

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

9273068136

ADDITIONAL MATHEMATICS

0606/23

Paper 2

October/November 2011

2 hours

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.

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Total	

Mathematical Formulae

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1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} .$$

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n,$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$.

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2} bc \sin A$$

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1 Solve the inequality x(2x-1) > 15.

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[3]

[2]

2 (i) Given that $y = (12 - 4x)^5$, find $\frac{dy}{dx}$.

(ii) Hence find the approximate change in y as x increases from 0.5 to 0.5 + p, where p is small.

3	(i)	Find the coefficient of x^3	in the expansion	of $(1 - 2)$	$(x)^{7}$.
•	(-)	- 1110 till Collision of #	THE COLO COMPANIES OF THE COLOR	or (r =	, .

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[2]

(ii) Find the coefficient of x^3 in the expansion of $(1 + 3x^2)(1 - 2x)^7$.

[3]

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4 Without using a calculator, find the positive root of the equation

[6]

$$(5 - 2\sqrt{2})x^2 - (4 + 2\sqrt{2})x - 2 = 0,$$

giving your answer in the form $a + b\sqrt{2}$, where a and b are integers.

A so	chool council of 6 people is to be chosen from a group of 8 students and 6 teachers. Calcumber of different ways that the council can be selected if	ılate	For Examine Use
(i)	there are no restrictions,	[2]	
(ii)	there must be at least 1 teacher on the council and more students than teachers.	[3]	
	er the council is chosen, a chairperson and a secretary have to be selected from the 6 cour mbers.	ıcil	
(iii)	Calculate the number of different ways in which a chairperson and a secretary can be selected.	[1]	

© UCLES 2011 0606/23/O/N/11 6 (i) In the space below sketch the graph of y = |(2x+3)(2x-7)|.

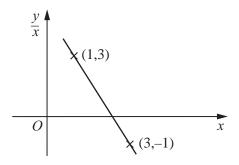
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[4]

(ii) How many values of x satisfy the equation |(2x+3)(2x-7)| = 2x?

[2]





The variables x and y are related in such a way that when $\frac{y}{x}$ is plotted against x a straight line is obtained, as shown in the graph. The line passes through the points (1, 3) and (3, -1).

(i) Express
$$y$$
 in terms of x .

[2]

(ii) Find the value of x and of y such that
$$\frac{y}{x} = -9$$
.

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8	A sector of a circle, of radius r cm, has a perimeter of 200 cm.							
	(i)	Express the area, $A \text{ cm}^2$, of the sector in terms of r .	[3]	Examiner's Use				
	(;;)	Civan that a con year, find the stationary value of A	г 2 1					
	(ii)	Given that r can vary, find the stationary value of A .	[3]					

		10		
9	An 480	aircraft, whose speed in still air is $350 \mathrm{kmh^{-1}}$, flies in a straight line from <i>A</i> to <i>B</i> , a distance km. There is a wind of $50 \mathrm{kmh^{-1}}$ blowing from the north. The pilot sets a course of 130° .	of For Examine Use	er's
	(i)	Calculate the time taken to fly from <i>A</i> to <i>B</i> .	5]	
	(ii)	Calculate the bearing of <i>B</i> from <i>A</i> .	3]	

© UCLES 2011 0606/23/O/N/11 10 The line y = 2x + 10 intersects the curve $2x^2 + 3xy - 5y + y^2 = 218$ at the points A and B. Find the equation of the perpendicular bisector of AB. [9]

11 (i) Solve
$$4\cot\frac{1}{2}x = 1$$
, for $0^{\circ} < x < 360^{\circ}$.

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[3]

(ii) Solve
$$3(1 - \tan y \cos y) = 5\cos^2 y - 2$$
, for $0^\circ < y < 360^\circ$.

[5]

© UCLES 2011 0606/23/O/N/11 (iii) Solve $3 \sec^2 z = 4$, for $0 < z < 2\pi$ radians.

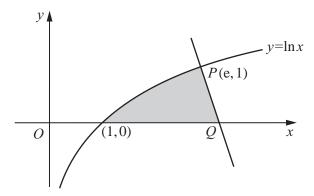
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[3]

12 Answer only **one** of the following two alternatives.

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EITHER



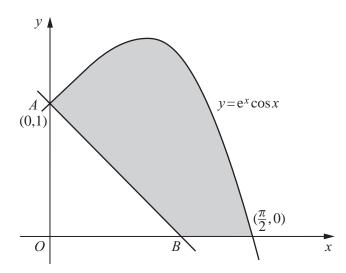
The diagram shows part of the curve $y = \ln x$ cutting the x-axis at the point (1, 0). The normal to the curve at the point P(e, 1) cuts the x-axis at the point Q.

(i) Show that
$$Q$$
 is the point $\left(e + \frac{1}{e}, 0\right)$. [4]

(ii) Show that
$$\frac{d}{dx}(x \ln x) = 1 + \ln x$$
. [1]

(iii) Hence find
$$\int \ln x dx$$
 and the area of the shaded region. [5]

OR



The diagram shows part of the curve $y = e^x \cos x$, cutting the *x*-axis at the point $\left(\frac{\pi}{2}, 0\right)$. The normal to the curve at the point A(0, 1) cuts the *x*-axis at the point B.

(i) Find the coordinates of
$$B$$
. [4]

(ii) Show that
$$\frac{d}{dx}[e^x(\cos x + \sin x)] = 2e^x \cos x$$
. [2]

(iii) Hence find
$$\int e^x \cos x dx$$
 and the area of the shaded region. [4]

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Start your answer to Question 12 here.				For
Indicate which question you are answering.	EITHER			Examiner's Use
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Continue your answer here if necessary.	For
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