# Distributed algorithms

# Pierre Colson

# Wednesday 05 January 2022

# Contents

General	2
Failure Detector	2
Fair-loss Links	2
Stubborn Links	2
Reliable (Perfect) Links	2
Reliable Broadcast	3
Best-effort Broadcast (beb)	3
Reliable Broadcast (rb)	3
Uniform Reliable Broadcast (urb)	4
Causal Broadcast	4
Causality	4
Causal Broadcast	
Reliable Causal Broadcast (rcb)	
Uniform Causal Broadcast (ucb)	
Reliable Causal Order Broadcast (rco)	
Total Order Broadcast (to)	6
Consensus	7
Algorithm 1 (cons)	7
Algorithm 2 (ucons)	
Algorithm 3	
Shared Memory	9
Regular Register	9
Atomic Register	10
Terminating Reliable Broadcast (trb)	11
Terminating Remaine Broadcast (115)	
Non-Blocking Atomic Commit (nbac)	12
Group Menbership and View Synchronous Communication	13
Group Menbership (gmp)	13
View Synchrony (vsc)	14

 $\begin{tabular}{ll} \bf Markdown & verion & on $github$ \\ Compiled using $pandoc$ and $gpdf$ $script$ \\ \end{tabular}$ 

#### General

- The distributed system is made of a finite set of **processes**: each process models a **sequencial** program
- Every pair of processes is connected by a link through which the processes exchange messages
- Safety is a property which states that nothing bad should happen
- Liveness is a property which states that something good should happen
- Two kinds of failures are mainly considered
  - Omissions: The process omits to send messages it is supposed to send
  - Arbitrary: The process sends messages it is not supposed to send
- A **correct** process is a process that does not fail (that does not crash)

#### Failure Detector

- Indication : <Crash ,p>
- A **Failure detector** is a distributed oracle that provides processes with suspicions about crashed processes
  - It is implemented using timing assumptions
- Perfect Failure Detector :
  - Strong Completness: Eventually, every process that crashes is permanantly suspected by every other correct process
  - Strong Accuracy : No process is suspected before it crashes
- Eventually Perfect Failure Dectector :
  - Strong Completness
  - Eventually Strong Accuracy: Eventually, no correct process is ever suspected

#### Fair-loss Links

- FL1. Fai-loss: If a message is sent infinitely often by  $p_i$  to  $p_j$ n and neither  $p_i$  or  $p_j$  crashes then m is delivered infinitely often by  $p_j$
- FL2. Finite duplication: If a message m is sent a finite number if times by  $p_i$  to  $p_j$ , m is delivered a finite number of times by  $p_i$
- FL3. No creation: No message is delivered unless it was sent

#### Stubborn Links

- SL1. Stubborn delivery: If a process  $p_i$  sends a message m to a correct process  $p_j$ , and  $p_i$  does not crash, then  $p_i$  delivers m an infinite number of times
- SL2. No creation: No message is delivered unless it was sent

```
Implements: StubbornLinks (sp2p)
Uses : FairLossLinks (flp2p)
upon event <sp2pSend, dest, m> do
    while (true) do
    trigger <flp2pSend, dest, m>
upon event <flp2pDeliver, src, m> do
    trigger <sp2pDeliver, src, m>
```

#### Reliable (Perfect) Links

- PL1. Validity: If  $p_i$  and  $p_j$  are correct
- PL2. No duplication: No message is delivered (to a process) more than once
- PL3. No creation: No message is delivered unless it was sent
- Roughly speaking, reliable links ensure that messages exchanged between correct processes are not lost

```
Implements: PerfectLinks (pp2p)
Uses: StubbornLinks (sp2p)
upon event <Init> do delivered = emptySet
upon event <pp2pSend, dest, m> do
   trigger <sp2Send, dest, m>
upon event <sp2pDeliver, src, m> do
   if m not in delivered then
      trigger <pp2pDeliver, src, m>
   add m to delivered
```

### Reliable Broadcast

### Best-effort Broadcast (beb)

- **Request**: <bebBroadcast, m>
- Indication : <bebDeliver, src, m>
- BEB1. Validity: If  $p_i$  and  $p_j$  are correct then every message broadcast by  $p_i$  is eventually delivered by  $p_j$
- BEB2. No duplication: No message is delivered more than once
- BEB3. No creation: No messages is delivered unless it was broadcast

```
Implements: BestEffortBroadcast (beb)
Uses: PerfectLinks (pp2p)
upon event <bebBroadcast, m> do
    forall pi in S do
        trigger <pp2pSend, pi, m>
upon event <pp2pDeliver, pi, m> do
    trigger <dedDeliver, pi, m>
```

#### Reliable Broadcast (rb)

- Request : <rbBroadcast, m>
- Indication : <rbDeliver, src, m>
- RB1 = BEB1
- $\mathbf{RB2} = \mathrm{BEB2}$
- RB3 = BEB3
- **RB4.** Agreement: For any message m, if any correct process delivers m, then every correct process delivers m

```
Implements: ReliableBroadcast (rb)
Uses:
    BestEffortBroadcast (beb)
    PerfectFailureDetector (P)
upon event <Init> do
    delivered = emptySet
    correct = S
    forall pi in S do from[pi] = emptySet
upon event <rbBroadcast, m> do
    delivered = delivered U {m}
    trigger <rbDeliver, self, m>
    trigger <bbroadcast, [data, self, m]>
upon event <crash, pi> do
    correct = correct \{pi}
    forall [pj, m] in from[pi] do
```

```
trigger <bebBroadcast, [data, pj, m]>
upon event <bebDeliver, pi, [data, pj, m]> do
  if m not in delivered then
  delivered = delivered U {m}
  trigger <rbDeliver, pj, m>
  if pi not in correct then
    trigger <bebBroadcast, [data, pj, m]>
  else
    from[pi] = from[pi] U {[pj, m]}
```

#### Uniform Reliable Broadcast (urb)

- Request : <urbBroadcast, m>
- Indication : <urbDeliver, src, m>
- URB1 = BEB1
- URB2 = BEB2
- URB3 = BEB3
- URB4. Uniform Agreement: For any message m, if any process delivers m, then every correct process delivers m

```
Implements: UniformBroadcast (urb)
Uses:
  BestEffortBroadcast (beb)
 PerfectFailureDetector (P)
upon event <Init> do
  correct = S
  delivered = forward = emptySet
  ack[Message] = emptySet
upon event <urbBroadcast, m> do
  forward = forward U {[self, m]}
  trigger <bebBroadcast, [data, self, m]>
upon event <bebDeliver, pi, [data, pj, m] > do
  ack[m] = ack[m] U \{pi\}
  if [pi, m] not in forward then
    forward = forward U {[pj, m]}
    trigger <bebBroadcast, [data, pj, m]>
upon event (for any [pj, m] in forward) <correct in ack[m] > and <m not in delivered > do
  delivered = delivered U {m}
  trigger <urbDeliver, pj, m>
```

#### Causal Broadcast

- A **non-blocking** algorithm using the past
- A blocking algorithm using vector clocks

#### Causality

- Let  $m_1$  and  $m_2$  be any two messages:  $m_1 \to m_2$  ( $m_1$  causally precedes  $m_2$ ) iff
  - C1. Fifo order: Some process  $p_i$  broadcast  $m_1$  before broadcasting  $m_2$
  - C2. Local order: Some process  $p_i$  delivers  $m_1$  and then broadcast  $m_2$
  - C3. Transitivity: There is a message  $m_3$  such that  $m_1 \to m_3$  and  $m_3 \to m_2$

#### Causal Broadcast

- Request : <coBroadcast, m>
- Indication : <coDeliver, src, m>
- CO: If any process  $p_i$  delivers a message  $m_2$ , then  $p_i$  must have delivered every message  $m_1$  such that  $m_1 \to m_2$

### Reliable Causal Broadcast (rcb)

- $\bullet \ \ \mathbf{Request}: < \!\! \mathrm{rcoBroadcast}, \ m \!\! >$
- Indication : <rcoDeliver, src, m>
- RB1, RB2, RB3, RB4
- CO

### Uniform Causal Broadcast (ucb)

- Request : <ucoBroadcast, m>
- Indication : <ucoDeliver, src, m>
- URB1, URB2, URB3, URB4
- CO

### Reliable Causal Order Broadcast (rco)

```
Implements: ReliableCausalOrderBroadcast (rco)
Uses : ReliableBroadcast (rb)
upon event <Init> do
  delivered = past = emptySet
upon event <rcoBroadcast, m> do
 trigger <rbBroadcast, [data, past, m]>
  past = past U {[self, m]}
upon event <rbDeliver, pi [data, pastm, m]> do
  if m not in delivered then
   forall [sn, n] in pastm do
      if n not in delivered then
        trigger <rcoDeliver, sn, n>
        delivered = delivered U {n}
        past = past U {[self, n]}
    trigger <rcoDeliver, pi, m>
    delivered = delivered U {m}
    past = past U {[pi, m]}
```

```
Implements ReliableCausalOrderBroadcast (rco)
Uses: ReliableBroadcast (rb)
upon event <Init> do
    forall pi in S: VC[pi] = 0
    pending = emptySet
upon event <rcoBroadcast, m> do
    trigger <rcoDeliver, self, m>
    trigger <rbBroadcast, [data, VC, m]>
    VC[self] = VC[self] + 1
upon event <rbDeliver, pj, [data, VCm, m]> do
    if pj not self then
        pending = pending U (pj, [data, VCm, m])
        deliver-pending
procedure deliver-pending is
```

```
while (s, [data, VCm, m]) in pending do
  if forall pk: (VC[pk] >= VCm[pk]) do
  pending = pending - (s, [data, VCm, m])
  trigger <rcoDeliver, self, m>
  VC[s] = VC[s] + 1
```

- These algo ensure causal reliable broadcast
- If we replace reliabe broadcast with uniform reliabe broadcast, these algo would ensure uniform causal broadcast

# Total Order Broadcast (to)

- In reliable broadcast, the processes are free to deliver messages in any order they wish
- In causal broadcast, the processes need to deliver messages according to some order (causal order)
  - The order imposed by causal broadcast is however partial: some messages might be delivered in different order by the processes
- In **total order** broadcast, the processes must deliver all messages according to the same order (i.e. the order is now total)
  - This order does not need to respect causality (or event FIFO ordering)
- **Request**: <toBroadcast, m>
- Indication : <toDeliver, src, m>
- **RB1.** Validity: If  $p_i$  and  $p_j$  are correct, then every message broadcast by  $p_i$  is eventually delivered by  $p_i$
- RB2. No duplication: No message is delivered more than once
- RB3. No creation: No message os delivered unless it was broadcast
- RB4. (Uniform) Agreement: For any message m. If a correct (any) process delivers m, then every correct process delivers m
- (Uniform) Total order: Let m and m' be any two messages. Let  $p_i$  be any (correct) process that delivers m without having delivered m'. Then no (correct) process delivers m' before m
- Uses consensus (see next chapter)

```
Implements: TotalOrder (to)
Uses:
  ReliableBroadcast (rb)
  Consensus (cons)
upon event <Init> do
  unordered = delivered = emptySet
  wait = false;
  sn = 1
upon event <toBroadcast, m> do
  trigger <rbBroadcast, m>
upon event <rbDeliver, sm, m> and (m not in delivered) do
  unordered = unordered U {(sm, m)}
upon event (unordered not emptySet) and not wait do
  wait = true
  trigger <Propose, unordered>sn
upon event <Decide, decided>sn do
  unordered = unordered \ decided
  ordered = deterministicSort(decided)
  forall (sm, m) in ordered do
    trigger <toDeliver, sm, m>
    delivered = delivered U {m}
  sn = sn + 1
  wait = false
```

### Consensus

- In the (uniform) consensus problem the processes propose values and need to agree on one among these values
- Request : <Propose, v>Indication : <Decide, v'>
- C1. Validity: Any value decided is a value proposed
- C2. (Uniform) Agreement: No two correct (any) processes decide differently
- C3. Termination: Every correct process eventually decides
- C4. Integrity: Every process decides at most once, No process decides twice

### Algorithm 1 (cons)

- A P-based (fail-stop) consensus algorithm
- The processes exchange and update proposals in rounds and decide on the value of the non-suspected process with the smallest id
- The processes go through rounds incrementally (1 to n): in each round, the process with the id corresponding to that round is the leader of the round
- The leader of a round decides its current proposal and broadcast it to all
- A process that is not leader in a round waits to deliver the proposal of the leader in that round to adopt, or to suspect the leader

```
Implements: Consensus (cons)
Uses:
  BestEffortBroadcast (beb)
  PerfectFailureDetector (P)
upon event <Init> do
  suspected = emptySet
  round = 1
  currentProposal = null
  broadcast = delivered[] = false
upon event <crash, pi> do
  suspected := suspected U {pi}
upon event <Propose, v> do
if currentPoposal = null then
  currentPoposal = v
upon event <bebDeliver, p round, value> do
  currentPoposal = value
  delivered[round] = true
upon event delivered[round] = true or p_round in suspected do
  round = round + 1
upon event p_round = self and broadcasted = false and currentPoposal not null do
  trigger <Decide, currentPoposal>
  trigger <bebBroadcast, currentPoposal>
 broadcast = true
```

### Algorithm 2 (ucons)

- A P-based (fail-stop) uniform consenus algorithm
- The processes exchange and update proposal in rounds, and after n rounds decide on the current proposal value
- Implements uniform consensus
- The processes go through rounds incrementally (1 to n): in each round I, process  $p_I$  sends its current-Proposal to all
- A process adpots any currentProposal it receives

 $\bullet$  Processes decide on their current Proposal values at the end of round n

```
Implements: Uniform Consensus (ucons)
Uses :
 BestEffortBroadcast (beb)
  PerfectFailureDetector (P)
upon event <Init> do
  suspected = emptySet
  round = 1
  currentProposal = null
  broadcast = delivered[] = false
  decided = false
upon event <crash, pi> do
  suspected = suspected U {pi}
upon event <Propose, v> do
  if currentProposal = null then
    currentProposal = v
upon event <bebDeliver, p_round, value> do
  currentProposal = value
  delivered[round] = true
upon event delivered[round] = true or p_round in suspected do
  if round = n and decided = false then
    trigger <Decide, currentProposal>
    decided = true
  else
    round = round + 1
upon event p_round = self and broadcast = false and currentProposal not null do
  trigger <bebBroadcast, currentProposal>
  broadcast = true
```

#### Algorithm 3

- A uniform consensus algorithm assuming
  - A correct majority
  - A <>P failure detector
- The processes alternate in the role of a phase coordinator until one of them succeds in imposing a decision
- <>P ensures
  - Strong completeness: eventually every process that crashes is permanantly suspected by all correct processes
  - Eventual strong accuracy: eventually no correct process is suspected by any process
    - \* Strong accuracy holds only after finite time
  - Correct processes may be falsely suspected a finite number of times
  - This breaks consensus algorithm 1 and 2
- This algorithm is also round based: process move incrementally from one round to the other
- Process  $p_i$  is leader in every round k such that  $k \mod N = i$
- In such a round,  $p_i$  tries to decide
  - $-p_i$  succeeds if it is not suspected (process that suspect  $p_i$  inform  $p_i$  and move to the next round,  $p_i$  does so as well)
  - If  $p_i$  succeeds,  $p_i$  uses a reliable broadcast to send the decision to all (the reliability of the broadcast is important here to preclude the case where  $p_i$  crashes, some other processes delivers the message and stop while rest keeps going without majority)
  - 1.  $p_i$  selects among a majority the latest adopted value (lastest with respect to the round in which the value is adopted)
  - 2.  $p_i$  imposes that value at a majority: any process in that majority adopts that value  $p_i$  fails if it

is suspected

3.  $p_i$  decides and broadcasts the decision to all

## **Shared Memory**

### Regular Register

- Assumes only one writer
- Provides *strong* guarantees when there is no concurrent operations
- When some operations are concurrent, the register provides minimal guarantees
- Read() returns:
  - The last value written if there is no concurrent or failed operations
  - Otherwise the last value written on *any* value concurrently written i.e. the input parameter of some Write()
- We assume fail-stop model
  - Process can fail by crashing (no recovery)
  - Channels are reliable
  - Failure detection is perfect
- $\bullet~$  We implement a  ${\bf regular}$  register
  - Every process  $p_i$  has a local copy of the register value  $v_i$
  - Every process reads locally
  - The writer writes **globally**

```
Write(v) at pi
  send [W, w] to all
  forall pj, wait until either
    receive [ack] or
    detect [pj]
  return ok
```

```
Read() at pi
return vi
```

```
At pi
when receive [W, w] from pj
vi = v
send [ack] to pj
```

- We assume while failure detection is not perfect
  - $-P_1$  is the writer and any process can be reader
  - A mojority of the process is correct
  - Channels are reliable
- We implement a **regular** register
  - Every process  $p_i$  maintains a local copy of the register  $v_i$ , as well as a sequence number  $sn_i$  and a read timestamp  $rs_i$
  - Process  $p_1$  maintains in addition a timestamp  $ts_1$

```
Write(v) at p1
  ts1 ++
  send [W, ts1, v] to all
  when receive [W, ts1, ack] from majority
    return ok

Read() at pi
  rsi ++
  send [R, rsi] to all
```

```
when receive [R, rsi, snj, vj] from majority
   v = vj with the largest snj
   return v

At pi
   when receive [W, ts1, v] from p1
   if ts1 > sni then
      vi = v
      sni = ts1
      send[W, ts1, ack] to p1
```

#### Atomic Register

when receive [R, rsj] from pj send [R, rsj, sni, vi] to pj

- An **Atomic Register** provides strong guarantees event when there is concurrency and failures: the execution is equivalent to a sequencial and failure-free execution
- Every failed (write) operation appears to be either complete or not to have been invoked at all
- Every complete operation appears to be executed at some instant between its invocation and reply time events
- We implement a fail-stop 1-N atomic register
  - Every process maintais a local value of the register as well as a sequence number
  - The writer,  $p_1$ , maintains, in addition a timestamp  $ts_1$
  - Any process can read in the register

```
Write(v) at p1
  ts1++
  send [W, ts1, v] to all
  forall pi wait until either
    receive [ack] or
    detect [pi]
  return ok
Read() at pi
  send [W, sni, vi] to all
  forall pi wait until either
    receive [ack] or
    suspect [pj]
return vi
At pi
  When pi receive [W, ts, v] from pj
    if ts > sni then
      vi = v
      sni = ts
    send [ack] to pj
```

• We implement a fail-stop N-N atomic register

```
Write(v) at pi
  send [W] to all
  forall pj wait until either
   receive [W, snj] or
  suspect [pj]
```

```
(sn, id) = (highest snj + 1, i)
  send [W, (sni, id), v] to all
  forall pj wait until either
    receive [W, (sn, id), ack] or
    detect [pi]
  return ok
Read() at pi
  send [R] to all
  forall pj wait until either
    recieve [R, (snj, idj), vj] or
    suspect pj
  v = vj with the highest (snj, idj)
  (sn, id) = highest (snj, idj)
  send [W, (sn, id), v] to all
  forall pj wait until either
    receive [W, (sn, id), ack] or
    detect [pj]
 return v
At pi
T1:
  when receive [W] from pj
    send [W, sn] to pj
  when receive [R] from pj
    send [R, (sn, id), vi] to pj
T2:
  when receive [W, (snj, idj), v] from pj
    if (snj, idj) > (sn, id) then
      vi = v
      (sn, id) = (snj, idj)
    send [W, (sn, id), ack] to pj
  when receive [W, (snj, idj), v] from pj
    if (snj, idj) > (sn, id) then
      vi = v
      (sn, id) = (snj, idj)
    send [W, (sn, id), ack] to pj
```

- From fail-stop to fail-silent
  - We assume a mojority of correct processes
  - In the 1-N algorithm, the writer writes in a majority using a timestamp determined locally and the reader selects a value from a majority and then imposes this value on a majority
  - In the N-N algorithm, the writers determines first the timestamp using a majority

# Terminating Reliable Broadcast (trb)

- Like reliable broadcast, terminating reliable broadcast (TRB) is a communication primitive used to disseminate a message among a set of processes in a reliable way
- TRB is however strictly stronger than (uniform) reliable broadcast
- Like with reliable broadcast, correct processes in TRB agree on the set of messages they deliver
- Like with (uniform) reliable broadcast, every correct process in TRB delivers every message delivered by any correct process
- Unlike with reliable broadcast, every correct process delivers a message, event if the broadcaster crashes

- The problem is defined for a specific broadcaster process  $p_i = src$  (know by all processes)
  - Process src is supposed to broadcast a message m (distinct from  $\varphi$ )
  - The other processes need to deliver m if src is correct but may deliver  $\varphi$  is src crashes
- Request : <trbBroadcast, m>
- Indication : <trbDeliver, p, m>
- TRB1. Integrity: If a press delivers a message m, then either m is  $\varphi$  or m was broadcasted by src
- TRB2. Validity: If the sender src is correct and broadcasts a message m, then src eventually delivers m
- TRB3. (Uniform) Agreement: For any message m, if a correct (any) process delivers m, then every correct process delivers m
- TRB4. Termination: Every correct process eventually delivers exactly one message

```
Implements: trbBroadcast (trb)
Uses:
  BestEffortBroadcast (beb)
 PerfectFailureDetector (P)
  Consensus (cons)
upon event <Init> do
 prop = 0
  correct = S
upon event <trbBroadcast, m> do
  trigger <bebBroadcast, m>
upon event <crash, src> and (prop = 0) do
 prop = phi
upon event <bebDeliver, src, m> and (prop = 0) do
  prop = m
upon event (prop not 0) do
  trigger <Propose, prop>
upon event <Decide, decision> do
 trigger <trbDeliver, src, decision>
```

- We give an algorithm that implements P unsign TRB. More precisely, we assume that every process  $p_i$  can use an infinite number of instances of TRB where  $p_i$  is the sender src
  - 1. Every process  $p_i$  keeps on trbBroadcasting messages  $m_{i1}, m_{i2}$  etc
  - 2. If a process  $p_k$  delivers  $\varphi_i$ ,  $p_k$  suspects  $p_i$

# Non-Blocking Atomic Commit (nbac)

- A transaction is an atomic program describing a sequence of accesses to shared and distributed information
  - Can be determined either by **committing** or **aborting**
- Atomicity: a transaction either performs entirely or none at all
- Consistency: a transaction transforms a consistent state into another consitent state
- Isolation : a transaction appears to be executed in isolation
- Durability : the effects of a transaction that commits are permanent
- As in consensus, every process has an initial value 0 (no) or 1 (yes) and must decide on a final value 0 (abort) or 1 (commit)
- The proposition means the ability to commit the transaction
- The decision reflects the contract with the user
- Unlike consensus, the processes here seek to decide 1 but every process has a veto right
- Request : <Propose, v>
- Indication : < Decide, v'>
- NBAC1. Agreement: No two processes decide differently
- NBAC2. Termination: Every correct process eventually decides

- NBAC3. Commit-Validity: 1 can only be decided if all process propose 1
- NBAC4. Abort-Validity: 0 can only be decided if some process crashes of votes 0

```
Implements: nonBlockingAtomicCommit (nbac)
Uses:
  BestEffortBroadcast (beb)
  PerfectFailureDetector (P)
  UniformConsensus (uniCons)
upon event <Init> do
  prop = 1
  delivered = emptySet
  correct = PI
upon event <crash, pi> do
  correct = correct \ {PI}
upon event <Propose, v> do
  trigger <bebBroadcast, v>
upon event <bebDeliver, pi, v> do
  delivered = delivered U {pi}
  prop = prop * v
upon event correct \ delivered = empty do
  if correct different PI then
    prop = 0
  trigger <uncPropose, prop>
upon event <uncDecide, decision> do
  trigger <Decide, decision>
```

### Group Menbership and View Synchronous Communication

### Group Menbership (gmp)

- In many distributed applications, processes neet to know which processes are **participating** in the computation and which are not
- Failure detector provide such information; however that information is **not coordinated** event if the failure detector is perfect
- Like with a failure detector, the processes are informed about failures, we say that the precesses **install** views
- Like with a perfect failure detector, the processes have accurate knowledge about failures
- Unlike with a perfect failure detector, the information about failures are **coordinated** : the processes install the same sequence of views
- Indication : <membView, V>
- Memb1. Local Monotonicity: if a process installs view (j, M) after installing (k, N), then j > k and M < N
- Memb2. Agreement: no two porcesses install views (j, M) and (j, M') such that  $M \neq M'$
- Memb3. Completness: if a process p crashes, then there is an integer j such that every correct porcess eventually installs view (j, M) such that  $p \notin M$
- Memb4. Accuracy: if some process installs view (i, M) and  $p \notin M$  then p has crashed

```
Implements: groupMenberShip (gmp)
Uses:
    PerfectFailureDetector (P)
    UniformConsensus (Ucons)
upon event <Init> do
    view = (0, S)
    correct = S
```

```
wait = false
upon event <crash, pi> do
    correct = corrext \{pi\}
upon event (view.memb > correct) and (wait = false) do
    wait = true
    trigger <ucPropose, (view.id + 1, correct)>
upon event <ucDecide, (id, memb)> do
    view = (id, memb)
    wait = false
    trigger <membView, view>
```

### View Synchrony (vsc)

- View synchronous broadcast is an abstraction that results from the combination of group membership and reliable broadcast
  - Ensures that the delivery of messages is coordinated with the installation of views
- Request : <vsBroadcast, m> (<vsBlockOk>)
- Indication : <vsDeliver, src, m>, <vsView, V> (<vsBlock>)
- Memb1, Memb2, Memb3, Memb4, RB1, RB2, RB3, RB4
- VS: a message is vsDelivered in the view where it is vsBroadcast
- If the application keeps **vsBroadcasting** messages, the **view synchrony** abstraction might never be able to **vsInstall** a new view, the abstraction would be impossible
  - We introduce a specific event for the abstraction to block the application from vsBroadcasting messages, this only happends when a process crashes

```
Implements: ViewSynchrony (vs)
Uses:
  GroupMembership (gmp)
  TerminationReliableBroadcast (trb)
  BestEffortBroadcast (beb)
upon event <Init> do
 view = (0, S)
  nextView = ()
 pending = delivered = trbDone = emptySet
  flushing = blocked = false
upon event <vsBroadcast, m> and (blocked = false) do
  delivered = delivered U {m}
  trigger <vsDeliver, self, m>
  trigger <bebBroadcast, [data, view.id, m]>
upon event <bebDeliver, src, [data, vid, m] > do
  if (view.id = vid) and (m not in delivered) and (blocked = false) then
    delivered = delivered U {m}
    trigger <vsDeliver, src, m>
upon event <membView, V> do
  addtoTail(pending, V)
upon event (pending not emptySet) and (flushing = false) do
 nextView = removeFromHead(pending)
  flushing = true
  trigger <vsBlock>
upon event <vsBlock0k> do
 blocked = true
  trbDone = emptySet
  trigger <trbBroadcast, self, (view.id, delivered)>
upon event <trbDeliver, p, (vid, del)> do
```

```
trbDone = trbDone U {p}
  forall m in del and m not in delivered do
    delivered = delivered U {m}
    trigger <vsDeliver, src, m>
upon event (trbDone = view.memb) and (blocked = true) do
  view = nextView
  flushing = blocked = false
  delivered = emptySet
  trigger <vsView, view>
Implements: ViewSynchrony (vs)
Uses:
  UniformConsensus (uc)
  BestEffortBroadcast (beb)
  PerfectFailureDetector (P)
upon event <Init> do
  view = (0, S)
  correct = S
  flushing = blocked = false
  delivered = dset = emptySet
upon event <vsBroadcast, m> and (blocked = false) do
  delivered = delivered U {m}
  trigger <vsDeliver, self, m>
  trigger <bebBroadcast, [data, view.id, m]>
upon event <bebDeliver, src, [data, vid, m]> do
  if (view.id = vid) and (m not in delivered) and (blocked = false) then
    delivered = delivered U {m}
    trigger <vsDeliver, src, m>
upon event <crash, p> do
  correct = correct \{p}
  if flushing = false then
    flushing = true
    trigger <vsBlock>
upon event <vsBlock0k> do
  blocked = true
  trigger <bebBroadcast, [DSET, view.id, delivered]>
upon event <bebDeliver, src, [DSET, vid, del] > do
  dset = dset U (src, del)
  if forall p in correct, (p, mset) in dset then
    trigger <ucPropose, view.id+1, correct, dset>
upon event <ucDecided, id, memb, vsdset> do
  forall (p, mset) in vsdest and p in memb do
    forall (src, m) in mset and m not in delivered do
      delivered = delivered U {m}
      trigger <vsDeliver, src, m>
    viewx = (id, memb)
    flushing = blocked = false
    dset = delivered = emptySet
    trigger <vsView, view>
```

• Using uniform reliable broadcast instead of best effort broadcast in the previous algorithms does not ensure the uniformity of the message delivery