

non-crashes is unknown. Besides, retrospective reports are often subject to recall and report bias: the drivers may not accurately recall the exact conditions at the time of the event; they may intentionally conceal some critical facts to escape from legal punishment (Dingus et al., 2011; Stern et al., 2019).

Naturalistic driving studies (NDSs) have been emerging in the past decade thanks to the advancement of technology. An NDS continuously collects driving data (including latitude, longitude, and speed) under real-world conditions using on-board unobtrusive equipment (Guo, 2019). In contrast to retrospective reports, an NDS resembles a cohort study: a pre-determined set of drivers are prospectively followed for a certain amount of time. Therefore, NDS comparatively has several advantages. First, NDS collects both crashes and non-crashes, so it is more useful in comparing the rates of events. Second, since vehicle crashes are extremely rare, it may take a huge amount of driving time to have sufficient sample of crashes. Instead, NDS focus safety-critical events (SCEs), which is defined as events that avoid crashes by last-second evasive maneuver (Dingus et al., 2011). SCEs can be 1000 times as high as real crashes and are argued to be good surrogates of crashes (Dingus et al., 2011; Guo et al., 2010). Third, NDS data are collected using programmed instruments or sensors, therefore they are less likely to be subject to human error or manipulation. Lastly, NDS collects data every a few seconds to minutes, and this large-scale high-resolution data provide a promising opportunity to quantifying driving risk (Guo, 2019).

However, many issues arise given the characteristics of NDSs. First, the sheer volume of NDS data creates a challenge to data management and aggregation (Mannering and Bhat, 2014). For example, a NDS data set can have billions rows of real-time speeds and locations, and it is important to have scalable and high-performance tools to aggregate these data into units that fit into the framework of statistical modeling. Second, routinely collected NDS data only have vehicle driving data. Crucial environmental variables such as weather and traffic need to be accessed from other sources and merged back to the driving data. Third, even with these data sources, management, and aggregation issues solved, scalable statistical models that account for the characteristics of NDS are needed to analyze the aggregated data.

A brief review of previous NDS analytic studies.

With increasing vehicle and insurance companies collecting NDS data on a regular basis, a scalable and generalizable analyzing framework serves as a pattern for follow-up researchers to better understand NDS data and gain insights into transportation safety. In this paper, we proposed a framework for data collection, aggregation, fusing, and statistical modeling, which is demonstrated in a case study. Although the NDS data used in this study were from large commercial truck drivers, the framework is generalizable to other drivers since the data collected among different drivers are similar.

57 2. Data

58 The data were collected by a leading freight shipping trucking company (we will name it as Company A for
59 confidentiality reasons) in the United States. From April 2015 to March 2016, Company A installed in-vehicle data
60 acquisition systems (DAGs) to all their trucks, which collect real-time *ping* and *SCEs* data. For demonstration
61 purposes, we selected 496 regional drivers who move freights in a region that can include surrounding states. Apart
62 from these vehicle driving data, demographic variables including age, gender, and race were also provided by
63 Company A. The names of the drivers were not provided to the research team to ensure confidentiality, while a
64 unique identification number was provided for each driver to link the three data sources. The study protocol was
65 reviewed and approved by the Institutional Review Board of Saint Louis University.

66 2.1. *ping* and *SCEs* data

67 Every a couple of seconds to minutes, the DAG collects the date and time (year, month, day, hour, minute, and
68 second), latitude and longitude (specific to five decimal places), driver identity number, and speed at that second.
69 In total, 13,187,289 pings were provided to the research team.

70 SCEs. Besides, the company also regularly collected real-time GPS location and time-stamped critical events
71 data for all their trucks. There were 12,458 critical events occurred to these 498 truck drivers during the study
72 period. Four types of critical events were recorded in this critical events data. The number of SCEs.

73 2.2. *Weather*

74 Apart from driver’s characteristics and driving condition, weather also poses a threat on truck crashes and
75 injuries (Naik et al., 2016; Uddin and Huynh, 2017; Zhu and Srinivasan, 2011). We obtained historic weather data
76 from the DarkSky Application Programming Interface (API), which allows us to query real-time and hour-by-hour
77 nationwide historic weather conditions according to latitude, longitude, date, and time (The Dark Sky Company,
78 LLC, 2019). The variables included visibility, precipitation probability¹ and intensity, temperature, wind and others.

79 2.3. *Other available sources*

80 Traffic and road geometry can be collected from Google map API and OpenStreet API.

¹Ideally, historic precipitation at a specific location and time should be yes or not. However, in reality, since the weather stations are distributed not densely enough to record the exact weather conditions in every latitude and longitude in the US, the DarkSky API uses their algorithms to infer the probability of precipitation in each location.

3. Data preparation

3.1. Data aggregation

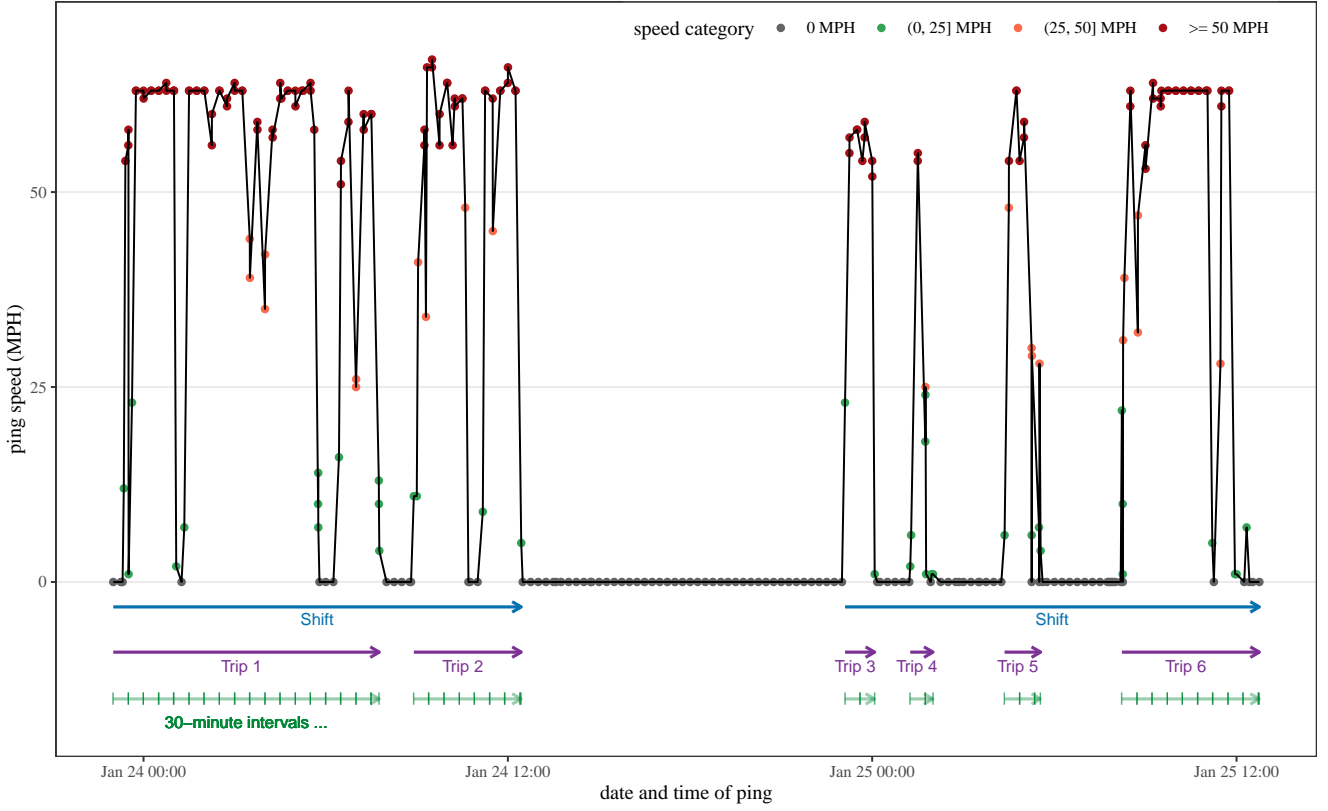


Figure 1: Data aggregation process from pings to shifts, trips, and 30-minute intervals.

To shrink the large size of over 10 million ping data, we rounded the GPS coordinates to the second decimal places, which are worth up to 1.1 kilometers, and we also round the time to the nearest hour. We then queried weather variables from the DarkSky API using the approximated latitudes, longitudes, date and hour. The weather variables used in this study include precipitation probability, precipitation intensity, and visibility.

For each of the truck drivers, if the ping data showed that the truck was not moving for more than 20 minutes, the ping data were separated into two different trips. These ping data were then aggregated into different trips. A **trip** is therefore defined as a continuous period of driving without stop. As Table demonstrates, each row is a trip. The average length of a trip in this study is 2.31 hours with the standard deviation of 1.8 hours.

After the ping data were aggregated into trips, these trips data were then further divided into different shifts according to an eight-hour rest time for each driver. A **shift** is defined as a long period of driving with potentially less than 8 hours' stops. The Shift_ID column in shows different shifts, separated by an eight-hour threshold. The average length of a shift in this study is 8.42 hours with the standard deviation of 2.45 hours.

95 3.2. Cumulative driving time as a measure of fatigue

96 Fatigue has been reported to be the most important predictor to truck crashes, considering that truck drivers are
97 exposed to long routes and lone working environment Stern et al. (2019).

98 Driver's fatigue is difficult to measure in real life. In this study, we attempt to use three proxies to measure the
99 fatigue of the truck drivers: cumulative driving time in a shift, the rest time before a shift, and the rest time before
100 a trip.

101 4. Methodology

102 4.1. Statistical models

103 Traditional statistical models assume that observations are independent from each other given their predictor
104 variables. However, natural data are almost never independent given the predictor variables. In the example of truck
105 driver's safety events, if we assume the external traffic, weather and driver's socioeconomic status are fixed, truck
106 drivers may exhibit similar driving patterns in multiple trips, and then drivers hired by the same company may
107 share similar culture and safety atmospheres. Therefore, traffic accidents are naturally nested within drivers and
108 drivers are nested within companies. Traditional statistical models that assume independence between observations
109 are not appropriate in this case since objects tend to be similar within a group. Hierarchical models, also known as
110 multilevel model, random-effects model or mixed model, have been developed to allow for the nested nature of data.
111 Instead of assuming independence given predictor variables, hierarchical models assume conditional independence.
112 Hierarchical models are advocated to be the default method since they can produce more precise prediction and
113 more robust results than traditional models.

114 Random-effects models (Han et al., 2018; Pantangi et al., 2019).

Here we model the probability of a critical event occurred using a Bayesian hierarchical Bernoulli regression. We categorized the number of safety events during a trip into a binary variable Y with the value of either 0 or 1, where 0 indicated that no critical event occurred during that trip while 1 indicated that at least 1 critical event occurred during the trip. Since each trip i has a different travel time t_i , we derived the Bernoulli distribution parameter p_i using the probability density function of the Poisson distribution, with the parameter λ_i equaled a linear combination of β_i and x_i .

$$\begin{aligned} P_i &= P(\text{at least one event in trip } i) \\ &= 1 - P(\text{no event in trip } i) \\ &= 1 - \frac{e^{-t_i \lambda_i} (t_i \lambda_i)^0}{0!} \\ &= 1 - \exp(-t_i \lambda_i) \\ &= 1 - \exp(-t_i e^{\beta_0 + \beta_i x_i}) \end{aligned} \tag{1}$$

Transform that into a linear function of β_i, x_i and t_i

$$\begin{aligned}
1 - P_i &= \text{EXP}(-t_i e^{\beta_0 + \beta_i x_i}) \\
\log(1 - P_i) &= -t_i e^{\beta_0 + \beta_i x_i} \\
\log \frac{1}{1 - P_i} &= e^{\beta_0 + \beta_i x_i + \log(t_i)} \\
\log \left(\log \frac{1}{1 - P_i} \right) &= \beta_0 + \beta_i x_i + \log(t_i)
\end{aligned} \tag{2}$$

Then, the random effects logistic model is

$$\begin{aligned}
Y_i &\sim \text{Bern}(P_i) \\
\log \left(\log \frac{1}{1 - P_i} \right) &= \beta_{0,d(i)} + \beta_{1,d(i)} \cdot \text{CT}_i + \xi \cdot \mathbf{W} + \nu \cdot \mathbf{D}_i + \log(t_i)
\end{aligned} \tag{3}$$

Here the trip is indexed by i , Y_i is the binary outcome variable of whether at least one critical event occurred in trip i ; $d(i)$ is the driver for trip i , $\beta_{0,d(i)}$ is the random intercept for driver $d(i)$; $\beta_{1,d(i)}$ is the random slope for the cumulative time (CT i) of driving in the shift (the sum of driving time for all previous trips) for driver $d(i)$; \mathbf{W} is a vector of external environment fixed effects, including precipitation intensity and probability, visibility, and whether it was sunrise or sunset time; \mathbf{D}_i are driver level fixed effects, including age group and business unit; t_i is the travel time for the trip i .

We assume that the drivers are random effects, and we assume exchangeable priors of the form

$$\beta_{0,d(1)}, \beta_{0,d(2)}, \dots, \beta_{0,d(n)} \sim \text{i.i.d.} N(\mu_0, \sigma_0^2)$$

and

$$\beta_{1,d(1)}, \beta_{1,d(2)}, \dots, \beta_{1,d(n)} \sim \text{i.i.d.} N(\mu_1, \sigma_1^2)$$

The parameters μ_0, σ_0, μ_1 , and σ_1 are hyperparameters with priors. Since we do not have much prior knowledge on the hyperparameters, we assigned diffuse priors for these hyperparameters.

$$\begin{aligned}
\mu_0 &\sim N(0, 10^2) \\
\mu_1 &\sim N(0, 10^2) \\
\sigma_0 &\sim \text{GAMMA}(1, 1) \\
\sigma_1 &\sim \text{GAMMA}(1, 1)
\end{aligned} \tag{4}$$

Since μ_0 and μ_1 can be any real number, so we assigned two normal distributions with mean of 0 and standard deviation of 10 as the priors for these two hyperparameters. In comparison, σ_0 and σ_1 must be strictly positive, so

we assigned $\text{GAMMA}(1, 1)$ with wide distribution on positive real numbers as their priors.

5. Results

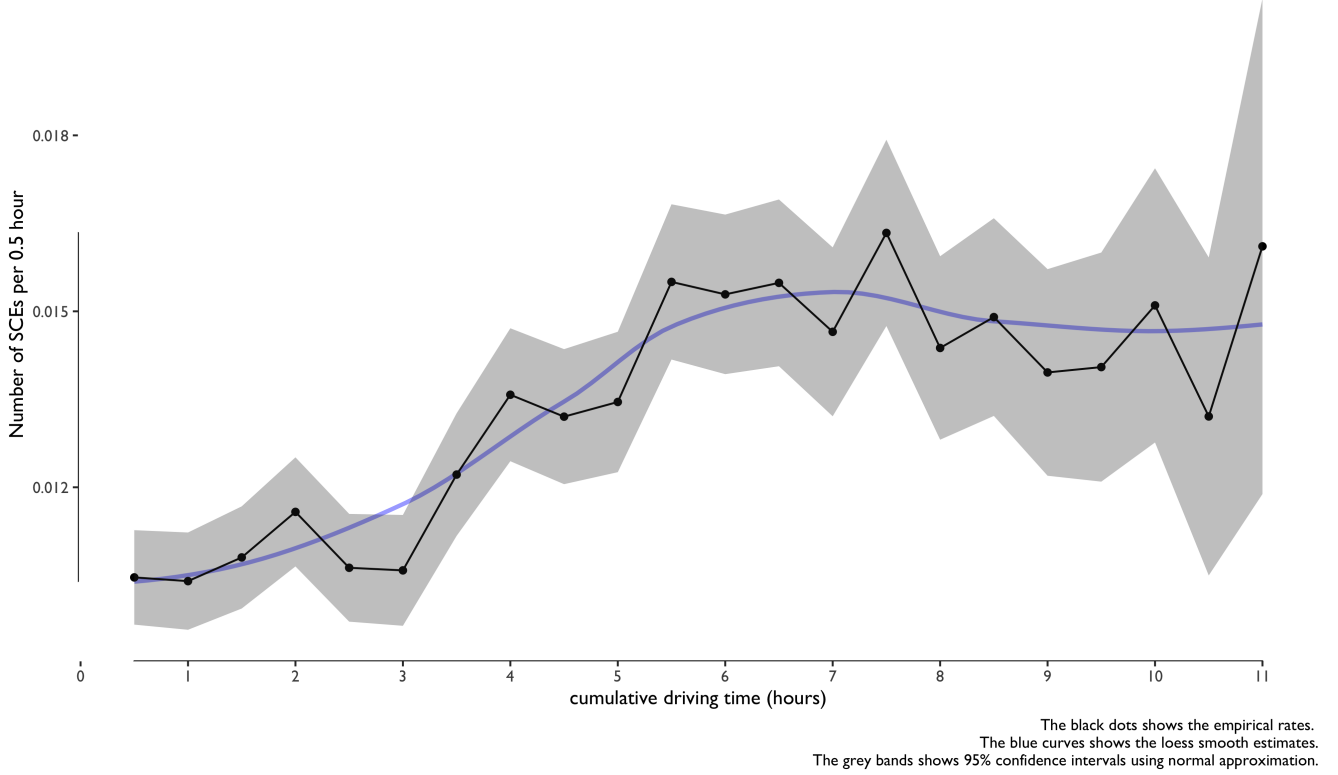


Figure 2: The rate of safety critical events and cumulative driving time

6. Discussion

7. Conclusions

Subsampling MCMC (Dang et al., 2019; Quiroz et al., 2019, 2018, 2016).

Acknowledgement

This work was supported in part by the National Science Foundation (CMMI-1635927 and CMMI-1634992), the Ohio Supercomputer Center (PMIU0138 and PMIU0162), the American Society of Safety Professionals (ASSP) Foundation, the University of Cincinnati Education and Research Center Pilot Research Project Training Program, and the Transportation Informatics Tier I University Transportation Center (TransInfo). We also thank the DarkSky company for providing us five million free calls to their historic weather API.

References

- Blower, D., Green, P.E., Matteson, A., 2010. Condition of trucks and truck crash involvement: Evidence from the large truck crash causation study. *Transportation Research Record* 2194, 21–28.
- Cantor, D.E., Corsi, T.M., Grimm, C.M., Özpolat, K., 2010. A driver focused truck crash prediction model. *Transportation Research Part E: Logistics and Transportation Review* 46, 683–692.
- Chen, C., Zhang, G., Tian, Z., Bogus, S.M., Yang, Y., 2015. Hierarchical bayesian random intercept model-based cross-level interaction decomposition for truck driver injury severity investigations. *Accident Analysis & Prevention* 85, 186–198.
- Dang, K.-D., Quiroz, M., Kohn, R., Tran, M.-N., Villani, M., 2019. Hamiltonian Monte Carlo with energy conserving subsampling. *Journal of Machine Learning Research* 20, 1–31.
- Dingus, T.A., Hanowski, R.J., Klauer, S.G., 2011. Estimating crash risk. *Ergonomics in Design* 19, 8–12.
- Dong, C., Dong, Q., Huang, B., Hu, W., Nambisan, S.S., 2017. Estimating factors contributing to frequency and severity of large truck-involved crashes. *Journal of Transportation Engineering, Part A: Systems* 143, 04017032.
- Guo, F., 2019. Statistical methods for naturalistic driving studies. *Annual Review of Statistics and Its Application* 6, 309–328.
- Guo, F., Klauer, S.G., Hankey, J.M., Dingus, T.A., 2010. Near crashes as crash surrogate for naturalistic driving studies. *Transportation Research Record* 2147, 66–74.
- Han, C., Huang, H., Lee, J., Wang, J., 2018. Investigating varying effect of road-level factors on crash frequency across regions: A bayesian hierarchical random parameter modeling approach. *Analytic methods in accident research* 20, 81–91.
- Hickman, J.S., Hanowski, R.J., Bocanegra, J., 2018. A synthetic approach to compare the large truck crash causation study and naturalistic driving data. *Accident Analysis & Prevention* 112, 11–14.
- Mannering, F.L., Bhat, C.R., 2014. Analytic methods in accident research: Methodological frontier and future directions. *Analytic methods in accident research* 1, 1–22.
- Meuleners, L., Fraser, M.L., Govorko, M.H., Stevenson, M.R., 2017. Determinants of the occupational environment and heavy vehicle crashes in western australia: A case-control study. *Accident Analysis & Prevention* 99, 452–458.
- Naik, B., Tung, L.-W., Zhao, S., Khattak, A.J., 2016. Weather impacts on single-vehicle truck crash injury severity. *Journal of Safety Research* 58, 57–65.
- National Highway Traffic Safety Administration, 2017. A Compilation of Motor Vehicle Crash Data from the Fatality Analysis Reporting System and the General Estimates System.
- Pantangi, S.S., Fountas, G., Sarwar, M.T., Anastasopoulos, P.C., Blatt, A., Majka, K., Pierowicz, J., Mohan, S.B., 2019. A preliminary investigation of the effectiveness of high visibility enforcement programs using naturalistic driving study data: A grouped random parameters approach. *Analytic Methods in Accident Research* 21, 1–12.

167 Quiroz, M., Kohn, R., Villani, M., Tran, M.-N., 2019. Speeding up MCMC by efficient data subsampling. *Journal*
168 *of the American Statistical Association* 114, 831–843.

169 Quiroz, M., Tran, M.-N., Villani, M., Kohn, R., 2018. Speeding up MCMC by delayed acceptance and data
170 subsampling. *Journal of Computational and Graphical Statistics* 27, 12–22.

171 Quiroz, M., Tran, M.-N., Villani, M., Kohn, R., Dang, K.-D., 2016. The block-Poisson estimator for optimally
172 tuned exact subsampling MCMC. *arXiv preprint arXiv:1603.08232*.

173 Sharwood, L.N., Elkington, J., Meuleners, L., Ivers, R., Boufous, S., Stevenson, M., 2013. Use of caffeinated
174 substances and risk of crashes in long distance drivers of commercial vehicles: Case-control study. *BMJ* 346, f1140.

175 Stern, H.S., Blower, D., Cohen, M.L., Czeisler, C.A., Dinges, D.F., Greenhouse, J.B., Guo, F., Hanowski, R.J.,
176 Hartenbaum, N.P., Krueger, G.P., others, 2019. Data and methods for studying commercial motor vehicle driver
177 fatigue, highway safety and long-term driver health. *Accident Analysis & Prevention* 126, 37–42.

178 The Dark Sky Company, LLC, 2019. Dark Sky API — Overview.

179 Uddin, M., Huynh, N., 2017. Truck-involved crashes injury severity analysis for different lighting conditions on
180 rural and urban roadways. *Accident Analysis & Prevention* 108, 44–55.

181 WHO, 2018. The top 10 causes of death.

182 Zhu, X., Srinivasan, S., 2011. A comprehensive analysis of factors influencing the injury severity of large-truck
183 crashes. *Accident Analysis & Prevention* 43, 49–57.