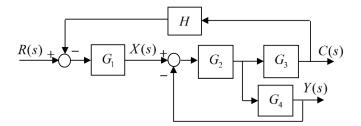
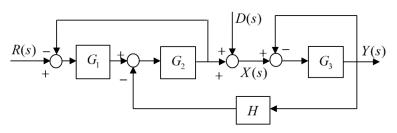


Course: CSE461 (Introduction to Robotics)

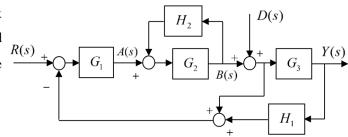
1. The closed-loop system shown in the block diagram has *one input* signal (R(s)) and *two output* signals (C(s) and Y(s)). Find the transfer functions $\frac{Y}{X}(s)$, $\frac{Y}{R}(s)$, and $\frac{C}{R}(s)$.



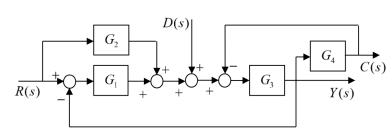
2. The closed-loop system shown in the block diagram has two input signals (R(s) and D(s)) and one output signal (Y(s)). Find the transfer functions $\frac{Y}{X}(s)$, $\frac{Y}{R}(s)$, and $\frac{Y}{D}(s)$.



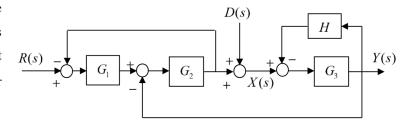
3. The closed-loop system shown in the block diagram has two input signals (R(s) and D(s)) and one output signal (Y(s)). Find the transfer functions $\frac{B}{A}(s)$, $\frac{Y}{R}(s)$, and $\frac{Y}{D}(s)$.



4. The closed-loop system shown in the block diagram has *one input* signal (R(s)) and *two output* signals (C(s)) and Y(s). Find the transfer functions $\frac{Y}{D}(s)$, $\frac{C}{D}(s)$, and $\frac{Y}{R}(s)$.



5. The closed-loop system shown in the block diagram has two input signals (R(s)) and (R(s)) and one output signal (Y(s)). Find the transfer functions $\frac{Y}{Y}(s)$, $\frac{Y}{R}(s)$, and $\frac{Y}{D}(s)$.



Answers

1.

$$\frac{Y}{X}(s) = \frac{G_2G_4}{1 + G_2G_4} \quad \frac{Y}{R}(s) = \frac{G_1G_2G_4}{1 + G_2G_4 + G_1G_2G_3H} \quad \frac{C}{R}(s) = \frac{G_1G_2G_3}{1 + G_2G_4 + G_1G_2G_3H}$$

2.

$$\frac{Y}{X}(s) = \frac{G_3}{1+G_3} \left[\frac{Y}{R}(s) = \frac{G_1G_2G_3}{(1+G_1G_2)(1+G_3)+G_2G_3H} \right] \left[\frac{Y}{D}(s) = \frac{G_3(1+G_1G_2)}{(1+G_1G_2)(1+G_3)+G_2G_3H} \right]$$

3.

$$\frac{B}{A}(s) = \frac{G_2}{1 + G_2 H_2} \left[\frac{Y}{R}(s) = \frac{G_1 G_2 G_3}{1 + G_2 H_2 + G_1 G_2 (1 + G_3 H_1)} \right] \left[\frac{Y}{D}(s) = \frac{G_3 (1 + G_2 H_2)}{1 + G_2 H_2 + G_1 G_2 (1 + G_3 H_1)} \right]$$

4

$$\frac{Y}{D}(s) = \frac{G_3}{1 + G_3(G_1 + G_4)} \left[\frac{C}{D}(s) = \frac{G_3G_4}{1 + G_3(G_1 + G_4)} \right] \left[\frac{Y}{R}(s) = \frac{G_3(G_1 + G_2)}{1 + G_3(G_1 + G_4)} \right]$$

5.

$$\boxed{\frac{Y}{X}(s) = \frac{G_3}{1 + G_3 H}} \boxed{\frac{Y}{R}(s) = \frac{G_1 G_2 G_3}{1 + G_1 G_2 + G_2 G_3 + G_3 H + G_1 G_2 G_3 H}} \boxed{\frac{Y}{D}(s) = \frac{G_3 (1 + G_1 G_2)}{1 + G_1 G_2 + G_2 G_3 + G_3 H + G_1 G_2 G_3 H}}$$