10 -Spatial Autoregressive Models

Ness Sandoval
Sociology
Saint Louis University

Outline

- Spatial Dependence
- OLS
- Spatial Weights
- Spatial Lag Models
- Spatial Error Models
- Goodness of Fit Statistics
- GeoDa Decision Tree
- Spatial Weights
- Lab Example

Spatial Dependence

The assumption of a BLUE model are not always satisfied in practice

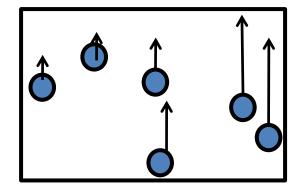
Spatial data may show spatial dependence in the variables and/or error terms

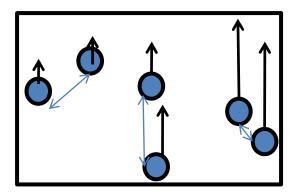
When a value observed in one location depends on the values observed at neighborhood locations, there is a spatial dependence

Spatial Dependence

If Spatial Autocorrelation exists:

- correlation coefficients and coefficients of determination appear bigger than they really are:
 - 1. The statistics are biased upward
 - 2. You think the relationship is stronger than it really is
 - 3. The variables in nearby areas affect each other





If Spatial Autocorrelation exists:

- *Standard errors* appear <u>smaller</u> than they really are:
 - You have exaggerated precision in your model
 - You think your predictions are better than they really are since standard errors measure predictive accuracy
 - More likely to conclude relationship is statistically significant.
 - You will more a Type I error.

$$t = \frac{b}{\text{SE(b)}}$$

Spatial Dependence

- The assumption of uncorrelated error terms is violated
 - Estimates are inefficient
- The assumption of independent observations is violated
 - Estimates are biased
- Analogous to the time-series lagged dependent variable model
- Possible diffusion process events in place predict an increased likelihood of similar events in neighboring places.

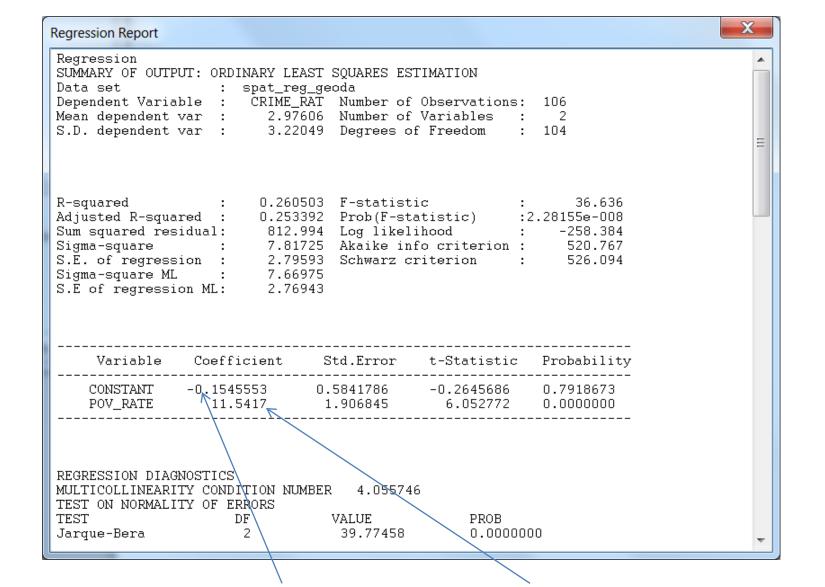
OLS

Regression modelling

$$y_i = \beta_0 + \beta_1 x_1 + \varepsilon_i$$

 ε_i
error captures all the determinants that you:
can't think of;
can't model;
can't measure correctly; and

don't have data to measure.



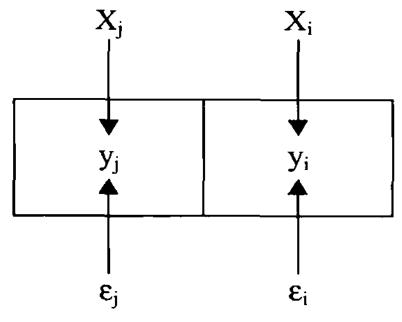
$$y_i = -.1545553 + 11.5417x_1 + \varepsilon_i$$

OLS ad the Spatial Context

• Fail to Reject the Null Hypothesis is assumed.

• This implies that there is no considerable positive association between the dependent variable and it neighbors or the error terms

OLS



No influence from neighbors

Spatial Lag Models

Spatial Dependence - Spatial Lag

- Incorporates spatial dependence by adding a "spatially lagged" DV (y) on the right-hand side of the regression equation
- Treats spatial correlation as a process or effect of interest
- The values of y in one area are directly influenced by the values of y found in neighboring areas
- Positive spatial lag provides evidence that the y's adjacent areas co-vary
- If we ignore the influence of spatially lagged terms:
 - Coefficients will be biased
 - If there is a positive effect of neighboring y's, usually coefficients are biased upward
 - Standard errors are wrong (p-values wrong)

Spatial Lag Model

$$(1)Y_{crime} = B_0 + B_1X_1 + error$$

$$(2a)Y_{crime} = B_0 + W * crime + B_1X_1 + error$$

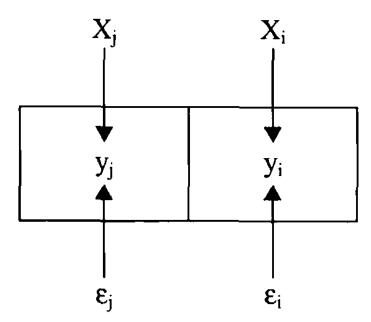
where W is a spatial weight matrix

$$(2b)Y_{crime} = B_0 + \rho w_i y_i + B_1 X_1 + error$$

$$\rho w =$$
 the "spatial lag" of Y_{crime}

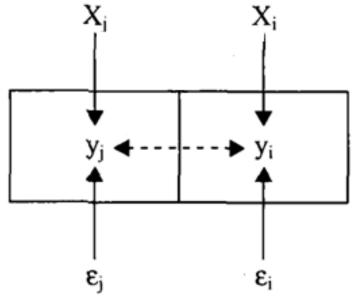
Spatial Lag and Spatial Error Models: conceptual comparison

OLS



No influence from neighbors

SPATIAL LAG



Dependent variable influenced by neighbors

Spatial Error Models

Spatial Error

• Spatial lag is viewed as a substantial issue, spatial error is viewed as a nuisance.

- It is an estimation problem, that needs to be fixed.
- The spatial error assumes that the errors are from the model are spatially correlated.

• Unmeasured factors, for some unknown reason, are correlated across the distance among the observations.

Spatial Error Model

$$(1)Y_{crime} = B_0 + B_1X_1 + error$$

$$(2a)Y_{crime} = B_0 + B_1X_E + error$$

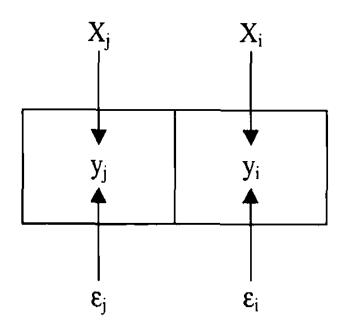
error=W*error+ μ

$$(2b)Y_{crime} = B_0 + B_1X_E + \lambda W\varepsilon + \xi$$

values of the residuals in neighboring locations (W ϵ) are included as an extra term in the equation.

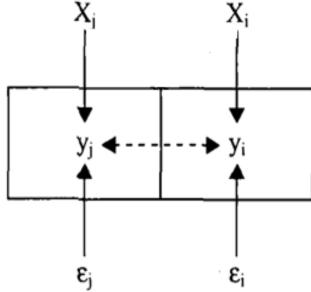
Spatial Lag and Spatial Error Models: conceptual comparison

OLS



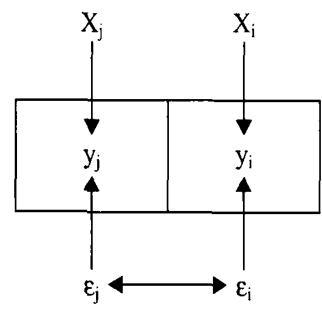
No influence from neighbors

SPATIAL LAG



Dependent variable influenced by neighbors

SPATIAL ERROR



Residuals influenced by neighbors

Goodness of Fit Statistics

Comparing our models

• R² should be used with caution to compare different spatial regression models

- Instead, Log Likelihood (LL) and/or *Akaike Information Criteria* (AIC) is recommended
 - the <u>higher</u> the LL value the <u>better</u> the model
 - the <u>smaller</u> the AIC value the <u>better</u> the model

GeoDa Decision Tree

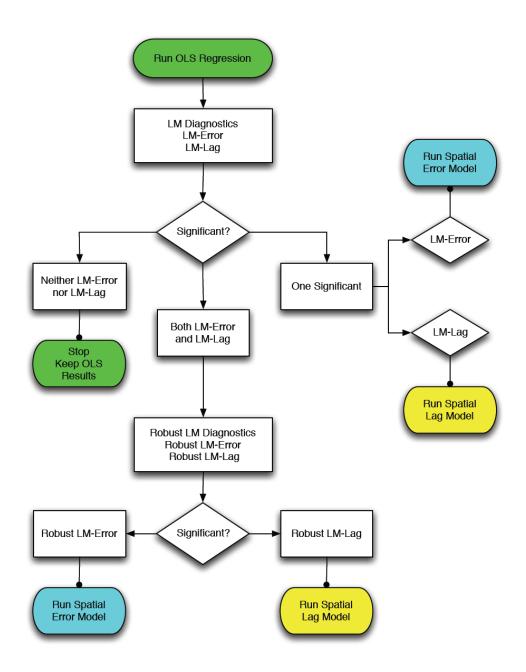


Figure 23.24: Spatial regression decision process.

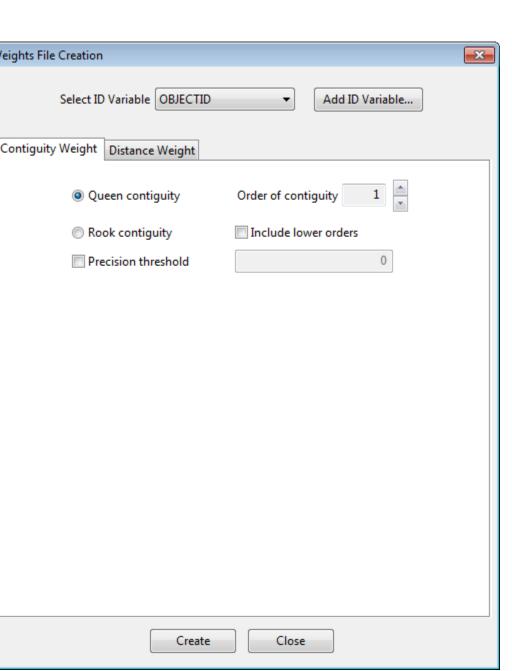
Spatial Weights

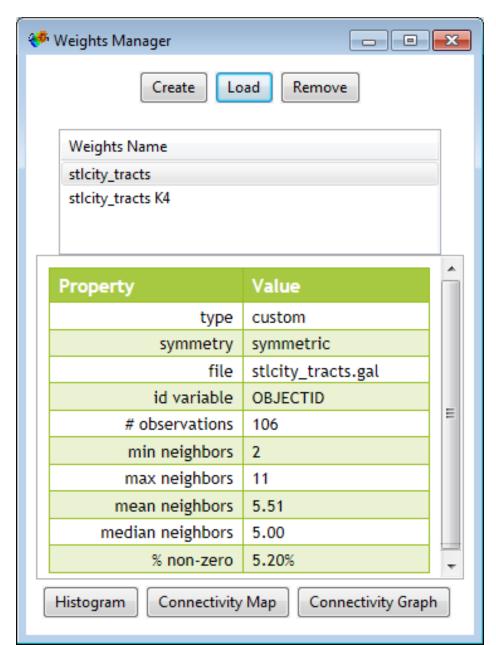
Why Spatial Weights? Part 1

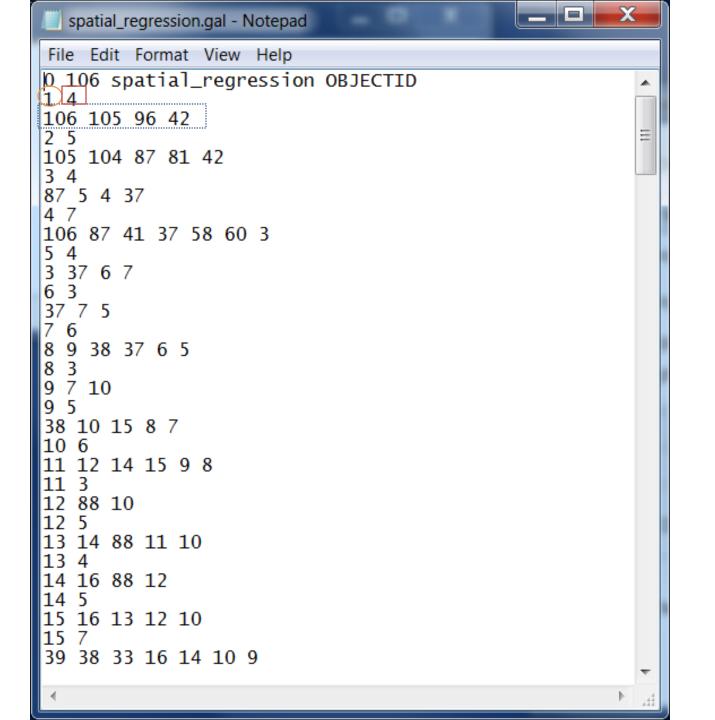
- The problem with spatial data is identification
 - (i.e., spatial co-variance)
 - How do neighbors interact with each other?
 - N2=100*100= 10000 interactions This is not possible.
- Spatial weights imposes structure on the data (i.e., connectivity)
 - What if the interactions were structure?
 - Assume the structure...
 - Quantify spatial similarity

Why Spatial Weights? Part 2

- Pre-specified the interaction
 - In practice, we don't work with non-interactions, we work with interactions
 - 1=interaction only focus on neighbor
 - o=non interaction
- Everything you do is based on the assumption of the spatial weight matrix
 - There is no best weight matrix or optimal weight matrix
 - We will use reasonable assumptions and use goodness of fit to justify choice



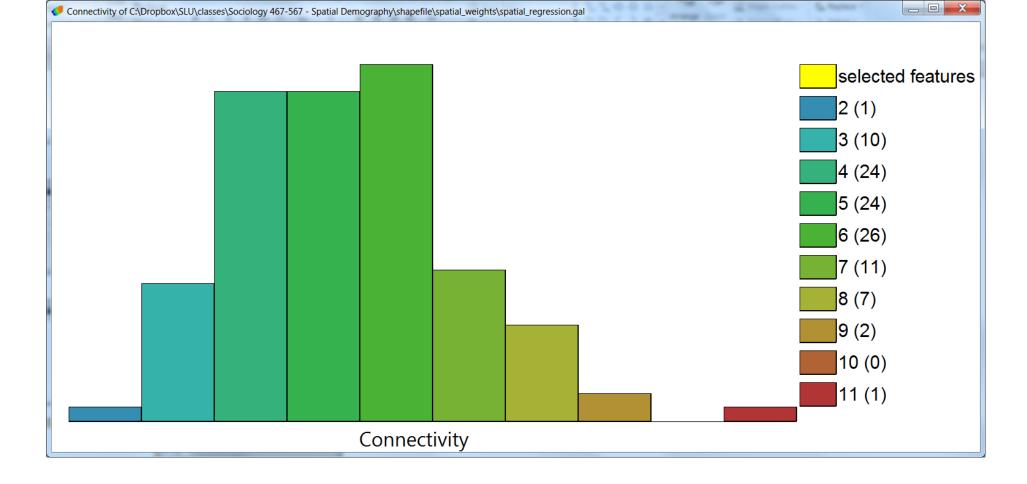




Polygon ID

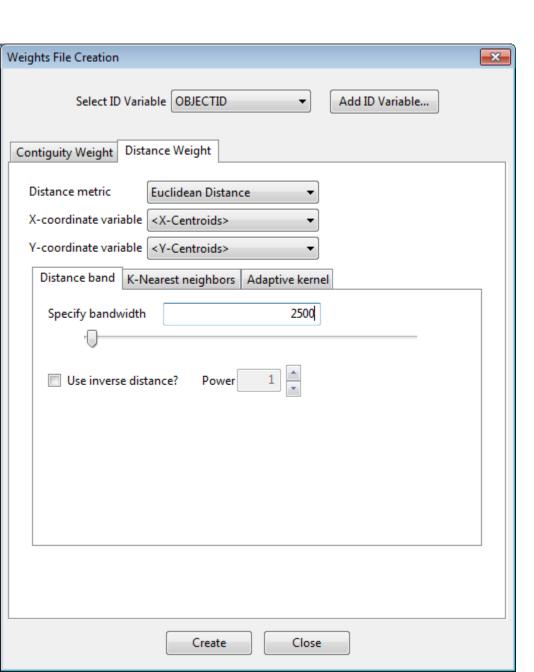
Number of Neighbors

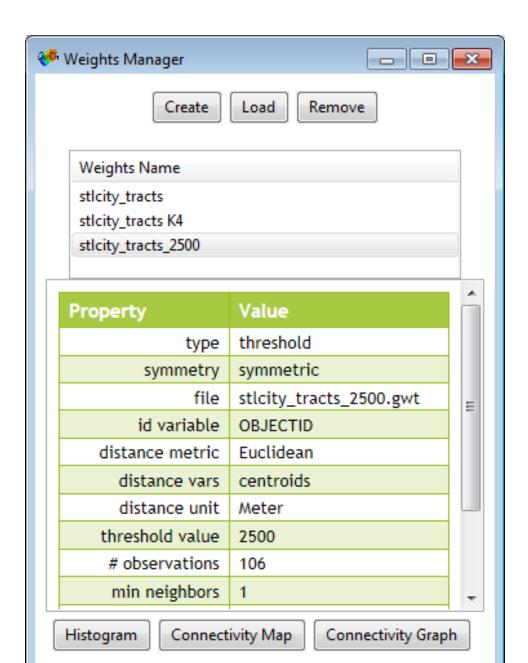
Neighbors

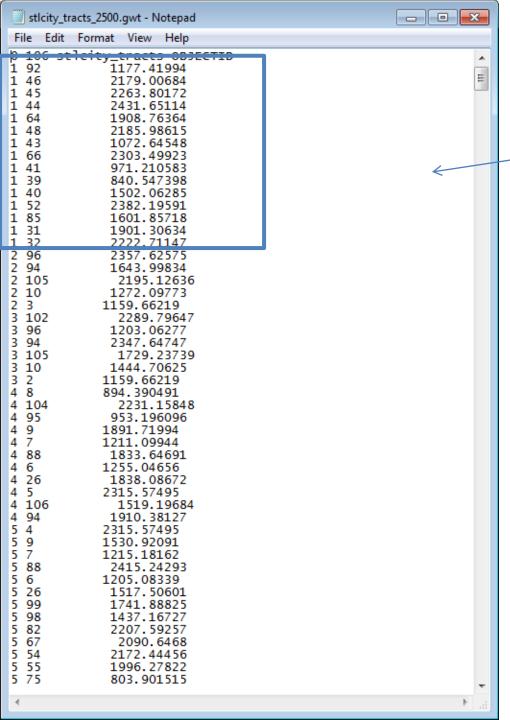


The histogram is particularly useful to identify:

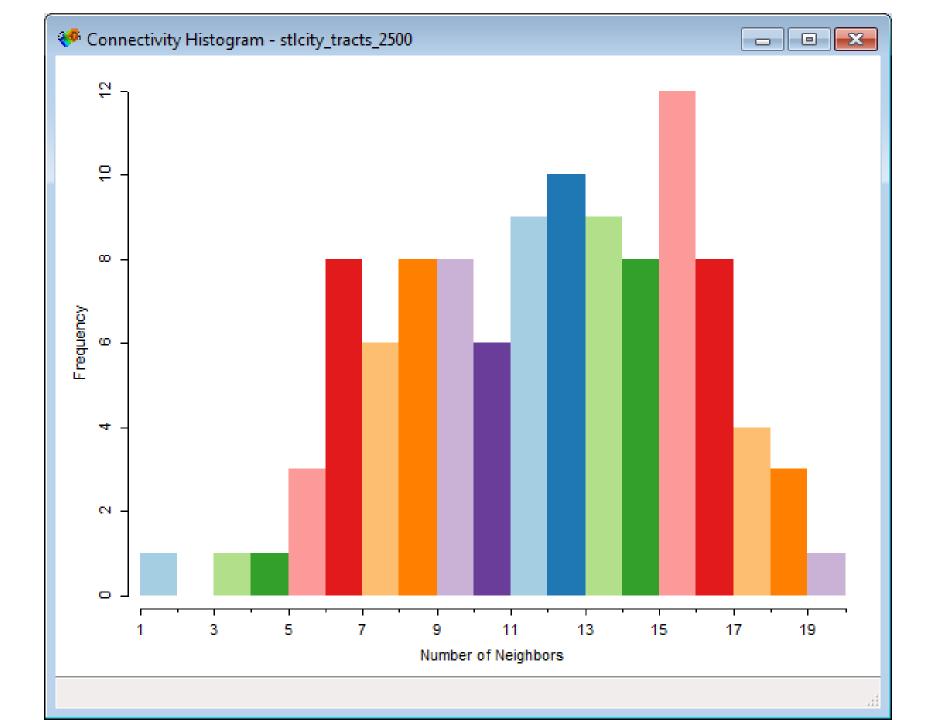
- islands,
- bimodal neighbor distributions,
- data quality problems (e.g., digitizing errors), and
- for linking with the map.

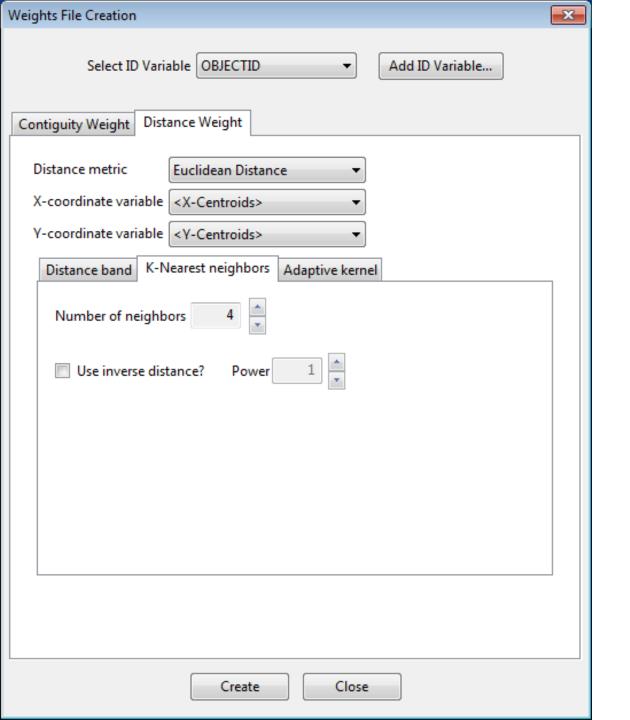


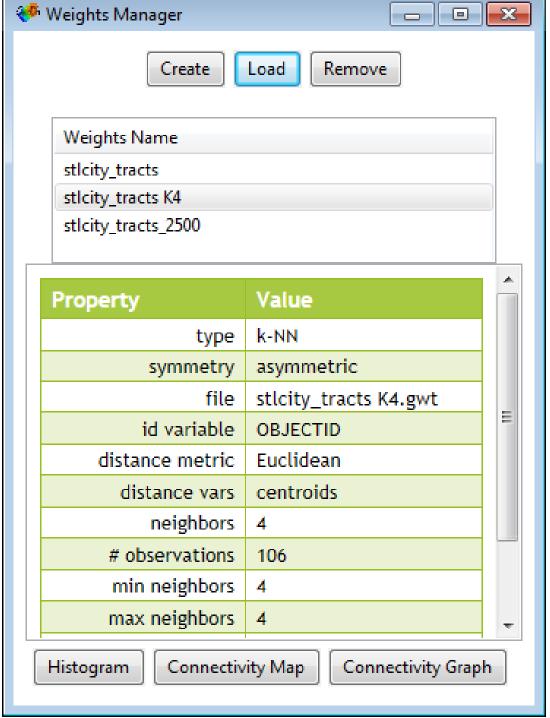


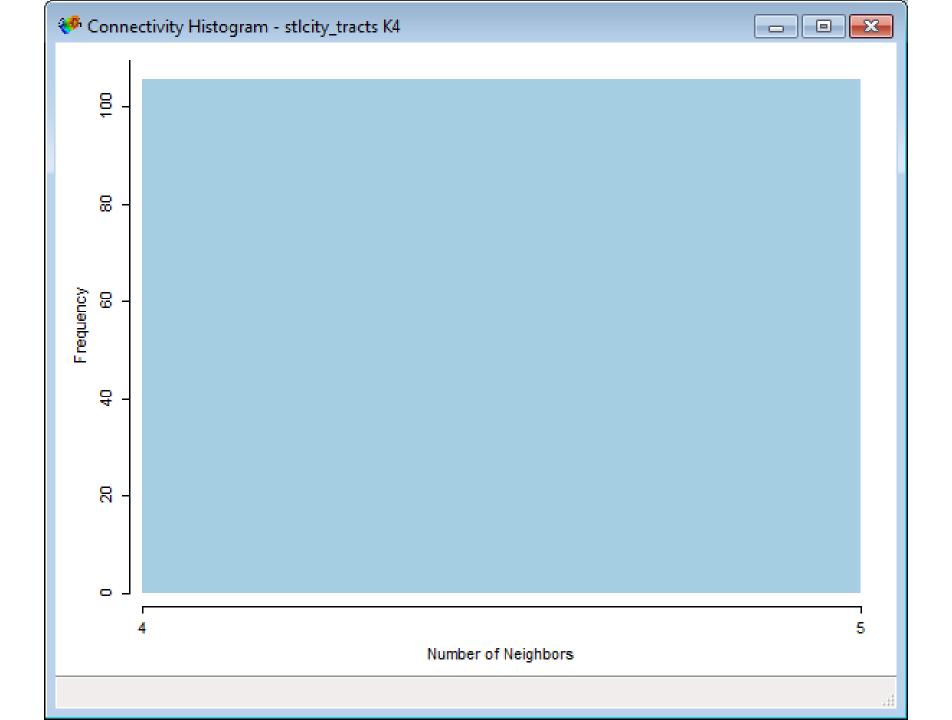


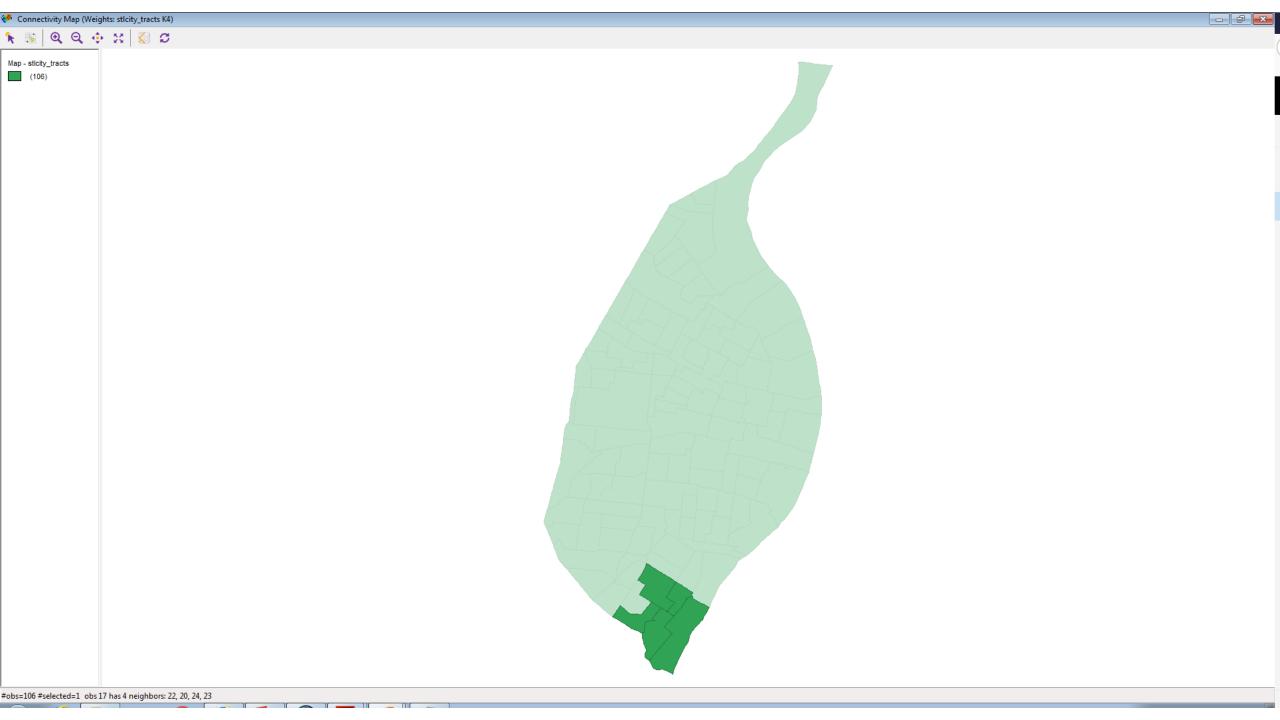
Polygon ID 1 – has 15 neighbors

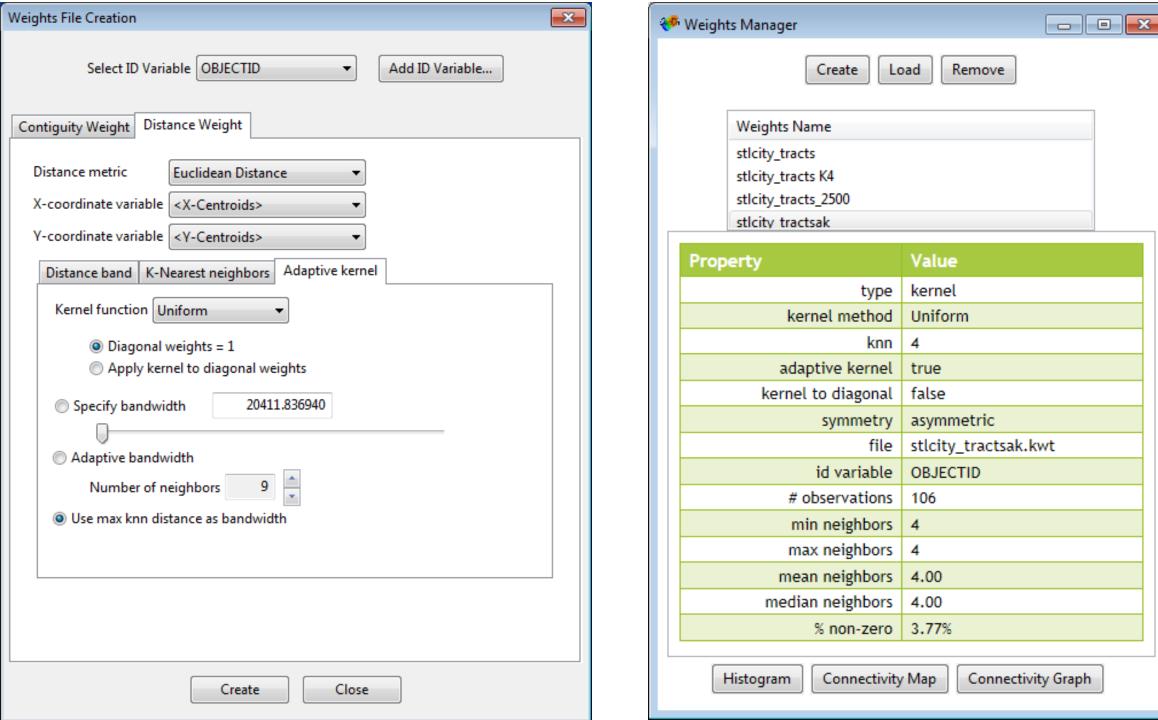


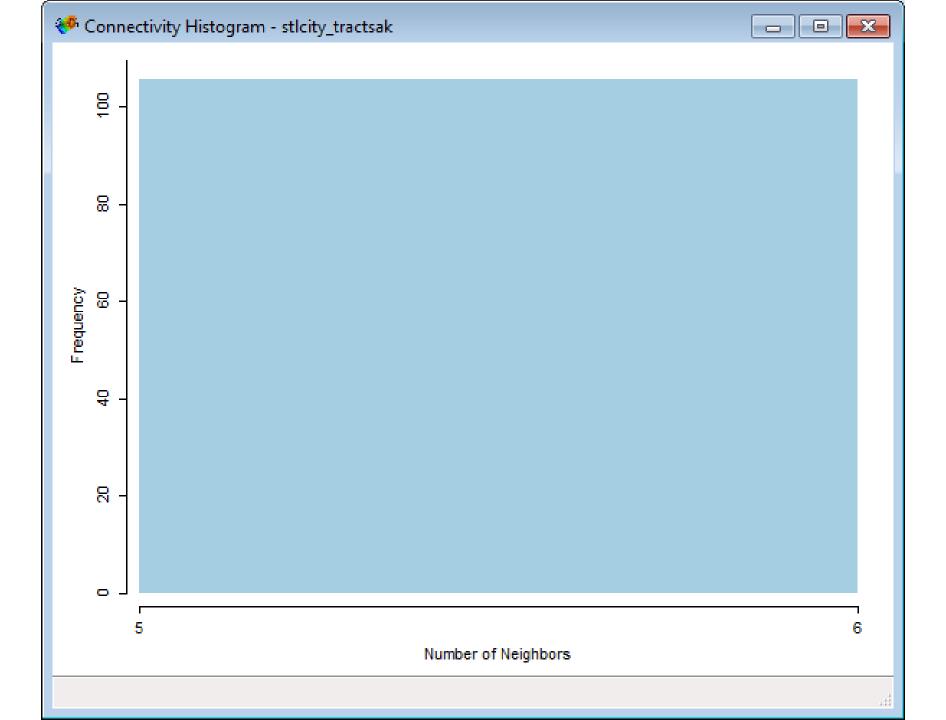


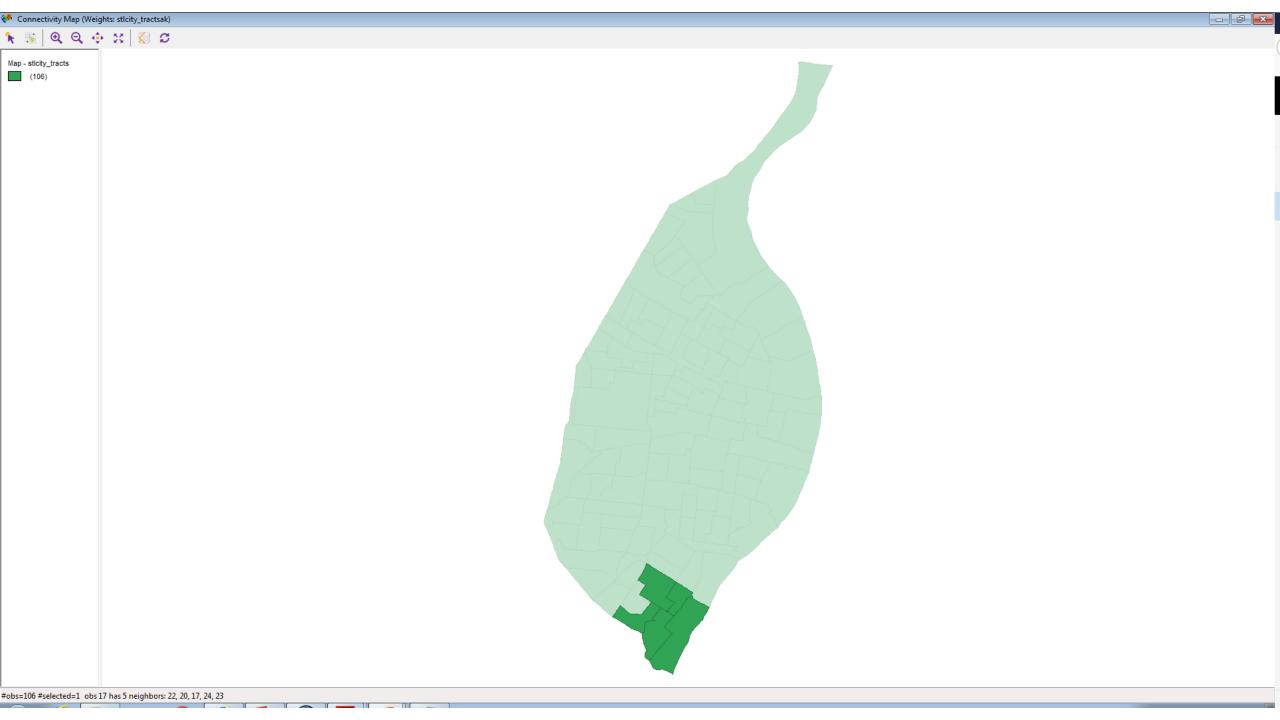






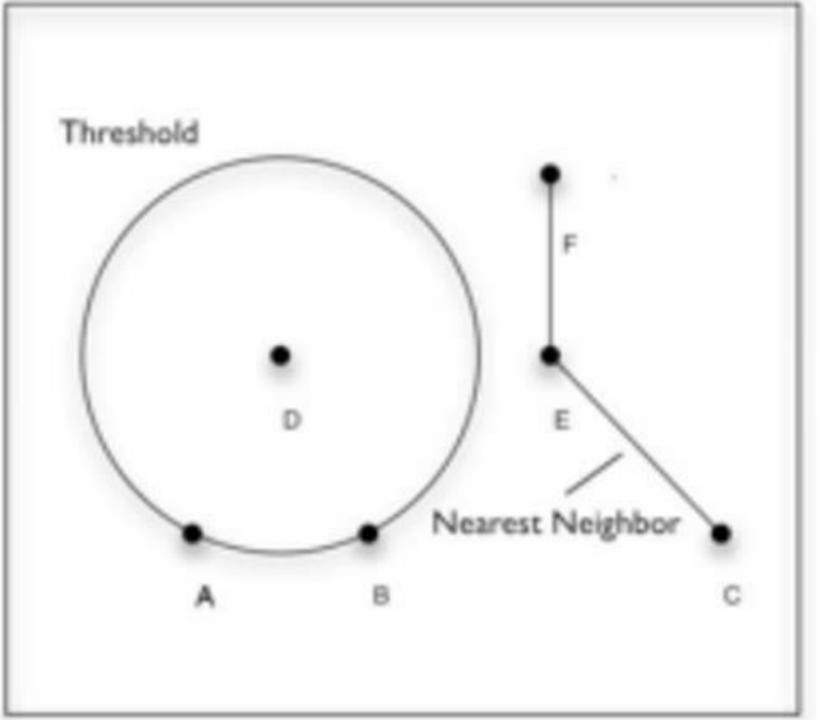






Important Note

- KNN is asymmetric (e.g., point A is B's nearest neighbor but point B does not have to be point A's nearest neighbor).
- Because of this asymmetry, it is difficult to correctly estimate spatial lag or error models with KNN weights in GeoDa. You have to compute this function in GeoSpace.



Let's Focus on D A and B are in radius

Let's Focus on E F is NN of E

E is the NN of C Therefore C is not the NN of E

This is a problem - Asymmetrical

Distance Band Weight (e.g., 14.1 Distance Band)

Symmetric

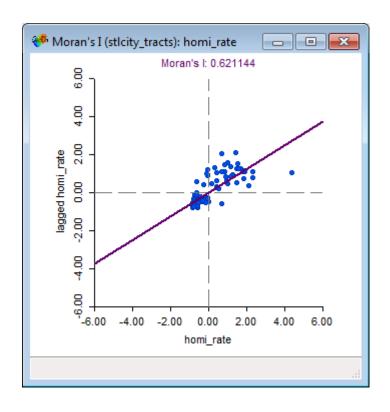
	A	В	C	D	E	F
A	0	10	30	11.2	22.4	28.3
В	10	0	20	11.2	14.1	22.4
C	30	20	0	26.9	14.1	22.4
D	11.2	11.2	26.9	О	15.0	18.0
E	22.4	14.1	14.1	15.0	0	10.0
F	28.3	22.4	22.4	18.0	10.0	0

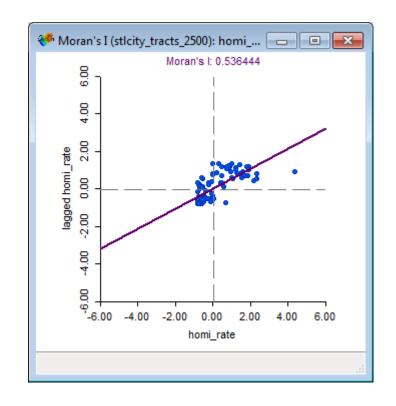
	A	В	С	D	E	F
A	0	1	O	1	О	О
В	1	O	O	1	1	O
C	O	O	O	O	1	O
D	1	1	O	O	O	O
E	O	1	1	O	O	1
F	O	O	O	O	1	O

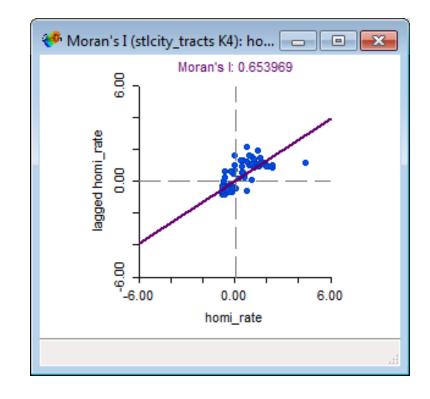
K – Nearest Neighborhood (e.g., k=3)

Asymmetric

	A	В	C	D	E	F		A	B		שן	E	ľ
A	O	10	30	11.2	22.4	28.3	A	0	1	0	1	1*	O
В	10	О	20	11.2	14.1	22.4	В	1	O	O	1	1	O
C	30	20	O	26.9	14.1	22.4	C	O	1	О	0	1	1
D	11.2	11.2	26.9	О	15.0	18.0	D	1	1	О	0	1	O
E	22.4	14.1	14.1	15.0	О	10.0	E	O	1	1	0	О	1
F	28.3	22.4	22.4	18.0	10.0	0	F	0	1	1	0	1	O







Queen Contiguity

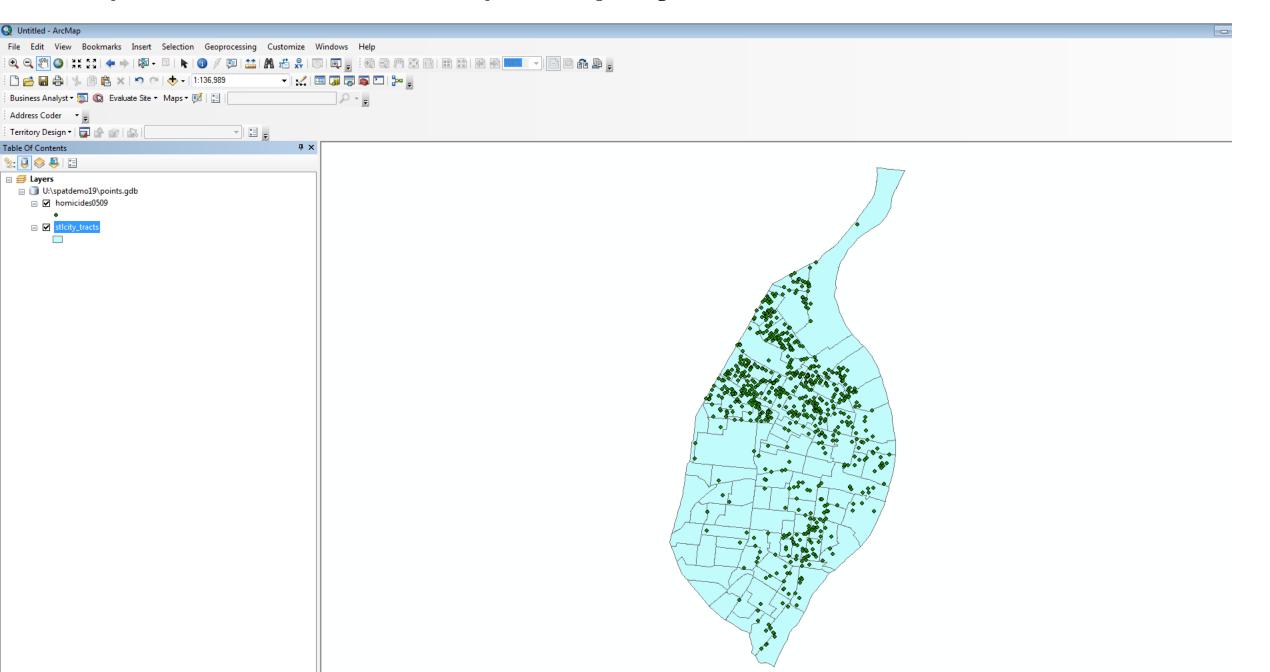
Distance

KNN

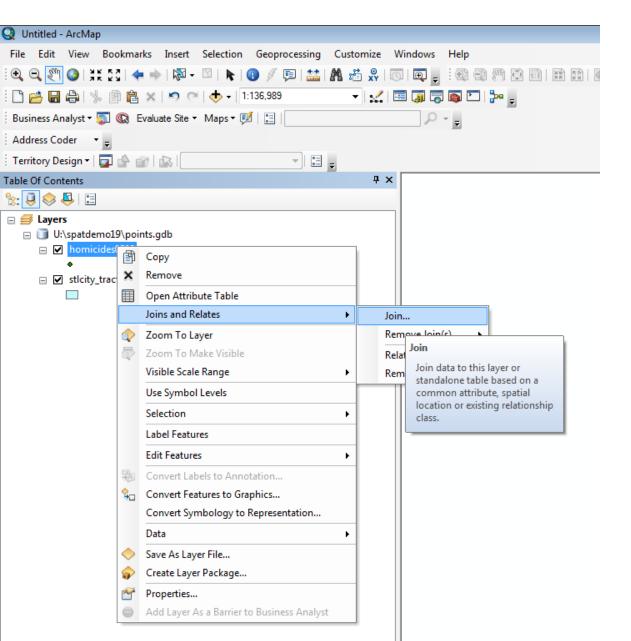
Example

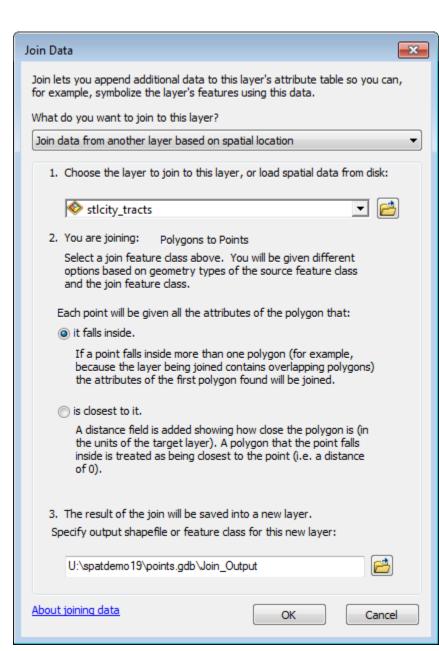
Create Crime Rate using Spatial Join

1. Load your crime data and tract data for city from the point geodatabase



- 2. Select Join Data and make sure you selected the point shapefile
- 3. Make sure you select "Joint data from another layer based on spatial location

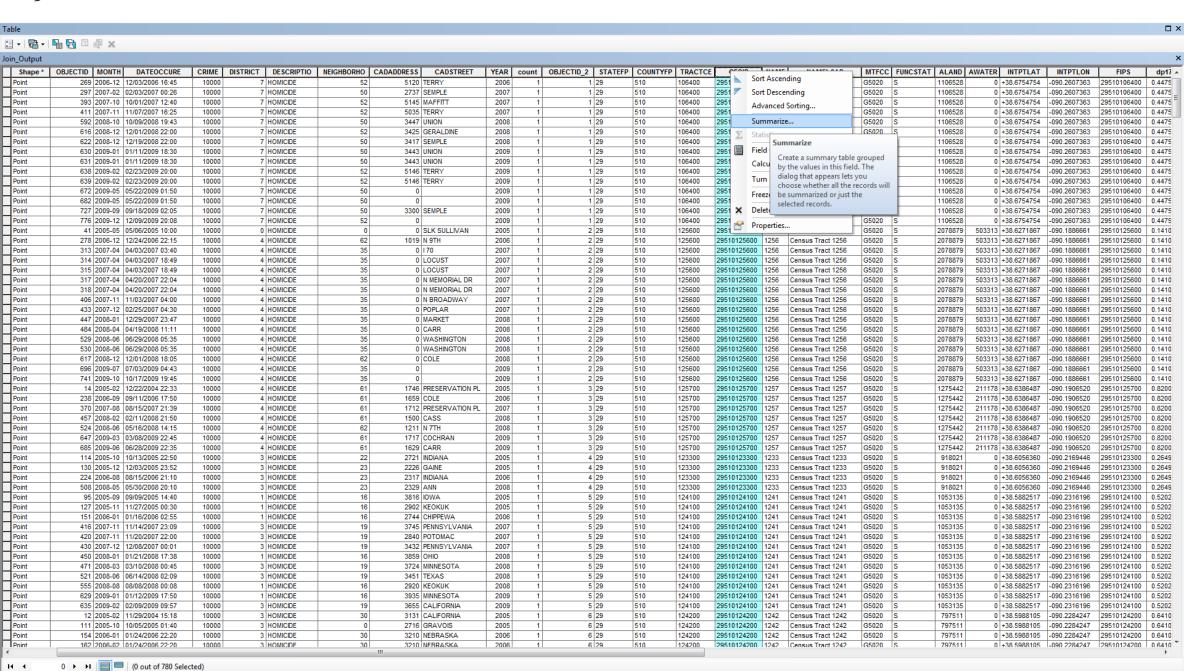




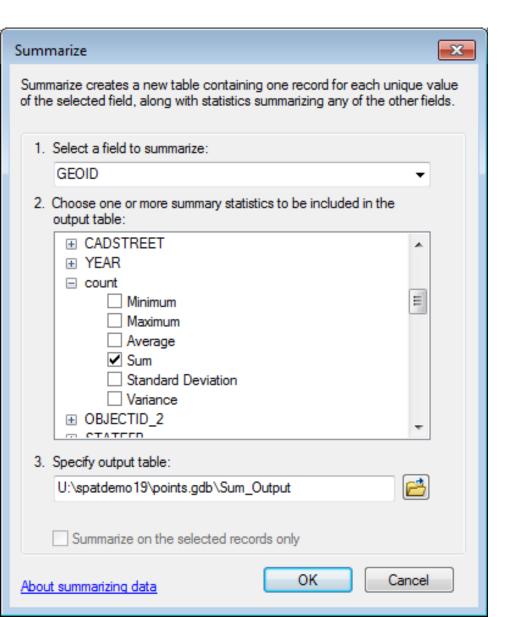
4. Each point has the attribute of the census tract

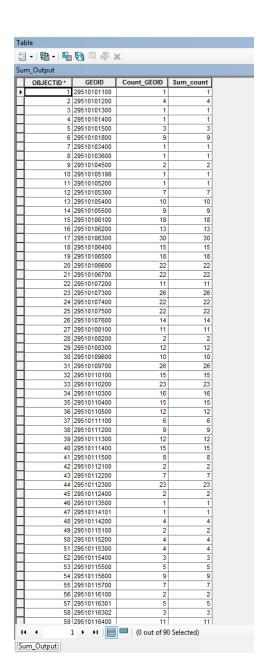
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	-	510 125		2951012570		Census Tract 1257		S 1275442		38.6386487	-090.1906520	29510125700	0.820058			0.368295		13 3772	_	_		0.003427 0.994464	1 29510125700		0.826652 C
		510 125		2951012570		Census Tract 1257		S 1275442		38.6386487	-090.1906520	29510125700	0.820058		0.220729			13 3772		-		0.003427 0.994464	1 29510125700	0.498373	0.826652 C
		510 125 510 125		2951012570		Census Tract 1257 Census Tract 1257		S 1275442 S 1275442		38.6386487 38.6386487	-090.1906520 -090.1906520	29510125700 29510125700	0.820058			0.368295 0.368295		13 3772 13 3772		_		0.003427 0.994464 0.003427 0.994464	1 29510125700 1 29510125700	0.498373	0.826652 C 0.826652 C
		510 125		2951012570		Census Tract 1257		S 1275442		38.6386487	-090.1906520	29510125700				0.368295		13 3772		_		0.003427 0.994464	1 29510125700		0.826652 C
	3 29	510 125	700	2951012570	0 1257	Census Tract 1257	G5020	S 1275442	211178 +	38.6386487	-090.1906520	29510125700	0.820058	0.599328	0.220729	0.368295	0.02739	13 3772	0	8	3793	0.003427 0.994464	1 29510125700	0.498373	0.826652 (
		510 123		2951012330		Census Tract 1233		S 918021		38.6056360	-090.2169446	29510123300	0.264998			0.367483		1912 889				0.652337 0.303309	1 29510123300	0.411635	1.715804 (
	. 20	510 1233 510 1233		2951012330 2951012330		Census Tract 1233 Census Tract 1233		S 918021 S 918021		38.6056360 38.6056360	-090.2169446 -090.2169446	29510123300 29510123300	0.264998		0.071213	0.367483 0.367483	0.58376 0.58376	1912 889 1912 889				0.652337 0.303309 0.652337 0.303309	1 29510123300	0.411635	1.715804 C 1.715804 C
		510 123		2951012330		Census Tract 1233		S 918021		38.6056360	-090.2169446	29510123300				0.367483		1912 889				0.652337 0.303309	1 29510123300	0.411635	1.715804 C
		510 124		2951012410		Census Tract 1241	G5020	S 1053135		38.5882517	-090.2316196	29510124100				0.270431		1138 3157	_	169		0.227737 0.631779	1 29510124100	0.511292	0.891857 (
		510 124		2951012410		Census Tract 1241		S 1053135		38.5882517	-090.2316196	29510124100				0.270431		1138 3157	533	_		0.227737 0.631779	1 29510124100		0.891857 C
		510 124		2951012410		Census Tract 1241		S 1053135		38.5882517	-090.2316196	29510124100	0.520231				0.707162	1138 3157	533			0.227737 0.631779	1 29510124100		0.891857 (
		510 124 510 124		2951012410	_	Census Tract 1241 Census Tract 1241		S 1053135 S 1053135		38.5882517 38.5882517	-090.2316196 -090.2316196	29510124100 29510124100	0.520231			0.270431		1138 3157 1138 3157	_		4997 4997	0.227737 0.631779 0.227737 0.631779	1 29510124100	0.511292 0.511292	0.891857 C 0.891857 C
		510 124		2951012410		Census Tract 1241		S 1053135		38.5882517	-090.2316196	29510124100	0.520231				0.707162	1138 3157				0.227737 0.631779	1 29510124100	0.511292	0.891857 (
	5 29	510 124		2951012410		Census Tract 1241		S 1053135		38.5882517	-090.2316196	29510124100	0.520231	0.409492	0.110739		0.707162	1138 3157	533			0.227737 0.631779	1 29510124100	0.511292	0.891857 C
		510 124		2951012410		Census Tract 1241		S 1053135		38.5882517	-090.2316196	29510124100				0.270431		1138 3157				0.227737 0.631779	1 29510124100	0.511292	0.891857 C
		510 124 510 124		2951012410		Census Tract 1241		S 1053135		38.5882517	-090.2316196	29510124100				0.270431		1138 3157				0.227737 0.631779	1 29510124100		
		510 124 510 124		2951012410		Census Tract 1241 Census Tract 1241		S 1053135 S 1053135		38.5882517 38.5882517	-090.2316196 -090.2316196	29510124100 29510124100	0.520231			0.270431	0.707162	1138 3157 1138 3157	533 533			0.227737 0.631779 0.227737 0.631779	1 29510124100	0.511292	0.891857 C 0.891857 C
		510 124		2951012410		Census Tract 1241		S 1053135		38.5882517	-090.2316196	29510124100	0.520231	0.409492	0.110739		0.707162	1138 3157			4997	0.227737 0.631779	1 29510124100		0.891857 C
	6 29	510 124	200	2951012420	0 1242	Census Tract 1242	G5020	S 797511	0 +:	38.5988105	-090.2284247	29510124200	0.641095	0.536115		0.195816	0.736704	872 2244		195	3658	0.238382 0.61345	1 29510124200		1.023155 (
		510 124		2951012420		Census Tract 1242		S 797511		38.5988105	-090.2284247	29510124200	0.641095			0.195816		872 2244				0.238382 0.61345	1 29510124200	0.361009	1.023155 (
		510 1243 510 1243				Census Tract 1242 Census Tract 1242	G5020 G5020	S 797511 S 797511		38.5988105	-090.2284247 -090.2284247	29510124200				0.195816		872 2244 872 2244				0.238382 0.61345 0.238382 0.61345	1 29510124200	0.361009	1.023155 C
l zi			- 1111		11/4/		TATE OF THE PARTY	(ratall)	ult.					ar accept to the	u niwan			//44	147	. (83)	. 201. 105 1		. 12.6.10124200	emmis	k investigation

5. Select GEOID and then select Summarize

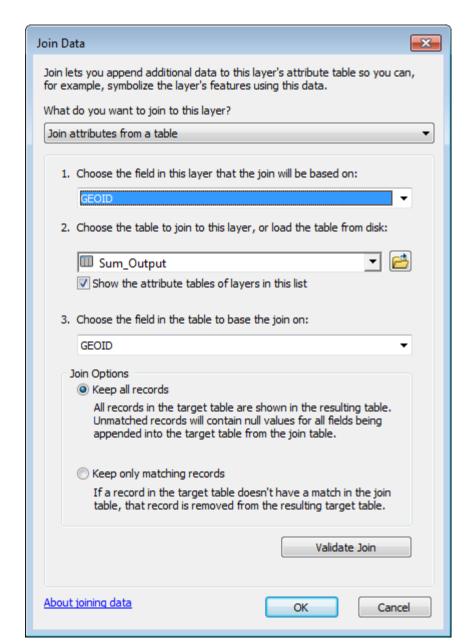


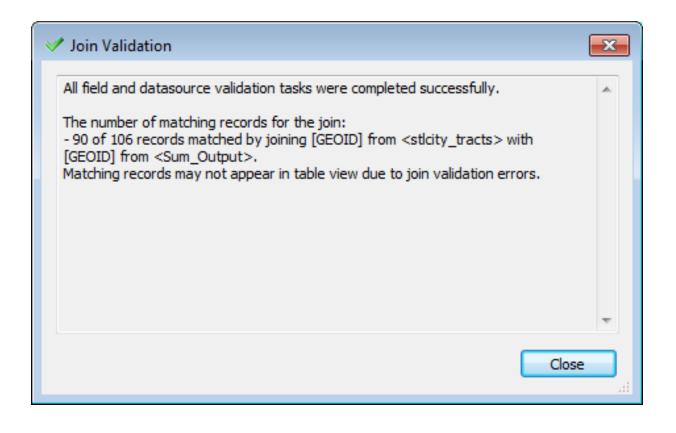
6. Select Count and then click on "Sum" – This will create a database of the number of homicides per census tract



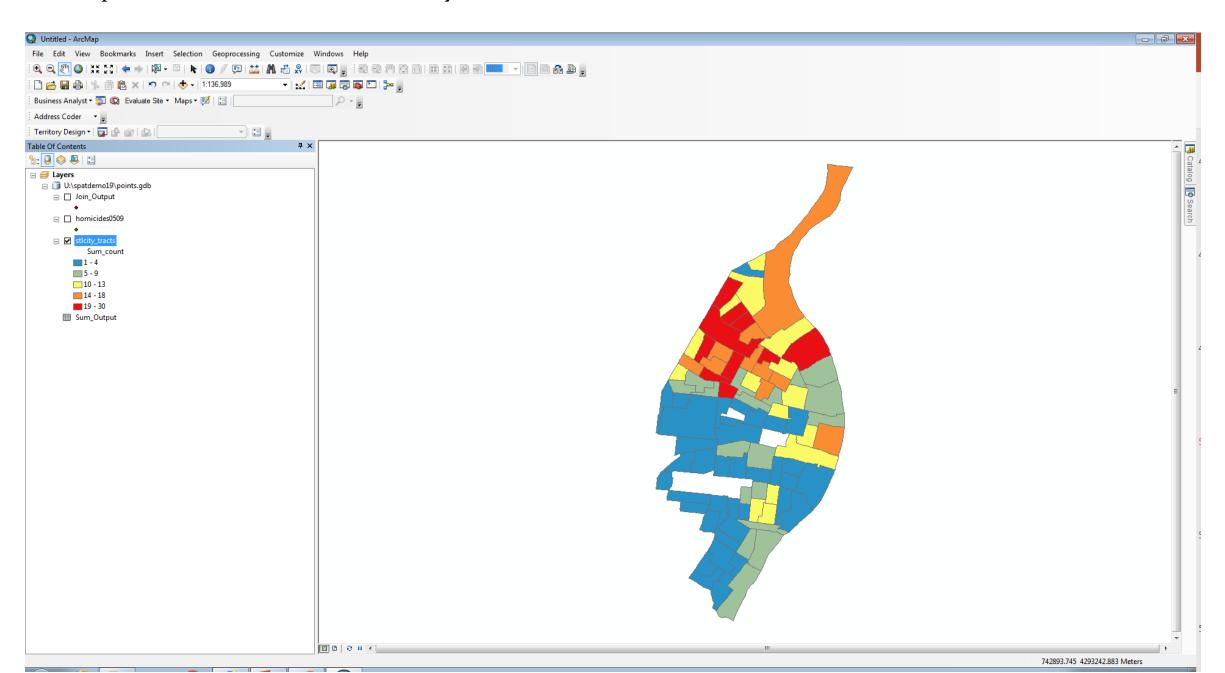


7. Join the Homicide database with the STL –Census Tract shapefile and make it a permanent joint

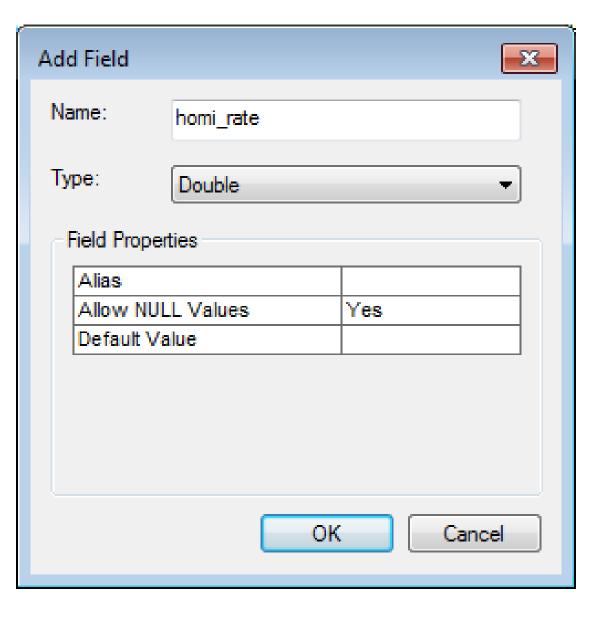


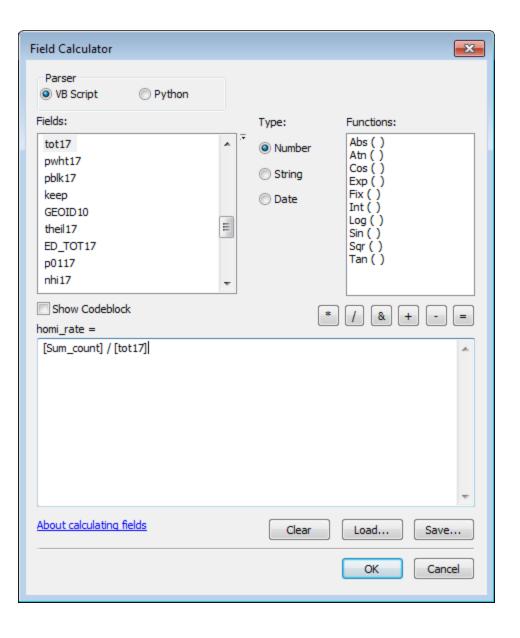


8. Example of the number of homicides by census tracts.



9. Create a homicide rate variable - add field and then use field calculator - Note: check your database you may have some cases where it is <Null>

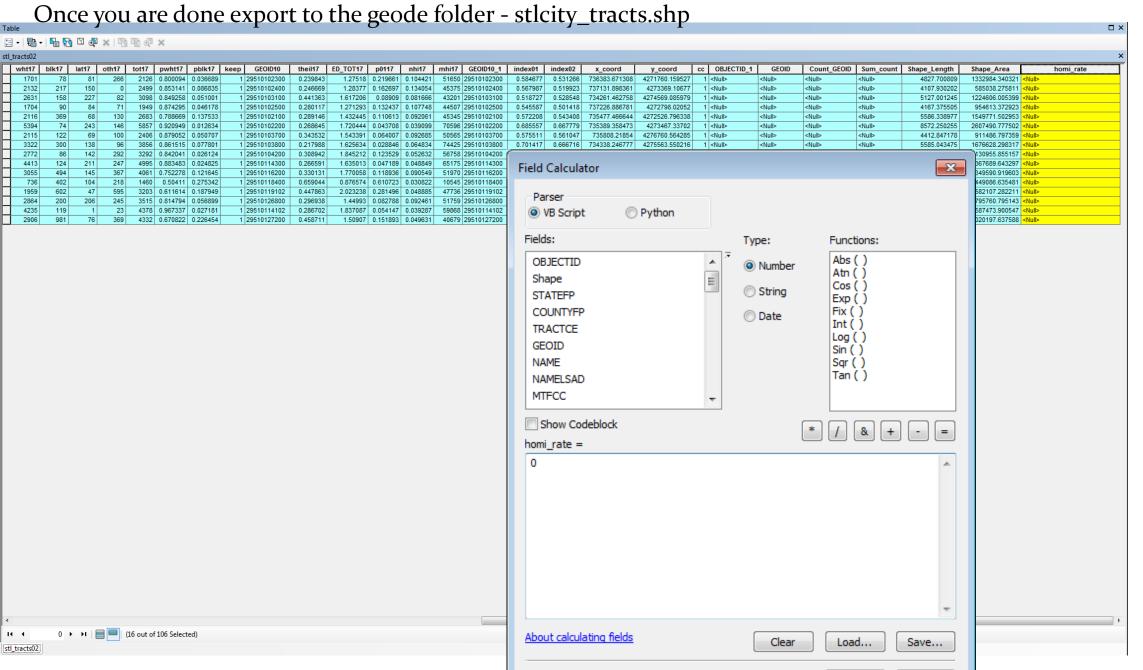




10. Note: check your database you may have some cases where it is <Null>. Convert those values to zero

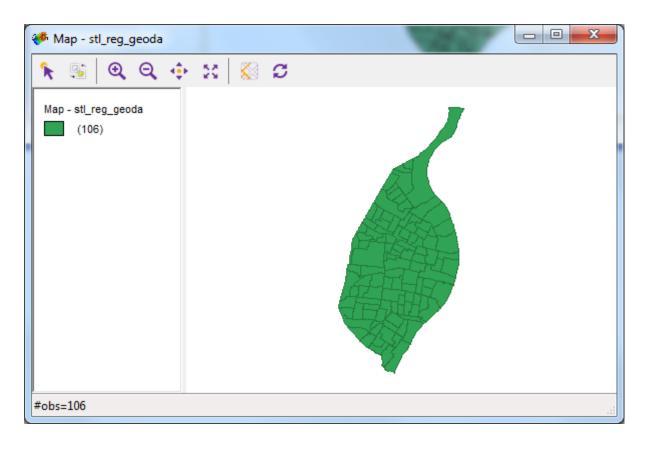
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racts02		_																				
	lat17 oth	17 tot1	nwht17	pblk17	keen	GEOID10	theil17	ED TOT17	p0117 nhi	17 mhi	17 GEOID10 1	index01	index02	x_coord	y_coord	cc OBJECTID_	1 GEOID	Count GEOID	Sum count	Shape_Length	Shape Area	homi rate
78		266 21				29510102300	0.239843	1.27518			650 29510102300	0.584677	0.531266	736383.671308	4271760.159527	1 <null></null>	<null></null>	<null></null>	<null></null>	4827.700809	1332984.340321 <null></null>	nonn_rate
217	150		9 0.85314	0.086835		29510102400	0.246669		.162697 0.134		375 29510102400	0.567987	0.519923	737131.898361	4273369.10677	1 <null></null>	<null></null>	<null></null>	<null></null>	4107.930202	585038.275811 <null></null>	
158	227	82 30	0.84925	0.051001	1 1 2	29510103100	0.441363	1.617206	0.08909 0.081	666 43	201 29510103100	0.518727	0.528548	734261.462758	4274569.085979	1 <null></null>	<null></null>	<null></null>	<null></null>	5127.001245	1224606.005399 <null></null>	
90	84	71 19	9 0.87429	0.046178	8 1 2	29510102500	0.280117	1.271293 0	.132437 0.107	748 44	507 29510102500	0.545587	0.501418	737226.886781	4272798.02052	1 <null></null>	<null></null>	<null></null>	<null></null>	4167.375505	954613.372923 <null></null>	
369	68	130 26	33 0.788669	0.137533	3 1 2	29510102100	0.289146	1.432445 0	.110613 0.092	2061 45	345 29510102100	0.572208	0.543408	735477.466644	4272526.796338	1 <null></null>	<null></null>	<null></null>	<null></null>	5586.338977	1549771.502953 <null></null>	
74	243	_	0.920949			29510102200	0.268645		.043708 0.039		596 29510102200	0.685557	0.667779	735389.358473	4273467.33702	1 <null></null>	<null></null>	<null></null>	<null></null>	8572.250255	2607490.777502 <null></null>	
122	69		0.879052			29510103700	0.343532		.064007 0.092		565 29510103700	0.575511	0.561047	735808.21854	4276760.564285	1 <null></null>	<null></null>	<null></null>	<null></null>	4412.847178	911486.797359 <null></null>	
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86			0.84204			29510104200	0.308942		.123529 0.052		758 29510104200	0.662088	0.667229	735024.50185	4278998.669158	1 <null></null>	<null></null>	<null></null>	<null></null>	4951.506314	1130955.855157 <null></null>	
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494			0.752278	0.121645		29510116200	0.330131		.118936 0.090		970 29510116200	0.627094	0.630712	738820.806105	4276376.847085	1 <null></null>	<null></null>	<null></null>	<null></null>	7242.514351	2349590.919603 <null> 1449086.635481 <null></null></null>	
402 602		218 14 595 32	0.5041			29510118400 29510119102	0.659044		.610723 0.030 .281496 0.048		545 29510118400 736 29510119102	0.600472	0.119347 0.645347	741411.011521 739091.841769	4279220.770478 4280637.05867	1 <null></null>	<null></null>	<null></null>	<null></null>	5291.592355 3821.854522	582107.282211 <null></null>	
200			15 0.81479			29510119102	0.296938		.082788 0.092		759 29510119102	0.586115	0.556228	734514.586924	4277514.581155	1 <null></null>	<null></null>	<null></null>	<null></null>	9385.981033	2795760.795143 <null></null>	
119	1		78 0.96733			29510126600	0.296936		.054147 0.039		868 29510126600	0.566115	0.556226	735372.690219	4274665.674622	1 <null></null>	<null></null>	<null></null>	<null></null>	5183.148221	2795760.795143 <null> 1587473.900547 <null></null></null>	
981	76		32 0.67082			29510114102	0.256702		.151893 0.049		679 29510114102	0.676555	0.486926	736987.476996	4276550.216833	1 <null></null>	<null></null>	<null></null>	<null></null>	6366.500637	2020197.637588 <null></null>	
731	29		29 0.65804			29510123200	0.46222		.142259 0.082		080 29510123200	0.56557	0.582202	742595.394086	4277547.149868		73 29510123200			4416.480643	1114047.786293	0.000
44	31		0.91021			29510103400	0.251956		.047849 0.083		509 29510103400	0.663384	0.632841	734965.828089	4276702.458033	1	7 29510103400		11	3918.135544	909792.352668	0.0005
176	221	_	0.75737			29510101100	0.184065		.122311 0.156		036 29510101100	0.600016	0.523443	737488.53046	4270908.681295	1	1 29510101100		1	6143.22599	1258502.093032	0.0003
489		113 40				29510101300	0.330073		.039333 0.049		387 29510101300	0.607832	0.59196	738355.647663	4272228.23722	1	3 29510101300		1	6581.446836	1975239.282872	0.0002
896	115	209 27	17 0.55097	0.329775		29510101400	0.330434	1.209096 0	.261318 0.113	611 39	107 29510101400	0.492679	0.453237	739301.476469	4271776.912455	1	4 29510101400	1	1	4461.516745	860519.13647	0.0003
1528	34	355 29	0.35692	0.51258	8 1 2	29510105200	0.393966	1.857766 0	.107155 0.034	552 60	938 29510105200	0.62675	0.642441	735936.350366	4281487.553295	1	11 29510105200	1	1	3908.071761	831471.669612	0.0003
41	4		98 0.912943	0.031587	7 1 2	29510103600	0.370173	1.505933 0	.195686 0.083	975 48	929 29510103600	0.550683	0.537307	736002.989174	4277749.696824	1	8 29510103600	1	1	5478.281664	1373211.988339	0.000
461	141	354 31	0.6935	0.147756	6 1 2	29510105198	0.408099	2.258488 0	.180707 0.027	244 57	222 29510105198	0.685098	0.740967	734987.857579	4281347.192408	1	10 29510105198	1	1	7469.296214	1176494.511445	0.0003
1212		827 41		0.294246		29510119300	0.579736	1.451338 0			056 29510119300	0.338509	0.370716	740380.236858	4280448.96763		68 29510119300			4556.306503	1180499.964657	0.0002
32	74	21 23	0.9468			29510113500	0.353701		.131854 0.069		436 29510113500	0.525326	0.506686	737304.945618	4277855.382854		46 29510113500		1	5412.654497	1798251.288294	0.0004
1829	105		0.590802			29510117200	0.343792		0.14513 0.049		094 29510117200	0.638405	0.636791	739353.942856	4277525.928429		62 29510117200		1	4994.157072	1268265.847714	0.0001
1041		229 28				29510119101	0.600654		0.27964 0.075		417 29510119101	0.446154	0.495947	738845.022317	4280242.536322		66 29510119101		-	3689.609763	506681.55008	0.0003
821			0.683800			29510114101	0.384234	1.462638 0			843 29510114101	0.520284	0.508591	736705.285672	4275115.706024		47 29510114101			4438.670895	950092.453159	0.00
675		127 30	_			29510124300	0.380279		.147852 0.149		500 29510124300	0.592299	0.583117	742042.075358	4275515.993251		77 29510124300		_	5187.84264	1168645.777583	0.000
1147		249 42				29510112100	0.457876		.135265 0.101		118 29510112100	0.622368	0.668554	736555.602807	4280379.252256	1 .	42 29510112100			11897.102971	6941014.275569	0.00
162		_	0.73216			29510104500	0.431062		.139769 0.125		286 29510104500	0.579293	0.595953	736706.849567	4278844.247574	1	9 29510104500			6818.338273	1940836.784673	0.0010
1302 660	22 391	51 20 183 45	19 0.31897 19 0.72693			29510119200 29510115100	0.517423	1.560127 0	.201302 0.08		219 29510119200 432 29510115100	0.482198 0.377382	0.49335	739478.824307 737681.426364	4281110.304673 4274296.845401		67 29510119200 49 29510115100		_	4361.245463 4313.925641	734108.90835 1146017.920623	0.0009
579			38 0.492382			29510115100	0.423917		.214261 0.151		021 29510116100	0.377362	0.45076	739067.686351	4275103.222049		56 29510115100		_	4019.217576	765638.413567	0.0004
1711		_	3 0.45808			29510118600	0.301004		.249925 0.138		952 29510118600	0.481002	0.43076	739319.681381	4279507.107182		55 29510118600			7998.933776	2739600.866464	0.000
445	37		0.665714			29510117100	0.423003	1.737705 0			098 29510117100	0.616302	0.618197	738388.014025	4277567.074629		61 29510117100			4306.915188	1083701.390177	0.001
1664	10		18 0.10114			29510121100	0.329556		.452299 0.120		690 29510121100	0.365841	0.32965	741554.586137	4280068.319171		70 29510121100			4546.186381	1099149.571928	0.0010
2376	5		4 0.01759			29510121100	0.321924		.262857 0.134		313 29510108200	0.423564	0.382889	739968.66333	4289145.532073		28 29510108200		_	4763.270388	817436.73322	0.0008
993	278	472 39				29510112400	0.521397		.158659 0.084		783 29510112400	0.592453	0.65284	738372.319821	4280949.075625		45 29510112400		_	5263.127004	939051.042635	0.0005
1411		277 46				29510117400	0.375356		.120306 0.095		865 29510117400	0.616448	0.619598	740548.661995	4277066.873578		63 29510117400			4622.318744	1146807.10887	0.0004
1754	46	19 22	0.191556	0.779556	6 1 2	29510127500	0.314057	1.310775 0	.191006 0.147	111 29	727 29510127500	0.489102	0.46445	742816.590214	4280242.721137	1	89 29510127500	2		6077.634156	1773091.296774	0.0008
1192	81	79 18	76 0.279318	0.635394	4 1 2	29510124600	0.473224	0.949234 0	.561732 0.159	915 20	329 29510124600	0.294993	0.269458	742650.626437	4274822.582007	1	78 29510124600	3	3	8190.128789	2738443.614411	0.0015
1462	109		33 0.53592			29510101500	0.362739		.350359 0.166		683 29510101500	0.384486	0.336247	738335.191664	4270214.745036	1	5 29510101500		_	6487.786461	1755421.8329	0.0008
727			1 0.515548			29510115400	0.262237		.280732 0.233		250 29510115400	0.461791	0.388228	738654.517741	4273174.98067		52 29510115400			4583.896078	978379.007943	0.0008
1100			14 0.145204			29510116302	0.352839		.271682 0.215		723 29510116302	0.405437	0.357464	739693.234111	4274865.775566		58 29510116302			3247.497998	616765.711355	0.0009
889	71		0.65233			29510123300	0.411635		.122783 0.087		381 29510123300	0.576484	0.58534	742342.975643	4276689.117654	1	74 29510123300		_		918613.418033	0.0013
196			15 0.850776			29510101200	0.268068	1.477315 0			159 29510101200	0.634251	0.596072	737432.825311	4271659.687491	1	2 29510101200			4698.961295	1084166.755706	0.0011
323		355 45				29510114200	0.274003		.137908 0.044		865 29510114200	0.645707	0.629934	736414.395497	4275727.813836		48 29510114200		-	6283.70748	1513655.81358	0.000.0
1408			0.348209			29510115200	0.339036		.376229 0.173		008 29510115200	0.405537	0.354189	738238.879033	4275137.600413		50 29510115200		-	6434.427985	1349470.110038	0.0012
1697		769 51	_			29510115300	0.25208	0.982523 0			806 29510115300	0.500961	0.428484	739103.746095	4273828.890325		51 29510115300		-	5297.424716	1656625.126631	0.0007
2112 641	104 45		0.34392			29510123100	0.357454		.180469 0.078		750 29510123100	0.533201	0.506274	741606.211818 743857.449545	4277293.900147		72 29510123100 90 29510127600		-	4652.833042 8809.059397	1031735.976138	0.0011 0.0013
4177			30 0.727986 29 0.244624			29510127600 29510115500	0.400043 0.415083	1.752521 0	.111604 0.068		094 29510127600 346 29510115500	0.594981	0.60423 0.335105	739916.783672	4276569.418755 4272914.180185		90 29510127600 53 29510115500		-	4827.392892	3759563.965957 1216212.656506	0.0013
439			9 0.244624			29510115500	0.415083		.151407 0.128		279 29510116301	0.366783	0.335105	739916.783672	4272914.180185		57 29510115500			3286.066219	646040.734955	0.0007
1885			0.71170			29510116501	0.299777	1.562422 0			913 29510116500	0.569032	0.558789	740588.469354	4276141.148258		57 29510116301 50 29510116500		-	3776.474916	904478.257254	0.001
1921	7	20 20				29510116300	0.332439		.391166 0.216		315 29510111100	0.374486	0.350894	740388.469334	4281385.251115		37 29510111100			5629.843797	1091538.842539	0.0013
3772	0		33 0 00342			29510111100	0.430130		587925 0 182		200 29510171100	0.374400			4280333 936847		81 29510171700		7	6415 529301	1487620 342645	0.0025
																		III .				
	10		(16 out of	106 Select	ted)																	

11. Select the cases and use field calculator to make the value equal to o.



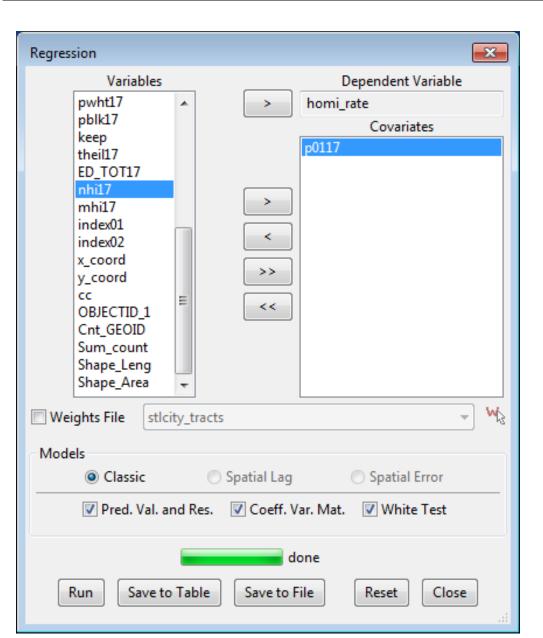
Start with OLS





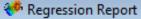
- 1. Open the shapefile
- 2. Create a weight matrix
- 3. Compute your Spatial Autocorrelation Statistic for crime rate and poverty
- 4. If you find you have positive spatial autocorrelation, then some evidence that OLS might not be appropriate.
- 5. To be on the conservative side, we will start with OLS



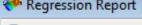


- . To run OLS go to Methods and select Regression.
- 2. Check the box predicted value, coefficient variance matrix and Moran's I Z-value
- 3. Select your dependent variable
- 4. Select your poverty rate.
- 5. Click the Run Button
- 6. Click the View Result Button.

Note: at this point do not click the weights file box.







>>03/20/19 11:33:39

REGRESSION

SUMMARY OF OUTPUT: ORDINARY LEAST SQUARES ESTIMATION

: stlcity tracts

Dependent Variable : homi rate Number of Observations: 106 Mean dependent var : 0.00340081 Number of Variables S.D. dependent var : 0.00407594 Degrees of Freedom

R-squared 0.240954 F-statistic 33.0141 Adjusted R-squared : 0.233655 Prob(F-statistic) :9.18912e-008 Sum squared residual: 0.00133669 Log likelihood 447.486 :1.28528e-005 Akaike info criterion : Sigma-square -890.971 S.E. of regression : 0.00358507 Schwarz criterion -885.644

Sigma-square ML :1.26103e-005

S.E of regression ML: 0.00355109

Variable	Coefficient	Std.Error	t-Statistic	Probability
CONSTANT	-0.000400913	0.000747688	-0.536204	0.59296
p0117	0.0140372	0.00244304	5.74579	0.00000

REGRESSION DIAGNOSTICS

MULTICOLLINEARITY CONDITION NUMBER

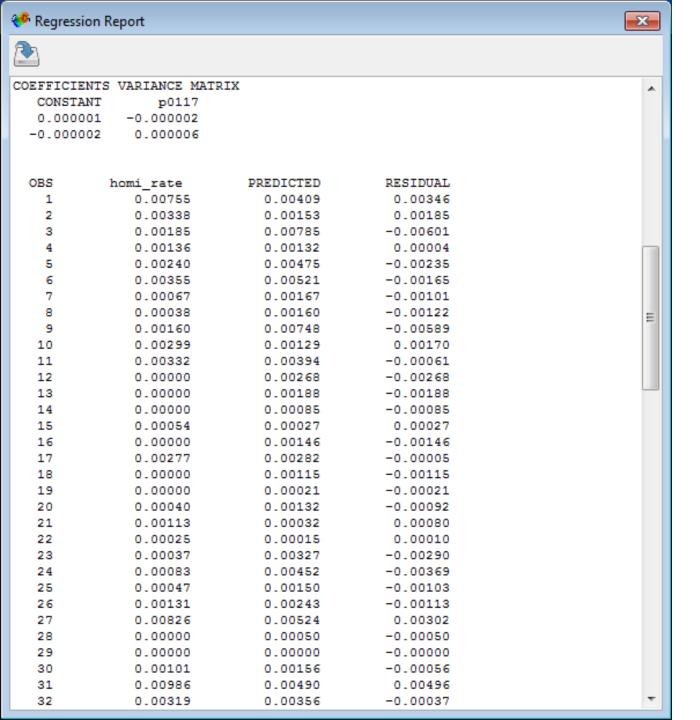
TEST ON NORMALITY OF ERRORS

TEST VALUE PROB Jarque-Bera 224.9842 0.00000

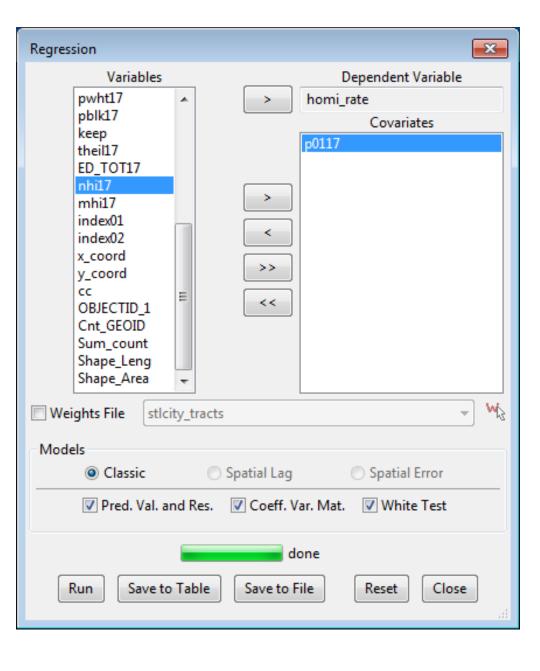
DIAGNOSTICS FOR HETEROSKEDASTICITY

- 1. Review the Output
- 2. Good of Fit Statistics
- Is poverty rate significant?
- 4. What is Multicolliearity? Note: this is not a test statistic. Looks for numbers greater than 20, numbers greater than 30 are problematic.
- 5. What is Heteroskedasticity?

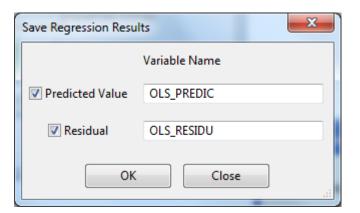
We may have a problem...

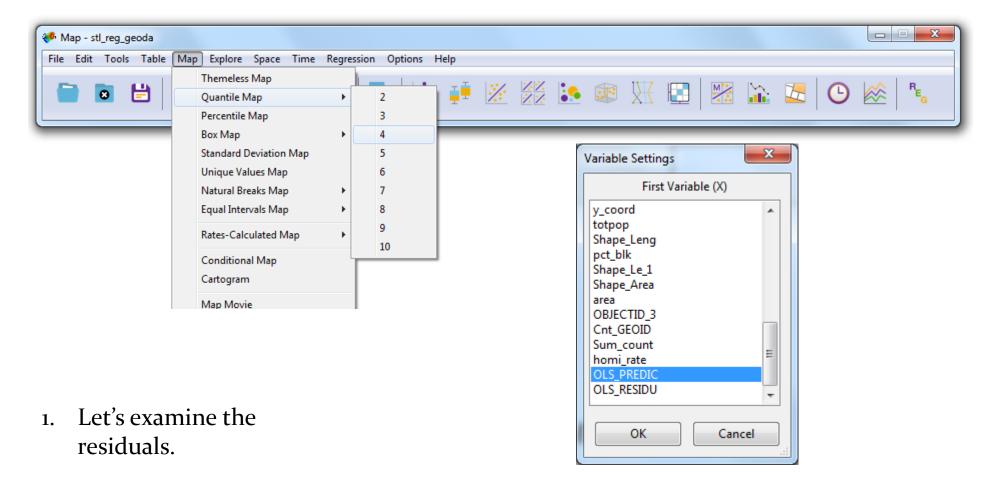


- Review the Coefficient Variance Matrix
- 2. Review the Predicated values and Residuals



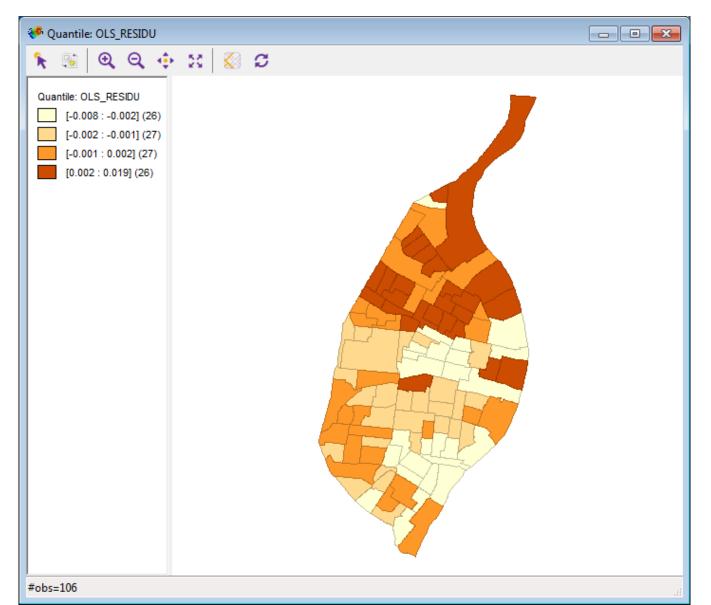
- If you want the predicted values and residuals click the save to table button.
- 2. You will need to add the variables.

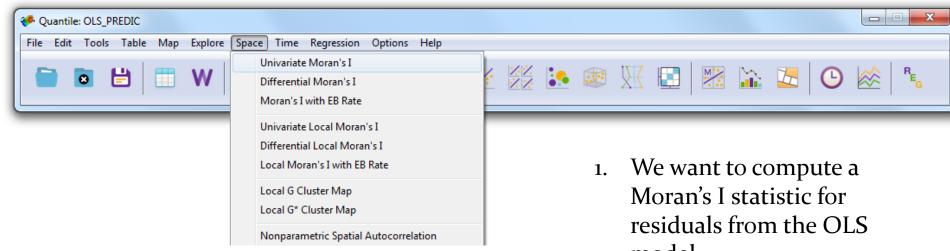


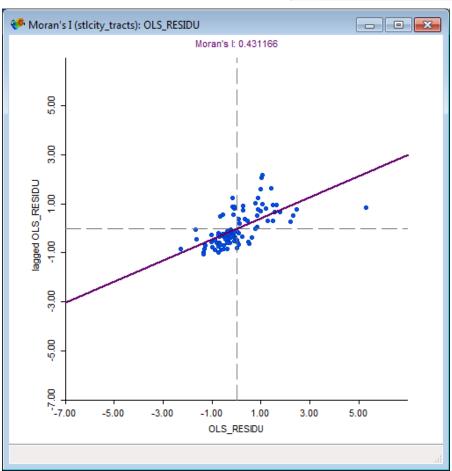


2. Create a Quantile Map

- 1. The map show spatial clustering
- 2. Let's compute a spatial autocorrelation statistics for the residuals



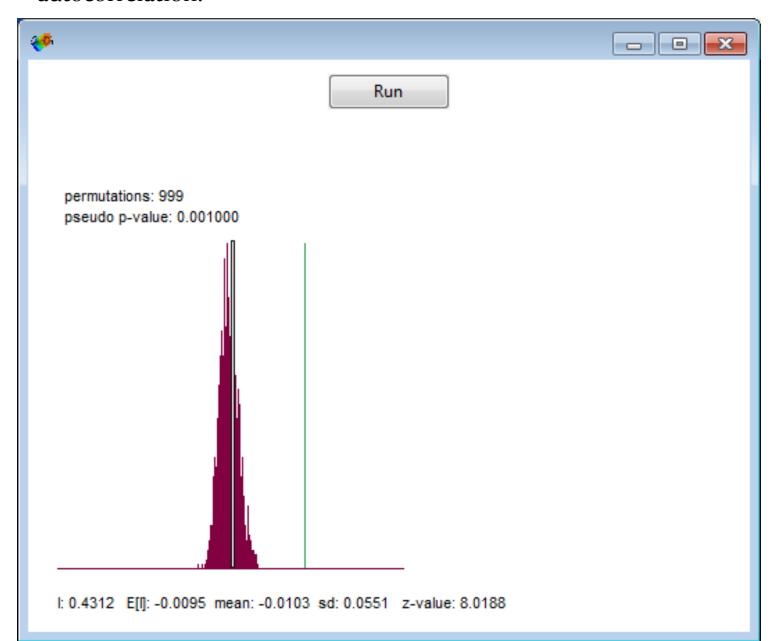




model.

Variable Settings	X
First Variable (X)	
index01 index02 x_coord y_coord cc OBJECTID_1 Cnt_GEOID Sum_count Shape_Leng Shape_Area homi_rate OLS_PREDIC	A
OLS_RESIDU	+
Weights stlcity_tracts	•
OK Cancel	

1. The accumulation of evidence suggest we have a problem of spatial autocorrelation.

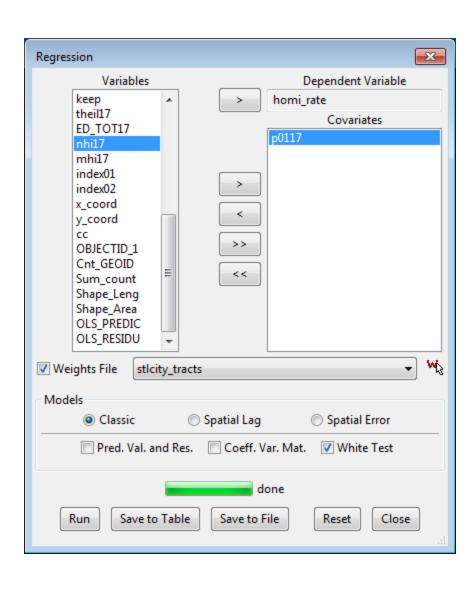


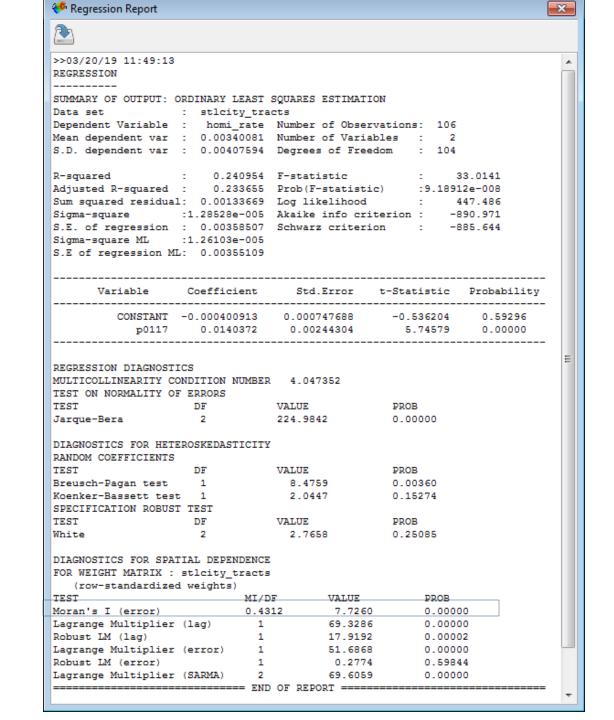
Variable	OLS
Poverty	.0140372 (.00244)***
Constant	-0.0004 (0.0007)
r-square	0.240954
Log likelihood	447.486
AIC	-890.971
Moran's I Residual	.431166***
N *< 05 **< 01 ***< 001	106

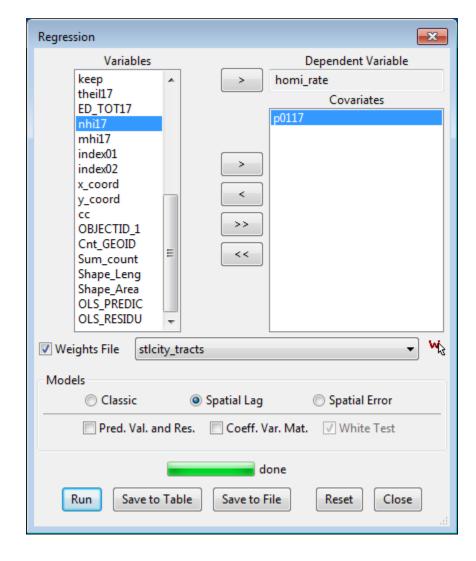
 $^{* \}le .05, ** \le .01, *** \le .001$

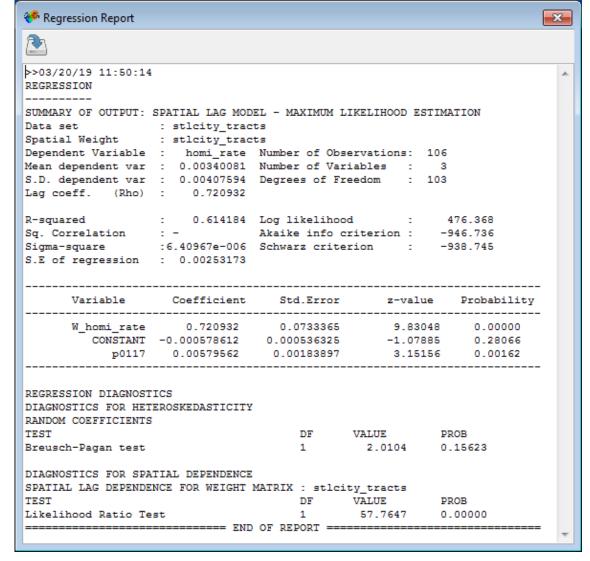
Standard Errors in Parentheses

Move to Spatial Lag

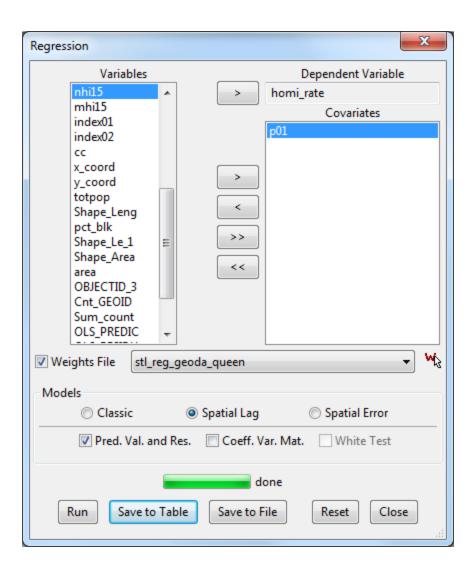




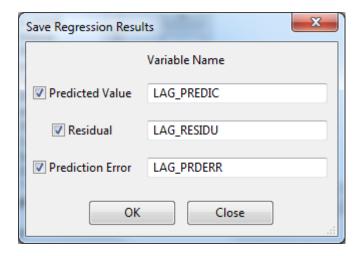


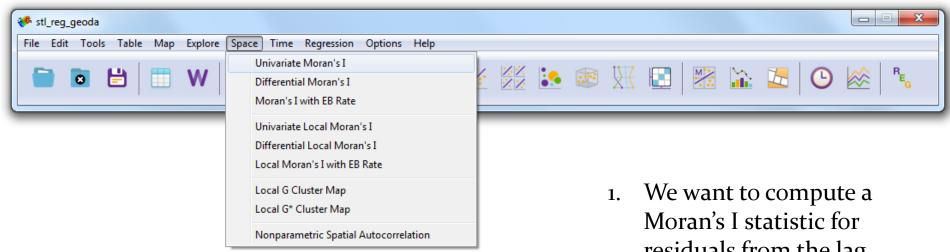


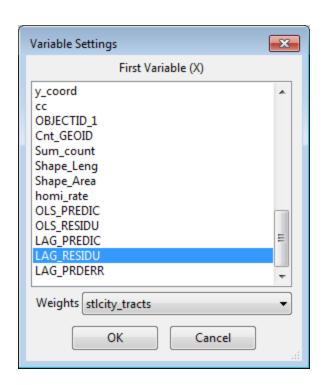
- The Likelihood Ratio Test tell us this model is better than the OLS model.
- 2. Our spatial lag variable W_homi_rat is significant



We want to save the predicted values, residual and prediction error

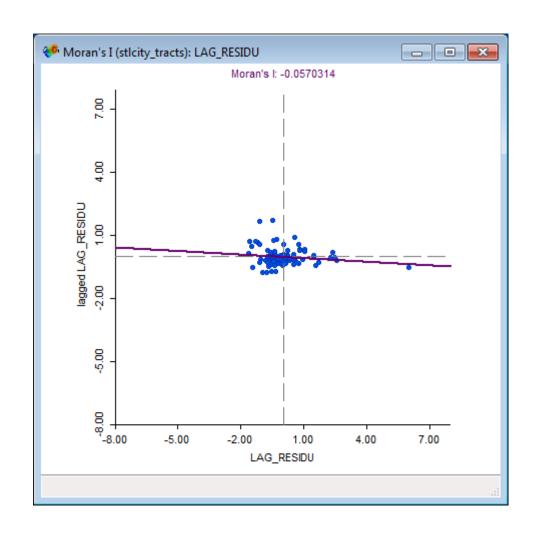


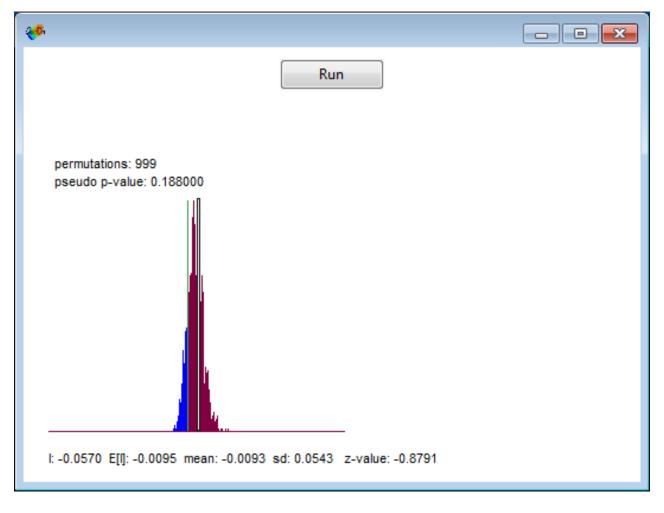




residuals from the lag model.

1. We no longer have a problem with spatial autocorrelation





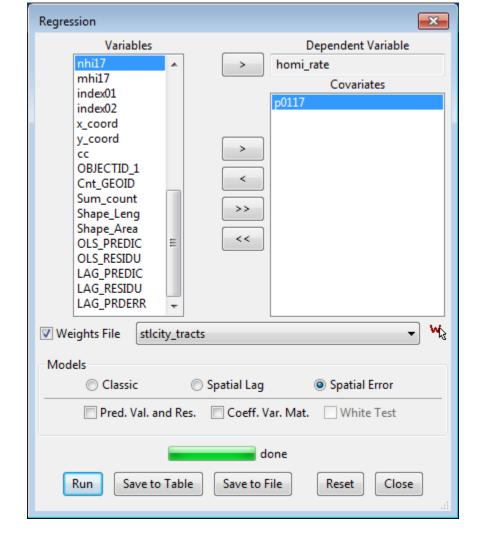
Variable	OLS	SLM
Poverty	.0140372 (.00244)***	0.00579562 (0.00183897) **
Constant	-0.0004 (0.0007)	-0.000578612 0.000536325
ρ		0.720932 (0.0733365) ***
r-square	0.240954	0.614184
Log likelihood	447.486	476.368
AIC	-890.971	-946.736
Moran's I Residual	.431166***	-0.0570314
N	106	106

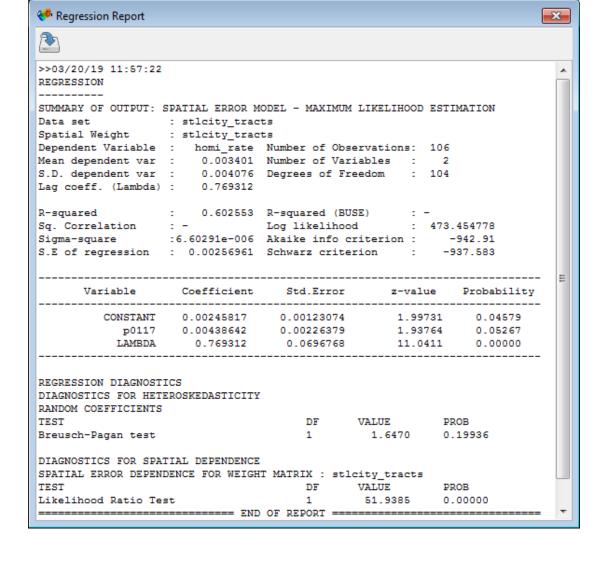
Standard Errors in Parentheses

The $^{\rho}$ coefficient is positive and highly significant, indicating strong spatial autocorrelation in the dependent variable. The Moran's I statistic indicates that the residuals are no longer spatially clustered.

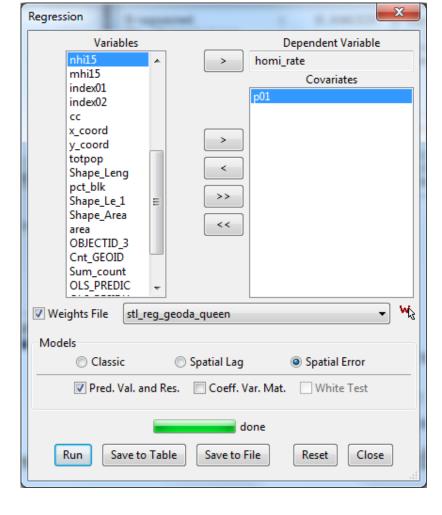
 $^{* \}le .05, ** \le .01, *** \le .001$

Move to Spatial Error

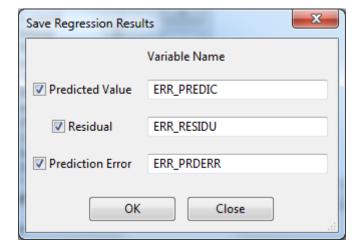


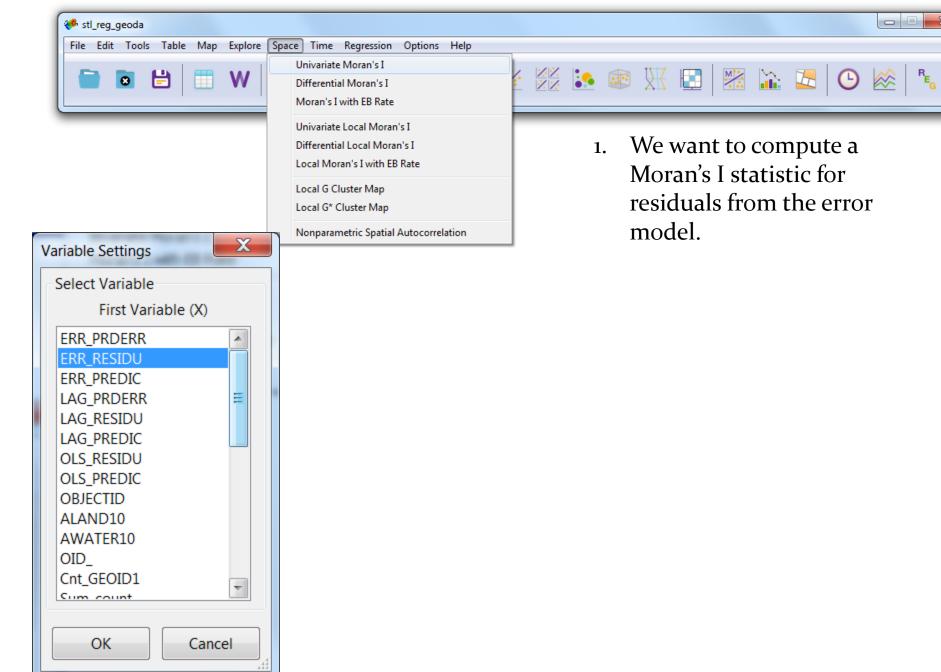


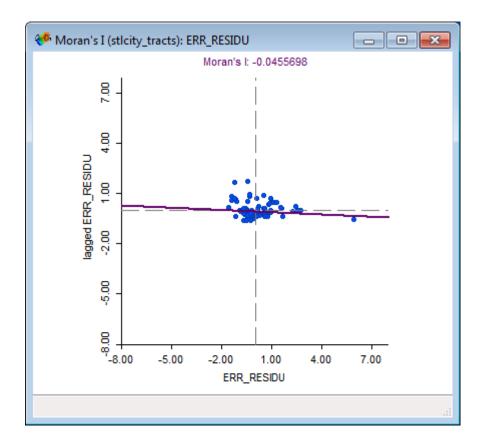
- The Likelihood Ratio Test tell us this model is better than the OLS model.
- 2. Our spatial error variable Lambda is significant



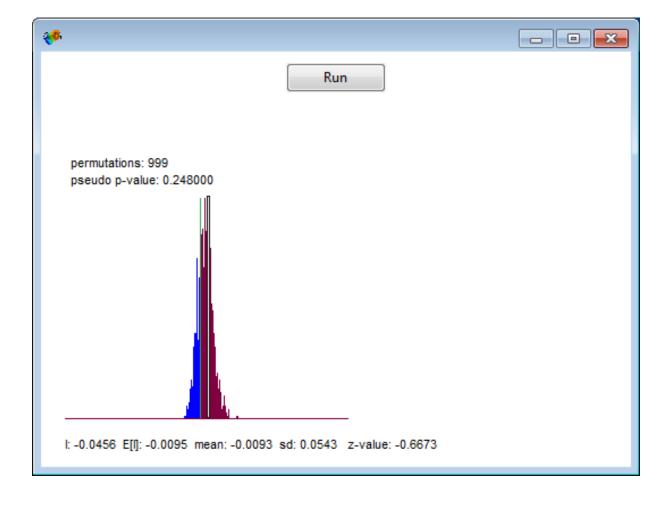
We want to save the predicted values, residual and prediction error







1. We no longer have a problem with spatial autocorrelation



Variable	OLS	SLM	SEM
Poverty	.0140372 (.00244)***	0.00579562 (0.00183897)**	0.00438642 (0.00226379)*
Constant	-0.0004 (0.0007)	-0.000578612 0.000536325	0.00245817 (0.00123074)
ρ		0.720932 (0.0733365) ***	
λ			0.769312 (0.0696768)***
r-square	0.240954	0.614184	0.602553
Log likelihood	447.486	476.368	473.454
AIC	-890.971	-946.736	-942.91
Moran's I Residual	.431166***	-0.0570314	-0.0455698
N	106	106	106

 $^{* \}le .05, ** \le .01, *** \le .001$

Standard Errors in Parentheses

The λ coefficient is positive and highly significant, indicating strong spatial autocorrelation in the dependent variable. The Moran's I statistic indicates that the residuals are no longer spatially clustered.

Final Decision

	OLS	SLM	SEM	Conclusion	Why?
Log likelihood	447.486	476.368	473.454	SLM is better	SLM>SEM> OLS
AIC	-890.971	-946.736	-942.91	SLM is better	SLM <sem< OLS</sem<
Moran's I Residual	.431166***	-0.0570314	-0.0455698	SLM and SEM better	Fail to reject Ho

Log Likelihood - The higher the value the better the fit AIC - The lower the value the better the fit

Spatial Regression by Method

Note: These tables are use the crime rate by 1000 using 2015 ACS data

Queen Weight Matrix

Variable	OLS	SLM	SEM
Poverty	12.2057 (2.16)***	5.11771 (1.66671) **	4.19772 (2.13146)*
Constant	-0.251479 (0.713962)	-0.46838 0.526285	2.20829 (1.13544)
ρ		o.69895 (.0776769) ***	
λ			0.74083 (0.0751734)***
r-square	0.234909	0.591147	0.578692
Log likelihood	-280.986	-254.216	-256.872
AIC	565.973	514.432	517.744
Moran's I Residual	.4414***	-0.0701	-0.605
N	106	106	106

 $^{* \}le .05, ** \le .01, *** \le .001$

Standard Errors in Parentheses

Distance Weight Matrix

Variable	OLS	SLM	SEM
Poverty	12.2057 (2.16)***	4.98793 (1.74544)**	4.43687 (2.13167)*
Constant	-0.251479 (0.713962)	-0.539434 (0.553934)	1.84796 (1.26047)
ρ		0.71194 (0.0852352)***	
λ			0.765561 (0.0798896)***
r-square	0.234909	0.547679	0.542255
Log likelihood	-280.986	-257.915	-259.597582
AIC	565.973	521.83	523.195
Moran's I Residual	.4414***	0.0257	-0.0230
N	106	106	106

Standard Errors in Parentheses

 $^{* \}le .05, ** \le .01, *** \le .001$

K-Nearest Neighbor (n=4)

Variable	OLS	SLM	SEM
Poverty	12.2057 (2.16)***	5.0658213 (1.6571861)**	4.4759007 (2.0709449)*
Constant	-0.251479 (0.713962)	-0.4149546 90.5243832)	1.9617256 (1.1007548)
ρ		0.6809633 (0.0730158)***	
λ			0.7265326 (0.0697611)***
r-square	0.234909	0.5993	0.2349
Log likelihood	-280.986	-254.462	-256.588
AIC	565.973	514.924	517.177
Moran's I Residual	.4414***	Not sig	Not sig
N	106	106	106

Standard Errors in Parentheses

 $^{* \}le .05, ** \le .01, *** \le .001$