

CSE331

Assignment 1

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Section: 16

Answer:

a. $L_1 = \{w \in \{0,1\}^* \mid 0^i 1^j \text{ where } i > j\}$

Assume L_1 is a regular Language

P the pumping length.

$$L_1 = 0^{P+1} 1^P$$

$[1 \leq 2]$
 $P = 4$

$$L_1 = 0^{4+1} 1^4 = 00000 1111$$

the pumping lemma $xy^iz \in L_1$

when $i = 0$ it $xy^0z = xz$

remove the string y decrease the number of 0, when xz there are

can not have more 0 than 1, it not

regular member of L_1 .

~~Do it~~ no L_1 is not regular

⑥

$$L_2 = \{w \in \{0,1\}^* \mid 0^i 1^j \text{ where } i \leq 2j\}$$

Assume \$L_2\$ is regular. Then there exists a pumping lemma string \$s\$.

approx \$L_2\$ is regular. Pumping lemma string \$s\$.

$$L_2 = 0^{3p-1} 1^p$$

$$x = 0^\alpha \quad y = 0^\beta \quad z = 0^{3p-1-\alpha-\beta} 1^p \quad [p \geq 1]$$

$$x y^i z = 0^\alpha 0^{i\beta} 0^{3p-1-\alpha-\beta} 1^p 0^{1+p} = 0^{3p-1-\beta+i\beta} 1^p \in L_2$$

$$3p-1+i\beta-\beta \leq 3p \quad \text{if } i=0 \text{ then } -1 \leq 0$$

$$\Rightarrow -1 + i\beta - \beta \leq 0$$

$$\Rightarrow i\beta - \beta \leq 1$$

$$\Rightarrow \beta(i-1) \leq 1$$

if \$i=2\$

$$2\beta - \beta \geq 1$$

$$\beta \geq 1$$

\$\therefore L_2\$ is not regular.

c. $L_3 = \{w \in \{0,1,2\}^* : 0^n 1^n 2^n \text{ where } n \geq 0\}$

$$L_3 = \{ \epsilon, 012, \dots \}$$

Assume L_3 is a regular language.
Pumping length is m

$$f = 0^m 1^m 2^m$$

So, if $m=4$ then we have loops for each 0, 1, 2.

$m=4$ so $f = 0^4 1^4 2^4$

$f = 000011112222$

Case 1.

$$\begin{array}{c} \underline{0000} \quad \underline{1111} \quad \underline{2222} \\ u \quad v \quad x \quad y \quad z \end{array}$$

$$uv^i x y^i z$$

$i=2$ $uv^2 x y^2 z$

$$000000011112222$$

$$0^6 1^4 2^5 \notin L_3$$

Case 2

$\underbrace{0000}_u \underbrace{1111}_v \underbrace{2222}_z$

$uv^i x y^i z$

$i=2 \quad uv^2 x y^2 z$

$000011001111112222 \notin L_3$
 $0^6 1^7 2^4$

So there are not equal numbers of 0, 1, 2.

It violates the pumping lemma.

We can say that L_3 is not regular language.

d. $L_4 = \{w \# w^R \mid |w| = |w^R|\}$

when $\{0, 1\}^*$

Suppose L_4 is regular. p is pumping length.

$$L = \{0^a 1^b \mid a \leq b\}$$

$$L = 0^p 1^0 \cup 0^{p+1} 1^1 \cup \dots$$

$$|L| = 2 + 2p + p!$$

If $p < 2 \dots$ then $p \leq \max(a, b)$

all the decompose of L into xyz

$$x = 0^a$$

$$y = 0^b \cdot b \geq 1$$

$$z = 0^{p-a-b} 1^{p+1} 1$$

$$xy^iz \in L$$

$$xy^iz = 0^a 0^{ib} 0^{p-a-b} 1^{p+1} 1$$

$$= 0^{p+ib-b} 0^{p+1} 1$$

$$P + (i-1)B \neq P + P!$$

$$\Rightarrow i \neq \frac{P!}{B} + 1 \quad \left[\frac{P!}{B} \text{ is integer} \right]$$

Here beta is between 1 and P and

it divides P factorial is one time factor. also

or it is integer or not. it is integer

then it is not equal to this.

$$so \quad i = \frac{P!}{B} + 1$$

The string is both side equal

~~no~~

$$x \neq 5 \neq x$$

$$x \neq 5 \neq x$$

$$x \neq 5 \neq x$$