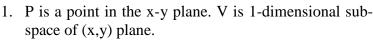
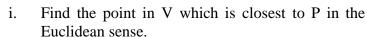
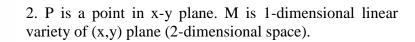
## EE 503, HW #1 (Due: Oct. 11, 2011)



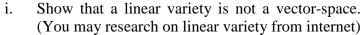
$$V = \{(x, y) : (x, y) = \alpha (\cos \Theta, \sin \Theta), \ \alpha \in R\}$$



b. By optimization over 
$$\alpha$$
.

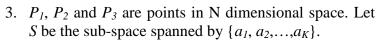


$$M = \{(x, y) : (x, y) = \underline{x_0} + \alpha (\cos \Theta, \sin \Theta), \ \alpha \in R\}$$



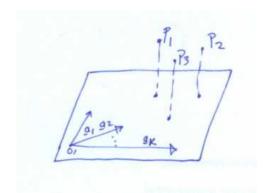
ii. Find the point in M which is closest to P (in the Euclidean sense), by optimizing over  $\alpha$ .

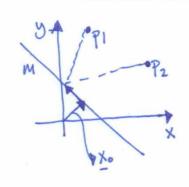
iii. Comment on the result found in part-ii. Is the orthogonality principle valid for linear variety?



i. Find the point  $\hat{P}$  in S such that  $\|\hat{P} - P_1\|^2 + \|\hat{P} - P_2\|^2 + \|\hat{P} - P_3\|^2 \text{ is minimum. (} \|x\| \text{ is the Euclidean norm.)}$ 

ii. Give a geometric interpretation.





4.  $P_1$  and  $P_2$  are two points in the x-y plane. M is 1 dimensional linear variety of (x,y) plane (2-dimensional space).

$$M = \{(x, y) : (x, y) = \underline{x_0} + \alpha (\cos \Theta, \sin \Theta), \ \alpha \in R\}$$

Let  $P_1=(1,0)$ ,  $P_2=(-1,0)$  and let M be the points on the line y=-x+4. Find the point  $\hat{P}$  in the variety M such that the sum of distances to  $P_1$  and  $P_2$ , i.e.  $\|\hat{P}-P_1\| + \|\hat{P}-P_2\|$ , is minimum. (Note: This problem is different from the

previous one. Here the cost is the distance itself, not the sum of distance *squares*). Hint: Consider drawing ellipses with the foci points P<sub>1</sub> and P<sub>2</sub>. (You may check http://torus.math.uiuc.edu/eggmath/Shape/ellipse-eq.html for more information.)