

Package ‘Brq’

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Description

This function implements the idea of Bayesian adaptive Lasso quantile regression employing a likelihood function that is based on the asymmetric Laplace distribution. The asymmetric Laplace error distribution is written as a scale mixture of normals as in Reed and Yu (2009). The proposed method (BALqr) extends the Bayesian Lasso quantile regression by allowing different penalization parameters for different regression coefficients (Alhamzawi et al., 2012).

Usage

```
BALqr(x,y, tau = 0.5, runs = 11000, burn = 1000, thin=1)
```

Arguments

x	Matrix of predictors.
y	Vector of dependent variable.
tau	The quantile of interest. Must be between 0 and 1.
runs	Length of desired Gibbs sampler output.
burn	Number of Gibbs sampler iterations before output is saved.
thin	thinning parameter of MCMC draws.

Author(s)

Rahim Alhamzawi

References

- [1] Alhamzawi, Rahim, Keming Yu, and Dries F. Benoit. (2012). Bayesian adaptive Lasso quantile regression. *Statistical Modelling* 12.3: 279-297.
- [2] Reed, C. and Yu, K. (2009). A partially collapsed Gibbs sampler for Bayesian quantile regression. *Technical Report*. Department of Mathematical Sciences, Brunel University. URL: <http://bura.brunel.ac.uk/bitstream/2438/3593/1/fulltext.pdf>.

Examples

```
# Example
n <- 150
p=8
Beta=c(5, 0, 0, 0, 0, 0, 0, 0)
x <- matrix(rnorm(n=p*n),n)
x=scale(x)
y <- x%%Beta+rnorm(n)
y=y-mean(y)
```

```
fit = Brq(y~0+x,tau=0.5, method="BALqr",runs=5000, burn=1000)
summary(fit)
```

BALtqr

Bayesian adaptive Lasso tobit quantile regression

Description

This function implements the idea of Bayesian adaptive Lasso tobit quantile regression employing a likelihood function that is based on the asymmetric Laplace distribution. The asymmetric Laplace error distribution is written as a scale mixture of normal distributions as in Reed and Yu (2009). The proposed method (BALtqr) extends the Bayesian Lasso tobit quantile regression by allowing different penalization parameters for different regression coefficients (Alhamzawi et al., 2013).

Usage

```
BALtqr(x,y, tau = 0.5, left = 0, runs = 11000, burn = 1000, thin=1)
```

Arguments

x	Matrix of predictors.
y	Vector of dependent variable.
tau	The quantile of interest. Must be between 0 and 1.
left	Left censored point.
runs	Length of desired Gibbs sampler output.
burn	Number of Gibbs sampler iterations before output is saved.
thin	thinning parameter of MCMC draws.

Author(s)

Rahim Alhamzawi

References

- [1] Alhamzawi, Rahim. (2013). Tobit Quantile Regression with the adaptive Lasso penalty. The Fourth International Arab Conference of Statistics, 450 ISSN (1681 6870).
- [2] Reed, C. and Yu, K. (2009). A partially collapsed Gibbs sampler for Bayesian quantile regression. *Technical Report*. Department of Mathematical Sciences, Brunel University. URL: <http://bura.brunel.ac.uk/bitstream/2438/3593/1/fulltext.pdf>.

Examples

```
# Example
n <- 150
p=8
Beta=c(5, 0, 0, 0, 0, 0, 0, 0)
x <- matrix(rnorm(n=p*n),n)
x=scale(x)
y <-x%%Beta+rnorm(n)
y=y-mean(y)
y=pmax(0, y)

fit = Brq(y~0+x,tau=0.5, method="BALtqr",runs=5000, burn=1000)
summary(fit)
model(fit)
```

BLqr

Bayesian Lasso quantile regression

Description

This function implements the idea of Bayesian Lasso quantile regression using a likelihood function that is based on the asymmetric Laplace distribution (Rahim, 2016). The asymmetric Laplace error distribution is written as a scale mixture of normal distributions as in Reed and Yu (2009). This function implements the Bayesian lasso for linear quantile regression models by assigning scale mixture of normal (SMN) priors on the parameters and independent exponential priors on their variances. We propose an alternative Bayesian analysis of the Bayesian lasso problem reported in Li, et al. (2010). A Gibbs sampling algorithm for the Bayesian Lasso quantile regression is constructed by sampling the parameters from their full conditional distributions.

Usage

```
BLqr(x,y, tau = 0.5, runs = 11000, burn = 1000, thin=1)
```

Arguments

x	Matrix of predictors.
y	Vector of dependent variable.
tau	The quantile of interest. Must be between 0 and 1.
runs	Length of desired Gibbs sampler output.
burn	Number of Gibbs sampler iterations before output is saved.
thin	thinning parameter of MCMC draws.

Author(s)

Rahim Alhamzawi

References

- [1] Alhamzawi, R. (2016). Bayesian variable selection in quantile regression using asymmetric Laplace distribution. Working paper.
- [2] Reed, C. and Yu, K. (2009). A partially collapsed Gibbs sampler for Bayesian quantile regression. *Technical Report*. Department of Mathematical Sciences, Brunel University. URL: <http://bura.brunel.ac.uk/bitstream/2438/3593/1/fulltext.pdf>.
- [3] Li, Q., Xi, R. and Lin, N. (2010). Bayesian regularized quantile regression. *Bayesian Analysis*, 5(3): 533-56.

Examples

```
# Example
n <- 150
p=8
Beta=c(5, 0, 0, 0, 0, 0, 0, 0)
x <- matrix(rnorm(n=p*n),n)
x=scale(x)
y <-x**Beta+rnorm(n)
y=y-mean(y)

fit = Brq(y~0+x,tau=0.5, method="BLqr",runs=5000, burn=1000)
summary(fit)
model(fit)
```

BLtqr

Bayesian tobit quantile regression

Description

This function implements the idea of Bayesian Lasso tobit quantile regression using a likelihood function that is based on the asymmetric Laplace distribution (Rahim, 2016). The asymmetric Laplace error distribution is written as a scale mixture of normal distributions as in Reed and Yu (2009). This function implements the Bayesian lasso for linear tobit quantile regression models by assigning scale mixture of normal (SMN) priors on the parameters and independent exponential priors on their variances. A Gibbs sampling algorithm for the Bayesian Lasso tobit quantile regression is constructed by sampling the parameters from their full conditional distributions.

Usage

```
BLtqr(x,y, tau = 0.5, left = 0, runs = 11000, burn = 1000, thin=1)
```

Arguments

x	Matrix of predictors.
y	Vector of dependent variable.
tau	The quantile of interest. Must be between 0 and 1.

left	Left censored point.
runs	Length of desired Gibbs sampler output.
burn	Number of Gibbs sampler iterations before output is saved.
thin	thinning parameter of MCMC draws.

Author(s)

Rahim Alhamzawi

Examples

```
# Example
n <- 150
p=8
Beta=c(5, 0, 0, 0, 0, 0, 0, 0)
x <- matrix(rnorm(n=p*n),n)
x=scale(x)
y <-x%*%Beta+rnorm(n)
y=y-mean(y)
y=pmax(0, y)

fit = Brq(y~0+x,tau=0.5, method="BLtqr",runs=5000, burn=1000)
summary(fit)
model(fit)
```

Body

Exploring Relationships in Body Dimensions

Description

This dataset contains 21 body dimension measurements as well as age, weight, height, and gender on 507 individuals. The 247 men and 260 women were primarily individuals in their twenties and thirties, with a scattering of older men and women, all exercising several hours a week.

Source:

Measurements were initially taken by Grete Heinz and Louis J. Peterson - at San Jose State University and at the U.S. Naval Postgraduate School in Monterey, California. Later, measurements were taken at dozens of California health and fitness clubs by technicians under the supervision of one of these authors.

Usage

data(Body)

Format

The data frame has the following components:

- BiacSk: Biacromial diameter (cm)
- BiilSk: Biiliac diameter, or "pelvic breadth" (cm)
- BitrSk: Bitrochanteric diameter (cm)
- CheDeSk: Chest depth between spine and sternum at nipple level, mid-expiration (cm)
- CheDiSk: Chest diameter at nipple level, mid-expiration (cm)
- ElbowSk: Elbow diameter, sum of two elbows (cm)
- WristSk: Wrist diameter, sum of two wrists (cm)
- KneeSk: Knee diameter, sum of two knees (cm)
- AnkleSk: Ankle diameter, sum of two ankles (cm)
- ShoulGi: Shoulder girth over deltoid muscles (cm)
- ChestGi: Chest girth, nipple line in males and just above breast tissue in females, mid-expiration (cm)
- WaistGi: Waist girth, narrowest part of torso below the rib cage, average of contracted and relaxed position (cm)
- NavelGi: Navel (or "Abdominal") girth at umbilicus and iliac crest, iliac crest as a landmark (cm)
- HipGi: Hip girth at level of bitrochanteric diameter (cm)
- ThighGi: Thigh girth below gluteal fold, average of right and left girths (cm)
- BicepGi: Bicep girth, flexed, average of right and left girths (cm)
- ForeaGi: Forearm girth, extended, palm up, average of right and left girths (cm)
- KneeGi: Knee girth over patella, slightly flexed position, average of right and left girths (cm)
- CalfGi: Calf maximum girth, average of right and left girths (cm)
- AnkleGi: Ankle minimum girth, average of right and left girths (cm)
- WristGi: Wrist minimum girth, average of right and left girths (cm)
- Age: (years)
- Weight: (kg)
- Height: (cm)
- Gender: (1 - male, 0 - female)

Source

Heinz, G., Peterson, L.J., Johnson, R.W. and Kerk, C.J. (2003), "Exploring Relationships in Body Dimensions", *Journal of Statistics Education* , 11.

Bqr

*Bayesian Quantile Regression***Description**

This function implements the idea of Bayesian quantile regression employing a likelihood function that is based on the asymmetric Laplace distribution (Yu and Moyeed, 2001). The asymmetric Laplace error distribution is written as scale mixtures of normal distributions as in Reed and Yu (2009).

Usage

```
Bqr(x,y, tau =0.5, runs =11000, burn =1000, thin=1)
```

Arguments

x	Matrix of predictors.
y	Vector of dependent variable.
tau	The quantile of interest. Must be between 0 and 1.
runs	Length of desired Gibbs sampler output.
burn	Number of Gibbs sampler iterations before output is saved.
thin	thinning parameter of MCMC draws.

Author(s)

Rahim Alhamzawi

Examples

```
# Example 1
n <- 100
x <- runif(n=n,min=0,max=5)
y <- 1 + 1.5*x + .5*x*rnorm(n)
Brq(y~x,tau=0.5,runs=2000, burn=500)
Brq(y~x,tau=0.95,runs=2000, burn=500)

# Example 2
n <- 100
x <- runif(n=n,min=0,max=5)
y <- 1 + 1.5*x + .5*x*rnorm(n)
plot(x,y, main="Scatterplot and Quantile Regression Fit", xlab="x", cex=.5, col="gray")
for (i in 1:5) {
  if (i==1) p = .05
  if (i==2) p = .25
  if (i==3) p = .50
  if (i==4) p = .75
```



```

if (i==5) p = .95
fit = Brq(y~x,tau=p,runs=1500, burn=500)
# Note: runs =11000 and burn =1000
abline(a=mean(fit$coef[1]),b=mean(fit$coef[2]),lty=i,col=i)
}
abline( lm(y~x),lty=1,lwd=2,col=6)
legend(x=-0.30,y=max(y)+0.5,legend=c(.05,.25,.50,.75,.95,"OLS"),lty=c(1,2,3,4,5,1),
lwd=c(1,1,1,1,1,2),col=c(1:6),title="Quantile")

```

Btqr

*Bayesian tobit quantile regression***Description**

This function implements the idea of Bayesian tobit quantile regression employing a likelihood function that is based on the asymmetric Laplace distribution (Yu and Stander, 2007). The asymmetric Laplace error distribution is written as scale mixtures of normal distributions as in Reed and Yu (2009).

Usage

```
Btqr(x,y, tau = 0.5, left = 0, runs = 11000, burn = 1000, thin=1)
```

Arguments

x	Matrix of predictors.
y	Vector of dependent variable.
tau	The quantile of interest. Must be between 0 and 1.
left	Left censored point.
runs	Length of desired Gibbs sampler output.
burn	Number of Gibbs sampler iterations before output is saved.
thin	thinning parameter of MCMC draws.

Author(s)

Rahim Alhamzawi

Examples

```

# Example
set.seed(12345)
x <- abs(rnorm(100))
y <- -0.5 + x + (.25 + .25*x)*rnorm(100)
plot(x,y, type="n")
h <-(y > 0)

```

```

points(x[h],y[h],cex=.9,pch=16)
points(x[!h],y[!h],cex=.9,pch=1)
y <- pmax(0,y)
for(tau in (2:8)/9){
  fit=Brq(y~x,tau=tau, method="Btqr", left=0, runs=1000, burn=500)$coef
  # Note: runs =11000 and burn =1000
  Xs=sort(x)
  Xc=cbind(1,sort(x))
  Xcf=Xc*%c(fit)
  Xcfp=pmax(0,Xcf)
  lines(Xs,Xcfp,col="red")}

```

ImmunogG

Immunoglobulin G Data

Description

This data set comprises the serum concentration (grams per litre) of immunoglobulin G in 298 children aged from 6 months to 6 years and is discussed in detail by Isaacs et al. (1983) and used in Keming et al. (2003).

Usage

```
data("ImmunogG")
```

Format

A data frame with 298 observations on the following 2 variables.

IgG The serum concentration (grams per litre) of immunoglobulin G

Age Age of children in years.

Source

[1] Isaacs, D., Altman, D. G., Tidmarsh, C. E., Valman, H. B. and Webster, A. D. B. (1983) Serum Immunoglobulin concentrations in preschool children measured by laser nephelometry: reference ranges for IgG, IgA and IgM. J. Clin. Path., 36, 1193-1196.

References

[1] Yu, K., Lu, Z., & Stander, J. (2003). Quantile regression: applications and current research areas. Journal of the Royal Statistical Society: Series D (The Statistician), 52(3), 331-350.?

Examples

```

data(ImmunogG)
attach(ImmunogG)
y=IgG
x=Age
X=cbind(x, x^2)
plot(Age,IgG)
plot(Age,IgG, main="Quantile Regression Fit", cex=.5, col="gray")
for (i in 1:5) {
  if (i==1) p = .05
  if (i==2) p = .25
  if (i==3) p = .50
  if (i==4) p = .75
  if (i==5) p = .95
  fit = Brq(y~X,tau=p,runs=400, burn=100)
  # Note: runs =11000 and burn =1000
  curve(fit$coef[1]+fit$coef[2]*x+fit$coef[3]*x^2,col=i,add=TRUE)
}

```

model

Model selection based on credible intervals

Description

Model selection based on credible intervals

Usage

```
model(object)
```

Arguments

object an output object of the Brq function.

plot.Brq

Produce the histogram, autocorrelation and trace plots for the objects of Brq function

Description

plot.Brq is an S3 method that produces histogram, autocorrelation and trace plots for the objects of Brq function

Usage

```
## S3 method for class 'Brq'
plot(x, plottype=c("hist", "trace", "ACF", "traceACF", "histACF", "tracehist",
  "traceACFhist"), Dim=1, breaks=30, lwd=1, col1=0, col2=1, col3=1, col4=1, ...)
```

Arguments

x	an output object of the Brq function, i.e. an S3 object of class Brq.
plottype	should be "hist", "trace", "ACF", "traceACF", "histACF", "tracehist" or "traceACFhist".
Dim	number of parameters that should be plotted
breaks	a single number giving the number of cells for the histogram,
lwd	line width relative to the default (default=1). 2 is twice as wide.
col1	color for the histograms
col2	color for the density of the histograms
col3	color for the autocorrelation
col4	color for the trace plots
...	additional arguments that are passed to the generic plot function

print.Brq	<i>Print the Bayesian quantile regression methods</i>
-----------	---

Description

print.Brq is an S3 method that prints the content of an S3 object of class Brq to the console.

Usage

```
## S3 method for class 'Brq'
print(x,...)
```

Arguments

x	object of class Brq
...	not used.

Value

Print the Bayesian quantile regression methods

print.summary.Brq	<i>Print the summary of Bayesian quantile regression methods.</i>
-------------------	---

Description

print.Brq.summary is an S3 method that prints the content of an S3 object of class Brq.summary to the console.

Usage

```
## S3 method for class 'summary.Brq'
print(x, ...)
```

Arguments

x	object of class Brq.
...	not used.

Value

Print the summary of Bayesian quantile regression methods.

Author(s)

Rahim Alhamzawi

Examples

```
# Simulate data from heteroskedastic regression
set.seed(666)
n <- 100
x <- runif(n=n,min=0,max=10)
y <- 2 + 2*x + 0.6 *x*rnorm(n=n, mean=0, sd=1)

fit <- Brq(y ~ x, tau=0.5, method="Bqr")

# Return Bayes estimates and credible intervals
Results<- summary(fit)

# Print the Brq.summary object
Results
```

Prostate

Prostate Cancer Data

Description

The data is taken from a prostate cancer study (Stamey et al., 1989). It has 97 rows and 9 columns. The response variable is the logarithm of prostate-specific antigen. The covariates are eight clinical measures: the logarithm of cancer volume (lcavol), the logarithm of prostate weight (lweight), age, the logarithm of the amount of benign prostatic hyperplasia (lbph), seminal vesicle invasion (svi), the logarithm of capsular penetration (lcp), the Gleason score (gleason) and the percentage Gleason score 4 or 5 (pgg45).

Usage

```
data("Prostate")
```

Format

The data frame has the following components:

- **lcavol** : The logarithm of cancer volume.
- **lweight** : The logarithm of prostate weight.
- **age** : Age
- **lbph** : The logarithm of the amount of benign prostatic hyperplasia.
- **svi** : Seminal vesicle invasion.
- **lcp** : The logarithm of capsular penetration.
- **gleason** : Gleason score.
- **pgg45** : Percentage Gleason scores 4 or 5.
- **lpsa** : The logarithm of prostate-specific antigen.

Source

Stamey, T. A., Kabalin, J. N., McNeal, J. E., Johnstone, I. M., Freiha, F., Redwine, E. A., and Yang, N. (1989). Prostate specific antigen in the diagnosis and treatment of adenocarcinoma of the prostate. II. Radical prostatectomy treated patients. The Journal of urology, 141(5), 1076-1083.

References

Stamey, T. A., Kabalin, J. N., McNeal, J. E., Johnstone, I. M., Freiha, F., Redwine, E. A., & Yang, N. (1989). Prostate specific antigen in the diagnosis and treatment of adenocarcinoma of the prostate. II. Radical prostatectomy treated patients. The Journal of urology, 141(5), 1076-1083.

Examples

```
data(Prostate)
y=Prostate[,9]
x=as.matrix(Prostate[, -9])
y=y-mean(y)
x=scale(x)
fit=Brq(y~0+x, method="BLqr")
plot(fit, plottype="hist",D=1:8)
plot(fit, plottype="hist",D=1:8, col2=4,lwd=2)
plot(fit, plottype="trace",D=1:8, col4=4)
```

salary	<i>Salaries of 459 US statistics professor data</i>
--------	---

Description

A university union collected data on the salaries of 459 US statistics professors and the number of years for which they had been professors during the period from 1980 to 1990 (Bailar, 1991).

Usage

```
data("salary")
```

Format

A data frame with 459 observations on the following 2 variables.

Salaries Salaries of 459 US statistics professor (1000s of dollars).

Years Number of years as professor

Source

[1] Bailar, B. (1991) Salary survey of U.S. colleges and universities offering degrees in statistics. Amstat News, 182, 3-10.

References

[1] Bailar, B. (1991) Salary survey of U.S. colleges and universities offering degrees in statistics. Amstat News, 182, 3-10.

summary.Brq	<i>Summarize the output of the Brq function</i>
-------------	---

Description

summary.Brq is an S3 method that summarizes the output of the Brq function in an object of class summary.Brq. This function produces the Bayesian estimates and credible intervals for the regression coefficients.

Usage

```
## S3 method for class 'Brq'
summary(object, ...)
```

Arguments

object	an object of class Brq.
...	not used.

Author(s)

Rahim Alhamzawi

References

[1] Alhamzawi, R. (2018). Brq: An R package for Bayesian Quantile Regression. Working paper.

Examples

```
# Example

fit = Brq(stack.loss~stack.x,tau=0.5, method= "Bqr", runs=5000, burn=1000)
summary(fit)
```

USgirl	<i>Weight and age for a sample of 4011 US girl data</i>
--------	---

Description

This data set comprises weight and age for a sample of 4011 US girls reported in Cole (1988) and used in Keming et al. (2003).

Usage

```
data(USgirl)
```


Format

A data frame with 4011 observations on the following 2 variables.

Age Age (years)

Weight Weight (Kg)

References

[1] Cole, T. J. (1988) Fitting smoothed centile curves to reference data (with discussion). J R. Statist. Soc. A, 151, 385-418.

[2] Yu, K., Lu, Z., & Stander, J. (2003). Quantile regression: applications and current research areas. Journal of the Royal Statistical Society: Series D (The Statistician), 52(3), 331-350.?

wheat

Wheat Data

Description

This is a regression data set consisting of 584 observations on 11 variables is taken from the national program for the development of wheat cultivation in Iraq - Qadisiyah governorate branch (2017). The outcome of interest in this dataset is the percentage increase in wheat yield per dunam (2500 square meters).

Usage

```
data("wheat")
```

Format

A data frame with 584 observations on the following 11 variables.

y The percentage increase in wheat yield per dunam (2500 square meters).

U Fertilizer urea (a numeric variable coding the quantity of fertilizer in kilogram).

Ds The date of sowing wheat seeds (a numeric variable coding date: 1 the ideal date, 2 early date, 3 late date).

Qs The quantity of sowing wheat seeds (a numeric variable coding the quantity of seeds in kilogram).

LT The laser field leveling technique (a numeric variable coding technique: 2 if there are used this technique; 1 otherwise; "LT").

NPK The fertilize the field with compound fertilizers (a numeric variable coding the quantity of fertilizer in kilogram).

SMT Seed sowing machine technique (a numeric variable coding the seed sowing machine technique: 2 if there are used this technique; 1 otherwise).

SC Planting mung bean crop (a numeric variable coding type: 2 planting mung bean, 1 otherwise).

- H Herbicide for weed control in crops (a numeric variable coding the quantity of herbicide in milliliter).
- K High potassium fertilizer for crops (a numeric variable coding the quantity of fertilizer in kilogram).
- ME Microelement fertilizer (numeric variable coding the quantity of fertilizer in gram).

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