

**PREDICTING TRUCK DRIVERS' CRITICAL EVENTS: EFFICIENT
BAYESIAN HIERARCHICAL MODELS**

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Dedication

I dedicate this dissertation to my parents, Zhimin Cai and Guizhen Xu, who believe in the power of higher education, hard work, and always support me.

Acknowledgement

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Chapter 1

INTRODUCTION

1.1 Transportation safety

Traffic safety is a pressing public health issue that involves huge lives losses and financial burden across the world and in the United States (US). As reported by the World Health Organization (WHO [2018b](#)), road injury was the eighth cause of death globally in 2016, killing approximately 1.4 million people, which consisted of about 2.5% of all deaths in the world. If no sustained action is taken, road injuries are predicted to be the seventh leading cause of death across the world by 2030 (WHO [2018a](#)). Compared to the victims who were claimed lives by diseases, people killed in traffic are mostly early- or middle-aged, particularly those aged 4 to 44 years old (Litman [2013](#); Evans [2014](#)). Without traffic accidents, these victims could have much longer lives with normal health.

Apart from fatal deaths, road traffic injuries were also reported to be the cause of 50 million non-fatal life injuries and approximately 75.5 million disability-adjusted life years globally (Staton et al. [2016](#)). In high-income countries, the majority of non-death costs were attributable to non-fatal crashes, with 2% of non-fatal events leading to over 40% of life-time medical costs (Ameratunga, Hajar, and Norton [2006](#)). Besides non-fatal injuries, traffic safety is a major economic burden. The global economic losses attributable to transportation safety were estimated to be 518 billion the United States Dollars (USD), which accounted for 1%

the gross domestic product (GDP) in low-income countries, 1.5% in middle-income countries, and 2% in high-income countries (Peden et al. 2004; Dalal et al. 2013).

Specifically in the United States, transportation contributed to the highest number of fatal occupational injuries, leading to 2,077 deaths and accounting for over 40% of all fatal occupational injuries in 2017 (The United States, Bureau of Labor Statistics 2017). The National Safety Council reported that the number of deaths attributable to car crashes will be at least 40,000 in 2018, which is the third straight year that this number is over 40,000 (The National Safety Council 2018). A comparison study of 26 developed countries revealed that 20 to 60 traffic deaths per billion kilometers were reduced from 2011 (Evans 2014). Even though fatality rates attributable to road traffic in the US were reduced by 40% during that period, the rates declined more rapidly in all other 25 countries. Given the large amounts of investments in roads, improved vehicle protection and traffic policy implementation, and advanced emergency and trauma care, the reduction in traffic associated fatality rates is nominal (Litman 2013). If the change of traffic fatality rates match those in other unremarkable countries, 20,000 traffic deaths could have been prevented each year (Evans 2014).

The impact of road injuries is even more impactful in developing countries than in developed countries (Goonewardene et al. 2010). Although low- and middle-income countries own only 48% of the registered vehicles in the world, 90% of road traffic fatalities and injuries were estimated to occur in these countries, which continue to be escalating due to rapid urbanization and motorization (Dalal et al. 2013; Staton et al. 2016). Ten developing countries, including Brazil, Cambodia, China, Egypt, India, Kenya, Mexico, Russia, Turkey, and Vietnam, account for almost half of all the road traffic in the world (Hyder et al. 2012). For example, China has around 100,000 traffic-related fatalities each year (Zhang et al. 2010), accounting for around 80% of all accidental deaths, with 87% of them were caused by motor vehicles in 2015 (Jiang et al. 2017). In comparison, 148,707 lives were claimed by road collisions in India in 2015, with the road fatality rate similar to the global average level of 17.4

deaths per 100,000 people (National Crime Records Bureau, Government of India [2015](#)).

1.2 Trucking safety

In the US, the large commercial truck industry is the backbone of the economy. Approximately 70% of freight is delivered via a truck at some point of their transportation, which account for 73.1% of value and 71.3% of volume of the domestic goods (Olson et al. [2016](#); Anderson et al. [2017](#)). However, among all vehicles, large trucks are associated with more catastrophic accidents and therefore are the primary concern of traffic safety. In 2016, the Federal Motor Carrier Safety Administration (FMCSA) reported that 27% fatal crashes in work zones involved large trucks (FMCSA [2018](#)). Among all 4,079 crashes involving large trucks or buses in 2016, 4,564 people (1.12 people per crash) were killed in the accidents (FMCSA [2016](#)). Large truck crashes approximately claim 5,000 lives and cause 120,000 injuries each year, but only 15% of these fatalities occur in the trucks, with a predominate 78% occurred in the other vehicles (Neeley and Richardson Jr [2009](#)). Besides, the economic losses associated with large truck crashes are also higher than those with passenger vehicles, with an estimated average cost of 91,000 US dollars per crash (Zaloshnja, Miller, and others [2008](#)).

The high risk of large trucks is attributed to two aspects of reasons (Huang et al. [2013](#)). First, large truck drivers generally need to drive alone for long routes, under on-time demands, challenging weather and traffic conditions. Professional truck drivers usually need to work in shifts, and sometimes unavoidable late-night or early-morning shifts (Pylkkönen et al. [2015](#)). These late-night or early-morning working shifts have been reported to be associated with sleep deprivation and disorders (Åkerstedt [1988](#); Mitler et al. [1997](#); Solomon et al. [2004](#); Sallinen et al. [2005](#)). Besides, commercial truck drivers are exposed to long route, constant concentration, and overtime work, which intertwines with sleep deprivation and disorder, and induce the fatigue symptoms among truck drivers. It is estimated that fatigue among long distance truck drivers caused up to 31% of single vehicle fatal truck crashes (National

Transportation Safety Board [1990](#); Mitler et al. [1997](#)).

On the other hand, trucks have huge weights, large physical dimensions, and potentially carry hazardous cargoes. Although these huge-size trucks boost the transportation efficiency by increasing cargo capacity and reducing fuel costs per trip, they also raise public safety concerns (Lemp, Kockelman, and Unnikrishnan [2011](#)). Large trucks can weight up to 80,000 pounds by federal law, which are twenty times as much as a passenger vehicle (Department of Transportation, Utah [2019](#)). If these trucks travel at the speed of 65 miles per hour on the highway, it will take them 525 feet to stop, which is about two times the length of a football field (Department of Transportation, Utah [2019](#)). The large physical size also creates large blind spots on both sides of the truck, which poses more threat on smaller-sized vehicles. When a crash occurs between a large truck and a smaller vehicle, the sheer size and weight of the truck result in the tragedy that the victims are from the smaller vehicle instead of the trucks in around 80% of the cases (Neeley and Richardson Jr [2009](#)). In even worse case, commercial trucks crashes can cause massive casualties and regional public health emergency when the carried hazardous materials (such as gasoline and sulfuric acid) are leaked.

The importance of truck industry and the potential catastrophic consequences of truck crashes underscore the need to reduce crash risk and improve the safety of truck transportation.

1.3 Crashes and critical events

To reduce the lives and economic losses associated with trucks, numerous studies attempted to screen the risk factors for truck-related traffic crashes and make accurate prediction. Data used in these studies are characterized by rare events (dozens to thousands of times fewer crashes than non-crashes) (Theofilatos et al. [2016](#), [2018](#)). Therefore, the most common study design is a case-control study, matching a crash with one to up to ten non-crashes, and use statistical models such as logistic regressions to explain the causes or predict the crashes (Braver et al. [1997](#); C. Chen and Xie [2014](#); Meulenens et al. [2015](#); Née et al. [2019](#)). However,

a case-control study is limited in estimating the incidence data. It may be contentious in selecting the ratio of controls to cases and how to select these controls (Grimes and Schulz 2005; Sedgwick 2014). Due to the retrospective nature of crash data, it is also unrealistic to trace back to the real-time traffic, weather, and other environmental factors that were associated with the crashes.

Past truck safety literature almost exclusively focused on crashes, while ignoring the precursors to crashes. A precursor to crashes, also known as a critical events, adverse events, or near-miss crashes, is a pattern or signature associated with an increasing chance of truck crash (Saleh et al. 2013; Janakiraman, Matthews, and Oza 2016). Truck critical events deserve more attention since they occur more frequently than crashes, suggest fatigue and a lapse in performance, and they can lead to giant crashes (Dingus et al. 2006).

With the rapid development of modern technology, real-time driving and critical events data are recorded more and more by truck companies (Janakiraman, Matthews, and Oza 2016). Although critical events do not always result in an accident, they could potentially be used as an early warning system to mitigate or prevent truck crashes (Kusano and Gabler 2012; Rome et al. 2018).

1.4 Proposal

I propose using real-time truck ping data provided by the J.B. Hunt, real-time weather and traffic data to

- 1) quantify the association between truck crashes and critical events;
- 2) construct predictive models for truck critical events;
- 3) establish scalable Bayesian hierarchical models for large truck data.

I believe that this work will contribute to statistical theories in constructing scalable Bayesian hierarchical statistical and reliability models using modern Markov chain Monte

Carlo simulations. Realistically, these predictive models will inform policy-makers the functional relationship between driver characteristics, traffic, weather, and other real-time driving environment. These predictive models can be further used to provide data-driven justification to optimize trucking routes and minimize unsafe driving behaviors.

Chapter 2

LITERATURE REVIEW

2.1 Precursors to crashes

2.2 Risk factors

2.2.1 Fatigue

Among all driver-related safety critical events, fatigue has become the most pressing problem of traffic accidents. It is estimated by National Sleep Foundation that approximately 32% of drivers in U.S drive with fatigue over twice a month (National Sleep Foundation [2008](#)). The American Automobile Association Foundation for Traffic Safety claimed that 16.5% of fatal traffic accidents and 12.5% of collisions related to injuries in the US in 2010 were associated with driving with fatigue (American Automobile Association Foundation for Traffic Safety [2010](#)).

(Anderson et al. [2017](#))

Federal Motor Carrier Safety Administration ([2017](#)) demands that property-carrying drivers should not drive more than 14 consecutive hours after coming on duty after 10 hours of rest. This 14-hour restriction cannot be extended by off-duty time.

Drowsy driving is an especially common practice in less-developed countries because

of cost control and tight schedule. Surveys of commercial and public road transportation companies in less-developed countries showed that employers were frequently forcing their employees to drive for longer hours and keep working even when they were exhausted (Zhang et al. 2016; Odero, Khayesi, and Heda 2003; Nantulya and Reich 2002). High proportions of drowsy driving have been found among Brazilian (22%) (Canani et al. 2005), Argentinean (44%) (Pérez-Chada et al. 2005), Pakistani (54%) (Azam et al. 2014), and Thai (75%) (Leechawengwongs et al. 2006) truck or bus drivers. The mechanism of fatigue leading to safety critical events is that a driver's capability to stay alert to ambient traffic and pedestrians will be largely impaired. The reaction time is subsequently prolonged in that situation (Zhang et al. 2014). It is estimated that 17 hours of continuous working lead to a deterioration of driving performance equivalent to a blood alcohol level of 0.05% (MacLean, Davies, and Thiele 2003). What makes the outcomes worse is that fatigue driving is more likely to happen on expressways and major highways where the speed limit is over 55 miles per hour (Knipling and Wang 1994). This is especially concerning because fatigue driving safety critical events are more likely to result in serious injuries and fatalities, compared with non-fatigue driving safety critical events.

Stern et al. (2018) reviewed the research related to fatigue of commercial motor vehicle drivers. Because of the difficulty of running a controlled experiment by imposing treatments, most research designs are observational studies, that is, they compare the effects of variables that are observed, not imposed. One exception to this is a *randomized encouragement design* where drivers are randomized to receive some sort of incentive to apply some treatment, but are not forced to do so. If an effect is observed, we would conclude that it is due to the incentive, not necessarily to the actual treatment. Many studies use a cohort design or a case-control study. In a cohort design, a number of drivers is identified and studied across time. In a case-control study, a number of cases (e.g., crashes, or some other safety measure) are identified and are matched with controls; focus is then placed on the differences between the cases and controls. Both cohort studies and case-control studies can be useful in assessing

safety.

Fatigue measurement

The reason why little has been done about drowsy driving is there is no simple way to objectively measure fatigue driving (Dement [1997](#)).

2.2.2 Driver characteristics

A study by Pack et al. ([1995](#)) revealed that the drivers were 25 years of age or younger in over a half of the 5,000 highway crashes in which they fell asleep whiling driving.

(Duke, Guest, and Boggess [2010](#)) Age-related safety.

Another driver-related risk factor of driving safety critical events is drivers' age. It is reported that younger drivers will experience more crashes than older drivers (Cantor et al. [2010](#)).

On the other hand, older drivers can also experience an increased risk of crash. To meet the huge demand services and supply chain management, it is very common to extend the retirement age or reemploy retired workers in developing countries (Popkin et al. [2008](#)). Aging drivers increase the chance of the safety critical events in three aspects: impaired eyesight, prolonged reaction time to exogenous stimuli, and vulnerability to fatigue (Di Milia et al. [2011](#)). Aged drivers are associated with eyesight diseases or functionality impairment, such as cataracts, narrowed peripheral vision and decreasing visual acuity (Di Milia et al. [2011](#)). In addition, working for truck companies often means irregular shifts and taking the night schedules, which disrupt the circadian time-keeping systems, especially for the aged workers (Moneta et al. [1996](#)).

Aged drivers may find it much more difficult to adjust for the sleep-wake cycle to keep pace with the schedule required by the employer company. Therefore, this disruption of the circadian systems, in turn, increases the chances to feel sleepy or fatigue for workers. It is indicated by research that the “critical age” of shiftwork intolerance is about 45 to 50 years, at which sleep disorder, persisting fatigue and digestive problems become the most obvious

(Di Milia et al. 2011). Young drivers are much better in the sense of physical health and resistance to fatigue compared with aged drivers, however, they are more vulnerable regarding the experience of driving. A study conducted by Clarke suggested that young drivers (17 – 19 years old), especially males, have significantly more accidents than other drivers during the hours of darkness, on rural curves, and rear-end shunts compared with male drivers aged 20 -25 years (Clarke et al. 2006). The reasons for these young driver accidents were not fully explained, but could largely be attributed to inexperience.

One more risk factor that could explain driving safety critical events is drivers' gender. Gender has been suggested to be related with outcomes in medical treatment, education, sports and other fields, and there is no exception for truck drivers' safety. In the first place, women are more likely to suffer from fatigue compared with men. A study found that women in general have 1.4 times higher chance of complaining of fatigue than men (Fjell et al. 2008). However, females are found to have longer sleeping hours than their male counterparts of the same race (Lauderdale et al. 2006). In that study, it was found that the mean sleep hours for white females was 6.7 hours compared with 6.1 hours for white males, and 5.9 hours for black female compared with 5.1 hours for black males even after adjusting for socioeconomic status, lifestyle and sleep apnea (Lauderdale et al. 2006). Gender differences are huge in terms of working conditions. Females had significantly fewer working hours per week, with 47 hours versus 52 hours per week (Rotenberg et al. 2008). In general, women tend to work fewer hours within a week but are more prone to feel fatigue and have a higher risk of traffic incidences.

2.2.3 Traffic

Although it is generally believed that lower **speed limits** can reduce the chances of traffic crashes, studies on speed limits and traffic fatalities showed inconsistent results (Neeley and Richardson Jr 2009; Korkut, Ishak, and Wolshon 2010; Zhu and Srinivasan 2011; Davis et al. 2015).

2.2.4 Weather

(Naik et al. 2016)

Weather has both direct and indirect effects on drivers' safety critical events. On one hand, the increase of ambient temperature places risks on drivers' occupational safety, and possibly leads to cognition loss, heat stroke, and impairment of wakefulness. Evidence showed that the risk of mistakes and safety critical events increase in hot weather (Kjellstrom et al. 2009; Basagaña et al. 2015). Leard and Roth found that for a day with temperature above 80F there is a 9.5% increase in fatality rates compared with a day at 50-60 F (Leard, Roth, and others 2015). A literature review found that 11 out of 13 studies indicated an increase in unintentional injuries associated with high temperatures (Kampe, Kovats, and Hajat 2016). On the other hand, real-time extreme weather conditions such as heavy rain, fog, storm, and snow can either impair the driver's visual capability or reduce the safety of driving on the road (Chang and Chen 2005; Al-Ghamdi 2007; Baker and Reynolds 1992). It is to noted that the cumulative time of driving in such extreme weather conditions could increase the chances of safety critical events. Studies that explore the association between precipitation and driving safety critical events consistently find a negative relationship. The positive linear relationship between precipitation and traffic accidents can be observed in both driver accidents and pedestrian accidents (Al-Ghamdi 2007; Graham and Glaister 2003). Abdel-Aty et al. used detector and sensor data to successfully predict more than 70% of accidents with low visibility conditions (Abdel-Aty et al. 2012). The common problem for the literature exploring the relationship between ambient weather and safety driving critical events is the failure to include the cumulative effect of weather conditions. Instead, they all use an indicator variable to represent whether extreme weather happened during the trip or not, which could lead to potential bias in prediction models.

2.2.5 Time of the day

Pack et al. (1995)'s analysis reported the crashes in which the drivers fell asleep occurred primarily from mid-night to 7 a.m. and from 2 p.m. to 4 p.m.

2.3 Predictive models

2.3.1 Overview

Explain or to predict Shmueli and others (2010); Breiman and others (2001).

The most commonly used statistical models for traffic safety are logistic regression and Poisson regression.

The parameterization of a logistic regression is shown in Model (2.1).

$$Y_i \sim \text{Bernoulli}(p_i)$$

$$\log\left(\frac{p_i}{1-p_i}\right) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \cdots + \beta_k x_k \quad (2.1)$$

Where Y_i is a binary variable that indicates whether an event occurred or not in the i -th observation. p_i is the mean parameter of a Bernoulli distribution, which is constrained on $[0, 1]$. The logit transformation of p_i then has the range from $-\infty$ to $+\infty$, which equals a linear combination of the predictors x_1, x_2, \dots, x_k and associated parameters $\beta_0, \beta_1, \dots, \beta_k$.

Logistic regression is commonly used to predict the crash likelihood (probability)

The parameterization of a Poisson regression is shown in Model (2.2).

$$Y_i^* \sim \text{Poisson}(\mu_i)$$

$$\log \mu_i = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \cdots + \beta_k x_k \quad (2.2)$$

Where Y_i^* is the number of events in the i -th observation, which must be a non-negative integer. μ_i is the mean and variance of the Poisson distribution, and it must be a non-

negative numeric value. The logarithm of μ_i transforms μ_i into the range of $(-\infty, +\infty)$, which equals a linear combination of the predictors x_1, x_2, \dots, x_k and associated parameters $\beta_0, \beta_1, \dots, \beta_k$.

2.3.2 Bayesian models

In contrast to traditional frequentist models that view parameters as unknown but fixed values, Bayesian models view parameters as random variables that have probability distributions (Gelman et al. 2013). Researchers have subjective prior beliefs (a probability distribution) on these parameters $p(\theta)$ before they collect any data. After observing the data \mathbf{X} , the researchers could change their prior beliefs. Therefore, the posterior distribution $p(\theta|\mathbf{X})$ is an unconditional distribution that is a compromise between the prior beliefs and the data. This compromise is given analytically by the Bayes Theorem (Equation (2.3)).

$$\begin{aligned} p(\theta|\mathbf{X}) &= \frac{p(\theta)p(\mathbf{X}|\theta)}{p(\mathbf{X})} \\ &= \frac{p(\theta)p(\mathbf{X}|\theta)}{\int p(\theta)p(\mathbf{X}|\theta)d\theta} \end{aligned} \tag{2.3}$$

Where $p(\mathbf{X}|\theta)$ is the likelihood function, which reflects the data generating process that gives rise to the data observed. The denominator $\int p(\theta)p(\mathbf{X}|\theta)d\theta$ is a normalizing constant that makes the posterior distribution integrates to one. The prior and likelihood function are straightforward since they both have analytical forms. The trickiest part of Bayesian inference is the normalizing constant in the denominator (Gelman et al. 2013).

The normalizing constant need to make the posterior distribution integrate to one since the posterior is supposed to be a probability density distribution. When there are more than two parameters in the model, the normalizing constant often becomes intractable since it involves integration in multiple dimensions. Modern Bayesian inference often uses numerical methods, such as Markov chain Monte Carlo (MCMC) methods or the integrated Laplace approximation, to directly sample from this posterior distribution or approximate

this constant.

Advantages of Bayesian inference

- Sparse data
- Posterior predictive distribution.

2.3.3 Hierarchical models

Most studies on traffic safety assume that the sampling unit is a spatial-temporal segment, which is a specific section of a road with relatively high rate of crashes during a period. However, it is not sufficient to only study the occasions where the crashes are more likely to occur; we must also study the non-crashes and compare them with crashes. On the other hand, these studies that focus on road segments ignore driver-level unobserved effects. It is reported that the chance of having crashes for truck drivers with crash history in the past year is nearly twice as high as those without crash history in the past year (Cantor et al. 2010). Most motor carrier insurance companies and employers also view historical safety events as an important measure of the driver's performance. Therefore, it is more natural to use driver-focused models to account for unobserved variation and characteristics associated with vehicle drivers.

In the Bayesian perspective, a hierarchical model is a statistical model with the probability distribution of one parameter depends on another parameter (Kruschke and Vanpaemel 2015). Suppose we have a model with two parameters α, β and data D . The joint prior distribution of the two parameters is $p(\alpha, \beta)$. According to the Bayes Theorem, the posterior distribution is proportional to the product of the prior distribution and the likelihood function: $P(\alpha, \beta|D) \propto P(\alpha, \beta)P(D|\alpha, \beta)$. In a hierarchical model setting, the product can be factored as a chain of products among parameters, also known as conditional independence, such as $P(\alpha, \beta)P(D|\alpha, \beta) = P(D|\beta)P(\beta|\alpha)P(\alpha)$. In this parameterization, the parameter α is known as the hyperparameter because it gives rise to the parameter β (the parameter of a parameter) (Kruschke and Vanpaemel 2015).

Model (2.4) demonstrates a random-intercept hierarchical logistic regression that predicts the likelihood of safety events. The outcome $Y_{i,d(i)}$ is a binary variable that indicates whether a safety event occurred or not, and it has a Bernoulli distribution with the mean parameter $p_{i,d(i)}$. The logit transformation of $p_{i,d(i)}$ can then be predicted by k variables x_1, x_2, \dots, x_k . The random intercept $\beta_{0,d(i)}$ determines that this is hierarchical model since they vary across different drivers $d(i)$. This model assumes that these random intercepts are sampled from a population of drivers with the mean of μ_0 and standard deviation of σ_0 , which are known as hyperparameters.

$$\begin{aligned}
 Y_{i,d(i)} &\sim \text{Bernoulli}(p_{i,d(i)}) \\
 \log \frac{p_{i,d(i)}}{1 - p_{i,d(i)}} &= \beta_{0,d(i)} + \beta_1 x_{1,i} + \beta_2 x_{2,i} + \dots + \beta_k x_{k,i} \\
 \beta_{0,d(i)} &\sim N(\mu_0, \sigma_0^2), \quad k = 1, 2, \dots, D
 \end{aligned} \tag{2.4}$$

Compared with traditional fixed-effects models that either pool all groups of data or estimate separate models individually for each group, a hierarchical model has the advantage of partial pooling across different groups (McElreath 2018). This partial pooling shrinks group-level parameter estimates towards the group mean and shares information across groups. Therefore, with reasonable assumptions on the data generating process, estimates from a hierarchical model are generally more robust to extreme observations and reasonably accurate for those groups with sparse data (Gelman and Hill 2006; Lambert 2018).

Hierarchical models also come with costs. They are particularly known for its complexity to estimate to coefficients in both frequentist maximum likelihood and Bayesian estimation. The de facto way of current Bayesian estimation is Markov chain Monte Carlo (MCMC). However, in the hierarchical model setting, it is difficult for MCMC to efficiently sample from the posterior distributions of hyperparameters due to the correlation between different levels of parameters, as well as the large number of parameters created by the hierarchy.

2.3.4 Markov chain Monte Carlo (MCMC)

In modern statistics, Bayesian inference almost indispensably relies on Markov chain Monte Carlo (MCMC) sampling to overcome the intractable denominator in the Bayes Theorem (Equation (2.3)). A **Monte Carlo simulation** is a technique to understand a target distribution by generating a large amount of random values from that distribution (Kruschke 2014). A **Markov chain** has the property that the probability distribution of the observation i only depends on the previous observation $i - 1$, not on any one prior to observation $i - 1$, as demonstrated in Equation (2.5).

$$P(X_i = x_i | X_1 = x_1, X_2 = x_2, \dots, X_{i-1} = x_{i-1}) = P(X_i = x_i | X_{i-1} = x_{i-1}) \quad (2.5)$$

Integrating Markov chains and Monte Carlo simulations, the MCMC method can characterize an unknown unconditional distribution without knowing its all mathematical properties by sampling from the distribution (Van Ravenzwaaij, Cassey, and Brown 2018). It has been widely applied in multiple fields such as statistics, physics, chemistry, and computer science (Craiu and Rosenthal 2014). The most notable application of MCMC is probably in Bayesian inference, in which it has been used to draw samples from the posterior distribution and calculate relevant statistics (such as mean, standard deviation, and intervals).

The first proposal of using MCMC dates to the paper by Metropolis et al. (1953), in which they tried to solve an intractable integral with a random walk MCMC. The Metropolis algorithm starts with a randomly defined initial value of the parameter θ . From a pre-defined symmetric proposal probability distribution $p(\theta|\mathbf{x})$, it then draw a proposal parameter value $\theta^{(\text{prop})}$, which only depends on the current parameter value $\theta^{(t)}$. This proposal value will be accepted with the probability of α defined in Equation (2.6).

$$\alpha = \min \left(1, \frac{p(\theta^{(\text{prop})}|\mathbf{x})}{p(\theta^{(t)}|\mathbf{x})} \right) \quad (2.6)$$

This proposal and acceptance with probability steps will be iterated for a pre-define

number of times. When the Metropolis algorithm reaches a steady state, these proposal values are random values drawn from the posterior distribution of parameter θ , which can be used to describe and characterize the posterior distribution.

After decades of successful empirical trials in physics, Hastings (1970) proposed a more generalized form of the Metropolis algorithm, in which the proposal distribution can be arbitrary, but the acceptance probability α^* is modified as shown in Equation (2.7). This Metropolis-Hasting (MH) algorithm is the most classic and widely-known MCMC algorithm used in multiple fields.

Let $p(\theta|\mathbf{X})$ be the posterior distribution we want to know, then the *Metropolis-Hasting algorithm* is:

1. Let $\theta^{(1)}$ denote an initial value for the continuous state Markov chain,
2. Set $t = 1$,
3. Let q be the proposal density which can depend on the current state $\theta^{(t)}$. Simulate one observation $\theta^{(\text{prop})}$ from $q(\theta^{(\text{prop})}|\theta^{(t)})$,
4. Compute the following probability:

$$\alpha^* = \min \left(1, \frac{p(\theta^{(\text{prop})}|\mathbf{x})}{p(\theta^{(t)}|\mathbf{x})} \frac{q(\theta^{(t)}|\theta^{(\text{prop})})}{q(\theta^{(\text{prop})}|\theta^{(t)})} \right) \quad (2.7)$$

5. Set $\theta^{(t+1)} = \theta^{(\text{prop})}$ with the probability of α^* ; otherwise set $\theta^{(t+1)} = \theta^{(t)}$. Set $t \leftarrow t + 1$ and return to 3 until the desired number of iterations is reached.

Although the M-H algorithm is simple and powerful for performing MCMC, its performance highly depends on the choice of the proposal distribution. When there are a few parameters in the model and the proposal distribution is not well-designed, the M-H algorithm will have a very low acceptance rate, which makes the M-H algorithm very inefficient. In view of this issue, Gibbs sampler was proposed with the idea that the proposed values are always accepted and each parameter is updated one at a time by generating samples from the conditional distributions (Geman and Geman 1987; Gelfand and Smith 1990; Lambert

2018). The development of the software *Bayesian inference Using Gibbs Sampler (BUGS)* (Lunn et al. 2000, 2009) was critical in increasing the popularity of applied Bayesian analyses considering its support for a wide variety of statistical distributions, automatic application of the Gibbs Sampler, and numerous textbooks, tutorials and discussion.

Suppose $\theta = [\theta_1, \theta_2, \dots, \theta_k]$ is a k -dimensional parameter. Let \mathbf{X} denote the data. The *Gibbs sampling* algorithm is then:

1. Begin with an estimate $\theta^{(0)} = [\theta_1^{(0)}, \theta_2^{(0)}, \dots, \theta_k^{(0)}]$ in the parameter space,
2. Set $t = 1$,
3. Simulate $\theta_1^{(t)}$ from $p(\theta_1 | \theta_2^{(t-1)}, \theta_3^{(t-1)}, \dots, \theta_k^{(t-1)}, \mathbf{X})$,
4. Simulate $\theta_2^{(t)}$ from $p(\theta_2 | \theta_1^{(t)}, \theta_3^{(t-1)}, \dots, \theta_k^{(t-1)}, \mathbf{X})$,
5. \dots ,
6. Simulate $\theta_k^{(t)}$ from $p(\theta_k | \theta_1^{(t)}, \theta_3^{(t)}, \dots, \theta_{k-1}^{(t)}, \mathbf{X})$,
7. Set $t \leftarrow t + 1$ and repeat steps 3 – 6 for a pre-specified number of iterations and make sure the Gibbs sampler reaches the steady state for a sufficient number of iterations.

The generality of the M-H algorithm and Gibbs sampler and the simplicity in software packages in **R** or **BUGS** help them gain popularity among applied researchers in the recent 30 years. However, as more and more data are available in applied field, the performance of the two most popular MCMC methods has been widely criticized (Betancourt 2019). The performance of the M-H algorithm crucially depends on the proposal distribution. An efficient proposal distribution in M-H algorithm should generate random draws with less auto-correlation, which enables more effective exploration of the parameter space (Quiroz 2015). On the other hand, the performance of the Gibbs Sampler crucially depends on the parameter structure. If there is a significant correlation between parameter estimates, the Gibbs Sampler will become very inefficient as the geometry of the distribution is not aligned with the stepping directions of each sampler (Lambert 2018).

2.4 Scalable Bayesian models

Recent ten years witnessed an explosive growth of data size and dimensionality. This poses a major challenge to Bayesian methods using MCMC. Traditional MCMC algorithm need to evaluate the entire data at each step of iteration, which could be expensive for computation in the case of tall data (Bardenet, Doucet, and Holmes 2017). In applied analysis, researchers often need to set thousands of iterations to reach stable posterior distribution, which takes hours or days to implement a single model. Besides, when the researchers have high dimensional data where high-probability regions are concentrated on a extremely limited region of sample space, it would very hard for random-walk MCMC to generate samples from these small regions (Barp et al. 2018). Hierarchical models even complicate this issue by adding random parameters for each subgroup, which further grows the dimensionality of parameter space. Furthermore, when there is high correlation between different parameters that often occur in the case of many parameters, neither the M-H algorithm or Gibbs sampler can efficiently generate samples from the posterior distribution. All the aforementioned problems motivate researchers in different fields to develop different scalable algorithms to make Bayesian inference for big data.

2.4.1 Hamiltonian Monte Carlo (HMC)

The M-H algorithm and Gibbs sampler can be very inefficient in big data settings because of sparse high-density parameter space, high costs of evaluating the entire data at each step, or a high correlation between parameters. Originally proposed by Duane et al. (1987) with the name of Hybrid Monte Carlo, the Hamiltonian Monte Carlo (HMC) modifies the random-walk behavior in M-H algorithm into a deterministic one by adding auxiliary momentum parameters p_n , thus more efficiently explores the high-density regions in big data settings compared to the traditional M-H algorithm or the Gibbs sampler (Betancourt 2017; Wang, Broccardo, and Song 2019). Although HMC was originally proposed in 1987 (Duane et al.

1987), it is only widely adopted by applied researchers in the recent five years, thanks to the development of the No-U-Turn Sampler (NUTS) (Hoffman and Gelman 2014) and the statistical programming language **Stan** (Carpenter et al. 2017).

Let \mathbf{q} denote the position vector and \mathbf{p} denote the momentum vector in the conservative dynamics physics system. Note that \mathbf{p} and \mathbf{q} must have the same length. The combination (\mathbf{q}, \mathbf{p}) then defines a position-momentum phase space, which can be calculated using the conditional distribution (Neal and others 2011; Betancourt 2017):

$$\pi(\mathbf{p}, \mathbf{q}) = \pi(\mathbf{p}|\mathbf{q})\pi(\mathbf{q})$$

This joint distribution can also be defined in terms of the *Hamiltonian*:

$$\pi(\mathbf{p}, \mathbf{q}) = e^{-H(\mathbf{p}, \mathbf{q})}$$

After a little bit of transformation, we have:

$$\begin{aligned} H(\mathbf{p}, \mathbf{q}) &= -\log \pi(\mathbf{p}, \mathbf{q}) \\ &= -\log \pi(\mathbf{p}|\mathbf{q}) - \log \pi(\mathbf{q}) \\ &= K(\mathbf{p}, \mathbf{q}) + V(\mathbf{q}) \end{aligned} \tag{2.8}$$

In the perspective of physics, the *Hamiltonian* $H(\mathbf{p}, \mathbf{q})$ is the total energy of the system, which composes of two parts: *kinetic energy* $K(\mathbf{p}, \mathbf{q})$ and *potential energy* $V(\mathbf{q})$. Note that the potential energy $V(\mathbf{q}) = -\log \pi(\mathbf{q})$ is essentially the negative log of the posterior distribution of the parameter posterior density \mathbf{q} .

In a static system, the Hamiltonian is a constant. The evolution of this system is governed

by the *Hamiltonian equations*:

$$\begin{aligned}\frac{d\mathbf{q}}{dt} &= \frac{\partial H}{\partial \mathbf{p}} = \frac{\partial K}{\partial \mathbf{p}} \\ \frac{d\mathbf{p}}{dt} &= -\frac{\partial H}{\partial \mathbf{q}} = -\frac{\partial K}{\partial \mathbf{q}} - \frac{\partial V}{\partial \mathbf{q}}\end{aligned}\tag{2.9}$$

It turns out that we can randomly generate high density proposals in the parameters space by taking advantage of the Hamiltonian system. Here is the general idea if the *HMC algorithm* (Lambert 2018):

1. Let $\theta^{(0)}$ denote a random initial value from a proposal distribution,
2. Set $t = 1$,
3. Generate a random initial momentum m from a proposal distribution (typically a multivariate normal distribution),
4. Use the leapfrog algorithm to solve the trajectory moving over the high-density posterior parameter space under the Hamiltonian mechanism for a period,
5. Calculate the new momentum m' and new position $\theta^{(\text{prop})}$
6. Compute the following probability:

$$\alpha^H = \min \left(1, \frac{p(\theta^{(\text{prop})}|\mathbf{x}) p(\theta^{(\text{prop})}) q(m')}{p(\theta^{(t)}|\mathbf{x}) p(\theta^{(t)}) q(m)} \right)\tag{2.10}$$

7. Set $\theta^{(t+1)} = \theta^{(\text{prop})}$ with the probability of α^H ; otherwise set $\theta^{(t+1)} = \theta^{(t)}$. Set $t \leftarrow t + 1$ and return to 3 until the desired number of iterations is reached.

The HMC is essentially an improved form of M-H algorithm by using the Hamiltonian to generate effective proposals instead of naive random-walk and revised form of the acceptance probability (Equation (2.10)).

Two parameters need to be tuned when implementing the HMC: step size ϵ and the optimal trajectory length T . The optimal trajectory length is the product of the number of steps L and step size ϵ (Neal and others 2011; Monnahan, Thorson, and Branch 2017). The

step size ϵ decides how similarly the symplectic methods (typically the leapfrog algorithm) imitates the true unnormalized posterior density. If ϵ is too small, it will take a lot of steps for the leapfrog algorithm to explore the posterior space. If ϵ is too big, the leapfrog algorithm will loop around and return to a place near its original step. The trajectory length $T = \epsilon L$, which need to be tuned in similar style with ϵ : if L is too short, it will be hard to simulate distant proposal and the algorithm is inefficient; if L is too long, the trajectory will loop back and become computationally inefficient. Hand tuning these two parameters was the major obstacle to implement HMC for applied researchers.

The No-U-Turn Sampler (NUTS) proposed by Hoffman and Gelman (2014) solves the difficulty of hand tuning ϵ and T in static HMC. NUTS calculates the optimal step size ϵ and number of steps L through a tree building algorithm (Monnahan, Thorson, and Branch 2017). The tree depth k is defined as the number of doublings, resulting in 2^k leapfrog steps to build the trajectory. This k is then decided by repeating the doubling iterations until the trajectory ‘makes a U-turn’ (loops back) or diverges (the Hamiltonian expands to infinity). Therefore, the NUTS can automatically create trajectories that can efficiently explore the high-density parameter space without having to hand tune ϵ and T .

2.4.2 Integrated Laplace Approximation (INLA)

(Rue, Martino, and Chopin 2009; Lindgren, Rue, and Lindström 2011; Martins et al. 2013; De Coninck et al. 2016; Rue et al. 2017; Verbosio et al. 2017; Kourounis, Fuchs, and Schenk 2018)

2.4.3 Subsampling MCMC

Stochastic Gradient HMC

(Quiroz et al., n.d., 2016; Gunawan et al. 2018; Quiroz, Tran, et al. 2018; Quiroz, Kohn, et al. 2018; Dang et al. 2017; Quiroz 2015)

T. Chen, Fox, and Guestrin (2014)

2.5 Conceptual framework

Cantor et al. (2010) suggested three factors that cause truck crashes: driver factors, vehicle factors (type and condition), and environmental factors.

Roshandel, Zheng, and Washington (2015) proposed five factors that affect traffic safety: (a) behavioral characteristics of the driver, e.g., impairment, fatigue, distractions; (b) vehicle — the condition of the vehicle; (c) traffic — the traffic conditions; (d) geometry — geometric characteristics of the road, e.g. curve, hill, ramps, etc.; and (e) environmental — characteristics of the surrounding environment, such as weather conditions (rain, snow, night-time driving, etc.). Traffic conditions are the most studied of these and we focus on discussing them in this subsection.

2.6 Gaps in literature

- A focus on crashes instead of precursors of crashes
- A focus on road segments rather than drivers
- A focus on case-control comparison given the rareness of truck crashes rather than rates

2.7 Research aims

1. **Aim1:** Explore the association between truck crashes and critical events.
2. **Aim2:** Predict critical events using hierarchical statistical models.
3. **Aim3:** scalable hierarchical Bayesian models using subsampling MCMC.

Chapter 3

METHODS

3.1 Data source

3.1.1 Real-time ping

The J.B. Hunt Transport Services, a trucking and transportation company in the United States, provided real-time ping data on 496 truck drivers who conducted regional work (REG, JBI00) from April 1st, 2015 to March 29th, 2016 to the research team. A small device was installed in each of their truck, which will ping irregularly (typically every 5-30 minutes). Each **ping** will collect real-time data on the vehicle number, date and time, latitude, longitude, driver identity number, and speed at that second. In total, 13,187,289 pings were collected and provided to the research team.

For each of the truck drivers, if the ping data showed that the truck was not moving for more than 20 minutes, the ping data were separated into two different trips. These ping data were then aggregated into different trips. A **trip** is therefore defined as a continuous period of driving without stop. The average length of a trip in this study is 2.31 hours with the standard deviation of 1.8 hours.

After the ping data were aggregated into trips, these trips data were then further divided into different shifts according to an eight-hour rest time for each driver. A **shift** is defined

as a long period of driving with potentially less than 8 hours' stops. The Shift_ID column in Table ?? shows different shifts, separated by an eight-hour threshold. The average length of a shift in this study is 8.42 hours with the standard deviation of 2.45 hours.

3.1.2 Truck crashes and critical events

The company regularly collected real-time GPS location and time-stamped critical events data for all their trucks. Four types of critical events were recorded in the critical events data:

1. Hard brake
2. Headway
3. Rolling stability
4. Collision mitigation

Once some thresholds with regard to the driver's operation were met, the sensor will be triggered and critical events will be recorded in their database. There were 12,458 critical events created by the 496 truck drivers during the study period.

3.1.3 Driver demographics

These variables can be linked to the trips and crashes table via a common unique identifier.

3.1.4 Weather data from the DarkSky API

We retrieved weather variables from the Dark Sky API: *precipitation intensity*, *precipitation probability*, *wind speed*, and *visibility*. The DarkSky API allows the users to query historic minute-by-minute weather data anywhere on the globe (The Dark Sky Company, LLC 2019). According to the official document, the Dark Sky API is supported by a wide range of weather data sources, which are aggregated together to provide the most precise weather data possible

for a given location (The Dark Sky API 2019). Among several different weather data providers we tested, the Dark Sky API provides the most accurate and complete weather variables.

To reduce the cost of querying weather data for the 13 million historic ping data, we rounded the latitudes and longitudes coordinates to two decimal places, which were worth up to 1.1 kilometers. We also rounded the time to the nearest hour and ignore those stopping pings. This scaled the original 13 million ping data down to 4.9 million unique latitude-longitude-date-time combinations. We used the R package **darksky** to obtain weather variables for these reduced 4.9 million unique combinations (Rudis 2018). The weather data for these combinations were then merged back to the origin data. A minimal example of R code to retrieve weather data from the DarkSky API can be found in Appendix 8.

3.1.5 Road geometry data from the OpenStreetMap

We queried two road geometry variables from the OpenStreetMap (OSM) project: *speed limit* and *the number of lanes*. The OSM data are collaboratively collected by over two million registered users via manual survey, GPS devices, aerial photography, and other open-access sources (Wikipedia contributors 2019). The OpenStreetMap Foundation supports a website to make the data freely available to the public under the Open Database License.

We queried the speed limit and the number of lanes by specifying a bounding box by defining a center point, as well as the width and height in meters in the `center_bbox()` function available from the **osmar** R package (Eugster and Schlesinger 2013). We used real-time longitudes and latitudes as the center point and defined a 100×100 meters box to retrieve the two variables. If the 100×100 meters box is too small to have any road geometry data, we expanded the box to 500×500 and then 1000×1000 to obtain geometry data. If the OSM API returned data from multiple geometry structures, we took the mean as the returned values. The R code to retrieve road geometry data can be found in Appendix 8.

3.2 Analytical Plan for Aim 1

This part will be based on truck driver's trips data and crashes data.

3.3 Analytical Plan for Aim 2

In this study, we use vehicle drivers as the sampling unit and adopt hierarchical statistical models that accounts for both driver-level variation and trip-level variation. The workflow is to sample a certain number of drivers from a population of drivers, observe their driving trips or shifts for a specific period, then compare the safety events with non-events, and make conclusions on risk factors associated with these safety events.

3.3.1 Logistic regression

$$\begin{aligned}
 Y_{i,d} &\sim \text{Bernoulli}(p_i) \\
 \log \frac{p_{i,d}}{1 - p_{i,d}} &= \beta_{0,d} + \beta_1 x_1 + \beta_2 x_2 + \cdots + \beta_k x_k \\
 \beta_{0,d} &\sim N(\mu_0, \sigma_0^2), \quad k = 1, 2, \dots, D
 \end{aligned} \tag{3.1}$$

3.3.2 Poisson regression

3.3.3 Non-homogeneous Poisson process

Mean function of a point process:

$$\Lambda(t) = E(N(t))$$

$\Lambda(t)$ is the expected number of failures through time t .

Rate of Occurrence of Failures (ROCOF): When Λ is differentiable, the ROCOF is:

$$\mu(t) = \frac{d}{dt} \Lambda(t)$$

The ROCOF can be interpreted as the instantaneous rate of change in the expected number of failures.

Intensity function: The intensity function of a point process is

$$\lambda(t) = \lim_{\Delta t \rightarrow 0} \frac{P(N(t, t + \Delta t] \geq 1)}{\Delta t}$$

When there is no simultaneous events, ROCOF is the same as intensity function.

Nonhomogeneous Poisson Process (NHPP): The NHPP is a Poisson process whose intensity function is non-constant.

Power law process (PLP): When the intensity function of a NHPP is:

$$\lambda(t) = \frac{\beta}{\theta} \left(\frac{t}{\theta} \right)^{\beta-1}$$

Where $\beta > 0$ and $\theta > 0$, the process is called the power law process (PLP).

Therefore, the mean function $\Lambda(t)$ is the integral of the intensity function:

$$\Lambda(t) = \int_0^t \lambda(t) dt = \int_0^t \frac{\beta}{\theta} \left(\frac{t}{\theta} \right)^{\beta-1} dt = \left(\frac{t}{\theta} \right)^{\beta}$$

There are two forms of truncation in a NHPP:

1. **Failure truncation:** When testing stops after a predetermined number of failures, the data are said to be failure truncated.
2. **Time truncation:** Data are said to be time truncated when testing stops at a predetermined time t .

The first event

The cumulative density function (cdf) of time to the first event is $F(t_1)$: $F_1(t_1) = P(T_1 \leq t_1) = 1 - S(t_1)$.

The survival function for the first event $S_1(t_1)$ is:

$$\begin{aligned}
 S_1(t_1) &= P(T_1 > t_1) \\
 &= P(N(0, t_1) = 0) \quad N \text{ is the number of events} \\
 &= e^{-\int_0^{t_1} \lambda_u du} (e^{-\int_0^{t_1} \lambda_u du})^0 / 0! \\
 &= e^{-\int_0^{t_1} \lambda_u du}
 \end{aligned}$$

The probability density function (pdf) of time to the first event can be calculated by taking the first order derivative of the cdf $F_1(t_1)$:

$$\begin{aligned}
 f_1(t_1) &= \frac{d}{dt_1} F_1(t_1) \\
 &= \frac{d}{dt_1} [1 - S_1(t_1)] \\
 &= -\frac{d}{dt_1} S_1(t_1) \\
 &= -\frac{d}{dt_1} e^{-\int_0^{t_1} \lambda(u) du} \\
 &= -(-\lambda_{t_1}) e^{-\int_0^{t_1} \lambda(u) du} \\
 &= \lambda(t_1) e^{-\int_0^{t_1} \lambda(u) du}
 \end{aligned}$$

If this NHPP is a PLL, we plug in the intensity function $\lambda(t) = (\beta/\theta)(t/\theta)^{\beta-1}$, then we have:

$$f_1(t_1) = \frac{\beta}{\theta} \left(\frac{t_1}{\theta}\right)^{\beta-1} e^{-\left(\frac{t_1}{\theta}\right)^\beta}, \quad t_1 > 0$$

This pdf is identical with the pdf of Weibull distribution, so we have:

$$T_1 \sim \text{Weibull}(\beta, \theta)$$

The second event

The Survival function of the second event given the first event occurred at t_2 is:

$$\begin{aligned}
S_2(t_2|t_1) &= P(T_2 > t_2|T_1 = t_1) \\
&= P(N(t_1, t_2) = 0|T_1 = t_1) \\
&= e^{-\int_{t_1}^{t_2} \lambda_u du} [\int_{t_1}^{t_2} \lambda_u du]^0 / 0! \\
&= e^{-\int_{t_1}^{t_2} \lambda_u du}
\end{aligned}$$

The we can derive the pdf of t_2 conditioned on t_1

$$\begin{aligned}
f(t_2|t_1) &= -\frac{d}{dt_2} S_2(t_2) \\
&= -\frac{d}{dt_2} e^{-\int_{t_1}^{t_2} \lambda(u) du} \\
&= \lambda(t_2) e^{-\int_{t_1}^{t_2} \lambda(u) du} \\
&= \frac{\beta}{\theta} \left(\frac{t_2}{\theta}\right)^{\beta-1} e^{-[(\frac{t_2}{\theta})^\beta - (\frac{t_1}{\theta})^\beta]} \\
&= \frac{\frac{\beta}{\theta} (\frac{t_2}{\theta})^{\beta-1} e^{-(t_2/\theta)^\beta}}{e^{-(t_1/\theta)^\beta}}, \quad t_2 > t_1
\end{aligned} \tag{3.2}$$

In the *failure truncated case*, we know the total number of events n before the experiment starts. We can get the joint likelihood function for $t_1 < t_2 < \dots < t_n$ in the failure truncated case based on Equation 3.2.

$$\begin{aligned}
f(t_1, t_2, \dots, t_n) &= f(t_1) f(t_2|t_1) f(t_3|t_1, t_2) \dots f(t_n|t_1, t_2, \dots, t_{n-1}) \\
&= \lambda(t_1) e^{-\int_0^{t_1} \lambda(u) du} \lambda(t_2) e^{-\int_{t_1}^{t_2} \lambda(u) du} \dots \lambda(t_n) e^{-\int_{t_{n-1}}^{t_n} \lambda(u) du} \\
&= \left(\prod_{i=1}^n \lambda(t_i) \right) e^{-\int_0^{t_n} \lambda(u) du} \\
&= \left(\prod_{i=1}^n \frac{\beta}{\theta} \left(\frac{t_i}{\theta}\right)^{\beta-1} \right) e^{-(t_n/\theta)^\beta}, \quad t_1 < t_2 < \dots < t_n
\end{aligned} \tag{3.3}$$

The log-likelihood function in the failure truncated case is therefore:

$$\log \ell = n \log \beta - n\beta \log \theta + (\beta - 1) \left(\sum_{i=1}^n \log t_i \right) - \left(\frac{t_n}{\theta} \right)^\beta$$

In the *time truncated case*, we assume that the truncated time is τ . The derivation of $f(t_1, t_2, \dots, t_n | n)$ is messy in math, we directly give the conclusion here:

$$f(t_1, t_2, \dots, t_n | n) = n! \prod_{i=1}^n \frac{\lambda(t_i)}{\Lambda(\tau)}$$

Therefore, the joint likelihood function for $f(n, t_1, t_2, \dots, t_n)$ is:

$$\begin{aligned} f(n, t_1, t_2, \dots, t_n) &= f(n) f(t_1, t_2, \dots, t_n | n) \\ &= \frac{e^{-\int_0^\tau \lambda(u) du} [\int_0^\tau \lambda(u) du]^n}{n!} n! \frac{\prod_{i=1}^n \lambda(t_i)}{[\Lambda(\tau)]^n} \\ &= \left(\prod_{i=1}^n \lambda(t_i) \right) e^{-\int_0^\tau \lambda(u) du} \\ &= \left(\prod_{i=1}^n \frac{\beta}{\theta} \left(\frac{t_i}{\theta} \right)^{\beta-1} \right) e^{-(\tau/\theta)^\beta}, \\ n &= 0, 1, 2, \dots, \quad 0 < t_1 < t_2 < \dots < t_n \end{aligned} \tag{3.4}$$

The log likelihood function l is then:

$$\begin{aligned} l &= \log \left(\left(\prod_{i=1}^n \frac{\beta}{\theta} \left(\frac{t_i}{\theta} \right)^{\beta-1} \right) e^{-(\tau/\theta)^\beta} \right) \\ &= \sum_{i=1}^n \log \left(\frac{\beta}{\theta} \left(\frac{t_i}{\theta} \right)^{\beta-1} \right) - \left(\frac{\tau}{\theta} \right)^\beta \\ &= n \log \beta - n\beta \log \theta + (\beta - 1) \left(\sum_{i=1}^n \log t_i \right) - \left(\frac{\tau}{\theta} \right)^\beta \end{aligned} \tag{3.5}$$

3.4 Analytical Plan for Aim 3

Chapter 4

THE PROBABLE CONTENT

This dissertation will be completed according to the three-paper model. The expected chapter headings are as follows:

Chapter 1: Introduction: The problem

A. Epidemiology of head and neck squamous cell carcinoma and its association with second primary malignancies

1. Cancer
2. Head and neck squamous cell carcinoma
3. Definition of second primary malignancies
4. second primary malignancies and Head and neck squamous cell carcinoma

B. Risk factors for second primary malignancies

1. Tobacco use
2. Excessive alcohol use
3. Human papillomavirus infection

C. Existing literature and gaps that exist in the area of second primary malignancies in patients with head and neck squamous cell carcinoma

Chapter 2: Literature review

A. Introduction

B. Methods

1. Source of data and eligibility/exclusion criteria
2. Definitions of primary and secondary outcomes and covariates
3. Statistical analysis

C. Results

1. Description of studies included in the study
2. Primary outcome results
3. Secondary outcome results
4. Publication bias and study quality assessment

D. Discussion/Conclusions

1. Implications
2. Strengths and limitations
3. Future research

Chapter 3: Aim 1 - Truck crashes and critical events

A. Introduction

B. Methods

1. Source of data and eligibility/exclusion criteria
2. Definitions of primary and secondary outcomes and covariates
3. Statistical analysis

C. Results

1. Demographics of study population

CHAPTER 4. THE PROBABLE CONTENT

2. Primary outcome results
3. Secondary outcome results

D. Discussion/Conclusions

1. Implications
2. Strengths and limitations
3. Future research

Chapter 4: Aim 2 - Statistical models predicting truck critical events

A. Introduction

B. Methods

1. Source of data and eligibility/exclusion criteria
2. Definitions of primary and secondary outcomes and covariates
3. Statistical analysis

C. Results

1. Demographics of study population
2. Primary outcome results
3. Secondary outcome results

D. Discussion/Conclusions

1. Implications
2. Strengths and limitations
3. Future research

Chapter 5: Aim 3 - Subsampling Markov Chain Monte Carlo methods

Chapter 6: DISCUSSION

A. Conclusion

B. Strengths and limitation

C. Future research

Chapter 5

TRUCK CRASHES AND CRITICAL EVENTS

Chapter 6

THREE STATISTICAL MODELS PREDICTING TRUCK CRITICAL EVENTS

6.1 Hierarchical logistic model

6.1.1 Model set up

6.1.2 Bayesian estimation based on simulated data

6.2 Hierarchical Poisson model

6.3 Hierarchical power law process

*Mean function of a point process**:

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The ROCOF can be interpreted as the instantaneous rate of change in the expected number of failures.

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$$\lambda(t) = \lim_{\Delta t \rightarrow 0} \frac{P(N(t, t + \Delta t] \geq 1)}{\Delta t}$$

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Where $\beta > 0$ and $\theta > 0$, the process is called the power law process (PLP).

Therefore, the mean function $\Lambda(t)$ is the integral of the intensity function:

$$\Lambda(t) = \int_0^t \lambda(t) dt = \int_0^t \frac{\beta}{\theta} \left(\frac{t}{\theta} \right)^{\beta-1} = \left(\frac{t}{\theta} \right)^{\beta}$$

6.3.1

6.3.2 Bayesian estimation based on simulated data

Chapter 7

HIERARCHICAL BAYESIAN MODELS USING SUBSAMPLING MARKOVE CHAIN MONTE CARLO METHODS

- Comparison with results given by frequentist models using REML (`lmer4`)
- Comparison with results given by Bayesian models using HMC (`rstan`)
- Comparison with results given Bayesian models using INLA (`INLA`)

Chapter 8

DISCUSSION

APPENDIX

Data query

Weather data

```
gps_sample =  
  structure(list(  
    from_lat = c(41.3473127, 41.8189037, 32.8258477, 40.6776808,  
                 40.2366043, 41.3945561, 32.6320605, 40.5413856,  
                 33.6287422, 40.0692742, 41.347986, 37.7781459,  
                 43.0843081, 41.48026, 43.495149, 41.5228684,  
                 41.5763081, 47.6728665, 41.0918361, 41.1537819),  
    from_lon = c(-74.2850908, -73.0835104, -97.0306677, -75.1450753,  
                 -76.9367494, -72.8589916, -96.8538145, -74.8547061,  
                 -113.7671634, -76.762612, -74.284785, -77.4615586,  
                 -76.0977384, -73.2107541, -73.7727896, -74.0739204,  
                 -88.1529175, -117.3224667, -74.1554972, -74.1887031),  
    beg_time = structure(  
      c(1453101738, 1437508088, 1436195038, 1435243088, 1454270680,  
        1432210106, 1438937772, 1446486480, 1450191622, 1449848630,  
        1457597084, 1432870446, 1457968284, 1451298724, 1431503502,  
        1443416864, 1438306368, 1445540454, 1452619392, 1436091072),  
      class = c("POSIXct", "POSIXt"), tzone = "UTC")),  
    .Names = c("from_lat", "from_lon", "beg_time"),  
    row.names = c(NA, 20L),  
    class = c("tbl_df", "tbl", "data.frame"))  
gps_sample
```

```
library(darksky)  
add_var = function(dat){  
  dat[,c("time", "summary", "icon", "precipIntensity",  
         "precipProbability", "temperature", "apparentTemperature",  
         "dewPoint", "humidity", "pressure", "windSpeed", "windGust",  
         "windBearing", "cloudCover", "visibility")] = NA  
  return(dat)  
}
```

```

for(i in 1:nrow(gps_sample)){
  t = get_forecast_for(gps_sample$from_lat[i], gps_sample$from_lon[i],
                      gps_sample$beg_time[i])
  gps_sample$summary[i] = ifelse(is.null(t[[3]]$summary), NA,
                                t[[3]]$summary)
  gps_sample$icon[i] = ifelse(is.null(t[[3]]$icon), NA, t[[3]]$icon)
  gps_sample$precipIntensity[i] = ifelse(is.null(t[[3]]$precipIntensity),
                                         NA, t[[3]]$precipIntensity)
  gps_sample$precipProbability[i] = ifelse(is.null(t[[3]]$precipProbability),
                                           NA, t[[3]]$precipProbability)
  gps_sample$temperature[i] = ifelse(is.null(t[[3]]$temperature), NA,
                                     t[[3]]$temperature)
  gps_sample$apparentTemperature[i] = ifelse(is.null(
    t[[3]]$apparentTemperature), NA, t[[3]]$apparentTemperature)
  gps_sample$dewPoint[i] = ifelse(is.null(t[[3]]$dewPoint), NA,
                                  t[[3]]$dewPoint)
  gps_sample$humidity[i] = ifelse(is.null(t[[3]]$humidity), NA,
                                  t[[3]]$humidity)
  gps_sample$pressure[i] = ifelse(is.null(t[[3]]$pressure), NA,
                                  t[[3]]$pressure)
  gps_sample$windSpeed[i] = ifelse(is.null(t[[3]]$windSpeed), NA,
                                   t[[3]]$windSpeed)
  gps_sample$windGust[i] = ifelse(is.null(t[[3]]$windGust), NA,
                                   t[[3]]$windGust)
  gps_sample$windBearing[i] = ifelse(is.null(t[[3]]$windBearing), NA,
                                     t[[3]]$windBearing)
  gps_sample$cloudCover[i] = ifelse(is.null(t[[3]]$cloudCover), NA,
                                    t[[3]]$cloudCover)
  gps_sample$visibility[i] = ifelse(is.null(t[[3]]$visibility), NA,
                                    t[[3]]$visibility)
}

```

Road geometry data

```

pacman::p_load(osmar, stringr)
src <- osmsource_api(url = "https://api.openstreetmap.org/api/0.6/")
road_data = function(i = 5, width = 100, data = df3){
  bb <- center_bbox(data$lon_short[i], data$lat_short[i],
                    width, width)
  ua = get_osm(bb, source = src)
  ua
  road_inf <- data.frame(ua$ways$tags)
  colnames(road_inf) <- c("ID", "Key", "Value")
}

```

```

road_inf$Key <- as.character(road_inf$Key)
road_inf$Value <- as.character(road_inf$Value)
row_speed <- which(road_inf$Key == "maxspeed", arr.ind=TRUE)
row_lane <- which(road_inf$Key == "lanes", arr.ind=TRUE)

max_speed <- as.numeric(str_extract(road_inf[row_speed, "Value"],
                                   "[[:digit:]]+"))
num_lanes <- as.numeric(str_extract(road_inf[row_lane, "Value"],
                                   "[[:digit:]]+"))
return(c(mean(max_speed), mean(num_lanes)))
}

loop_data = function(start_index = 1, loop_length = 100000){
  end_index = start_index + loop_length
  out_data = data.frame(matrix(0, ncol = 2, nrow = loop_length))
  df_index_diff = start_index-1

  for (i in start_index:end_index) {
    out_data[i-df_index_diff,] = road_data(i, data = df)
    print(paste0(end_index - i, " remained (",
                  round((end_index - i)*100/
                        (end_index-df_index_diff), 3), "%)")
  )
  }

  return(out_data)
}

df = data.table::fread("data/20190605_ping_compressed_3digits.csv")
dfcontainer12 = loop_data(start_index = 1)

```


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