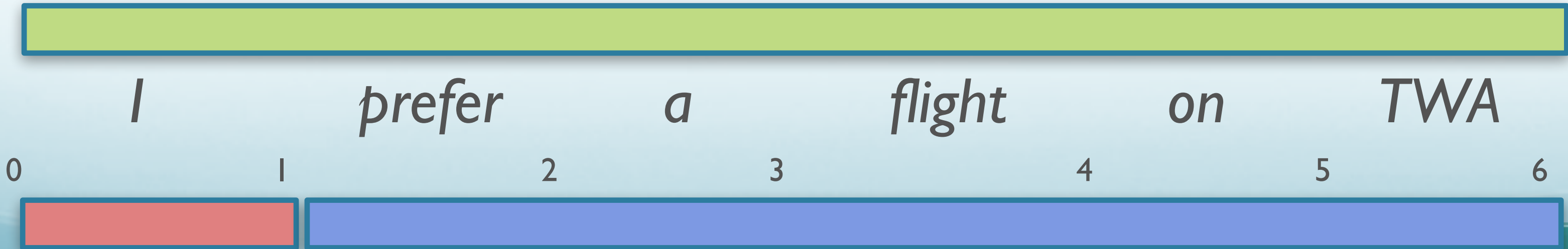
$VP \rightarrow book\ /\ include\ /\ prefer$
 $VP \rightarrow Verb\ NP$
 $VP \rightarrow X2\ PP$
 $X2 \rightarrow Verb\ NP$
 $VP \rightarrow Verb\ PP$
 $VP \rightarrow VP\ PP$

$PP \rightarrow Preposition\ NP$

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$
 $Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$
 $Pronoun \rightarrow I\ /\ she\ /\ me$
 $Proper-Noun \rightarrow Houston\ /\ TWA$
 $Aux \rightarrow does$
 $Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$
 $Verb \rightarrow book\ /\ include\ /\ prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar

$S \rightarrow NP VP$

$S \rightarrow X1 VP$

$X1 \rightarrow Aux NP$

$S \rightarrow book \mid include \mid prefer$

$S \rightarrow Verb NP$

$S \rightarrow X2 PP$

$S \rightarrow Verb PP$

$S \rightarrow VP PP$

$NP \rightarrow I \mid she \mid me$

$NP \rightarrow TWA \mid Houston$

$NP \rightarrow Det Nominal$

$Nominal \rightarrow book \mid flight \mid meal \mid money$

$Nominal \rightarrow Nominal Noun$

$Nominal \rightarrow Nominal PP$

$VP \rightarrow book \mid include \mid prefer$

$VP \rightarrow Verb NP$

$VP \rightarrow X2 PP$

$X2 \rightarrow Verb NP$

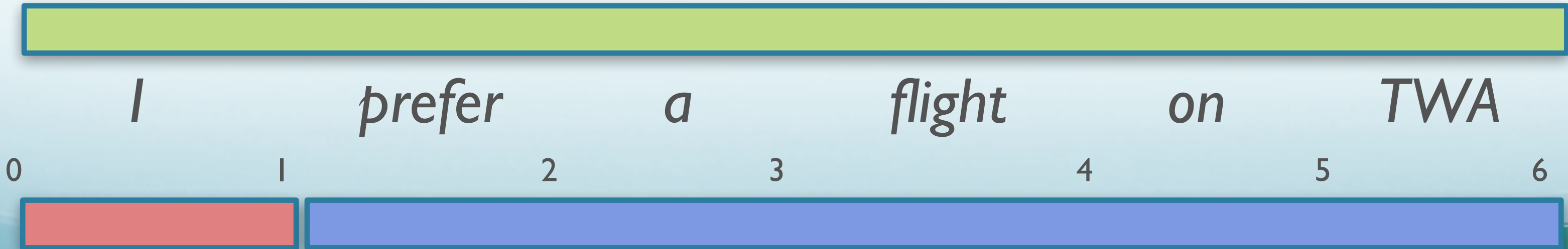
$VP \rightarrow Verb PP$

$VP \rightarrow VP PP$

$PP \rightarrow Preposition NP$

Lexicon
$Det \rightarrow that \mid this \mid a$
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$Aux \rightarrow does$
$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Verb \rightarrow book \mid include \mid prefer$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]



\mathcal{L}_1 Grammar	
$S \rightarrow NP\ VP$	
$S \rightarrow X1\ VP$	
$X1 \rightarrow Aux\ NP$	
$S \rightarrow book\ /\ include\ /\ prefer$	
$S \rightarrow Verb\ NP$	
$S \rightarrow X2\ PP$	
$S \rightarrow Verb\ PP$	
$S \rightarrow VP\ PP$	
<hr/>	
$NP \rightarrow I\ /\ she\ /\ me$	
$NP \rightarrow TWA\ /\ Houston$	
$NP \rightarrow Det\ Nominal$	
<hr/>	
$Nominal \rightarrow book\ /\ flight\ /\ meal\ /\ money$	
$Nominal \rightarrow Nominal\ Noun$	
$Nominal \rightarrow Nominal\ PP$	
<hr/>	
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$VP \rightarrow Verb\ NP$	
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$VP \rightarrow Verb\ PP$	
$VP \rightarrow VP\ PP$	
<hr/>	
$PP \rightarrow Preposition\ NP$	
<hr/>	

Lexicon

$Det \rightarrow that\ /\ this\ /\ a$	
$Noun \rightarrow book\ /\ flight\ /\ meal\ /\ money$	
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$Proper-Noun \rightarrow Houston\ /\ TWA$	
$Aux \rightarrow does$	
$Preposition \rightarrow from\ /\ to\ /\ on\ /\ near\ /\ through$	
$Verb \rightarrow book\ /\ include\ /\ prefer$	

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	S [0,6]
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP, X2, S [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]

0

1

2

3

4

5

6

I
prefer
a
flight
on
TWA

Current CKY Algorithm

- Limitations:
- Only stores non-terminals in cell
 - Not rules or cells corresponding to RHS
- Stores SETS of non-terminals
 - Multiple rules with same LHS collide
- Currently only ***acceptance/recognition***

CKY *Parser*

- Pair each nonterminal with backpointer to cells from which it was derived
- Last step: construct trees from backpointers in $[0, n]$

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]

$VP \rightarrow VP PP$

```
bp_1 = BackPointer()
bp_1.l_child = [VP, (1,4)]
bp_1.r_child = [PP, (4,6)]
```

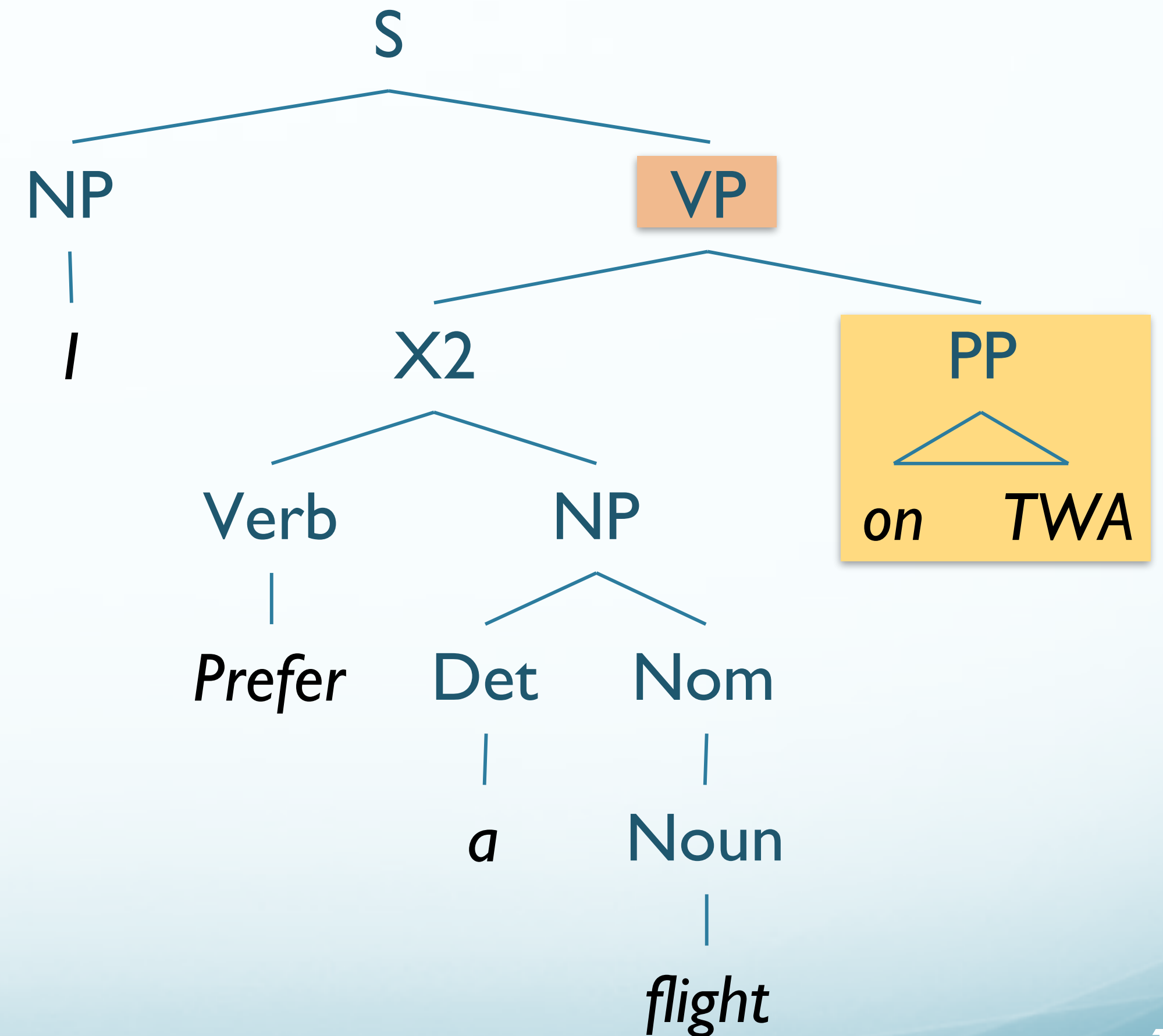
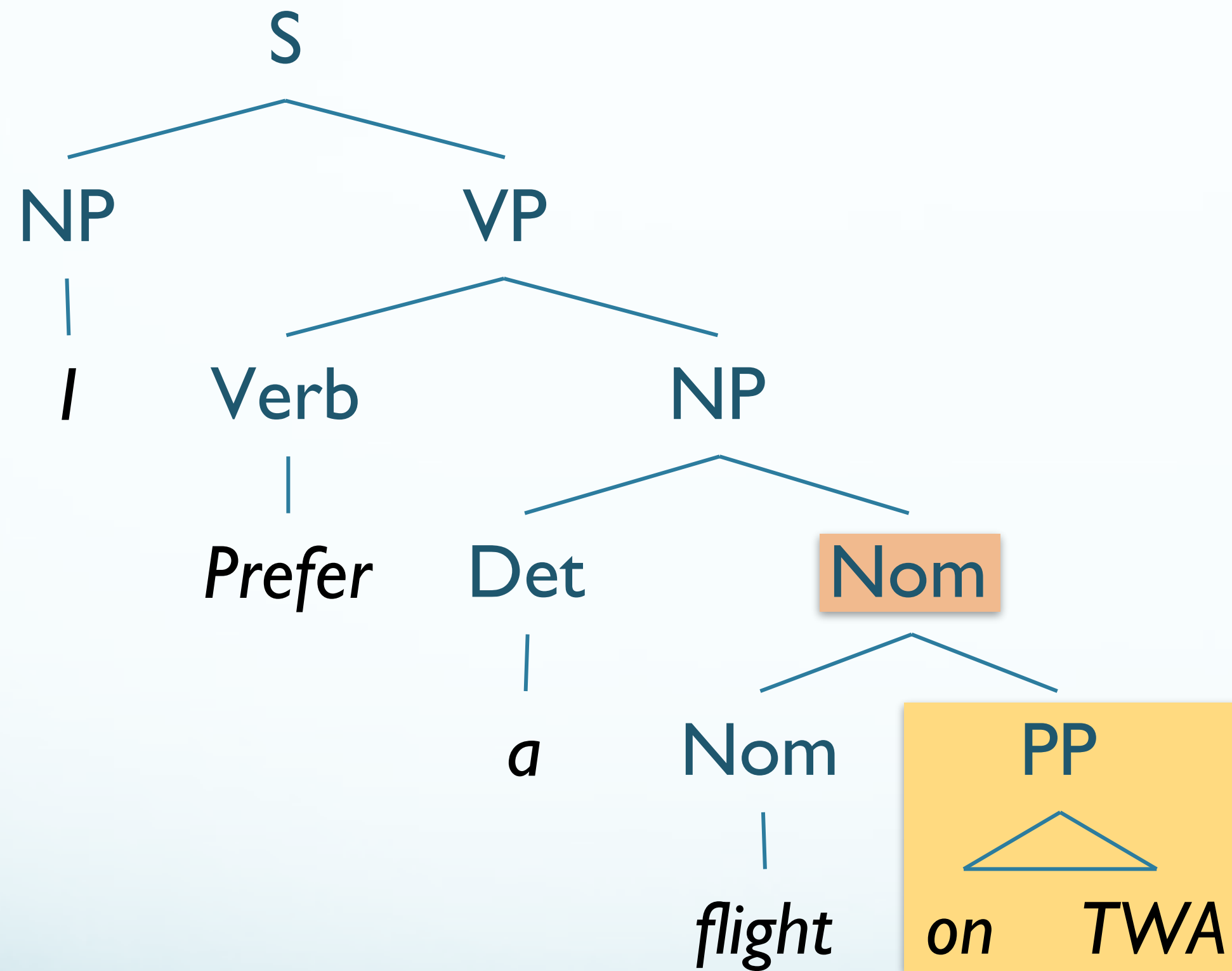
NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]

$VP \rightarrow X_2 PP$

```
bp_2 = BackPointer()
bp_2.l_child = [X2, (1,4)]
bp_2.r_child = [PP, (4,6)]
```

NP, Pronoun [0,1]	S [0,2]	[0,3]	S [0,4]	[0,5]	
	Verb, VP, S [1,2]	[1,3]	VP, X2, S [1,4]	[1,5]	VP [1,6]
		Det [2,3]	NP [2,4]	[2,5]	NP [2,6]
			Noun, Nom [3,4]	[3,5]	Nom [3,6]
				Prep [4,5]	PP [4,6]
					NNP, NP [5,6]

Resulting Parses



CKY Discussion

- Running time:
 - $O(n^3)$ where n is the length of the input string
 - Inner loop grows as square of # of non-terminals
- Expressiveness:
 - As implemented, requires CNF
 - Weak equivalence to original grammar
 - Doesn't capture full original structure
 - Back-conversion?
 - Can do binarization, terminal conversion
 - Unit productions requires change in CKY

Parsing: PCFGs

Ling 571

Deep Processing Techniques for NLP

January 18, 2017

Probabilistic Context-free Grammars: Roadmap

- Motivation: Ambiguity
- Approach:
 - Definition
 - Disambiguation
 - Parsing
 - Evaluation
 - Enhancements

Motivation

- What about ambiguity?
- Current algorithm can ***represent*** it
- ...can't resolve it.

Probabilistic Parsing

- Provides strategy for solving disambiguation problem
 - Compute the probability of all analyses
 - Select the most probable
- Employed in language modeling for speech recognition
 - N-gram grammars predict words, constrain search
 - Also, constrain generation, translation

PCFGs: Formal Definition

N	a set of non-terminal symbols (or variables)
Σ	a set of terminal symbols (disjoint from N)
R	a set of rules of productions, each of the form $A \rightarrow \beta[p]$, where A is a non-terminal where A is a non-terminal, β is a string of symbols from the infinite set of strings $(\Sigma \cup N)^*$ and p is a number between 0 and 1 expressing $P(\beta A)$
S	a designated start symbol

PCFGs

- Augment each production with probability that LHS will be expanded as RHS
 - $P(A \rightarrow \beta)$
 - $P(A \rightarrow \beta | A)$
 - $P(RHS \mid LHS)$

PCFGs

- Sum over all possible expansions is 1

$$\sum_{\beta} P(A \rightarrow \beta) = 1$$

- A PCFG is **consistent** if sum of probabilities of all sentences in language is 1
 - Recursive rules often yield inconsistent grammars ([Booth & Thompson, 1973](#))

Example PCFG: Augmented \mathcal{L}_1

Grammar		Lexicon
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30] \mid meal [.15] \mid money [0.5]$
$S \rightarrow VP$	[.05]	$\mid flights [0.40] \mid dinner [.10]$
$NP \rightarrow Pronoun$	[.35]	$Verb \rightarrow book [.30] \mid include [.30] \mid prefer [.40]$
$NP \rightarrow Proper-Noun$	[.30]	$Pronoun \rightarrow I [.40] \mid she [.05] \mid me [.15] \mid you [.40]$
$NP \rightarrow Det Nominal$	[.20]	$Proper-Noun \rightarrow Houston [.60] \mid NWA [.40]$
$NP \rightarrow Nominal$	[.15]	$Aux \rightarrow does [.60] \mid can [.40]$
$Nominal \rightarrow Noun$	[.75]	$Preposition \rightarrow from [.30] \mid to [.30] \mid on [.20] \mid near [.15]$
$Nominal \rightarrow Nominal Noun$	[.20]	$\mid through [.05]$
$Nominal \rightarrow Nominal PP$	[.05]	
$VP \rightarrow Verb$	[.35]	
$VP \rightarrow Verb NP$	[.20]	
$VP \rightarrow Verb NP PP$	[.10]	
$VP \rightarrow Verb PP$	[.15]	
$VP \rightarrow Verb NP NP$	[.05]	
$VP \rightarrow VP PP$	[.15]	
$PP \rightarrow Preposition NP$	[1.0]	

Example PCFG: Augmented \mathcal{L}_1

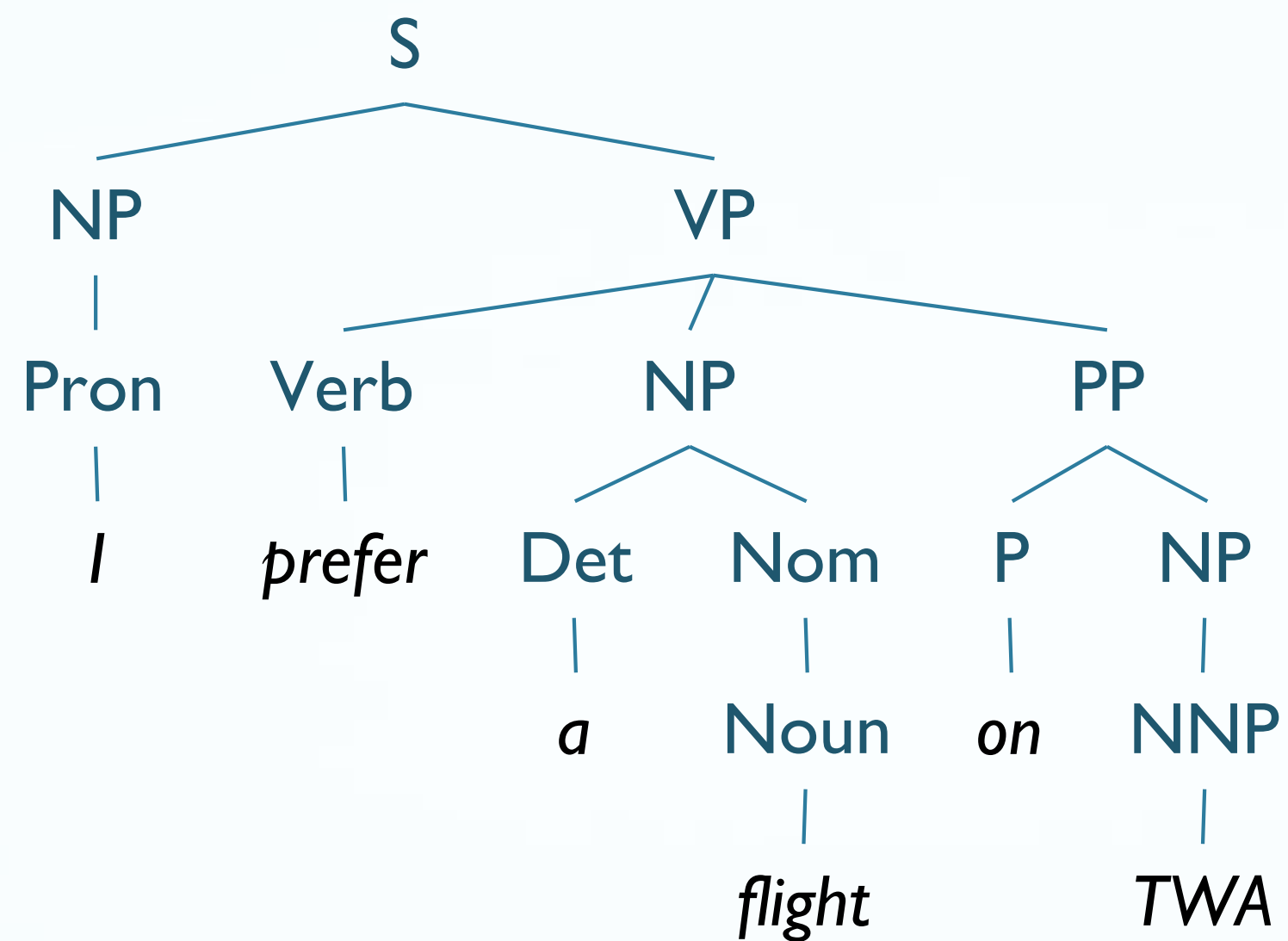
Grammar		Lexicon	
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$	
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30] \mid meal [.15] \mid money [0.5]$	
$S \rightarrow VP$	[.05]	$\mid flights [0.40] \mid dinner [.10]$	
$NP \rightarrow Pronoun$	[.35]	$Verb \rightarrow book [.30] \mid include [.30] \mid prefer [.40]$	
$NP \rightarrow Proper-Noun$	[.30]	$Pronoun \rightarrow I [.40] \mid she [.05] \mid me [.15] \mid you [.40]$	
$NP \rightarrow Det Nominal$	[.20]	$Proper-Noun \rightarrow Houston [.60] \mid NWA [.40]$	
$NP \rightarrow Nominal$	[.15]	$Aux \rightarrow does [.60] \mid can [.40]$	
$Nominal \rightarrow Noun$	[.75]	$Preposition \rightarrow from [.30] \mid to [.30] \mid on [.20] \mid near [.15]$	
$Nominal \rightarrow Nominal Noun$	[.20]	$\mid through [.05]$	
$Nominal \rightarrow Nominal PP$	[.05]		
$VP \rightarrow Verb$	[.35]		
$VP \rightarrow Verb NP$	[.20]		
$VP \rightarrow Verb NP PP$	[.10]		
$VP \rightarrow Verb PP$	[.15]		
$VP \rightarrow Verb NP NP$	[.05]		
$VP \rightarrow VP PP$	[.15]		
$PP \rightarrow Preposition NP$	[1.0]		

Disambiguation

- A PCFG assigns probability to each parse tree T for input S
- Probability of T : product of all rules used to derive T

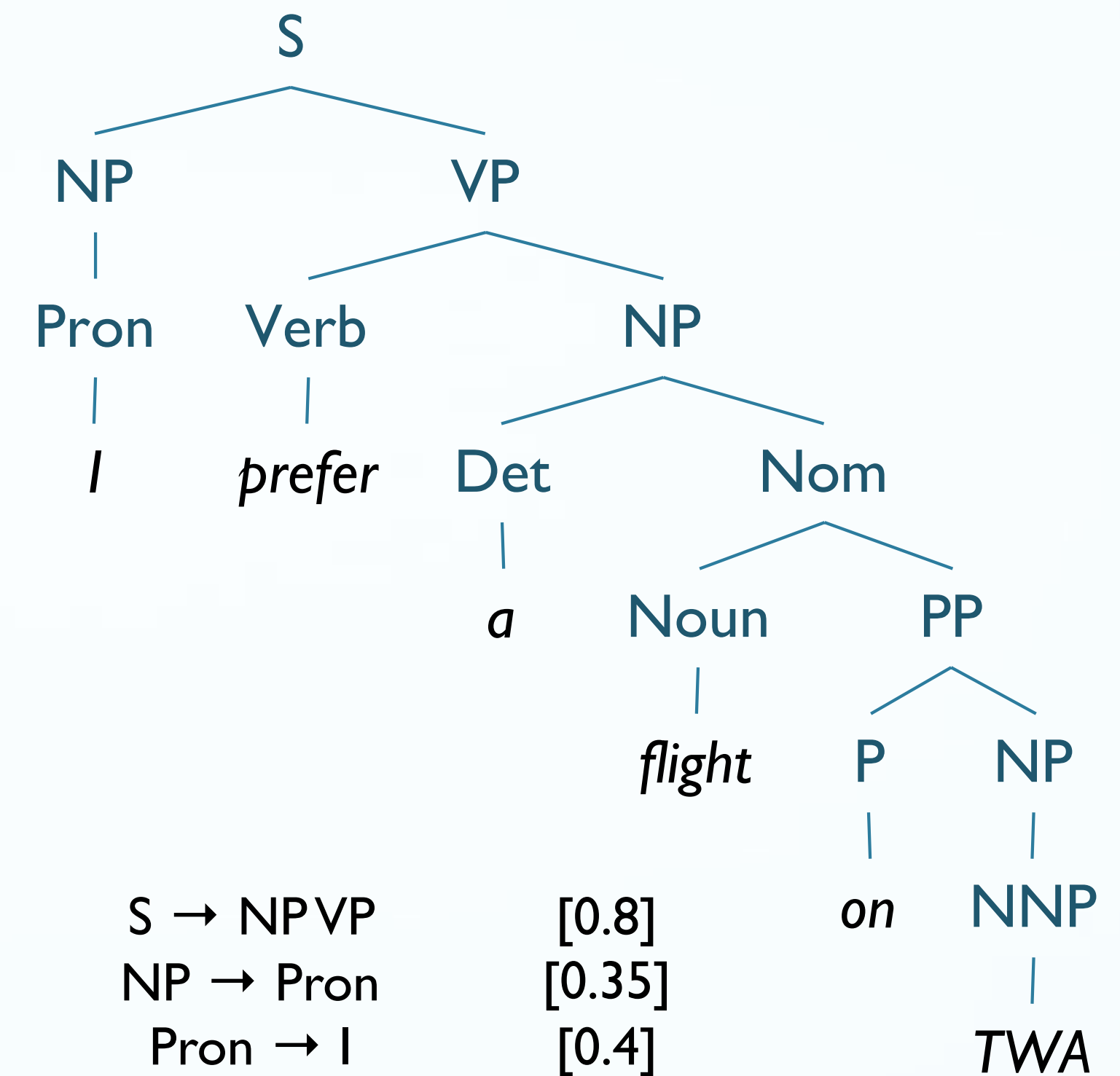
$$P(T, S) = \prod_{i=1}^n P(RHS_i | LHS_i)$$

$$P(T, S) = P(T)P(S | T) = P(T)$$



$S \rightarrow NP VP$	[0.8]
$NP \rightarrow Pron$	[0.35]
$Pron \rightarrow I$	[0.4]
$VP \rightarrow V NP PP$	[0.1]
$V \rightarrow prefer$	[0.4]
$NP \rightarrow Det Nom$	[0.2]
$Det \rightarrow a$	[0.3]
$Nom \rightarrow N$	[0.75]
$N \rightarrow flight$	[0.3]
$PP \rightarrow P NP$	[1.0]
$P \rightarrow on$	[0.2]
$NP \rightarrow NNP$	[0.3]
$NNP \rightarrow NWA$	[0.4]

$\sim 1.452 \times 10^{-6}$



$S \rightarrow NP VP$	[0.8]
$NP \rightarrow Pron$	[0.35]
$Pron \rightarrow I$	[0.4]
$VP \rightarrow V NP$	[0.2]
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$NP \rightarrow Det Nom$	[0.2]
$Det \rightarrow a$	[0.3]
$Nom \rightarrow Nom PP$	[0.05]
$Nom \rightarrow N$	[0.75]
$N \rightarrow flight$	[0.3]
$PP \rightarrow P NP$	[1.0]
$P \rightarrow on$	[0.2]
$NP \rightarrow NNP$	[0.3]
$NNP \rightarrow NWA$	[0.4]

$\sim 1.452 \times 10^{-7}$

Parsing Problem for PCFGs

- Select T such that (*s.t.*)

$$\hat{T}(S) = \operatorname{argmax}_{Ts.t.S=yield(T)} P(T)$$

- String of words S is *yield* of parse tree
- Select the tree \hat{T} that maximizes the probability of the parse

Unit Testing

Unit Testing

- Strategy of testing individual pieces of code in isolation
- Helps ensure:
 - Basic functionality in isolation
 - Complex functionality when individual components are combined

Unit Testing in Python

- Many good tutorials on the web [[here's one](#)]
- In a nutshell:

```
from unittest import TestCase
```

```
class longTests(TestCase):
```

```
    def test_three(self):
```

```
        length_3_rule = parse Productions('A -> B C D')
```

```
        target_rules = parse Productions('' 'A -> B _X0_  
                                         _X0_ -> C D' '')
```

```
        self.assertEqual(set(target_rules),  
                          set(fix_long_rules(length_3_rule)))
```


Unit Testing in Python

- “nose” is a test running framework that will detect all `test_*` method functions
`python3 -m nose hw2.py`

```
AssertionError: Items in the first set but not the second:
```

```
A -> B _X0_
```

```
_X0_ -> C D
```

```
Items in the second set but not the first:
```

```
A -> B C
```

```
-----  
Ran 12 tests in 0.040s
```

```
FAILED (failures=1)
```

Unit Testing

- Good practice:
 - Save input that crashes your program for a unit test

HW #3

CKY Parsing: Goals

- Complete implementation of CKY parser
- Implement dynamic programming approach
- Incorporate/follow backpointers to recover parse

Implementation

- Build full parser
- Can use any language, per course policies
- You may use existing data structures for rules, trees
 - e.g. NLTK has nice **tree** data structure
 - CKY algorithm must be your own
- Dynamic programming table filling crucial!
- Will use smaller grammar (similar to HW #1)
- Back to ATIS for HW #4

Notes

- Teams:
 - You may work in teams of two on this assignment
- Test grammar
 - Pre-converted to CNF
 - Start symbol: **TOP**
 - Parse should span input and be rooted at: **TOP**