UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS GCE Ordinary Level

MARK SCHEME for the October/November 2011 question paper for the guidance of teachers

4024 MATHEMATICS (SYLLABUS D)

4024/21 Paper 2, maximum raw mark 100

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

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Abbreviations

cao correct answer only cso correct solution only

dep dependent

ft follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

www without wrong working

soi seen or implied

| Qu | Answers | Mark | Part marks |
|----|--|------|--|
| 1 | (a) 3.64 | 2 | M1 for 10tan20 oe |
| | (b) 8.24 – 8.28 | 2ft | M1 for 10(tan50 – tan20) oe |
| | (c) 24.2, 24.3 | 3ft | M1 for $(PC =)$ $\frac{10}{\cos 20}$ oe $(= 10.64)$ and M1 for their (a) + 10 + their PC |
| 2 | (a) $0 - \frac{7}{3}$ oe isw | 2 | B1 for one correct |
| | (b) $x = 1$ $y = -\frac{1}{2}$ oe (c) $\frac{6p + 23}{(p-2)(2p+3)}$ final Ans | 3 | B2 for one correct www or M1 for reaching such as $hx = 11, 11x = k$, or $py = -22, 44y = q$ M1 for $\frac{5(2p+3)-4(p-2)}{(p-2)(2p+3)}$ soi and A1 for numerator $10p+15-4p+8$, |
| | (d) $\frac{q+1}{2q-1}$ final Ans | 3 | condoning one sign error, and correct denominator seen at some stage B1 for $(q-1)(q+1)$ seen and B1 for $(2q-1)(q-1)$ seen |
| 3 | (a) 60 alternate angles | 1 | |
| | (b) (i) 130 | 1 | |
| | (ii) 310 | 1 | |
| | (iii) 250 | 1ft | ft 360 – (their (a) + 50) or their (b)(ii) – their (a) |
| | (c) (i) Triangles equiangular | 1 | |
| | (ii) 51 | 3 | M2 for $\frac{TQ}{85 - TQ} = \frac{3}{2}$ oe or M1 for $\frac{TQ}{TR} = \frac{3}{2}$ oe |

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| | | | T |
|---|--------------------------------------|-----|---|
| 4 | (a) (i) $\frac{1}{5}$ oe | 1 | |
| | (ii) 1 oe | 1 | |
| | (b) (i) Correct completion | 2 | B1 after up to 3 errors |
| | (ii) (a) 0 | 1ft | ft from their table |
| | (b) $\frac{6}{25}$ oe | 1ft | Both fts dep on at least B1 scored in (b)(i) |
| | (c) $\frac{1}{25}$ | 2 | B1 for $5 \times 5 \times 5$ soi |
| 5 | (a) Convincing explanation | 1 | |
| | (b) (i) $4(\pi)$ | 1 | |
| | (ii) $\frac{3}{4}$ | 2ft | B1 for 3π |
| | 4 | | |
| | (c) (i) 75.4 | 2 | M1 for $\frac{60}{360} \times \pi \times (\text{their } r)^2$ |
| | (ii) 45.7 | 3 | M1 for $\frac{1}{2} \times 6 \times 6 \times \sin 60$ or $\frac{1}{2} \times \pi \times 3 \times 3$ and M1 for their 75.4 – their $\frac{1}{2} \times 6 \times 6 \times \sin 60$ – their $\frac{1}{2} \times \pi \times 3 \times 3$ evaluated |
| 6 | (a) (i) 3:5 | 1 | |
| | (ii) 9 600 | 1 | |
| | (iii) 20 000 | 2 | M1 for ÷ figs 1125 oe |
| | (b) (i) 252.48 | 1 | |
| | (ii) 110.8(0) | 2 | M1 for $395 + kx = 3054.20$ soi |
| | (iii) 33.4 | 2 | M1 for ÷ figs 2395 soi |
| 7 | (a) (i) Congruency case complete www | 3 | D1 for common angle of 60 and S1 for $AP=BQ=CR$ or $AR=BP=CQ$ |
| | (ii) (a) $\frac{16}{25}$ oe | 1 | |
| | (b) $\frac{3}{25}$ oe | 1 | |

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| | (b) (i) Angle in a semicircle oe | 1 | |
|---|---|-----|--|
| | (ii) Equal arcs or equal chords subtend equal angles at the circumference | 2 | B1 for $AB = BC$ |
| | (iii) (a) 45 | 1 | |
| | (b) 135 | 1ft | ft 3 × their (a) |
| | (iv) 98 | 2 | B1 for an angle correctly identified as 37°, 53° or 127° |
| 8 | (a) 8 correct plots joined | 2 | P1 for at least 5 correct plots joined |
| | (b) 5.5 – 7.5 | 2 | M1 for a correct tangent |
| | (c) (i) Correct line | 2 | L1 for correct freehand line or a ruled line with gradient – 1 or intercept 2 |
| | (ii) 1.3 | 1ft | |
| | (iii) $B = 4$ $C = 5$ | 3 | B2 for one correct www or |
| | | | $\mathbf{M1} \text{ for } 2x - \frac{5}{2x} = 2 - x \text{ soi}$ |
| | (d) (i) Convincing demonstration | 1 | |
| | (ii) Correct completion of graph | 1 | |
| 9 | (a) 122 working seen www | 4 | M1 for $\frac{\sin ABC}{11} = \frac{\sin 25}{5.5}$ and further M1 for $\sin ABC = \frac{11\sin 25}{5.5}$ |
| | | | M1 for $\sin ABC = \frac{11 \sin 25}{5.5}$ soi and A1 for 58 or B1 for 180 – their 58 |
| | (b) (i) Correct equation derived www | 3 | M2 for $(12^2) = x^2 + (5+x)^2 - 2x(5+x)\cos 120$ or M1 for $(12^2) = x^2 + (5+x)^2 + 2x(5+x)\cos 120$ |
| | (ii) 4.276 and –9.276 final answer | 4 | B3 for one correct or both not or wrongly corrected or B1 for $p = -15$ and $r = 6$ and B1 for $q = 1653$ or $\sqrt{q} = 40.657$ or B1 for $\left(x + \frac{5}{2}\right)^{(2)}$ and B1 for $\frac{551}{12} = 45.916$ or 6.776 |

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| | (iii) 93 | 1ft | ft from their positive root in (ii) |
|----|--|-----|---|
| 10 | (a) Correct histogram | 3 | H2 for at least 4 correct columns or H1 for 1 correct column |
| | | | For wrong or no vertical scale award SC2 for all heights correct and all widths correct SC1 for all heights correct or all widths correct |
| | (b) (i) 35 65 100 128 | 1 | |
| | (ii) Correct curve | 3 | P2 for 7 correct ft plots or PC2 for 4 correct ft plots and curve or P1 for 4 correct ft plots |
| | (c) (i) (51) | 1ft | |
| | (ii) (10) | 2ft | B1 for reading from the graph at 105 |
| | (d) (16.5) | 2ft | B1 for reading from the graph at 30 |
| 11 | (a) (i) (a) (-2,3) | 1 | |
| | (b) (-3,2) | 1ft | |
| | (c) (-3,2) | 2 | B1 for one coordinate correct |
| | (ii) (a) $\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$ | 1 | |
| | (b) M _y | 1 | |
| | (b) (i) 5 | 1 | |
| | (ii) 5 | 2 | B1 for $\sqrt{(4-7)^2 + (4-8)^2}$ |
| | (iii) (a) (0, 2) | 2 | M1 for appropriate perpendicular bisectors |
| | (b) 307 | 1 | |