

Using Vertical Structure to Infer the Dynamical Mass Hidden in the AU Mic Debris Disk

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ABSTRACT

The vertical distribution of dust in debris disks is particularly sensitive to the total mass of planetesimal bodies stirring the disk, and is therefore well suited for constraining the prevalence of otherwise unobservable Uranus and Neptune analogs. Inferences of dynamical mass from debris disk vertical structure have previously been applied to infrared and optical observations of several systems, but the smaller particles traced by short-wavelength observations are ‘puffed up’ by radiation pressure, yielding only upper limits on the total dynamical mass. The large grains that dominate the emission at millimeter wavelengths are essentially impervious to the effects of stellar radiation, and therefore trace the underlying mass distribution more directly. Here we present ALMA 1.3 mm dust continuum observations of the debris disk around the nearby M star AU Mic. The 3 au spatial resolution of the observations, combined with the favorable edge-on geometry of the system, allows us to measure the vertical structure of the disk; we report a scale height-to-radius aspect ratio of $h = 0.031 \pm 0.005$. Comparing the observed aspect ratio to a theoretical model of steady-state, size-dependent velocity distributions in the collisional cascade we estimate the total mass of bodies stirring the disk to be $\sim 1.5 M_{\oplus}$. These measurements rule out the presence of a gas giant or Neptune analog in the outer disk, but are suggestive of the presence of large planetesimals stirring the dust distribution.

1. INTRODUCTION

Planets form during a relatively short and early stage in the lifetime of stellar systems, when the host star is still encircled by a protoplanetary disk rich in gas. Planet formation (as well as processes including accretion, photoevaporation, and winds) causes first-generation protoplanetary material to dissipate over time (Williams & Cieza 2011; Ercolano & Pascucci 2017). The first-generation material is replaced by second-generation ‘debris,’ produced by a collisional grinding of larger (Pluto-sized) planetesimals into small dust grains in a process known as a collisional cascade (Wyatt 2008). The resulting debris disks, optically thin and significantly less luminous than their protoplanetary counterparts, are found around at least 25% of Solar-type stars and are likely to be as common as the exoplanetary systems with which they are thought to be associated (Montesinos et al. 2016).

Analysis of the morphological and emissive properties of debris disks sheds light on the final stages of planetary system evolution and can reveal the presence of planets hidden within. Planets can imprint features such as rings/gaps, clumps, or other asymmetries on their parent disks, although it is rarely straightforward to infer the properties of planets directly from the disk morphology (Hughes et al. 2018). In gas-poor systems, the vertical structure of a debris disk can serve as a probe of the total mass of large bodies stirring the collisional cascade. The presence of massive bodies increases the inclination dispersion of the constituent dust particles and thus the scale height H of the observed dust distribution.

The dynamical excitation of a disk can therefore be measured from its aspect ratio H/r , which in turn allows inferences about the presence and size of the bodies responsible for the dynamical stirring. Such work has been undertaken by several authors using visible and infrared observations (Artymowicz 1997; Thébault & Augereau 2007; Quillen et al. 2007). However, Thébault (2009) demonstrate that radiation pressure from the host star should preferentially excite the smallest dust grains in the disk, imparting a ‘natural’ scale height even in the absence of large bodies dynamically stirring the disk. Thus longer-wavelength ($\lambda \geq 50 \mu\text{m}$) observations are required to measure disk scale height as determined by dynamical stirring alone, since the grains dominating the emission at these wavelengths are large enough to be impervious to the effects of radiation pressure.

The M3IVe star AU Mic presents a particularly favorable target for such observations due to its proximity ($9.91 \pm 0.10 \text{ pc}$; van Leeuwen 2007) edge-on inclination,

and apparently symmetric morphology at millimeter wavelengths. The first M star detected to have a far-infrared excess, AU Mic hosts one of the best-studied debris disks (Moshir & et al. 1990). As a member of the β Pic Moving Group, it is thought to be relatively young: 23 ± 2 Myr (Binks & Jeffries 2014; Mamajek & Bell 2014; Malo et al. 2014). The disk around AU Mic was first resolved by Kalas et al. (2004) in scattered light, and a host of observations spanning the optical to the submillimeter have followed (Augereau & Beust 2006; MacGregor et al. 2013; Matthews et al. 2015; Schneider et al. 2014; Wang et al. 2015). Notably, the debris around AU Mic exhibits a so-far-unique time variability at scattered light wavelengths. Boccaletti et al. (2015) identify five features—local intensity maxima offset from the disk midplane—on the SE side of the disk. These features are quickly moving away from the star along the disk midplane at projected velocities that are not consistent with Keplerian rotation; in fact, the outermost two features appear to be unbound from the star. Both dust emission from a localized source such as a planet (Boccaletti et al. 2015; Sezestre et al. 2017) and collisional dust avalanches (Chiang & Fung 2017) have been proposed to explain these features.

In this work we present new $0.3''$ Atacama Large Millimeter/submillimeter Array (ALMA) 1.3 mm observations of the AU Mic debris disk. These observations represent a factor of ~ 2 improvement in both spatial resolution and rms noise relative to MacGregor et al. (2013)’s previous ALMA observations of the system, and our analysis indicates that the vertical structure of the disk is resolved with $4\text{--}6\sigma$ confidence. In §2 we present the new observations and describe the data reduction. §3 quotes the basic observational results regarding the disk flux, morphology, and gas content. In §4 we conduct a parametric exploration of a 2-dimensional disk model in order to investigate the degeneracy between vertical structure, radial structure, and viewing geometry. In §5 we discuss our results, particularly the constraints on the dynamical excitation of the disk imposed by our measurement of the scale height, and compare them to previous observations. The results of our measurement of scale height and its implications for the total disk mass are summarized in §6.

2. OBSERVATIONS

AU Mic was observed with ALMA on three dates: 26 March 2014, 18 August 2014, and 24 June 2015 (see Table 1). The baseline lengths range between 12 m and 1320 m; the longest baseline among the three observations traces an angular scale of $0.22''$ and a spatial scale of 2.2 au. All observations employed ALMA’s 12m antennas

Observational parameters	26 March 2014	18 August 2014	24 June 2015
Antennas:	32	35	37
Baseline length (m):	12–406	19–1160	30–1320
On-source time (min):	35	35	33
Flux calibrator:	Titan	J2056-472	Titan
Bandpass calibrator:	J1924-2914	J2056-4714	J1924-2914
Gain calibrator:	J2101-2933	J2101-2933	J2056-3208
pwv range (mm):	[0.63, 0.66]	[1.58, 1.69]	[0.67, 0.74]
Imaging parameters			
Beam size (arcsec):	1.27×0.74	0.33×0.30	0.47×0.31
Peak intensity ($\mu\text{Jy}/\text{beam}$):	630	240	320
rms noise ($\mu\text{Jy}/\text{beam}$):	30	30	20

Table 1. Observational and imaging parameters for the three datasets used in this work. Images were created using the **CASA** task **tclean** with natural weighting.

and Band 7 receivers, including four independently tunable spectral windows. One spectral window was centered around the CO $J = 2 - 1$ transition at a rest frequency of 230.538001 GHz, with a total bandwidth of 1.875 GHz and a channel spacing of 0.6 km/s. The remaining three spectral windows were configured to detect continuum emission with central frequencies of 228.5, 213.5, and 216.0 GHz, total bandwidths of 2 GHz, and channel spacings of 21.7 km/s.

Calibration, reduction, and imaging were carried out using the **CASA** (McMullin et al. 2007) and **MIRIAD** (Sault et al. 1995) software packages. Standard ALMA reduction scripts were applied to the datasets: phase calibration was accomplished via gain calibration and water vapor radiometry tables, while system temperature calibrations were performed to account for variations in instrument and weather conditions. Flux and bandpass calibrations were subsequently applied; the flux calibration is subject to a 10% systematic uncertainty. In addition to these standard procedures, the weights of the visibilities were recalculated using the variance around each baseline as in Flaherty et al. (2017).

During the last segment of the June observation (04:23:38–04:29:58 UT), the host star flared. To determine the flux of the flare as a function of time, we binned the data into one-minute intervals using the **CASA** task **split** and fit a point source in each bin to baselines between 100 k λ and 1400 k λ with **uvmodelfit**. The resulting

Time (UTC)	Point-source Flux (μJy)
03:45:0–04:20:0 (no flare)	$(4.1 \pm 0.2) \times 10^2$
4:23:38–4:24:00	$(9.2 \pm 1.7) \times 10^2$
4:24:00–4:25:00	$(1.146 \pm 0.010) \times 10^4$
4:25:00–4:26:00	$(3.59 \pm 0.10) \times 10^3$
4:26:00–4:27:00	$(1.58 \pm 0.10) \times 10^3$
4:27:00–4:28:00	$(4.50 \pm 1.0) \times 10^2$
4:28:00–4:29:00	$(4.60 \pm 1.0) \times 10^2$
4:29:00–4:29:58	$(5.20 \pm 1.0) \times 10^2$

Table 2. Central point source flux before and during the June flare

flare fits can be found in Table 2. We exclude from our analysis the seven minutes during which the flare occurred, as it proved difficult to separate the stellar emission from the disk emission while it was changing so rapidly.

Since AU Mic is a high proper motion system, its equatorial coordinates changed significantly over the 1.5 years between first and last observations. We were able to obtain a more precise alignment of the datasets from the bright chromospheric emission of the central star than from the measured proper motion. We fit an image-domain elliptical Gaussian to a small region around the star on each date with the task `imfit`, and used the centroid of the Gaussian fit to define the star position. Each dataset was then phase-shifted using the task `fixvis` so that the pointing center of the data was the same as the fitted star position. We note that the exclusion of the flare changed the centroid of the Gaussian fit for the June observations by 0.710 ± 0.018 au (18% of the synthesized beam) although the errors reported here, derived from the `imfit` uncertainties, are a factor of five smaller than those given by the ratio of beam size to SNR. This change in the fit stellar location could be explained if the flare were not symmetric with respect to the star.

Imaging was performed using standard Fourier inversion methods as implemented in the CASA task `tclean`. Two weighting schemes were used: (i) natural weighting with no taper to trace the small-scale disk structure and (ii) natural weighting with a $200\text{ k}\lambda$ Gaussian taper applied to long baselines to bring out the disk emission on larger spatial scales. In scheme (i) the rms noise σ was $15\ \mu\text{Jy}/\text{beam}$ and the restoring beam was $0.52'' \times 0.39''$ with a position angle (PA) of $77^\circ.9$. In scheme (ii), the corresponding values are $20\ \mu\text{Jy}/\text{beam}$, $0.87'' \times 0.71''$, and $80^\circ.8$. Because the

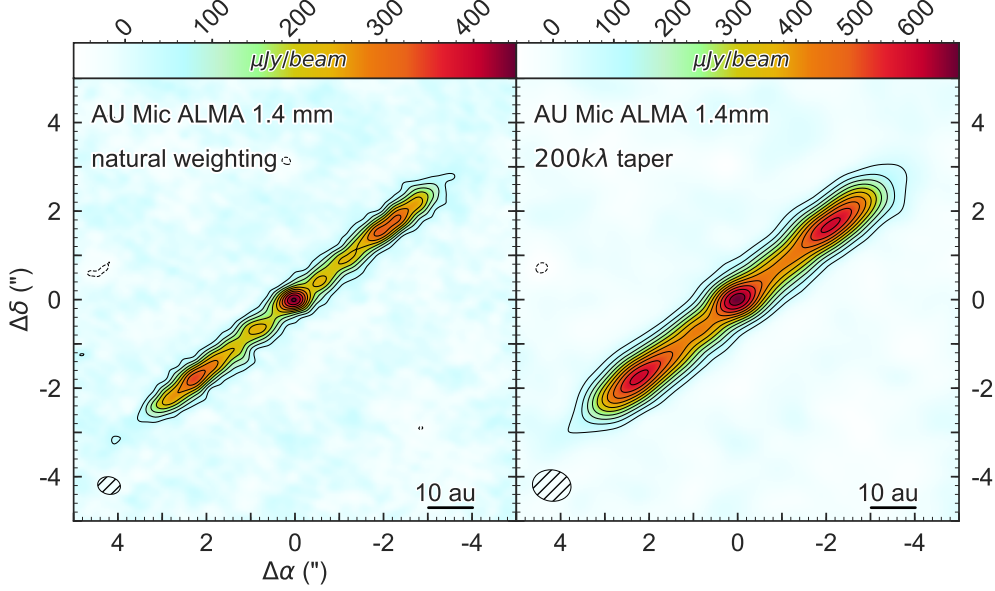


Figure 1. The AU Mic system imaged by ALMA at a wavelength of 1.3 mm, using natural weighting with and without a Gaussian taper on the long baselines. For the untapered weighting, the rms noise is $15 \mu\text{Jy/beam}$ and the restoring beam has dimensions $0.52'' \times 0.39''$ with a PA of $77^\circ 9$. The corresponding values for the tapered weighting are $20 \mu\text{Jy/beam}$, $0.87'' \times 0.71''$, and $80^\circ 8$. Contours are integer multiples of the three times the rms noise. The hatched ellipse in the bottom left of each pane designates the size and shape of the restoring beam.

CASA task `tclean` preserves pointing center offsets when converting several visibility datasets into an image, it was necessary to combine the data into a single file (with a common pointing center) before cleaning in order to account for the offset in phase center between datasets. This was done using the task `concat`, which combines datasets with pointing centers aligned so long as their pointing centers do not differ by a value greater than the parameter `dirtol`.

3. RESULTS

Figure 1 shows the combined dust continuum emission from all three observations at 1.3 mm; chromospheric emission from the M star is visible as a point source at the center of the image (Cranmer et al. 2013). The peak signal-to-noise ratio of dust emission is ~ 23 . Using the MIRIAD task `cgcurs`, we measure an integrated flux of $4.97 \pm 0.08 \text{ mJy}$ enclosed within the 3σ contours of the naturally weighted image.

Note that this value represents the combined emission from the disk *and* the star. Faithfully disentangling the two components proved difficult, both because stellar and disk emission are blurred together in the central beam and because the stellar flux varied significantly across the three nights of observation (Table 3). Consequently, the most accurate way to isolate the disk flux from the stellar contribution is through parametric modeling (see §4) where the two components can be specified separately; our modeling yields a disk flux of 4.80 ± 0.17 mJy. The ansa to the NW exhibits a maximum flux density of $330 \pm 15 \mu\text{Jy}/\text{beam}$ at a separation of 24.8 ± 0.2 au and PA of $128^\circ 2 \pm 0.4$, while the ansa to the SE exhibits a maximum flux density of $340 \pm 15 \mu\text{Jy}$ at a separation of 29.0 ± 0.2 au and PA of $128^\circ 7 \pm 0.4$. The peak flux densities of the ansae differ by less than the rms noise, indicating that there is no significant difference in brightness between the two limbs of the disk. Indeed, the apparent flux asymmetry in these data is in the opposite direction of the apparent flux asymmetry in [MacGregor et al. \(2013\)](#), providing further circumstantial evidence that there is no significant flux asymmetry at millimeter wavelengths. Additionally, the discrepancy in position angle between the two peaks falls within the estimated uncertainties and so we are not able to confirm the scattered light PA offset observed by [Boccaletti et al. \(2015\)](#).

The vertical and radial structure of AU Mic’s disk is traced in Figure 2. At each radial location along the disk major axis, a one-dimensional Gaussian was fit to the vertical surface brightness profile. The top, center, and bottom panes correspond respectively to the amplitude, centroid, and beam-subtracted FWHM of the Gaussian fits. Broadening effects of the synthesized beam in the vertical direction have been removed by subtracting in quadrature the Gaussian beam FWHM from the Gaussian fit FWHM. In more physical terms, the three panes represent the intensity at the location of the disk “spine,” the spine’s elevation from the midplane, and the disk FWHM. We were unable to detect (in either the combined dataset or the three individual epochs) the intensity variations or excursions of the disk spine from the midplane that characterize the fast-moving features observed by [Boccaletti et al. \(2015\)](#). This is not entirely surprising, as both [Sezestre et al. \(2017\)](#) and [Chiang & Fung \(2017\)](#) suggest that the clouds are composed of sub-micron-sized grains which do not emit efficiently in the millimeter.

The disk is resolved across ~ 17 beams along the major axis, and cursory image-domain analysis indicates the disk is marginally resolved perpendicular to the major

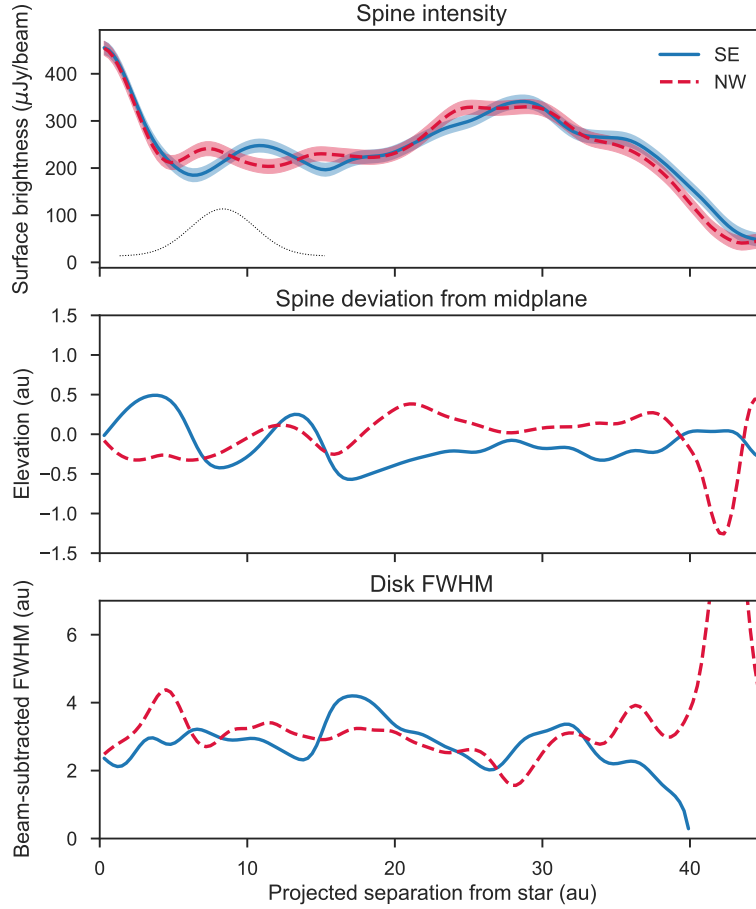


Figure 2. Image-domain analysis of the AU Mic debris disk radial and vertical structure. The solid blue line shows the southeast limb of the disk, while the dashed red line shows the northeast limb. From top to bottom, the three panes show i) the disk spine surface brightness with errors given by the rms noise, ii) the disk spine deviation from the midplane, and iii) the disk FWHM as a function of projected separation from the star. The Gaussian traced by the dotted line in the first pane shows the projected width in the radial direction of the naturally weighted synthesized beam of the combined dataset. The fact that the image-domain vertical height of the disk is in excess of the beam contribution implies that our data spatially resolve the vertical structure of the disk.

axis as well (Figure 2, bottom pane). 3σ emission as determined from the surface brightness profile in Figure 2 extends to a radial distance of ~ 43 au on the NW side and ~ 46 au on the SE side. We note the presence of local intensity maxima, nearly symmetric about the star at a distance of ~ 10 au; it is unclear if these are real features of the disk or are artifacts of the rms noise or cleaning process. We examine the significance of these features in §4.

There is no evidence that the AU Mic system harbors a significant reservoir of molecular gas. We set a 3σ upper limit of $0.07 \text{ Jy km s}^{-1}$ on the CO $J = 2 - 1$ integrated flux. For a given excitation temperature, an upper limit on the total gas mass can be inferred from the upper limit on integrated flux. We find the upper limit on the total gas mass to range between $1.79 \times 10^{-7} M_{\oplus}$ and $9.06 \times 10^{-7} M_{\oplus}$ for excitation temperatures between 10 K and 250 K.

4. ANALYSIS

Previous studies of the scale height of debris disks have demonstrated a degeneracy between vertical structure, radial structure, and viewing geometry (e.g., Milli et al. 2014). In light of this, we adopt a modeling approach that combines appropriate ray tracing methods with a Markov Chain Monte Carlo (MCMC) algorithm in order to investigate the degree to which these known degeneracies impact our ability to measure the vertical structure of the disk.

4.1. Modeling Formalism

We use the parametric structure and ray tracing disk code described in Flaherty et al. (2015), itself an adaptation of earlier work by Rosenfeld et al. (2013). Synthetic sky-projected images are generated from a given temperature and density structure and are subsequently Fourier transformed to create model visibilities that can be directly compared to the interferometric data.

We assume the disk to be azimuthally symmetric and vertically isothermal. The disk vertical structure is set by the aspect ratio $h = H(r)/r$. At a given radius r , the vertical density profile is assumed to be Gaussian with a standard deviation equal to the scale height $H(r)$. The dust opacity is set to $2.3 \text{ cm}^2 \text{ g}^{-1}$ (Beckwith et al. 1990), placing the model disk in the optically thin regime for the range of dust masses explored. For an optically thin disk, the observed thermal emission is determined by both the surface density and temperature of the dust; to break the degeneracy between these two parameters, we assume that the dust grains are in blackbody

equilibrium with the central star. Thus the dust temperature at a distance r from the host star is given by

$$T_{dust}(r) = \left(\frac{L_{\star}}{16\pi r^2 \sigma} \right)^{1/4} \quad (1)$$

where L_{\star} is the bolometric luminosity of the star and σ is the Stefan-Boltzmann constant. We assume that the radial surface density takes the form of a power law:

$$\Sigma(r) = \begin{cases} \Sigma_c r^p & r_{in} \leq r \leq r_{out} \\ 0 & \text{otherwise} \end{cases} \quad (2)$$

where p is the power law exponent, and r_{in} and r_{out} are the disk inner and outer radius. Σ_c normalizes the surface density structure for a given total dust mass M_{dust} :

$$\Sigma_c = \frac{M_{dust} (p + 2)}{2\pi \left[r_{out}^{(p+2)} - r_{in}^{(p+2)} \right]}. \quad (3)$$

The observed disk PA and inclination i are free parameters. We adopt a stellar luminosity of $0.09 L_{\odot}$ (Plavchan et al. 2009) and a distance to the star of 9.91 ± 0.10 pc (van Leeuwen 2007);¹ the observed 1.3 mm stellar flux F_{\star} is left as a free parameter for each observation date. We note that the uncertainty in the stellar distance could affect the modeled disk mass and disk radial extent, while the 10% systematic flux uncertainty could affect the modeled disk mass and stellar flux. The spatial resolution of the resulting model sky image is set to 0.3 au per pixel, chosen to be $\sim 10\%$ of the spatial scale sampled by the longest baseline in the data. After the model image is generated by the ray tracing code, it is Fourier transformed into the visibility domain and sampled at the same spatial frequencies as the ALMA data with the MIRIAD task `uvmodel`. This allows the model to be compared directly to the visibilities in the Fourier domain, where uncertainties are better characterized than in the image domain. A χ^2 metric is used to assess the quality of the fit.

We explore the parameter space of the model using the affine-invariant formulation of the MCMC algorithm described by Goodman & Weare (2010) and implemented in Python as `emcee` (Foreman-Mackey et al. 2013). MCMC routines sample parameter space such that the density of samples in a given region is proportional to the

¹ We are currently re-running all models with the new Gaia distance of 9.725 ± 0.005 pc.

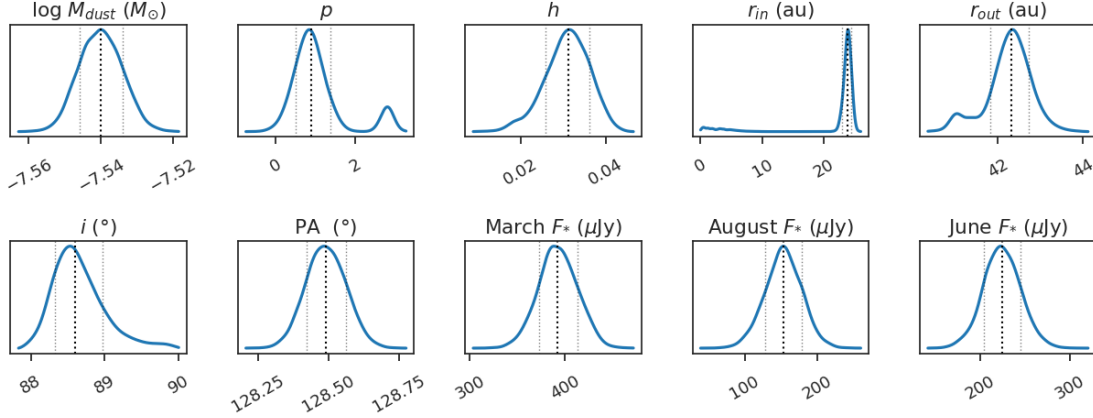


Figure 3. Kernel density estimates of the marginalized posterior probability distributions for the fiducial run. The central dashed line designates the median of each distribution while the outer lines mark the 16th and 84th percentiles (1σ confidence intervals).

local probability density, allowing estimation of the posterior probability functions themselves. The process therefore not only identifies regions of high probability in parameter space, but also allows uncertainties and degeneracies between parameters to be determined from the correlations between the posteriors of each parameter. We assume uniform priors for all parameters; the dust mass was sampled in logarithmic space, formally equivalent to assuming a log uniform prior. No prior bounds were placed on the logarithm of the dust mass. Priors placed on the stellar flux and disk inner radius, width, and aspect ratio ensured that these parameters were always greater than zero, while the prior placed on the power law exponent ensured $-5 < p < 10$. The position angle was confined to the range $1^\circ < \text{PA} < 360^\circ$, and the inclination to $0^\circ < i < 90^\circ$. Leaving the inclination unbounded does not affect the preferred inclination; the MCMC chain simply converges to two positions symmetric about 90° . We performed several MCMC runs in order to investigate a variety of model formalisms. All runs used 50 walkers, and 10^5 samples were drawn from each run to allow accurate statistical comparison between runs.

Initially we varied ten parameters: the logarithm of the disk dust mass ($\log M_{\text{dust}}$), the disk inner radius (r_{in}), width (Δr), power law exponent (p), scale height aspect ratio (h), inclination (i), position angle (PA), and finally a separate stellar flux (F_\star) for each of the three observation dates. After the fact, the posterior distribution for Δr was replaced by the outer radius posterior $r_{\text{out}} = r_{\text{in}} + \Delta r$ to allow for easier

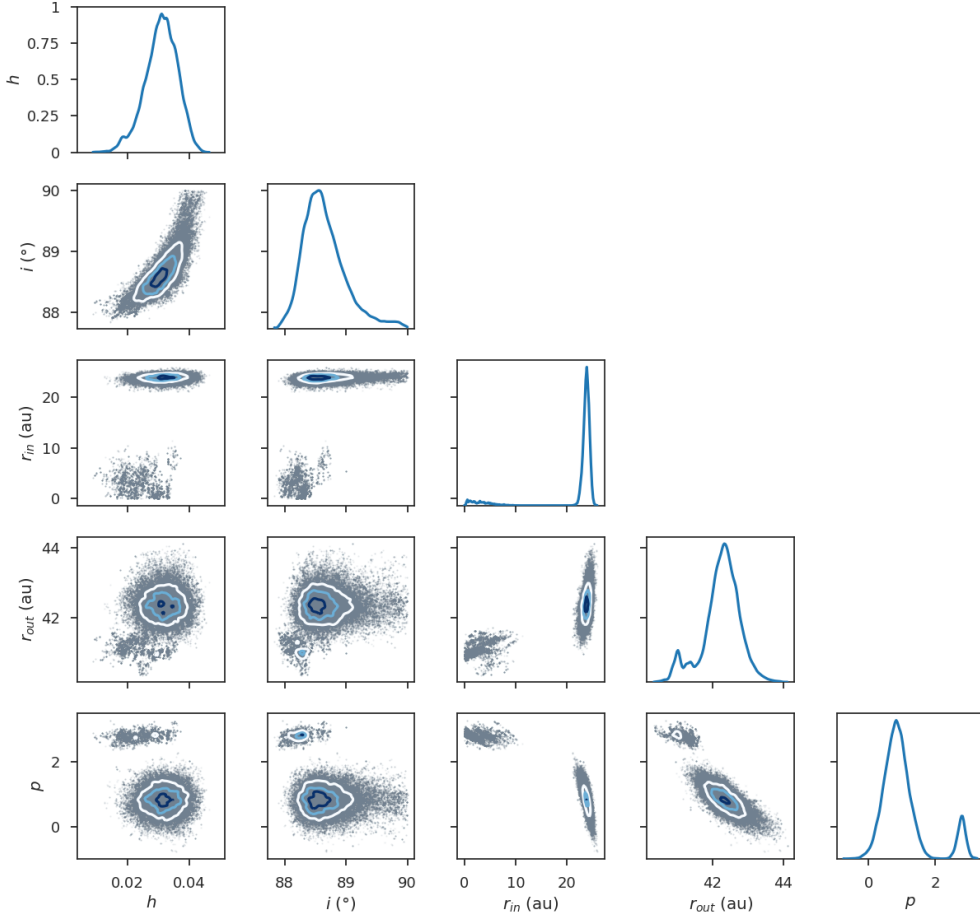


Figure 4. ‘Corner’ plot showing degeneracies between a subset of the free parameters for the fiducial model. Two families of solutions are visible, and are most prominent in the p , r_{in} , and r_{out} distributions. In addition, the two-dimensional slices through parameter space show limited degeneracies between radial structure, vertical structure, and viewing geometry.

interpretation. This model formalism resulted in a best-fit χ^2 value of 626163.598 (reduced $\chi^2 = 2.053$), and we treat this parameterization as our fiducial model.

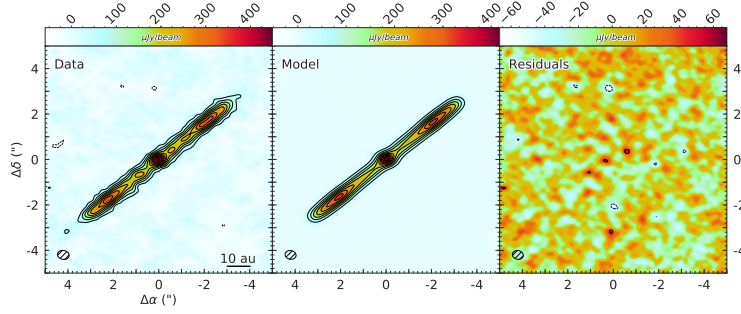
4.2. Investigating Radial Structure

Marginalized posterior probability distributions for the fiducial model parameters are shown in Figure 3. While the majority of the distributions are Gaussian, the

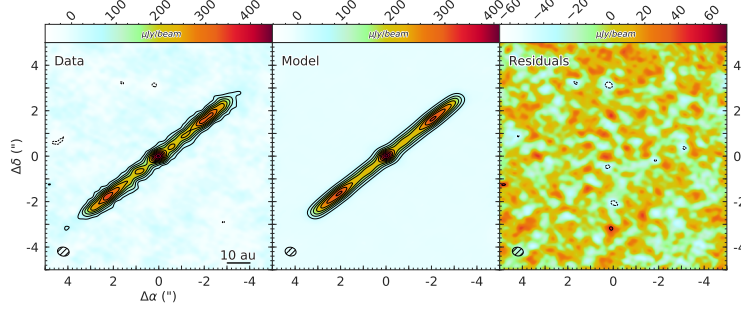
three parameters that determine the radial structure of the disk (p , r_{in} , and r_{out}) exhibit slight bimodality. All three parameters are degenerate as can be seen from the ‘corner’ plot in Figure 4; in fact, the bimodality of the three parameters is a result of the existence of two distinct families of solutions in parameter space. While the fiducial best-fit model has $p = 0.8$, $r_{in} = 24.0$ au, and $r_{out} = 42.3$ au, a lower-likelihood family of solutions can clearly be seen in Figure 4. The highest-likelihood model associated with this family has $p = 2.8$, $r_{in} = 5.2$ au, and $r_{out} = 41.0$ au. More generally, mild degeneracies between the parameters determining vertical structure, radial structure, and viewing geometry are visible, but the aspect ratio h remains relatively uncorrelated with other aspects of AU Mic’s structure.

The fiducial best-fit model image and residuals found in Figure 5a provide further information as to the cause of the bimodal posterior distribution. As can be seen from the residual map, the outer regions of the disk are reproduced well by the model; however 3σ residuals remain at the location of the star, as well as at symmetric positions at a separation of ~ 10 au on either side of the star. We note the symmetric residuals share the locations of the local intensity maxima described in §3. The convergence of these features leads us to consider the possibility of either a dust density enhancement (a ring) or reduction (a gap) in the inner regions of the disk. As a gap/ring would cause the radial surface brightness profile of the disk to deviate from that given by the simple power law used in our modeling, it could explain the bimodality in the posterior distributions of the parameters governing disk radial structure.

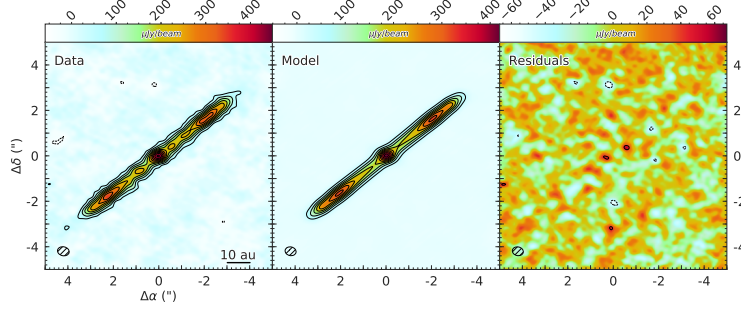
We first explored the effects of adding a gap to the inner regions of the disk. The gap inner and outer radii were left as free parameters and the dust density within the gap was set to zero. The gap consistently converged to regions where the dust density was already zero (interior to the disk inner radius or exterior to the disk outer radius); we take this as evidence that the data are not well characterized by a gap. As a next step, we experimented with adding a ring to the disk. The ring inner radius r_{ring} was once again left as a free parameter and the ring width was fixed to 0.3 au. The ring was also characterized by a dust mass M_{ring} , which was evenly distributed across the radial extent of the ring. As can be seen in Figure 5b this parameterization was better able to reproduce the ‘bump’ in the radial surface brightness profile at $r \sim 10$ au, reducing the best-fit model residuals by $\sim 25\%$. However, 2σ residuals are still present at the location of the bumps; the ring model’s



(a) Fiducial run best-fit model and residuals.



(b) Ring run best-fit model and residuals.



(c) 'Skinny' disk run best-fit model and residuals.

Figure 5. Best-fit model image and residuals, sampled at the spatial frequencies of the ALMA data and cleaned using natural weighting. Contours are integer multiples of the ALMA data 3σ confidence level. For the fiducial model (a), 3σ residuals can clearly be seen at the location of the star and at symmetric positions ~ 10 au from the star. Adding an additional ring of dust to the model (b) reduces these residuals by $\sim 25\%$, but statistical analysis indicates that best-fit ring model does not conclusively describe the data better than the fiducial model. Fixing the scale height well below ALMA's resolution limits (c) results in a less statistically significant model, especially in the outer regions of the disk where ALMA is sensitive to the vertical structure of the disk.

failure to accurately reproduce these features could be explained by the fact that the two local intensity maxima are not perfectly symmetric about the star. Image domain analysis indicates that the bump to the SE has a separation of ~ 11 au, while the NW bump has a separation of ~ 8 au (Figure 2). This discrepancy could be explained if the hypothetical ring were eccentric.

The median values and best-fit model parameters for the fiducial and ring parameterizations can be found in Table 3. We use both the AICc, a form of the Akaike Information Criterion (AIC) corrected for finite datasets, and the Bayesian Information Criterion (BIC) to compare goodness of fit between models with different numbers of free parameters. The best-fit ring model is preferred to the fiducial model with 3.7σ confidence on the AICc; conversely, the fiducial model is preferred to the ring model on the BIC with $\Delta\text{BIC} = 4.3$. As such, we are not able to conclusively confirm the presence of an additional ring of mm dust grains in the AU Mic disk.

A model with a single F_\star across all three dates was also investigated, but did not reproduce the data to the same degree of accuracy as the fiducial model. Significant residuals were visible at the location of the star, and a stellar flux varying by more than a factor of 2 over a period of months to years is preferred with 7.3σ confidence by the AICc and with $\Delta\text{BIC} = 36.7$.

4.3. Investigating Vertical Structure

The posterior distribution for the aspect ratio h suggests that the data are capable of measuring AU Mic’s scale height despite the mild degeneracy between aspect ratio and other parameters like the radial structure and viewing geometry. Even when marginalized over these other parameters, the posterior distribution indicates a measured value of $h = 0.031 \pm 0.005$, which translates to a $\sim 6\sigma$ measurement of the scale height rather than an upper limit. At the ~ 40 au outer edge of the disk, this aspect ratio implies a vertical scale height of 1.2 ± 0.2 au. The corresponding disk FWHM is 2.8 ± 0.5 au, consistent with an image-domain FWHM of ~ 3 au estimated from Figure 2. To verify that we in fact measured the scale height, we investigate a model parameterization in which the scale height is set to a value well below ALMA’s resolution limits. The aspect ratio is fixed at a value of 0.003, so that even at the outer edge of the disk the scale height is $\sim 3\%$ of the beam size along the disk’s vertical axis. If the disk is in fact resolved, such a ‘skinny’ disk model should perform significantly worse than the fiducial model. The best-fit model image and

Table 3. MCMC Fitting Results

Parameter	Fiducial		Disk + Ring	
	Median	Best Fit	Median	Best Fit
$\log M$ (M_\odot)	$-7.540^{+0.006}_{-0.006}$	-7.540	$-7.548^{+0.007}_{-0.007}$	-7.545
p	$0.9^{+0.5}_{-0.4}$	0.8	$0.8^{+0.6}_{-0.4}$	0.9
h	$0.031^{+0.005}_{-0.005}$	0.032	$0.027^{+0.004}_{-0.005}$	0.028
r_{in} (au)	$23.8^{+0.6}_{-0.9}$	24.0	$24.1^{+0.6}_{-0.9}$	23.9
r_{out} (au)	$42.3^{+0.4}_{-0.5}$	42.3	$42.3^{+0.4}_{-0.5}$	42.4
i ($^\circ$)	$88.6^{+0.4}_{-0.3}$	88.7	$88.27^{+0.22}_{-0.16}$	88.3
PA ($^\circ$)	$128.49^{+0.07}_{-0.07}$	128.50	$128.50^{+0.07}_{-0.07}$	128.48
March F_* (μJy)	390^{+20}_{-20}	390	370^{+20}_{-20}	370
August F_* (μJy)	150^{+20}_{-30}	160	150^{+20}_{-30}	140
June F_* (μJy)	220^{+20}_{-20}	220	220^{+20}_{-20}	210
r_{ring} (au)			$11.9^{+1.7}_{-1.8}$	10.8
M_{ring} ($M_\oplus \times 10^{-4}$)			$1.8^{+0.5}_{-0.7}$	1.7
ln Likelihood	-313087^{+2}_{-4}	-313082	-313077^{+2}_{-5}	-313072

residuals are shown in Figure 5c. The skinny model results in a significantly poorer fit to the data than the fiducial model with variable aspect ratio, with the best fits differing at the 3.9σ level according to the AICc and by a value of 7.5 on the BIC.

The preferred disk FWHM is only $\sim 2/3$ the size of the combined-data beam projected onto the vertical axis of the disk. While it may seem improbable that we measure a scale height below the image-domain spatial resolution of the combined data, our results can be explained by the following observations. First, the beam size of the naturally weighted combined image ($0.52'' \times 0.39''$) is not wholly representative of the longest baselines in the data. The smallest naturally weighted beam FWHM from the three individual observations is $0.30''$ (3 au; Table 1), while the spatial scale traced by the longest baseline is $0.22''$ (2.2 au). Second, the scale height H refers to the disk height as measured from the midplane; the observable quantity that must be resolved in order to measure the scale height is actually the total vertical thickness $2H$. Third, the scale height represents the standard deviation of a Gaussian distribution of dust particles that in fact reaches well beyond the extent of the scale

height. For example, considering that the peak SNR of the data is ~ 23 and that the vertical distribution of dust is assumed to be Gaussian, the SNR should remain above 3 over a total vertical extent of $0.38''$ (3.8 au). The combination of these factors indicates that it is plausible that we are able to detect a scale height smaller than the resolution of the image-domain data.

5. DISCUSSION

Parametric modeling suggests that AU Mic’s debris disk is nearly edge on, exhibits an increasing surface density with radius until ~ 42 au, and reaches a maximum scale height of ~ 1.2 au. There is also marginal evidence for an additional annulus of dust at $r \sim 10$ au. Here we compare the results of our analysis with previous studies of AU Mic’s debris disk.

The geometric properties of the disk inferred from our modeling agree well with the literature. Our median inclination of $88.6^{+0.4}_{-0.3}$ is consistent with previous estimates of the disk’s inclination within uncertainties (Metchev et al. 2005; Krist et al. 2005). The median PA of 128.49 ± 0.07 falls within uncertainties of measurements by MacGregor et al. (2013) and Krist et al. (2005); however, the limb-averaged PA interior to 50 au from Metchev et al. (2005) is 129.8 ± 0.2 , and Schneider et al. (2014) report an optical-wavelength PA of 127.8 ± 0.2 between 50 au to 100 au. The preferred dust mass ($0.01 M_{\oplus}$) is identical to the value derived from resolved 1.3 mm imaging by MacGregor et al. (2013) and from low-resolution $850 \mu\text{m}$ imaging by Matthews et al. (2015); the latter quote a 20% uncertainty. Similarly, Liu et al. (2004) report $0.011 M_{\oplus}$ from unresolved $850 \mu\text{m}$ observations. Strubbe & Chiang (2006) calculate $0.01 M_{\oplus}$ by deriving a steady-state collisional cascade grain size distribution and fitting the disk’s surface brightness and thermal spectrum to V - and H -band HST observations. As discussed in §3, even a large gas excitation temperature of 250 K implies a 3σ upper limit on the total gas mass of only $9.06 \times 10^{-7} M_{\oplus}$; combined with our preferred dust mass, this mass corresponds to an upper limit on the gas-to-dust ratio of $\sim 10^{-4}$. Such a low dust-to-gas ratio excludes the possibility of gas influencing the millimeter grain kinematics, and thus our measurement of the scale height.

Our analysis indicates with high confidence that AU Mic exhibited long-term millimeter variability over the ~ 1.5 yr observation period. The stellar fluxes preferred by our modeling vary by more than a factor of two from one observation to the next, and are comparable to MacGregor et al. (2013)’s best-fit flux of $320 \pm 60 \mu\text{Jy}$. It

seems likely that this variability is distinct from the 6 minute flare spanning two orders of magnitude that occurred during the June observations. That being said, we cannot rule out the possibility that the observations caught the star in varying states of flare decay, especially as [White \(1996\)](#) note that shorter-wavelength radio flares tend to have slower decay timescales. Simulations of radio emission from low-mass stars allow for variability of more than a factor of two over the entire longitudinal extent of a star ([Llama et al. 2018](#)); it is also possible that different longitudinal regions of AU Mic were facing Earth during the three observations. [Cox & Gibson \(1985\)](#) detect small-scale ($\sim 50\%$) variations over a two-week period in 2 cm to 20 cm observations of AU Mic with the VLA, possibly due to ‘several independent mini-flares’ or rotational modulation of the star. In fact, factor of ~ 2 variability over months to years is typical of ‘quiescent’ microwave emission from cool stars ([Guedel 1994](#)). Regardless of the origin of AU Mic’s short- and long-term variability, we emphasize the importance of accounting for stellar emission/variability in observations of circumstellar disks around low-mass stars, especially in light of the Proxima Centauri flare discovered by [MacGregor et al. \(2018\)](#).

5.1. Radial Structure

Modeling of the radial structure discussed in §4.2 is broadly consistent with the previous analysis of millimeter wavelength emission from the disk performed by [MacGregor et al. \(2013\)](#) as can be seen in Figure 6. However, the factor of ~ 2 increase in spatial resolution introduces additional interpretive complexities when comparing the results. While our outer radius is only 2 au larger than the previously reported value of 40.3 au (confidence intervals are ~ 0.4 au for both measurements), things become more complicated when considering the inner radius r_{in} and surface brightness power law index p . In contrast to $r_{in} = 23.8^{+0.6}_{-0.9}$ au preferred by our MCMC analysis, [MacGregor et al. \(2013\)](#) report $8.8^{+11.0}_{-1.0}$ au. Neither parameter is well constrained: the authors report a 3σ upper limit of 21 au, whereas conversely we find a 2σ lower limit of ~ 1 au. Similar discrepancies arise in the posterior distribution for p , which is degenerate with r_{in} . While [MacGregor et al. \(2013\)](#) finds $p = 2.32^{+0.21}_{-0.31}$, we recover a median value of $p = 0.9^{+0.5}_{-0.4}$. In our analysis, the uncertainties in these two parameters arise from the existence of two families of solutions: one at $r_{in} \sim 23$ au, $r_{out} \sim 42$ au, $p \sim 0.8$ and another at $r_{in} \sim 5$ au, $r_{out} \sim 41$ au, $p \sim 2.8$ (Figure 6). The latter family, which has a lower likelihood, is probably associated with the local intensity maxima on either of the star examined in §4. Our exploratory

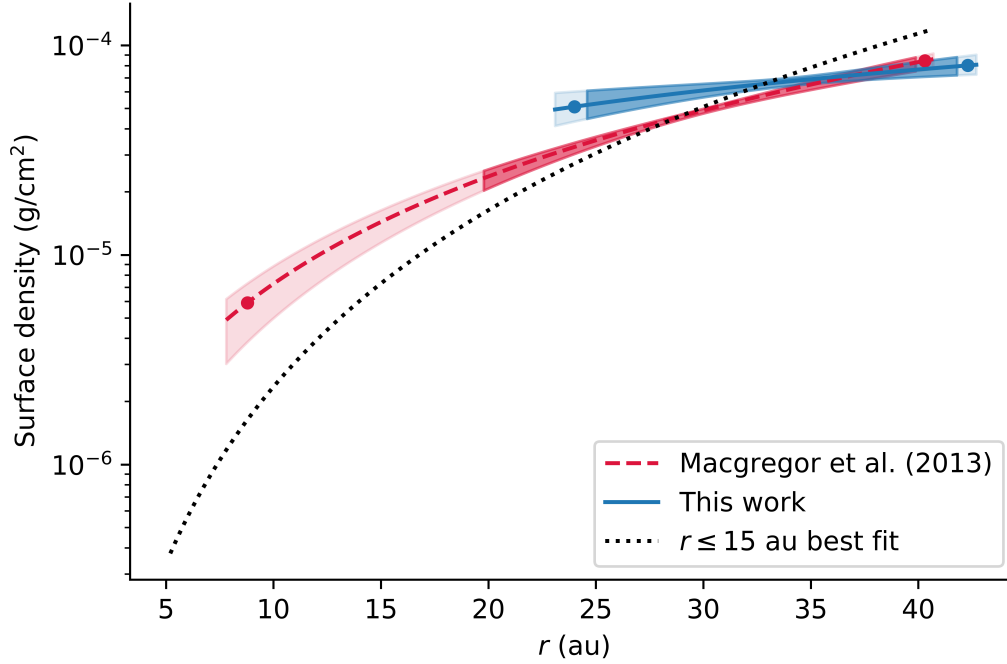


Figure 6. Comparison between the best-fit surface density profiles obtained in [MacGregor et al. \(2013\)](#) (solid red line) and this work (dashed blue line). Also included is the best-fit surface density profile associated with the lower-likelihood family of solutions (dotted black line). The vertical extent of the shaded regions marks 1σ confidence intervals on the surface density. The points designate the best-fit inner and outer radii for each model, and the horizontal extent of the more transparent shaded regions show 1σ confidence intervals on the inner and outer radii. Not included in the uncertainties are the 10% flux uncertainties of each observation.

modeling of these features raises the possibility of an annulus of dust interior to the main disk—if such an annulus does exist, the ~ 2 times lower resolution observations from [MacGregor et al. \(2013\)](#) would probably not have been able to distinguish the annulus emission from that of the main disk. In fact, an unresolved annulus would likely bias the inner radius preferred by the authors’ modeling towards smaller values and could account for the differences in our characterization of the radial structure.

While the annulus model provides only a marginally significantly improved fit to the data, previous observations spanning a wide range of wavelengths have recovered surface brightness enhancements at the same projected stellocentric separation

(~ 10 au) as the hypothetical annulus. A local maximum is present to the SE of the star at this separation in lower-resolution ALMA observations by [MacGregor et al. \(2013\)](#), and there is a suggestive peak in the noise on the opposite side of the star as well. Although these surface brightness enhancements do not attain 3σ significance after subtraction of an axisymmetric model, the independent detection of these features in both data sets suggests that they may be real. [Schneider et al. \(2014\)](#) also observe an optical-wavelength ‘bump’ ~ 13 au SE of the star and slightly elevated from the disk midplane (i.e. to the NE). No matching surface brightness enhancement is observed on the NW side of the disk, which is obscured by the STIS occulting wedge for $r \lesssim 12$ au. On the other hand, the scattered light emission on the NW side is not symmetric about the midplane and the authors tentatively identify a warp below the midplane extending to a distance of ~ 45 au from the star. They note that these features may share a common causality, and posit that dust orbits in the inner disk are non-coplanar with those found at larger separations.

Near-infrared GPI observations presented in [Wang et al. \(2015\)](#) further corroborate the presence of a ‘bump’ to the SE, characterized by a FWHM roughly triple the FWHM at an equivalent separation on the NW side of the disk. No features are detected at a corresponding separation to the NW. Figure 4 of [Wang et al. \(2015\)](#) shows a composite map of the bump as seen by GPI, STIS, and ALMA; the common location of the bump in both scattered light and mm observations would indicate that the mm- and micron-sized grains are cospatial. The micron-sized grains traced by scattered light are thought to be mostly confined to a narrow ‘birth ring’ at ~ 40 au ([Strubbe & Chiang 2006](#)). Thus, if the millimeter bump visible in both this work and in [MacGregor et al. \(2013\)](#) is indeed cospatial with the scattered light bump, it would suggest that the true stellocentric separation of the millimeter feature is ~ 40 au and that its apparent stellocentric separation of ~ 10 au is due to projection effects.

5.2. Vertical Structure

As discussed in §4.3, our MCMC analysis yields a median aspect ratio of $h = 0.031 \pm 0.005$; at a reference point of 40 au, this translates to a vertical scale height $H = 1.2 \pm 0.2$ au. This measurement is marginally consistent with values cited in the literature, ranging from roughly 0.6 au to 2 au and derived from observations spanning the optical to the sub-millimeter. [Schüppler et al. \(2015\)](#) place an upper limit of 0.05 on the 1.3 mm opening angle (equivalent to the aspect ratio for

small angles) by extracting the image-domain vertical profile from MacGregor et al. (2013)’s vertically unresolved ALMA observations, and estimate a visible-wavelength opening angle of 0.03 by reading off the vertical scale height from Schneider et al. (2014)’s STIS image of the disk. Metchev et al. (2005) approximate a H -band Keck FWHM of ~ 4 au at a separation of 40 au; Krist et al. (2005) fit a vertical Lorentzian profile to multicolor HST observations of the disk and find the FWHM interior to 50 au to fall between 2.5 au and 3.5 au.

Because the measurements quoted above are determined from the observed vertical thickness of AU Mic’s disk, they can be affected by the radial structure and viewing geometry of the disk as well as scattering effects. As such, parametric modeling provides a more reliable way to assess AU Mic’s vertical structure. Krist et al. (2005) report a FWHM between 1.73 au and 1.74 au at a separation of 20 au from three-dimensional scattering models. Collisional modeling can also be used to learn about AU Mic’s vertical structure: collisional velocities—and thus dust production—are affected by the maximum eccentricity of planetesimal bodies e_{max} , which in turn can be related to the disk vertical structure (see §5.3 below). Schüppler et al. (2015) perform such modeling constrained by photometric observations spanning visible to millimeter wavelengths and quote a reference model opening angle of 0.015. The authors go on to note that an opening angle of 0.005 better reproduces the disk spectral energy distribution (SED) in the long-wavelength regime beyond $100\ \mu\text{m}$, but is unable to reproduce flux measurements for $\lambda \leq 70\ \mu\text{m}$.

In sum, estimates of AU Mic’s vertical structure vary widely depending on the wavelength of observation, the techniques used, and the assumptions made. Rigorous comparison between measurements in the literature is difficult—for example, Krist et al. (2005) assume a flared vertical profile while other authors use a linear parameterization for the scale height. Nevertheless, some general statements may be made. Values determined from optical and near-infrared observations range from roughly $H = 1.2$ au to 2 au at a radius of 40 au, while the values determined at least in part from mm observations range from $H = 0.6$ au to 2 au, the latter being an upper limit. Estimates based on millimeter observations (including this work) tend to be smaller than those derived from shorter-wavelength observations, although the two wavelength regimes do not provide radically different values.

It is not unexpected that optical and infrared measurements of the scale height would exceed millimeter-wavelength estimates. Thébault (2009) suggests that the

smaller grains traced by short-wavelength observations can be placed on inclined orbits by radiation pressure (and to first order, disk winds) even in the absence of large bodies dynamically stirring the disk. This effect preferentially excites smaller dust grains, ‘puffing’ up the disk at mid-IR to visible wavelengths, while the larger grains that dominate emission at longer wavelengths remain near the midplane. [Thébault \(2009\)](#) proposes a ‘natural’ minimum debris disk thickness of $h = 0.04 \pm 0.02$ as seen at wavelengths smaller than $50 \mu\text{m}$. The author also runs a collisional model tailored to the AU Mic system assuming no intrinsic dynamical excitation, and reports $H = 1 \text{ au}$ for $r \leq 40 \text{ au}$ when degraded to the resolution of scattered light images. Although this scale height falls within the range of ‘natural’ debris disk thicknesses, the authors stress that this does not amount to an assertion that the disk is dynamically cold due to the simplicity of their model and fitting process.

In recent years, the vertical structure of several other debris disks has been tentatively resolved with ALMA. $\sim 5.5 \text{ au}$ spatial resolution observations of CO J = 3 – 2 and 2 – 1 line emission from the edge-on β Pic debris disk presented by [Matrà et al. \(2017\)](#) suggest that the disk is resolved in the vertical direction. The beam-subtracted apparent FWHM, determined in a similar manner as the bottom pane of Figure 2 in this work, ranges between $\sim 7 \text{ au}$ and 12 au over the $\sim 100 \text{ au}$ radial extent of the disk. Assuming an Keplerian rotation and edge-on inclination, the authors report the following scale height-radius relation:

$$H = 7.0 \pm 0.6 \times \left(\frac{R}{85 \text{ au}} \right)^{0.75 \pm 0.02} \text{ au} \quad (4)$$

where the scale height H is the standard deviation of the Gaussian vertical density distribution. For reference to this work, this corresponds to a scale height of 4 au at a separation of 40 au . [Kennedy et al. \(2018\)](#) analyze $11.6 \text{ au} \times 13.1 \text{ au}$ spatial resolution observations of the HR 4796A debris disk, reporting a marginal detection of the disk scale height. The authors find that a vertically resolved ring ($\text{FWHM} = 7 \pm 1 \text{ au}$) is favored over a vertically unresolved ring ($\text{FWHM} < 4 \text{ au}$) with $\Delta BIC = 6.8$. This FWHM corresponds to a Gaussian standard deviation $H \approx 3.0 \pm 0.4 \text{ au}$ and, at the $\sim 80 \text{ au}$ radial location of the ring, a scale factor of $h \approx 0.038 \pm 0.005$. Although the relative BIC reported by the authors meets the condition for ‘strong’ evidence of a statistically higher-quality fit ($\Delta BIC > 6$), the fact that the preferred FWHM is nearly a factor of two smaller than the spatial resolution of the data calls into question the certainty of the measurement. In sum, the vertical structure of debris

disks is just beginning to be resolved in the millimeter thanks to the improvements in sensitivity and resolution provided by ALMA; to our knowledge, AU Mic exhibits the narrowest millimeter-wavelength scale height of any known debris disk.

5.3. *Inferring the Mass of Stirring Bodies*

Information regarding the bodies dynamically stirring AU Mic’s disk can be recovered by relating the scale height to the dynamical excitation of the disk’s dust grains. As discussed by [Th  bault \(2009\)](#) and [Quillen et al. \(2007\)](#), the planetesimals responsible for stirring the disk impart kinetic energy to the dust, perturbing them from a Keplerian orbit and thus increasing their eccentricity dispersion $\langle e^2 \rangle$. Here we define $\bar{e} = \sqrt{\langle e^2 \rangle}$ and $\bar{i} = \sqrt{\langle i^2 \rangle}$, where $\langle i^2 \rangle$ is the inclination dispersion of the dust grains. In equilibrium there is an equipartition between the vertical and in-plane components of the velocities imparted to the grains, so $\bar{i} = \bar{e}/2$. For low inclinations, inclination can be related to the observed aspect ratio using $\bar{i} = \sqrt{2}h$. The interparticle relative velocity $\langle v_{rel} \rangle$ can then be determined directly from observables using the following relation ([Wetherill & Stewart 1993](#); [Wyatt & Dent 2002](#)):

$$\langle v_{rel} \rangle = v_{Kep}(r) \sqrt{\bar{i}^2 + 1.25\bar{e}^2} \quad (5)$$

where $v_{Kep}(r)$ is the Keplerian velocity at radius r . Adopting a stellar mass of $0.5 M_\odot$ from the literature ([Plavchan et al. 2009](#); [Houdebine & Doyle 1994](#)) and taking $r = 40$ au, $h = 0.031 \pm 0.005$ yields $v_{rel} = 360 \pm 60$ m/s.

The collisional velocities v_{rel} of dust grains will never exceed the escape velocities $v_{esc}(a_{big})$ of the large bodies governing the disc’s dynamics; $v_{rel} = v_{esc}(a_{big})$ only if velocity damping is not significant and all the bodies in the disk have had time to be gravitationally excited by the largest planetesimals. As such, we can use our estimate for v_{rel} to place a lower limit on the escape velocity and thus size a_{big} of bodies stirring the disk. Assuming a density of 2 g cm^{-3} , we find $a_{big} \sim 340 \pm 60$ km and $m_{big} \sim 3.2 \pm 1.1 \times 10^{20}$ kg, i.e. 2.5% the mass of Pluto. On the other hand, the disk may be in a steady state in which velocity damping is balanced with excitation (rather than damping being inefficient). Under this condition the scale height provides an estimate of the total mass of stirring bodies, not their size. To relate the observed disk scale height to the total mass of bodies stirring the disk, we refer to [Pan & Schlichting \(2012\)](#)’s theoretical models of steady state size-dependent velocity distributions in the collisional cascade. Assuming a scale height of 1.2 au at 40 au, a stellar mass

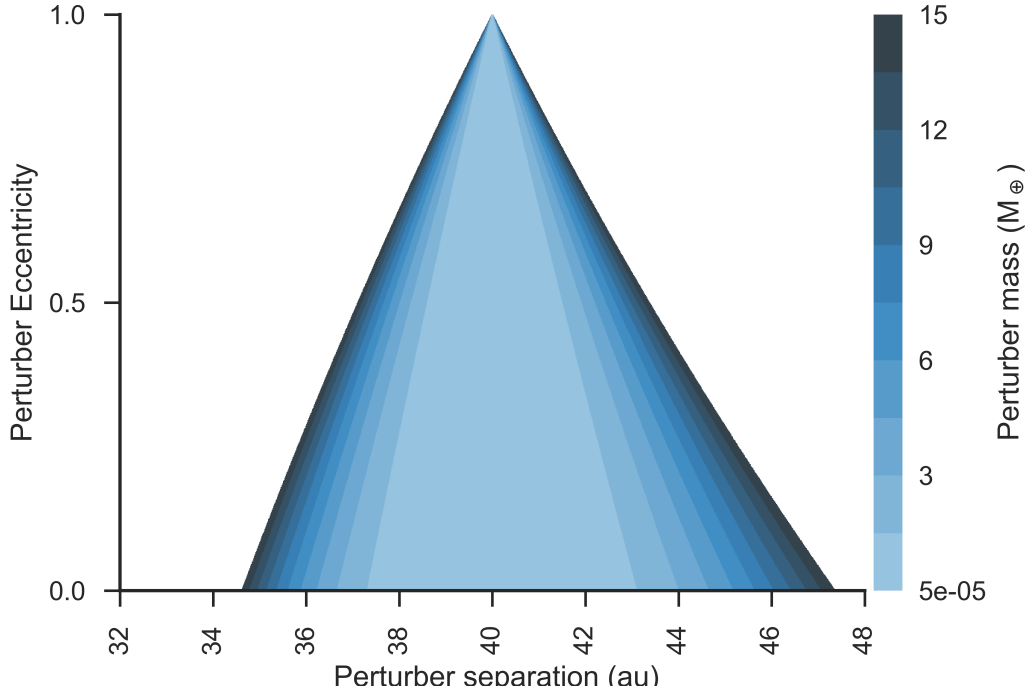


Figure 7. An illustration of the relationship between the mass, separation, and eccentricity of for a single stirring body. The colormap shows the minimum stirring mass for a given orbital separation and eccentricity. Colormap values range from $5 \times 10^{-5} M_{\oplus}$ (the lower limit placed on the perturber mass m_{big}) to $15 M_{\oplus}$ (slightly less than the mass of Neptune). The lightest shade of blue covers the entire range of perturber masses predicted by our calculations.

of $0.5 M_{\odot}$, and a dust mass of $0.01 M_{\oplus}$, these models indicate a dynamical mass of $\sim 1.5 M_{\oplus}$. If all of the $1.5 M_{\oplus}$ were locked up in a single body, it would have a radius of $\sim 1.1 R_{\oplus}$ assuming a mean density of 5.5 g cm^{-3} characteristic of Earth.

In sum, the largest bodies in the AU Mic disk cannot be smaller than $340 \pm 60 \text{ km}$ or they would not be able to stir the dust grains to the collisional velocities inferred from the measured scale height. Conversely, the largest body stirring the disk cannot be larger than $\sim 1.5 M_{\oplus}$ or the scale height would exceed the value measured in this work. It should also be noted that because the scale height measured at the outer edge of the disk is comparable to the spatial resolution of the data, and since scale height decreases with decreasing radius, the observations are only sensitive to the scale height near the $\sim 40 \text{ au}$ outer disk radius. If the disk is stirred by an ensemble

of 340 km planetesimals, they would necessarily be located within this outer region of the disk. That being said, a planet is capable of stirring the disk at a distance of roughly five Hill Radii (Greenzweig & Lissauer 1990), defined as²

$$r_H = a(1 - e) \left(\frac{m_p}{3M_\star} \right)^{1/3}. \quad (6)$$

Thus if the mass were concentrated within a single $1.5 M_\oplus$ body, it could be located as far as 3 au interior or exterior to the debris belt. Similarly, our measurement of the scale height excludes Uranus or Neptune analogs of mass $\sim 15 M_\oplus$ within 6 au of the parent body belt. Figure 7 shows the relationship between the eccentricity, orbital separation, and mass of a single perturbing body.

6. CONCLUSION

We have presented new 1.3 mm ALMA observations of thermal dust emission from the debris disk around AU Mic at nearly double the angular resolution of previous observations. Both the vertical and radial structure of the disk are resolved. MCMC analysis prefers an aspect ratio $h = 0.031$, corresponding to a vertical scale height $H = 1.2$ au in the outer regions of the disk. Our analysis suggests that this is not a lower limit; a model with vertically resolved structure provides a statistically improved fit to the data over a model with unresolved vertical structure at a 4σ confidence level. Furthermore, the disk vertical FWHM derived from parametric modeling corresponds well with image-domain estimates of the beam-subtracted FWHM of the emission perpendicular to the disk plane.

By comparing our measurement of the scale height to the steady-state collisional modeling of Pan & Schlichting (2012) we are able to place constraints on the mass and size of bodies stirring AU Mic’s disk. In the lower-limit case where collisional velocity damping is inefficient, the stirring bodies would have a radius of 340 ± 60 km, corresponding to a characteristic mass ~ 50 times less than that of Pluto. On the other hand, velocity damping may balance stirring; this condition allows us to place an upper limit of $\sim 1.5 M_\oplus$ on the mass of stirring bodies. This is a dynamical mass, distinct from the lunar mass of dust grains inferred from the millimeter flux of the disk. These results therefore rule out the presence of a gas giant or Neptune analog

² To Margaret and Hilke: Meredith and I are a little confused here, as the expression for the Hill radius would imply that the stirring zone of a planet goes to 0 as its eccentricity goes to 1. Is this okay?

in the outer disk, but are suggestive of a significant population of large asteroids or perhaps an Earth-mass planet stirring the dust distribution.

We see no indication of the fast-moving features detected by Boccaletti et al. (2015), but the data are suggestive of an additional ring of dust at ~ 10 au. Models with a ring interior to the main disk provide a better fit to the data, but measures of statistical significance remain equivocal as to whether such models minimize the information lost in the modeling process. Thus the presence of a ring remains uncertain. If a secondary ring of dust does exist in the AU Mic debris disk, planets are of course an obvious explanation; P. Plavchan et al. (in preparation) propose a Jovian-mass exoplanet candidate interior to 1 au, but AU Mic’s stellar activity make it difficult to confirm the radial velocity detection. Even if the candidate is confirmed, it is unlikely that a planet so close to the star would be responsible for a ring at 10 au. That being said, a confirmed detection could provide a promising origin for AU Mic’s fast-moving features.

Looking forward, the scale height measurement presented in this work could be combined with other measurements of AU Mic’s scale height at widely-separated (sub)millimeter wavelengths. This would allow the size-dependent velocity dispersion and internal strengths of bodies in AU Mic’s collisional cascade to be constrained, testing the assumption of collisional cascade theory that velocity dispersion is constant with grain size. The ALMA Band 9 observations of AU Mic presented in the forthcoming work of Carter et. al (in preparation) may be able to provide such constraints. Our measurements of the AU Mic system provide a proof of concept that spatially resolved observations of the vertical structure at millimeter wavelengths can constrain the presence of Uranus and Neptune analogs, which are undetectable by other planet-detection techniques. Applying this technique to other high-inclination debris disks with a range of central stellar masses will provide unique constraints on the prevalence of Uranus and Neptune analogs throughout the galaxy.

ACKNOWLEDGEMENTS

C.D. is sponsored by a NASA CT Space Grant Undergraduate Research Fellowship and Wesleyan University’s Research in the Sciences Fellowship. C.D., A.M.H., E.C., and K.F. gratefully acknowledge support from NSF grant AST-1412647. This paper makes use of the following ALMA data: ADS/JAO.ALMA#2012.1.00198.S. ALMA is a partnership of ESO (representing its member states), NSF (USA) and NINS (Japan), together with NRC (Canada), MOST and ASIAA (Taiwan), and KASI

(Republic of Korea), in cooperation with the Republic of Chile. The Joint ALMA Observatory is operated by ESO, AUI/NRAO and NAOJ. The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc.

Software: CASA (McMullin et al. 2007), MIRIAD (Sault et al. 1995), NumPy (Van Der Walt et al. 2011), Astropy (The Astropy Collaboration et al. 2018), Pandas (McKinney 2010), emcee (Foreman-Mackey et al. 2013), Uncertainties, <http://pythonhosted.org/uncertainties/>

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