

Prime Patterns and Relations

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(Move this to end!!!!!!!) The code used in this paper will be submitted with the project and can also be found at: <https://github.com/cag51574/PrimePatterns>
Notice that you must have java 8 to run this project.

For this paper, I examine the relation of prime numbers to the primes that occur after it. I seek to identify interesting patterns in relations. This paper is based after the research of Dr. Kannan Soundararajan of Stanford University. He identified a pattern in the final digit of the prime numbers that I find rather counter intuitive. It is well known that primes are very random. If you examine the distribution of final digits of prime numbers in base 10, you find that the 1's, 3's, 7's and 9's are distributed relatively evenly regardless of the scale. The intuitive assumption would be that primes are random and that there is no influence from one prime to the next. Interestingly, Dr Soundararajan found this to not be the case at all. Infact, the final digit of a prime number seems to directly influence the final digit of a prime number that occurs next. In this paper, I check the results he finds and attempt to delve deeper into this phenomenon in an attempt to find additional interesting patterns.

First we check the results that Dr. Soundararajan finds relating to the final digits of prime distributions.

Next we look at further patters to see if there are some patterns the the primes that will always be more common than others. When analyzing the first 10 million primes in base 10, the max patterns at different depths are:

Depth	Number	Percent	Pattern
1	2500283	25.0028%	7
2	820368	8.2037%	9 → 1
3	256932	2.5693%	9 → 1 → 7
4	81324	0.8132%	3 → 9 → 1 → 7
5	24413	0.2441%	1 → 3 → 9 → 1 → 7
6	7872	0.0787%	9 → 1 → 3 → 9 → 1 → 7
7	2521	0.0252%	3 → 9 → 1 → 3 → 9 → 1 → 7
8	758	0.0076%	7 → 3 → 9 → 1 → 3 → 9 → 1 → 7

The 10 most common patterns at depth 5 over a million primes are

First 10 million

Depth	Number	Percent	Pattern
5	24413	0.2441%	$1 \rightarrow 3 \rightarrow 9 \rightarrow 1 \rightarrow 7$
5	24270	0.2427%	$9 \rightarrow 1 \rightarrow 3 \rightarrow 9 \rightarrow 1$
5	24183	0.2418%	$9 \rightarrow 1 \rightarrow 7 \rightarrow 9 \rightarrow 1$
5	24167	0.2417%	$3 \rightarrow 9 \rightarrow 1 \rightarrow 7 \rightarrow 9$
5	23069	0.2307%	$3 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9$
5	22961	0.2296%	$7 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9$
5	22904	0.2290%	$1 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 3$
5	22866	0.2287%	$1 \rightarrow 7 \rightarrow 3 \rightarrow 9 \rightarrow 1$
5	22821	0.2282%	$9 \rightarrow 1 \rightarrow 7 \rightarrow 3 \rightarrow 9$
5	22699	0.2270%	$1 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 7$

First 100 million

Depth	Number	Percent	Pattern
5	220752	0.2208%	$9 \rightarrow 1 \rightarrow 3 \rightarrow 9 \rightarrow 1$
5	220393	0.2204%	$1 \rightarrow 3 \rightarrow 9 \rightarrow 1 \rightarrow 7$
5	220347	0.2203%	$9 \rightarrow 1 \rightarrow 7 \rightarrow 9 \rightarrow 1$
5	218761	0.2188%	$3 \rightarrow 9 \rightarrow 1 \rightarrow 7 \rightarrow 9$
5	210841	0.2108%	$1 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 3$
5	210425	0.2104%	$7 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9$
5	209231	0.2092%	$1 \rightarrow 7 \rightarrow 3 \rightarrow 9 \rightarrow 1$
5	208463	0.2085%	$3 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9$
5	208337	0.2083%	$9 \rightarrow 1 \rightarrow 7 \rightarrow 3 \rightarrow 9$
5	207712	0.2077%	$1 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 7$

1 Billion primes with depth 7

Depth	Number	Percent	Pattern
7	187110	0.0187%	$7 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9 \rightarrow 1 \rightarrow 7$
7	185850	0.0186%	$3 \rightarrow 9 \rightarrow 1 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 3$
7	184150	0.0184%	$3 \rightarrow 9 \rightarrow 1 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 7$
7	184041	0.0184%	$3 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9 \rightarrow 1 \rightarrow 7$
7	182959	0.0183%	$7 \rightarrow 9 \rightarrow 1 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 3$
7	182869	0.0183%	$7 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9 \rightarrow 1 \rightarrow 3$
7	178559	0.0179%	$9 \rightarrow 1 \rightarrow 7 \rightarrow 3 \rightarrow 9 \rightarrow 1 \rightarrow 7$
7	178017	0.0178%	$3 \rightarrow 9 \rightarrow 1 \rightarrow 7 \rightarrow 3 \rightarrow 9 \rightarrow 1$
7	177663	0.0178%	$3 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9 \rightarrow 1$
7	177647	0.0178%	$1 \rightarrow 7 \rightarrow 9 \rightarrow 1 \rightarrow 3 \rightarrow 9 \rightarrow 1$
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