

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS General Certificate of Education Ordinary Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

6260308166

ADDITIONAL MATHEMATICS

4037/12

2 hours

Paper 1 May/June 2012

Candidates answer on the Question Paper.

No Additional Materials are required.

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.

For Examiner's Use				
1				
2				
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12				
Total				

Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n,$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$

$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2} bc \sin A$$

1 (i) Find
$$\int \sqrt{7x-5} \, dx$$
.

(ii) Hence evaluate
$$\int_{2}^{3} \sqrt{7x-5} \, dx$$
.

	4		
2	Using the substitution $u = 2^x$, find the values of x such that	$2^{2x+2} = 5(2^x) - 1.$ [5]	For Examiner's Use

3 Show that $\cot A + \frac{\sin A}{1 + \cos A} = \csc A$.

[4] For Examiner's Use

4 Solve the simultaneous equations 5x + 3y = 2 and $\frac{2}{x} - \frac{3}{y} = 1$.

For Examiner's Use

[5]

5 Differentiate the following with respect to x.

(i)
$$(2-x^2)\ln(3x+1)$$

[3]

$$(ii) \quad \frac{4 - \tan 2x}{5x}$$

6 You must not use a calculator in this question.

(i)	Express $\frac{8}{\sqrt{3}+1}$	in the form	$a(\sqrt{3}-1)$, where a	is an	integer
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For Examiner's Use

[2]

An equilateral triangle has sides of length $\frac{8}{\sqrt{3}+1}$.

(ii) Show that the height of the triangle is $6 - 2\sqrt{3}$.

[2]

(iii)	Hence, or otherwise, integers.	find the area	of the trian	ngle in the	form $p\sqrt{3}$	– q, wł	nere p and	<i>q</i> are [2]	For Examiner's Use

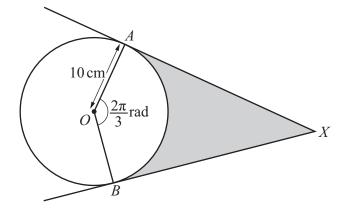
7	(i)	Sketch the graph of $y = x^2 - x - 6 $, showing the coordinates of the points w	where the curve
		meets the coordinate axes.	[3]

For Examiner's Use

(ii) Solve
$$|x^2 - x - 6| = 6$$
.

[3]

For Examiner's Use



The figure shows a circle, centre O, with radius 10 cm. The lines XA and XB are tangents to the circle at A and B respectively, and angle AOB is $\frac{2\pi}{3}$ radians.

(i) Find the perimeter of the shaded region.

[3]

(ii) Find the area of the shaded region.

[4]

9 Variables N and x are such that $N = 200 + 50e^{\frac{x}{100}}$.

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(i) Find the value of N when x = 0.

[1]

(ii) Find the value of x when N = 600.

[3]

(iii) Find the value of N when $\frac{dN}{dx} = 45$.

[4] For Examiner's Use

10 (a) It is given that $f(x) = \frac{1}{2+x}$ for $x \neq -2$, $x \in \mathbb{R}$.

(i) Find f''(x).

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(ii) Find $f^{-1}(x)$.

[2]

[2]

(iii) Solve $f^2(x) = -1$.

[3]

(b) The functions g, h and k are defined, for
$$x \in \mathbb{R}$$
, by
$$g(x) = \frac{1}{x+5}, \ x \neq -5,$$
$$h(x) = x^2 - 1,$$

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$$k(x) = 2x + 1.$$

Express the following in terms of g, h and/or k.

(i)
$$\frac{1}{(x^2-1)+5}$$

(ii)
$$\frac{2}{x+5}+1$$

	16	
11	The point P lies on the line joining $A(-1, -5)$ and $B(11, 13)$ such that $AP = \frac{1}{3}AB$.	For Examiner's
	(i) Find the equation of the line perpendicular to AB and passing through P .	[5] Use
	The line perpendicular to AB passing through P and the line parallel to the x -axis passing through B intersect at the point Q .	gh
	(ii) Find the coordinates of the point Q .	[2]

(iii)	Find the area of the triangle <i>PBQ</i> .	[2]	For Examiner's
			Use

Answer only **one** of the following two alternatives.

For Examiner's Use

12 EITHER

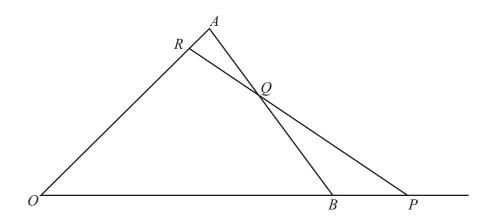
At 1200 hours, a ship has position vector $(54\mathbf{i} + 16\mathbf{j})$ km relative to a lighthouse, where \mathbf{i} is a unit vector due East and \mathbf{j} is a unit vector due North. The ship is travelling with a speed of $20 \,\mathrm{km} \,h^{-1}$ in the direction $3\mathbf{i} + 4\mathbf{j}$.

- (i) Show that the position vector of the ship at 15 00 hours is $(90\mathbf{i} + 64\mathbf{j})$ km. [2]
- (ii) Find the position vector of the ship t hours after 1200 hours. [2]

A speedboat leaves the lighthouse at 1400 hours and travels in a straight line to intercept the ship. Given that the speedboat intercepts the ship at 1600 hours, find

- (iii) the speed of the speedboat, [3]
- (iv) the velocity of the speedboat relative to the ship, [1]
- (v) the angle the direction of the speedboat makes with North. [2]

OR



The position vectors of points A and B relative to an origin O are \mathbf{a} and \mathbf{b} respectively. The point P is such that $\overrightarrow{OP} = \frac{5}{4} \overrightarrow{OB}$. The point Q is such that $\overrightarrow{AQ} = \frac{1}{3} \overrightarrow{AB}$. The point R lies on OA such that \overrightarrow{RQP} is a straight line where $\overrightarrow{OR} = \lambda \overrightarrow{OA}$ and $\overrightarrow{QR} = \mu \overrightarrow{PR}$.

- (i) Express \overrightarrow{OQ} and \overrightarrow{PQ} in terms of **a** and **b**. [2]
- (ii) Express \overline{QR} in terms of λ , **a** and **b**. [2]
- (iii) Express \overline{QR} in terms of μ , **a** and **b**. [3]
- (iv) Hence find the value of λ and of μ . [3]

Start your answer to Question 12 here.]	For
Indicate which question you are answering.	EITHER			Examiner's Use
marcute which question you are answering.	OR			
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Continue your answer here if necessary.	For
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