

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS General Certificate of Education Ordinary Level

| CANDIDATE NAME | | | | | |
|-------------------|--|--|---------------------|--|--|
| CENTRE NUMBER | | | CANDIDATE NUMBER | | |

7640942147

ADDITIONAL MATHEMATICS

4037/23

Paper 2

October/November 2011

2 hours

Candidates answer on the Question Paper.

No Additional Materials are required.

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.

| For Examiner's Use | | |
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Mathematical Formulae

For Examiner's Use

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$, $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$.

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n,$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$.

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$

 $\Delta = \frac{1}{2} bc \sin A$

| 1 | Solve t | the inec | mality | x(2x - | - 1) > | 15 |
|---|---------|----------|--------|--------|--------|----|



[3]

2 (i) Given that
$$y = (12 - 4x)^5$$
, find $\frac{dy}{dx}$.

[2]

(ii) Hence find the approximate change in y as x increases from 0.5 to 0.5 + p, where p is small.

| 3 | (i) | Find the coefficient of x^3 in the expansion of $(1 - 2x)^7$. |
|---|-----|--|
| | | |

For Examiner's Use

[2]

(ii) Find the coefficient of
$$x^3$$
 in the expansion of $(1 + 3x^2)(1 - 2x)^7$.

[3]

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4 Without using a calculator, find the positive root of the equation

$$(5 - 2\sqrt{2})x^2 - (4 + 2\sqrt{2})x - 2 = 0,$$

giving your answer in the form $a + b\sqrt{2}$, where a and b are integers.

[6]

| A school council of 6 people is to be chosen from a group of 8 students and 6 teachers. Calculate the number of different ways that the council can be selected if | | | | | | | |
|--|--|---|--|--|--|--|--|
| there are no restrictions, | [2] | | | | | | |
| there must be at least 1 teacher on the council and more students than teachers. | [3] | | | | | | |
| er the council is chosen, a chairperson and a secretary have to be selected from the 6 counbers. Calculate the number of different ways in which a chairperson and a secretary can be selected. | ncil | | | | | | |
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| | there are no restrictions, there must be at least 1 teacher on the council and more students than teachers. there must be at least 1 teacher on the council and more students than teachers. er the council is chosen, a chairperson and a secretary have to be selected from the 6 counbers. Calculate the number of different ways in which a chairperson and a secretary can be | there are no restrictions, [2] there must be at least 1 teacher on the council and more students than teachers. [3] er the council is chosen, a chairperson and a secretary have to be selected from the 6 council nbers. Calculate the number of different ways in which a chairperson and a secretary can be | | | | | |

6 (i) In the space below sketch the graph of y = |(2x+3)(2x-7)|.

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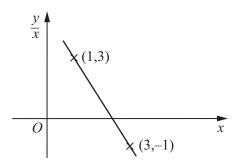
[4]

(ii) How many values of x satisfy the equation |(2x+3)(2x-7)| = 2x?

[2]







The variables x and y are related in such a way that when $\frac{y}{x}$ is plotted against x a straight line is obtained, as shown in the graph. The line passes through the points (1, 3) and (3, -1).

(i) Express y in terms of x.

(ii) Find the value of x and of y such that $\frac{y}{x} = -9$.

| 5 | A S | sector of a circle, of radius r cm, has a perimeter of 200 cm. | | | | | |
|---|------|--|-----|-----------------|--|--|--|
| | (i) | Express the area, $A \text{ cm}^2$, of the sector in terms of r . | [3] | Examiner Use | | | |
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| | (ii) | Given that r can vary, find the stationary value of A . | [3] | | | | |
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| 9 | An aircraft, whose speed in still air is $350 \mathrm{kmh^{-1}}$, flies in a straight line from A to B , a distance of $480 \mathrm{km}$. There is a wind of $50 \mathrm{kmh^{-1}}$ blowing from the north. The pilot sets a course of 130° . | | | | | | | |
|---|--|-----|--------------------|--|--|--|--|--|
| | 480 km. There is a wind of 50 kmh ⁻¹ blowing from the north. The pilot sets a course of 1 (i) Calculate the time taken to fly from <i>A</i> to <i>B</i> . | [5] | For Examiner's Use | | | | | |
| | (ii) Calculate the bearing of B from A . | [3] | | | | | | |

10 The line y = 2x + 10 intersects the curve $2x^2 + 3xy - 5y + y^2 = 218$ at the points A and B. Find the equation of the perpendicular bisector of AB. [9]

[9] For Examiner's Use

11 (i) Solve
$$4\cot \frac{1}{2}x = 1$$
, for $0^{\circ} < x < 360^{\circ}$.

[3] For Examiner's Use

(ii) Solve
$$3(1 - \tan y \cos y) = 5\cos^2 y - 2$$
, for $0^\circ < y < 360^\circ$.

[5]

(iii) Solve $3 \sec^2 z = 4$, for $0 < z < 2\pi$ radians.

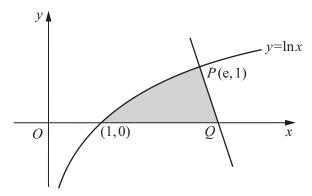
For Examiner's Use

[3]

12 Answer only **one** of the following two alternatives.

For Examiner's Use

EITHER



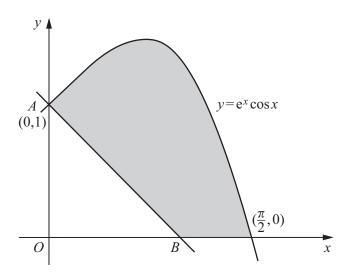
The diagram shows part of the curve $y = \ln x$ cutting the x-axis at the point (1, 0). The normal to the curve at the point P(e, 1) cuts the x-axis at the point Q.

(i) Show that
$$Q$$
 is the point $\left(e + \frac{1}{e}, 0\right)$. [4]

(ii) Show that
$$\frac{d}{dx}(x \ln x) = 1 + \ln x$$
. [1]

(iii) Hence find
$$\int \ln x dx$$
 and the area of the shaded region. [5]

OR



The diagram shows part of the curve $y = e^x \cos x$, cutting the *x*-axis at the point $\left(\frac{\pi}{2}, 0\right)$. The normal to the curve at the point A(0, 1) cuts the *x*-axis at the point *B*.

(i) Find the coordinates of
$$B$$
. [4]

(ii) Show that
$$\frac{d}{dx} [e^x (\cos x + \sin x)] = 2e^x \cos x$$
. [2]

(iii) Hence find
$$\int e^x \cos x dx$$
 and the area of the shaded region. [4]

| Start your answer to Question 12 here. | | F |
|--|--------|-----------|
| Indicate which question you are answering. | EITHER | Exam U |
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