

# **Topic 1: Course Overview and Introduction**

## **Part 1: Macroeconomic data facts**

- ✓ 1. Course Logistics (syllabus and lectures plan)
- 2. Please note HW0 on course website
- 3. Basic Business Cycle Facts
- 4. A Brief History of Modern Business Cycle Theory

## About me: Camilo Granados

- Assistant Professor of Economics – UT Dallas, EPPS
- Background: Ph.D. in Economics (U. Washington, Seattle), B.S. and M.S. Economics and Postgraduate Diploma in Statistics (U. Nacional, Colombia)
- Born in Colombia
- Worked in a Central Bank for 13 years, including a leave for the Ph.D.
  - Economist, Researcher
- Teaching experience:
  - UTD: international finance
  - UW: advanced macro (this course thrice), international finance, business finance, introduction to macroeconomics, MBA microeconomics, elements of statistics
  - Before the PhD: Advanced Econometrics, Advanced Microeconomics, Game Theory, Principles of Economics.

## General Teaching Philosophy

- Train students how to think about economics
- Ultimately, it is not just what you know but also how you think - synthesize and process information - that matters
- Lectures won't follow textbooks exactly; they draw out important concepts from some books and rely on study notes.
- Lecture slides available ahead of lecture to facilitate note-taking.
  - My advice: download them and take notes on top during class
- Slides with annotations are posted AFTER lecture
- Aim for more interaction - please "raise hands"

## Requirements:

See Syllabus (read it closely, It contains our “playing rules” and I will assume it is common knowledge to everyone)

( + Modern Macro by Sanjay Chugh) } Not Required

**Textbook:** Romer, Advanced Macroeconomics, 5ed., McGraw Hill

(we'll use it for some end of chapter problems but you can do the whole course with the slides and study notes only)

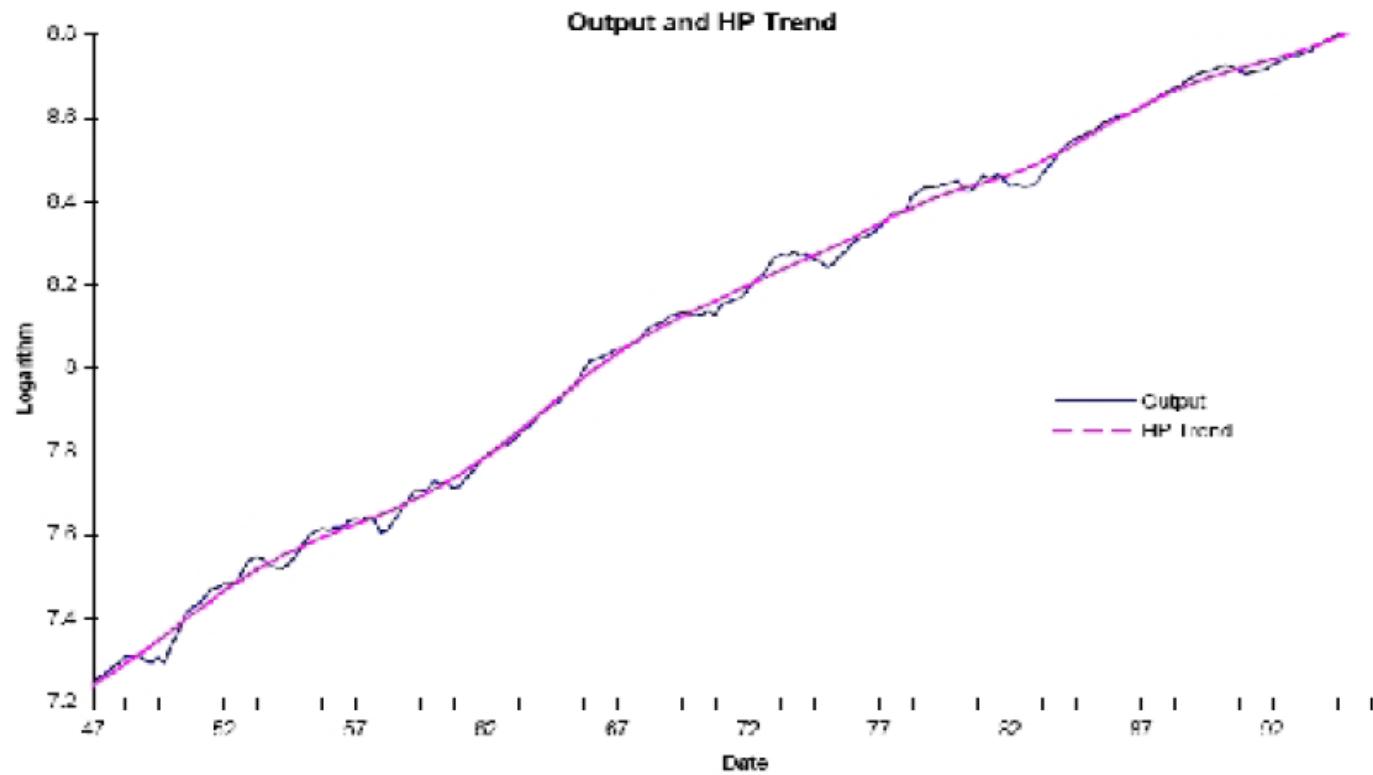
This course is not easy: heavy on math

Given that, I try to help:

- Most of the grading weight is put on take-home assignments rather than in-lecture tests (only one test in the classroom)
- The heavy lifting is put on the homework and practical projects
- If I see effort I am happy to adjust the grading weights along the way

# Some Business Cycle Facts (for the U.S. 1947:1 – 1996:4)

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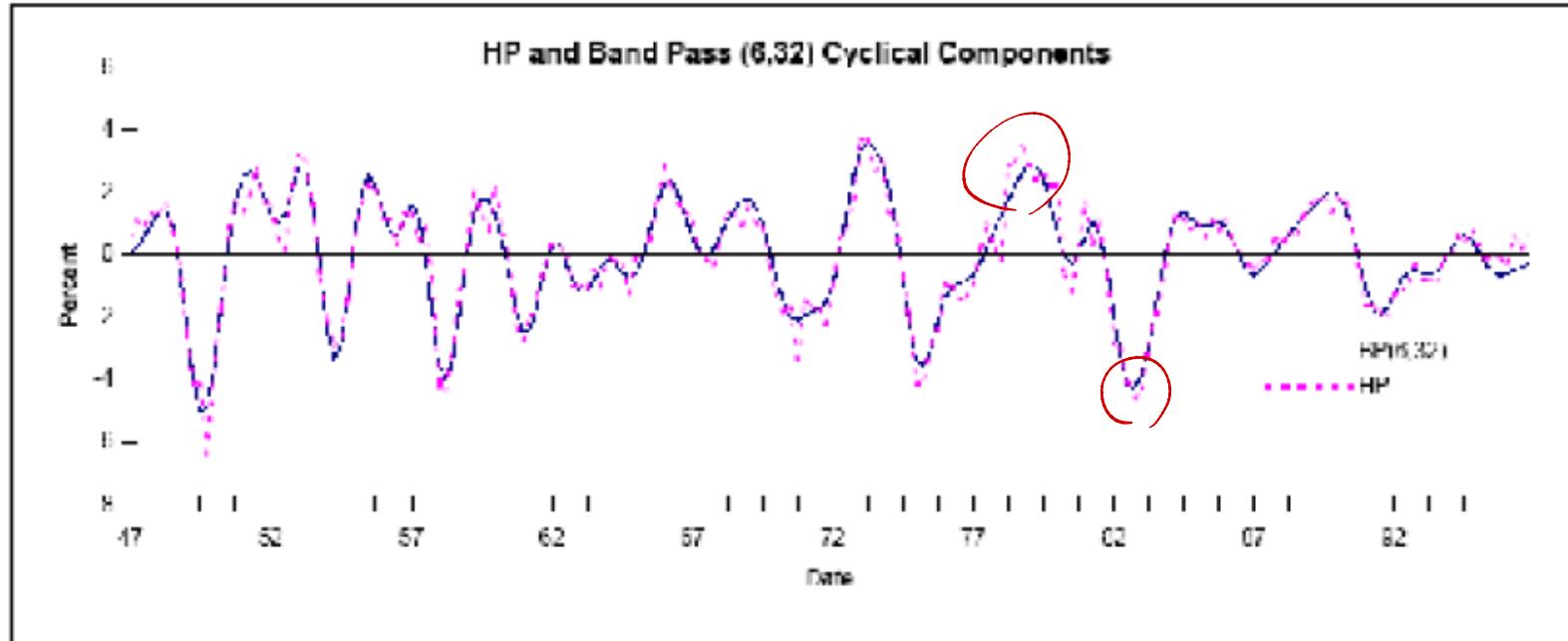
Decompose "Trend" vs. "Cycles" in a time series

$$y_t = y_t^T + y_t^C \text{ (e.g., with filters)}$$

$$GDP_t = GDP_t^{\text{Trend}} + \underbrace{GDP_t^{\text{Cycle}}}_{\text{b}} \rightarrow \text{wiggle or fluctuations around trend}$$

$$y_t - \hat{y}_t^{\text{trend}} = y_t^{\text{Cyc}}$$

↳ Hodrick-Prescott filter  
 ↳ Band Pass ; Christiano-Fitzgerald



Common filters: linear, Hodrick-Prescott (HP), Bandpass

Intuitively: a way to extract the long-run growth portion or the “low frequency” components of the data

for HW1 → hpfilter.m  
 Parameters:  $\lambda = 1600$

## Business Cycle Dating

NBER

(business Cycles dating)

↳ are we  
in a recession?

high  
Variance

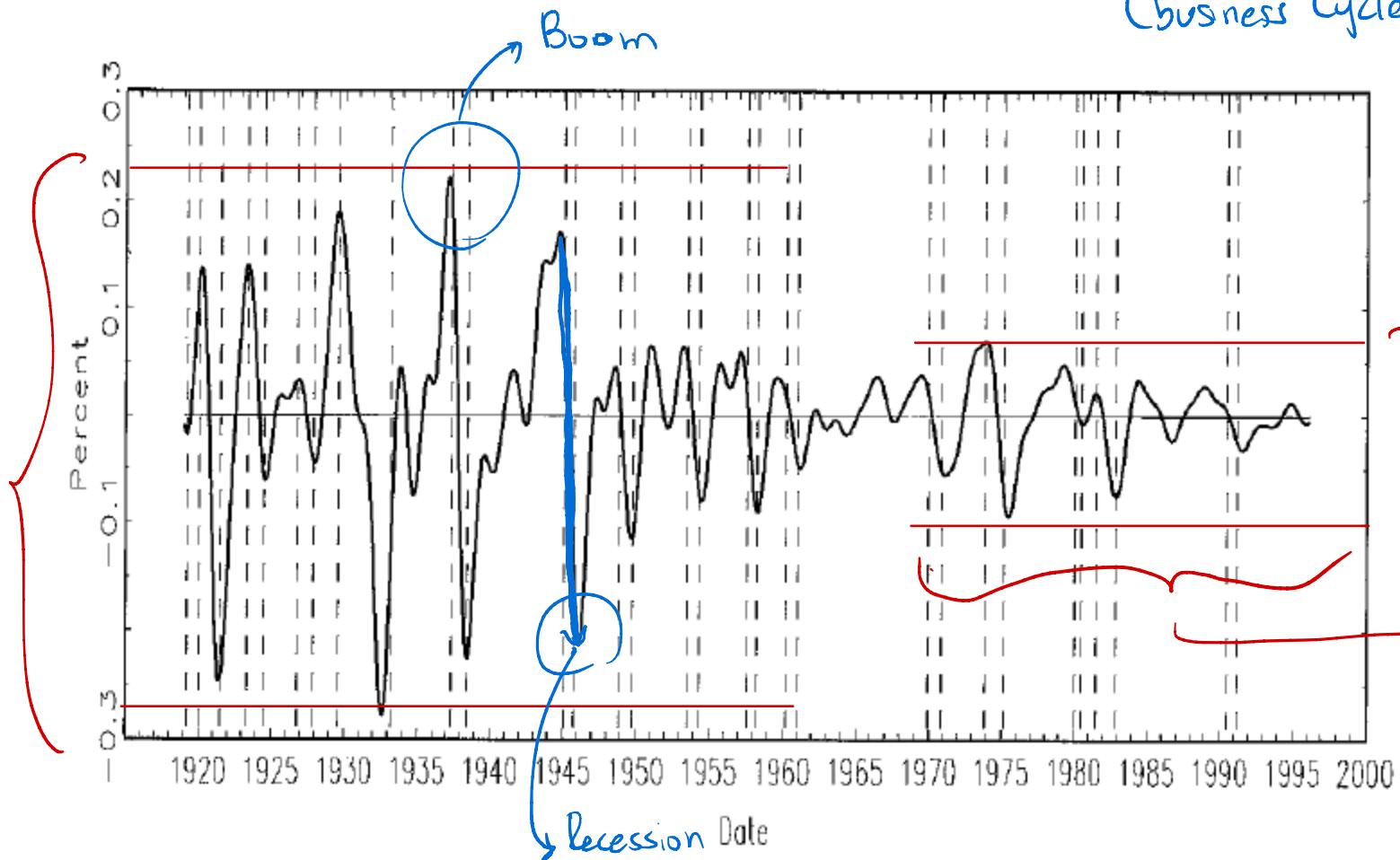


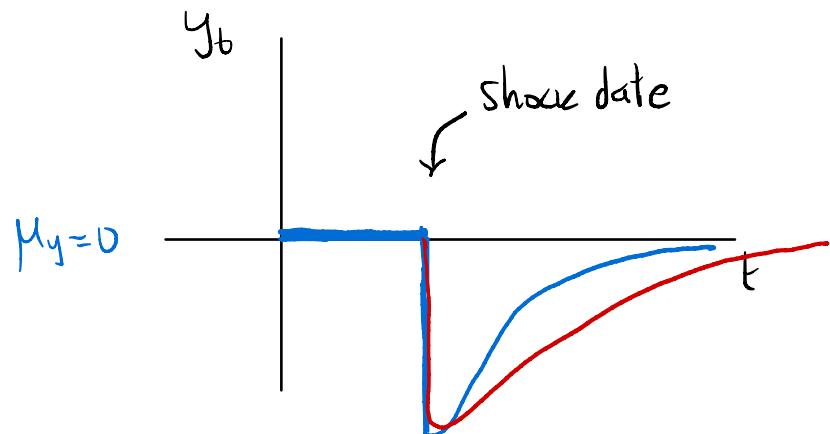
Fig. 1.2. Business cycle component of industrial production index.

# Some Stylized Facts about the U.S. Business Cycles:

What do we look for?

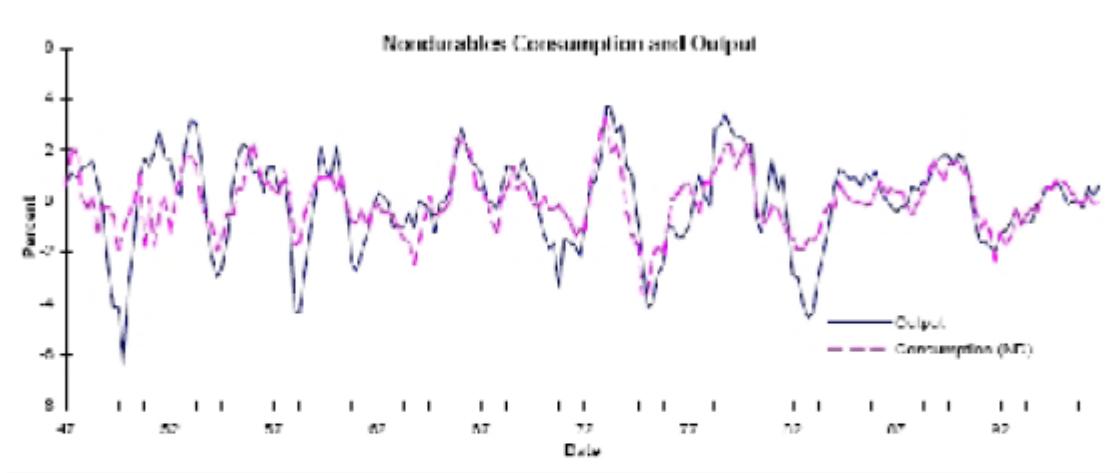
1. Volatility/amplitude of fluctuations → Variance of cycle  
(Standard deviation)
2. Comovements → Covariances & Correlations w/ other macro variables
3. Persistence/lead and lag patterns → Autoregressive pattern

$$\text{AR process: } Y_t = \mu_y + \alpha Y_{t-1} + \epsilon_t$$



$$Y_t = C_t + I_t + G_t + \cancel{N X_t}^{\circ \text{ (Closed economy)}}$$

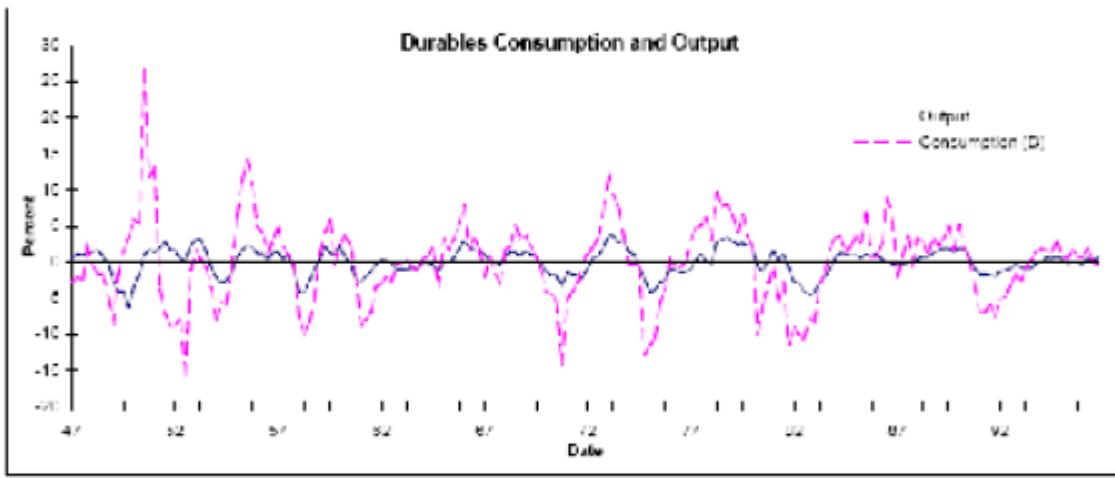
↴ Non durable      **Nondurable consumption**  
 ↴ durable



$$\sigma_{C, \text{nondurable}} < \sigma_y$$

\* Less volatile than output

# Consumer durables



$\sigma_{C, \text{non durable}} < \sigma_y$

$\sigma_{C, \text{durables}} > \sigma_y$

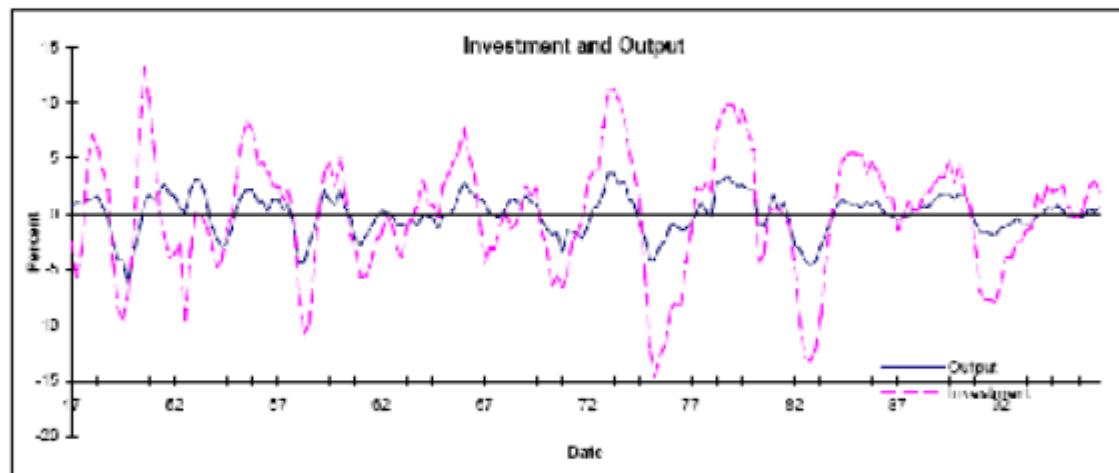
\* More volatile than output

$$\sigma_{C,\text{non-durable}} < \sigma_y$$

$$\sigma_{C,\text{durables}} > \sigma_y$$

$$\sigma_I > \sigma_y$$

## Investment

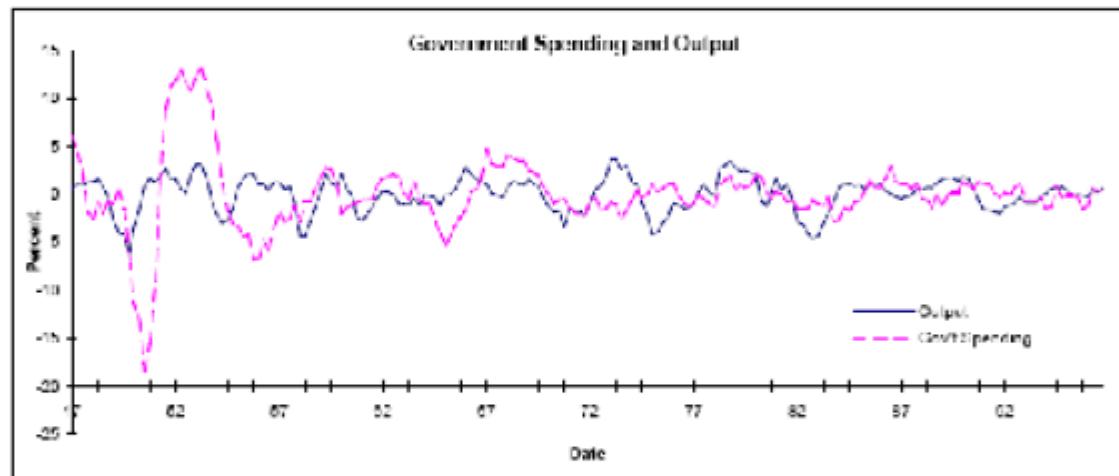


\* 3 times more volatile than output

$$Y_t = C_t + I_t + G_t$$

## Government expenditures

$$\begin{aligned} \sigma_{C, \text{nondurable}} &< \sigma_y \\ \sigma_{C, \text{durables}} &> \sigma_y \\ \sigma_I &> \sigma_y \\ \sigma_G &< \sigma_y \end{aligned}$$

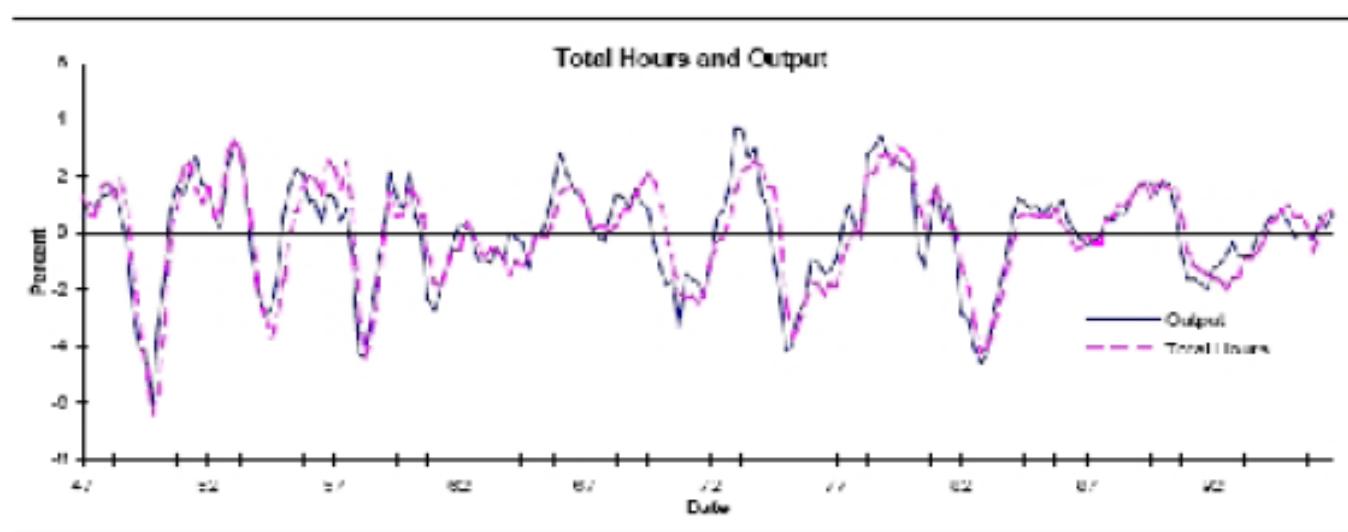


\* Less volatile than output

## Total hours worked

$$( N \times \text{hrs per worker} )$$

Number of workers



$$\sigma_{\text{Total hours}} \approx \sigma_y$$

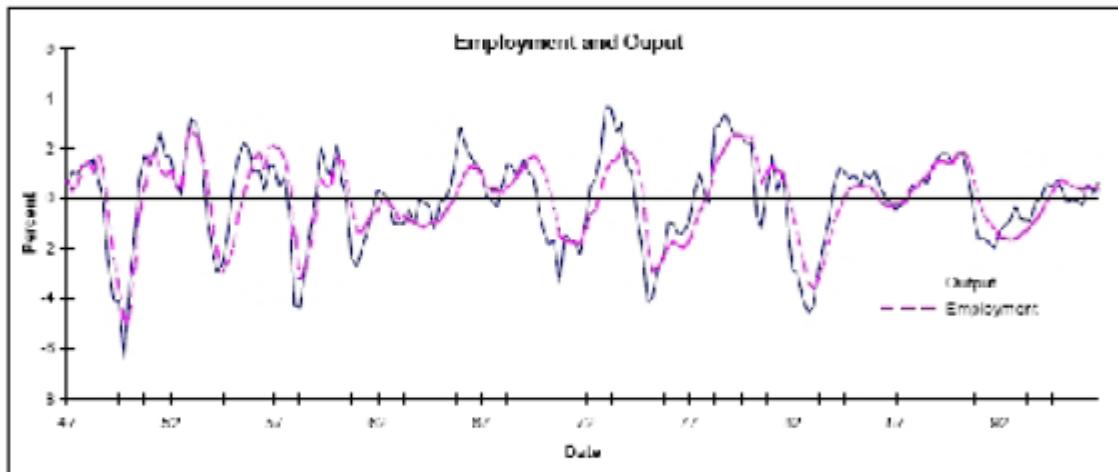
highly correlated  
with output

- About as volatile as output
- Business cycle is most clearly manifested in the labor market

# Employment

↳ # of workers

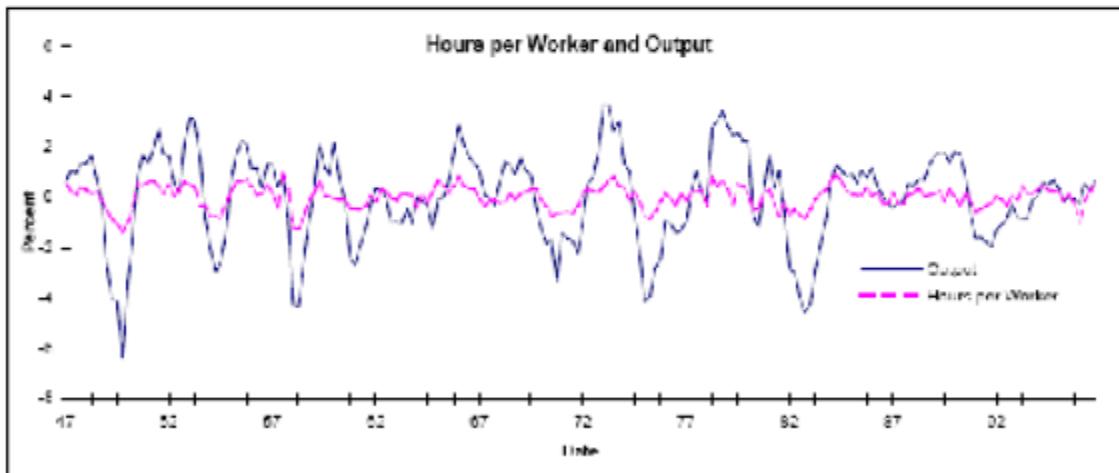
$$\sigma_N \approx \sigma_y$$



- as volatile as output

## Hours worked

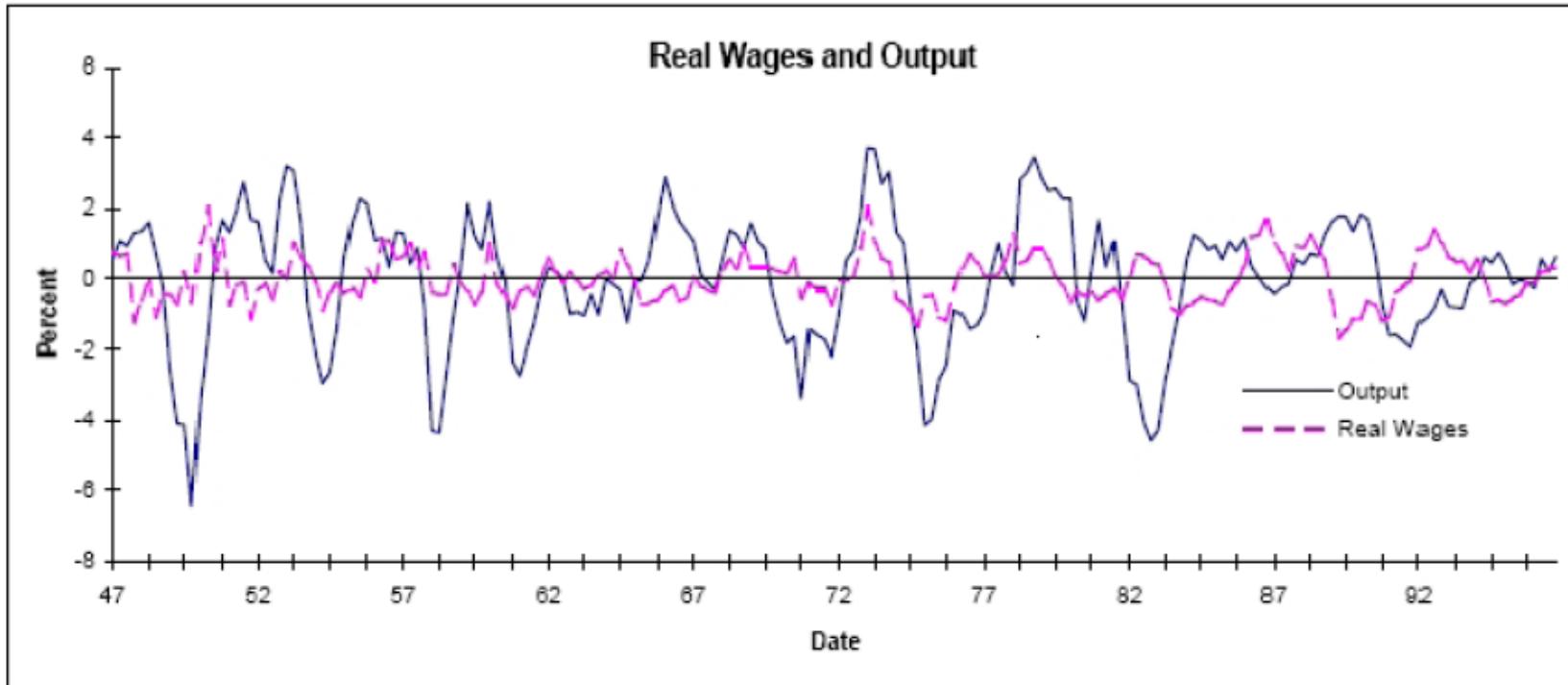
$$\sum \text{hours} < \sum y$$



- **Hours per worker:** Much less volatile than output
- Most variation in total hours stems from changes in employment, rather than adjustment in hours worked per employee.

$$\text{Real Wage} = \frac{W}{P} \xrightarrow{\substack{W \rightarrow \text{Nominal wage} \\ P \rightarrow \text{Price level}}} \text{Real Wage} \sim MPL$$

$$\log \text{real wage} = \log W - \log P$$



- Much less volatile than output
- Slightly **PRO-cyclical** (correlation = 0.14) => important fact

Or even  $\alpha$ -cyclical

Are we still going through a great moderation?  
(HW1)

## An Obvious Question

- What do the US business cycle statistics look like post-1999 & post-2007?  
Are the patterns described above still true? How about other countries?
  - How to produce the basic business cycle statistics: discussed in the first two sections of King and Rebelo (1999) Handbook chapter
- 

### Data Sources:

- for the US: FRED
  - <https://fred.stlouisfed.org/>
- international macro: IMF-International Financial Statistics (IFS)

} Related to HW1

Can you see in the data the following view?

- Old Macro: Analyzes pre- versus post- 1984:Q4.  
*Great Moderation*
- New Macro: Analyzes pre- versus post- August 2007  
*Global Financial Crisis*
  - End of the **Great Moderation**
  - Downturn precipitated by disruption of **Financial Intermediation (2008)**
  - **Unconventional Monetary Policy** and **Zero Lower Bound**, balance sheet management, macro-prudential policy...

- COVID-19 macro

Supply side shock?

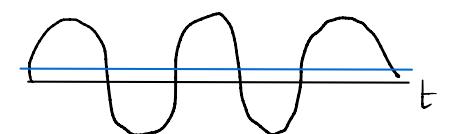
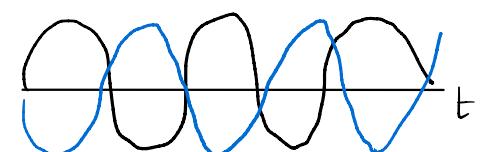
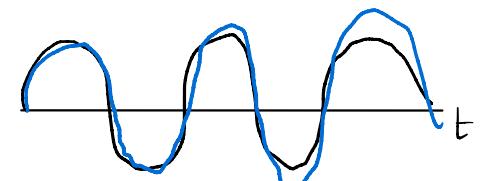
Demand Side shock? or both?

How transitory?

Procyclical

Countercyclical

Bycyclical



As we go through models after models after models\*... ALWAYS ask yourself:

- 1.What is the Motivation behind the model?
- 2.What is the Economic intuition?
- 3.What is the relevant Technique/Tool to pick up?
- 4.What does the Data say?
- 5.What are some Alternatives to model or test the same phenomenon (or hypothesis)?

=> Learn not (just) their thoughts, but how they THINK (how to approach and formalize the issue at hand)

## **Key Questions (Extra Credit)**

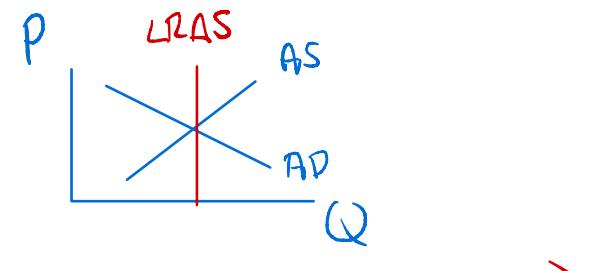
- What are some “stylized facts” about US Business cycle dynamics up?
- What is Neoclassical Synthesis?
- ... more to follow

## Part 2: From IS-LM Neo Classical Synthesis to New Synthesis

A. Some course logistics – **important dates: posted on course website!**

B. Brief History of Modern Macro

- The Neoclassical Synthesis → IS-LM
- The Breakdown of the Consensus → 1970's stagflation ( $\uparrow P, \downarrow Q?$ )
  - Price Adjustment: Phillips-Solow-Samuelson vs. Friedman-Phelps
- Is the Long-Run Phillips Curve Really Vertical?
- Rational Expectations Revolution
- Main Approaches to modeling Aggregate Supply since then
- The New-Neoclassical Synthesis



## Housekeeping:

- First midterm is “take-home” and is done after **Topic 2**

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- The ~~5~~<sup>6</sup> Homework assignments are submitted in class
  - First Assignment (HW0) due next week: Get full credits just by submitting (only for HW0)
- A **Final Exam**, at the end of the semester
- Last week of class: group project presentations
- Reminder: **Extra credit option**: submitting answers to “Key Questions” at the end of each lecture (before the start of the next)

## A VERY Brief History of Macro:

- Neoclassical Synthesis (IS-LM : AD-AS Intermediate macro)
- The Breakdown of the Consensus + the Rational Expectations Revolution
- Main approaches to modeling Aggregate Supply in the 80s & 90s
- “New” Neoclassical Synthesis →
  - Old lessons from initial synthesis
  - + Rational Expectations
  - + Intertemporal Decision making
- Post-2008: Financial Friction, “Unconventional” Monetary Policy...etc.
- Now?

I. **Neoclassical Synthesis**: Consensus in the 1960's (Review of intro to macro)

a. **Aggregate Demand**: from IS-LM framework: **goods market** and **money market** equilibria, and Walras Law implies **asset market clearing** (*Supply = Demand*)

$$\textcircled{1} \quad \text{Goods market: } Y = C(Y - T) + I(r) + G + \cancel{NX}$$

Ignore for now

$$\textcircled{2} \quad \text{Money market: } \frac{M^s}{P} = L(i, Y)$$

$\uparrow \log P_t - \log P_{t-1}$

+ Walras Law: If  $N-1$  markets are in equilibrium, the  $N$ -th remaining market is in equilibrium.

$\Rightarrow$  obtains Aggregate Demand (from IS-LM equilibrium)

b. Aggregate Supply: Keynesian vs. Classicalist: Are prices sticky?

i) Keynesian Nominal rigidity (sticky prices/wages) => Short-run

$$P = \bar{P} \text{ (constant)}$$



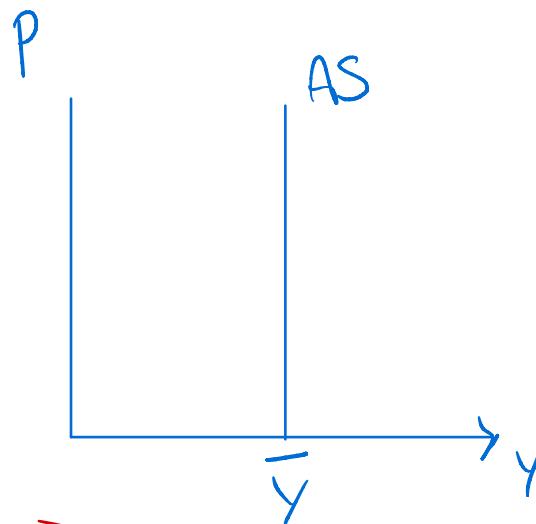
ii) Natural Rate Hypothesis (prices/wages fully flexible) & monetary neutrality => Long-run

$$Y = \bar{Y}^{NR} = \bar{Y}^{\text{Full Employment}}$$



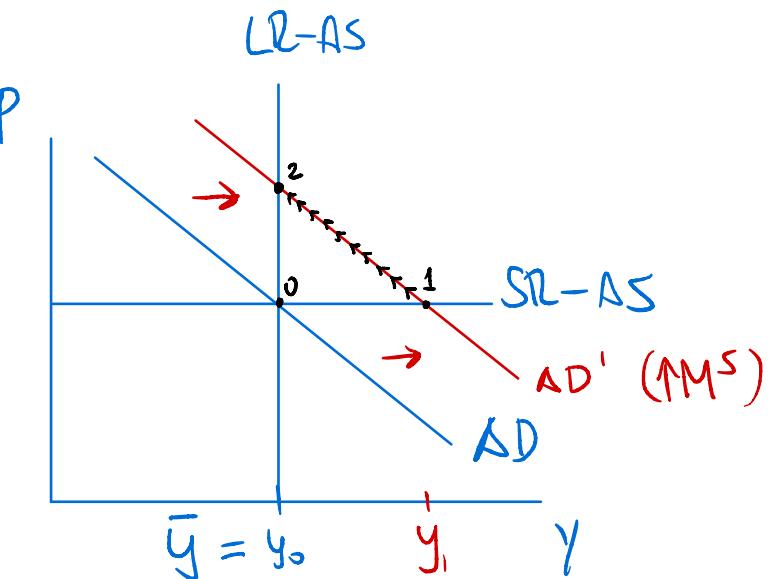
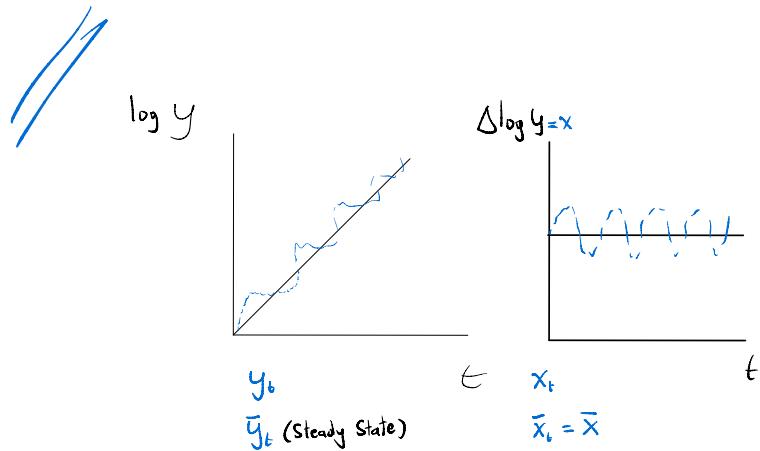
associated to  
trend level of output

$$Y = f(\text{Labor}, K, \text{Nat Resources})$$



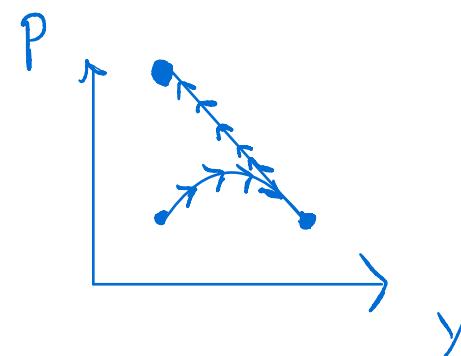
Neoclassical Synthesis: put 1-3 above together,

- with 1) and 2) giving AD
- i) for Short-Run AS
- ii) for Long-Run AS



How do we adjust from SR to LR?

SR:  $y > y^N \rightarrow \uparrow P$   
 Economy is overheated ( $\uparrow \pi$ )



c. linking SR and LR with **price-adjustment dynamics: the Phillips Curve:**

$$\pi = \alpha (Y - Y^N) = -\beta(u - u^N)$$

$\overset{\nearrow \alpha}{\curvearrowleft}$        $\overset{\nearrow \beta}{\curvearrowleft}$

$\downarrow$   
 $\alpha > 0$

$u$ : Unemployment rate

$\square \text{Corr}(Y_N) > 0$   
 $\square \text{Corr}(Y, u) < 0$

## How well did this “model” do?

- Data in the 50's-60s supported the above => tradeoff between  $\pi$  and  $u$ , providing **scope for policy actions**
- At the applied level: refinements of above
  - large-scaled models: “MPS”, Harvard, Fed models with several hundred of equations
  - these models are based on empirically observed relationships (between output and consumption, money demand, in unemployment... etc)
  - the aim of these models was to predict the effects of policies
  - they were pretty successful at it until the 1960s
- Bob Solow: “Macroeconomics is finished” (as in done/completed!)

## The Breakdown of the Consensus in the early 1970s

a. Empirically:

Models couldn't explain the simultaneous rising inflation AND unemployment in the 1970s: Vietnam War,  $G \uparrow$ ,  $M^S \uparrow \Rightarrow \pi \uparrow$  but no  $u \downarrow$

b. Theoretically:

- Friedman (1968), Phelps (1968): Phillips' curve cannot be right!

Violation of the **Natural Rate Hypothesis**: Long run unemployment should NOT depend on the average rate of money growth, i.e. What if Fed changes the money growth rate?? Say from 0% to 5%,  $\Rightarrow \pi = 5\% \Rightarrow u \downarrow$  and  $Y \uparrow$  in the LR!

$\Rightarrow$  **Expectation-augmented Phillips Curve**

$$\pi = -\beta(u - u^N) + \gamma E\pi$$

Stagflation:  
Simultaneous Increase of  
 $\pi$  and  $u$

as policy changes from 0 to 5%  
(money growth)  
 $E[\pi]$  increases from 0 to 5%

- Lucas Critique ('73) and the **Rational Expectation** revolution
  - When evaluating policy, expectations: if policy maker changes the rule, public expectation will adjust as well, so the equilibrium condition for the economy will change too.

=> All of the above point to the “danger” of using ad hoc, reduced-form empirical relationships with no “micro-foundation”!

  
Correlations

Tom Sargent, “Macro is finished”... (as in “destroyed”)

20+ years of confusion and division to follow....

## Lucas Critique ('73) and the Rational Expectation Revolution

- Expectation-augmented Phillips curve:

$$\pi = -\beta(u - u^N) + \gamma E\pi$$

↗ Feedback of expectations to  $\pi$   
↘ Expected Inflation

Or:

$$\pi_t = a - bu_t + \gamma E_{t-1}\pi_t$$

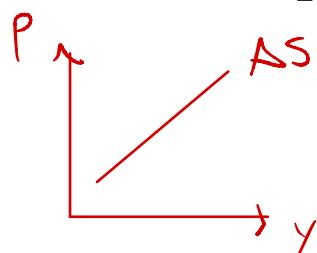
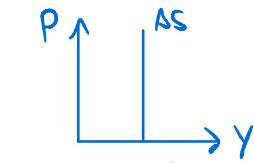
↗ Forward looking Component

Note: in the long-run,  $\boxed{\pi = E\pi}$  (by definition, of LR)

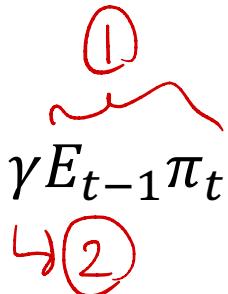
Long Run:

- If  $\gamma = 1$ , then  $u = u^N$ , so LR, at  $u^N$  and  $Y^N \Rightarrow$  LR-AS is vertical  
 $\gamma=1 \Rightarrow \pi = -\beta(u-u^N) + \gamma\pi \Rightarrow u=u^N (\gamma=Y^N)$
- Otherwise,  $u$  will depend on both  $u^N$  and  $\pi \Rightarrow$  LR-AS is sloped ( $Y$  or  $u$  depend on prices/inflation)

$$(\gamma \neq 1, \gamma < 1) \Rightarrow \pi = \frac{-\beta}{1-\gamma} (u - u^N) \rightarrow$$



## How to Measure/Model $E\pi$

$$\pi_t = a - bu_t + \gamma E_{t-1}\pi_t$$


- It is therefore important to know the value of  $\gamma$ ,
- To gauge its value: look into past data of inflation and unemployment,

BUT:

- also need to know how to measure and model  $E\pi$

## **Lucas Critique ('73) and the Rational Expectation Revolution**

- Nobel Prize 1995
- Much of what economists were doing and the policy conclusions were **WRONG**
  - Using a model with fixed coefficients estimated from reduced-form equations and historical data to evaluate the effects of new policy would give misleading results because **expectations need to be endogenous**
  - i.e. Changes in policy will affect expectations
- True whenever expectations are forward-looking (need not be rational)

**“Rational” = model-consistent**

## Three Methodological Tenets for Rational Expectations<sup>1</sup>

- Results widely applicable; use Phillips Curve as an example below

### 1. Partial Equilibrium. <sup>1 market</sup>

Agents form expectations appropriately given the **stochastic process** generating the variables of interest. Expectations cannot be specified without first specifying the underlying stochastic process.

e.g. Given  $\pi_t = a - bu_t + \gamma E_{t-1}\pi_t$  (\*), want to know  $\gamma$

=> first specify how  $\pi_t$  is determined

e.g.  $\pi_t$  follows an AR(1) process

$$\pi_t = \underbrace{\rho \pi_{t-1}}_{0 < \rho < 1} + \underbrace{\varepsilon_t}_{\text{Shock (white noise)}}$$

$$\begin{aligned}E(\varepsilon_t) &= 0 \\E(\varepsilon_t^2) &= \sigma^2 \\E(\varepsilon_t, \varepsilon_s) &= 0\end{aligned}$$

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<sup>1</sup> N.G. Mankiw

Explain Expectation Operator (and take  $E_{t-1}\pi_t$  given it is AR(1))

$E[X_t]$ : Expected value of  $X_b$

$$E_{t-1}[X_t] = E[X_t \mid \text{Information up to } t-1] = E[X_b \mid I_{t-1}]$$

Properties:

- ①  $E[-]$  is a linear operation
- ②  $E[\alpha X_b] = \alpha E[X_b]$

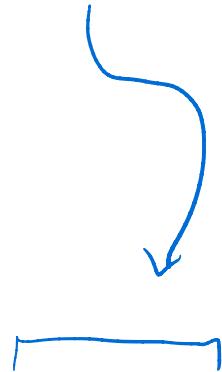
$$\left. \begin{array}{l} E[\pi_t] = E_{t-1}[P\pi_{t-1} + \varepsilon_t] \\ E_{t-1}[\pi_t] = E_{t-1}[P\pi_{t-1}] + E_{t-1}[\varepsilon_t] \end{array} \right\}$$

$$E_{t-1}[\pi_b] = P E_{t-1}[\pi_{b-1}]$$

$$E_{t-1}[\pi_b] = P \pi_{b-1}$$

Given the stochastic process,  $E_{t-1}\pi_t = \rho\pi_{t-1}$  under Rational  
Expectation

- Plug this into (\*), we see that

Plug into PC

$$\pi_t = a - bu_t + \gamma\rho\pi_{t-1}$$

- What does this say about finding  $\gamma$  by looking at the historical relationship b/w inflation and unemployment?

## 2. General Equilibrium.

The stochastic process of any variable generally depends on the entire model. To solve for expectations, one must assume that agents know and solve correctly the model of the economy.

Simple GE<sub>q</sub> model (all variables in logs)

$$\textcircled{1} \quad m_t - p_t = y_t \quad (\text{AD})$$

$$\textcircled{2} \quad y_t = \alpha (p_t - E_{t-1} p_t) \quad (\Delta S)$$

$$\hookrightarrow y_t = \alpha (\underbrace{\pi_{t-1}}_{p_t - p_{t-1}} - E_{t-1} \pi_t)$$

$$p_t - p_{t-1} - E_{t-1} (p_t - p_{t-1})$$

$$\textcircled{1} \quad m_t - p_t = y_b \quad (\Delta D)$$

$$\textcircled{2} \quad y_t = \alpha (p_b - E_{t-1} p_b) \quad (\Delta S)$$

from (1)  $p_t = m_t - y_t$

take  $E_{t-1}$ :  $E_{t-1} p_t = E_{t-1} (m_t - y_t) \quad (1')$

from (2)  $E_{t-1}[y_b] = \alpha E_{t-1}(p_b - E_{t-1} p_t)$

$$= \alpha E_{t-1} p_b - \underbrace{\alpha E_{t-1}[E_{t-1} p_t]}_{E_{t-1} p_t} = 0$$

$$E_{t-1}[E_{t-1}[x_b]]$$

$$= E_{t-1}[x_t]$$

$\Rightarrow$  in (1'):  $E_{t-1} p_t = E_{t-1} m_t$

back in AS:

$$y_b = \alpha (p_b - E_{t-1} p_b)$$

$$y_t = \alpha (m_t - y_t - E_{t-1} m_t)$$

Now solve for  $y_b$ :

$$y_t = \frac{\alpha}{1+\alpha} (m_t - E_{t-1} m_t) \quad (\Delta S^{\text{new}})$$

$y$  is a function of unexpected movements in the money supply

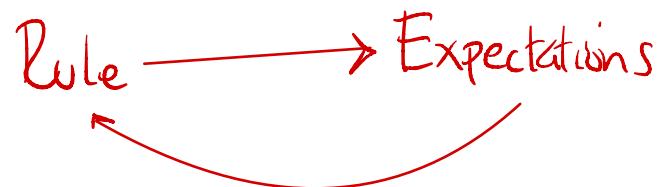
Policy Rule: Framework according to which policy is set

### 3. Policy Evaluation

The rules governing policy are among the equations in any complete model of the economy. Because a change in a policy rule alters the stochastic processes generating many variables, it also changes the way people form expectations. Hence, when evaluating alternative policy rules, one must take account of this feedback between the policy rule and the way expectations are formed. Any policy evaluation that fails to take account of this feedback is flawed and useless.

'Lucas Critique'

↳ Need to specify a rule



e.g. Simple rule:  $m_t = \mu_a + m_{t-1} + \epsilon_t$  (3) (Use it along w/ AD<sup>AS</sup> (1), (2))

$$E_{t-1}m_t = \mu_a + E_{t-1}m_{t-1} + E_{t-1}\cancel{\epsilon_t}$$

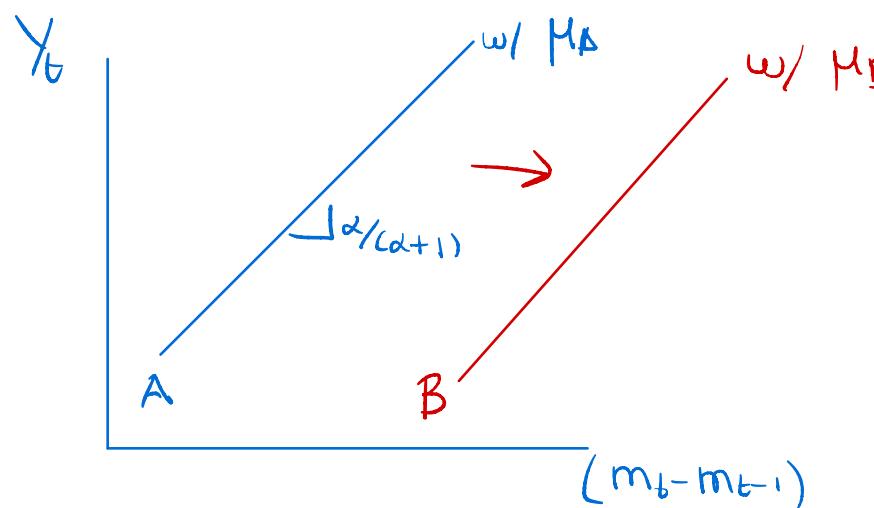
$$E_{t-1}m_t = \mu_a + m_{t-1} \quad (\text{Plug into AS}^{\text{new}})$$

$$y_t = \frac{\alpha}{\alpha+1} [m_t - E_{t-1} m_t]$$

Subst  $E_{t-1} m_t = \mu_A + m_{t-1}$

$$\Rightarrow y_t = \frac{\alpha}{\alpha+1} [m_t - m_{t-1} - \mu_A] (*)$$

growth rate  
 of money



$y$  depends on growth rate of  
money 'wedge' relative to  $\mu_A$

New Rule:  $m_t = \mu_B + m_{t-1} + E_t$   
 $(\mu_B > \mu_A)$

Key: Original relationship is valid only  
under the original rule (3) ( $w/ \mu_A$ )

In reality w/ new rule we should re-solve  
the system:

New AS would be  $y_t = \frac{\alpha}{1+\alpha} (m_t - m_{t-1} - \mu_B)^{40}$

$$y_t = \frac{\alpha}{1+\alpha} (m_t - E_{t-1} m_t) \quad (\Delta S^{\text{new}})$$

$$E_{t-1} m_t = \mu_A + m_{t-1}$$

## Summary:

- When evaluating policy, need to take into account the feedback with expectations.
  - If policy maker changes the rule, expectation will change so the equilibrium condition for the economy will change too.
- ⇒ All of the above point to the “danger” of using ad hoc, reduced-form empirical relationships with no “micro-foundation”!

## Results of the RE revolution:

- 1) More focus on structural modeling of the economy (micro-foundation based on first principles), rather than estimating reduced-form equations. Identification key!
- 2) Taking expectations seriously  
Lucas Critique does NOT imply policy ineffectiveness, but that policy making should focus on developing on-going strategy and long-term rules, not one-time change

⇒ **Four Main Approaches to Aggregate Supply**

# Unification Again Since the 1990's

## “New Neoclassical Synthesis”

- RBC techniques + New Keynesian insights
- Dynamic Stochastic General Equilibrium Modeling
- Business Cycles may be caused by real shocks, but nominal rigidity leads to inefficiency, hence role for policy

◦ Modified AS      } NK DSGE  
◦ "      " AD  
◦ Policy Rule

## Key Questions – Extra credit

- What are some “stylized facts” about the US Business cycle dynamics (up to around 2000)?
- What is the Natural Rate Hypothesis?
- What does money neutrality mean?
- What is the Neoclassical Synthesis? And what were its main problems?

## Part 3: Rational Expectations

### A. Outline:

- Recap/Continuation of Rational Expectations

### B. Housekeeping

- HW0 due on ✓
- HW1 due on 2/13 (you'll be ready to start by today)

## Recap./Cont. of Rational Expectations in Macro:

### Brief History of Modern Macro

- The Neoclassical Synthesis       $IS-LM \rightarrow AD-AS$
- The Breakdown of the Consensus      *Stagflation of 70's*
- Is the Long-Run Phillips Curve Really Vertical?
- Rational Expectations Revolution
- Main Approaches to modeling Aggregate Supply since then
- The **New** Neoclassical Synthesis

## Summary from before:

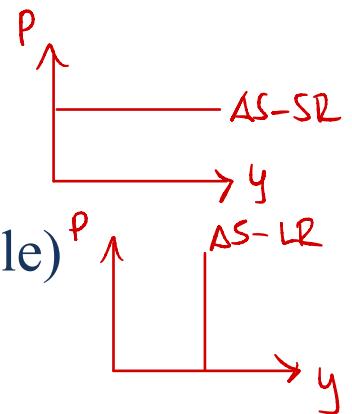
### Neoclassical Synthesis: Consensus in the 1960's

1. **Aggregate Demand**: comes from IS-LM framework

2. **Aggregate Supply**:

a) Short-run: Keynesian Nominal rigidity (sticky prices/wages)

b) Long-run: Natural Rate Hypothesis (prices/wages fully flexible)



3. **Phillips curve**: price adjustment from SR to LR

$$\pi = \alpha (Y - Y^N) = -\beta(u - u^N)$$

## **Phillips curve:**

$$\pi_t = \alpha (Y_t - Y^N) = -\beta(u_t - u^N)$$

- Data in the 50's-60s, support above relationship
- Negative relationship implies a tradeoff between  $\pi$  and  $u$  and scope for policy actions

## **Breakdown of the Consensus due to:**

- Friedman-Phelps' critique + Poor empirical support (in 70's)
- Lucas' Rational Expectation revolution

$$\hat{Y}_t = \alpha - bU_t + \gamma E_{t-1} Y_{t-1}$$

## Lucas Critique ('73) and the Rational Expectation Revolution

- Nobel Prize 1995
- Much of what economists were doing and the policy conclusions were **WRONG**
  - Using a model with fixed coefficients estimated from reduced-form equations and historical data to evaluate the effects of new policy would give misleading results because **expectations need to be endogenous**
  - i.e. Changes in policy will affect expectations
- True whenever expectations are forward-looking (need not be rational)

## Three Methodological Tenets for Rational Expectations<sup>2</sup>

- Results widely applicable; below look at examples regarding PC

### 1. Partial Equilibrium.

Agents form expectations appropriately given the stochastic process generating the variables of interest. Expectations cannot be specified without first specifying the underlying stochastic process.

How to measure  $E_{t-1} \pi_t$

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<sup>2</sup> N.G. Mankiw

- Given the stochastic process,  $E_{t-1}\pi_t = \rho\pi_{t-1}$  under Rational Expectation
- Plug this into (\*), we see that
  - $\pi_t = a - bu_t + \gamma\rho\pi_{t-1}$

*Need to account for extra features affecting  
the feedback of expectations*
- What does this say about finding  $\gamma$  by looking at the historical relationship b/w inflation and unemployment?

[Further look into the implications of the stochastic process and the expectation operator]

- **Note:** Given  $\pi_t = \rho\pi_{t-1} + \varepsilon_t$  where  $\varepsilon_t$  is a “white noise” process:
- $\varepsilon_t$  is a time series process that's independently and identically distributed (iid), with zero mean  $E(\varepsilon_t) = 0$ , a constant variance  $E(\varepsilon_t^2) = \sigma^2$ , and  $E(\varepsilon_t\varepsilon_s) = 0$

**Applying the Expectation operator  $E_{t-1}$  to  $\pi_t$**  (taking its expectation at time t-1, implying based on information we have at time t-1):

$$\begin{aligned} E_{t-1}\pi_t &= E_{t-1}[\pi_t] = E[\pi_t | I_{t-1}] && \text{different notations for the same thing} \\ &= E_{t-1}[\rho\pi_{t-1} + \varepsilon_t] && \text{substituting in the definition of } \pi_t \\ &= E_{t-1}[\rho\pi_{t-1}] + E_{t-1}[\varepsilon_t] && \text{“operation” is linear (can do it term by term)} \\ &= \rho\pi_{t-1} + 0 && \text{what you expect at any time given info at that time = the info itself} \end{aligned}$$

Our (\*) equation, the expectation-augmented Phillips Curve is then:

$$\begin{aligned}\pi_t &= a - bu_t + \gamma E_{t-1} \pi_t \\ &= a - bu_t + \gamma \rho \pi_{t-1}\end{aligned}$$

What does this imply?

- 1) the relation b/w inflation and unemployment depends on **lagged inflation** ( $\pi_{t-1}$ ) too
- 2) Without specifying  $\rho$  first, we cannot determine  $\gamma$

## 2. General Equilibrium.

The stochastic process of any variable generally depends on the entire model. To solve for expectations, one must assume that agents know and solve correctly the model of the economy.

- In our case, it means endogenizing  $\pi_t$ : have it determined from within the system
- We will adopt a variant of the Phillips curve (\*) instead too.

Consider an economy described by a simple General Equilibrium (GE) model (note, all variables are in logs, allowing us to use linear equations):

$$1) m_t - p_t = y_t \quad (\text{AD})$$

$$2) y_t = \alpha(p_t - E_{t-1}p_t) \quad (\text{AS})$$

[Clarifying note: Relation btw Phillips Curve we saw before and (2) in last slide]

**Note:** The AS in the previous page is another way to express the expectation-augmented Phillips curve (\*). From either of these expressions (again, equivalent):

$$\pi_t = a - bu_t + \gamma E_{t-1} \pi_t$$

$$\pi_t = -\beta(u_t - u^N) + \gamma E_{t-1} \pi_t$$

Since output  $y_t$  is inversely related to unemployment  $u_t$ :

$$\pi_t = cy_t + \gamma E_{t-1} \pi_t$$

Since inflation is the difference in prices:  $\pi_t = p_t - p_{t-1}$

$$p_t - p_{t-1} = cy_t + \gamma E_{t-1}[p_t - p_{t-1}]$$

Re-arrange and note:

$$E_{t-1}[p_{t-1}] = p_{t-1}$$

$$y_t = \alpha(p_t - E_{t-1}p_t)$$

To Solve for Y from the system of AD and AS:

from (1)  $P_b = m_b - y_b$

take  $E_{t-1}$ :  $E_{t-1}[P_b] = E_{t-1}[m_t] - E_{t-1}[y_b]$

Take  $E_{t-1}$  in (2):  $E_{t-1}[y_b] = \alpha E_{t-1}[P_b - E_{t-1} P_b]$  ( $E_{t-1} E_{t-1} P_b = E_{t-1} P_b$ )  
 $E_{t-1}[y_b] = 0$

$\Rightarrow E_{t-1}[P_b] = E_{t-1}[m_t]$

AS:  $y_b = \alpha(P_b - E_{t-1} P_t) = \alpha[m_b - y_b - E_{t-1}[m_b]]$

Solve for  $y$ :  $y_b(1 + \alpha) = \alpha[m_b - E_{t-1} m_b]$ ,  $\downarrow$

What does this result mean?

$$\rightarrow y_t = \frac{\alpha}{1 + \alpha} [m_t - E_{t-1} m_t] \quad (*)$$

- Output depends on “surprised” or unexpected money

### 3. Policy Evaluation

- Policy rules are part of the equations in most good macro models.
- A change in a policy rule alters the stochastic processes generating many variables => it also changes the way people form expectations.
- Any policy evaluation that fails to take account of this feedback is flawed.

Add a rule

$$m_t = \mu_d + m_{t-1} + \epsilon_t$$

$\mu_d$  indicates the expected money growth:

$$m_t - m_{t-1} = \mu_d + \text{Error}$$

$\underbrace{\log \Delta}_{\text{diff}} \approx \text{growth}$

$$E_{t-1}[m_t] - E_{t-1}[m_{t-1}] = E_{t-1}[\mu_d] + E_{t-1}[\text{Error}]$$

$$E_{t-1}[m_t] - m_{t-1} = \mu_d$$

$$\Rightarrow E_{t-1}[m_t] = \mu_d + m_{t-1}$$

## Key Questions (Extra Credit, due next session)

- What is the Lucas Critique?
- Intuitively, how do the three perspectives of rational expectations differ (and/or improve, complement each other)?
- How is Lucas' rational expectation captured within economic models?

## Part 4: Approaches to model the Aggregate Supply

### A. Reminder:

- HW1 due on by 2/13

### B. Brief History of Modern Macro

- Rational Expectations Revolution (cont.)
- **Main Approaches to modeling Aggregate Supply since then**
- **The New Neoclassical Synthesis**

## Summary from before:

Expectation-Augmented Phillips Curve:

$$\pi_t = -\beta(u_t - u^N) + \gamma E_{t-1} \pi_t$$

$$\pi_t = a - bu_t + \gamma E_{t-1} \pi_t$$

$$y_t = \alpha(p_t - E_{t-1} p_t)$$

## Lucas Critique ('73) and the Rational Expectation Revolution

- Policy evaluation must consider how change in policy will affect (forward-looking) expectations
- “Rational”: model-consistent

To form “model-consistent” rational expectations:

**1. Partial Equilibrium:** specify the **stochastic process** generating the variables of interest

e.g. Given  $\pi_t = \rho_1\pi_{t-1} + \rho_2\pi_{t-2} + \varepsilon_t$  where  $\varepsilon_t$  is a white noise process

- This is called an autoregressive process of degree 2, or AR(2), with the two  $\rho$ 's (“rho”) as the AR coefficients (constants)
- $E_{t-1}\pi_t = ?$

$$\begin{aligned} E_{t-1}\pi_t &= E_{t-1}[\rho_1\pi_{t-1} + \rho_2\pi_{t-2} + \varepsilon_t] \\ &= E_{t-1}[\rho_1\pi_{t-1}] + E_{t-1}[\rho_2\pi_{t-2}] + E_{t-1}[\varepsilon_t] \\ &= \rho_1\pi_{t-1} + \rho_2\pi_{t-2} \end{aligned}$$

## 2. General Equilibrium.

- The stochastic process of a variable generally depends on the entire model
- To solve for expectations, one must assume that agents know and solve correctly the model of the economy

e.g. (note, variables are in logs; see next page)

$$1) m_t - p_t = y_t \quad (\text{AD})$$

$$2) y_t = \alpha(p_t - E_{t-1}p_t) \quad (\text{AS})$$

$$y_t = \frac{\alpha}{1 + \alpha} [m_t - E_{t-1}m_t]$$

=> Output depends on “surprised” or unexpected money

[Clarification-Why we use logs or similar approximations]

### A note about **linearized equations**:

- We will be working with “linearized” equations frequently, to make the models easier to solve.
- In order to express general economic equations in linear forms, we often take the (natural) logs of the variables. For example, the quantity theory of money,  $M_t V_t = P_t Y_t$  can be expressed as  $m_t + v_t = p_t + y_t$  where each of the lower-case variables is the log of the capitalized variables.
- We will use variations of  $m_t + v_t = p_t + y_t$  to represent **aggregate demand** for a while.

### 3. Policy Evaluation (where does $m_t$ come from?)

- The rules governing policy are among the equations in any complete model of the economy
- Because a change in a policy rule alters the stochastic processes generating many variables, it also changes people's expectations
- Hence, when evaluating alternative policy rules, one must take account of this feedback between policy rules and how expectations are formed.
- Any policy evaluation that fails to take account of this feedback is flawed and useless (Lucas Critique)

(3) Consider a simple monetary policy rule:  $m_t = \mu_A + m_{t-1} + \varepsilon_t$   
where  $\mu_A$  ("mu" \_A) is a constant and  $\varepsilon_t$  is a **white noise** process gain

Note: since these variables are in logs,  $\mu_A = E(m_t - m_{t-1})$  represent the **expected growth rate of money or the trend money growth rate** (Remember: log (small) differences = % change or growth rate.)

Combining (1)-(3) to solve the GE model:

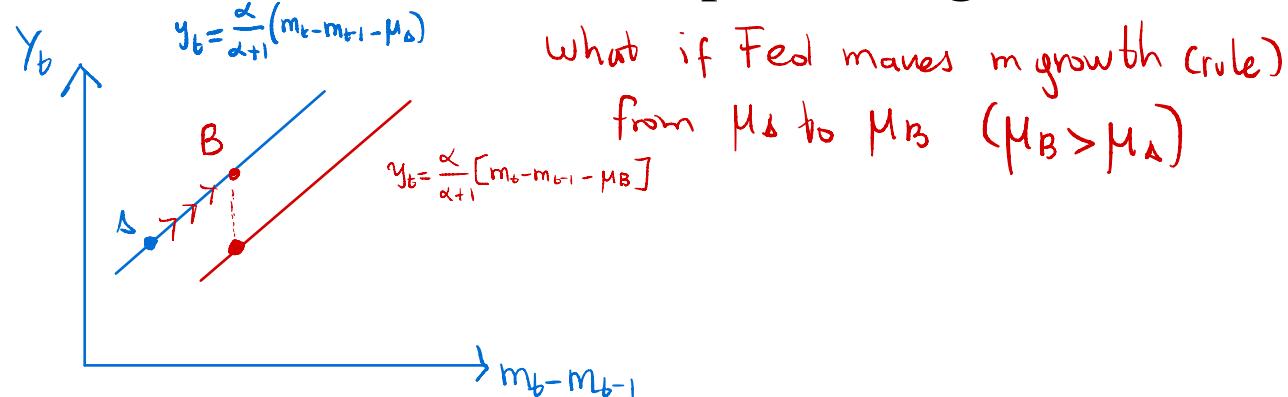
$$E_{t-1}m_t = \mu_A + m_{t-1}$$

$$\Rightarrow y_t = \frac{\alpha}{1+\alpha} [m_t - m_{t-1} - \mu_A]$$


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- This tells us that in general equilibrium, the level of output at each time depends on both money growth from the previous period ( $m_t - m_{t-1}$ ), but also on the general trend growth rate set by monetary policy ( $\mu_A$ )

## What is the policy implication from this rational expectation general equilibrium model?



- Output level is positively correlated with money growth from period-to-period. However, this relationship does NOT imply **policy tradeoff** because the line above is only valid under the policy rule (3) with  $\mu_A$
- If policymaker increases money growth rate from point A to point B (e.g. by changing money growth from  $\mu_A$  to  $\mu_B$ ), (3) would no longer be the correct rule. The rule would have trend money growth  $\mu_B$  instead
- People forming rational expectations would adjust as well based on the new rule. Resolving the system, we see that the curve **shifts to the right** (to reflect the new output-money growth relationship)

## Results of the RE revolution:

- 3) More focus on structural modeling of the economy: micro-foundation based on first principles, rather than estimating reduced-form equations. Identification: correlation does not equal causality
- 4) Taking expectations seriously  
Lucas Critique does NOT imply policy ineffectiveness, but that policy making should focus on developing on-going strategy and long-term rules, not one-time change

## Four Main Approaches to Aggregate Supply

		<b>Do Markets Clear?</b> (instantaneously)	
		<b>Yes</b>	<b>No</b>
<b>Is Money Neutral?</b> <small>(in medium, Long run)</small>	<b>Yes</b>	<b>1. Classical/RBC</b> Kydland & Prescott Minnesota	<b>3. Real Rigidity</b> e.g. Efficiency wage theory Akerlof, Yellen
	<b>No</b>	<b>2. Imperfect Information</b> Friedman Lucas '77	<b>4. Nominal Rigidity</b> Nominal contracts, menu costs: Fischer, Taylor, Calvo ...

## Unification Again Since the 1990's

### “**New** Neoclassical Synthesis”

- Real Business Cycle tools (Romer Ch.5) + New Keynesian (Ch. 6) ideas
- Dynamic Stochastic General Equilibrium Modeling
- Business cycle may be caused by real shocks, **but nominal rigidity leads to inefficiency, hence role for policy**

## **References:**

- Mankiw, N Gregory. 1990. "A Quick Refresher Course in Macroeconomics," Journal of Economic Literature
- Woodford, Michael. 1999, "Revolution and Evolution in Twentieth-Century Macroeconomics."
- Goodfriend, M. 2002. "Monetary Policy in the New Neoclassical Synthesis: A Primer"