# Lecture 15 Neural and Neuro-Symbolic Synthesis

(with material from Alex Polozov)

## Plan for this week

#### Tuesday: pre-LLM era

- statistical language models for code
- neural architectures
- better search with neural guidance

#### Thursday: LLM era

- synthesis from natural language
- how can we make LLMs generate better code?

## Statistical Language Models

Originated in Natural Language Processing

In general: a probability distribution over sentences in a language

• P(s) for  $s \in L$ 

#### In practice:

- must be in a form that can be used to guide generation / search
- and also that can be learned from the data we have

# Statistical Models in Synthesis

#### What are we modeling (conditioning)?

- A corpus of programs: what are likely programs in this language / DSL / for this specific task?
- Spec-program pairs: what are likely programs for this spec?

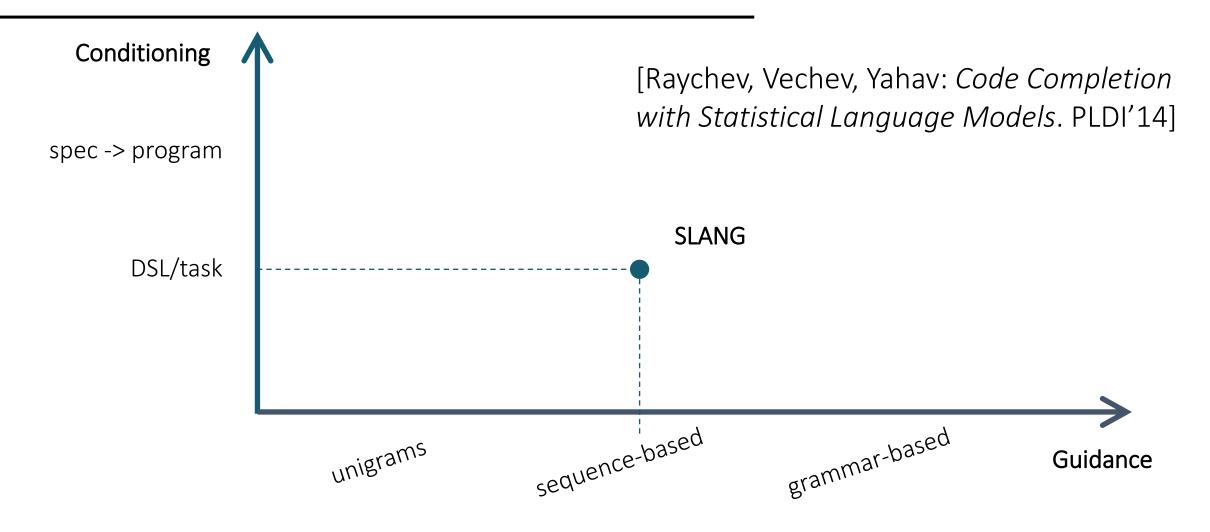
#### Kinds of guidance:

- Likely components (unigrams)
- Sequence-based: probability of next token (given previous tokens)
- Grammar-based: probability of grammar rule

#### Model architecture:

n-grams, PHOG, neural, ...

# Statistical Models in Synthesis



## **SLANG**

Input: code snippet with holes

```
SmsManager smsMgr = SmsManager.getDefault();
int length = message.length();
if (length > MAX_SMS_MESSAGE_LENGTH) {
   ArrayList<String> msgList =
        smsMgr.divideMsg(message);
   ? {smsMgr, msgList} // (H1)
} else {
   ? {smsMgr, message} // (H2)
}
```



Output: holes completed with (sequences) of method calls

```
SmsManager smsMgr = SmsManager.getDefault();
int length = message.length();
if (length > MAX_SMS_MESSAGE_LENGTH) {
   ArrayList<String> msgList =
        smsMgr.divideMsg(message);
   smsMgr.sendMultipartTextMessage(...msgList...);
} else {
   smsMgr.sendTextMessage(...message...);
}
```

# **SLANG:** inference phase

#### code snippet with holes

```
SmsManager smsMgr = SmsManager.getDefault();
int length = message.length();
if (length > MAX_SMS_MESSAGE_LENGTH) {
   ArrayList<String> msgList =
        smsMgr.divideMsg(message);
   ? {smsMgr, msgList} // (H1)
} else {
   ? {smsMgr, message} // (H2)
}
```

#### abstract histories of objects

#### learned generative model:

- bigrams suggest candidates
- n-grams / RNNs rank them

Partial History	Id	Candidate Completions	Pr
$\langle \texttt{getDefault}, \texttt{ret} \rangle \cdot \langle \texttt{H2}, \texttt{smsMgr} \rangle$	11	$\langle  exttt{getDefault, ret}  angle \cdot \langle  exttt{sendTextMessage, 0}  angle$	0.0073
	12	(getDefault.ret) · (sendMultipartTextMessage.0)	0.0010
$\langle \texttt{getDefault}, \texttt{ret} \rangle \cdot \langle \texttt{divideMsg}, 0 \rangle \cdot \langle \texttt{H1}, \texttt{smsMgr} \rangle$	21	$\langle  exttt{getDefault,ret}  angle \cdot \langle  exttt{divideMsg}, 0  angle \cdot \langle  exttt{sendMultipartTextMessage}, 0  angle$	0.0033
	22	$\langle  exttt{getDefault,ret}  angle \cdot \langle  exttt{divideMsg}, 0  angle \cdot \langle  exttt{sendTextMessage}, 0  angle$	0.0016
$\langle  exttt{length}, 0  angle \cdot \langle  exttt{H2},  exttt{message}  angle$	31	$\langle \text{length}, 0 \rangle \cdot \langle \text{length}, 0 \rangle$	0.0132
	32	$\langle \text{length}, 0 \rangle \cdot \langle \text{split}, 0 \rangle$	0.0080
	33	$\langle  exttt{length}, 0  angle \cdot \langle  exttt{sendTextMessage}, 3  angle$	0.0017
	34	(length,0) $\cdot$ (sendMultipartTextMessage,1)	0.0001
$\langle divideMsg, ret \rangle \cdot \langle H1, msgList \rangle$	41	$\langle  ext{divideMsg, ret}  angle \cdot \langle  ext{sendMultipartTextMessage}, 3  angle$	0.0821

## **SLANG**

Predicts completions for sequences of API calls

Treats programs as (sets of) abstract histories

• Performs static analysis to abstract programs into finite histories

Training: learns bigrams, n-grams, RNNs on histories

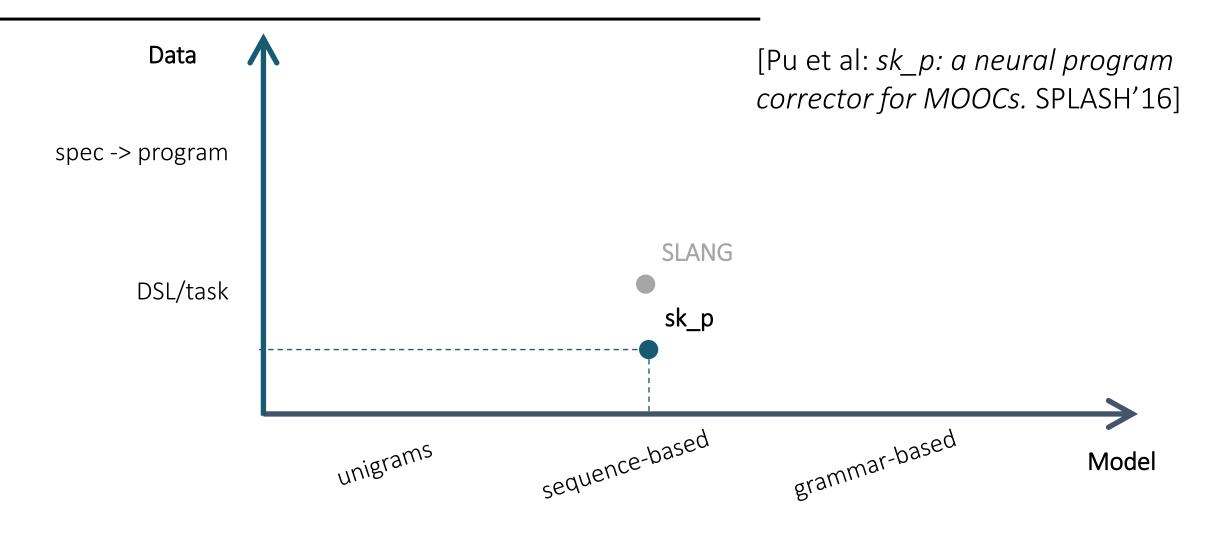
Inference: given a history with holes

- Uses bigrams to get possible completions
- Uses n-grams / RNN to rank them
- Combines history completions into a coherent program

Features: fast (very little search)

Limitations: all invocation pairs must appear in training set

# Statistical Models in Synthesis



```
Input: incorrect program
      + test suite
```

```
def evaluatePoly(poly, x):
  \mathsf{a}=\mathsf{0}
  f = 0.0
  for a in range (0, len(poly) - 1):
    f = poly[a]*x**a+f
    a += 1
  return f
```



def evaluatePoly(poly, x):

 $\mathsf{a}=\mathsf{0}$ 

return f

```
f = 0.0
                                     while a < len(poly):
Output: corrected program
                                       f = poly[a]*x**a+f
                                       a += 1
```

# sk\_p

```
_start_
  def evaluatePoly(poly, \times):
                                                                x^2 = 0
    a = 0
                                   normalize variables
                                                                x3 = 0.0
    f = 0.0
                                                                for x2 in range (0, len (x0) - 1):
    for a in range (0, len(poly) - 1):
                                                                  x3 = x0 [x2] * x1 ** x2 + x3
      f = poly[a]*x**a+f
                                                                                                             extract
                                                                  x2 += 1
      a += 1
                                                                return x3
    return f
                                                                                                              partial
                                                              _end_
                                                                                                             fragments
                                                                               Partial Fragment 1:
   def evaluatePoly(poly, x):
     a = 0
                                                                               _start_
     f = 0.0
     while a < len(poly):
                                                                                 x3 = 0.0
       f = poly[a]*x**a+f
                                                                               Partial Fragment 2:
       a += 1
     return f
                                                                                 x2 = 0
                                                                                for x2 in range (0, len (x0) - 1):
                                                                  neural net
                                                                               Partial Fragment 3:
                                                                  (seq2seq)
beam search
                                                                                 x3 = 0.0
                           0.141, while x^2 < len (x^0):
                            0.007, for x4 in range ( len ( x0 ) ) :
                                                                                 x3 = x0 [x2] * x1 * * x2 + x3
                           0.0008, for x4 in range (0):
```

# sk\_p

Program corrections for MOOCs

Treats programs as a sequence of tokens

Abstracts away variables names

Uses the skipgram model to predict which statement is most likely to occur between the two

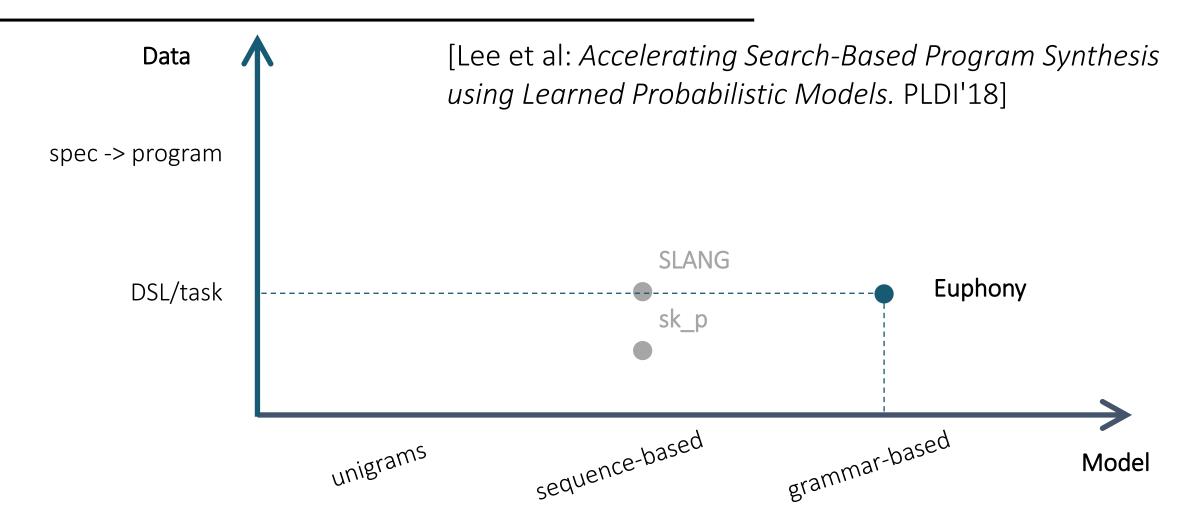
#### Features

Can repair syntax errors

#### Limitations

Needs all algorithmically distinct solutions to appear in the training set

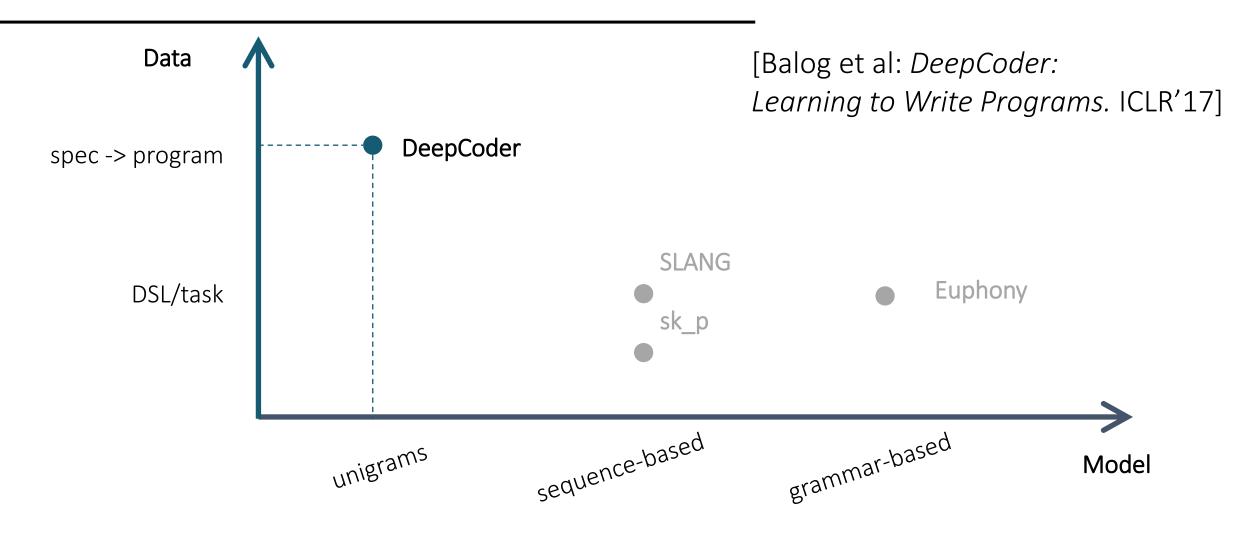
# Statistical Models in Synthesis



# Euphony

Trains a PHOG on a corpus of solutions to simple problems Uses it to guide top-down search with A\* Normalizes constants (transfer learning)

# Statistical Models in Synthesis



## DeepCoder

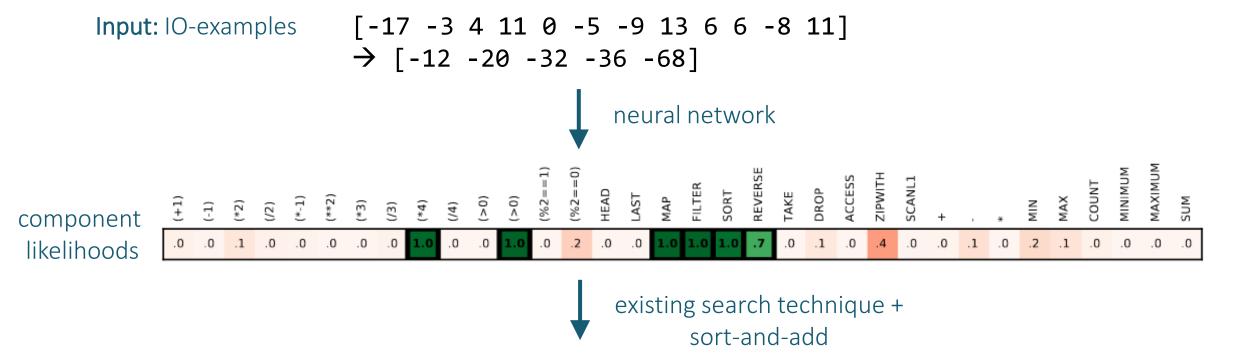
Input: IO-examples 
$$[-17 -3 \ 4 \ 11 \ 0 \ -5 \ -9 \ 13 \ 6 \ 6 \ -8 \ 11]$$

$$\rightarrow [-12 \ -20 \ -32 \ -36 \ -68]$$



Output: Program in a list DSL

## DeepCoder



Output: Program in a list DSL

## DeepCoder

#### Predicts likely components from IO examples

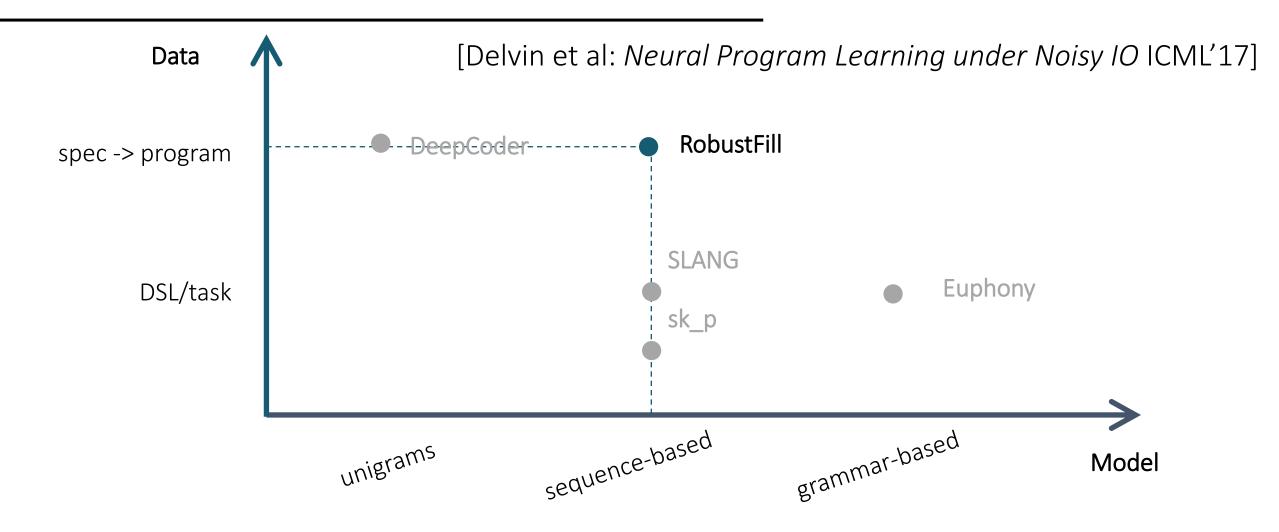
#### Features

- Trained on synthetic data
- Can be easily combined with any enumerative search
- Significant speedups for a small list DSL

#### Limitations

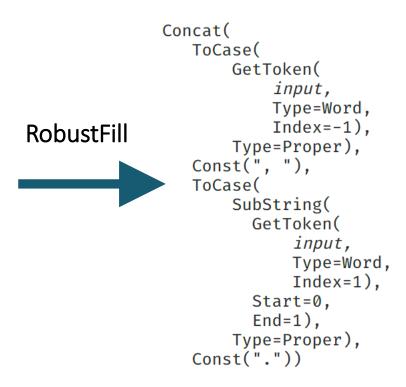
- Unclear whether it scales to larger DSLs or more complex data structures
- e.g. uses a simple feed-forward neural net, cannot encode arbitrarylength examples

# Statistical Models in Synthesis

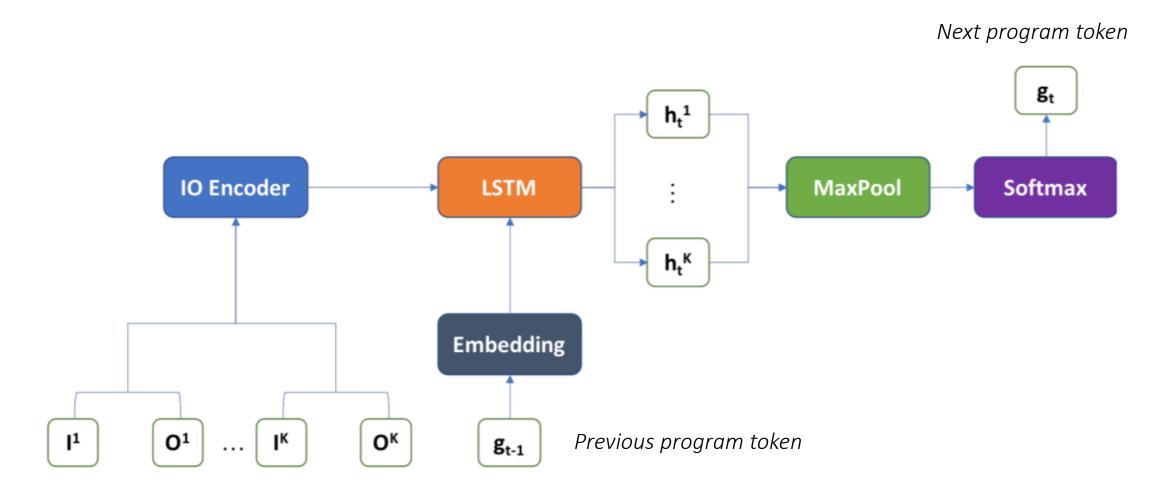


## RobustFill, aka neural FlashFill

Input String	Output String
jacob daniel devlin	Devlin, J.
jonathan uesato	Useato, J
Surya Bhupatiraju	Bhupatiraju S.
Rishabh q. singh	Singh, R.
abdelrahman mohamed	Mohamed, A.
pushmeet kohli	Kohli, P.



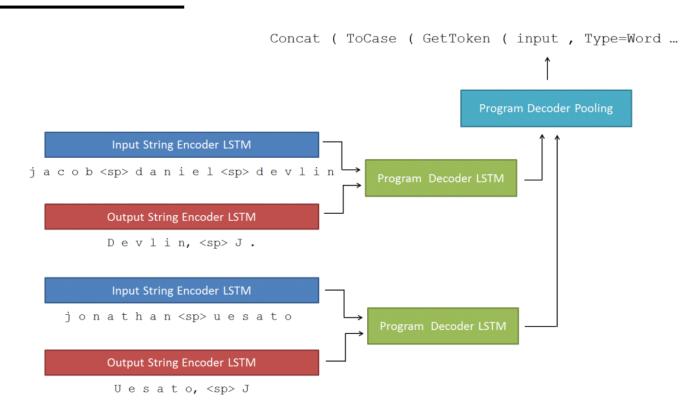
# RobustFill: PBE as Seq2Seq



## RobustFill

#### Key ideas:

Embed I/O examples with LSTM encoders
Emit program tokens with LSTM decoders
Train from large-scale random data



## RobustFill

#### Key ideas:

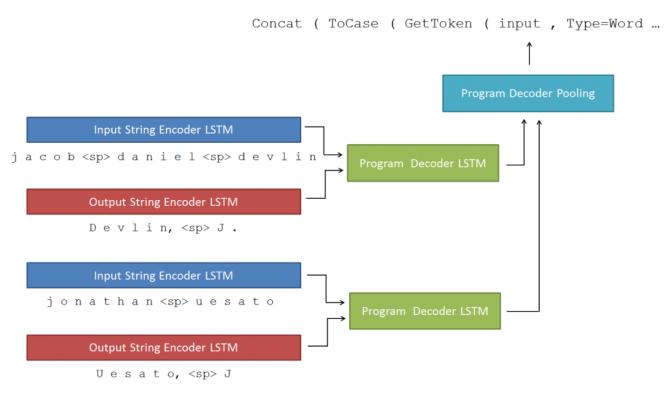
Embed I/O examples with LSTM encoders
Emit program tokens with LSTM decoders
Train from large-scale random data

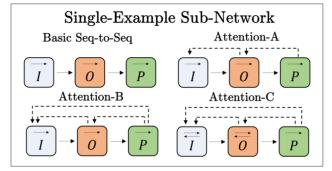
#### Architecture:

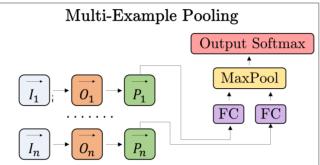
- *Pooling* across examples at each step to predict one program token
- Attention to examples during program decoding

#### Beam search with execution constraints

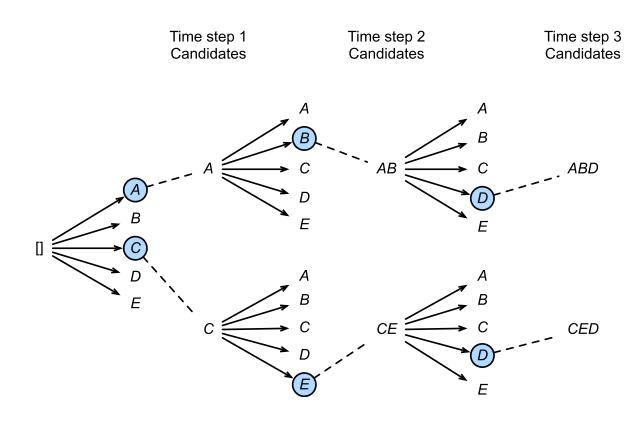
 Execute decoded subexpressions; remove programs whose outputs are not prefixes of the target







## Beam search with constraints



## RobustFill

IO examples to program translation as a Seq2Seq task

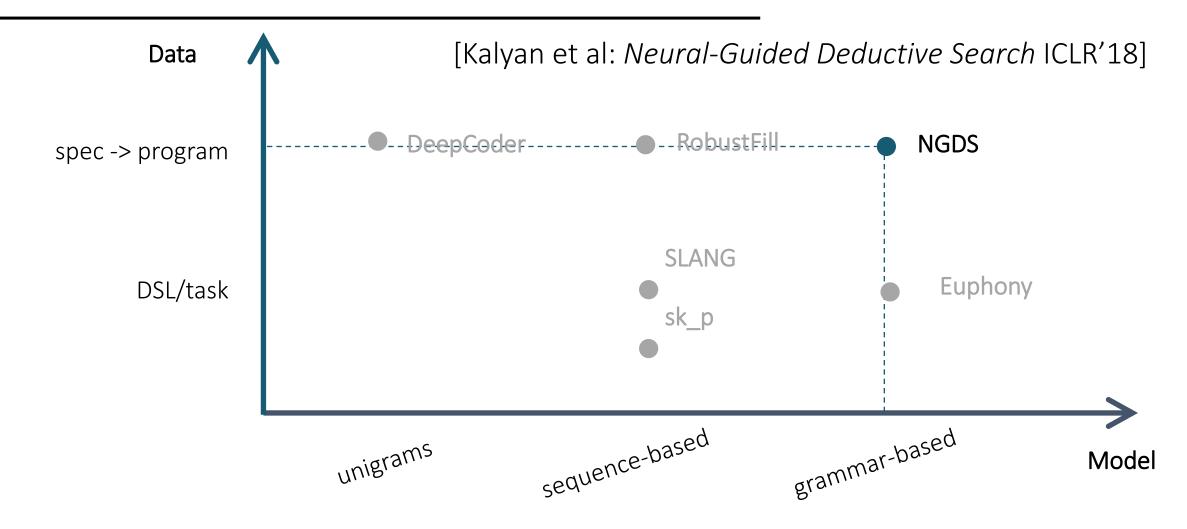
#### Features

- Trained on synthetic data
- Unlike FlashFill, does not require inverse semantics
- Noise-tolerant

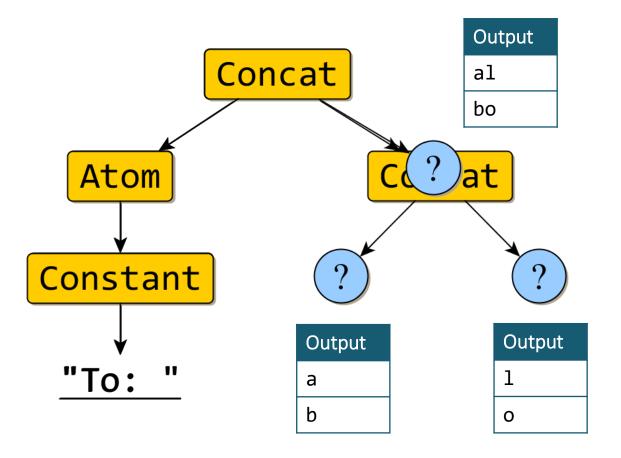
#### Limitations

- Does not guarantee consistency with IO examples
- Requires constraints/postprocessing to ensure grammar syntax
- Hard to design synthetic data generation realistically

# Statistical Models in Synthesis



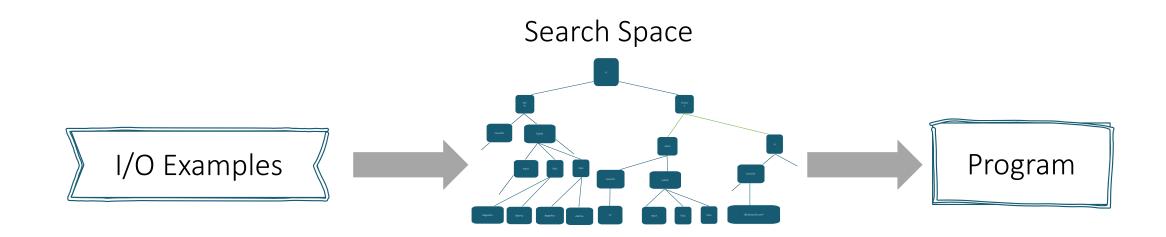
### **Deductive Search**



Input	Output
alice liddell	To: al
bob o'reilly	To: bo

- 1. Select a hole.
- 2. Select an operator to expand.
- 3. Propagate the examples.
- ✓ Correct by construction
- ✓ Constraint propagation exists for many operations & domains
- ✓ Easy to add a ranking function
- **X** Exponentially slow

## **Deductive Search**



Why so slow? Explores the entire search space (unless deduction prunes some of it)

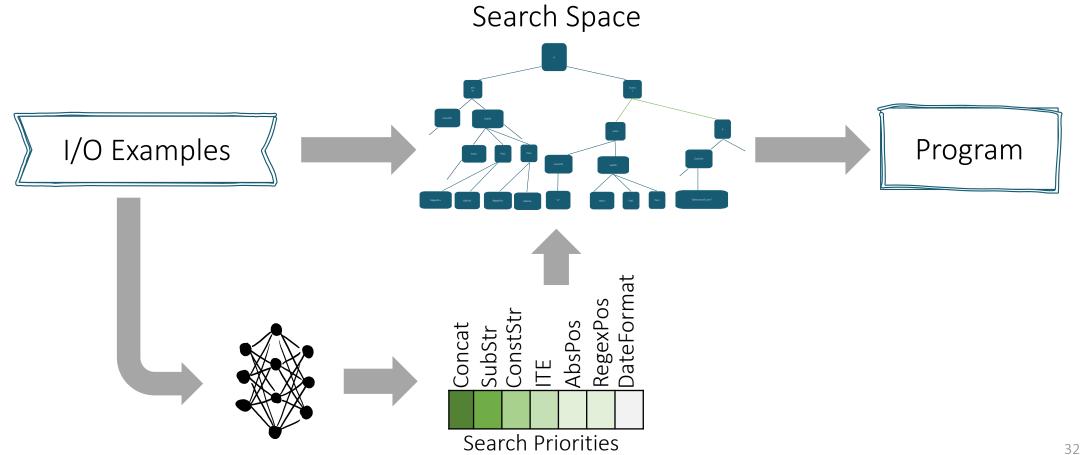
# Machine-learned insights

Input	Output		
alice liddell	To: al		
bob o'reilly	To: bo		

Can't be a substring, requires concatenation

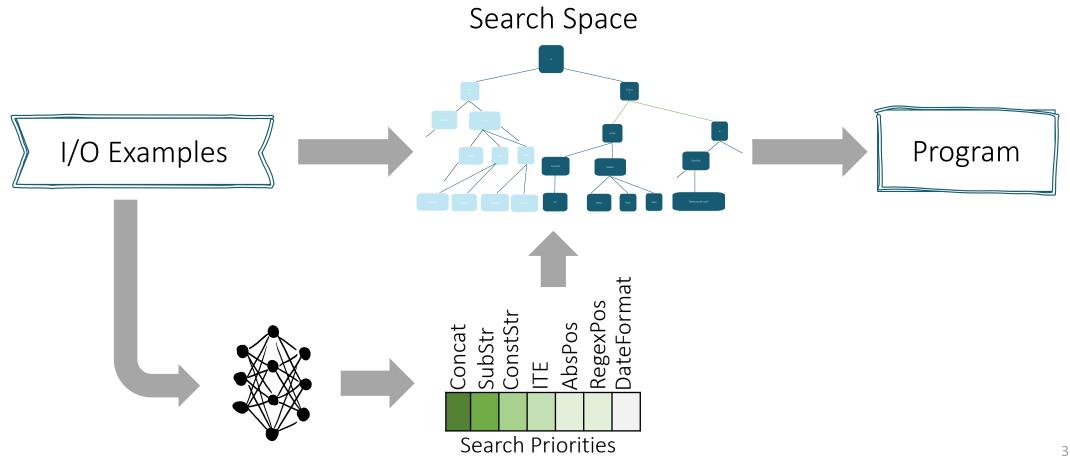
## DeepCoder: Learning to Write Programs

Idea: Order the search space based on a priority list from DNN before starting



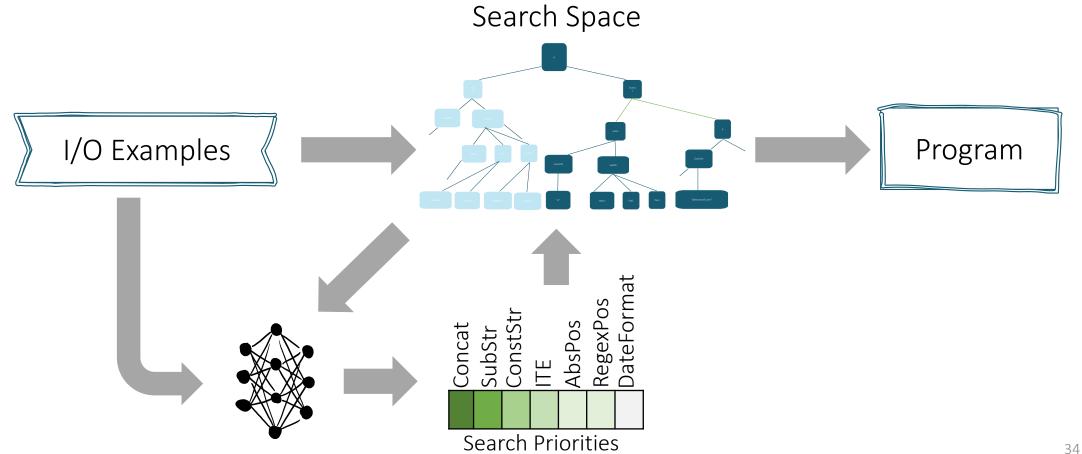
## DeepCoder: Learning to Write Programs

Idea: Order the search space based on a priority list from DNN before starting



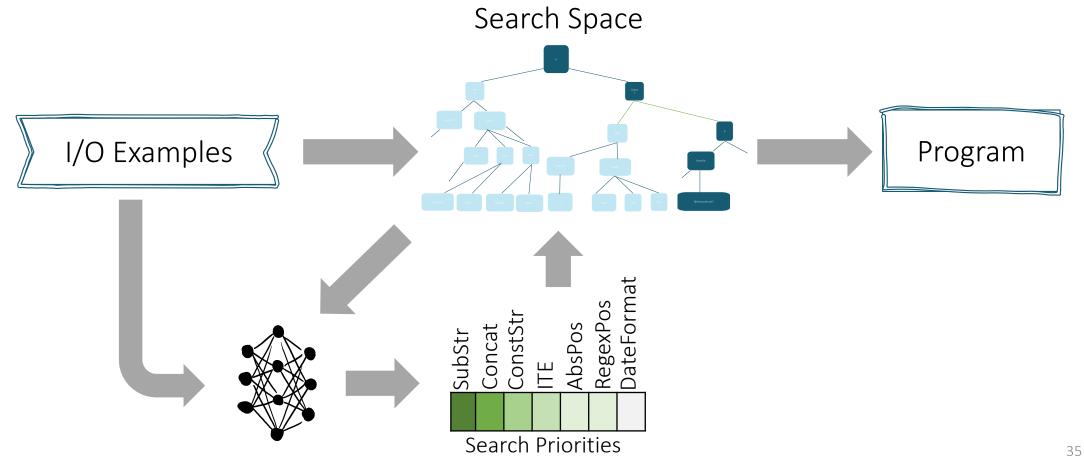
## Neural-Guided Deductive Search

Idea: Order the search space based on a priority list from DNN at each step



## Neural-Guided Deductive Search

Idea: Order the search space based on a priority list from DNN at each step



## Search branch prediction

Collect a complete dataset of intermediate search results:

```
at a search branch N \coloneqq F_1(\dots) \mid F_2(\dots) \mid \dots \mid F_k(\dots) given a spec \varphi = \{x \rightsquigarrow y\} produced programs P_1, \dots, P_k with scores h(P_1, \varphi), \dots, h(P_k, \varphi)
```

Learn a predictive model f s.t.  $f(F_j, \varphi) \approx h(P_j, \varphi)$ 

- $\varphi$  is an input-output example spec:  $\varphi = \{x \mapsto y\}$
- *f*: (enum production\_id, string x, string y) -> float

## Search branch prediction

Collect a complete dataset of intermediate search results:

at a search branch 
$$N \coloneqq F_1(\dots) \mid F_2(\dots) \mid \dots \mid F_k(\dots)$$
 given a spec  $\varphi = \{x \leadsto y\}$  produced programs  $P_1, \dots, P_k$  with scores  $h(P_1, \varphi), \dots, h(P_k, \varphi)$ 

Learn a predictive model f s.t.  $f(F_j, \varphi) \approx h(P_j, \varphi)$ 

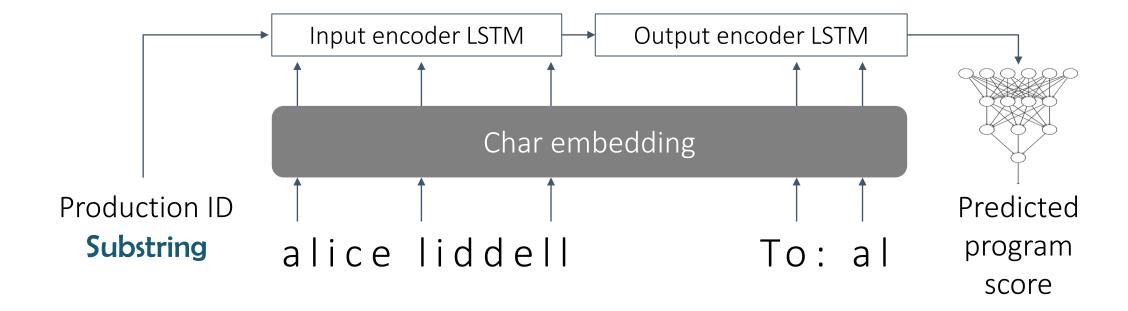
Train using squared-error loss over program scores:

Objective: 
$$\mathcal{L}(f; F_j, \varphi) = [f(F_j, \varphi) - h(P_j, \varphi)]^2$$

Q: Why not re-ranking of branches?

Because the magnitude of score values matters.

## Model architecture



### Search

### Threshold-based

- For a fixed threshold  $\theta$
- explore all branches within  $\theta$  from the best

### Branch-and-bound

- Explore branches depth-first in the order of scores
- Discard unexplored branches if they are predicted to be worse than current optimum

### **NGDS**

### VSA-based search + neural guidance

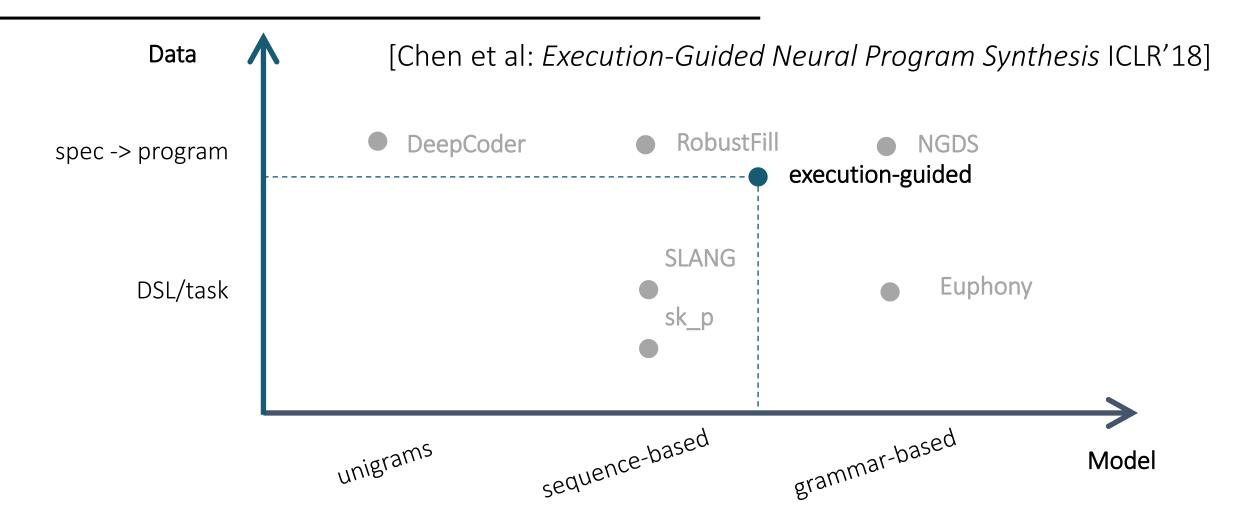
### Features

- Guarantees consistency with IO examples
- Thanks to top-down prop, we only need to learn a single grammar expansion => can generate many training examples from one synthesis problem

### Limitations

Requires inverse semantics (like FlashFill)

# Statistical Models in Synthesis



### Execution-guided neural synthesis

NGDS uses top-down propagation to make the model's task easier

• but this requires inverse semantics 🕾

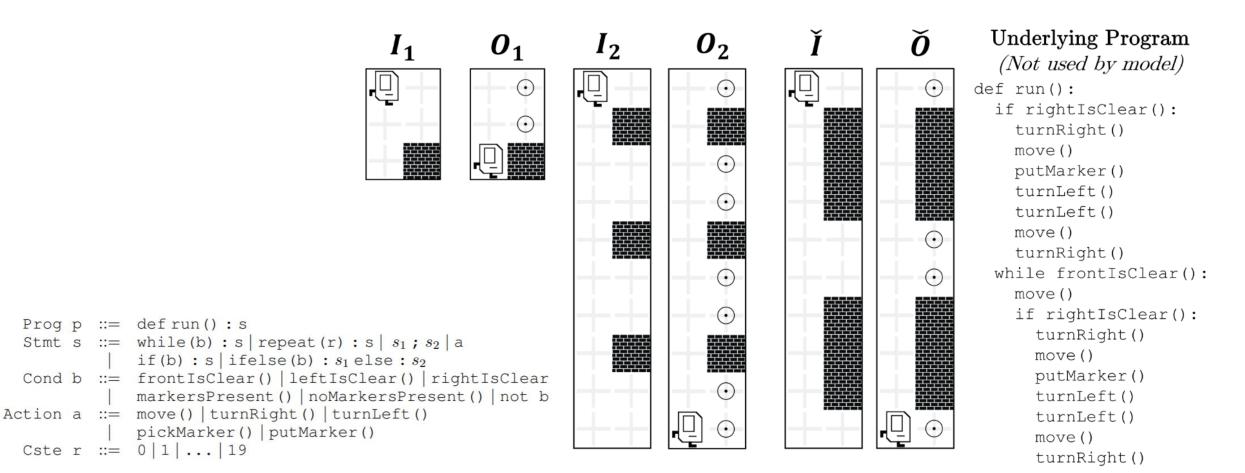
Can we do something similar but only using forward semantics?

yes we can, for imperative programs!

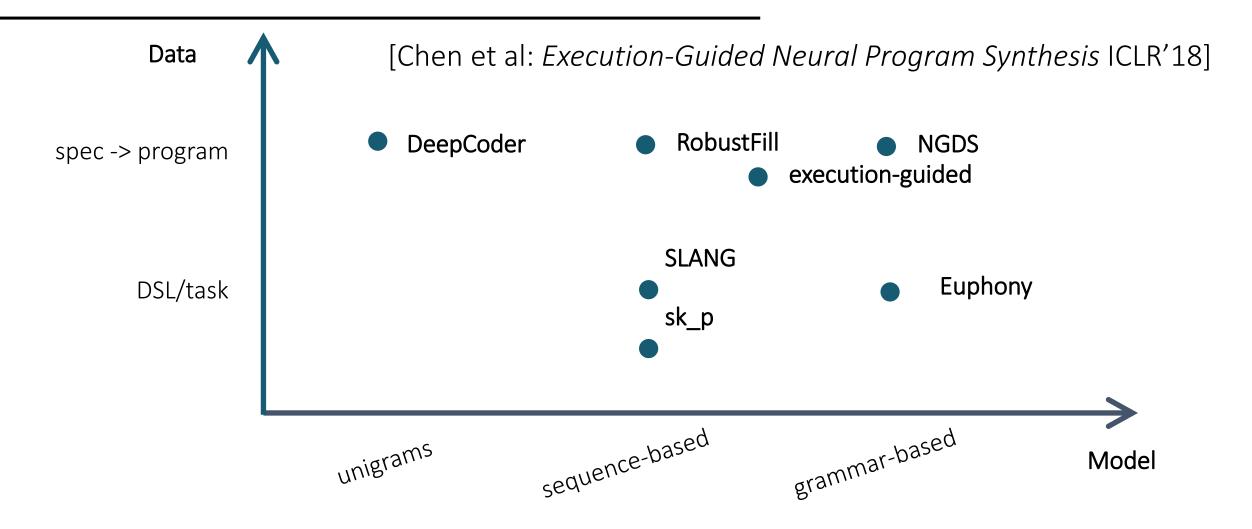
# Karel: robot navigation DSL

Prog p ::= defrun():s

Cste r ::= 0 | 1 | ... | 19



# Statistical Models in Synthesis



# Takeaways

### Neural networks excel at noticing patterns in input data

don't expect magic, task must be solvable by a human

### Needs appropriate network architecture

• e.g. LSTM for sequential examples, CNN for grids, ...

### Needs a search algorithm

• A\*, branch-and-bound, beam, MCTS, sequential monte-carlo, ...

# Takeaways (training)

### To train a model, you need enough data + appropriate loss

• For NNs: 10-100K diverse data points for an "average" task

### How to increase data efficiency?

- abstract the programs (Slang, Skip, Euphony)
- for spec->program can use synthetic data because we are learning semantics, not properties of the corpus (DeepCoder, Robustfill)
- the less context the guidance needs, the more data points we can extract from a given set of programs (NGDS)

### Plan for this week

### Tuesday: pre-LLM era

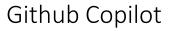
- statistical language models for code
- neural architectures
- better search with neural guidance

### Thursday: LLM era

- synthesis from natural language
- how can we make LLMs generate better code?

# LLMs are changing the world...







Chat GPT

and more...



Amazon CodeWhisperer

# LLMs are changing the world...

```
parse_expenses.py
                                                ddresses.rb
sentiment.ts
 1 #!/usr/bin/env ts-node
 3 import { fetch } from "fetch-h2";
 6 // Use a web service
 7 async function isPositive(text: string): Promise<boolean> {
     const response = await fetch('http://text-processing.com/api/sentiment/', {
       method: "POST",
       body: 'text=${text}',
       headers: {
         "Content-Type": "application/x-www-form-urlencoded",
     const json = await response.json();
     return json.label === "pos";
    8 Copilot
```

# ... but they are not perfect

### according to a survey of 410 developers [Liang et al, ICSE'24]:

• the most popular reason developers don't use LLMs is that generated code "doesn't meet functional or non-functional (e.g., security, performance) requirements that I need"

### according to [Perry et al, CCS'23]:

- participants with an AI assistant wrote significantly less secure code
- and were more likely to believe that they wrote secure code!

### Two challenges

### Accuracy

LLMs provide no guarantees that spec is satisfied

How do we increase the probability that a generated program matches user intent?

### **Validation**

Spec is partly informal: NL, code context

How do we determine if a program matches user intent?

# Techniques

### Accuracy

Constrained Decoding

Fine Tuning

### **Validation**

Self-consistency

User interaction

High-level DSL

# **Techniques**

Accuracy

**Constrained Decoding** 

Fine Tuning

Validation

Self-consistency

User interaction

High-level DSL

### Monitor-guided decoding

with static analysis of repository context. NeurIPS'23]

LLMs struggle to produce correct code in the context of a repo

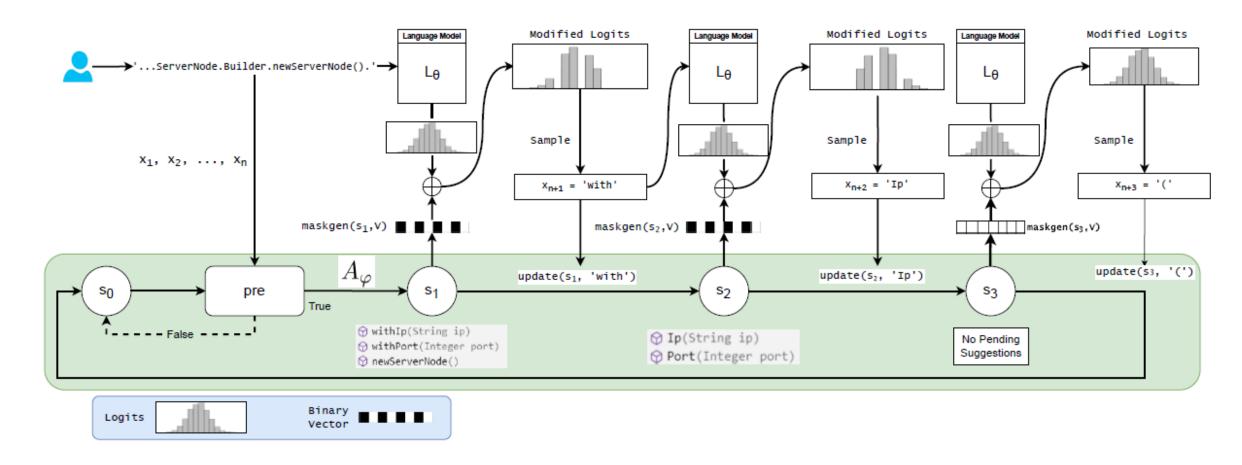
*Idea:* use a language server to mask LLM token predictions

```
text-davinci-003 and SantaCoder
            Method to be completed
private ServerNode parseServer(String url) {
                                                        host(arr[0])
    Preconditions.checkNotNull(url);
                                                        .port(Integer.parseInt(arr[1]))
    int start = url.indexOf(str:"/") + 2;
                                                        .build();
    int end = url.lastIndexOf(str:"?") == -1 ?
       url.length() : url.lastIndexOf(str:"?");
   String str = url.substring(start, end);
    String [] arr = str.split(regex:":");
                                                        SantaCoder with monitor guided decoding
    return ServerNode.Builder
                                                      withIp(arr[0])
            .newServerNode()
                                                      .withPort(Integer.parseInt(arr[1]))
                                                      .build();
```

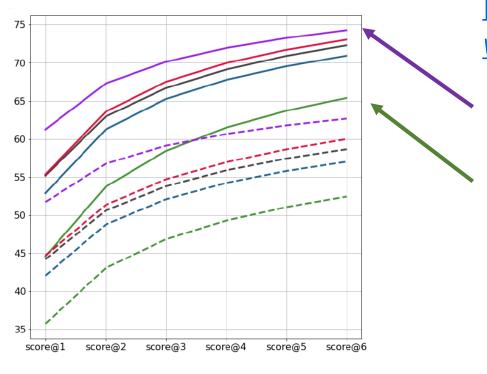
[Agrawal et al: Monitor-guided decoding of code LMs

### Monitor-guided decoding

[Agrawal et al: Monitor-guided decoding of code LMs with static analysis of repository context. NeurIPS'23]



### Monitor-guided decoding: results



compilation rate

[Agrawal et al: Monitor-guided decoding of code LMs with static analysis of repository context. NeurIPS'23]

text-davinci-003

code-gen 350M

Thanks to monitor guidance, a model with 1000x fewer parameters can generate better code than GPT3!

# **Techniques**

Accuracy

Constrained Decoding

Fine Tuning

Validation

Self-consistency

User interaction

High-level DSL

# Self-Play

AlphaZero got better at Go through self-play; can we do this for code?

*Idea:* use LLM to generate programming puzzles and solutions to those puzzles

# [Haluptzok et al: Language models can teach themselves to program better. ICLR'23]

```
def f(c: int):
    return c + 50000 == 174653

def g():
    return 174653 - 50000

assert f(g())
```

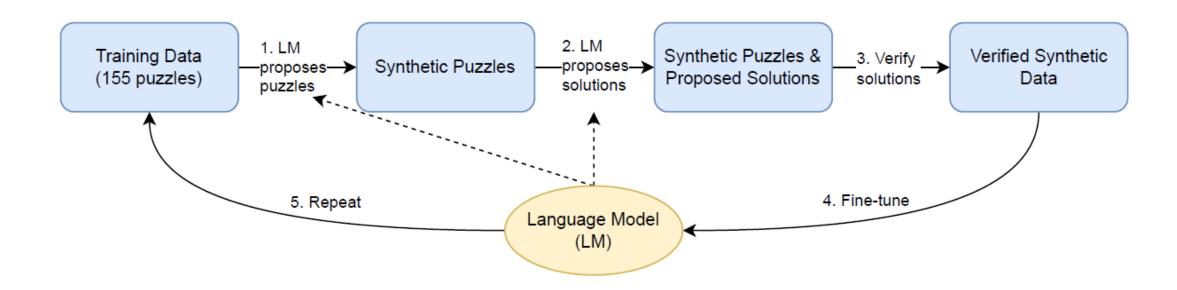
```
def f(x: str, chars=['Hello', 'there', 'you!'], n=4600):
    return x == x[::-1] and all([x.count(c) == n for c in chars])

def g(chars=['Hello', 'there', 'you!'], n=4600):
    s = "".join([c*n for c in chars])
    return s + s[::-1]

assert f(g())
```

# Self-Play

[Haluptzok et al: Language models can teach themselves to program better. ICLR'23]



# Self-Play: results

[Haluptzok et al: Language models can teach themselves to program better. ICLR'23]

fine-tune dataset	Verified	Puzzles	Solutions (Count)	# Tokens	Pass@100
Baseline	N/A	No puzzles	No solutions (0)	0	7.5%
Human	Yes	Human	Synthetic (635)	$74 \mathrm{K}$	10.5%
$ m Verified ext{-}125M$	Yes	Synthetic	Synthetic (1M)	74M	15.4%
Verified-1.3B	Yes	Synthetic	Synthetic (1M)	65M	18.9%
Verified-2.7B	Yes	Synthetic	Synthetic (1M)	66M	20.6%
Unverified-Codex	No	Synthetic	Synthetic (1M)	113M	21.5%
Verified-Codex	Yes	Synthetic	Synthetic (1M)	98M	38.2%

Test performance of the Neo-2.7B model after fine-tuning on puzzles produced by different models

Large pass@k improvement from one round of fine-tuning Puzzles from larger models are more helpful Unverified Codex is not as helpful!

# Techniques

Accuracy

Constrained Decoding

Fine Tuning

Validation

**Self-consistency** 

User interaction

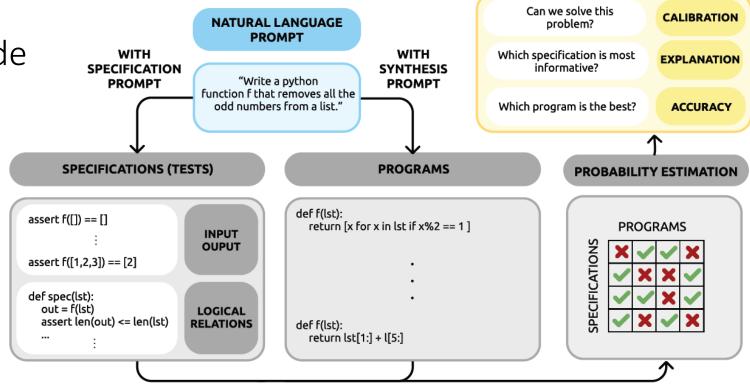
High-level DSL

# Speculyzer

[Li, Key, Ellis: *Towards trustworthy neural program synthesis.* 2023]

*Goal*: Increase trustworthiness of NL->code

*Idea:* generate *tests* alongside programs

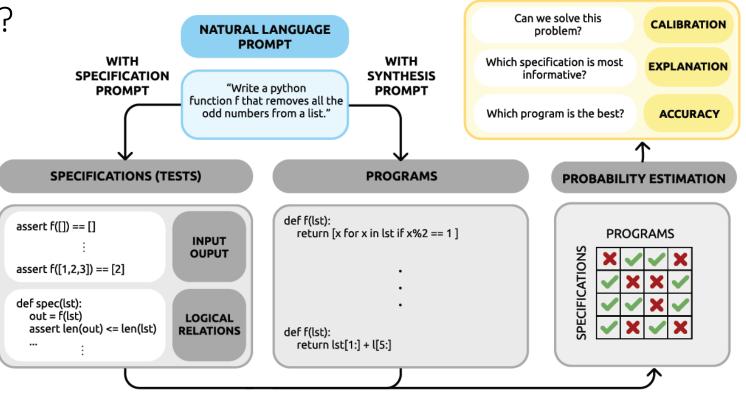


# Speculyzer

### What can we do with the tests?

- rank programs based how many tests they pass
- cluster programs based on their behavior on test inputs
- train a classifier to predict if the model knows the solution
- pick the most selective tests to show to the user

# [Li, Key, Ellis: *Towards trustworthy* neural program synthesis. 2023]



# Speculyzer

#### **PROGRAM**

```
def derivative(xs: list):
    """ xs represent coefficients of a polynomial.
    xs[0] + xs[1] * x + xs[2] * x^2 + ....
    Return derivative of this polynomial in the same form.
    >>> derivative([3, 1, 2, 4, 5])
    [1, 4, 12, 20]
    >>> derivative([1, 2, 3])
    [2, 6]
    """
    return [x * i for i, x in enumerate(xs) if i != 0]
```

#### **TOP LOGICAL RELATION**

```
def test_derivative(xs: list):
    """ Given an input `xs`, test whether the function `derivative`
is implemented correctly.

"""
    ys = derivative(xs)
    assert len(ys) == len(xs) - 1
    for i in range(len(ys)):
        assert ys[i] == xs[i+1] * (i + 1)

# run `test_derivative` on a new testcase
test_derivative([3, 1, 2, 4, 5])
```

#### **RANDOM LOGICAL RELATION**

```
def test_derivative(xs):
    """ Test function derivative().
    # TODO
    pass
# run `test_derivative` on a new testcase
test_derivative([2, 3, 4, 10, -12])
```

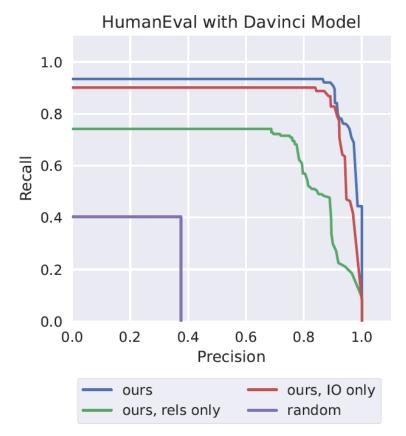
[Li, Key, Ellis: *Towards trustworthy neural program synthesis*. 2023]

Picking the most selective test to show to the user

# Speculyzer: results

Can achieve *zero error rate* on human eval in exchange for dropping recall from 93% to 44%!

# [Li, Key, Ellis: *Towards trustworthy neural program synthesis.* 2023]



# **Techniques**

Accuracy

Constrained Decoding

Fine Tuning

**Validation** 

Self-consistency

User interaction

High-level DSL

### The validation challenge

"In the context of Copilot, there is a shift from writing code to understanding code"

Taking Flight with Copilot, ACM Queue, Dec 22

#### validation is hard

• [Vaithilingam et al] observed 8 cases of over-reliance: bugs due to skipped validation

#### validation is a bottleneck

• single most prevalent activity according to [Mozannar et al]

prevalence of a validation strategy depends on its cost [Liang et al]

to help with validation, we need to lower its cost

### **LEAP**

[Ferdowsi et al: *Validating AI-Generated Code with Live Programming.* CHI'24]

lowers the cost of validation by execution using live programming

demo

# User study

no-LP

Al suggestions

+

terminal

LP

Al suggestions

+

live programming

### Research questions

how does live programming affect...

over- / under-reliance on Al validation strategies cognitive load

### Tasks

algorithmic

multiple correct suggestions

pandas

clean dataframe and compute stats
using pandas

API-heavy

algorithmic

no correct suggestions

bigrams

find most frequent bigram in a string

fixed prompt

### box plot

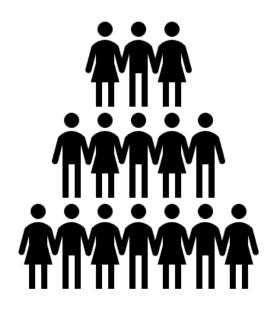
overlay scatter plot over boxplot using matplotlib

### string rewriting

parse rewrite rules and apply to string

open prompt

### **Participants**



n = 17

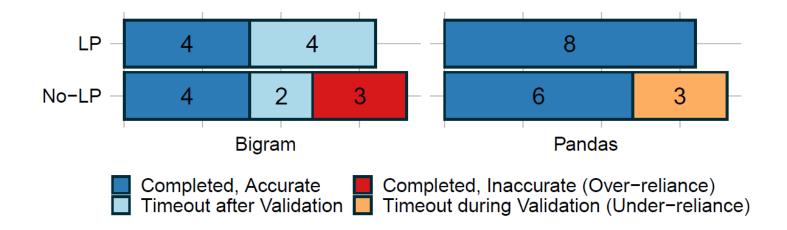
occupation:

15 academia / 2 industry

Python usage:

- 2 occasionally /
- 8 regularly /
- 7 almost every day

### RQ1: over-/under-reliance



6 no-PB vs O PB participants mid-judged correctness of their solution

by lowering the cost of validation, leap reduces over-/under-reliance on Al

### RQ1: over-/under-reliance

"it was easy to understand the behavior of a code suggestion because the little boxes on the side allowed for you to preview the results." (P3)

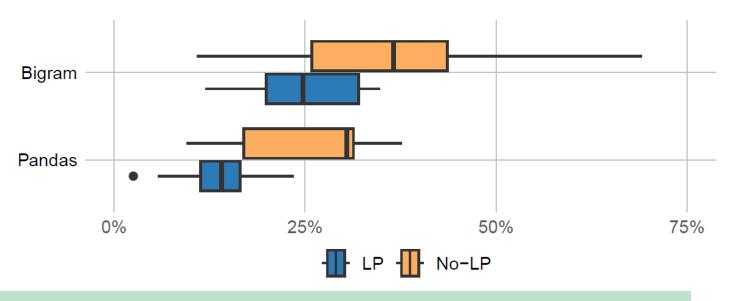
"it saved me the effort of writing multiple print statements." (P1)

6 no-PB vs O PB participants mid-judged correctness of their solution

by lowering the cost of validation, leap reduces over-/under-reliance on Al

# **RQ2:** validation strategies

percentage of time spent in Suggestion Panel

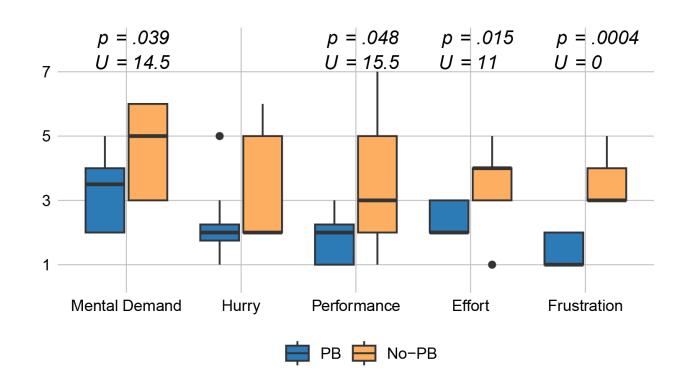


"I didn't look too closely in the actual code,
I was just looking at the runtime values on the side." (P1)

leap participants spent less time reading code

# RQ3: cognitive load

NASA TLX cognitive load metrics on Pandas



leap significantly reduced cognitive load of AI-assisted programming on tasks amenable to validation by execution

# **Techniques**

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### SatLM

#### Input

Q: Alex, Stan, and Adelwolfe are trying to catch them all, Pokemon that is. Together they have caught 339 Pokemon. Alex has caught 5 more than Stan, and Stan has caught 13 less than 4 times as many as Adelwolfe has caught. How many Pokemon has Stan caught?

#### CoT

#### LLM (Parse + Plan + Execute)



Let X be the number of Pokemon Stan has caught. Alex has caught 5 more than Stan, so Alex has caught X + 5.

Stan has caught 13 less than 4 times as many as Adelwolfe has caught, so Stan has caught 4X - 13. Together they have caught 339 Pokemon, so X + 5 + 4X - 13 = 339.

Combining like terms produces 5X + 5 = 339. Subtracting 5 from both sides produces 5X = 334. Dividing both sides by 5 produces X = \$66.80, so Stan has caught 66 Pokemon.

The answer is 66.



#### **ProgramLM**

#### LLM (Parse + Plan) # solution



stan pokemon = 4

adelwolfe pokemon = 13

stan pokemon = (total pokemon - alex pokemon - adelwolfe pokemon \* stan pokemon) / (1 -

stan pokemon)

result = stan pokemon

#### **Program**

#### Interpreter (Execute)



result = -94



#### SatLM

#### LLM (Parse)



(G)

total pokemon = 339

stan\_pokemon = Variable()

alex\_pokemon = stan\_pokemon + 5

stan pokemon = adelwolfe pokemon \* 4 - 13

total\_pokemon = alex\_pokemon + stan\_pokemon +

adelwolfe pokemon

result = stan pokemon

solve(result)



**FOL Formulas** 

#### Solver (Plan + Execute)



result = 147



֍

### SatLM: Contributions

### Declarative prompting is easier for the LLM

• it only does translation, not planning or execution

Significant accuracy increase across domains

- wrt standard prompting, CoT, ProgLM
- domains: arithmetic reasoning, logical reasoning, regex synthesis

Can use satisfiability/ambiguity for validation

### SatLM: Limitations

Limited to SMT-decidable logics

Some problems are better fit for imperative encoding

Some problems might require ambiguity

### SatLM: Fig 3 in Z3Py

#### **SAT Solution**

```
total_height = 120
joe_height = 2 * sara_height + 6
total_height = sara_height + joe_height
solve(joe_height)
```

```
from z3 import *

s = Solver()
sara_height = Int('sara_height')
joe_height = Int('joe_height')
total_height = 120
s.add(joe_height == 2 * sara_height + 6)
s.add(total_height == sara_height + joe_height)

if s.check() == sat:
    print(s.model()[joe_height])
```



# SatLM: ambiguity check

```
s.add(joe_height >= 2 * sara_height + 6)
s.add(total_height == sara_height + joe_height)
if s.check() == sat:
    res = s.model()[joe_height]
    s.add(joe height != res)
    if s.check() == sat:
        print('AMBIG')
    else:
        print(res)
else:
    print('UNSAT')
```

Z3 AMBIG

# SatLM: Potential Improvements

### Run multiple times and

- ignore attempts that don't parse or produce AMBIG/UNSAT
- even better: check answers for consistency

### Run in a loop, providing feedback to the LLM

- if AMBIG, tell the LLM to strengthen the constraints
- if UNSAT, get UNSAT core and tell the LLM to weaken one of those

### Combine individual constraints from different solutions

maybe perform lattice search until we get a SAT, unambiguous set