

Breakeven occurs when return of credit bond equals return of govt bond.

If credit bond initially has rating  $i$  :

$$t_{i1}r_{i1} + \dots + t_{i8}r_{i8} = g$$

where

$t_{ij}$  is the probability of bond currently rated  $i$  ending up rated  $j$

$r_{ij}$  is the return of a bond currently rated  $i$  which ends up rated  $j$

$g$  is the return of a government bond

Now

$$r_{ij} = \frac{q_j + c_j}{p_i} - 1$$

where

$p_i$  is the current price of a bond rated  $i$

$q_j$  is the final price of a bond which ends up rated  $j$

$c_j$  is the coupon of a bond which end up rated  $j$

$c_j = y$ , for  $j = 1, \dots, 7$  where  $y$  is the (annualised) yield of a government bond

$c_j = 0$ , for  $j = 8$

$$\therefore \sum_{j=1}^8 t_{ij} \left( \frac{q_j + c_j}{p_i} - 1 \right) = g$$

$$\therefore \sum_{j=1}^8 t_{ij} q_j + y(1 - t_{i8}) = p_i (g + 1) \quad \text{since} \quad \sum_{j=1}^8 t_{ij} = 1$$

$$\therefore \sum_{j=1}^8 t_{ij} q_j = p_i (g + 1) - y(1 - t_{i8})$$

$$\therefore \sum_{j=1}^7 t_{ij} q_j = p_i (g + 1) - (y(1 - t_{i8}) + t_{i8} q_8) \quad (\text{note summation range})$$

where  $q_8$  is the assumed recovery rate

Rewrite this as:

$$Tq = p^*$$

$$\therefore q = T^{-1}p^*$$

In other words, this gives us the final prices of all credit bonds for breakeven, from which we can calculate the corresponding yields and spreads.