

International Finance 4832

Lecture 4: Exchange Rates in the Short Run - The Asset Approach

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Before: LR \rightarrow PPP \rightarrow get E_{hf}^e
(Prices are flexible)

Now: SR \rightarrow UIP, ~~or~~ \rightarrow get E_{hf} (spot)
(Prices are sticky) (given i_h, i_f, E_{hf}^e)

This Lecture: Exchange Rates

This lecture - Exchange Rates in the Short Run and Integrated theory (LR and SR) (Chapter 15)

1. Last lecture: Exchange Rates in the **long run** - Monetary Approach to the ER

- ▶ Flexible prices
- ▶ PPP and UIP (both hold)
- ▶ Quantity theory of money (with interest sensitive liquidity) $\rightarrow L(i)$
- ▶ $i_h = r^* + \pi_h$ (Fisher equation with real rate convergence)
- ▶ Exchange Rate \rightarrow determined by prices/inflation $\quad d\text{ln}f = \bar{r}_{\text{L}} - \bar{r}_{\text{F}} \quad / \quad E_{\text{ln}f} = P_h / P_f$

2. Now: Exchange Rates in the **short run** (Chapter 15)

- ▶ Fixed prices (sticky)
- ▶ Long-run depreciation of ER is taken as given (as known) $(E_{\text{ln}f}^e)$
- ▶ Assumptions: UIP holds (PPP doesn't)
- ▶ Quantity theory of money (but with \bar{P})
- ▶ i determined by M / \bar{P} and $\underline{L(i)Y}$
- ▶ Exchange Rate \rightarrow determined by Interest Rates (From UIP)

3. Next: Integrating both approaches (LR and SR) and the Open Economy Trilemma (still Chapter 15)

Recap: UIP

Expected depreciation

$$i_{\$} = i_{\epsilon} + \underbrace{\left(\frac{E^e_{\$/\epsilon}}{E_{\$/\epsilon}} - 1 \right)}_{\text{Foreign Return (FR)}} \rightarrow \text{Future ER (given in the SR)} \rightarrow \text{Spot ER}$$

Domestic Return (DR)

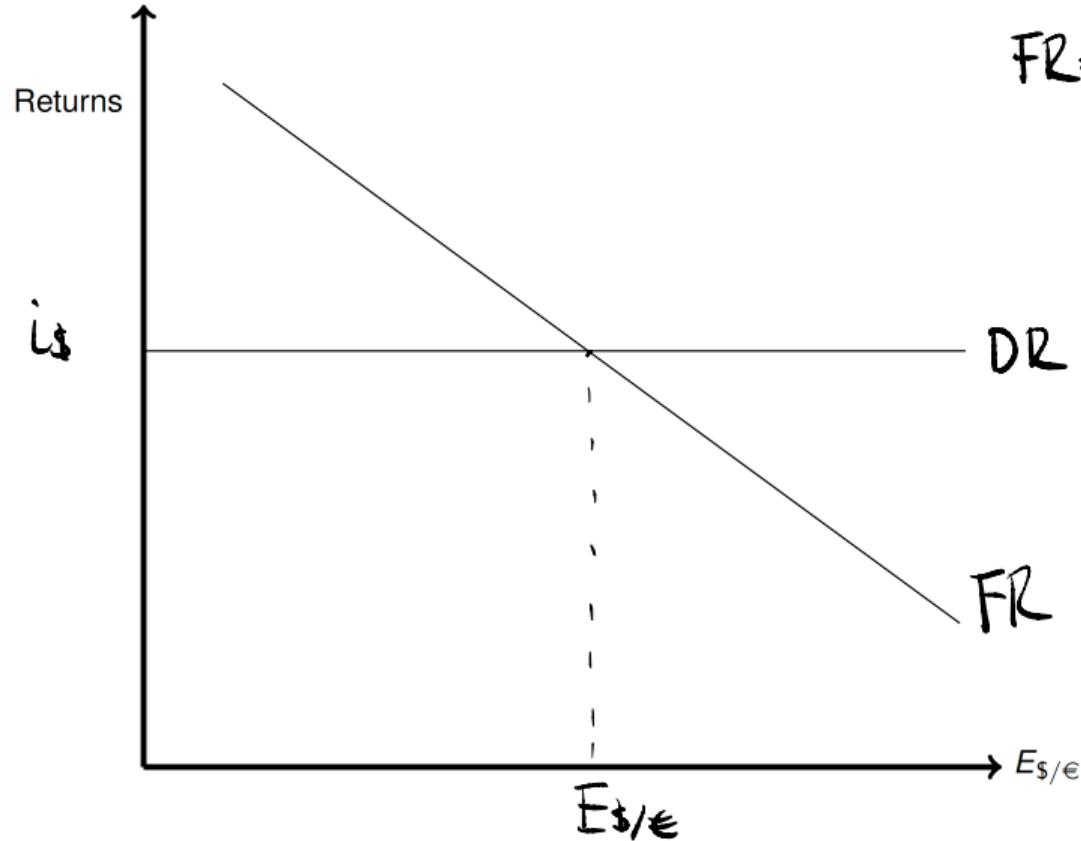
(notice we work here with the approximated UIP after taking logs. Conclusions are the same as with the first one)

- ▶ Left-hand side: return to investing in dollars (at home)
 - ▶ Right-hand side: return to investing in euros (abroad)
 - ▶ $\frac{E_{\$/\epsilon}^e}{E_{\$/\epsilon}} - 1 = d_{\$/\epsilon}^e \rightarrow$ Expected depreciation rate of the dollar
 - ▶ Known/given variables: $i_{\$}$, i_{ϵ} , $E_{\$/\epsilon}^e$
 - ▶ Unknown (to be solved for): $E_{\$/\epsilon}$ (Spot ER)

Plotting both sides of the UIP

Figure: Foreign and Domestic Returns (in UIP)

FX market



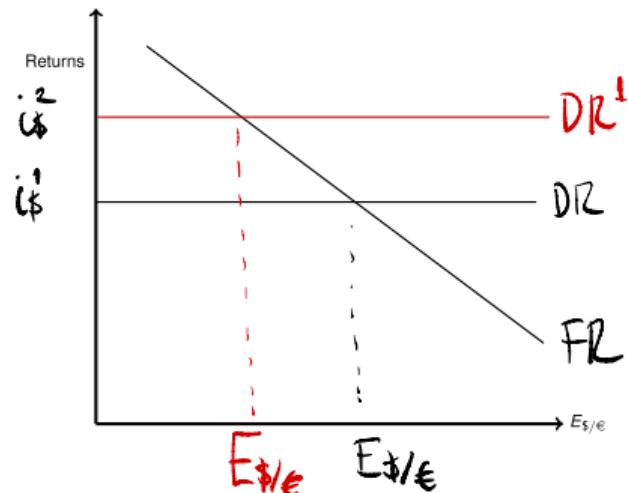
$$DR = i_{\$}$$
$$FR = i_{\epsilon} + \left(\frac{E_{\$/\epsilon}^e}{E_{\$/\epsilon}} - 1 \right)$$

Recap: UIP (cont.)

- ▶ Foreign Return (FR) curve: $FR = i_{\epsilon} + \left(\frac{E_{\$/\epsilon}^e}{E_{\$/\epsilon}} - 1 \right)$
- ▶ Domestic Return (DR) curve: $DR = i_{\$}$
- ▶ How do the curves shift and what happens to $E_{\$/\epsilon}$ when:
 - ▶ (i) $i_{\$}$ increases?, (ii) i_{ϵ} decreases?, (iii) $E_{\$/\epsilon}^e$ decreases?

Figure: Foreign and Domestic Returns: Increase in $i_{\$}$

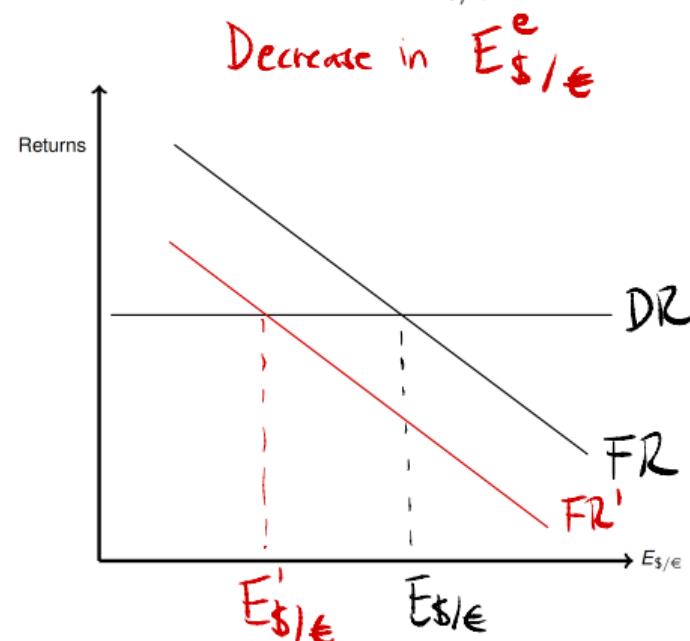
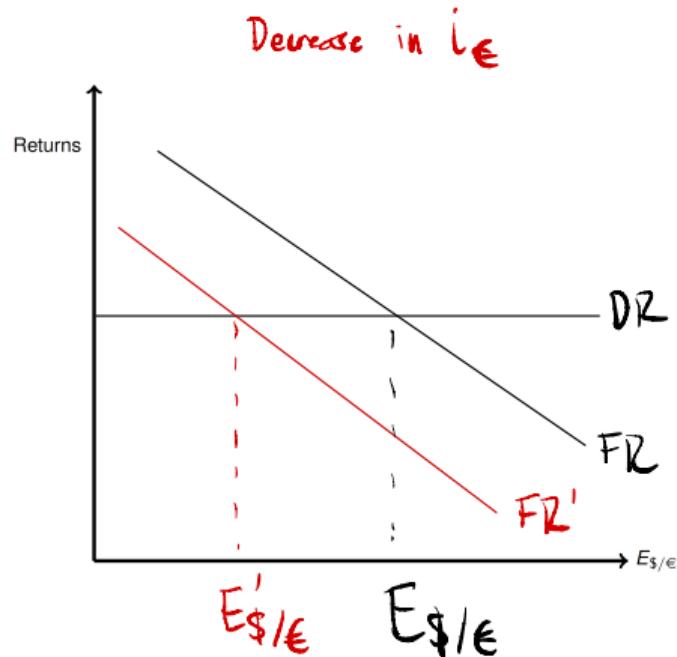
$$i_{\$}^1 \rightarrow i_{\$}^2 \quad (i_{\$}^2 > i_{\$}^1)$$



Recap: UIP (cont.)

$$DR = i_{\$/\text{€}}$$
$$FR = \underline{i_{\$/\text{€}}} + \left(\frac{E_{\$/\text{€}}^e}{E_{\$/\text{€}}} - 1 \right)$$

Figure: Foreign and Domestic Returns: Decrease in $i_{\$/\text{€}}$ (left), and decrease in $E_{\$/\text{€}}^e$ (right)



Determining the Spot Exchange Rate

UIP: given known $i_{\$}$, i_{ϵ} and $E_{\$/\epsilon}^e$ we can determine: $E_{\$/\epsilon}$

But where do $i_{\$}$, i_{ϵ} and $E_{\$/\epsilon}^e$ come from?

- ▶ $i_{\$}$, i_{ϵ} : come from Quantity Theory of Money in the Short Run
- ▶ $E_{\$/\epsilon}^e$: from the Quantity Theory and the PPP in the Long Run

This is why we analyze first the LR model and later the SR model

We solve for $E_{\$/\epsilon}^e$ first in the LR model and given that, we later get the $\boxed{\text{Spot ER } (E_{\$/\epsilon})}$

Short Run nominal interest rates

Assumptions:

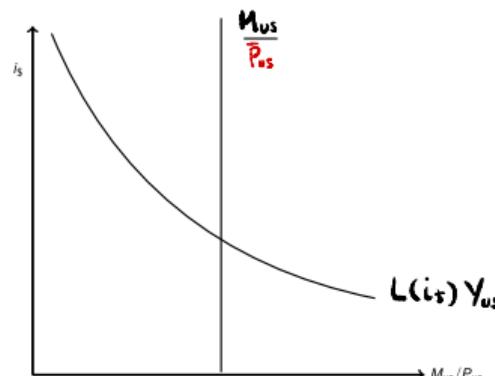
1. Prices level is fixed (sticky): $\bar{P}_{us}, \bar{P}_{eu}$
2. Nominal interest rate (i) adjusts to clear money market

Quantity Theory of Money with fixed prices:

$$\frac{M_{us}}{\bar{P}_{us}} = L(i_{us}) Y_{us} \quad \frac{M_{eu}}{\bar{P}_{eu}} = L(i_{eu}) Y_{eu}$$

Here we focus on the US, but analogous results hold for EU (or any other location)

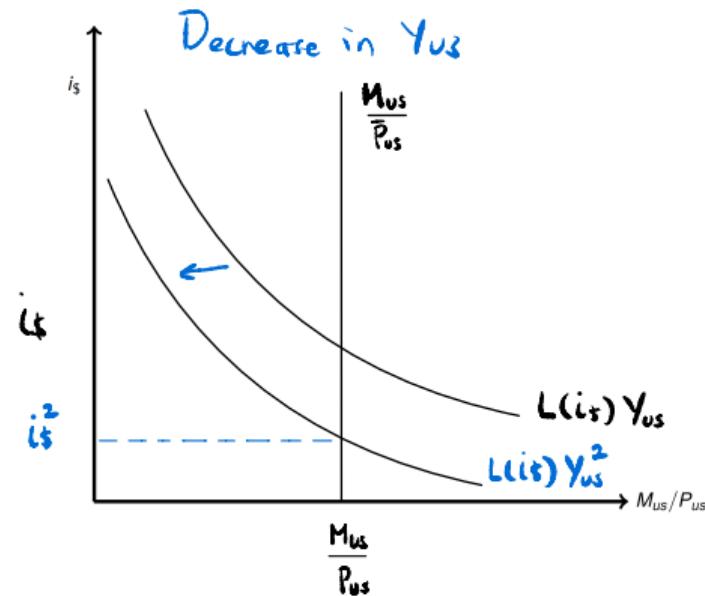
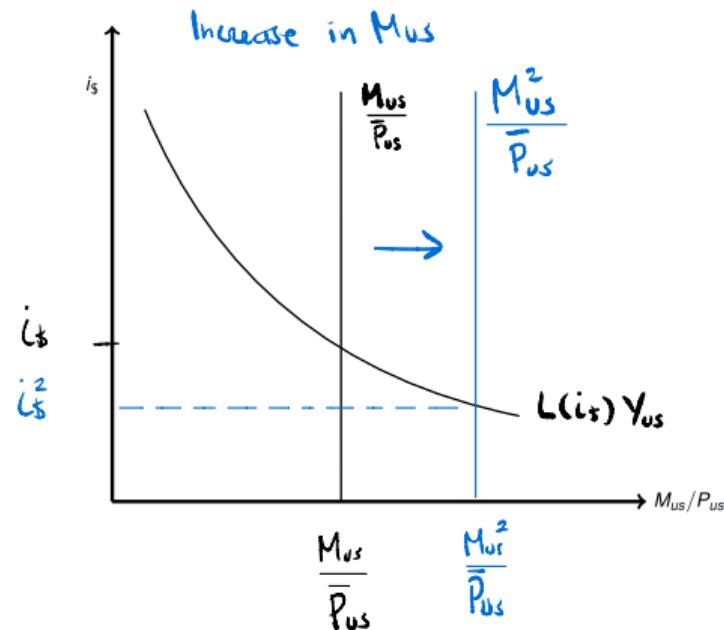
Figure: Home (US) money market



Home money market

How do the curves shift and what happens to $i_{\$}$ when: M_{us} increases? Y_{us} decreases?

Figure: Home (US) money market: Increase in M_{us} (left) and Decrease in Y_{us} (right)



Determining the Spot Exchange Rate (cont.)

UIP: given $i_{\$}$, i_{ϵ} and $E_{\$/\epsilon}^e$ —→ get $E_{\$/\epsilon}$

But where do $i_{\$}$, i_{ϵ} and $E_{\$/\epsilon}^e$ come from?

- ▶ $i_{\$}$, i_{ϵ} : come from Quantity Theory of Money in the Short Run (last slide)
- ▶ $E_{\$/\epsilon}^e$: from the Quantity Theory and the PPP in the Long Run

$$E_{\$/\epsilon}^e = \frac{P_h}{P_f}$$

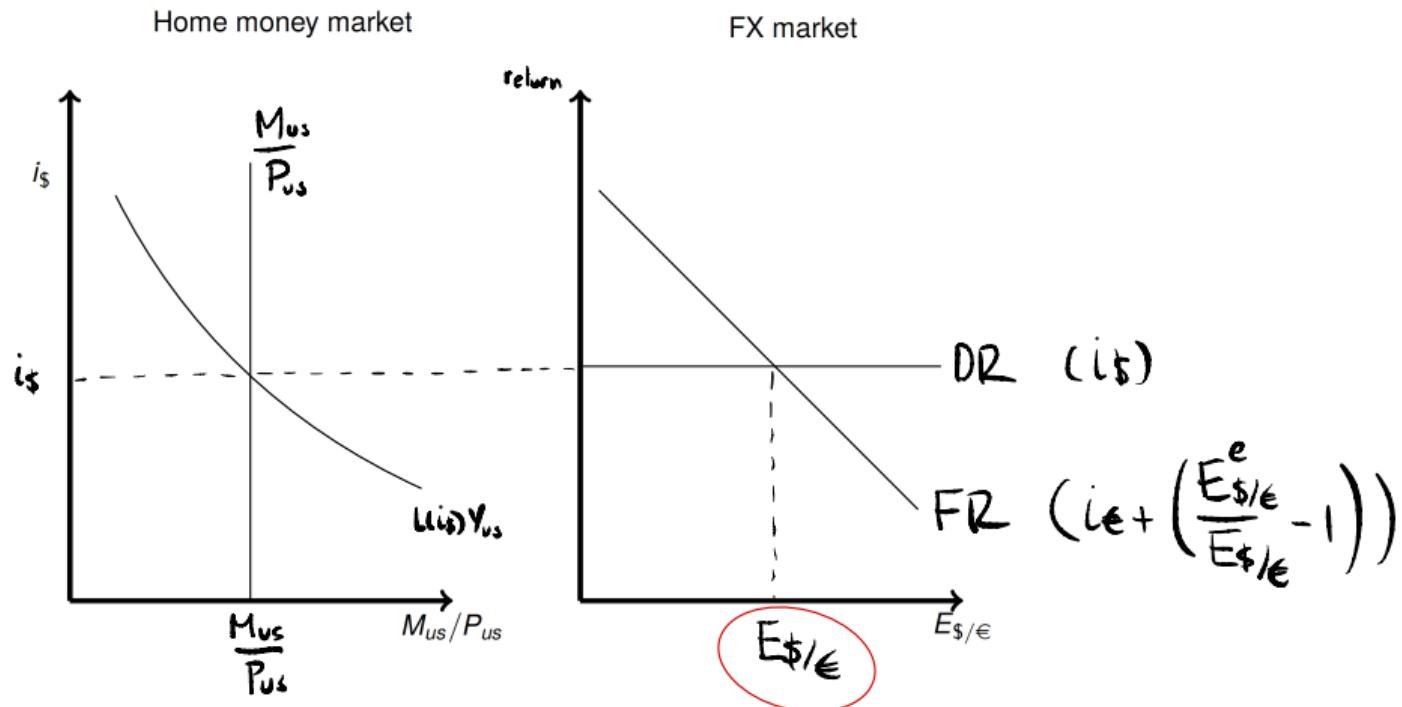
Now: Put together quantity theory and UIP in the short run.

(Short run analysis only in this step: Thus take $E_{\$/\epsilon}^e$ as given for now)

Short run part of the model

Markets in which $E_{\$/\epsilon}^e$ is taken as given (see how axes do not change with $E_{\$/\epsilon}^e$)

Figure: Joint determination of Interest rates and Spot ER



Determining the Spot Exchange Rate

The central bank in each economy determines M (Money Supply)

The equilibrium interest rate i will be such that real supply of money equals demand: $\frac{M}{P} = L(i)Y$

Via UIP: $i_{\$}$ and i_{ϵ} (and $E_{\$/\epsilon}^e$) determine the spot ER: $E_{\$/\epsilon}$

C_q in money mkt
determines i

What if M_{us} temporarily increases?

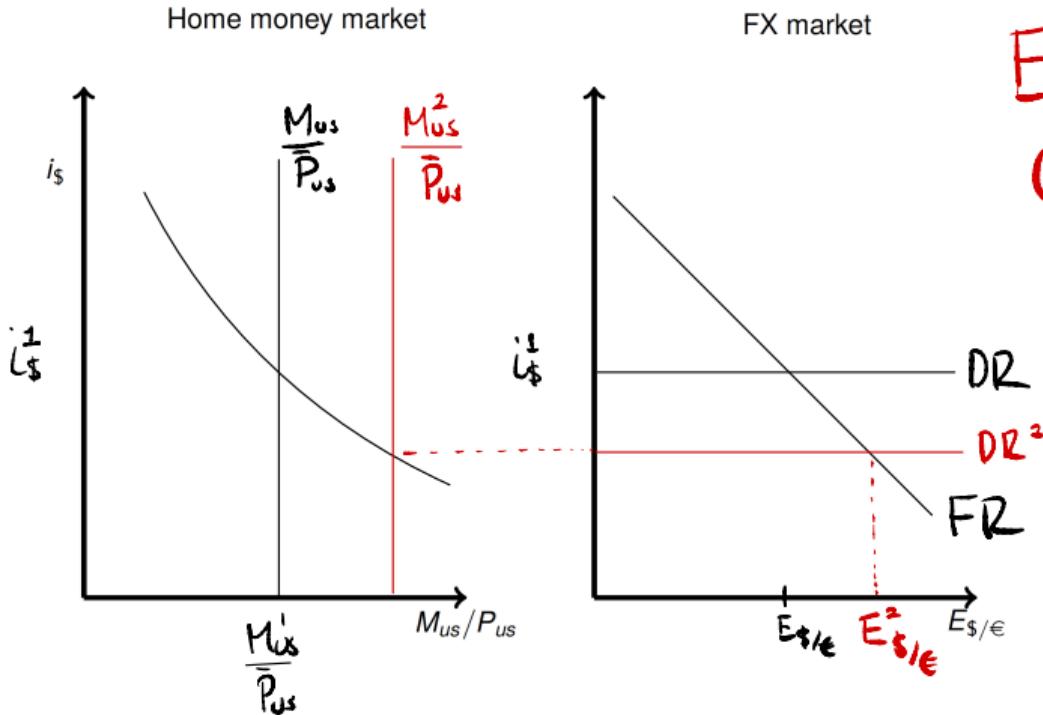
Can analyze the "temporary" increase case here because the expectations of future ER won't change (so we can keep taking expected ER as given)

If permanent (increase): we have to change $E_{\$/\epsilon}^e$ as well and the resulting spot ER will differ
(we check this case some slides ahead)

($E_{\$/\epsilon}^e$ does not change)

Temporary increase in home money supply (M_{us})

Figure: Joint determination of Interest rates and Spot ER



ER goes from $E_{\$/\epsilon}$ to $E_{\$/\epsilon}^2$ (Depreciation)

Determining the Spot Exchange Rate (cont.)

Temporary increase in M_{us} :

(Key) **temporary:** $E_{\$/\epsilon}^e$ does not change (expected future ER is the same)

$$\overline{M}, \overline{P} \Rightarrow \uparrow \frac{M}{\overline{P}}$$

1. Real money supply curve shifts (prices are fixed and M rises)
2. $i_{\$}$ lowers to new equilibrium $\downarrow i_{\$}$
3. DR curve shifts down $DR = i_{\$}$
4. Dollar depreciates (spot) $\uparrow E_{\$/\epsilon}$: from $E_{\$/\epsilon}^1$ to $E_{\$/\epsilon}^2$

Putting the Long Run and Short Run theories together

Outline

Exchange rates in the long run

- ▶ Flexible prices
- ▶ PPP and UIP hold
- ▶ Quantity theory of money (with P)
- ▶ $i_h = r^* + \pi_h$ (Fisher)
- ▶ Exchange rate determined by prices/inflation (we use this block to get expected future ER)

$$E_{h/f}^e = P_h/P_f$$

Exchange Rates in the short run

- ▶ Fixed prices (sticky) $\rightarrow \bar{P}$
- ▶ Long-run depreciation is given (exogenous)
- ▶ ~~UIP holds, PPP does not~~
- ▶ Quantity theory of money (with \bar{P})
- ▶ i determined by $\frac{M}{\bar{P}}$ and $L(i)Y$
- ▶ Exchange rate determined by interest rates (we use this block to get Spot ER)

$$i_s - i_t = \frac{\partial \$/e}{T}$$

$$\frac{E_{\$/e}^e}{E_{t/e}} - 1$$

Integrated approach (SR and LR)

Now we integrate the long-run (LR) and short-run (SR) models

- ▶ LR model (PPP) pins down expectations ($E_{\$/\epsilon}^e$)
- ▶ Short-run model takes expectations from LR model and pins down Spot ER (with UIP gets $E_{\$/\epsilon}$)

With a model that also includes the LR we can think about permanent changes in the variables

Before we could only check temporary ones with the SR model only

In a nutshell:

SR Model: $E_{h/f}^e$ Fixed

SR and LR Model: $E_{h/f}^e$ can change

↳ ^{can analyze}
Permanent Policies

Short-run model

UIP:

$$i_{\$} = i_{\epsilon} + \left(\frac{E_{\$/\epsilon}^e}{E_{\$/\epsilon}} - 1 \right)$$

Quantity theory with theory with sticky prices (\bar{P}):

$$\bar{P}_{us} = \frac{M_{us}}{L_{us}(i_{\$})} Y_{us} \quad \bar{P}_{eu} = \frac{M_{eu}}{L_{eu}(i_{\epsilon})} Y_{eu}$$

$E_{\$/\epsilon}^e$ is given (in reality comes from LR model but from SR perspective is just exogenous)

Solution given inputs above:

i comes from money market equilibrium, $E_{\$/\epsilon}$ is obtained from FX market equilibrium

$\hookrightarrow i_{\$}$
 i_{ϵ}

$\hookrightarrow E_{\$/\epsilon}$

Long-run model

$$E_{\$/\epsilon}^e = \frac{P_{us}^e}{P_{eu}^e}$$

Purchasing power parity (PPP):

$$E_{\$/\epsilon}^e = \frac{P_{us}^e}{P_{eu}^e}$$

Quantity theory with flexible prices: (i.e. with P instead of \bar{P})

$$P_{us} = \frac{M_{us}}{L_{us}(i_{\$})} Y_{us}$$

$$P_{eu} = \frac{M_{eu}}{L_{eu}(i_{\epsilon})} Y_{eu}$$

Model is set in terms of expected future variables

(if it holds today, we can just think of the whole thing in terms of expectations)

From this model we get: $E_{\$/\epsilon}^e$



Permanent change in M_{us}

Short-run model: $E_{\$/\epsilon}^e$ had to be fixed. Then it only could describe temporary shocks

A permanent shock would change $E_{\$/\epsilon}^e$

Now: with LR and SR → Can study permanent shocks

Example: money grows permanently in the US to a new level (from M_{us}^1 to M_{us}^2)

We solve this model "backwards":

1. We solve the long-run → getting $E_{\$/\epsilon}^e$
2. We solve the short-run with the new value of $E_{\$/\epsilon}^e$ and with constant prices

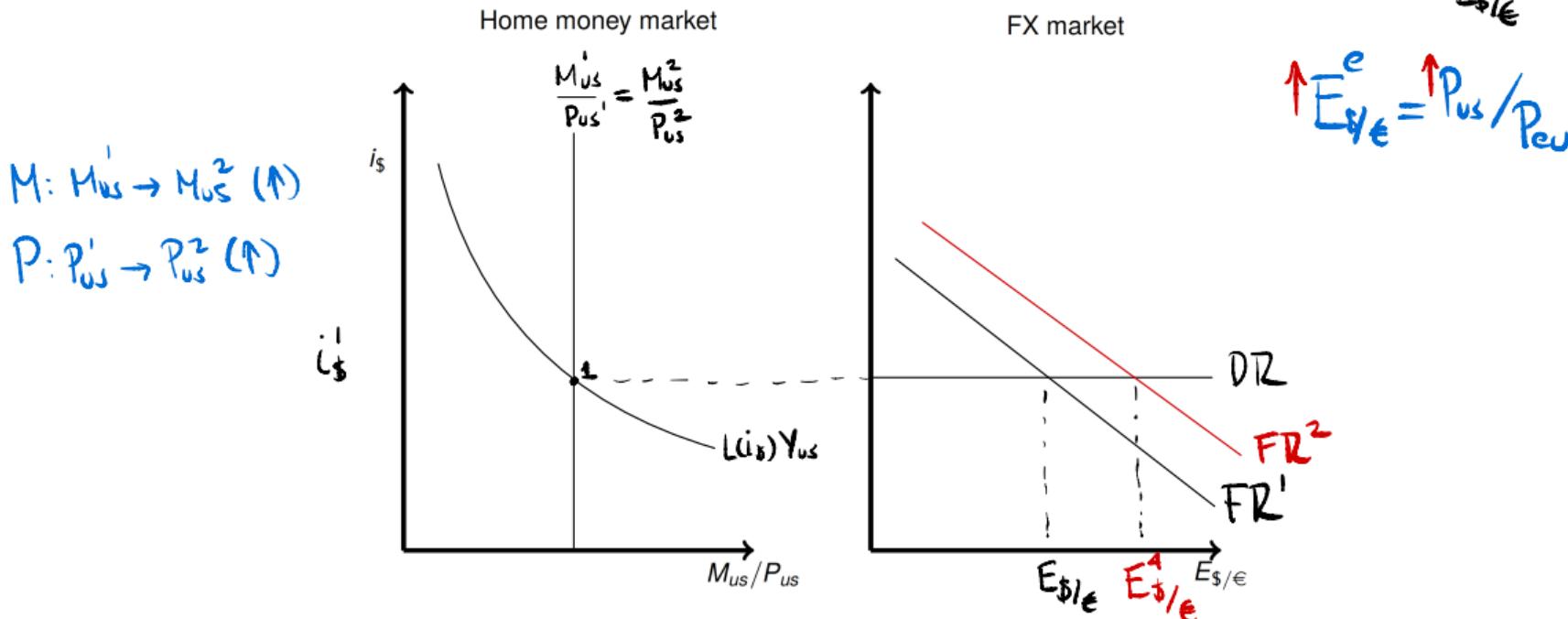
After the second step we get the new interest rate ($i_{\$}$) and the new spot ER ($E_{\$/\epsilon}$)

Once we get everything we work out the adjustment from short-run values to the long-run

Permanent increase in home money supply (M_{us})

Figure: Long-run (permanent increase in money supply)

$$FR: i \leftarrow \frac{E_{\$/\epsilon}^e}{E_{\$/\epsilon}} - 1$$



Equilibrium interest rate is the same (in the LR), but notice the Spot ER is different (USD depreciates)

Permanent change in M_{us}

1. We solve the long-run \rightarrow getting $E_{\$/\epsilon}^e$

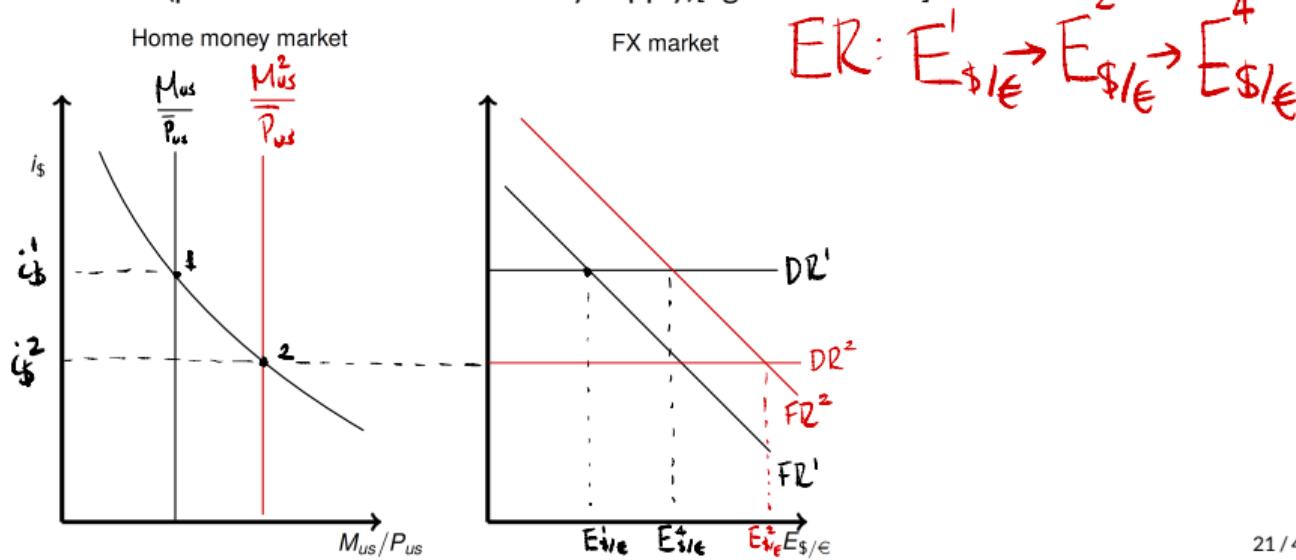
Done! the LR Exchange Rate goes from $E_{\$/\epsilon}^1$ to $E_{\$/\epsilon}^4$ (increased)

The money market won't change (because P adjusted to change in M).

However, FR curve shifts permanently and the ER is permanently depreciated

2. Now: We solve the short-run with the new value of $E_{\$/\epsilon}^e$ and with constant prices

Figure: Short-run (permanent increase in money supply)[fig. 15-12 in FT]



Permanent change in M_{us} (cont.)

1. We solve the long-run → getting $E_{\$/\epsilon}^e$

Done! the LR Exchange Rate goes from $E_{\$/\epsilon}^1$ to $E_{\$/\epsilon}^4$ (increased)

The money market won't change (because P adjusted to change in M). ($\frac{M}{P}$ stays the same in the LR)

However, FR curve shifts permanently and the ER is permanently depreciated

In LR: ER is $E_{\$/\epsilon}^4$ (\uparrow)

2. Then, we solve the short-run with the new value of $E_{\$/\epsilon}^e$ and with constant prices

Done! In the short run:

- FR shifts up as in the long-run

- interest rates fall because real money supply increases $\uparrow \frac{M_{us}}{P_{us}} \rightarrow SR \text{ decrease in } i_{\$}$

Short-run ER depreciates to $E_{\$/\epsilon}^2 \rightarrow$ a larger depreciation than will be seen in the LR: $E_{\$/\epsilon}^2 > E_{\$/\epsilon}^4$

We then say the short-run ER "overshoots" the long-run ER

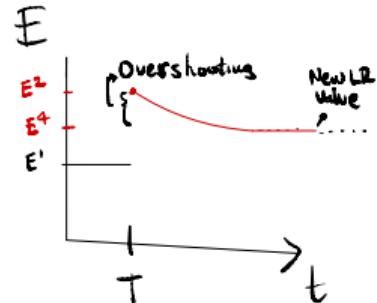
i.e., it instantly overreacts in the same expected direction and later converges to the new long-run equilibrium

↳ overshooting

Adjustment from SR to LR

The economy eventually adjust from the SR to the LR:

- ▶ As P slowly changes $\rightarrow \frac{M}{P}$ falls until it returns to its initial (and long-run) level
- ▶ As $\frac{M}{P}$ falls, i increases until it is back to its initial level
- ▶ FR curve does not return to its original position: there has been a permanent change in expected inflation (and then in LR depreciation) because the increase in money supply is permanent
 - ↳ PPP: P goes up to a new permanent level P^2
 - ▶ The ER eventually appreciates to $E_{\$/\epsilon}^4$

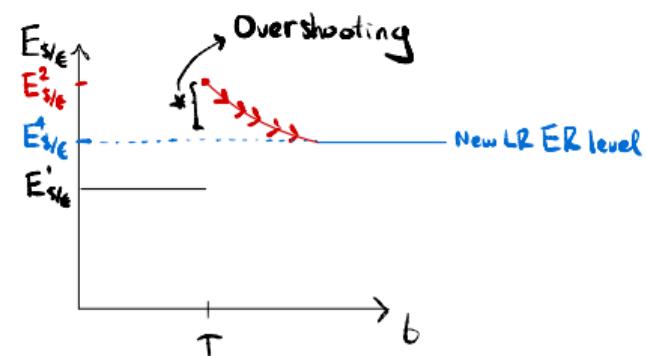
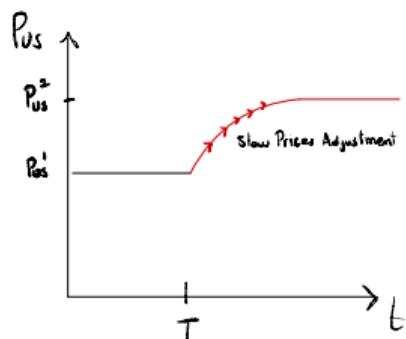
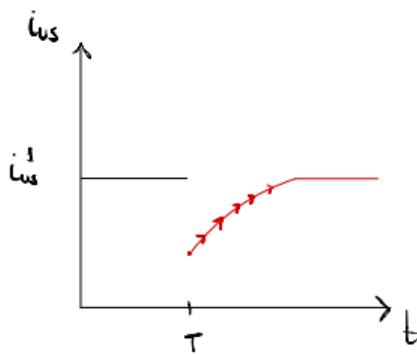
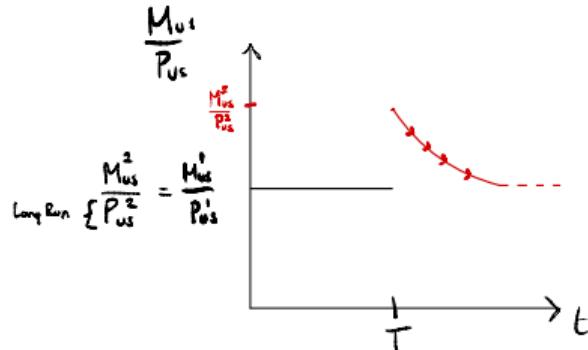
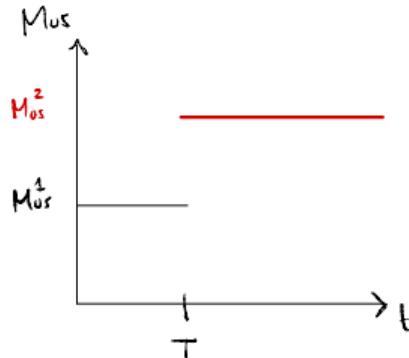


Notice the "appreciates" of the last point. How is this possible? wasn't the ER supposed to depreciate with the increase in money supply?

Well, in the SR the ER overreacts and depreciates too much (**overshooting**) ... from there the ER has to gradually lower (appreciate) to its new LR value (which is higher than the ER before the money change)

We can see the trajectory of these variables over time in the next slide

Permanent increase in M_{us} : Path of variables over time



Overshooting

- ▶ Key to overshooting: change in expectations
 - ▶ Expectations change because the change in money supply (M) is permanent
 - ▶ With a temporary change, the only change in the FX market is $i_{\$}$... (DR curve)
 - ▶ In contrast, with a permanent change the shift of FR provides the extra depreciation in the SR
- eventually P increases
(Permanently)

Why did the FR shifted? because of the increase in the expected (future) ER

Reminder:

$$FR = i_{\epsilon} + \left(\frac{E^e_{\$/\epsilon}}{E^e_{\$/\epsilon}} \right) - 1$$

Via PPP: $E^e_{\$/\epsilon} = \frac{P^e_{us}}{P^e_{eu}}$

Summary

- ▶ Long Run model: can handle permanent changes
- ▶ Short Run model: can handle temporary changes
- ▶ LR and SR models together: allows us to study the effect of permanent shocks (in the short run)

- ▶ What is new: the long run model lets people forecast the future ER
 - ▶ In the SR this makes FR shift → prompting a larger depreciation of the USD.
- ▶ In the SR: the exchange rate **overshoots** its new LR level (over reacts in the same direction of the LR change)
- ▶ Monetary policies (and shocks) that are expected to last longer create more volatility in the ER

The Trilemma and the Fixed Exchange Regime

Outline

- (Recap of) the Floating Exchange Rate regime
- the Fixed Exchange Rate regime model
- The Trilemma (or impossible trinity in -international- economics)

Examples

Floating Exchange Rate regimes

Focus so far: floating exchange rate regimes with capital mobility (UIP holds)

$$i_h = i_f + d_{h/f}^e$$

Short run: central bank chooses M (money supply) $\Rightarrow i$ and $E_{h/f}$ determined via UIP (in the FX market)

$$M_h \rightarrow \frac{M_h}{\bar{P}_h} \rightarrow i_h \quad \Rightarrow \quad i_h = i_f + \frac{E_{h/f}^e}{E_{h/f}} - 1$$

(we get spot rate from here because money market determines i_h , and i_f and the expected ER are taken as given)

Long run: central bank chooses M which determines P (flexible) $\Rightarrow E_{h/f}$, i determined by PPP + Fisher:

(from quant. theory):

$$P_h = M_h / (L(i_h) Y_h)$$

(in PPP):

$$E_{h/f} = P_h / P_f$$

(in Fisher eq.):

$$i_h = \pi_h^e + r^*$$

Now: Fixed Exchange Rate regimes

Fixed exchange rate regime: set ER at a Fixed level

Central bank chooses an exchange level $\bar{E}_{h/f}$ (e.g., $\bar{E}_{dk/\epsilon} = 1$)

Why? to implement a nominal anchor: "Imports" inflation of f country

Assumption: capital moves freely across borders → **international capital mobility**

What changes?

Economy compromises its monetary policy to maintain ER peg (in every horizon: LR, SR)

Must have this

for UIP to work

Fixed exchange rate regimes in the Short Run

A fixed exchange rate (+ capital mobility) determines the interest rate

Fixed \rightarrow ER does not change: $\bar{E}_{h/f} = \bar{E}_{h/f}^e$, then : Peg (Fixed ER Regime)

$$i_h = i_f + \left(\frac{\bar{E}_{h/f}^e}{\bar{E}_{h/f}} - 1 \right) \xrightarrow{0} \Rightarrow i_h = i_f$$

Home loses control of i_h as it now follows i_f (controlled by a foreign country)

What about money supply at home? \rightarrow the same:

$$M_h = \bar{P}_h L(i_f) Y_h$$

Controlled now by 'f' country

Money supply now only depends on foreign variables (i_f) (or on variables that are not changing)

Takeaway: with a fixed ER the central bank sets M_h at the level that keeps $i_h = i_f$ (it has no other choice)

Fixed exchange rate regimes in the Long Run

Central bank chooses an exchange rate level $\bar{E}_{h/f}$

P_h still determined via PPP:

$$P_h = \frac{\bar{E}_{h/f}}{P_f}$$

But exchange rate is fixed (at $\bar{E}_{h/f}$) and foreign prices are determined abroad (P_f).

Then, in the LR home prices P_h are also completely determined in the foreign country (f)
(or by foreign factors, no matter what happens at home)

(By UIP) $i_h = i_f$ and money supply is:

$$M_h = P_h L(i_f) Y_h$$

$$M_h = \frac{\bar{E}_{h/f}}{P_f} L(i_f) Y_h$$

In LR determined by 'f' country

Again, in the LR the money supply is stuck at the level dictated by the variables of other countries
(no policy choice)

Recap

Flexible exchange rates

- ▶ Central bank chooses M_h
- ▶ Long Run: policy choice determines P_h and $E_{h/f}$ (PPP)
- ▶ Short Run: policy determines i_h and spot rate $E_{h/f}$ (sticky prices and UIP)

Fixed exchange rates

- ▶ Central bank chooses peg $\bar{E}_{h/f}$ (commits to maintain ER at such level)
- ▶ Long Run: P_h and M_h must ensure that $i_h = i_f$ (CSR)
- ▶ Short Run: M_h must ensure $i_h = i_f$ (CSR)

Then, central bank's policies are compromised to ensure the peg holds ($E_{h/f} = \bar{E}_{h/f}$ or $i_h = i_f$)

That is, we get a loss of monetary policy autonomy in both the short and long run

The Open Economy Trilemma

Also called "Impossible Trinity" (of international economics) or Mundellian trilemma

Out of these 3, can pick at most 2:

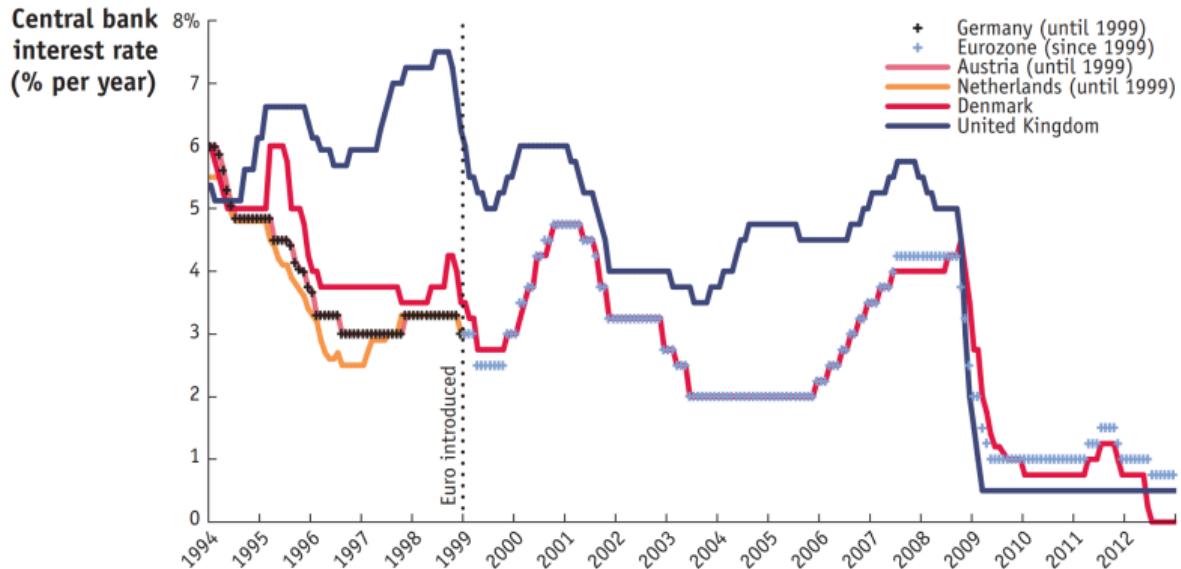
1. Fixed Exchange Rate
2. International capital mobility (UIP holds)
- + 3. Monetary policy independence (allowing $i_h \neq i_f$)

Examples:

1. Fixed ER + capital mobility: UK in the 1990s, Denmark today
2. Fixed ER + monetary policy autonomy: China today
3. Capital mobility + monetary policy: USA today

Example: the trilemma in Europe

Figure: Central Banks' interest rates (1994-2012)



Two different regimes in action:

UK: float against the German mark (and then vs. the Euro) → interest rate can change independently

Denmark: peg krone to the mark (and then to Euro) → interest rate decided for them in Germany(ECB)

Example: UK in 1992

Fixed exchange rate & free movement of capital \implies No monetary policy independence:

UK and Germany had a fixed exchange rate as part of a system of European Fixed rates (the ERM I)

Germany wants to increase interest rate to fight inflation

That means UK must adopt higher interest rates to defend the peg (UIP: $i_{gr} = i_{uk}$)

But with a weak UK economy \rightarrow high interest rates are not desirable

This lowers UK credibility (of its compromise with peg) and invites speculation on its currency

$\uparrow i_{uk}$ $\downarrow \text{Eur GE}$

BoE can: (i) \uparrow interest rates, (ii) devalue currency or (iii) intervene in FX mkt & use reserves to prevent devaluation
(let $i_{uk} < i_{gr}$ and make up shortage of German marks)

Speculative attack: Given costs of (i), (iii) investors speculate that BoE would rather devalue the pound
they borrow in pounds and sell pounds for marks massively

BoE must act by increasing rates, draining reserves, or devalue (no way out)

UK in 1992 (cont.)

Black Wednesday: September 16, 1992

UK raises interest rates from 10% to 12% and promises to raise rate to 15% later that day

This does not stop speculators from selling pounds → Government abandons Fixed ER regime

A likely self-fulfilling crisis: Fixed ER may have held if not attacked

("attacked": speculative private agents trading against the currency in flocks)

Figure: Black Wednesday (20% devaluation)



China, today

Fixed rate + independent monetary policy \Rightarrow No free movement of capital

China fixes ER against dollar: yuan appears stable and undervalued vs. what the floating ER would be

PBC can change its monetary policy

can raise (lower) interest rates to lower inflation (raise output)

capital controls keep UIP from forcing ER rate to change

(even if there are arbitrage opportunities, agents can't use them)

Costs of capital controls:

- ▶ hinders efficient use of capital (limits financial development)
- ▶ overvaluation can lead to black market for currency
- ▶ can discourage foreign investment

In principle, may be affecting economic growth (by hindering investment)

United States, today

Capital mobility + independent monetary policy → floating exchange rate

Federal Reserve's mandate (what they commit to do)



- ▶ low and stable inflation
 - ▶ maximum sustainable employment
- ⇒ no rule/constraint regarding ER

Monetary policy based on domestic conditions (feasible, as mon. pol. is independent to that of foreign countries)

Free movement of capital (into/out of country)

Changes in interest rates → changes in expectations → changes in ER

Exchange rates in these countries

Exchange rate variation (1999 - 2014)

	Floating rates			Fixed rates		
	euro-usd	yen-usd	pound-usd	yuan-usd	hkd-usd	dk-usd
mean	0.84	105.12	0.61	7.50	7.78	7.45
st. dev.	0.14	14.48	0.06	0.84	0.02	0.01
var. coef.	0.17	0.14	0.10	0.11	0.003	0.001

Volatility: More variation in floating exchange rates

At times, maintaining peg is hard and a new (more sustainable) peg has to be defined

The trilemma: overview

The Trilemma: **Impossible to have all three of**

1. Fixed Exchange Rate (or very stable ER)
2. International Capital Mobility
3. Independent Monetary Policy

Benefits of a Fixed ER:

- ▶ Serves as nominal anchor (e.g., to stabilize inflation by setting it at the level of the foreign country)
- ▶ Facilitates cross-border trade and investment (stable international prices of goods and assets)

Costs of a Fixed ER:

- ▶ Sacrifice of monetary policy or capital mobility
- ▶ Subject to speculative attacks (hard to maintain)