

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS General Certificate of Education Ordinary Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		



STATISTICS 4040/22

Paper 2 October/November 2011

2 hours 15 minutes

Candidates answer on the question paper.

Additional Materials: Mathematical tables

Pair of compasses

Protractor

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a soft pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions in Section A and not more than four questions from Section B.

If working is needed for any question it must be shown below that question.

The use of an electronic calculator is expected in this paper.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.



Section A [36 marks]

Answer all of the questions 1 to 6.

A college has asked a statistician to carry out a survey of its catering facilities. As part of his survey the statistician measures the time that students, chosen randomly, spend in a queue in the refectory, from the moment they join the queue until the moment they leave the serving area. The following times, **in completed minutes**, are those recorded for twelve of the chosen students.

7 8 7 0 1 1 6 5 3 7 4 6

For	each of the following state whether it is true or false about this sample of data.
(i)	The mode of the times is 8 minutes.
	[1]
(ii)	The median time is 5.5 minutes.
	[1]
(iii)	The range is a suitable measure of dispersion for this data.
	[1]
(iv)	The mean waiting time is 5 minutes.
	[1]
(v)	The mean waiting time is 4.58 minutes (to 2 decimal places).
	[1]
(vi)	The value 0 must be incorrect because a person has to spend at least a short time being served.
	[1]

2

(a)	Give	e a brief explanation of each of the following terms in the context of moving averages.
	(i)	Time series
		[1]
((ii)	Seasonal variation
		[1]
(iii)	Trend
		[1]
(b)	(i)	Give an example of a variable which you would expect to be subject to seasonal variation.
		[1]
((ii)	State what would be a 'season' for your chosen variable.
		[1]
(iii)	State, with a reason, whether moving average values based on your chosen variable would need to be centred.
		[1]

3 The following table gives the exchange rates between the United States dollar and a number of other currencies on 1 January 2009, and on 1 January 2010. For example, on 1 January 2009, one dollar could be exchanged for 0.690 pounds. The final column of the table is to show the percentage change in each exchange rate between the two dates.

Currency	Exchange rate on 1/1/09	Exchange rate on 1/1/10	Percentage change in exchange rate
Pound	0.690	0.620	-10.1
Yen	90.459	92.586	+2.4
Euro	0.712	0.696	
Rupee	49.900	46.899	
Rouble	29.158	30.314	

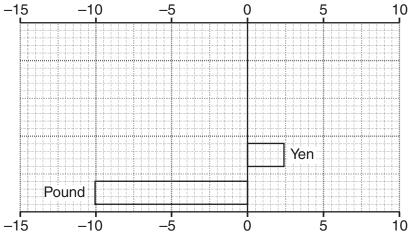
(i) Give the calculations to show that the percentage change in the pound exchange rate is -10.1%.

[1]

(ii) Calculate the percentage changes in the exchange rates of each of the euro, rupee and rouble, and insert them in the table.

[1]

(iii) Complete the change chart below to illustrate the percentage changes for all five currencies.



Percentage change in exchange rates 2009–2010

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1	_	п
L	_	J.

(iv) Give one advantage and one disadvantage of displaying data in a change chart.

Advantage	
Disadvantage	
	ro.
	[2]

4 Values of a variable, *Y*, were measured for each of the four quarters of three consecutive years. Using these measurements, values of an appropriate centred moving average were calculated. These were, in turn, used to estimate the four seasonal components, and to draw the trend line of values of *Y* from which the seasonal components had been removed.

The estimated seasonal components are given in the following table.

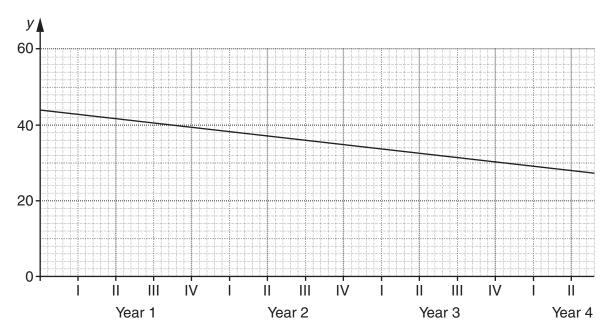
Season	I	II	III	IV
Seasonal Component	12	q	-16	-2

(i)	State, giving a reason, whether you would expect the value of Y for quarter III of any year to
	be above or below the trend line.

	[0]

(ii) Find the value of q.

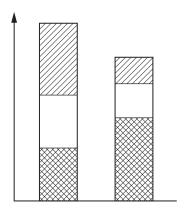
The grid below shows the graph of the trend line.



(iii) Use the graph to estimate the value of Y for quarter I of year 4.

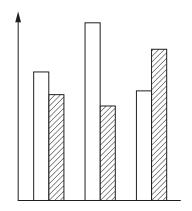
.....[2]

5 (i) Name the type of bar chart illustrated in the diagram below.



	1	1		
--	---	---	--	--

(ii) Name the type of bar chart illustrated in the diagram below.



[1]

(iii) Both diagrams are incomplete. List four items of information which need to be added to each of them to make them meaningful.

1	
2	

(iv)	A diagram of the type in part (ii) is to illustrate the quantities of different blends of tea drunk in the United Kingdom in three consecutive years. State one advantage and one disadvantage of using this type of diagram for this purpose.
	Advantage
	Disadvantage
	[2]

6 The table below shows the marks obtained in two tests, Mathematics and Statistics, by each of two students, Peter and John. It also shows the mean and the standard deviation of the marks in these two tests of all the students in the class of which Peter and John are members.

	Mathematics	Statistics				
Peter	40	43				
John	30	48				
Class mean	20	44				
Class standard deviation	10	4				

	9		
The marks in both subjects are to b	pe scaled to a mean of	f 50 and a standa	rd deviation of 16.
(i) Obtain the scaled marks for to suitable table.			
			[4]
Each student's total mark is obtained	ed by adding the two t	est marks togethe	er.
(ii) Show that one student has the mark.	e higher total raw mark	, but the other ha	s the higher total scaled
(iii) Explain briefly what has cause	ed the situation describ	oed in part (ii) .	[1]

Section B [64 marks]

Answer not more than **four** of the questions 7 to 11.

Each question in this section carries 16 marks.

7	In a game, a player throws an unbiased dice, with faces numbered 1, 2, 3, 4, 5 and 6, three times
	On any throw, if the number on the upper face is 6, or if the number on the upper face on the
	previous throw was 6, then she scores the number on the upper face, otherwise she scores 0. The
	player's total is then the sum of her three scores.

	,											
For	example,											
	the sequence	6	1	6	gives a total of $0+6+3=9$, gives a total of $6+1+6=13$, gives a total of $6+2+0=8$.							
Pos	ssible totals are	0, a	nd a	all ir	ntegers from 6 to 18 inclusive.							
(i)	State one poss	sible	e se	que	ence of three throws which would give a total of 0.							
					[1]						
(ii)	(ii) Calculate the probability that a player's total is 0.											
					[2	2]						
	•	-		_	ne once is \$1. A prize of \$8 is paid for a total greater than 15, an 10 and 15 inclusive. Nothing is paid for a total of less than 10.	C						

(iii) Calculate the probability of winning a prize of \$8.

.....[5]

The	e probability of failing to win a prize is $\frac{5}{6}$.
(iv)	Calculate, to the nearest cent, a player's expected profit or loss if she plays the game once.
	[6]
(v)	If the entry fee and other prizes remain unchanged, calculate, to the nearest cent, the prize which should be paid for a total of 10 to 15 inclusive to make the game fair.
	[2]

8 The table below shows, under five headings, the expenditure, to the nearest \$1000, of a small company in the year 2007, together with the price relatives in the year 2008 for the same headings, taking 2007 as the base year.

	2007 expenditure (\$'000)	2008 price relatives					
Wages	375	108.8					
Equipment	72	116.7					
Buildings	100	107.0					
Fuel	52	140.4					
Telephone	131	100.0					

(i)	State what can be deduced from the value of 100.0 for the telephone price relative.
	[1]
(ii)	Calculate, to 1 decimal place, an 'unweighted average of price relatives' index for 2008, taking 2007 as base year.
	Unweighted index =[2]
	Onweighted index =[2]
(iii)	Using the expenditure for 2007 as weights, calculate, to 1 decimal place, a weighted aggregate cost index for 2008.
	Weighted index =[5]

State, with a reason, which of the two indices you have calculated in parts (ii) and (iii) is more likely to reflect the actual increase in expenditure.												
[2]												
Use the total 2007 expenditure, and the two indices, to obtain an estimate, for each index, of the total 2008 expenditure.												
Estimate for unweighted index =												
Estimate for weighted index =[3]												
en the company's accounts for 2008 were published, they showed that actual expenditure in year had been \$807000.												
State, with a reason, whether this figure justifies your answer to part (iv).												
[1]												
Using the information in the table, suggest a reason why one of the two indices is far too high.												
[2]												

9	(a)	A st	andard pack of 52 playing cards is shuffled, and one card placed face down on a table.
		(i)	State the probability that this card is an ace.
			[1]
		You	are then told that this card is a heart.
		(ii)	What is now the probability that this card is an ace?
			[1]
		(iii)	State, with a reason, what the probabilities you have given in parts (i) and (ii) tell you about the events 'the card is an ace' and 'the card is a heart'.
		(iv)	State, with a reason, whether the events 'the card is an ace' and 'the card is a heart' are mutually exclusive.
			[2]
	(b)		events A and B are two possible outcomes of a statistical experiment such that $A = 0.7$, $A = 0.3$, $A =$
		(i)	State, with a reason, whether events A and B are mutually exclusive.

(ii)	State, with a reason, whether events A and B are independent.
	[2]
(iii)	Calculate the quantity $P(A \cup B)$, and interpret in words what it represents.
	[4]
(iv)	Calculate the quantity $P(A) + P(B) - 2P(A \cap B)$, and interpret in words what it represents.
	[2]

10	road transport and 10 on sea transport.																					
		have and										of the	se b	ooks	, but	have	only	enc	ough	res	ource	s of
	(i)	Stat	te t	he ı	num	ber	of bo	ooks	you v	would	d nee	d to	inclu	de in	your	samı	ole.					
																	[1]					
	(ii)	-							•			-				ed to o		ent t	type	s of t	transp	oort,
	boo sele	ks, a	ind aric	60 us :	to 6	9 to	the .Nu	sea mbei	boors ou	ks, a tside	nd a	re go	ing t	o use	e the	rand	om r	numb	oer t	table	the r below	w to
							٦	WO.	-DIGI	IT RA	ANDO	OM N	IUME	BER 1	ABL	E						
							20 87 02	74 99 33	21 19 45		30 30 55	25 95 41	38 39 85		83 13 10	39 04 36						
	(iii)	(a)									first r requi			table	e, and	d mov	ing a	along	g the	e row	ı, sele	ect a
																						[1]
		(b)			-	_				ur sa	mple) .									the t	
			••																			
	(iv)	A s	yst	em	atic	san	nple	is to	be s	elect	ted.											
		(a)		rite elec		n th	ne sr	nalle	st po	ssible	e and	d larg	est p	ossik	ole tw	o-dig	jit nu	mbe	rs of	f the	first b	ook
																						[1]

The systematic sample is selected by starting at the beginning of the second row of the table,

	and	moving along the row.
	(b)	Write down the number of the first book selected.
		[1]
	(c)	Write down the numbers of the other books selected for the systematic sample.
		[2]
(v)	A sa	ample stratified by type of transport is to be selected.
	(a)	State how many books on each type of transport would be selected for such a sample.
		[1]
	(b)	Starting at the beginning of the third row of the table, and moving along the row, select a sample stratified by type of transport. Use every number if the type of transport to which it relates has not yet been fully sampled.
		[4]
(vi)	•	lain whether or not the composition of the simple random sample you have selected in t (iii)(a) would give you cause for concern.
		IO.

11 This question must be answered by calculation; graphical solutions will not be awarded any marks.

The following table summarises the net value, in dollars, of the 690 orders received in one week by a mail order company. The net value is the total cost of the goods purchased before taxes and any other additional charges are added.

Net value of order (\$)	Number of orders	Cumulative frequency
5 – under 10	85	
10 – under 20	120	
20 – under 30	225	
30 – under 50	135	
50 – under 100	105	
100 – under 150	20	

(i)	Without carrying out any calculations, explain why the mean net value of these orders would be expected to be greater than the median.
	[2]
(ii)	State, with a reason, which measure of dispersion would be most appropriate to represent this data.
	[2]
(iii)	Calculate the cumulative frequencies, and write them in the third column of the above table.

[1]

	19
	cause it finds small orders uneconomic to process, the company is considering not accepting ers with a net value below \$12.50.
(iv)	Estimate, correct to 1 decimal place, the percentage of these orders which would not be accepted if this limit had been in place.
	[3]
	oucher giving a discount off a future order is included with the 15% of orders which have the nest net value.
(v)	Estimate, to the nearest cent, the lowest net value of these orders which will qualify for a voucher.

The gross value of an order is calculated by adding a tax of 20% to the net value, and **then** adding \$5 for packing and delivery.

(vi) (a) If the voucher were to be given to the 15% of orders with the highest gross value, estimate, to the nearest cent, the minimum gross value which would qualify for a voucher.

.....[2]

.....[4]

[Question 11 continues on the next page]

(b) The standard deviation of the net orders is \$26.04.

Estimate, to the nearest cent, the standard deviation of the gross orders.
[2

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