

Equivalent Circuits on Connected Arrays

$$Z_{in, slot} = \frac{1}{4dx} \sum_{m_x=-\infty}^{\infty} \frac{-\text{sinc}^2\left(\frac{k_{xm}\delta_s}{2}\right)}{D_{00}(k_{xm})}$$

$$D_{00}(k_{xm}) = \frac{1}{dy} \sum_{m_y=-\infty}^{\infty} G_{xx}^{hm}(k_{xm}, k_{ym}) \delta_0\left(\frac{k_{ym} \omega_s}{2}\right)$$

$$Z_{slot}^a = Z_{m_x=0} + Z_{m_x \neq 0} = -\frac{1}{dx} \frac{\text{sinc}^2\left(\frac{k_{x0}\delta_s}{2}\right)}{4 D_{00}(k_{x0})}$$

$$-\frac{1}{4dx} \sum_{m_x \neq 0} \frac{\text{sinc}^2\left(\frac{k_{xm}\delta_s}{2}\right)}{D_{00}(k_{xm})}$$

we can decompose sum in infinity

$$Y_{m_x=0} = -\frac{4dx}{\text{sinc}^2\left(\frac{k_{x0}\delta_s}{2}\right)} D_{00}(k_{x0}) = Z_{00} + Z_{m_x \neq 0, m_y \neq 0}$$

$$= -\frac{4dx \delta_0\left(\frac{k_{y0}\omega_s}{2}\right) G_{xx}^{hm}(k_{x0}, k_{y0})}{dy \text{sinc}^2\left(\frac{k_{x0}\delta_s}{2}\right)} - \frac{4dx}{dy \text{sinc}^2\left(\frac{k_{x0}\delta_s}{2}\right)}$$

$$\sum_{m_y \neq 0} G_{xx}^{hm}(k_{x0}, k_{ym}) \delta_0\left(\frac{k_{ym}\omega_s}{2}\right)$$

$$Y_{00} = -n^2 G_{xx}^{hm}(k_{x0}, k_{y0}), \text{ where } n^2 \text{ is:}$$

$$n^2 = \frac{4dx \delta_0\left(\frac{k_{y0}\omega_s}{2}\right)}{dy \text{sinc}^2\left(\frac{k_{x0}\delta_s}{2}\right)}$$

$$-G_{xx}^{hm}(k_{x0}, k_{y0}) = \frac{1_{TE} k_x^2 - i_{TM} k_y^2}{k_p^2} = i_{TE} \cos^2 \phi - i_{TM} \sin^2 \phi$$

$$Y_{00} = n^2 (i_{TE} \cos^2 \phi - i_{TM} \sin^2 \phi)$$

$$-G_{xx}^{HM} = i_{TE} \cos^2 \phi - i_{TM} \sin^2 \phi$$

