Lista 3 - Calculo I

September 10, 2023

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.

$$\frac{d}{dx}(3x^3 - 2x^2 + x - 100)$$
$$9x^2 - 4x + 1$$

11.

$$\frac{d}{dx} \left(\frac{1-x}{x+1} \right)$$

$$\frac{(1-x)'(x+1) - (1-x)(x+1)'}{(x+1)^2}$$

$$\frac{1(x+1) - (1-x)(1)}{(x+1)^2}$$

$$\frac{(x+1) - (1-x)}{(x+1)^2}$$

$$\frac{x+1-1+x}{(x+1)^2}$$

$$\frac{2x}{(x+1)^2}$$

12.

$$f'(x) = \frac{d}{dx} (x^3 - 6x^2 + 9x - 1)$$

$$f'(x) = 3x^2 - 12x + 9$$

$$3x^2 - 12x + 9 = 0$$

$$x^2 - 4x + 3 = 0$$

$$(x_1, x_2) = (1, 3)$$

13.

$$L'(p) = \frac{d}{dx} \left(-p^3 + 7p^2 - 11p + 5 \right)$$

$$L'(p) = -3p^2 + 14p - 11$$

$$-3p^2 + 14p - 11 = 0$$

$$3p^2 - 14p + 11 = 0$$

$$(x_1, x_2) = \frac{14 \pm \sqrt{196 - 12 \times 11}}{6}$$

$$(x_1, x_2) = \frac{14 \pm \sqrt{196 - 132}}{6}$$

$$(x_1, x_2) = \frac{14 \pm \sqrt{64}}{6}$$

$$(x_1, x_2) = \frac{14 \pm 8}{6}$$

$$(x_1, x_2) = \left(\frac{22}{6}, \frac{6}{6}\right)$$

$$(x_1, x_2) = \left(\frac{11}{3}, 1\right)$$

14.

15.

$$f'(x) = \frac{d}{dx} \left(\frac{1}{x}\right)$$
$$f'(x) = \frac{0 \times x - 1 \times 1}{x^2}$$
$$f'(x) = -\frac{1}{x^2}$$
$$f'(1) = -\frac{1}{1^2} = -1$$