

**Doc**

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# Preface

This is a Quarto book.

To learn more about Quarto books visit <https://quarto.org/docs/books>.

```
using QuartoDocumenter, AstrodynamicalModels
QuartoDocumenter.autodoc(AstrodynamicalModels)
```

Precompiling QuartoDocumenter

QuartoDocumenter

1 dependency successfully precompiled in 1 seconds. 27 already precompiled.

Provides astrodynamical models as `AstrodynamicalModels.ODESystems`. Check out the `ModelingToolkit` docs to learn how to use these systems for orbit propagation with `DifferentialEquations`, or see `GeneralAstrodynamics` for some convenient orbit propagation wrappers.

## Extended help

### 0.0.0.0.1 \* License

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#### **0.0.0.0.2 \* Exports**

- AttitudeFunction
- AttitudeParameters
- AttitudeState
- AttitudeSystem
- CR3BFunction
- CR3BOrbit
- CR3BParameters
- CR3BState
- CR3BSystem
- CartesianOrbit
- CartesianState
- KeplerianOrbit
- KeplerianParameters
- KeplerianState
- NBFunction
- NBSystem
- Orbit
- OrbitalElements
- PlanarEntryFunction
- PlanarEntryParameters
- PlanarEntryState
- PlanarEntrySystem
- R2BFunction
- R2BOrbit
- R2BParameters
- R2BState
- R2BSystem
- dynamics
- parameters
- state
- system

#### **0.0.0.0.3 \* Imports**

- Base
- Core
- DocStringExtensions

- LinearAlgebra
- Memoize
- ModelingToolkit
- SciMLBase
- StaticArrays
- Symbolics

```
AttitudeFunction(; stm, name, kwargs...)
```

Returns an `ODEFunction` for spacecraft attitude dynamics.

### Extended Help

#### 0.0.0.0.0.1 \* Usage

The `stm` and `name` keyword arguments are passed to `Attitude`. All other keyword arguments are passed directly to `SciMLBase.ODEFunction`.

```
f = AttitudeFunction()
let u = randn(7), p = randn(15), t = NaN # time invariant
    f(u, p, t)
end
```

```
struct AttitudeParameters{F} <: AstrodynamicalModels.AstrodynamicalParameters{F, 15}
```

A parameter vector for attitude dynamics.

```
mutable struct AttitudeState{F} <: AstrodynamicalModels.AstrodynamicalState{F, 7}
```

A mutable state vector for attitude dynamics.



```
AttitudeSystem(; stm, name, defaults, kwargs...)
```

A `ModelingToolkit.ODESystem` for atmospheric entry. Currently, only exponential atmosphere models are provided! The output model is cached with `Memoize.jl`. Planet-specific parameters default to Earth values.

The order of the states follows:  $[q, \dot{q}, \ddot{q}, \ddot{\dot{q}}, \ddot{\ddot{q}}, \ddot{\ddot{\dot{q}}}]$ .

The order of the parameters follows:  $[\mathbf{J}, \mathbf{L}, \mathbf{f}]$

### Extended Help

This model describes how an object moves through an exponential atmosphere, above a spherical planet.

#### 0.0.0.0.1 \* States

1.  $q$ : scalar-last attitude quaternion
2.  $\dot{q}$ : body rates (radians per second)

#### 0.0.0.0.2 \* Parameters

1.  $\mathbf{J}$ : inertial matrix
2.  $\mathbf{L}$ : lever arm where input torque is applied
3.  $\mathbf{f}$ : torques on the vehicle body (Newton-meters)

#### 0.0.0.0.2.1 \* Usage

```
model = Attitude()
```

```
CR3BFunction(; stm, name, kwargs...)
```

Returns an `ODEFunction` for CR3B dynamics.

The order of the states follows: [ ].

The order of the parameters follows: [ ].

### Extended Help

#### 0.0.0.0.1 \* Usage

The `stm`, and `name` keyword arguments are passed to `CR3B`. All other keyword arguments are passed directly to `SciMLBase.ODEFunction`.

```
f = CR3BFunction(; stm=false, jac=true)
let u = randn(6), p = randn(1), t = 0
    f(u, p, t)
end
```

```
struct Orbit{var"#s25"<:CartesianState, var"#s24"<:CR3BParameters} <: AstrodynamicalModels
```

An Orbit which exists within CR3BP dynamics.

```
struct CR3BParameters{F} <: AstrodynamicalModels.AstrodynamicalParameters{F, 1}
```

A parameter vector for CR3BP dynamics.

```
mutable struct CartesianState{F} <: AstrodynamicalModels.AstrodynamicalState{F, 6}
```

CartesianState

```
CR3BSystem(; stm, name, defaults, kwargs...)
```

A `ModelingToolkit.ODESystem` for the Circular Restricted Three-body Problem.

The order of the states follows:  $[x, y, z, \dot{x}, \dot{y}, \dot{z}]$ .

The order of the parameters follows:  $[\ ]$ .

### Extended Help

The Circular Restricted Three-body Problem is a simplified dynamical model describing one small body (spacecraft, etc.) and two celestial bodies moving in a circle about their common center of mass. This may seem like an arbitrary simplification, but this assumption holds reasonably well for the Earth-Moon, Sun-Earth, and many other systems in our solar system.

#### 0.0.0.0.1 \* Usage

```
model = CR3BSystem(; stm=true)
```

```
struct Orbit{var"#s25"<:CartesianState, P<:(AbstractVector)} <: AstrodynamicalModels.Astro
```

An `Orbit` which exists within R2BP dynamics.

```
mutable struct CartesianState{F} <: AstrodynamicalModels.AstrodynamicalState{F, 6}
```

A mutable vector, with labels, for 6DOF Cartesian states.



```
struct Orbit{var"#s25"<:OrbitalElements, var"#s24"<:KeplerianParameters} <: AstrodynamicalM
```

An Orbit which exists within Keplerian dynamics.

```
struct KeplerianParameters{F} <: AstrodynamicalModels.AstrodynamicalParameters{F, 1}
```

A parameter vector for Keplerian dynamics.

```
mutable struct OrbitalElements{F} <: AstrodynamicalModels.AstrodynamicalState{F, 6}
```

OrbitalElements

```
NBFunction(N; stm, name, kwargs...)
```

Returns an `ODEFunction` for NBP dynamics. The order of states and parameters in the `ODEFunction` arguments are equivalent to the order of states and parameters for the system produced with `NBP(N)`. As a general rule, the order of the states follows:  $[x, y, z, \dots, \dot{x}, \dot{y}, \dot{z}, \dots, \ddot{x}, \ddot{y}, \ddot{z}]$ .

#### Note

Unlike `R2BP` and `CR3BP`, `jac` is set to `false` by default. The number of states for NBP systems can be very large for relatively small numbers of bodies ( $N$ ). Enabling `jac=true` by default would cause unnecessarily long waiting times for this (**memoize?**) function to return for  $N \geq 3$  or so. If  $N=2$  and `stm=true`, setting `jac=true` could still result in several minutes of calculations, depending on the computer you're using.

#### Warning

Be careful about specifying `stm=true` for systems with  $N \geq 3$ ! If state transition matrix dynamics are enabled, you can calculate the total number of system states with  $N*6 + (N*6)^2$ . Note that this increases exponentially as  $N$  grows! For  $N == 6$ , unless you're using parallelization, your computer may run for several hours.

## Extended Help

### 0.0.0.0.1 \* Usage

The `stm`, and `name` keyword arguments are passed to `NBP`. All other keyword arguments are passed directly to `SciMLBase.ODEFunction`.

```
f = NBFunction(3; stm=false, name=:NBP, jac=false, sparse=false)
let u = randn(3*6), p = randn(1 + 3), t = 0
    f(u, p, t)
end
```

```
NBSystem(N; stm, name, defaults, kwargs...)
```

A `ModelingToolkit.ODESystem` for the Newtonian N-body Problem.

The order of the states follows:  $[x, y, z, \dots, x, y, z, \dot{x}, \dot{y}, \dot{z}, \dots, \dot{x}, \dot{y}, \dot{z}]$ .

The order of the parameters follows:  $[G, m, m, \dots, m]$ .

#### Warning

Be careful about specifying `stm=true` for systems with  $N \geq 3$ ! If state transition matrix dynamics are enabled, you can calculate the total number of system states with  $N*6 + (N*6)^2$ . Note that this increases exponentially as  $N$  grows! For  $N == 6$ , unless you're using parallelization, your computer may run for several hours.

### Extended Help

The N-body problem is a model which describes how  $N$  bodies will move with respect to a common origin. This problem typically involves many bodies which act due to one force: electromagnetism, gravity, etc. This model applies most closely to many celestial bodies moving due to gravity. That's about right for a model in a package called `AstrodynamicalModels`!

#### 0.0.0.0.1 \* Usage

```
# One model for ALL the planets in our solar system
model = NBSystem(9)
```

```
struct Orbit{U<:(AbstractVector), P<:(AbstractVector)} <: AstrodynamicalModels.Astrodynamic
```

A full representation of an orbit, including a numerical state, and the parameters of the system.

```
mutable struct OrbitalElements{F} <: AstrodynamicalModels.AstrodynamicalState{F, 6}
```

A mutable vector, with labels, for 6DOF Keplerian states.

```
PlanarEntryFunction(; name, kwargs...)
```

Returns an ODEFunction for Planar Entry dynamics. Results are cached with Memoize.jl.

The order of the states follows: [ , v, r, ].

The order of the parameters follows: [R, P, H, m, A, C, ]

### Extended Help

#### 0.0.0.0.1 \* Usage

The name keyword argument is passed to PlanarEntry. All other keyword arguments are passed directly to SciMLBase.ODEFunction.

```
f = PlanarEntryFunction()
let u = randn(4), p = randn(7), t = NaN # time invariant
    f(u, p, t)
end
```



```
struct PlanarEntryParameters{F} <: AstrodynamicalModels.AstrodynamicalParameters{F, 7}
```

A parameter vector for planar entry dynamics.

```
mutable struct PlanarEntryState{F} <: AstrodynamicalModels.AstrodynamicalState{F, 4}
```

A state vector for planar entry dynamics.

```
PlanarEntrySystem(; name, defaults, kwargs...)
```

A `ModelingToolkit.ODESystem` for atmospheric entry. Currently, only exponential atmosphere models are provided! The output model is cached with `Memoize.jl`. Planet-specific parameters default to Earth values.

The order of the states follows: [ , `v`, `r`, ].

The order of the parameters follows: [R, P, H, m, A, C, ]

### Extended Help

This model describes how an object moves through an exponential atmosphere, above a spherical planet.

**0.0.0.0.1** \* Usage

```
model = PlanarEntrySystem()
```

```
R2BFunction(; stm, name, kwargs...)
```

Returns an `ODEFunction` for R2B dynamics.

The order of the states follows:  $[x, y, z, \dot{x}, \dot{y}, \dot{z}]$ .

The order of the parameters follows:  $[\ ]$ .

### Extended Help

#### 0.0.0.0.0.1 \* Usage

The `stm`, and `name` keyword arguments are passed to R2B. All other keyword arguments are passed directly to `SciMLBase.ODEFunction`.

```
f = R2BFunction(; stm=false, name=:R2B, jac=true)
let u = randn(6), p = randn(1), t = 0
    f(u, p, t)
end
```

```
struct Orbit{var"#s25"<:CartesianState, var"#s24"<:R2BParameters} <: AstrodynamicalModels.A
```

An Orbit which exists within R2BP dynamics.

```
struct R2BParameters{F} <: AstrodynamicalModels.AstrodynamicalParameters{F, 1}
```

A parameter vector for R2BP dynamics.

```
mutable struct CartesianState{F} <: AstrodynamicalModels.AstrodynamicalState{F, 6}
```

CartesianState

```
R2BSystem(; stm, name, defaults, kwargs...)
```

A `ModelingToolkit.ODESystem` for the Restricted Two-body Problem.

The order of the states follows:  $[x, y, z, \dot{x}, \dot{y}, \dot{z}]$ .

The order of the parameters follows:  $[\ ]$ .

### Extended Help

The Restricted Two-body Problem is a simplified dynamical model describing one small body (spacecraft, etc.) and one celestial body. The gravity of the celestial body exhibits a force on the small body. This model is commonly used as a simplification to describe our solar systems' planets orbiting our sun, or a spacecraft orbiting Earth.

#### 0.0.0.0.1 \* Usage

```
model = R2BSystem()
```



```
dynamics(orbit, args; kwargs...)
```

Return the underlying dynamics of the system in the form of a `ModelingToolkit.ODEFunction`.

```
parameters(orbit)
```

Return the parameter vector for an `Orbit`.

```
state(orbit)
```

Return the state vector for an `Orbit`.

```
system(orbit, args; kwargs...)
```

Return the underlying dynamics of the system in the form of a `ModelingToolkit.ODESystem`.

# 1 Introduction

This is a book created from markdown and executable code.

See Knuth (1984) for additional discussion of literate programming.

## 2 Summary

In summary, this book has no content whatsoever.

## References

Knuth, Donald E. 1984. “Literate Programming.” *Comput. J.* 27 (2): 97–111. <https://doi.org/10.1093/comjnl/27.2.97>.