

# UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

#### **CAMBRIDGE INTERNATIONAL MATHEMATICS**

0607/06

Paper 6 (Extended)

For Examination from 2010

SPECIMEN MARK SCHEME

1 hour 30 minutes

**MAXIMUM MARK: 40** 



### **TYPES OF MARK**

- **M** marks are given for a correct method.
- A marks are given for an accurate answer following a correct method.
- **B** marks are given for a correct statement or step.
- **D** marks are given for clear and appropriately accurate drawing.
- P marks are given for accurate plotting of points.
- E marks are given for correctly explaining or establishing a given result.
- C marks are given for clear communication (Papers 5 and 6 only).
- **R** marks are given for appropriate reasoning (Papers 5 and 6 only).

#### **ABBREVIATIONS**

- ft Follow throughoe Or equivalentsoi Seen or implied
- www Without wrong working

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## A Investigation

1	(a)	$\frac{3}{24} + \frac{4}{24} = \frac{7}{24}$	AR1	(both accuracy & reasons are required)
	(b)	$\frac{2}{12} + \frac{3}{12} = \frac{5}{12}$	AR1	
2	(a)	$\frac{1}{3} + \frac{1}{6} = \frac{2}{6} + \frac{1}{6} = \frac{3}{6} = \frac{1}{2}$	R1	
	(b)	$\frac{1}{3} = \frac{1}{4} + \frac{1}{12}$	B1	
	(c)	$\frac{1}{4} = \frac{1}{5} + \frac{1}{20}$	B2	
		$\frac{1}{5} = \frac{1}{6} + \frac{1}{30}$ 1 1 1	B1	for three correct
		$\frac{1}{6} = \frac{1}{7} + \frac{1}{42}$ $= \frac{1}{8} + \frac{1}{56}$		
	(d)	$\frac{1}{99} = \frac{1}{100} + \frac{1}{9900}$	B1	
	(e)	$\frac{1}{n} = \frac{1}{n+1} + \frac{1}{n(n+1)}$	B2	B1 for $\frac{1}{x} + \frac{1}{nx}$
3	(a)	$\frac{2}{3} = 2 \times \frac{1}{3} = 2\left(\frac{1}{4} + \frac{1}{12}\right) = \frac{2}{4} + \frac{2}{12} =$	R2	
		$\frac{1}{2} + \frac{1}{6}$		
	(b) (i)	$\frac{2}{5} = 2\left(\frac{1}{6} + \frac{1}{30}\right) = \frac{1}{3} + \frac{1}{15}$	AR1	
	(ii)	$\frac{2}{7} = 2\left(\frac{1}{8} + \frac{1}{56}\right) = \frac{1}{4} + \frac{1}{28}$	AR1	
	(c) (i)	$\frac{2}{5} = 2\left(\frac{1}{6} + \frac{1}{30}\right) = \frac{1}{3} + \frac{1}{15}$ $\frac{2}{7} = 2\left(\frac{1}{8} + \frac{1}{56}\right) = \frac{1}{4} + \frac{1}{28}$ $\frac{3}{8} = 3\left(\frac{1}{9} + \frac{1}{72}\right) = \frac{1}{3} + \frac{1}{24}$	AR1	
	(ii)	$\frac{4}{11} = 4\left(\frac{1}{12} + \frac{1}{132}\right) = \frac{1}{3} + \frac{1}{33}$	AR1	

4	(a)		Multiply $\frac{a}{xy} = \frac{1}{kx} + \frac{1}{ky}$ by $kxy$ $\frac{akxy}{xy} = \frac{kxy}{x} + \frac{kxy}{y}  (M1) \Rightarrow ak = y + x$ $\Rightarrow k = \frac{x+y}{a}$	M1	
	(b)	<b>(i)</b>	$\frac{1}{6} + \frac{1}{10} = \frac{5}{30} + \frac{3}{30} = \frac{8}{30} = \frac{4}{15}$	C1	
			$x = 3$ and $y = 5$ (or vice versa) in which case $k = \frac{5+3}{4} = 2$	B1	
		(iii)	$x = 1$ and $y = 15$ (or vice versa) in which case $k = \frac{15+1}{4} = 4$ and $\frac{4}{15} =$		
			$\frac{1}{4} + \frac{1}{60}$	B2	
5			Taking $x = 1$ and $y = 20$ gives $k = 7$ and $\frac{3}{20} = \frac{1}{7} + \frac{1}{140}$	B1	
			Taking $x = 2$ and $y = 10$ gives $k = 4$ and $\frac{3}{20} = \frac{1}{8} + \frac{1}{40}$	B1	
			Taking $x = 4$ and $y = 5$ gives $k = 3$ and $\frac{3}{20} = \frac{1}{12} + \frac{1}{15}$	B1	

6 (a)	$1 = \frac{1}{2} + \frac{1}{2} = \frac{1}{2} + \frac{1}{3} + \frac{1}{6} \text{ using the}$ pattern in part 2. $1 = \frac{1}{2} + \frac{1}{4} + \frac{1}{4}$	B1	
(b)	In the first result, breaking down $\frac{1}{3}$	B1	no penalty if missing
	gives $1 = \frac{1}{2} + \frac{1}{4} + \frac{1}{12} + \frac{1}{6}$ breaking down $\frac{1}{6}$ gives $1 = \frac{1}{2} + \frac{1}{3} + \frac{1}{3}$	B1	
	$\frac{1}{7} + \frac{1}{42}$ <b>OR</b> $1 = \frac{1}{2} + \frac{1}{3} + \frac{1}{10} + \frac{1}{15}$ using the method	B1	
	in question 4, with $x = 2$ and $y = 3$ . In the second result, breaking down $\frac{1}{4}$ gives $1 = \frac{1}{2} + \frac{1}{4} + \frac{1}{5} + \frac{1}{20}$	B1	
	For clear communication and reasoning throughout part <b>A</b> award C2		

Total: 31 marks scaled down to 25.

## **B** Modelling

1			Suitable scales chosen Correct plots	D1D1 P2	P1 for 1 or 2 incorrect.
2	(a)		T = 40 is incorrect. It should be 36.	B1	
	(b)		T = 0.3 S	M1 A1	correct form
3			$n = 2$ $B = 0.01 S^2$	B1 A1	
4	(a)		$D = 0.3S + 0.01 S^2$	B1	
	<b>(b)</b>	(i)	40 metres	A1A1	(units required)
		(ii)	At 30 km/h $D = 18$ metres	A1	
			% reduction = $\frac{22}{40}$ = 55%.	A1	(follow through)
5	(a)		braking distance = $180$ – thinking distance at $100$ km/h = $180 - 30 = 150$ metres. So $k 100^2 = 150 \Rightarrow k = 0.015$ $D = 0.3S + 0.015$ $S^2$	M1 A1	
	<b>(b)</b>		Solve $0.3S + 0.015$ $S^2 = 88$ 67.2 km/h using graphics calculator.	M1 A1	
			For clear communication and reasoning throughout part <b>B</b> award C2.		

Total: 20 marks scaled down to 15.

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