

(c) Dividing $\frac{6}{7}$ by what number gives $\frac{4}{3}$?

Express each answer in simplest form.

(f) $\frac{8}{2-\frac{2}{3}}$

(h) $\frac{\frac{2}{3}+\frac{5}{6}}{\frac{3}{4}-\frac{1}{2}}$

$$(d) \frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} + \frac{1}{4 \cdot 5} + \frac{1}{5 \cdot 6}.$$

4.7.6 What is the sum of the reciprocals of the positive divisors of 12? Express your answer as a fraction in simplest form.

4.7.9 Consider the sum $\frac{1}{4} + \frac{1}{4}$. We have $\frac{1}{4} + \frac{1}{4} = \frac{2}{4} = \frac{1}{2}$. Notice that the sum, when written in simplest form, has a smaller denominator than either of the two fractions we originally added. Find two fractions in simplest form with *different denominators* such that the sum of the fractions, written in simplest form, has a smaller denominator than either of the original two fractions.

4.8.2 Find the largest integer that is smaller than the sum $2\frac{1}{2} + 3\frac{1}{3} + 4\frac{1}{4} + 5\frac{1}{5} + 6\frac{1}{6}$.

4.8.3 Evaluate $(7a^2 - 11a + 3)(3a - 4)$ for $a = 1\frac{1}{3}$.

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4.8.6 Out of each hour of TV programming, $6\frac{1}{2}$ minutes are allocated to commercials. What fraction of each hour is dedicated to television programs? (Source: MATHCOUNTS)

4.9 Summary

$$(1) \quad 6\left(11\frac{2}{3} + 4\frac{1}{2}\right)$$

4.70 List every fraction that satisfies all four of the following conditions:

- (i) The fraction is in simplest form.
- (ii) The fraction is greater than $\frac{1}{6}$.
- (iii) The reciprocal of the fraction is an integer.
- (iv) The numerator of the fraction is positive.

4.72 Simplify the product $\frac{15}{42} \left(-\frac{63}{55}\right) \left(\frac{3}{2}\right)^{-2} \left(\frac{11}{2}\right)^2$.

4.74 Express as a fraction in simplest form: $\frac{9}{5} \left(3\frac{1}{3} \cdot \frac{1}{4} - \frac{10}{12} \cdot \frac{1}{8}\right)$.

4.77 The reciprocals of what three different positive integers have sum equal to 1?

4.80 Solve each of the following problems without writing anything.

(a) Which is greater, $\frac{23}{44}$ or $\frac{33}{64}$? **Hints:** 90

4.81 Evaluate in simplest form: $\frac{\left(\frac{6}{5}\right)^3 \left(\frac{25}{36}\right)^4}{\left(\frac{5}{6}\right)^4}$.

- 4.85 Find the number halfway between $-2\frac{5}{6}$ and $\frac{3}{5}$ on the number line. **Hints:** 158, 148
- 4.86 Two 600 ml pitchers contain vinegar. One pitcher is $\frac{1}{3}$ full and the other pitcher is $\frac{2}{5}$ full. Oil is added to fill each pitcher completely, and then both pitchers are poured into one large container. What fraction of the mixture in the large container is vinegar? (*Source: AMC 8*)
- 4.87★ I climb half the steps in a staircase. Next I climb one-third of the remaining steps. Then I climb one-eighth of the rest and stop to catch my breath. What is the least possible number of steps in the staircase? (*Source: MOEMS*)
- 4.89★ Loki, Moe, Nick, and Ott are good friends. Ott had no money, but the others did. Moe gave Ott one-fifth of his money, Loki gave Ott one-fourth of his money, and Nick gave Ott one-third of his money. Each gave Ott the same amount of money. What fractional part of the group's money does Ott now have? (*Source: AMC 8*) **Hints:** 58, 120