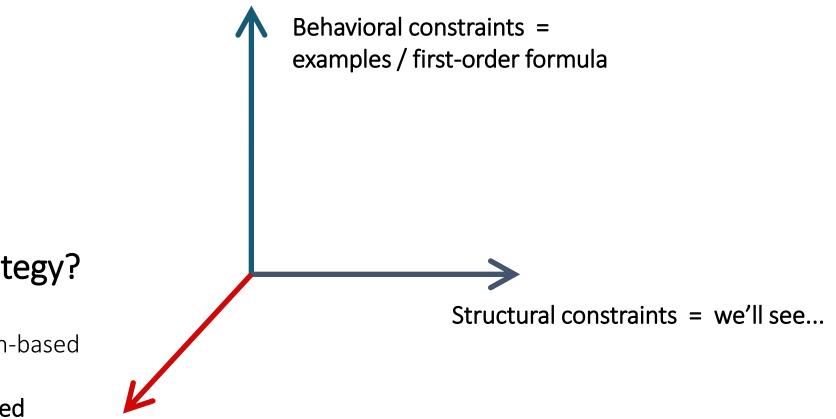
Lecture 8 Constraint-based search

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The problem statement



Search strategy?

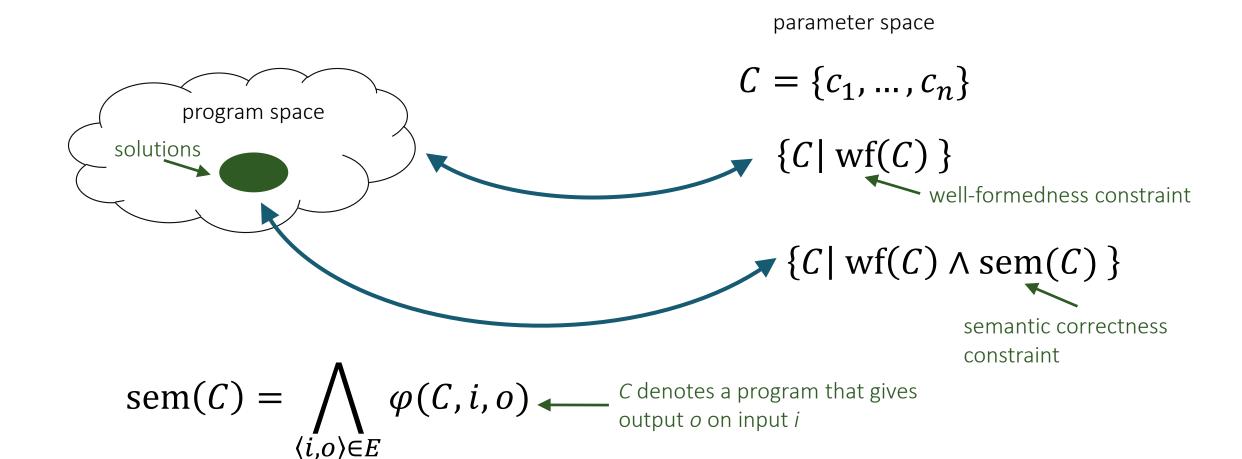
Enumerative Representation-based Stochastic

Constraint-based

Constraint-based search

Idea: encode the synthesis problem as a SAT/SMT problem and let a solver deal with it

What is an encoding?



How to define an encoding

```
Define the parameter space C = \{c_1, \dots, c_n\}
```

- encode : Prog → C
- decode : C → Prog (might not be defined for all C)

Define a formula $wf(c_1, ..., c_n)$

• that holds iff decode[C] is a "well-formed" program

Define a formula $\varphi(c_1, ..., c_n, i, o)$

that holds iff (decode[C])(i) = o

Constraint-based search

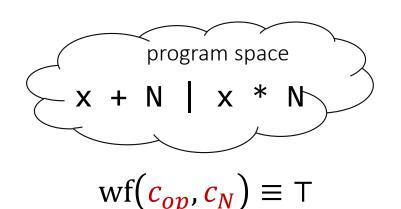
```
constraint-based (wf, \varphi, E = [i \rightarrow o]) {
    match SAT(wf(\mathcal{C}) \land \land_{\langle i,o \rangle \in E} \varphi(\mathcal{C},i,o)) with \longleftarrow for c_1, \ldots, c_n
    Unsat -> return "No solution" (i and o are fixed)

Model C* -> return decode[C*]
```

SAT encoding: example

```
x is a two-bit word
                                                                         parameter space
      program space
                                     (x = x_h x_1)
                                                                      C = \{c : Bool\}
                                     E = [11 \rightarrow 01]
                                                                       decode[0] \rightarrow x
                                                                       decode[1] \rightarrow x \& 1
wf(c) \equiv T
\varphi(c, i_h, i_l, o_h, o_l) \equiv (\neg c \Rightarrow o_h = i_h \land o_l = i_l)
\wedge (c \Rightarrow o_h = 0 \wedge o_l = i_l)
SAT(\varphi(c, 1, 1, 0, 1))
                                                                                     SAT solver
SAT((\neg c \Rightarrow 0 = 1 \land 1 = 1) \land (c \Rightarrow 0 = 0 \land 1 = 1))
                                                                                                      Model \{c \rightarrow 1\}
                                     return decode[1] i.e. x & 1
```

SMT encoding: example



N is an in integer literal x is an integer input

$$E = [2 \rightarrow 9]$$

parameter space

$$C = \{c_{op} : Bool, c_N : Int\}$$

$$decode[0,N] \rightarrow x + N$$

$$decode[1,N] \rightarrow x * N$$

$$\varphi(c_{op}, c_N, i, o) \equiv (\neg c_{op} \Rightarrow o = i + c_N) \land (c_{op} \Rightarrow o = i * c_N)$$

SAT
$$(\phi(c_{op}, c_N, 2,9))$$
SAT $((\neg c_{op} \Rightarrow 9 = 2 + c_N) \land (c_{op} \Rightarrow 9 = 2 * c_N))$

SMT solver

return decode[0,7] i.e. x + 7

What is a good encoding?

Sound

• if $wf(C) \wedge sem(C)$ then decode[C] is a solution

Complete

• if decode[C] is a solution then $wf(C) \wedge sem(C)$

Small parameter space

avoid symmetries

Solver-friendly

• decidable logic, compact constraint

DSL limitations

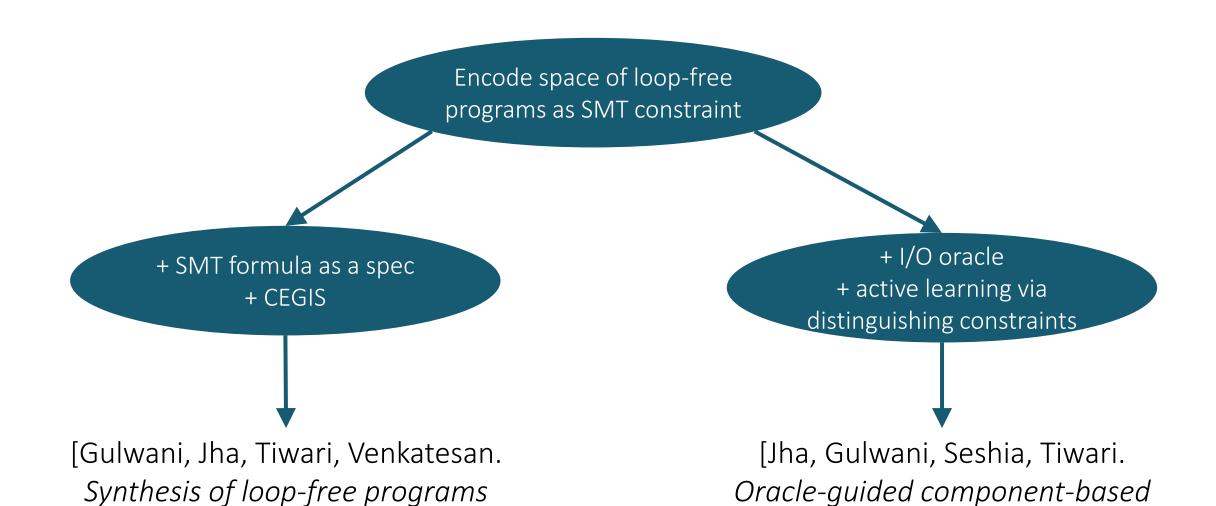
Program space can be parameterized with a finite set of parameters

Program semantics $\varphi(\mathcal{C},i,o)$ is expressible as a (decidable) SAT/SMT formula

Counterexample

Brahma

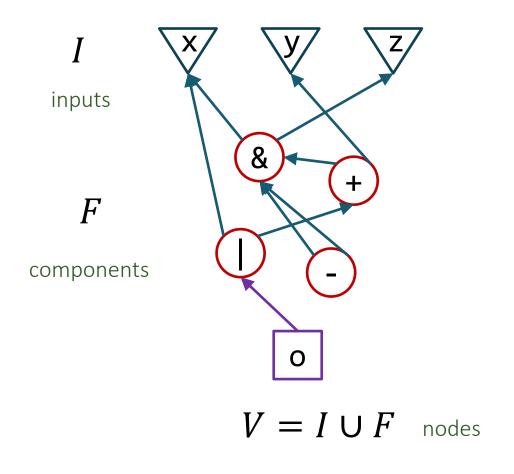
PLDI'11]



program synthesis. ICSE'10]

Brahma encoding: take 1

program = DAG

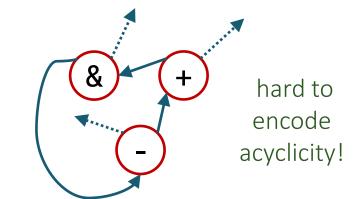


parameter space

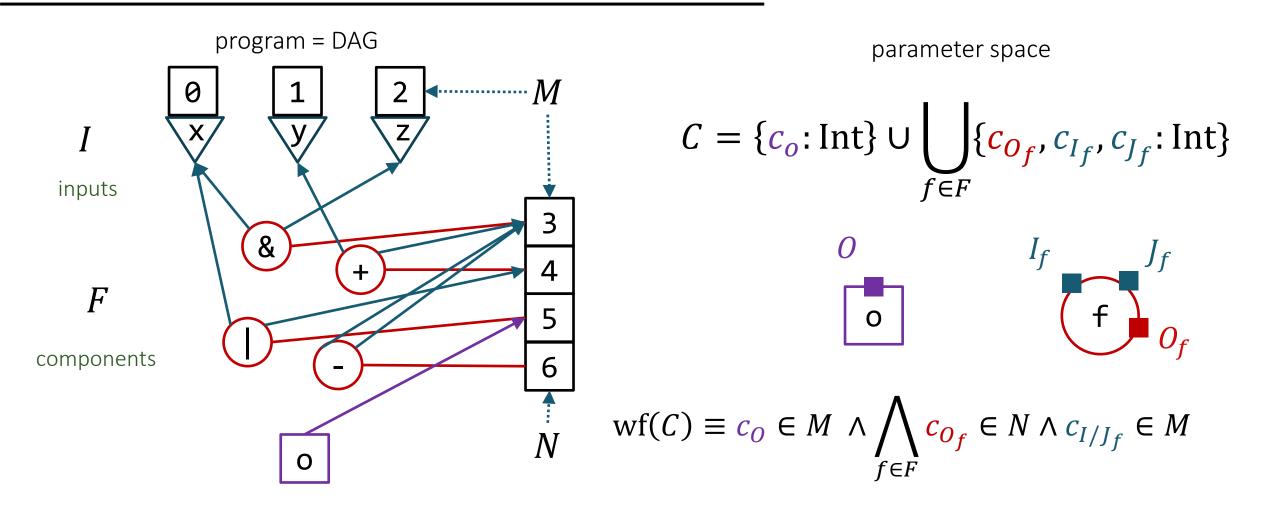
$$C = \{c_o: V\} \cup \bigcup_{f \in F} \{c_1^f, c_2^f: V\}$$



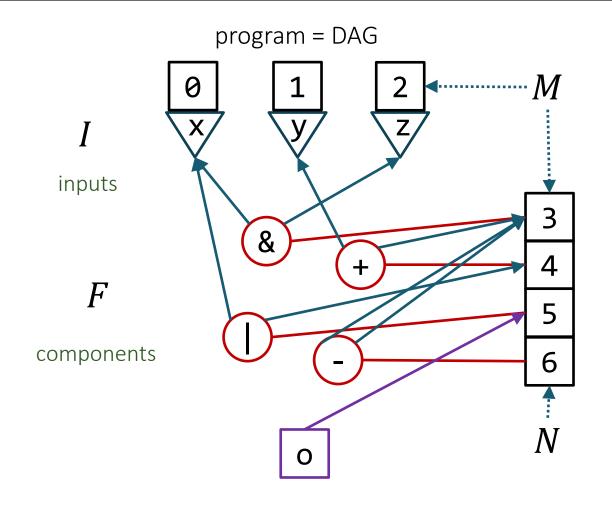
 $wf(C) \equiv ?$



Brahma encoding: take 2



Brahma encoding: take 2



parameter space

$$C = \{c_o: \operatorname{Int}\} \cup \bigcup_{f \in F} \{c_{O_f}, c_{I_f}, c_{J_f}: \operatorname{Int}\}$$

$$P = \bigcup_{f \in F} \{I_f, J_f\} \qquad R = \bigcup_{f \in F} \{O_f\}$$

$$\varphi(C, I, O) \equiv \exists P, R. \bigwedge_{f \in F} O_f = F(I_f, J_f)$$

$$\wedge \bigwedge_{x \in P \cup R \cup I \cup \{O\}} c_x = c_y \Rightarrow x = y$$

Brahma: contributions

SMT encoding of program space

- sound?
- complete?
- solver-friendly?
- why does line 5 in ExAllSolver use conjunction instead of implication?

SMT solver can guess constants

• e.g. 0x5555555 in P23

Brahma: limitations

Requires component multiplicities

- What happens if user provides too many? too few?
- What's the alternative to including dead code?
- How would you extend this approach to work without multiplicities?

Requires precise SMT specs for components

• What happens if we give an over-approximate spec?

Brahma: limitations

No ranking

Cannot handle:

- loops
- types
 - Can we add these things?

Brahma: questions

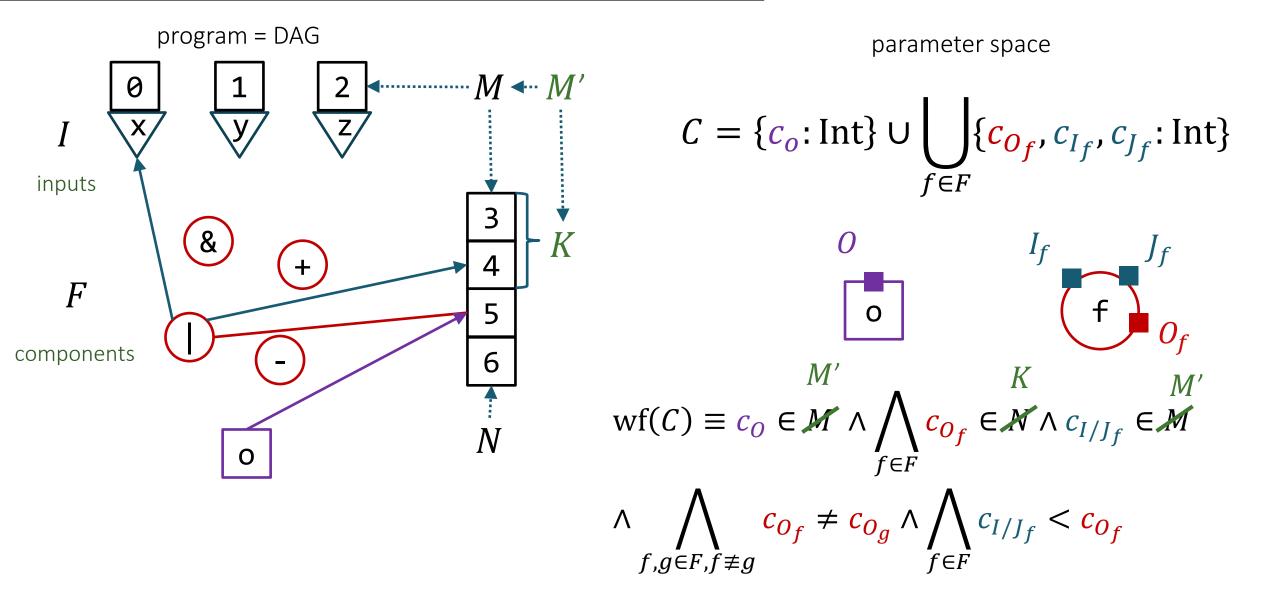
Behavioral Constraints? Structural Constraints? Search Strategy?

- First-order formula
- A multiset of components + straight-line program
- Constraint based + CEGIS

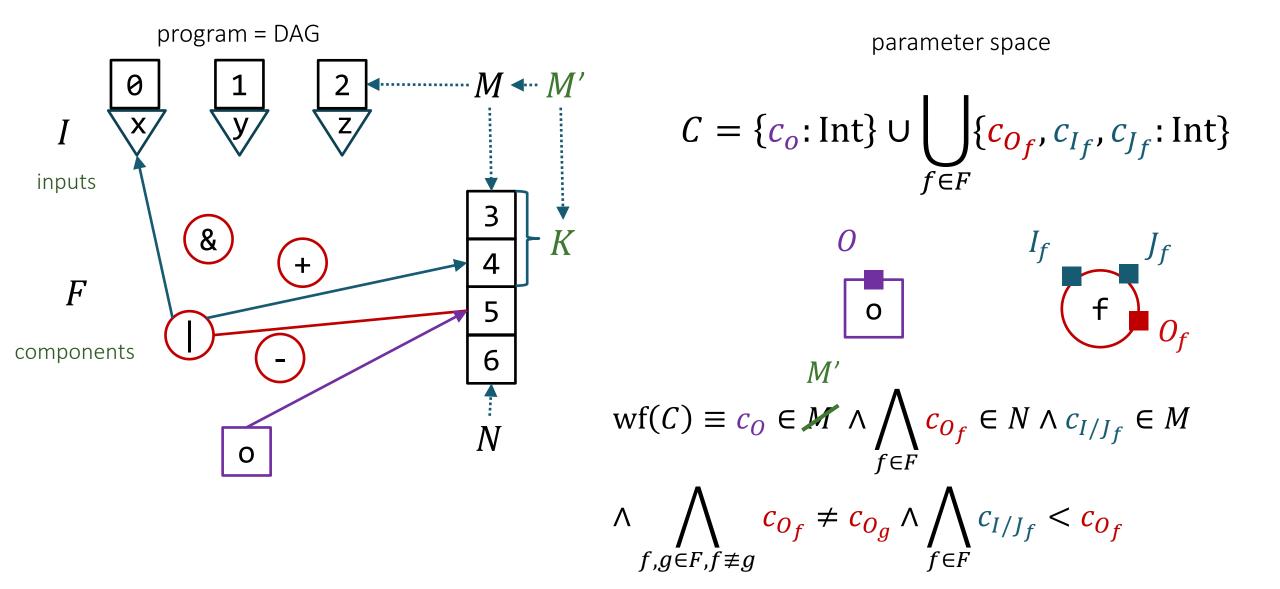
Can we represent these structural constraints as a grammar?

- Yes and no
- No because grammars cannot encode multiplicities
- Yes because the set is finite, so we can simply enumerate all possible programs
 - but this is not useful for synthesis

Limit #components to K?



Limit #components to K?



Comparison of search strategies

