



# Programación Estadística con Python

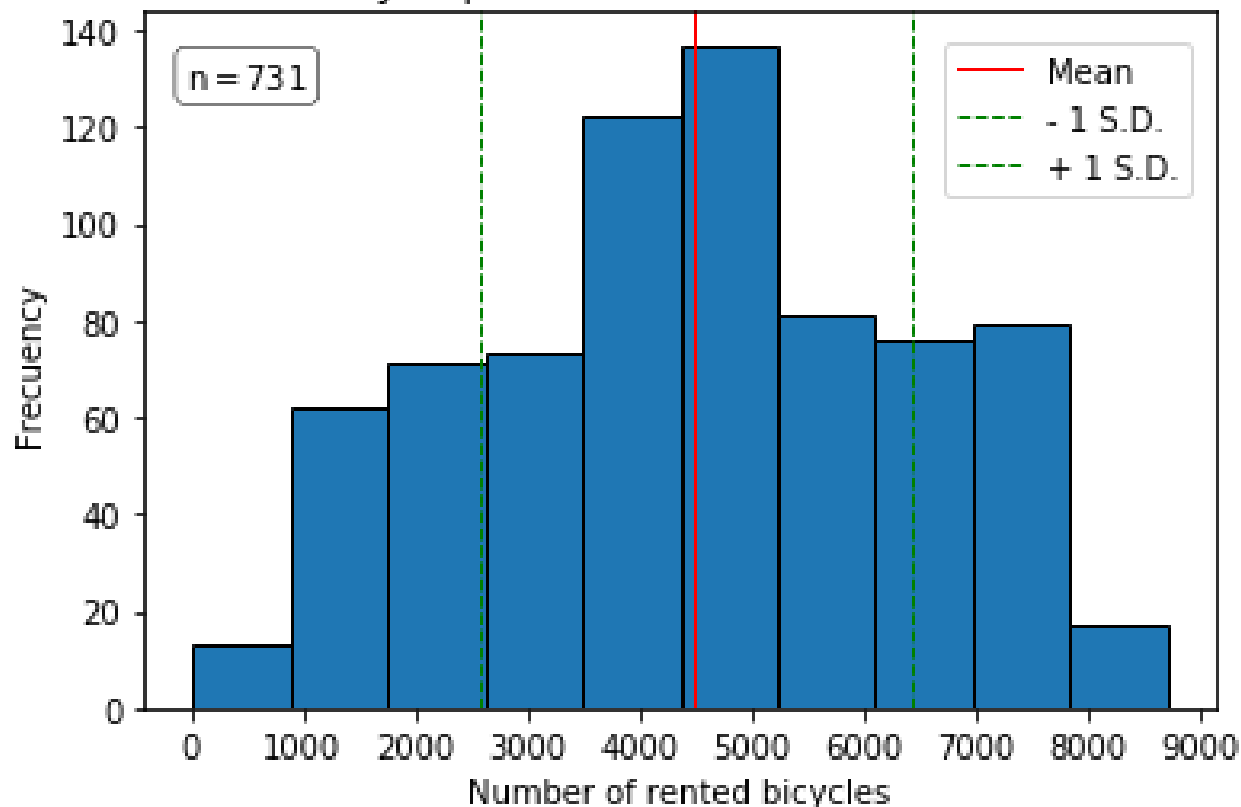
**Sesions 7-8**  
**Mean comparisons**

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**MASTER EN DATA ANALYTICS PARA LA EMPRESA**

# Describing quantitative variables

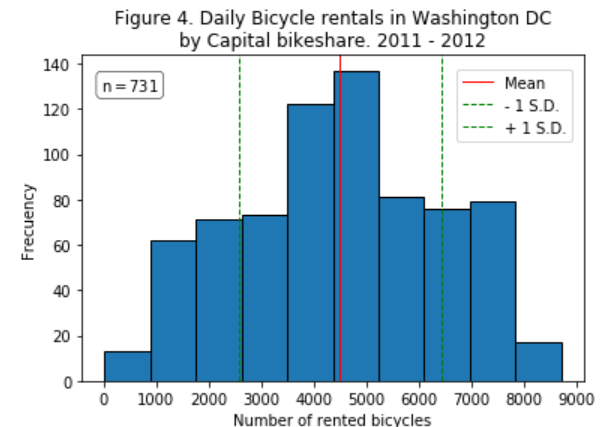
Figure 4. Daily Bicycle rentals in Washington DC  
by Capital bikeshare. 2011 - 2012



# Research Question

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Why some days are rent *more* bikes than other days in Washington D.C.?



- $H_0$ .:  $\mu$  rentals in **working days** =  $\mu$  rentals in **holidays**
- $H_1$ .:  $\mu$  rentals in **working days**  $\neq$   $\mu$  rentals in **holidays**

# Mean comparison (2 groups)

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- $H_0$ .:  $\mu$  rentals in **working days** =  $\mu$  rentals in **holidays**
- $H_1$ .:  $\mu$  rentals in **working days**  $\neq$   $\mu$  rentals in **holidays**
  
- **Numeric Procedure**       $\Rightarrow$  **t test** for independent samples
  
- **Graphic procedure**       $\Rightarrow$  **confidence interval** plot

# Mean comparison (2 groups)

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1. **Describe the two variables involved in the hypothesis**
2. **Perform the numeric test: t.test**
3. **Perform the graphic test: plot of the means**
4. **When posible:** combine both numeric and graphic in same plot

# Mean comparison (2 groups)

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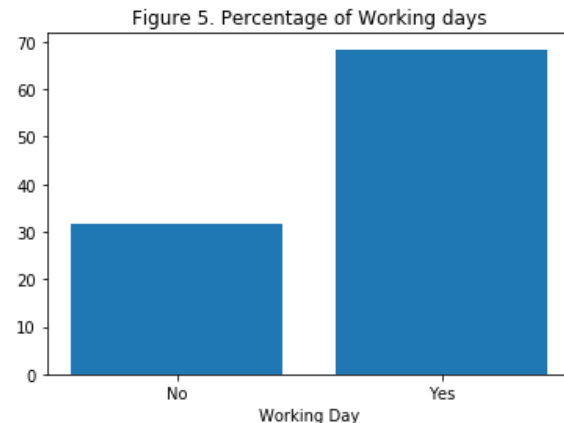
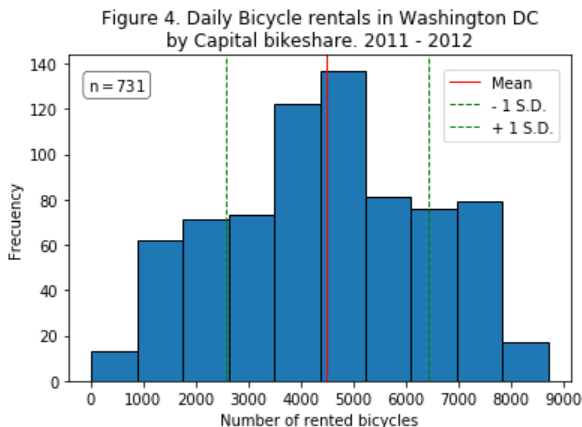
## 1. Describe the two variables involved in hypothesis

### Rentals

```
wbr.cnt.describe()  
plt.hist(wbr.cnt)
```

### Working days

```
mytable = pd.crosstab(index=wbr["wd_cat"],  
columns="count")  
n=mytable.sum()  
  
mytable2 = (mytable/n)*100  
  
plt.bar(mytable2.index, mytable2['count'])
```



# Mean comparison (2 groups)

## 2. Perform the numeric test: t.test

```
#Descriptive comparison:
wbr.groupby('wd_cat').cnt.mean()

#Statistical comparison:
#Extract the two sub samples and store them in two objects
cnt_wd=wbr.loc[wbr.wd_cat=='Yes', "cnt"]
cnt_nwd=wbr.loc[wbr.wd_cat=='No', "cnt"]

#Perform a t test for mean comparison
#import scipy.stats as stats
stats.ttest_ind(cnt_wd, cnt_nwd, equal_var = False)
```

Output:

```
wd_cat
No      4330.168831
Yes     4584.820000
```

```
Ttest_indResult(statistic= 1.60137, pvalue = 0.1105)
```

# Mean comparison (2 groups)

## 3. Perform the mean comparison graphic test (I)

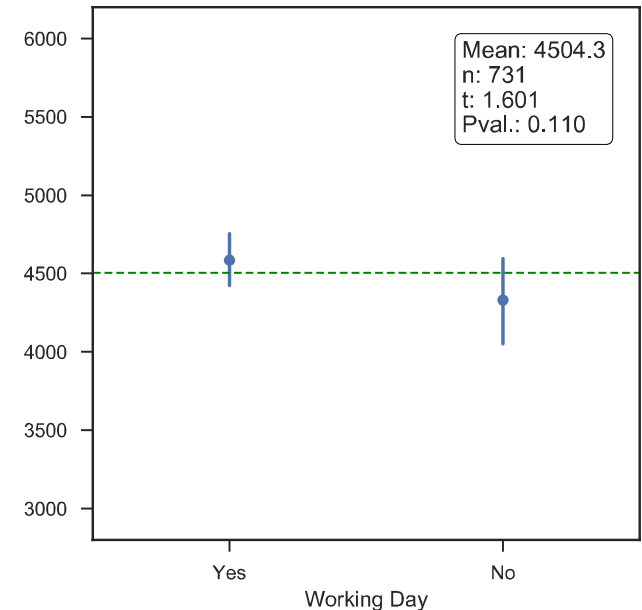
### 3.1. Define parameters & plot

```
#CI meanplot
import seaborn as sns
import matplotlib.pyplot as plt

plt.figure(figsize=(5,5))
ax = sns.pointplot(x="wd_cat", y="cnt",
                   data=wbr,ci=95, join=0)
plt.yticks(np.arange(3000, 7000, step=500))
plt.ylim(2800,6200)
plt.axhline(y=wbr.cnt.mean(),
            linewidth=1,
            linestyle= 'dashed',
            color="green")
props = dict(boxstyle='round',
             facecolor='white', lw=0.5)
plt.text(0.85,5400,'Mean:4504.3'\n'n:731' '\n' 't:1.601' '\n' 'Pval.:0.110',      bbox=props)
plt.xlabel('Working Day')
plt.title('Figure 6. Average rentals by Working Day.''\n')
```



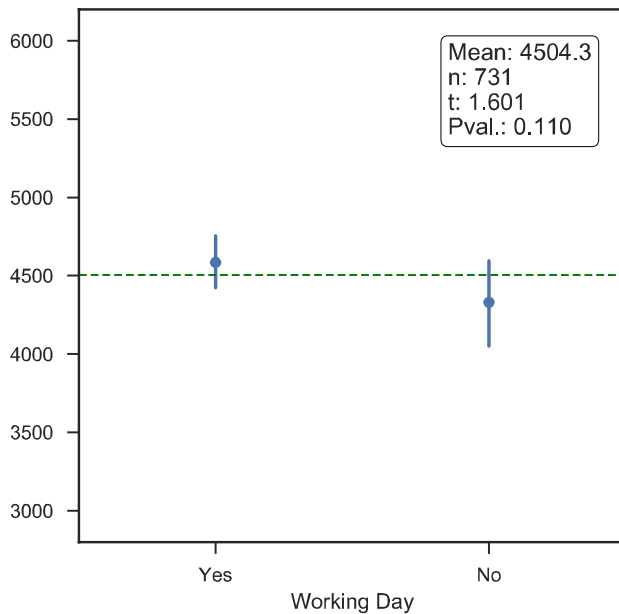
Figure 6. Average rentals by Working Day.





# Mean comparison (2 groups)

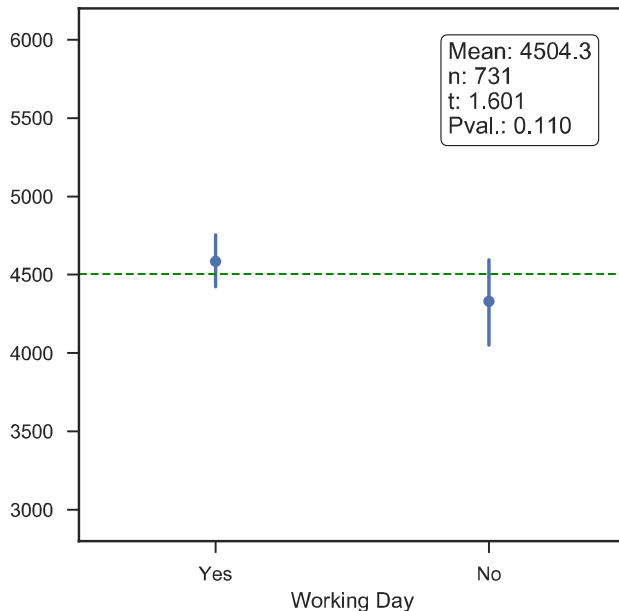
Figure 6. Average rentals by Working Day.



# Mean comparison (2 groups)

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Figure 6. Average rentals by Working Day.



$H_0: \mu \text{ rentals in work days} = \mu \text{ rentals in holidays}$



$H_1: \mu \text{ rentals in work days} \neq \mu \text{ rentals in holidays}$



CONCLUSION:

As  $P. Val > 0.05$ , we do NOT REJECT  $H_0$ .

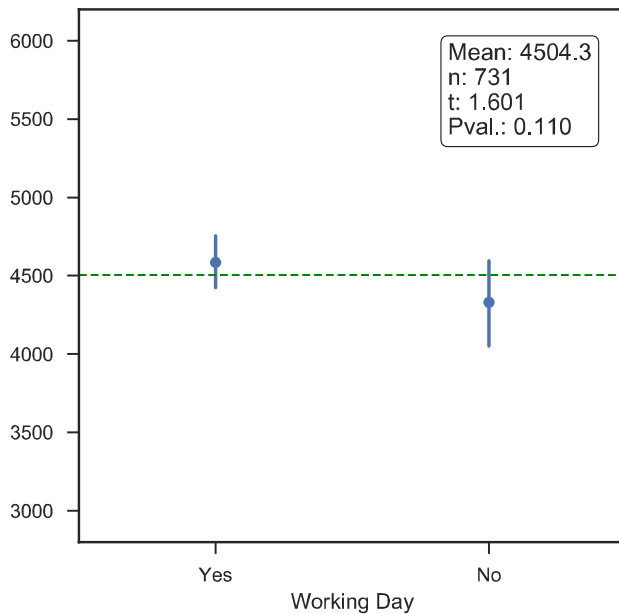
In other words:

**Average rentals do not significantly differ in Working days and Non working days.**

# Mean comparison (2 groups)

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Figure 6. Average rentals by Working Day.



CONCLUSION:  
As P. Val > 0.05

**Average rentals do not significantly differ in Working days and Non working days.**

# Mean comparison (2 gr.) Example #2

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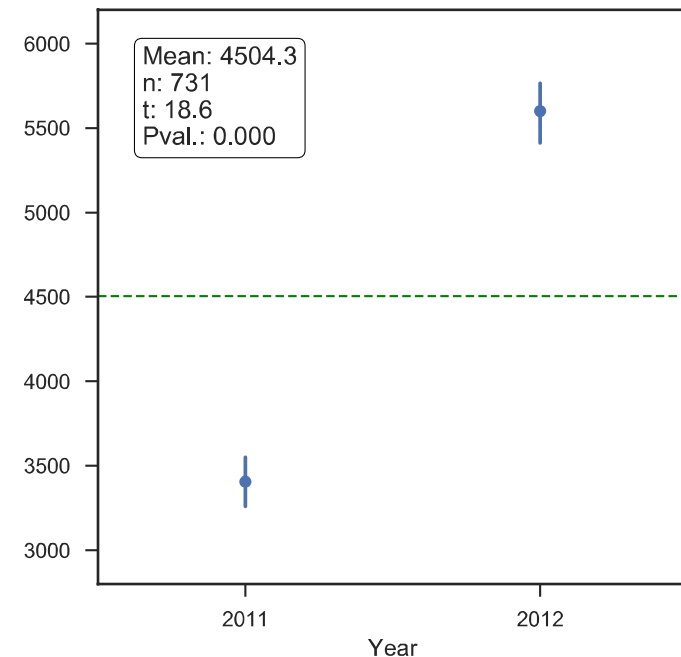
- ✗  $H_0: \mu \text{ rentals in 2011} = \mu \text{ rentals in 2012}$
- ✓  $H_1: \mu \text{ rentals in 2011} \neq \mu \text{ rentals in 2012}$

```
#Plotmeans
plt.figure(figsize=(5,5))
ax=sns.pointplot(x="yr",y="cnt",data=wbr,ci=95,join=0)
ax.set_ylabel('')
plt.yticks(np.arange(3000, 7000, step=500))
plt.ylim(2800,6200)
plt.axhline(y=wbr.cnt.mean(),
            linewidth=1,
            linestyle= 'dashed',
            color="green")

props = dict(boxstyle='round', facecolor='white', lw=0.5)
plt.xticks((0,1), ("2011", "2012"))
plt.xlabel('Year')
plt.title('Figure 7. Average rentals by Year.''\n')
```

```
plt.text(-0.35,5400,'Mean:4504.3''\n''n:731' '\n' 't:18.6' '\n' 'Pval.: 0.000',bbox=props)
```

Figure 7. Average rentals by Year.



# A Panel of results:

Figure 6. Average rentals by Working Day.

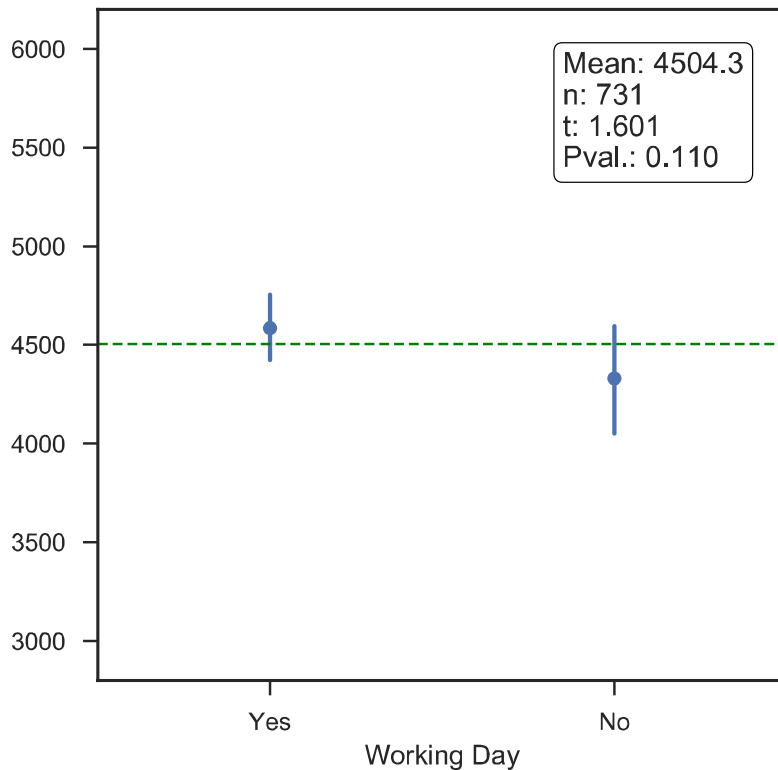
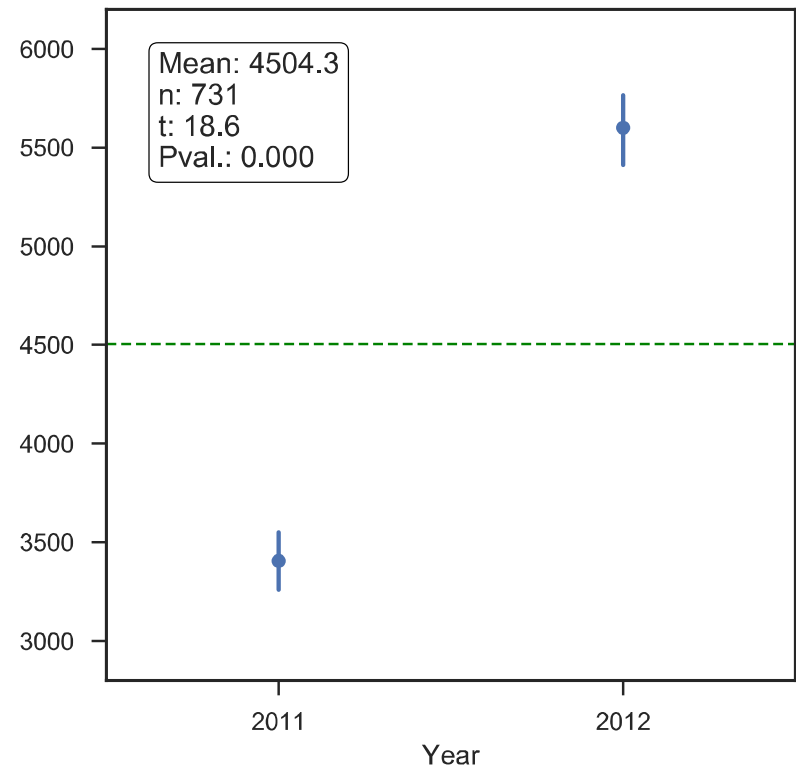


Figure 7. Average rentals by Year.



# A Panel of results:

Figure 6. Average rentals by Working Day.

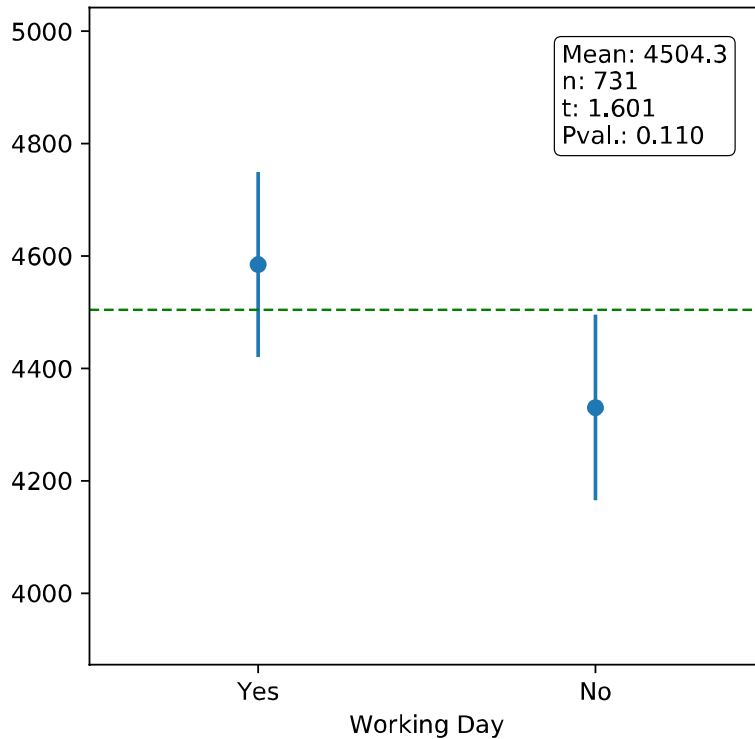
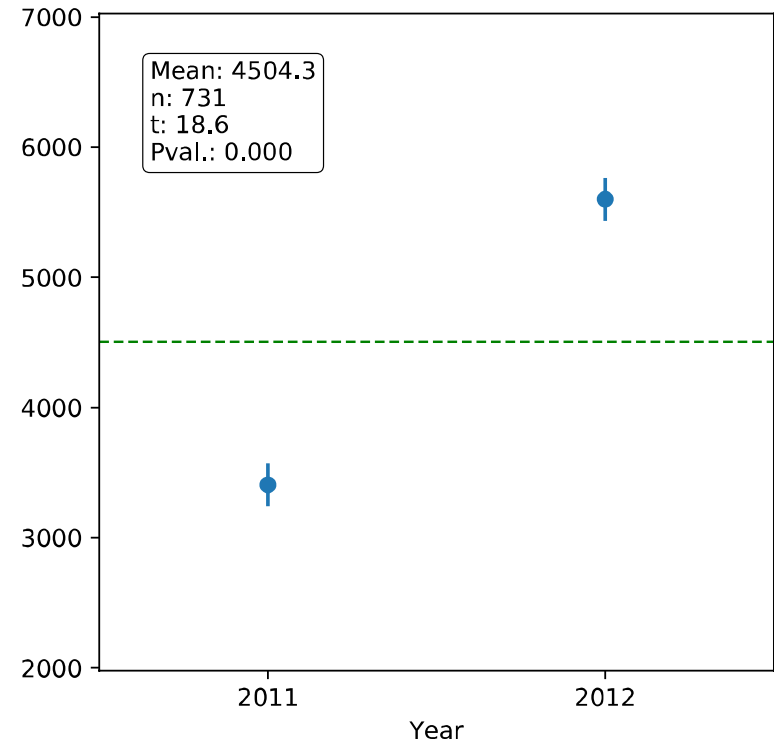


Figure 7. Average rentals by Year.

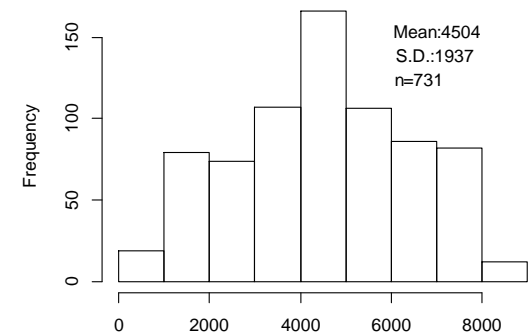


# Research Question

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## Why some days are rent *more* bikes than other days in Washington D.C.?

Daily Bicycle rentals in Washinton DC. 2011-2012



- $H_0$ .:  $\mu$  rentals **sunny** =  $\mu$  rentals **cloudy** =  $\mu$  rentals **stormy**.
- $H_1$ .:  $\mu$  rentals differ in **at least** 2 of the 3 groups compared.

# Mean comparison ( **> 2 groups** )

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- $H_0$ .:  $\mu$  rentals **sunny** =  $\mu$  rentals **cloudy** =  $\mu$  rentals **stormy**.
- $H_1$ .:  $\mu$  rentals differ in **at least** 2 of the 3 groups compared

▣ **Numeric Procedure**       $\Rightarrow$  **One-Way ANOVA**

▣ **Graphic procedure**       $\Rightarrow$  **Confidence interval plot**



# Mean comparison ( $> 2$ groups)

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1. **Describe the two variables involved in the hypothesis**
2. **Perform the numeric test: One-Way ANOVA**
3. **Perform the graphic test: plot of the means**
4. **When possible: combine both numeric and graphic in same plot.**

# Mean comparison ( > 2 groups) EDEM Centro Universitario

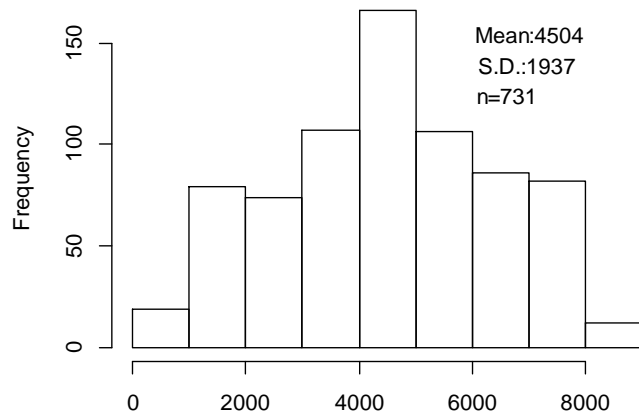
18

1. **Describe** the two variables involved in hypothesis

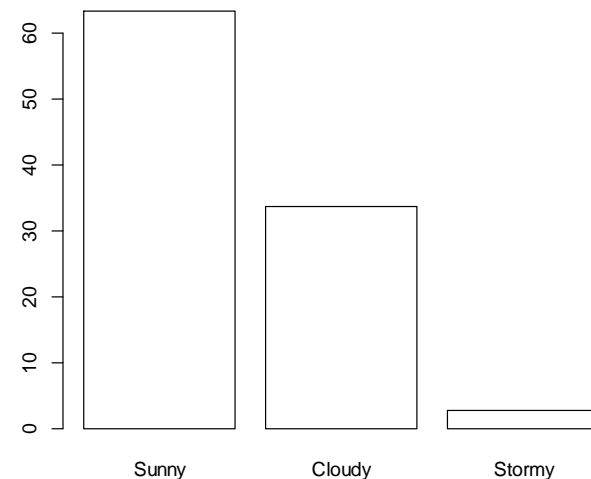
Rentals

Weather condition

Daily Bicycle rentals in Washinton DC. 2011-2012



Percentage of weather condition in Washington



# Mean comparison ( $> 2$ groups)

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## 2. Perform the numeric test: One-Way ANOVA

```
##Descriptive comparison
wbr.groupby('ws_cat').cnt.mean()

#Statistical comparison
cnt_sunny=wbr.loc[wbr.ws_cat=='Sunny', "cnt"]
cnt_cloudy=wbr.loc[wbr.ws_cat=='Cloudy', "cnt"]
cnt_rainy=wbr.loc[wbr.ws_cat=='Rainy', "cnt"]

stats.f_oneway(cnt_sunny, cnt_cloudy, cnt_rainy )
```

OUTPUT:

Sunny	4876.786177
Cloudy	4035.862348
Rainy	1803.285714

```
F_onewayResult(statistic=40.0660, pvalue=3.10631e-17)
```

Interpretation.

As P.Value  $< 0.05$ : **REJECT** the  $H_0$  about equality of the means in all groups.  
In other words: **at least two groups differ** in average bicycle rentals

# Mean comparison ( $> 2$ groups)

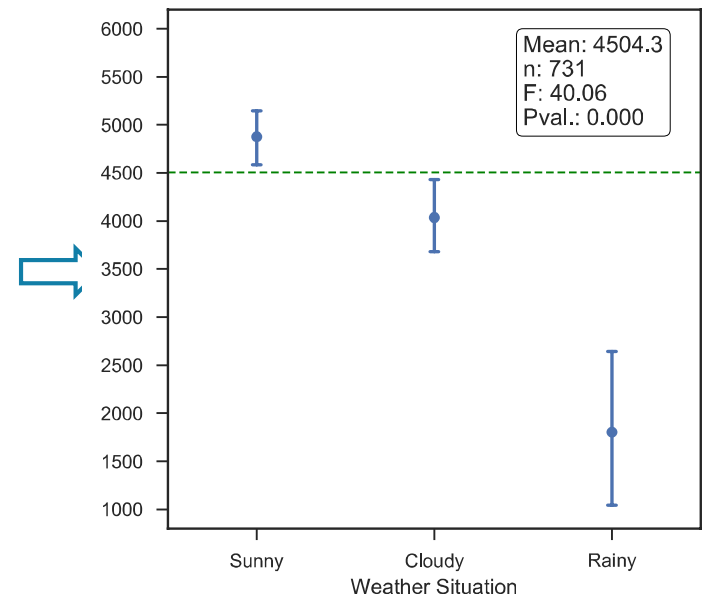
20

## 3. Perform the graphic test: plot of the means

```
#Graphic comparison: confidence intervals for the means
plt.figure(figsize=(5,5))
ax = sns.pointplot(x="ws_cat", y="cnt", data=wbr, capsize=0.05,
ci=99.9, join=0)
ax.set_ylabel('')
plt.yticks(np.arange(1000, 7000, step=500))
plt.ylim(800,6200)
plt.axhline(y=wbr.cnt.mean(),
            linewidth=1,
            linestyle= 'dashed',
            color="green")

props = dict(boxstyle='round', facecolor='white', lw=0.5)
plt.text(1.5, 5000, 'Mean: 4504.3'\n'n: 731' '\n' 'F: 40.06'
'\n' 'Pval.: 0.000',      bbox=props)
plt.xlabel('Weather Situation')
plt.title('Figure 8. Average rentals by Weather Situation.''\n')
```

Figure 8. Average rentals by Weather Situation.

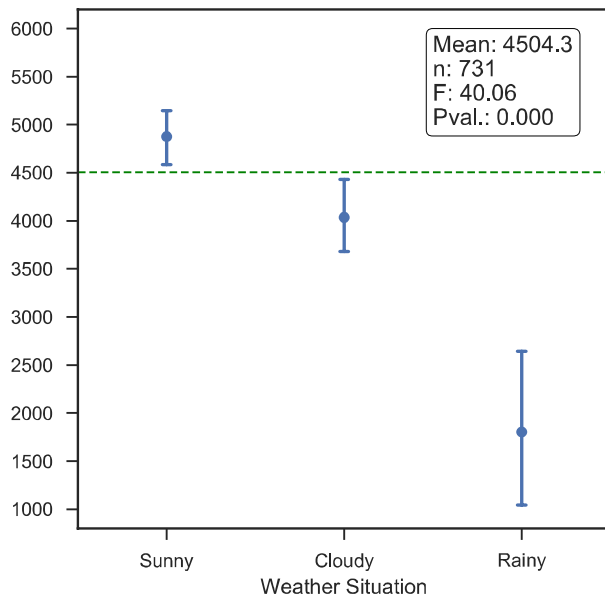


# Mean comparison ( > 2 groups)

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## 4. Combine graphic & numeric tests

Figure 8. Average rentals by Weather Situation.



- ✗  $H_0: \mu \text{ rentals sunny} = \mu \text{ rentals cloudy} = \mu \text{ rentals stormy}.$
- ✓  $H_1: \mu \text{ rentals differ in at least 2 of the 3 groups compared}$

### CONCLUSION:

As P. Value < 0.05\*, we do REJECT  $H_0$ .

In other words:

**Different weather conditions** are significantly associated to **different average in rentals**.

\* Note: In this specific case, as p.value is indeed < 0.01, we reject  $H_0$  with a confidence level larger than 99 percent.

# Mean Comparison Summing UP

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- General Remainder:
  - ▣ Always **describe/explore your data** (numerically + graphically) prior to perform any statistical analysis.
- Main Graphic Procedure:
  - ▣ Confidence interval plot
- Main Numeric Procedures:
  - ▣ 2 Groups : t test
  - ▣ >2 Groups: One-way ANOVA

**Questions?**

**Thank you !**

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