

## UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS General Certificate of Education Ordinary Level

CANDIDATE NAME					
CENTRE NUMBER		I .	NDIDATE JMBER		
	 			400	A 14 4

# 241476782

#### MATHEMATICS (SYLLABUS D)

4024/11

Paper 1 October/November 2010

2 hours

Candidates answer on the Question Paper.

Additional Materials: Geometrical instruments

#### **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown in the space below that question. Omission of essential working will result in loss of marks.

### NEITHER ELECTRONIC CALCULATORS NOR MATHEMATICAL TABLES MAY BE USED IN THIS PAPER.

The number of marks is given in brackets [ ] at the end of each question or part question. The total of the marks for this paper is 80.

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This document consists of 20 printed pages.



## NEITHER ELECTRONIC CALCULATORS NOR MATHEMATICAL TABLES MAY BE USED IN THIS PAPER.

For Examiner's Use

1	(a)	Evaluate	35 -	- 27 3

Answer (a) .....[1]

**(b)** Evaluate  $1.3 \times 0.03$ .

*Answer* (b) .....[1]

**2** (a) Evaluate  $\frac{1}{3} + \frac{3}{7}$ .

Answer (a) .....[1]

**(b)** Evaluate  $2 \div 2\frac{2}{3}$ .

*Answer* (b) .....[1]

3	(a)	Express 60% as a fraction, giving your answer in	n its lowest terms.	For Examiner's
				Use
			Answer (a)[1]	
	(b)	The mass of a jar and its contents is 1.6 kg. The contents have a mass of 875 grams.		
		Calculate the mass, in grams, of the jar.		
			Answer (b) g [1]	
_		7. 1		-
4	(a)	Evaluate $4^0 + 4^1$ .		
			Answer (a)[1]	
	(b)	Evaluate $\left(\frac{1}{4}\right)^{-2}$ .		
	()	(4)		
			Answer (b)[1]	
_				

5	(a)	In the diagram in the answer space, two small squares are shaded.
		Shade one more small square, so that the figure will then have one line of symmetry.
		Answer (a) [1]
	(b)	In the diagram in the answer space, two small triangles are shaded.
		Shade four more small triangles, so that the figure will then have rotational symmetry of order 3.
		Answer (b) [1]
6	The	length of a side of an equilateral triangle is given as 41 mm, correct to the nearest millimetre.
Ü		Write down the lower bound for the length of a side.
	(b)	Answer (a) mm [1] Giving your answer in <b>centimetres</b> , calculate the lower bound for the perimeter of the triangle.
		Answer (b) cm [1]

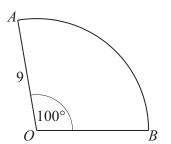
7	y varies inversely as the square of x. Given that $y = 4$ when $x = 3$ , find the value of y when $x = 2$ .	For Examiner's Use
	$Answer y = \dots [2]$	
8	By writing each number correct to one significant figure, estimate the value of	
	$\frac{0.387 \times 7.03^2}{\sqrt[3]{8.11}}  \cdot$	
	Answer[2]	

9	(a)	Solve the inequality $18 - 3x < x$ .	For Examine Use
		Answer $(a) x$ [1]	
	(b)	Given that $n$ is an integer, where $-10 \le 3n < -3$ , find the possible values of $n$ .	
		Answer (b) $n =[1]$	
10	The	temperatures, in °C, at midnight on 12 consecutive days were	
		-1, $0$ , $-4$ , $1$ , $2$ , $-2$ $-1$ , $-3$ , $1$ , $2$ , $3$ , $2$ .	
	(a)	Find the mode of these temperatures.	
		Answer (a)°C [1]	
	(b)	Find the median of these temperatures.	
		Answer (b)°C [1]	

11	Tho	diagram shows throu parallal lines		
11		diagram shows three parallel lines. Find $x$ .		$ \begin{array}{c} 74^{\circ} \\ \hline  & \\  & \\$
	(b)	Find $y$ .	Answer	(a) $x = \dots [1]$
	(c)	Find $z$ .	Answer	(b) y =[1]
12	(a)	Remove the brackets and simplify $4(7x-3) - 3(5x-3)$		$(c) z = \dots [1]$
	(b)	Express as a single fraction in its simplest form $\frac{4}{3y}$		(a)[1]
	(c)	Simplify $(4a^2b) \times (3ab^3)$ .	Answer	( <i>b</i> )[1]
			Answer	(c)[1]

13	(a)	Factorise completely $16a^2 - 6a$ .	
			( )
			Answer (a)[1]
	<b>(b)</b>	Factorise completely $6x + 3xy - 4y - 8$ .	
			Answer (b)[2]
14	The Wri	e speed of light is given as $3 \times 10^5$ km/s. ting each answer in standard form, calculate	
	(a)	the distance, in kilometres, that light travel	s in one minute,
			Answer (a) km [1]
	<b>a.</b> )		
	(D)	the time, in seconds, that light takes to trav	ei 130km.
			Answer (b) seconds [2]

15 The diagram shows a sector of a circle, centre O. The radius of the circle is 9 cm and the sector angle is 100°. Taking the value of  $\pi$  to be 3.14, calculate



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(a) the length of the arc AB,

Answer (a) ...... cm [2]

**(b)** the perimeter of the sector.

Answer (b) ..... cm [1]

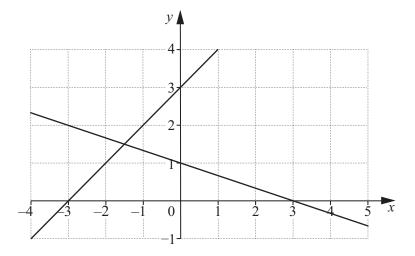
- 16 The lines 3y + x = 3 and y = x + 3 are shown in the diagram below.
  - (a) Find the gradient of the line 3y + x = 3.

Answer (a) .....[1]

**(b)** On the diagram shade, and label with the letter R, the region defined by the inequalities

$$3y + x \ge 3$$
,  $y \le x + 3$ ,  $x \ge 0$ .

Answer (b)



[2]

17 
$$\mathbf{A} = \begin{pmatrix} 4 & -3 & 0 \\ 0 & 6 & -2 \end{pmatrix}$$
  $\mathbf{B} = \begin{pmatrix} 5 & -4 & -1 \\ 0 & 6 & 2 \end{pmatrix}$   $\mathbf{C} = (2 \ 1)$ 

(a) Find 2A - B.

Answer 
$$(a)$$
 [2]

(b) Find CA.

Answer 
$$(b)$$
 [1]

18	Solve	the	simultaneous	equations
		ULIC	Difficulted as	o quatrons

x + 2y = 8,
$y = \frac{1}{3}x + 9$ .
$y = \frac{1}{3}x + 9$ .

Answer $x =$

$$y =$$
.....[3]

19 Two bags contain beads.

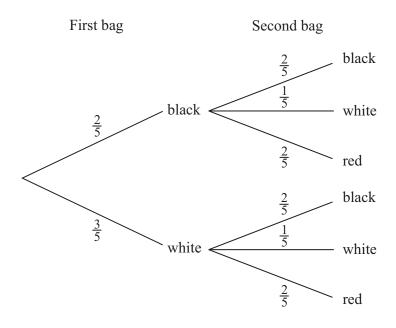
The first bag contains 2 black and 3 white beads.

The second bag contains 2 black, 1 white and 2 red beads.

A bead is taken, at random, from each bag.

The tree diagram that represents these outcomes is drawn below.





Giving each answer in its simplest form, find the probability that

(a) both beads are black,

*Answer* (a) ......[1]

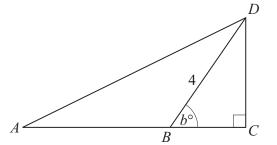
**(b)** both beads are red,

*Answer* (b) ......[1]

(c) exactly one bead is black.

Answer (c) .....[2]

20	M is the midpoint of the line joining $P$ and $Q$ .					
		R lies on $PQ$ produced, such that $PR = 3PQ$ . Find $PM : PR$ .		For Examiner's Use		
	(b)	P is $(1, -2)$ and $Q$ is $(5, 6)$ .  (i) Find the coordinates of $M$ .	Answer (a)[1]			
		(ii) The line $4x + ky + 10 = 0$ passes through $Q$ (5) Find the value of $k$ .	Answer (b)(i) () [1]			
			Answer (b)(ii) $k =$			



$\sin b^{\circ}$	$\cos b^{\circ}$	tan b°
0.85	0.53	1.6

In the diagram, ABC is a straight line. BD = 4 cm,  $B\hat{C}D = 90^{\circ}$  and  $C\hat{B}D = b^{\circ}$ .

Use as much information given in the table as is necessary to answer the following questions.

(a) Calculate the value of  $\sin A\hat{B}D + \cos A\hat{B}D$ .

Answer (a) .....[2]

**(b)** Calculate *BC*.

Answer (b) BC = .... cm [2]

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22 The grouped frequency table below shows the times taken for 70 students to solve a problem.

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Time (t minutes)	$0 < t \le 3$	$3 < t \le 4$	4 < t ≤ 5	$5 < t \le 6$	$6 < t \le 8$
Number of students	24	12	16	10	8

(a) Complete the cumulative frequency table for this information.

Answer (a)

Time (t minutes)	<i>t</i> ≤ 3	<i>t</i> ≤ 4	<i>t</i> ≤ 5	<i>t</i> ≤ 6	<i>t</i> ≤ 8
Number of students	24				

[1]

**(b)** In which group of the frequency table does the 40th percentile lie?

*Answer* (b) ......[1]

**(c)** Complete the frequency density table for this information.

Answer (c)

Time (t minutes)	$0 < t \le 3$	3 < t ≤ 4	4 < t ≤ 5	5 < t ≤ 6	6 < t ≤ 8
Frequency density	8	12	16		

[2]

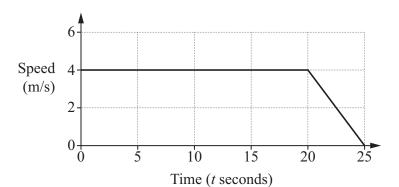
		1	6	
23	Look at this pattern.			For
		$2^2 - 0^2 =$	= 4×1	Examiner's Use
		$3^2 - 1^2 =$	= 4×2	
		$4^2 - 2^2 =$	= 4×3	
		$5^2 - 3^2 =$	= 4×4	
	(a) Write down the 7th line of	the pattern.		
	Answer (a)		[:	]
	<b>(b)</b> Write down the <i>n</i> th line of	the pattern.		
	Answer (b)		[	1]
	(c) Use the pattern to find 52	$21^2 - 519^2$ .		
			Answer (c)[	
	(d) Use the pattern to find the	nositive integers	x and y such that $x^2 - y^2 = 484$ .	
	()	F		

Answer (d)  $x = \dots$ 

*y* = .....[1]

	Ans	wer (a)		
				[2]
(b)			onto triangle $C$ by a rotation, centre the origin, through 90° anticles $C$ and $C$ and $C$ are $C$ are $C$ and $C$ are $C$	ockwise
	(i)		, triangle $C$ on the diagram.	
		Answer (b)(i)		
			3	
			2	
			$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
			-3	
			ii	[1]
	(ii)	Write down the	matrix that represents this transformation.	
	( )		The state of the s	
			Answer (b)(ii)	[1]

25



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The diagram is the speed-time graph of the last 25 seconds of a car's journey. From t = 0 to t = 20 the car moves with a constant speed of 4 m/s. From t = 20 to t = 25 the car moves with a constant retardation.

(a) Calculate the retardation when t = 22.5.

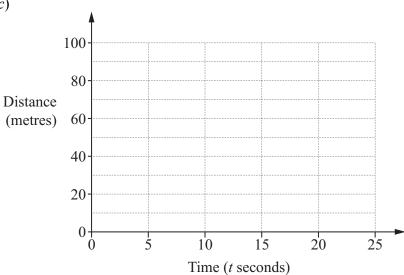
Answer	(a)	 $m/s^2$	Г17
Answer	( u )	 111/5	1

**(b)** Show that the distance travelled during the 25 seconds is 90 m.

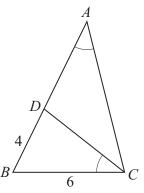
Answer (b)	
	Г11

(c) On the grid below, draw the distance-time graph for the 25 seconds.

Answer(c)



[2]



The diagram shows triangle ABC. D is the point on AB such that  $B\hat{C}D = B\hat{A}C$ .

(a)	Explain why triangle $ABC$ is similar to triangle $CBD$ .
	Answer (a)
	[1]

**(b)** Given that BD = 4 cm and BC = 6 cm, calculate AD.

Answer (b) AD = .... cm [3]

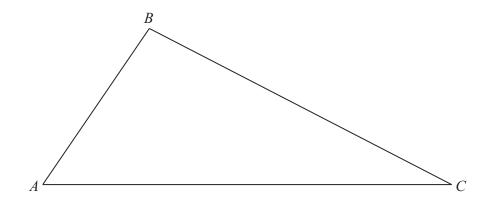
Question 27 is printed on the following page

- 27 The diagram below shows triangle *ABC*.
  - (a) Measure  $A\hat{B}C$ .

Answer (a) 
$$A\hat{B}C = \dots$$
 [1]

- (b) On the diagram, construct the locus of points inside the triangle that are
  - (i)  $8 \operatorname{cm} \operatorname{from} C$ ,
  - (ii) equidistant from AB and AC. [1]
- (c) On the diagram, shade the region inside the triangle containing the points that are more than 8 cm from C and nearer to AB than to AC.

Answer (b),(c)



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