

Converting infix expressions to postfix
expressions

Infix to Postfix Conversion using a stack

- Read the input
- If the input is an operand, write to output
- If the input is an operator
 - Pop until the top of the stack has an element of lower precedence, and write them to output
 - Push the new operand into stack
- If the input is ')', pop until we find the matching '(' and write them to output. Do not write the ')' to the output. Remove the '(' from stack.
- When we reach the end of input, pop all the remaining operands

Infix to Postfix Conversion

Example

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

- Stack:
- Output:

Infix to Postfix Conversion

Example-Continued

(14+8)*(8-4)/((6-2*2)*(1+2))

Processing '(' -- Push into stack

- Stack: (
- Output:

Infix to Postfix Conversion

Example-Continued

$$(\underline{14}+8)*(8-4)/((6-2*2)*(1+2))$$

Processing 14 -- Write to output

- Stack: (
- Output: 14

Infix to Postfix Conversion

Example-Continued

$$(14_8)*(8-4)/((6-2*2)*(1+2))$$

Processing '+' -- Push into stack

- Stack: (+
- Output: 14

Infix to Postfix Conversion

Example-Continued

$$(14+\underline{8})*(8-4)/((6-2*2)*(1+2))$$

Processing '8' -- Write to output

- Stack: (+
- Output: 14 8

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing ')' -- Pop until you find '('

- Stack:
- Output: 14 8 +

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

Processing * -- Push into stack

- Stack: *
- Output: 14 8 +

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

Processing '(' -- Push into stack

- Stack: * (
- Output: 14 8 +

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(\underline{8}-4)/((6-2*2)*(1+2))$$

Processing '8' -- Write to output

- Stack: * (
- Output: 14 8 + 8

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

Processing '-' -- Push into stack

- Stack: * (-
- Output: 14 8 + 8

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-\underline{4})/((6-2*2)*(1+2))$$

Processing '4' -- Write to output

- Stack: * (-
- Output: 14 8 + 8 4

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing ')' -- Pop until you find '('

- Stack: *
- Output: 14 8 + 8 4 -

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing '/' -- Pop '*' and push '/' into stack

- Stack: /
- Output: 14 8 + 8 4 - *

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing '(' -- push into stack

- Stack: / (
- Output: 14 8 + 8 4 - *

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing '(' -- Push into stack

- Stack: / ((
- Output: 14 8 + 8 4 - *

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((\underline{6}-2*2)*(1+2))$$

Processing '6' -- Write to output

- Stack: / ((
- Output: 14 8 + 8 4 - * 6

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

Processing '-' -- Push into stack

- Stack: / ((-
- Output: 14 8 + 8 4 - * 6

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-\underline{2}*2)*(1+2))$

Processing '2' -- Write to output

- Stack: / ((-
- Output: 14 8 + 8 4 - * 6 2

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing '*' -- Push into stack

- Stack: / ((- *
- Output: 14 8 + 8 4 - * 6 2

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*\underline{2})*(1+2))$

Processing '2' -- Write to output

- Stack: / ((- *
- Output: 14 8 + 8 4 - * 6 2 2

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

Processing ')' -- Pop until you find '('

- Stack: / (
- Output: 14 8 + 8 4 - * 6 2 2 * -

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing '*' -- Push into stack

- Stack: / (*
- Output: 14 8 + 8 4 - * 6 2 2 * -

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

Processing '(' -- Push into stack

- Stack: / (* (
- Output: 14 8 + 8 4 - * 6 2 2 * -

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing '1' -- Write to output

- Stack: / (* (
- Output: 14 8 + 8 4 - * 6 2 2 * - 1

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

Processing '+' -- Push into stack

- Stack: / (* (+
- Output: 14 8 + 8 4 - * 6 2 2 * - 1

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+\underline{2}))$$

Processing '2' -- Write to output

- Stack: / (* (+
- Output: 14 8 + 8 4 - * 6 2 2 * - 1 2

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing ')' -- Pop until you find '('

- Stack: / (*
- Output: 14 8 + 8 4 - * 6 2 2 * - 1 2 +

Infix to Postfix Conversion

Example-Continued

$(14+8)*(8-4)/((6-2*2)*(1+2))$

Processing ')' -- Pop until you find '('

- Stack: /
- Output: 14 8 + 8 4 - * 6 2 2 * - 1 2 + *

Infix to Postfix Conversion

Example-Continued

$$(14+8)*(8-4)/((6-2*2)*(1+2))$$

No more input -- Empty stack

- Stack:
- Output: 14 8 + 8 4 - * 6 2 2 * - 1 2 + * /