

Explaining the Macroeconomic Inertia Puzzle

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Abstract

Many macroeconomic models struggle to explain the sluggish response of aggregate variables to sudden shocks and changes in policy. While numerous theories of adjustment frictions and bounded rationality have been proposed to explain this macroeconomic inertia, no consensus has emerged among them. I show that canonical heterogeneous-agent models — [Blanchard \(1985\)](#) perpetual youth and [Bewley \(1986\)](#) incomplete markets — are consistent with aggregate consumption inertia if agents' average expectations of income and interest rates align with survey expectations of these variables. To determine the causes and analyze the policy implications of inertia, I adopt a model of frictional Bayesian learning which can explain patterns of forecast errors in expectations data that existing theories struggle to account for. Incorporating this form of learning into a standard heterogeneous-agent New Keynesian environment, I provide a theory for how inertia arises endogenously. Inertia results when the equilibrium amplification of an initial shock exceeds expectations, causing them to slowly unanchor. This theory yields a novel drawback for inertial monetary policy rules and delayed financing of fiscal deficits. Policy regimes that act more gradually result in longer transmission lags.

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1 Introduction

Macroeconomic variables often respond slowly and persistently to sudden shocks and policy changes¹. Understanding the sources of this macroeconomic inertia is an important challenge for business cycle research for two reasons. First, long lags in monetary and fiscal policy transmission make them unreliable tools for stabilizing business cycle fluctuations (Friedman 1960, Friedman 1968). Second, the textbook New Keynesian model (Woodford 2004, Galí 2015), a leading framework for business cycle analysis, cannot rationalize this fact and instead predicts policy actions have immediate effects. Many theories of adjustment frictions and bounded rationality have been proposed to dampen the highly responsive behavior of forward-looking agents that prevent this model from generating inertia. However, no consensus has emerged as for which theory best accounts for the evidence.

This paper takes a step-by-step approach to assess whether heterogeneous-agent New Keynesian (HANK) models, a modern version of the textbook model, are consistent with inertia in aggregate consumption spending and whether they can explain the deeper reasons why consumption exhibits inertia. I begin by narrowly focusing on the heterogeneous-agent decision problem resulting from these models before adding assumptions on expectation formation and the New Keynesian equilibrium environment.

My first main result is canonical heterogeneous-agent models — the perpetual youth model (Blanchard 1985, Yaari 1965) and the standard incomplete markets model (Bewley 1986, Imrohoroglu 1989, Huggett 1993, Aiyagari 1994) — can reproduce observed consumption inertia if average agents beliefs align with average expectations in survey data, but the standard representative-agent model cannot.

The systematic patterns of forecast errors in the expectations data are not well-explained by many existing theories of bounded rationality that imply systematic under-reaction relative to a rational expectations benchmark. I adopt a model of frictional Bayesian learning that is able to explain these patterns, which are best summarized as “over-extrapolation bias” — the expectation that variables will remain at the level of their most recently observed value. Incorporating this form of learning into an equilibrium HANK model, I proceed to characterize the sources of macroeconomic inertia and how policy transmission is influenced by it.

My second main result explains why canonical heterogeneous-agent models are not just consistent with aggregate consumption inertia but fundamentally contribute to its emergence. An interaction between over-extrapolation bias and the belief multiplier, a key model quantity representing the size of equilibrium amplification, determines whether inertia emerges in the model and how protracted it is. This multiplier is large when the current marginal propensity to consume is high and the elasticity of substitution is low, which I find in the parameter estimates obtained in my first main result.

Model-implied impulse responses with expectations data To test whether heterogeneous-agent models can reproduce observed consumption inertia, I utilize a representation of the aggregate “consumption function” introduced in Auclert et al. (2020), Auclert et al. (2021). This

¹These include monetary policy shocks (Romer and Romer 2004), productivity shocks (Kurmann and Sims 2021), government spending shocks (Ramey 2011), oil price shocks (Känzig 2021), and “max-share” shocks that explain the majority of fluctuations at a business cycle frequency in a large panel of macroeconomic aggregates (Angeletos et al. 2020). For a comprehensive survey of macroeconomic shocks and their propagation, see Ramey (2016).

function takes in the full history of (cross-sectional) average subjective expectations, formed for all future horizons, and realizations of aggregate income and interest rates. Notably, this representation does not require a fully-specified model of expectation formation. Following [Bardóczy and Guerreiro \(2023\)](#) I replace the average subjective expectation of agents within the model with the average expectation reported in survey data. Given these data are available, with a caveat that far-horizon expectations missing from the data must be extrapolated, one can simply plug them into this model representation and evaluate model-implied aggregate consumption.

To assess model-implied consumption impulse responses against empirical ones, I adopt the estimation approach from [Barnichon and Mesters \(2020\)](#) and [Lewis and Mertens \(2022\)](#). This approach differs in two important respects relative to traditional impulse response matching as introduced by [Christiano et al. \(2005\)](#). As mentioned, it replaces model-based assumptions on expectations, such as rational expectations or a particular theory of bounded rationality, with expectations data in each models' aggregate consumption functions. In addition, instead of imposing an equilibrium model that rationalizes these expectations, I directly use empirical impulse responses of realized and expected income and interest rates to compute model-implied impulse responses of consumption given these variables. This avoids the need to choose a model analog for the shock used as the external instrument and alleviates potential bias in consumption parameter estimates due to equilibrium model misspecification ([Canova and Sala 2009](#), [Janssens 2023](#)). Finally, the intuition of "regressing" the model-implied impulse responses against the observed response to estimate parameters can be formalized as a particular application of the generalized method of moments.

The main limitation of this method is that the robustness of my findings relies on the quality of the expectations data. While household survey data may be the most natural proxy for model subjective expectations, most existing data sources lack point forecasts of interest rates, one of the two required consumption inputs. Because of the need to extrapolate medium- and long-horizon expectations from existing data, I also require multiple near-term horizons of expectations data to extrapolate accurately. To address both concerns, I use the Bluechip Economic Indicators and Financial Forecasts forecaster surveys, which contains both real disposable income and interest rate forecasts for multiple horizons.

While I choose forecaster expectations largely out of necessity, it remains important to address concerns that they may differ qualitatively from household expectations ([Candia et al. 2020](#), [Gemmi and Valchev 2023](#)). To assuage concerns, household surveys have been found to exhibit similar forms of expectational bias in expectations of income ([Rozsypal and Schlafmann 2023](#)) that I document in this paper. A recent household survey also finds interest rate expectations align with that of forecasters ([De Silva and Mei 2024](#)) in high stakes decisions. Finally, while households may impart "supply-side" stories to economic fluctuations ([Kamdar and Ray 2023](#), [Andre et al. 2022](#)), potentially misunderstanding the effects of demand and policy shocks, I focus on the response of consumption to an externally-identified oil price news shock from [Känzig \(2021\)](#) in my main application.

Given the dynamics of survey expectations are sufficient to generate model-implied consumption inertia that matches the data, what features or biases explain the expectations data? As in [Angeletos et al. \(2021\)](#) and [Bardóczy and Guerreiro \(2023\)](#), I find the dynamic patterns of forecast errors in survey expectations to be inconsistent with full-information rational ex-

pectations, which requires the ex-ante unpredictability of ex-post forecast errors (Coibion and Gorodnichenko 2015). Most models of expectation formation, which uniformly predict either under- or over-reaction relative to the full-information rational expectations benchmark, fare no better given the asymmetries in bias across variables and time.

The simplest explanation for this bias turns out to be persistent over-extrapolation of the current observation to expectations of future horizons. For example, upon observing the current period’s income realized level conditional on the shock, forecasters’ conditional expectations of future income anchors on the current realization. If income is low today, they expect it to be similarly low tomorrow and so on. This over-extrapolation is also fairly long-lived, in certain cases persisting for many quarters after the initial shock impact period. For variables whose realized response to the shock is monotonically decreasing, this bias appears to be pure over-reaction. However, for those that exhibit an inertial hump-shaped response, this bias first appears to be under-reaction before eventually becoming over-reaction.

Inertia as an equilibrium phenomenon Why do expectations which over-extrapolate result in aggregate consumption inertia? To jointly explain these features of the data and to consider policy counterfactuals, I now impose additional structure in the form of a model of expectation formation, disciplined to the data, and a standard New Keynesian equilibrium environment. I assume expectations are formed with Bayesian learning in an equilibrium environment where fundamental shocks are comprised of transitory and persistent components that are imperfectly observed (Afrouzi et al. 2023, Crump et al. 2023, Farmer et al. 2024, Nagel 2024). This form of learning has been shown to explain systematic patterns in expectations bias in cross-sectional, experimental, and unconditional time-series evidence. In this model, when agents mistakenly attribute a transitory change to a persistent shock, their expectations over-extrapolate the current observation forward.

Inertia occurs when over-extrapolating expectations gradually amplify the equilibrium response of consumption over the direct effect of an exogenous shock. The extent of inertia, that is the duration of amplification, depends in turn on the speed of learning.

While in the rational learning baseline agents will over-extrapolate initially, learning occurs quickly as agents beliefs update away from the persistent component soon after. Therefore, any amplification in the response of real variables to these beliefs will be short-lived. I consider an important deviation from this baseline by imposing agents perceived equilibrium law of motion are “truncated” relative to the state space of the actual equilibrium law of motion. For example, if the actual equilibrium law of motion is a function of the full history shocks, the perceived law of motion may only account for a few recent periods. One interpretation of this friction is as a complexity limit as in Molavi (2022) or a memory constraint as in Azeredo da Silveira et al. (2024).

The consequence in this context is agents cannot fully internalize the general equilibrium consequences of their misinformed actions on the evolution of their future beliefs. Hence, overly responsive consumption to a transitory demand shock, which increases realized income in equilibrium by more than expected, now reinforces beliefs that the shock itself was persistent. This feedback loop results in the endogenous unanchoring of expectations, which prolongs amplification, impedes learning, and results in a greater degree of inertia.

The two key factors that determine consumption inertia, the size of amplification and the

degree of unanchoring, are connected by a simple sufficient statistic χ , which I will refer to as the “belief multiplier”. The multiplier χ increases in the income sensitivity of consumption demand but decreases in the interest rate sensitivity. Consequently, it tends to be large in heterogeneous-agent economies but small or often negative in representative-agent ones. I demonstrate formally that inertia emerges when the belief multiplier χ is positive and sufficiently large but is absent otherwise.

How inertia influences policy transmission The frictions in expectation formation that give rise to inertia introduce new trade-offs in stabilization policy. For the monetary policy examples, I focus on real output stabilization with respect to demand shocks, given the divine coincidence of output and inflation stabilization (Blanchard and Galí 2007) holds in my setting.

The first example I consider builds on an insight by Eusepi et al. (2024). When shocks are imperfectly distinguishable, an overly-responsive Taylor rule on output may destabilize the economy because of its unanchoring effects on expectations. A Taylor rule that is sufficiently but not overly-responsive can shut down the feedback loop that generates inertia by reducing the effective belief multiplier. However, by exercising this restraint the monetary authority must permit some pass-through of the shock it seeks to stabilize. Christiano and Takahashi (2020) derive a similar result where overly-restrictive policy can be undesirable.

Next, I consider the choice of a lagged or “inertial” term in the output Taylor rule. With this specification, interest rate policy responds to current output fluctuations but also partially passes through changes in past policy rates. In standard rational expectations settings, forward-looking agents can understand the dynamic equilibrium implications of interest rates changes due to both of these reasons equally well. Because agents are able to accurately reason about the far-horizon equilibrium effects of interest rates, highly inertial policy rules can have powerful stabilizing effects on current output even if the current response of interest rates is muted.

I compare the counterfactual implications of demand shock transmission under two monetary policy regimes that vary by the degree of policy inertia. These regimes are chosen to obtain the same the discounted sum of squared output deviations, a proxy measure for welfare loss, under rational expectations. However, under frictional learning the “gradual regime” that exhibits higher policy inertia results in larger welfare losses than the low policy inertia. The reason is learning frictions impair agents ability to comprehend the dynamic equilibrium effects that make inertial Taylor rules effective under rational expectations. When the policy response to a demand shock is delayed, agents instead perceive policy to be less responsive overall, resulting in a greater degree of expectations unanchoring.

Learning frictions also alter the transmission of deficit-financed fiscal policy through the same mechanism. Angeletos et al. (2023) show that delayed financing of a one-time, unanticipated transfer can substantially amplify the output response to this policy shock under rational expectations. I consider this exercise under learning frictions and show that the peak response of output to a transfer shock shifts further out in time as financing is delayed. Elevated output persistence due to endogenous expectations unanchoring also significantly shifts the cumulative output response, resulting in a more protracted boom than under rational expectations.

Related literature This paper relates to a large literature that seeks to understand and quantify the sources of macroeconomic inertia. A major strand of this literature focuses on preference- and technology-based explanations for the slow adjustment of aggregate variables, such as consumption, inflation, and investment. The main preference-based approach takes the form of habit formation in consumption spending (Fuhrer 2000, Dynan 2000, Chetty and Szeidl 2016, Havranek et al. 2017). A separate strand relaxes the full-information, rational expectations (FIRE) assumption, dampening the responsiveness of forward-looking decisions to generate inertia. Theories that depart from FIRE and generate inertia include adaptive learning (Evans and Honkapohja 1999, Williams 2003, Eusepi and Preston 2011, Milani 2011), incomplete information (Woodford 2001), sticky information and expectations (Mankiw and Reis 2002, Carroll et al. 2020), and rational and behavioral inattention (Sims 2003, Luo 2008, Maćkowiak and Wiederholt 2015, Gabaix 2019).

Auclert et al. (2020) was the first paper to point out that models with consumption habits and FIRE cannot simultaneously produce sluggish aggregate consumption adjustment and high marginal propensities to consume (MPCs) in line with microeconomic evidence. They demonstrate that heterogeneous-agent New Keynesian (HANK) models capable of matching high MPCs must therefore relax the FIRE assumption to be able to match aggregate consumption inertia. Bardóczy and Guerreiro (2023) extend the methodological approach introduced by Auclert et al. (2020) and demonstrate that HANK models can be estimated by replacing a model of expectation formation directly with expectations data using the impulse response matching estimation framework of Christiano et al. (2005).

My paper builds on the approaches of Auclert et al. (2020) and Bardóczy and Guerreiro (2023) by showing that the same methodology can be applied to estimate parameters of the heterogeneous-agent consumption-savings decision without imposing a model of expectation formation or the New Keynesian equilibrium assumptions. I do this by adopting the instrumental variables approach of Barnichon and Mesters (2020) and Lewis and Mertens (2022). By using current and lagged structural shocks as the set of instruments, the instrumental variables estimation of the heterogeneous-agent model can instead be interpreted as the regression of impulse responses of observed consumption on model-implied consumption conditional on expectations data. This approach allows me to retain the impulse response matching interpretation of my results without needing to compute model-implied impulse responses within a fully-specified equilibrium model or impose a model of expectation formation.

My paper extends from the tradition of a series of papers that use survey expectations data for structural estimation following Manski (2004). Del Negro and Eusepi (2011) incorporate survey inflation expectations into a Bayesian estimation framework for representative-agent equilibrium models with rational expectations. Kosar and O’Dea (2023) discuss wide-ranging applications of expectations data in estimating models of individual and household behavior. Bardóczy and Guerreiro (2023) introduce the use of survey expectations data in HANK estimation.

The main theoretical result in my paper complements the work of Angeletos and Huo (2021) and Christiano et al. (2024), which contain similar mechanisms. In these papers, when measures of equilibrium amplification or complementarity are large, learning is delayed and inertia can be prolonged. In contrast to Angeletos and Huo (2021), the model of expectation formation I adopt admits a tractable form for the belief law of motion, where the amplification param-

eter is a simple function of structural primitives. This allows me to analytically characterize the joint evolution of beliefs with equilibrium outcomes. [Christiano et al. \(2024\)](#) focuses on characterizing the speed of convergence of the perceived equilibrium law of motion to the rational expectations equilibrium. The focus of my analysis is instead on the learning behavior of Bayesian agents with fixed, potentially-flawed perceived laws of motion trying to infer imperfectly observable shocks.

[Molavi \(2022\)](#) is a closely related paper that demonstrates that inertia can arise when agents are constrained to entertain low-dimensional state-space representations of the equilibrium law of motion. I show that this inertia can be exaggerated when distorted beliefs formed by a similar, low-dimensional state-space model are reinforced due to an equilibrium feedback loop that is particularly strong in heterogeneous-agent economies.

[Eusepi et al. \(2024\)](#) demonstrates the equilibrium implications of the same model of expectation formation in a representative-agent New Keynesian model but with a different focus. While these authors prioritize illustrating the limits of short-run stabilization policy when expectations over-extrapolate, a theme I revisit briefly in the policy section of this paper, I focus on the contribution of over-extrapolating expectations in generating inertia and the consequences of this inertia for policy conduct.

2 Model-Implied Impulse Responses Using Expectations Data

This section demonstrates how to compute model-implied impulse responses from structural models with only a limited set of assumptions. The goal is to show how impulse responses using the minimal structure implied by heterogeneous-agent models can rationalize observed aggregate consumption inertia. I first demonstrate how to substitute expectations data into these models in place of a particular model of expectation formation, such as rational expectations. As opposed to specifying an equilibrium environment to determine income and interest rates, I then use empirical impulse responses of realizations and survey expectations of these variables instead. I first illustrate this approach in a familiar representative-agent example and then proceed to the heterogeneous-agent case.

2.1 Representative-agent example

To justify later substituting expectations data, I start by assuming subjective expectations E_t are arbitrary. Given this, a representative household solves the following standard consumption-savings problem

$$\max_{C_t, A_t} \sum_{t=0}^{\infty} \beta^t \zeta_t E_0 \left[\frac{C_t^{1-\sigma^{-1}}}{1-\sigma^{-1}} \right] \quad (1)$$

$$\text{s. to } C_t + A_t = Y_t + (1 + r_{t-1})A_{t-1} \quad (2)$$

The household consumes C_t and saves in a one-period, risk-free asset A_t , taking as given real income Y_t , ex-ante real interest rates r_t , and a discount factor shock ζ_t .

Taking first-order conditions and linearizing around the steady-state $\beta(1+r) = 1$, we obtain the consumption function, given subjective expectations $E_t[\cdot]$. $W_t = r_{t-1}A + (1+r)A_{t-1}$

denotes financial wealth and $\gamma := \sigma - (1 - \beta)A$ denotes the net interest rate elasticity.

$$C_t = (1 - \beta) \left(\sum_{h=0}^{\infty} \beta^h E_t[Y_{t+h}] + W_t \right) - \gamma \sum_{h=0}^{\infty} \beta^{h+1} E_t[r_{t+h}] + \varepsilon_t \quad (3)$$

I will treat ε_t as the primitive demand shock, as opposed to the discount factor shock ζ_t . This shock plays the role of an unobserved source of endogeneity faced by the econometrician in trying to estimate parameters of the household problem. I assume current-period variables Y_t, r_t are directly observed by households in that period and equivalently denoted as horizon $h = 0$ expectations. That is, $E_t[Y_t] \equiv Y_t, E_t[r_t] \equiv r_t$. This serves to simplify the information structure and ease interpretation of the problem. I relax this assumption in the heterogeneous-agent case.

Suppose we want to estimate the model given in Equation (3) to match the empirical impulse response of consumption C_t to an identified exogenous shock z_t . The classic approach in the literature introduced by [Christiano et al. \(2005\)](#) is to impose full-information rational expectations and construct a fully-specified general equilibrium model, which includes Equation (3). Then, choosing a model analog for the shock z_t , one can estimate the model's free parameters by fitting the model impulse response to the empirical one.

Denote the net present value of expected income and rates as

$$\mathcal{Y}_t := \sum_{h=0}^{\infty} \beta^h E_t[Y_{t+h}] \quad (4)$$

$$\mathcal{R}_t := \sum_{h=0}^{\infty} \beta^{h+1} E_t[r_{t+h}] \quad (5)$$

Instead of then imposing assumptions on expectation formation to map $\mathcal{Y}_t, \mathcal{R}_t$ to current period state variables, one could instead substitute expectations data in place of model subjective expectations. Suppose we have imperfectly measured expectations data, denoted E_t^{data} , for all future horizons and substitute them into Equations (4) and (5), denoting the new quantities as $\mathcal{Y}_t^{\text{data}}, \mathcal{R}_t^{\text{data}}$. I collect the differences into the measurement error term $\mu_t := \mathcal{Y}_t - \mathcal{Y}_t^{\text{data}} + \mathcal{R}_t - \mathcal{R}_t^{\text{data}}$. Taken together, we obtain

$$C_t = (1 - \beta) \left(\mathcal{Y}_t^{\text{data}} + W_t \right) - \gamma \mathcal{R}_t^{\text{data}} + \varepsilon_t + \mu_t \quad (6)$$

How do we compute model-implied impulse responses from Equation (6)? Following [Bar-nichon and Mesters \(2020\)](#) and [Lewis and Mertens \(2022\)](#), I adopt a semi-structural approach for computing model-implied impulse responses, which comes as an intermediate step in structural estimation of model parameters. A key intuition from these papers is the equivalence of instrumental variables estimation of Equation (6) using current and lagged values of the shock $\{z_{t-\ell}\}_{\ell \geq 0}$ and ordinary least-squares regression on impulse responses of the variables to the shock z_t . I make the following standard instrumental variables assumptions

$$\text{Unconditional Exogeneity} \quad \mathbb{E}[\varepsilon_t z_{t-\ell}] = \mathbb{E}[\mu_t z_{t-\ell}] = 0, \quad \forall \ell \geq 0$$

$$\text{Rank} \quad \mathbb{E} \left[\mathcal{R}_t^{\text{data}} z_{t-\ell} \right] \neq 0$$

Note $\mathcal{Y}_t^{\text{data}}$ does not show up in the rank condition because the discount factor $\beta = (1 + r)^{-1}$ is a known quantity. The net interest rate elasticity γ contains the elasticity of intertemporal substitution (EIS) σ , which is the only free parameter to estimate. Post-multiplying and taking expectations we see immediately that the new explanatory and response variables are precisely local projection estimands or equivalently impulse responses².

$$\mathbb{E}[C_t z_{t-\ell}] = (1 - \beta) \left(\mathbb{E}[(\mathcal{Y}_t^{\text{data}} + W_t) z_{t-\ell}] \right) - \gamma \mathbb{E}[\mathcal{R}_t^{\text{data}} z_{t-\ell}], \ell \geq 0 \quad (7)$$

Equation (7) can then be interpreted as the impulse response of consumption C_t to the shock $\{z_{t-\ell}\}_{\ell \geq 0}$ implied by the representative-agent model.

To write a more general representation of the consumption function that will lead us to the heterogeneous-agent case, let's re-consider Equation (6). Model-implied consumption C_t is the sum of endogenous and exogenous components, $\mathcal{C}_t, \mathcal{E}_t$ respectively

$$C_t = \mathcal{C}_t(\mathcal{Y}_t^{\text{data}}, \mathcal{R}_t^{\text{data}}, W_t; \sigma) + \mathcal{E}_t(\varepsilon_t, \mu_t) \quad (8)$$

Using the budget constraint (2) we can recursively substitute the asset state A_{t-1} out of Equation (8) to obtain an alternate representation

$$C_t = \mathcal{C}_t(\{\mathcal{Y}_\tau^{\text{data}}, \mathcal{R}_\tau^{\text{data}}, r_{\tau-1} A\}_{\tau \leq t}; \sigma) + \mathcal{E}_t(\{\varepsilon_\tau, \mu_\tau\}_{\tau \leq t}) \quad (9)$$

These representations are connected by a simple but useful intuition. Current financial wealth accumulates the *total* effect of past consumption-savings decisions based on past expectations and realizations on current consumption. By integrating out this state variable, we can instead compute the *individual* contribution of a particular past belief, say $E_\tau^{\text{data}}[Y_{\tau+h}]$, on past expected income $\mathcal{Y}_t^{\text{data}}$ and in turn on current consumption C_t through Equation (9).

While state variables like W_t are low-dimensional in representative-agent models, they can be function-valued in heterogeneous-agent models. This not only complicates the task of measuring them in the data but also makes solving the model itself difficult. However, as I will show in the following section, with a few limited assumptions one can obtain an analogous aggregate consumption function representation to Equation (9) and moment condition (10) in heterogeneous agent models, like the standard incomplete markets model.

To conclude this example, applying our instrumental variables conditions to Equation (9) we have the moment condition that encapsulates model-implied impulse response estimation

$$\mathbb{E}[(C_t - \mathcal{C}_t(\{\mathcal{Y}_\tau^{\text{data}}, \mathcal{R}_\tau^{\text{data}}, r_{\tau-1} A\}_{\tau \leq t}; \sigma)) z_{t-\ell}] = 0, \ell \geq 0 \quad (10)$$

The functional forms of the general moment conditions I will use in model estimation are specified in the following section. They include Equation (10) as a special case.

²Technically these quantities $\mathbb{E}[C_t z_{t-\ell}]$ are just the numerators of the local projection estimands, but we can divide through by the $z_{t-\ell}$ variance term to obtain an equivalent expression in terms of the actual local projection estimand values.

2.2 Heterogeneous-agent consumption functions and moment conditions

I now derive a moment condition akin to Equation (10) for a class of heterogeneous-agent models that include idiosyncratic risk, incomplete markets, and borrowing constraints (Bewley 1986, Imrohoroglu 1989, Huggett 1993, Aiyagari 1994). Doing so allows us to assess whether the heterogeneous-agent, model-implied impulse response of aggregate consumption matches the empirical impulse response well. I first follow Auclert et al. (2020), Auclert et al. (2021), and Bardóczy and Guerreiro (2023)³ to demonstrate how aggregated consumption decisions from a first-order solution of heterogeneous-agent models can be written as functions of histories of average subjective expectations and realizations. I then adopt a separate estimation approach and outline the assumptions required to construct the moment conditions.

Dynamic programming problem setup Suppose individuals- i have time- t subjective expectations $E_{i,t}[\cdot]$. Let an individual- i 's optimization problem be defined by the following value function with common structural parameters θ

$$\mathbf{v}_{i,t} = v(E_{i,t}[\mathbf{v}_{i,t+1}], \mathbf{S}_{i,t}) \quad (11)$$

An individual- i 's state $\mathbf{S}_{i,t} = (\mathbf{s}_{i,t}, \mathbf{X}_t)$ has an idiosyncratic component $\mathbf{s}_{i,t}$ and an aggregate one \mathbf{X}_t . Individuals- i take aggregates \mathbf{X}_t as given⁴, which represent either aggregate exogenous shocks or aggregate endogenous variables determined in equilibrium. I purposefully deviate from the usual definition of the state $\mathbf{S}_{i,t}$, which includes the full information set of expectation $E_{i,t}$, to help conceptually separate variables which directly influence the decision problem in Equation (11) via current constraints and flow payoffs, denoted $\mathbf{S}_{i,t}$, and those that influence expectations, implicit in $E_{i,t}[\cdot]$. This distinction allows me to state assumptions more clearly.

Assumption 1. (Idiosyncratic rationality) Exogenous idiosyncratic states $\mathbf{x}_{i,t} \subset \mathbf{s}_{i,t}$ are stochastic processes described by a finite-state, positive recurrent Markov chain that is common and known across individuals- i .

Because I focus on the effects of common biases in average expectations on aggregate realizations, I reduce the generality of this problem setup, only considering deviations from full-information, rational expectations at the aggregate level. By Assumption 1, subjective expectations $E_{i,t}[\cdot]$ of functions of idiosyncratic states $\mathbf{x}_{i,t}$ are therefore taken with respect to their true density. I place the following additional structure on subjective expectations.

Assumption 2. Individual- i , time- t subjective conditional expectations $E_{i,t}[\cdot]$ satisfy

- a) **Consistency** $E_{i,t}[\mathbf{v}_{i,t+h}] = E_{i,t}[v(E_{i,t+h}[\mathbf{v}_{i,t+h+1}], \mathbf{S}_{i,t+h}; \theta)]$ for $h > 1$ via Equation (11)
- b) **Independence** variables that induce heterogeneity in the information set of $E_{i,t}[\cdot]$ across- i are independent of $\mathbf{s}_{i,t}$
- c) **Law of iterated expectations**

³The problem setup that leads to the consumption function derivation is also outlined in Bardóczy and Guerreiro (2023), albeit focusing on a different representation of this consumption function in terms of forecast errors and revisions. These representations are equivalent.

⁴That is, they act as if they are atomistic with respect to aggregate outcomes \mathbf{X}_t , even though their actions may collectively determine \mathbf{X}_t variables in equilibrium.

The main substantive assumption is independence, which restricts correlated heterogeneity in expectations of aggregate variables with individual-level characteristics. An example of a violation of this assumption would be if individual attention correlated with the incidence of aggregate income on individual income, as in [Guerreiro \(2023\)](#). While this restriction is not innocuous, I proceed with it nonetheless given many theories of bounded rationality with respect to aggregate variables satisfy this condition.

Let \mathcal{I} denote the index set of all individuals- i . The law of motion of the full distribution of individual- i state variables \mathbf{D}_t is then defined by the transition equation

$$\mathbf{D}_{t+1} = \Lambda(\{\mathbf{v}_{i,t}\}_{i \in \mathcal{I}}, \mathbf{X}_t, \mathbf{D}_t) \quad (12)$$

The aggregation of individual decision rules $y_{i,t}(E_{i,t}[\mathbf{v}_{i,t+1}], \mathbf{X}_t; \theta_i)$ is given by

$$Y_t = \mathcal{Y}(\{y_{i,t}(\mathbf{v}_{i,t})\}_{i \in \mathcal{I}}, \mathbf{D}_t) \quad (13)$$

for a scalar, aggregate output variable Y_t .

Definition 1. A **steady state** $(\{\mathbf{v}_i, \mathbf{s}_i\}_{i \in \mathcal{I}}, \mathbf{D}, \mathbf{X}, Y)$ is the constant-valued fixed point consistent with [\(11, 12, 13\)](#).

Given **Assumptions 1, 2** and the system of equations [\(11, 12, 13\)](#), the first-order response (locally around a steady state) of aggregated decisions Y_t to an aggregate shock \mathbf{X}_t is given by

$$Y_t = \sum_{\tau \leq t} \sum_{h \geq 0} \sum_{X \in \mathbf{X}} \mathcal{F}_{t-\tau,h}^X E_\tau[X_{\tau+h}] \quad (14)$$

where $\mathcal{F}_{t-\tau,h}^X$ is the $(t - \tau, h)$ entry of the “fake news” matrix \mathcal{F}^X , defined in [Auclert et al. \(2021\)](#) for an aggregate output variable Y with respect to an aggregate input variable X .

Our earlier representative-agent consumption function fits into the general representation given by Equation (14). Given the standard incomplete markets model of household consumption-savings ([Bewley 1986, Imrohoroglu 1989, Huggett 1993, Aiyagari 1994](#)) can be defined by the above system, a consumption function of the form in Equation (14) can also be derived for this model without having to impose further restrictions on expectation formation.

Let us consider the heterogeneous-agent consumption function from Equation (14) and interpret the coefficients on its typical inputs, income, interest rates, and demand shocks⁵.

$$C_t = \sum_{\tau \leq t} \sum_{h \geq 0} \mathcal{F}_{t-\tau,h}^Y E_\tau[Y_{\tau+h}] + \mathcal{F}_{t-\tau,h}^r E_\tau[r_{\tau+h}] + \mathcal{F}_{t-\tau,h}^\varepsilon E_\tau[\varepsilon_{\tau+h}]$$

Similarly to the representative-agent case in Equation (9), aggregate consumption is a function of both current and past (average) expectations of income, interest rates, and demand shocks. The coefficient $\mathcal{F}_{t-\tau,h}^Y$ can be interpreted as the effect on consumption at time- t of a change in expectations formed at time- τ of time- h income holding all other beliefs and realizations across time and variables fixed. While [Auclert et al. \(2021\)](#) offers a detailed explanation of these terms,

⁵The fake news matrix for ε_t depends on the particular micro-foundation one uses for the primitive demand shock that comprises this exogenous intercept term. For example, if ε_t is a linear combination of discount factor shocks, then \mathcal{F}^ε will be functions of the interest rate matrix \mathcal{F}^r , since discount factor shocks alter consumption similarly to perturbations to the ex-ante interest rate.

I offer an intuitive explanation to help understand its construction.

Suppose at time- τ households suddenly thought income at a future time- h would be higher. They would likely borrow in advance of its receipt to smooth consumption. However, given other beliefs and realizations are fixed, in the next period time- $\tau + 1$ households realize their expectation in the prior period was mistaken, hence the name “fake news”. Nonetheless, the consequences of dissaving in the prior period affected the wealth they inherited this period. This in turn affects their subsequent savings decisions many periods afterward, resulting in consequences that last until (and beyond) time- t .

The logic of the coefficients in \mathcal{F} applies identically whether expectations are formed with full-information rational expectations, or any other deviation satisfying the above assumptions. The simple reason is certainty equivalence due to our first-order solution in aggregates. For example, if households expect future income will be higher, regardless of whether beliefs are accurate or distorted, the first-order impact of those beliefs on their decisions remains the same.

Moment conditions I proceed to construct moment conditions to estimate heterogeneous-agent models using expectations data, following [Barnichon and Mesters \(2020\)](#). Suppose we have a vector of current and lagged structural shocks $\mathbf{z}_t = \{z_{t-\ell}\}_{\ell=0,\dots,N_\ell}$ to use as instruments.

Assumption 3. (Serially uncorrelated) $z_{t-\ell}$ are serially uncorrelated across ℓ

Partition \mathbf{X}_t into variables unobserved by the econometrician, $\boldsymbol{\varepsilon}_t$, and those observed, \mathbf{W}_t .

Assumption 4. (Exogeneity) $\mathbb{E}[E_\tau[\varepsilon_{\tau+h}] z_{t-\ell}] = 0, \quad \forall h \geq 0, \varepsilon_{\tau+h} \in \boldsymbol{\varepsilon}_{\tau+h}, z_{t-\ell} \in \mathbf{z}_t$

This exogeneity condition is slightly more general than the one in the representative-agent example, encompassing the case where shocks may be imperfectly observed by economic agents. If $z_{t-\ell}$ instruments are not systematically predictable by information available prior to time- $t - \ell$, it is natural to assume orthogonality to measurable functions of earlier information sets, i.e. $E_\tau[\varepsilon_{\tau+h}]$ for $\tau < t - \ell$. For $\tau \geq t - \ell$, this assumption requires agents to be aware that even with uncertainty over a given shock $E_\tau[\varepsilon_{\tau+h}]$, they observe $z_{t-\ell}$ and understand it to be orthogonal to time- t information relevant for determining $\varepsilon_{\tau+h}$. Alternatively, one could directly assume the shocks are observable by agents, obtaining the standard exogeneity condition stated previously.

Assume **Assumptions 1, 2, 3, 4**. Given cross-sectional average, subjective expectations $E_t[\cdot]$, a vector of instruments \mathbf{z}_t , and applying Equation (14), where $\mathbf{W} \subseteq \mathbf{X}$ denotes the subset of aggregate inputs \mathbf{X} that are observable to the econometrician, we obtain the following N_ℓ moment conditions

$$\mathbb{E} \left[\left(Y_t - \sum_{\tau=t-\ell}^t \sum_{h \geq 0} \sum_{\mathbf{W} \in \mathbf{W}} \mathcal{F}_{t-\tau,h}^{\mathbf{W}}(\boldsymbol{\theta}) E_\tau[W_{\tau+h}] \right) z_{t-\ell} \right] = 0, \quad \text{for } z_{t-\ell} \in \mathbf{z}_t$$

where we make the dependence of the fake news entries \mathcal{F} on the structural parameter vector $\boldsymbol{\theta}$ explicit.

Suppose we have data on realizations and cross-sectional average expectations of observed inputs up to a finite horizon H , denoted by $\{E_t^{\text{data}}[\mathbf{W}_{t+h}]\}_{h \leq H}$. Let $\boldsymbol{\vartheta}$ denote a parameter vector for an auxiliary model fit to the data to extrapolate missing horizons $h > H$. For example, $\boldsymbol{\vartheta}$ could be coefficients of a VAR(p) process fit to $\{E_t^{\text{data}}[\mathbf{W}_{t+h}]\}_{h \leq H}$ across horizons h .

Let $F_t[\mathbf{W}_{t+h}; \boldsymbol{\theta}]$ be an auxiliary parametric model of expectation $E_t[\mathbf{W}_{t+h}]$ with parameter vector $\boldsymbol{\theta}$. Given a loss function $\mathcal{L}(\cdot, \cdot)$, we can solve for the best-fitting ...

$$\hat{\boldsymbol{\theta}} = \arg \min_{\boldsymbol{\theta}} \mathcal{L}(\{F_t[\mathbf{W}_{t+h}; \boldsymbol{\theta}], E_t^{\text{data}}[\mathbf{W}_{t+h}]\}_{h \leq H})$$

Let expectations data augmented with the missing horizons from the auxiliary model be $\{E_t^{\text{data}}[\mathbf{W}_{t+h}; \boldsymbol{\theta}]\}_{h \geq 0}$.

Assumption 5. (Measurement error exogeneity)

$$\mathbb{E}[(E_\tau[W_{\tau+h}] - E_\tau^{\text{data}}[W_{\tau+h}; \hat{\boldsymbol{\theta}}])z_t] = 0, \quad \forall \tau \leq t, W_{\tau+h} \in \mathbf{W}_{\tau+h}, z_t \in \mathbf{z}_t$$

Given data $\{\mathbf{z}_t, Y_t, \{E_t^{\text{data}}[\mathbf{W}_{t+h}]\}_{h \leq H}\}$ and the fitted model $F_t[\cdot; \hat{\boldsymbol{\theta}}]$, we obtain

$$\mathbb{E} \left[\left(Y_t - \sum_{\tau=t-\ell}^t \sum_{h \geq 0} \sum_{W \in \mathbf{W}} \mathcal{F}_{t-\tau, h}^W(\boldsymbol{\theta}) E_\tau^{\text{data}}[W_{\tau+h}; \hat{\boldsymbol{\theta}}] \right) z_{t-\ell} \right] = 0, \quad \text{for } z_{t-\ell} \in \mathbf{z}_t \quad (15)$$

Equation (15) is a collection of unconditional moment conditions, which can be estimated with two-step generalized method of moments (Newey and McFadden 1994). The first step is the estimation of the nuisance parameter $\boldsymbol{\theta}$ used to extrapolate missing data. Following that one can evaluate the moment condition to estimate the structural parameters of interest $\boldsymbol{\theta}$. Using Equation (15), I construct the following set of moment conditions for the heterogeneous-agent models that I estimate in the following section.

$$\mathbb{E} \left[\left(C_t - \sum_{\tau=t-\ell}^t \sum_{h \geq 0} \mathcal{F}_{t-\tau, h}^Y(\boldsymbol{\theta}) E_\tau[Y_{\tau+h}; \hat{\boldsymbol{\theta}}] + \mathcal{F}_{t-\tau, h}^r(\boldsymbol{\theta}) E_\tau[r_{\tau+h}; \hat{\boldsymbol{\theta}}] \right) z_{t-\ell} \right] = 0, \quad \text{for } z_{t-\ell} \in \mathbf{z}_t \quad (16)$$

As before, we can interpret the quantities contained in the moment conditions as impulse response coefficients with respect to $z_{t-\ell}$.

Remarks The intuition of the additional Assumption 5 is that the expectations data we use, even for directly observed horizons $h \leq H$, may be an imperfect measurement of the model subjective expectations. This assumption will typically hold for measurement error due purely to noise, such as classical measurement error. However, I will later provide substantive and specific arguments for its validity because of my need to use professional forecaster expectations in place of household expectations when estimating consumption functions. The substance of this assumption is that the expectations data used must respond similarly to how we think agents' expectations in the model would respond. This will inform my choice of instruments, which I discuss in depth in the following section.

There is typically sparse availability of expectations data with a large set of horizons H . Therefore, choosing an auxiliary model with a large number of parameters $\boldsymbol{\theta}$ may overfit the noise in expectations data, potentially violating Assumption 5. While not explicitly testable, I err on the side of caution by choosing auxiliary models with few parameters. The choice of these models is informed by the impulse response interpretation of moment condition (15) when using exogenous structural shocks and their lags as instruments. As discussed briefly in Barnichon and Mesters (2020), exploiting the typical assumptions implied by structural models

that impulse response functions are smooth justifies the focus on low-dimensional auxiliary models for extrapolation.

3 Estimating Model-Implied Consumption Impulse Responses

This section evaluates model-implied impulse responses of aggregate consumption from a set of standard heterogeneous-agent models against the response of realized consumption to an externally-identified, exogenous supply shock. Typical impulse response matching as in [Christiano et al. \(2005\)](#) is done in the context of a fully-specified equilibrium model, requiring assumptions on expectation formation and the equilibrium environment. I instead adopt a semi-structural approach, using the consumption function implied by these models as a set of cross-variable restrictions on consumption, income, and interest rates in an otherwise empirical impulse response estimation setting. This allows me to focus solely on these models' ability to match realized consumption dynamics, taking as given data on realized and expected income and interest rates.

3.1 Consumption functions from structural consumption-savings models

While I focus on demonstrating the fit of heterogeneous-agent models to macroeconomic data, it is useful to contrast them with a representative-agent benchmark. Recall the earlier-derived representative-agent consumption function in Equation (3), omitting the shock for brevity.

$$C_t = (1 - \beta) \left(\sum_{h=0}^{\infty} \beta^h E_t[Y_{t+h}] + W_t \right) + \gamma \sum_{h=0}^{\infty} \beta^{h+1} E_t[r_{t+h}]$$

The first heterogeneous agent model I consider is the tractable perpetual youth, overlapping generations model from [Angeletos et al. \(2023\)](#), which builds on [Yaari \(1965\)](#), [Blanchard \(1985\)](#). The consumption function from the model solution linearized around steady state $\beta(1 + r) = 1$ is

$$C_t = (1 - \beta\omega) \left(\sum_{h=0}^{\infty} (\beta\omega)^h E_t[Y_{t+h}] + W_t \right) - \gamma \sum_{h=0}^{\infty} (\beta\omega)^h E_t[r_{t+h}] \quad (17)$$

where aggregate wealth is given by W_t and the net interest elasticity $\gamma := \sigma\beta\omega - (1 - \beta\omega)\beta A$.

The attractiveness of this model is it closely mirrors its representative-agent counterpart, albeit with one additional degree of freedom, $\omega \in [0, 1]$, the perpetual youth hazard rate. When $\omega < 1$ the overlapping generations model exhibits greater income sensitivity of consumption, for example as measured by the current marginal propensity to consume (MPC) out of unearned income. Given the discount factor β is pinned down in both models by the steady state real interest rate r , it is not a degree of freedom for estimation. It will prove useful to compare these two models which differ along this single dimension given their otherwise similar structure.

The second heterogeneous-agent model I consider is the standard incomplete markets model of [Bewley \(1986\)](#), [Imrohoroglu \(1989\)](#), [Huggett \(1993\)](#), [Aiyagari \(1994\)](#). In this model, a unit mass of households face idiosyncratic income risk, borrowing constraints, and incomplete markets in the form of a one-period risk-free asset. The individual- i household problem is given

by

$$\begin{aligned}
V(e_{i,t}, a_{i,t-1}) &= \max_{c_{i,t}, a_{i,t}} \frac{c_{i,t}^{1-\sigma^{-1}}}{1-\sigma^{-1}} + \beta E_t[V(e_{i,t+1}, a_{i,t})|e_{i,t}] \\
c_{i,t} + a_{i,t} &= e_{i,t}Y_t + (1 + r_{t-1})a_{i,t-1} \\
a_{i,t} &\geq 0
\end{aligned}$$

where E_t denotes the time- t subjective expectation. Idiosyncratic productivity $e_{i,t}$ is a stationary, commonly-known Markov process with persistence ρ_e and variance σ_e^2 . It has a fixed transition matrix $\Pi(e, e')$ with an associated stationary distribution $\pi(e)$ and a stationary mean normalized to one, i.e. $\sum_e \pi(e)e = 1$.

I restate here the aggregate consumption function derived in the previous section

$$C_t = \sum_{\tau \leq t} \sum_{h \geq 0} \mathcal{F}_{t-\tau, h}^Y E_\tau[Y_{\tau+h}] + \mathcal{F}_{t-\tau, h}^r E_\tau[r_{\tau+h}] \quad (18)$$

To map model expectations to their data equivalents I will assume that horizon-0 expectations and realizations coincide, i.e. $E_t^{\text{data}}[Y_t] = Y_t$ and $E_t^{\text{data}}[r_t] = r_t$ for all times- t . In general, these consumption functions do not necessarily enforce horizon-0 expectations to align with realizations, where allowing for a wedge between them may be reasonable in certain information settings. One example is a consumption-savings problem where households are rationally inattentive and cannot perfectly observe state variables even after the period they are realized, as in [Luo \(2008\)](#).

All linearized consumption functions are local approximations about a steady state, which I calibrate following [McKay et al. \(2016\)](#).

| Parameter | Description | Value |
|---------------------------------------|--|-------|
| r | Real interest rate | 0.005 |
| $\frac{\text{Assets}}{\text{Income}}$ | Assets to disposable income ratio | 1.4 |
| ρ_e | Idiosyncratic productivity persistence | 0.966 |
| σ_e^2 | Idiosyncratic productivity variance | 0.504 |

Table 1: Steady state model calibration

Note: The real interest rate and disposable income are both listed at a quarterly frequency.

The representative-agent model discount factor β is pinned down by the steady state real interest rate $\beta(1 + r) = 1$. The standard incomplete markets model discount factor β must be calibrated to hit the asset-to-disposable income calibration target for a given value of the elasticity of intertemporal substitution. This leaves these already sparsely parameterized consumption-savings models with few degrees of freedom to estimate, which I report in Table 2. In fact, this is precisely the goal of this estimation: to test the minimal structure implied by these models, without assumptions on expectation formation or a surrounding equilibrium environment.

| Parameter | Description |
|------------|--|
| σ | Elasticity of intertemporal substitution (EIS) |
| ω^* | Perpetual youth hazard rate |

Table 2: Parameters to estimate

Note: * This parameter is only available for estimation in the perpetual youth overlapping generations model.

3.2 Data

The consumption function representations of all models require data on realized and expected real disposable income and interest rates.

Realizations data The income measure I use is real disposable personal income (DSPIC96), sourced from the Bureau of Economic Analysis. The interest rate measure I use is the nominal federal funds rate (DFF), deflated by one-period ahead realized consumer price index inflation (CPIAUCSL), sourced from the Bureau of Labor Statistics.

In typical linearized macroeconomic models without financial frictions, there is a single interest rate due to no-arbitrage conditions on asset choice. In reality, households face different interest rates for saving or borrowing products, which makes the choice of a single interest rate data series non-obvious. Given our consumption functions are local approximations around a steady state where all households hold either strictly positive wealth or are borrowing constrained, a savings rate is the best analog to the model interest rate. Due to this, I use the federal funds rate as the data series proxying for the model-based savings rate, given savings rates tend to move closely with the federal funds rate.

Expectations data I use consensus expectations reported by the Bluechip Economic Indicators and Financial Forecasts for real disposable personal income, the nominal federal funds rate, and CPI inflation. As mentioned earlier, because I am estimating household consumption functions, a household-level survey like the Michigan Survey of Consumers or the Survey of Consumer Expectations conducted by the Federal Reserve Bank of New York would be most ideal. However, given neither of these sources nor other commonly-used household surveys elicit point forecasts of interest rates, we would have to make auxiliary assumptions to map qualitative responses about interest rates in these surveys to point forecasts. In addition, household surveys tend to report a single shorter horizon, typically one-year ahead, and a longer five-to-ten year horizon forecast. Because of the need to extrapolate horizons it is useful to have a more complete term structure of near-term expectations from the Bluechip. For consistency across available data periods, I use Bluechip expectations for one through four-quarters ahead for each forecasted variable.

Instrumental variables There are other substantive reasons that may alleviate some concerns of using forecaster as opposed to household survey expectations. [Rozsypal and Schlafmann \(2023\)](#) analyze household income expectations from the Michigan survey and find evidence of over-persistence bias, where households extrapolate expectations of future income

from realized current income. This is precisely the form of bias I document empirically in upcoming results on forecaster expectations of real disposable income. In recent work, [De Silva and Mei \(2024\)](#) document that household interest rate expectations tend to be close to forecaster expectations during periods of high-stakes decisions, such as home purchases.

However, household and forecaster expectations have been documented to exhibit some systematic differences. [Candia et al. \(2020\)](#) and [Kamdar and Ray \(2023\)](#) find that household expectations overweight “supply-side” narratives, which emphasize the negative co-movement of real variables like real output and inflation, and underweight “demand-side” narratives. [Andre et al. \(2022\)](#) document the mental models households use to understand and form expectations of the economic effects of supply shocks, such as sudden changes in oil prices, are similar to those of forecasters but differ materially for monetary and fiscal policy shocks.

Using shocks which are interpreted in a systematically different way by households and forecasters would violate the measurement error exogeneity assumption. Using a supply shock to instrument forecaster expectations is the best way to address this concern given forecaster and household expectations exhibit qualitatively similar responses to these shocks. Therefore, I estimate model-implied impulse responses with respect to an oil supply news shock from [Känzig \(2021\)](#). Identified using a high-frequency identification approach, this shock captures variation in oil futures prices around a narrow time window of OPEC production announcements.

3.3 Empirical impulse response estimation

To estimate impulse responses of macroeconomic variables and their forecasts, I adopt the proxy structural vector autoregression (VAR) approach, outlined in [Stock and Watson \(2018\)](#) and follow the empirical setup and notation from [Känzig \(2021\)](#) closely. I first estimate a reduced-form VAR, with a constant and a deterministic linear trend

$$\mathbf{Y}_t = \boldsymbol{\alpha} + \delta t + \sum_{l=1}^p \boldsymbol{\beta}_l \mathbf{Y}_{t-l} + \mathbf{u}_t$$

where $\boldsymbol{\alpha}, \delta t, \{\mathbf{Y}_{t-l}\}_{l=0}^p, \mathbf{u}_t$ are vectors of length n and $\boldsymbol{\beta}_l$ is a matrix of dimension $n \times n$. I then adopt the usual assumption that the reduced-form residuals \mathbf{u}_t are a linear combination of i.i.d structural shocks $\boldsymbol{\varepsilon}_t$

$$\mathbf{u}_t = \mathbf{S} \boldsymbol{\varepsilon}_t$$

where $\mathbb{E}[\boldsymbol{\varepsilon}_t] = \mathbf{0}$ and $\mathbb{E}[\boldsymbol{\varepsilon}_t \boldsymbol{\varepsilon}_t'] = \boldsymbol{\Omega}$, a positive, diagonal matrix.

Assuming an instrument z_t satisfies the standard identifying assumptions

$$\begin{aligned} \mathbb{E}[z_t \boldsymbol{\varepsilon}_{1,t}] &= \alpha \neq 0 \\ \mathbb{E}[z_t \boldsymbol{\varepsilon}_{2:n,t}] &= \mathbf{0} \end{aligned}$$

where the structural shock we are identifying is ordered first in the VAR, without loss of generality. I can identify the first column of \mathbf{S} up to sign and scale, which I denote \mathbf{s}_1 , given by

$$\mathbf{s}_1 = \mathbb{E}[z_t \mathbf{u}_t]$$

Finally, to pin down the sign and scale factor $s_{1,1} := \frac{\mathbb{E}[z_t u_{1,t}]}{x}$ for the econometrician's desired value x , I can normalize the impact effect of the identified shock on variable $y_{1,t} = x$, using the re-scaled structural impact vector $\tilde{s}_1 = s_1/s_{1,1}$ provided $\mathbb{E}[z_t u_{1,t}] \neq 0$.

Specification The variables included in the baseline specification are real gross domestic product, real disposable income, the consumer price index (CPI), the nominal federal funds rate, real oil price and world oil production measures. The real oil price is the WTI crude oil price deflated by CPI inflation and will be the proxy SVAR's first-stage variable, scaled such that the on-impact effect of a positive oil supply news shock increases real oil prices by 10 percentage points. I then augment the baseline specification with real personal consumption expenditures and Bluechip expectations at each horizon- h period ahead one variable at a time. The data are measured at a quarterly frequency and in log-levels, aside from the federal funds rate. The time period spans 1985-Q1 through 2017-Q3, due to availability of the Bluechip data.

3.4 Impulse responses of income and interest rates to an oil shock

The upper panel of Figure 1 displays impulse responses of realizations and Bluechip expectations of real income and real interest rates. In response to an inflationary oil shock, realized (black line) real income and real interest rates exhibit a prolonged decline.

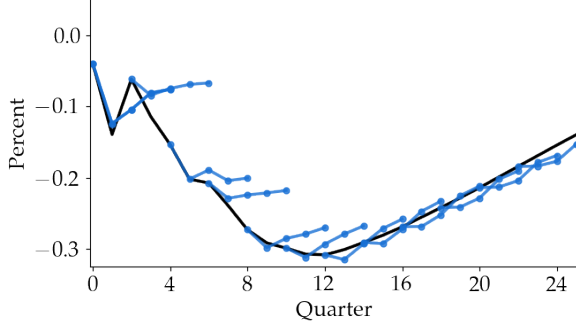
The lower panel of Figure 1 displays the impulse responses of CPI inflation and the nominal federal funds rate, the two variables used to construct our real interest rate measure. From these responses, we see that the majority of the decline in real interest rates is driven by elevated CPI inflation. The literature on the real effects of oil price shocks point to the central role of contractionary response of systematic monetary policy (Bernanke et al. 1997, Gagliardone and Gertler 2023). However, the response of the nominal federal funds rate in our limited sample period beginning in 1985 is relatively muted compared to these papers, whose sample periods typically extend back to the early 1970s.

The blue lines extending outward from the realized impulse responses of each variable represent the impulse response of expectations across horizons, a useful way to visualize the bias in expectations across the term structure as shown in Bardóczy and Guerreiro (2023). To clarify interpretation, consider the definition of the impulse response across periods- ℓ of a horizon- h income expectation

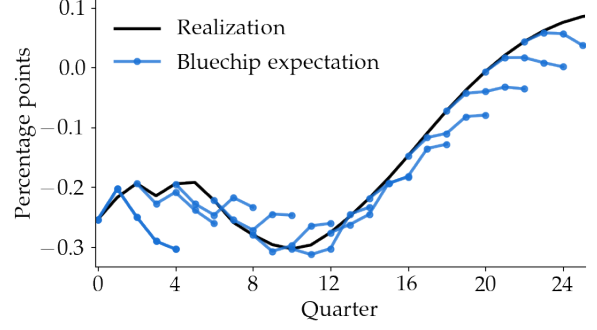
$$\Psi(E_t[Y_{t+h}]; \varepsilon_{t-\ell}) := \mathbb{E}[E_t[Y_{t+h}] | \varepsilon_{t-\ell} = 1] - \mathbb{E}[E_t[Y_{t+h}] | \varepsilon_{t-\ell} = 0] \quad (19)$$

where $\mathbb{E}[\cdot]$ is the unconditional expectation across time- t and the index ℓ denotes the periods elapsed between the shock onset and the time- t that expectations are formed. The blue line is given by fixing the elapsed period- ℓ since the shock and plotting expectations across horizons- h . This construction is interpretable as the average response of expectations across all horizons- h formed ℓ -periods after an initial shock.

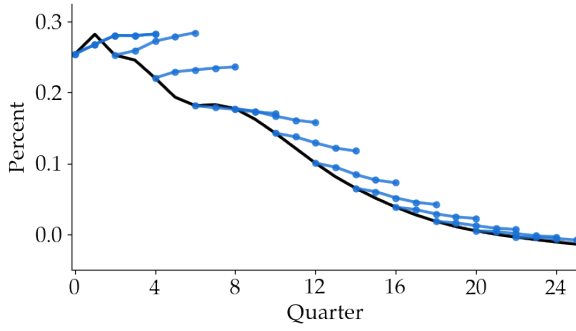
I proceed to analyze the systematic patterns of ex-post forecast errors in the expectations data shown in Figure 1 and consider whether they can be explained by existing models of expectation formation. To do so it is useful to consider the behavior of subjective expectations if they were formed under full-information rational expectations with respect to a hypothetical equilibrium economy. Let us define full-information to mean either $\varepsilon_{t-\ell}$ is directly public



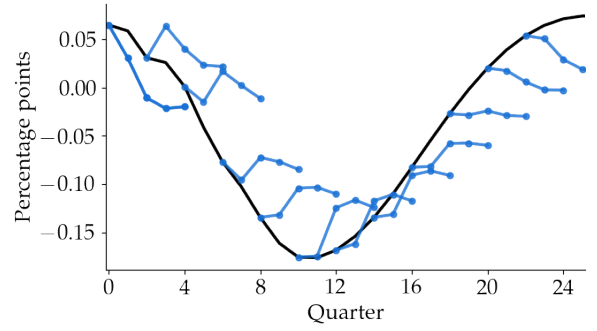
(a) Real Disposable Income



(b) Real Federal Funds Rate



(c) Consumer Price Inflation



(d) Nominal Federal Funds Rate

Figure 1: Impulse responses of realizations and Bluechip survey expectations

Note: each panel contains an impulse response function of realizations (black) to a positive [Känzig \(2021\)](#) oil price news shock. Each expectation “hair” (blue) collects quarter- ℓ impulse response coefficients of Bluechip survey expectations for horizons $h = 1, \dots, 4$ quarters ahead. The real federal funds rate is the nominal federal funds rate deflated by consumer price inflation.

information as of time- $t - \ell$, or that $\varepsilon_{t-\ell}$ is measurable in (invertible from) the set of publicly-observed time- $t - \ell$ variables in the economy. Assuming the equilibrium state variables are jointly stationary, the law of iterated expectations applies to Equation (19) and yields

$$\Psi(Y_{t+h}; \varepsilon_{t-\ell}) := \mathbb{E}[Y_{t+h} | \varepsilon_{t-\ell} = 1] - \mathbb{E}[Y_{t+h} | \varepsilon_{t-\ell} = 0], \quad \forall \ell, h \geq 0$$

In words, the impulse response of the horizon- h expectation conditional on an ℓ -period past shock should equal the realization impulse response in the horizon period h . Given this, we can interpret the vertical gaps between the black and blue lines in Figure 1 as suggestive evidence that expectations deviate from the full-information rational expectations assumption.

Many theories of bounded rationality result in subjective expectations that systematically under- or over-react relative to the full-information rational expectations benchmark. Systematic under-reaction corresponds to expectation “hairs” (blue) that extend from the realization (black) always remaining closer to zero than the realization. Over-reaction conversely has the “hairs” remaining further from zero than the realization.

Theories of systematic under-reaction, such as sticky information ([Mankiw and Reis 2002](#)) or cognitive discounting ([Gabaix 2020](#)), are unable to explain the over-reaction of measured expectations to certain variables, such as the response of CPI inflation expectations in Figure 1d. Conversely, while theories of systematic over-reaction, such as diagnostic expectations ([Bordalo et al. 2018](#)), can explain the response of CPI inflation, they are unable to match the initial under-reaction of real disposable income expectations displayed in Figure 1a. [Angeletos et al. \(2021\)](#) and [Bardóczy and Guerreiro \(2023\)](#) convey this point as well, documenting similar patterns in impulse responses from the Survey of Professional Forecasters for other variables and shocks.

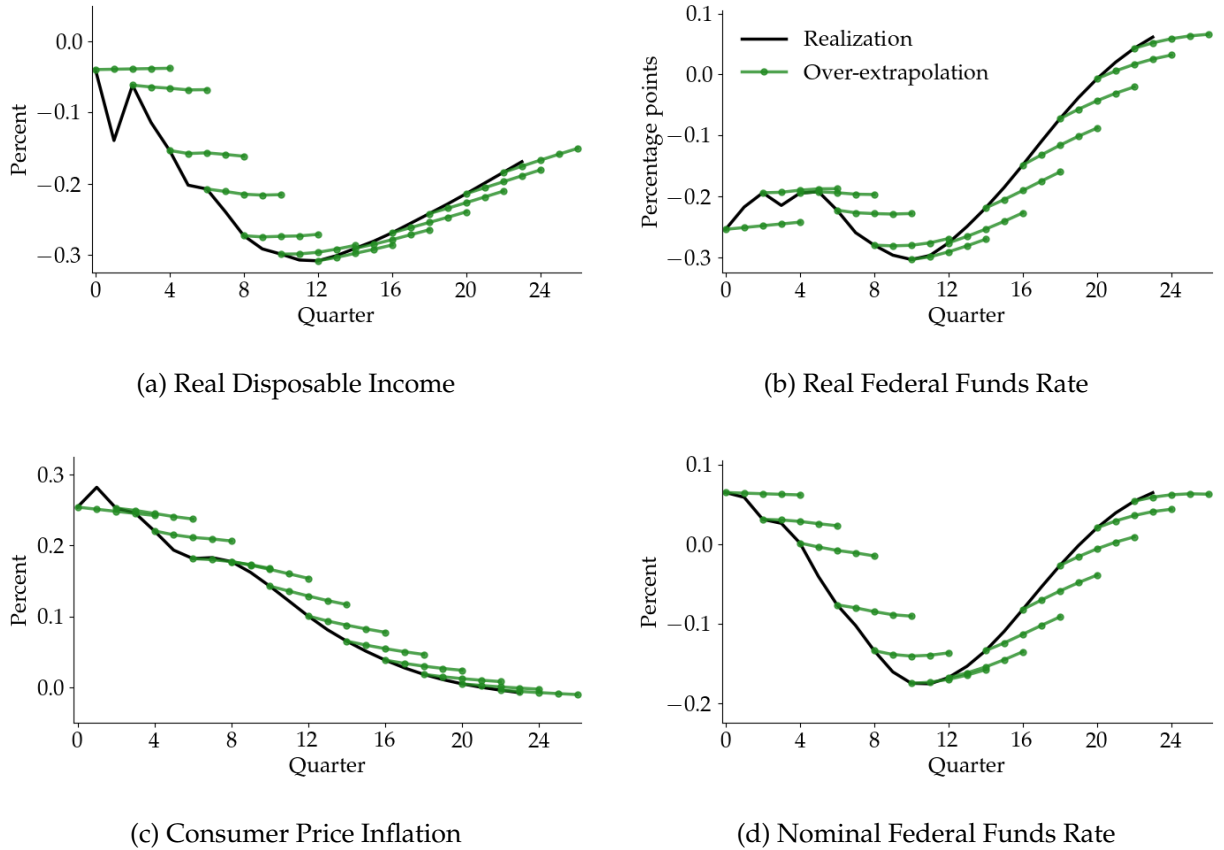


Figure 2: Impulse responses of realizations and parametric “over-extrapolation” expectations

Note: each panel contains an impulse response function of realizations (black) to a positive [Känzig \(2021\)](#) oil price news shock. Each expectation “hair” (red) collects quarter- ℓ impulse response coefficients of the parametric “over-extrapolation” model for horizons $h = 1, \dots, 4$ quarters ahead. The real federal funds rate is the nominal federal funds rate deflated by consumer price inflation.

While it is difficult to summarize these biases solely as systematic under- or over-reaction relative to the full-information rational expectation, they can however be rationalized as over-extrapolation of the most recent realization. I demonstrate this with an illustrative two-parameter model fit across all variables, time- ℓ and horizons- h . The model parameterizes the impulse re-

sponse (IR) of subjective expectations $\Psi(E_t[Y_{t+h}], \varepsilon_{t-\ell})$, in the following way

$$\Psi(E_t[Y_{t+h}], \varepsilon_{t-\ell}) = \omega^\ell \theta^h \underbrace{\Psi(Y_t, \varepsilon_{t-\ell})}_{\text{Extrapolation IR}} + (1 - \omega^\ell) \underbrace{\Psi(Y_{t+h}, z_{t-\ell})}_{\text{Full-information rational expectation IR}}$$

The parameter θ determines the persistence of extrapolation from the current observation across expectation horizons- h and ω determines how long this bias lasts across response periods- ℓ . The parameter $\omega \in (0, 1)$ ensures that extrapolation bias will eventually diminish and expectations will converge back to the rational benchmark as time- ℓ progresses.

Figure 2 displays the impulse response of expectations implied by this simple over-extrapolation model, which replicates Figure 1 quite well. This observation motivates my later adoption of a Bayesian learning model that exhibits a similar form of over-extrapolation bias.

In addition to the fitted model producing Figure 2, I consider a battery of other simple parametric models fit to the same data to extrapolate missing horizons. One could view the use of these models to extrapolate missing horizons as shape restrictions on expectational impulse responses across horizons- h , as the simple parametric model I fit demonstrates. As a baseline, I use an estimated AR(2) process, constrained to be stationary, to extrapolate missing horizons. The results in the following section on consumption function estimation are robust to alternate choices. Details for the choice of auxiliary models for extrapolation, their estimation, and resulting structural parameter estimates are in Appendix A.

3.5 Empirical vs. model-implied impulse responses of consumption

The expectation impulse responses plotted in Figure 1 correspond to the impulse response estimands reported in the model-implied consumption moment condition (15). Figure 3 displays the model-implied impulse responses of consumption from the estimated representative-agent, perpetual youth overlapping generations, and standard incomplete markets models. Recall these models only have one or two structural parameters to be used as degrees of freedom for estimation across numerous impulse response periods. The elasticity of intertemporal substitution σ is estimated across all models, and the hazard rate ω , which allows for heightened income sensitivity of consumption, is additionally estimated for the perpetual youth model.

My baseline estimates for the elasticity of intertemporal substitution (EIS) across models are low. For the representative-agent benchmark the estimated EIS approaches zero, while for the heterogeneous-agent models the estimated EIS is around 0.1. The main intuition stems from observing in Figure 1b that realized and expected real interest rates decline in response to the oil price shock. The estimated EIS is pushed downward to mitigate the positive intertemporal substitution response of model-implied consumption and amplify the negative income effects from lower rates.

One key reason why the estimated EIS is low across all models is that the magnitude of the observed decline in consumption to this shock exceeds that of disposable income. Hence, for model-implied consumption to match the observed decline, negative income effects from interest rates must be sufficiently large.

While an EIS estimate of 0.1 is low it is not unprecedented. In a quasi-experimental setting, [Best et al. \(2020\)](#) exploit borrower bunching behavior around loan-to-value thresholds used to price mortgages and also find an estimated EIS of 0.1. Likewise, [Ring \(2024\)](#) finds evidence for a

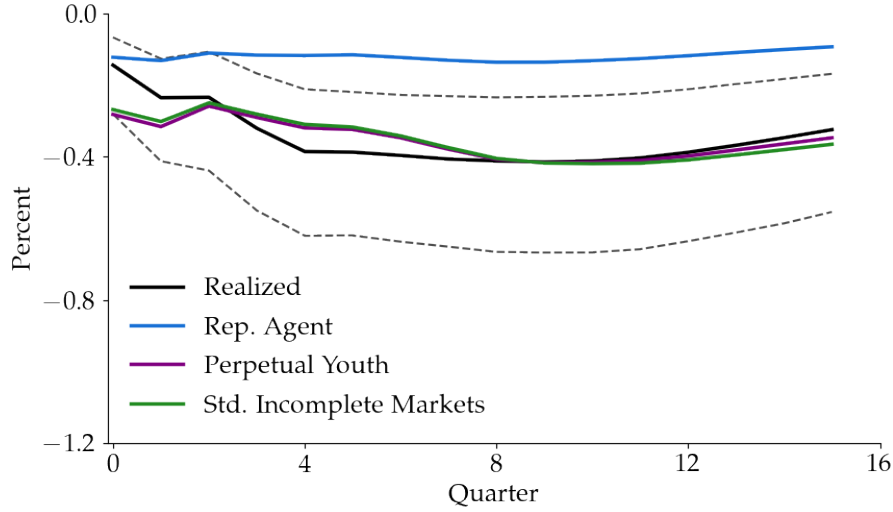


Figure 3: Model-implied consumption impulse responses

Note: the realized (black) consumption impulse response and model-implied consumption impulse responses to a positive [Känzig \(2021\)](#) oil price news shock. Model-implied responses are produced by evaluating each models consumption function using empirical impulse responses of realized and expected income and interest rates. The dashed lines are 68% confidence bands produced using moving block bootstrap by [Jentsch and Lunsford \(2019\)](#).

similarly low EIS using Norwegian administrative data and geographic variation to investigate the relative size of substitution and income effects of wealth taxation on savings behavior.

Recall that most of the decline in the real interest rate from the oil price shock is due to the increase in realized and expected inflation. One concern might be that forecasters' inflation expectations respond differently than household expectations due to this shock. Figure 7 of [Känzig \(2021\)](#) provides suggestive evidence that the magnitude of households' inflation expectation responses to oil shocks may be larger than that of forecasters'. However, this would imply an even lower expected real rate taking account of household expectations reinforcing the need for a low estimated EIS.

The income sensitivity of consumption, as measured by the current marginal propensity to consume (MPC) out of unearned income, is small in the representative-agent model by construction. In contrast, heterogeneous-agent models can have substantially higher MPCs, and indeed I find this to be the case in this estimation. The estimated hazard rate for the perpetual youth model implies an MPC of approximately five percent at a quarterly frequency. While the standard incomplete markets model did not have an independent degree of freedom from the EIS to estimate, due to the discount factor being used to target the steady-state level of assets, its estimated MPC matches that of the perpetual youth model at five percent. As Figure 3 demonstrates, the higher MPC in the heterogeneous-agent models proves crucial to match the pronounced consumption contraction due to the oil shock. Due to the much longer effective horizons for income smoothing, the representative-agent models' response to the shock is less severe.

| Consumption-Savings Models | | | |
|---------------------------------------|-----------------|-----------------------------|------------|
| Parameter | Perpetual Youth | Standard Incomplete Markets | Rep. agent |
| EIS | 0.08 | 0.09 | 0.00 |
| MPC | 0.04 | 0.05 | 0.005 |
| $\frac{\text{Assets}}{\text{Income}}$ | 1.4 | 1.4* | 1.4 |
| EIS | 0.80 | 0.05 | - |
| MPC | 0.2* | 0.2* | - |
| $\frac{\text{Assets}}{\text{Income}}$ | 1.4 | 0.425 | - |

Table 3: Estimated/targeted parameters from consumption-savings models

Note: The top panel contains estimated parameters enforcing that the steady state assets-to-income ratio is equal to the initial calibration target. The bottom panel contains estimated parameters when models instead target a higher marginal propensity to consume (MPC). The EIS σ is the elasticity of intertemporal substitution. MPC and income are reported at a quarterly frequency.

MPCs in micro-calibration versus macro-estimation It is well-known that the standard incomplete markets model is unable to simultaneously match typical microeconomic estimates of the current MPC and the steady state level of household assets (Kaplan and Violante 2022). By restricting the estimated model to match the latter, I attain an implied MPC of around 0.05 at a quarterly frequency, which is lower than typical microeconomic estimates which range from 0.15 to 0.25. However, this MPC that is consistent with our targeted macroeconomic impulse responses and has been shown to be consistent with a broader range of macroeconomic moments in full-information HANK estimation on macroeconomic time series Bayer et al. (2024).

I consider how calibrating the MPC in both the perpetual youth and standard incomplete markets models to 0.2, in line with microeconomic evidence, affects their implied impulse response fit. In the standard incomplete markets model I calibrate the discount factor β to now match the MPC target. While the fit deteriorates, as shown in Figure 4, they both still remain within a one standard deviation bound of the empirical impulse response of consumption. However, the estimated parameters for the EIS now diverge between these models. The estimated EIS is an order of magnitude larger in the perpetual youth model, while in the standard incomplete markets model it is slightly lower. In addition, the perpetual youth model now overshoots the empirical response, whereas the standard incomplete markets model undershoots.

To explain the reason for this change, consider an important difference between these two models: given the linearization in aggregates, the perpetual youth model lacks a precautionary savings motive. Recall in the perpetual youth model that the steady state level of assets is independent of the MPC. Therefore, changing the EIS only scales the relative size of the substitution versus income effects in response to the discounted value of expected interest rate changes, as shown in Equation (17). Given the large, prolonged decline in realized and expected real interest rates in response to the shock shown in Figure 1, higher MPCs in the perpetual youth model at the original, lower EIS estimate would have excessively amplified the negative income effect from lower rates.

The standard incomplete markets model requires a lower discount factor to attain a high MPC, which in turn reduces steady state asset demand because agents are less patient. Whether

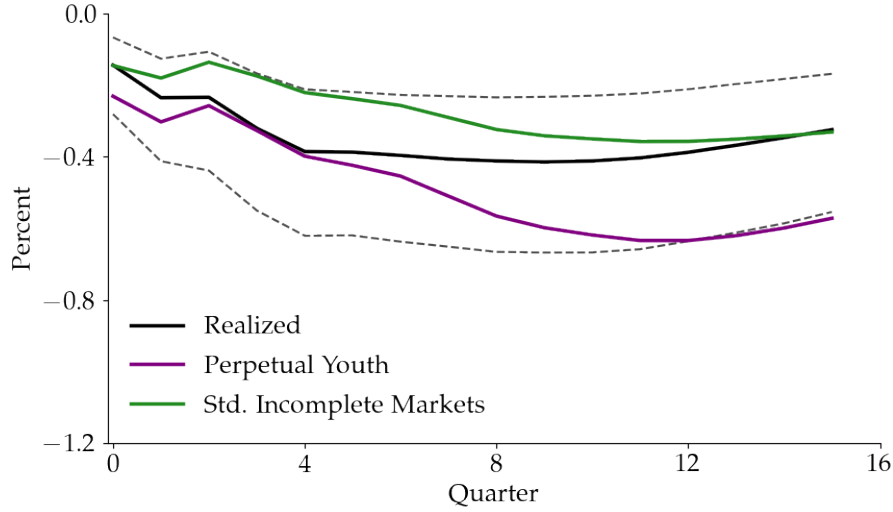


Figure 4: Model-implied consumption impulse responses, matching micro MPCs

Note: the realized (black) consumption impulse response and model-implied consumption impulse responses to a positive [Känzig \(2021\)](#) oil price news shock. Model-implied responses are produced by evaluating each models consumption function using empirical impulse responses of realized and expected income and interest rates. The dashed lines are 68% confidence bands produced using moving block bootstrap by [Jentsch and Lunsford \(2019\)](#).

the net effect of a higher MPC and a lower stock of steady state assets contributes positively to the magnitude of interest rate income effects is a quantitative question. In this case, the effect of the lower stock of steady state assets on interest rate income effects outweighs that of the heightened MPC. This then requires the EIS to be lowered further, increasing the level of steady state assets due to precautionary savings, which maintains the large negative income effect from lower rates.

Because I directly use the canonical standard incomplete markets model, I cannot resolve the fundamental tension between these parameter calibrations. Nonetheless, I show in the above figures that conditioning directly on expectations data, the model is similarly able to rationalize the observed inertia in aggregate consumption.

Full-information, rational expectations comparison It is natural to consider how model-implied consumption responses may differ in comparing those using expectations data with those formed via full-information, rational expectations (FIRE). However, without the complete specification of an equilibrium model we are not able to consider this counterfactual because of the Lucas critique. Suppose we observed the response of consumption to an identified shock occurring in an equilibrium economy where expectations exhibited a form of bias encapsulated by expectations data. We should not then expect the equilibrium dynamics of realized real income and interest rates to remain the same under a counterfactual model of expectation formation.

In Section 3.4, we could directly assess the validity of the FIRE assumption by making relative comparisons of average expectations and realizations. Here, however, we are unable to consider the counterfactual implications of full-information rational expectations versus data-

based expectations without understanding how it changes the data-generating process of realizations themselves. Given this, I proceed by adding structure in the form of a model of expectation formation informed by the data and an equilibrium environment to understand the joint determinants of observed expectations biases and consumption inertia.

4 An Equilibrium Macroeconomic Model with Inertia

In this section, I develop a theory for how inertia arises endogenously within a heterogeneous-agent New Keynesian (HANK) equilibrium model. I begin by defining the temporary equilibrium, given subjective expectations in a standard HANK environment, and consider the features of expectations that are required for inertia to arise. I then proceed to adopt a form of frictional Bayesian learning as my model of expectation formation. I demonstrate how the interactions between learning frictions and the core features of HANK — high income sensitivity and low interest rate sensitivity of consumption demand — play a key role in generating macroeconomic inertia.

4.1 Temporary equilibrium definition

I begin by defining a temporary equilibrium, an intermediate step toward a fully-specified general equilibrium that does not yet place restrictions on how forward-looking agents form expectations. As in [Woodford \(2013\)](#), I immediately resort to using the linearized equilibrium⁶, whose level deviations are given by time-indexed variables, e.g. C_t , around a non-stochastic steady state, whose notation is given by non-time-indexed variables, e.g. C .

The equilibrium environment closely follows [Angeletos et al. \(2023\)](#), although I simplify along a few dimensions that are not central to my analysis. I briefly discuss the shared equilibrium ingredients, such as the firm problem, policy rules, and market clearing conditions and elaborate only on my points of departure.

Households and firms I use the [Angeletos et al. \(2023\)](#) specification of the perpetual youth overlapping generations model, resulting in the earlier-estimated consumption function in Equation (17).

Labor unions intermediate labor markets, ensuring households supply an identical quantity of labor and equalizing the real wage and the average marginal rate of substitution between consumption and labor supply. Households therefore receive the identical labor income. Firm production follows the textbook New Keynesian model ([Galí 2015](#)), where identical monopolistically-competitive firms operate a linear-in-labor production technology and face Calvo price-setting frictions. This gives rise to an aggregate price inflation New Keynesian Phillips curve linearized around a zero-inflation steady state.

$$\pi_t = \kappa Y_t + \beta E_t[\pi_{t+1}] \quad (20)$$

Firms distribute dividends identically, ensuring households receive the same profit income.

⁶The consumption functions written earlier are in level as opposed to log deviations. To maintain this notation, I normalize steady state output $Y = 1$ such that level and log deviations for the below-defined variables can be interpreted identically.

Policy and market clearing The real interest rate is determined by the real Taylor rule

$$i_t - E_t[\pi_{t+1}] \equiv r_t = \phi Y_t \quad (21)$$

The monetary authority sets nominal interest rates accounting for the equilibrium consequences on subjective inflation expectations E_t to achieve a real interest rate target of ϕY_t . As discussed in Auclert et al. (2024), a rule of this form allows the monetary authority to conduct policy as if it maintained direct control of the ex-ante real interest rate. Adopting this rule therefore allows us to focus on the equilibrium determination of household consumption as a function of real interest rates without needing to separately account for the dynamics of subjective inflation expectations.

Market clearing in the goods market is given by

$$C_t = Y_t \quad (22)$$

Definition 2. A (linearized) **temporary equilibrium** consists of sequences of prices $\{i_t, \pi_t\}$ and quantities C_t, Y_t that satisfy (17), (20), (21), (22) for all periods t , given subjective expectations of $\{E_t[Y_{t+h}], E_t[\pi_{t+h}], E_t[i_{t+h}]\}_{h>0}$.

Assets are in zero net supply so households hold zero wealth in equilibrium.

4.2 General equilibrium dynamics with Bayesian learning

Closing the temporary equilibrium defined in Section 4.1, I assume households form expectations with a particular class of Bayesian learning models. These models have been shown to be consistent with multiple dimensions of evidence on expectation formation, including in the cross-section of households (Nagel 2024), experiments (Afrouzi et al. 2023), and unconditional time-series (Farmer et al. 2024, Crump et al. 2023).

In these models, Bayesian agents observe variables such as output or interest rates, understanding them to be driven by unobserved shocks that each are the sum of a transitory and a persistent component⁷. Because they cannot immediately distinguish these components, they gradually update their beliefs about them by solving a filtering problem given the time series of observed variables.

I assume that the only exogenous shock in the baseline economy is a demand shock ε_t , which is the sum of two unobserved mean-zero AR(1) components

$$\varepsilon_t = \lambda_t + \eta_t$$

with persistence parameters $\rho_\lambda > \rho_\eta$ and mean-zero Gaussian i.i.d innovations with variances $\sigma_\lambda^2, \sigma_\eta^2$. I refer to λ_t as the “persistent” component, due to its higher persistence, and η_t as the “transitory” component. I assume household have common knowledge of the functional form of the demand shock and the values of its parameters.

What remains to be specified is how agents draw inference about the underlying shock

⁷Some of the cited literature adopt the convention that the persistent component is a non-stochastic, long-run mean parameter, which agents are nonetheless uncertain about. The inference problem is similar to the case I study here and results in similar forms of over-extrapolation that lie at the core of my analysis.

components λ_t, η_t from observing variables Y_t, π_t, i_t . Define the perceived laws of motion of Y_t, π_t, i_t as a set of stochastic variables $\tilde{Y}_t, \tilde{\pi}_t, \tilde{i}_t$, which are also linear functions of the histories of the unobserved components $\{\lambda_{t-\ell}, \eta_{t-\ell}\}_{\ell \geq 0}$. However, I permit the perceived laws to differ from the actual laws of motion, that is, the coefficients⁸ on their component histories $\{\lambda_{t-\ell}, \eta_{t-\ell}\}_{\ell \geq 0}$ may differ.

Subjective expectations are evaluated with respect to the perceived laws of motion. For example, if $\tilde{Y}_t = \lambda_t + \eta_t$ then expected one-period ahead output is given by

$$E_t[Y_{t+1}] = E_t[\lambda_{t+1}] + E_t[\eta_{t+1}]$$

Agents' beliefs can be represented by the following state-space model with the AR(1) coefficients collected in the diagonal matrix \mathbf{F} and the perceived law of motion coefficients collected in the lag⁹ polynomial matrix $\tilde{\mathbf{A}}(L)$

$$\begin{bmatrix} \lambda_{t+1} \\ \eta_{t+1} \end{bmatrix} = \mathbf{F} \begin{bmatrix} \lambda_t \\ \eta_t \end{bmatrix} + \begin{bmatrix} u_{\lambda,t+1} \\ u_{\eta,t+1} \end{bmatrix}, \quad \begin{bmatrix} \tilde{Y}_t \\ \tilde{\pi}_t \\ \tilde{i}_t \end{bmatrix} = \tilde{\mathbf{A}}(L) \begin{bmatrix} \lambda_t \\ \eta_t \end{bmatrix}$$

Due to linearity and normality of innovations, the subjectively optimal state estimates, conditional on the perceived state-space model and past observations, are given by the Kalman update equation

$$\begin{bmatrix} E_t[\lambda_{t+1}] \\ E_t[\eta_{t+1}] \end{bmatrix} = \mathbf{F} \begin{bmatrix} E_{t-1}[\lambda_t] \\ E_{t-1}[\eta_t] \end{bmatrix} + \mathbf{G} \begin{bmatrix} Y_t - E_{t-1}[Y_t] \\ \pi_t - E_{t-1}[\pi_t] \\ i_t - E_{t-1}[i_t] \end{bmatrix}$$

where \mathbf{G} is the steady-state Kalman gain implied by the agents' perceived state-space model.

I make the typical learning assumption that the information set for time- t decisions determining equilibrium Y_t, π_t, i_t is the history of past observables $\{Y_{t-\ell}, \pi_{t-\ell}, i_{t-\ell}\}_{\ell \geq 1}$. To reflect this staggered timing, subjective expectations that inform time- t decisions are labeled E_{t-1} .

If the perceived and actual laws of motion differ, $E_{t-1}[Y_t]$ will be a sub-optimal forecast for Y_t , even though it is perceived to be optimal. Distorted component expectations $E_{t-1}[\lambda_t], E_{t-1}[\eta_t]$ are reinforced over time as decisions based on them determine future observables Y_t, π_t, i_t that are used for future inference to update component expectations $E_t[\lambda_{t+1}], E_t[\eta_{t+1}]$ and so on.

Definition 3. A **learning equilibrium** is a temporary equilibrium and a collection of subjective expectations $\{E_t[Y_{t+h}], E_t[\pi_{t+h}], E_t[i_{t+h}]\}_{h \geq 0}$ induced by a perceived law of motion $\tilde{Y}_t, \tilde{\pi}_t, \tilde{i}_t$ and past observations $\{Y_{t-\ell}, \pi_{t-\ell}, i_{t-\ell}\}_{\ell \geq 1}$.

To greatly simplify the model I proceed by assuming the perceived law of motion $\tilde{Y}_t, \tilde{\pi}_t, \tilde{i}_t$ is consistent with the policy rule (21). This allows us to isolate the equilibrium determination of output, which will be the focus of the remainder of the paper, from inflation and nominal

⁸I do not consider subjective uncertainty over and learning of the coefficients of the perceived law of motion itself, which is the subject of a separate literature on equilibrium learning. I assume the coefficients of the perceived law of motion are constant.

⁹If there are lag terms, then the backward-looking expectations of lagged components, e.g. $E_{t-1}[\lambda_{t-\ell}]$ for $\ell > 1$, can be computed using the Kalman smoother. This contrasts with the simple case $\tilde{Y}_t = \lambda_t + \eta_t$ discussed above, where forward-looking component expectations, e.g. $E_t[\lambda_{t+1}]$, can be computed using the Kalman filter.

interest rates. Consequently because it is commonly understood that these variables are determined by output, they provide no additional information about the components λ_t, η_t . Hence, we can treat realized output Y_t as the only observable variable agents learn from.

Consolidating equilibrium conditions into a simple aggregate demand equation, I obtain

$$Y_t \propto (1 - \beta\omega - \beta\omega\sigma\phi) \sum_{h=1}^{\infty} (\beta\omega)^h E_t[Y_{t+h}] + \varepsilon_t$$

Note that Y_t is not equal to the right-hand side because of the within-period general equilibrium feedback of Y_t, r_t . The constant of proportionality that I have omitted, $\beta\omega(1 + \sigma\phi)$, only affects the overall level of Y_t and not the shape of its impulse response to ε_t across periods. In the following sub-sections I focus on characterizing the shape and not the overall level of impulse responses. Therefore, without loss of generality, I normalize the variance of ε_t by $(\beta\omega(1 + \sigma\phi))^2$ and proceed using Equation (23) with equality. When considering policy counterfactuals in Section 5 I undo this normalization to ensure the level contribution of counterfactuals is properly accounted for.

Let $\chi := (1 - \beta\omega - \beta\omega\sigma\phi)$ and permanent income $\mathcal{Y}_t := \sum_{h=1}^{\infty} (\beta\omega)^h E_t[Y_{t+h}]$. Re-writing the aggregate demand equation we obtain the following simple expression for equilibrium output.

$$Y_t = \chi \mathcal{Y}_t + \varepsilon_t \quad (23)$$

Informally, we can see that if ε_t does not exhibit inertia in the form of hump-shaped impulse responses then for Y_t to exhibit inertia \mathcal{Y}_t must exhibit inertia and χ must be sufficiently large such that Y_t inherits its inertia. Given \mathcal{Y}_t is the variable that summarizes the effect of future output beliefs on current realized output, I will refer to χ as the *belief multiplier*. To formalize this intuition, I proceed by considering concrete examples of perceived laws of motion to demonstrate how output inertia Y_t arises endogenously due to the effects of the shock on the evolution of beliefs.

4.3 Simple learning

As before, suppose households' perceived law of motion of output is given by the simple form

$$\tilde{Y}_t = \lambda_t + \eta_t \quad (24)$$

This perceived law of motion means households completely disregard the general equilibrium feedback of the shock when forming expectations of future output. Whenever they observe a given output realization, they simply assume it was due to direct changes in the underlying shock components. While this assumption is stark, it is useful to illustrate the consequences of perceived laws of motion which do not fully account for general equilibrium feedback. The kinds of distortions these mistaken beliefs impart on realized output dynamics will carry over to more sophisticated but still imperfect beliefs and will serve as a useful example to compare to the rational learning benchmark.

With this perceived law of motion, permanent income takes the form

$$\mathcal{Y}_t = \frac{\beta\omega\rho_\lambda}{1 - \beta\omega\rho_\lambda} E_{t-1}[\lambda_t] + \frac{\beta\omega\rho_\eta}{1 - \beta\omega\rho_\eta} E_{t-1}[\eta_t]$$

With $\rho_\lambda > \rho_\eta$ the same-sized belief update of $E_{t-1}[\lambda_t]$ raises expected future income \mathcal{Y}_t by more than a comparable change in $E_{t-1}[\eta_t]$ because it corresponds to the belief that future income $\{E_t[Y_{t+h}]\}_{h>1}$ will be persistently higher. I denote the effective horizon of the persistent component belief as $h_\lambda := \frac{\beta\omega\rho_\lambda}{1-\beta\omega\rho_\lambda}$ and likewise for the transitory component $h_\eta := \frac{\beta\omega\rho_\eta}{1-\beta\omega\rho_\eta}$.

The equilibrium dynamics of output can be represented as a system of two equations. The first is the aggregate demand equation for output derived from Equation (23) given component expectations. The second is the law of motion of component expectations, as a function of the output forecast error $Y_t - E_{t-1}[Y_t]$.

$$Y_t = \underbrace{\chi \mathbf{h} E_{t-1}[\boldsymbol{\varepsilon}_t]}_{\text{Belief feedback}} + \underbrace{\mathbf{1} \boldsymbol{\varepsilon}_t}_{\text{Direct shock effect}} \quad (25)$$

$$E_t[\boldsymbol{\varepsilon}_{t+1}] = \mathbf{F} E_{t-1}[\boldsymbol{\varepsilon}_t] + \mathbf{g}' \underbrace{(\chi \mathbf{h} E_{t-1}[\boldsymbol{\varepsilon}_t] + \mathbf{1}(\boldsymbol{\varepsilon}_t - E_{t-1}[\boldsymbol{\varepsilon}_t]))}_{\text{Forecast error } Y_t - E_{t-1}[Y_t]} \quad (26)$$

(Row) vector notation denotes the shock components $\boldsymbol{\varepsilon}_t := (\lambda_t, \eta_t)$, effective horizons $\mathbf{h} := (h_\lambda, h_\eta)$, $\mathbf{1} := (1, 1)$, autoregression persistences $\mathbf{F} := \text{diag}(\rho_\lambda, \rho_\eta)$, and steady-state Kalman gains $\mathbf{g} := (g_\lambda, g_\eta)$.

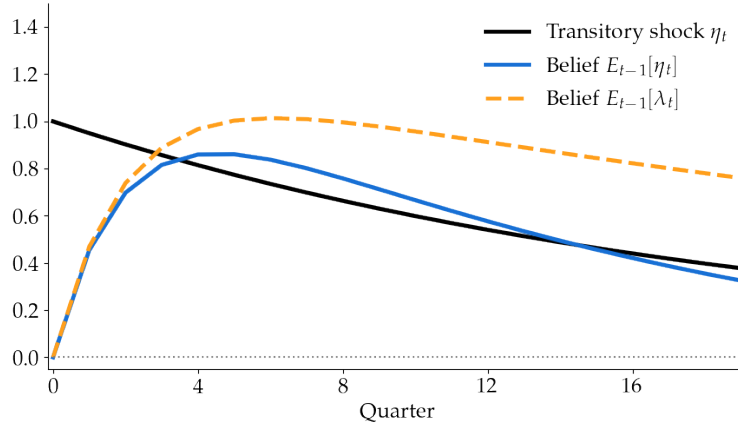


Figure 5: Component belief impulse responses to a transitory demand shock

Figure 5 shows the response of beliefs about the transitory and persistent components to a transitory shock. Even though no persistent shock occurred, beliefs about both components increase because observing output does not allow households to perfectly distinguish the components in the early onset of a shock. Due to gradual learning, we see the adjustment of component beliefs exhibit inertia in response to the shock.

A distinctive and important consequence of this simple perceived law of motion is the appearance of the belief feedback term $\chi \mathbf{h} E_{t-1}[\boldsymbol{\varepsilon}_t]$ in the evolution of component beliefs in Equation (26). This contrasts with the rational learning Kalman update that I consider in the next sub-section, where the output forecast error $Y_t - E_{t-1}[Y_t]$ is simply equal to the current shock relative to beliefs $\mathbf{1}(\boldsymbol{\varepsilon}_t - E_{t-1}[\boldsymbol{\varepsilon}_t])$. This belief feedback wedge appears precisely because households are unaware that equilibrium output is determined in part by their consumption decisions and not just the direct effect of the shock. By consuming based on their distorted

beliefs they alter equilibrium output, and by incorrectly updating after observing equilibrium output their beliefs become further distorted. I will refer to this self-reinforcing feedback loop as *expectations unanchoring*.

A high degree of belief feedback into output, relative to the direct effect of a shock, and component beliefs which unanchor and reinforce this feedback over time cause output Y_t to exhibit inertia as shown in Figure 6a. Because the initial shock was transitory but beliefs also update toward the persistent component, output expectations are overly persistent, exhibiting systematic forecast errors which diminish gradually with time. The combination of these features permit this model to jointly explain output inertia (equivalently consumption and income in this setting) and expectations that persistently over-extrapolate from the most recent observation, as documented in Section (3).

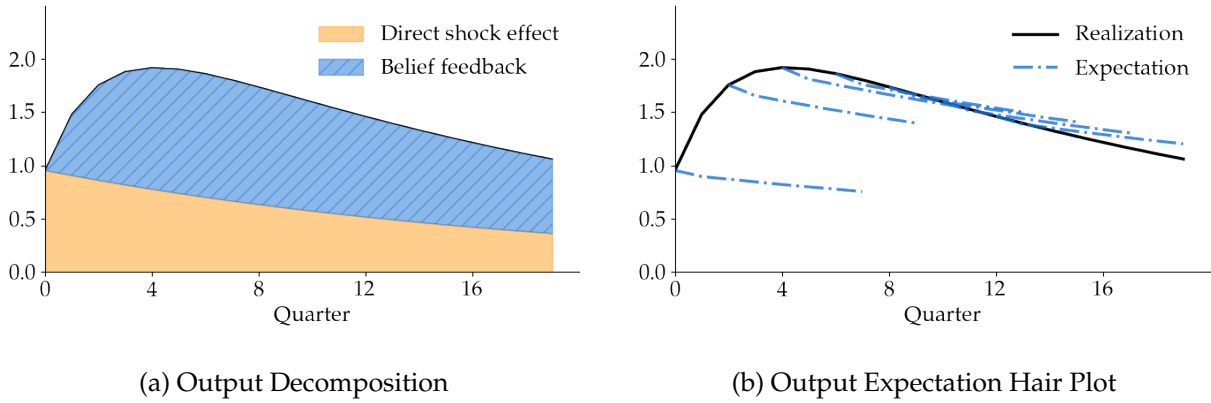


Figure 6: Output impulse response to a transitory demand shock

Note: The left panel decomposes the output impulse response to a transitory demand shock into the direct effect of the shock (gold solid) and the belief feedback effect (blue hatched) in Equation (25). The right panel expectation “hairs” (blue dot-dash) collect impulse response coefficients of quarter- ℓ subjective output expectations.

Inertia and the belief multiplier χ After displaying an example of inertia arising in the simple perceived law of motion above, I now formalize the intuition for why a high belief multiplier χ induces greater output Y_t inertia. This happens both because the multiplier χ scales the relative contribution of inertial component beliefs embedded in expected permanent income \mathcal{Y}_t and because it scales the belief feedback wedge that appears in the component belief law of motion, increasing the persistence of beliefs.

Definition 4. Let $X_t = \sum_{\ell=0}^{\infty} (a_{\ell}\lambda_{t-\ell} + b_{\ell}\eta_{t-\ell})$ denote the Wold representation of a variable X_t . X_t exhibits **inertia** with respect to a component shock $\lambda_{t-\ell}$ if its corresponding Wold coefficients $\{a_{\ell}\}$ are weakly increasing (decreasing) for $\ell \leq \bar{\ell} > 0$ and if $|a_{\ell}| \leq a_{\bar{\ell}}$ for $\ell > \bar{\ell}$. Denote the impulse response period $\ell = \bar{\ell}$ as the **inertial peak**. These definitions hold symmetrically for component shock $\eta_{t-\ell}$ and its coefficients $\{b_{\ell}\}$.

The above definition essentially states that a variable is inertial with respect to a shock if its maximal impulse response period, which I call the inertial peak, is not the initial shock period.

Proposition 1. For each component shock $e_t \in \{\lambda_t, \eta_t\}$ there corresponds an interval $(\underline{X}_e, \bar{X}_e)$ where if $\chi \in (\underline{X}_e, \bar{X}_e)$, Y_t will exhibit inertia and its inertial peak period $\bar{\ell}$ will be weakly increasing in χ .

This result demonstrates the tight connection between output inertia and the belief multiplier χ , where inertia results when the multiplier is large as demonstrated in Figure 7. Recall the form of the belief multiplier χ from the perpetual youth model

$$\chi := (1 - \beta\omega - \beta\omega\sigma\phi) \equiv (\text{MPC} - (1 - \text{MPC})\text{EIS}\phi)$$

It is useful to re-write the parameter values in terms of more interpretable quantities, namely the current marginal propensity to consume (MPC) and the elasticity of intertemporal substitution (EIS). We see that the multiplier χ is larger when MPC is high, which is the distinctive difference between heterogeneous-agent and representative-agent models of consumption, and when the EIS is low.

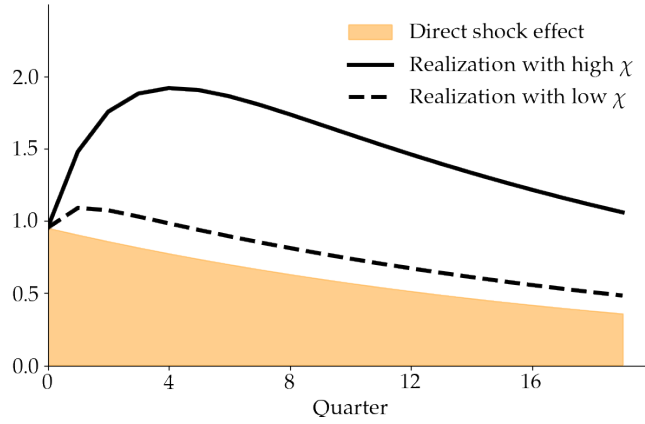


Figure 7: Output impulse responses under different belief multipliers χ

Note: The black solid and dashed lines represent the output impulse response under high and low belief multiplier calibrations. The direct shock effect (gold solid) is the same under both calibrations. The gap between the direct shock effect and the black solid and dashed lines represent the size of expectation feedback under each calibration.

The intuition of the lower thresholds for χ in Proposition 1 is the following. For output to exhibit inertia at all, the belief multiplier χ must be sufficiently large for the additional endogenous persistence in output Y_t contributed by the belief feedback term to exceed the exogenous decay of the direct shock effect. In other words, output inertia results when belief feedback is sufficiently amplified by χ .

The interval in which increasing χ prolongs output inertia, resulting in a further peak period, comes in part from identifying the range of parameters for which χ increases the eigenvalues of the belief component law of motion. The idea here is by increasing the multiplier χ and thus increasing the persistence of the component belief system, expectation feedback will be relatively longer lasting and contribute more to output inertia. Figure 8 demonstrates the responses of persistent and transitory component beliefs to a transitory shock in economies with different-sized belief multipliers χ .

While in the initial period the criteria for inertia to arise simply required the response of belief feedback to exceed the exogenous decay of the direct shock effect, for periods beyond the first the relevant comparison is whether the endogenous persistence of the persistent belief component $E_{t-1}[\lambda_t]$ exceeds the combined decay from the endogenous transitory belief

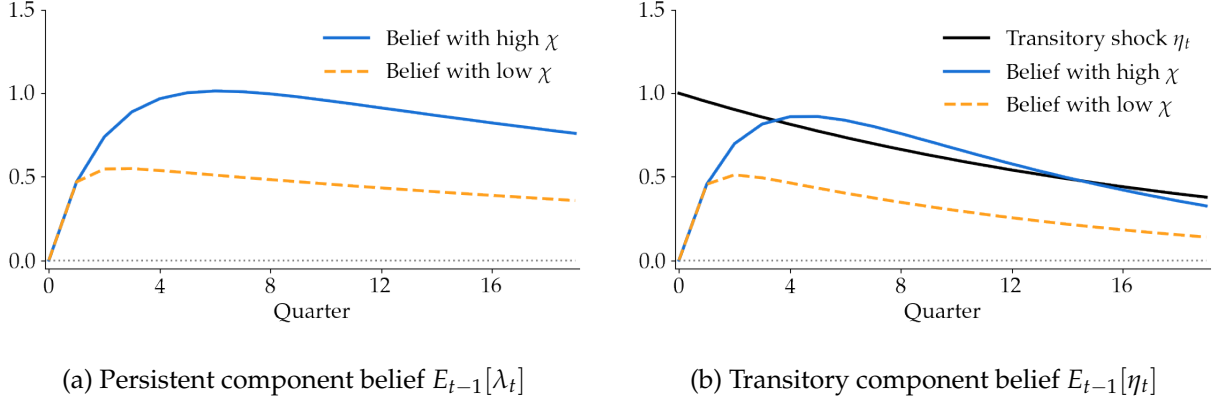


Figure 8: Component belief impulse responses under different belief multipliers χ

Note: The blue solid lines represent the impulse response of component beliefs to a transitory demand shock under a high belief multiplier calibration. The gold dashed line represent the analogous responses for a low belief multiplier calibration.

component $E_{t-1}[\eta_t]$ and the exogenous decay of the transitory shock η_t itself.

4.4 Rational and constrained-rational learning

This sub-section contrasts the simple perceived law of motion with more sophisticated beliefs and demonstrates that inertia may be absent in certain cases of learning and present in others. The first case I consider is rational learning, where the perceived and actual laws of motion coincide. With rational learning households are able to account for the equilibrium impacts of their decisions on their own expectations and hence optimally incorporate past observations of output into their component forecasts. The rational learning equilibrium solution yields

$$Y_t \equiv \tilde{Y}_t = \left(\frac{\chi}{1 - \beta\omega\rho_\lambda - \chi} E_{t-1}[\lambda_t] + \frac{\chi}{1 - \beta\omega\rho_\eta - \chi} E_{t-1}[\eta_t] \right) + \lambda_t + \eta_t \quad (27)$$

The second case, which I call “constrained-rational” learning, still restricts households’ beliefs to be functions of the contemporaneous components λ_t, η_t but permits their coefficients to be optimally estimated given their economic environment. This allows me to later consider policy counterfactuals that are robust to the Lucas critique within this class of models with imperfect learning, while still retaining similar limitations and implications as simple learning.

$$\tilde{Y}_t = \tilde{a}\lambda_t + \tilde{b}\eta_t$$

Given the Wold decomposition of output $Y_t = \sum_{\ell=0}^{\infty} (a_\ell u_{\lambda,t-\ell} + b_\ell u_{\eta,t-\ell})$, we can solve for the optimal coefficients \tilde{a}, \tilde{b} by projecting the constrained-rational perceived law of motion \tilde{Y}_t onto the actual one Y_t . Doing so obtains the following pair of implicit equations, which define \tilde{a}, \tilde{b} .

Lacking an analytical solution, I solve this fixed point numerically.

$$\begin{aligned}\tilde{a} &= (1 - \rho_\lambda^2) \sum_{\ell=0}^{\infty} \rho_\lambda^\ell a_\ell(\tilde{a}, \tilde{b}) \\ \tilde{b} &= (1 - \rho_\eta^2) \sum_{\ell=0}^{\infty} \rho_\eta^\ell b_\ell(\tilde{a}, \tilde{b})\end{aligned}$$

Let us now consider the differences between these three perceived laws of motion by analyzing their implications on agents' forward-looking reasoning. Suppose just for the present explanation that η_t is i.i.d so we can simplify exposition. Consider realized output at a future horizon- $h > 0$, which takes the general form

$$Y_{t+h} = \underbrace{(\alpha_1 \lambda_{t+h-1} + \alpha_2 \lambda_{t+h-2} + \alpha_3 \lambda_{t+h-3} + \dots)}_{\text{Belief feedback } \chi E_{t+h-1}[\lambda_{t+h}]} + \underbrace{\lambda_{t+h}}_{\text{Direct shock effect}}$$

Rational learning adopts this exact form and hence can fully account for the contributions of past and current shocks to time- $t + h - 1$ beliefs. The simple perceived law of motion is on the opposite extreme, only accounting for the direct shock effect in the perceived law of motion.

Constrained-rational learning constitutes a middle ground between these two cases. The state variable λ_{t+h} in the perceived law of motion \tilde{Y}_{t+h} cannot span the infinite history of past shocks $\{\lambda_{t+h-\ell}\}_{\ell>0}$, which appear from the Wold decomposition of the belief feedback $\chi E_{t+h-1}[\lambda_{t+h}]$. However, because λ_{t+h} is an autoregressive process it correlates with the past innovations $\{u_{\lambda,t+h-\ell}\}_{\ell>0}$ and consequently the past shocks $\{\lambda_{t+h-\ell}\}_{\ell>0}$ that determine time- $t + h - 1$ beliefs $E_{t-1}[\lambda_{t+h-\ell}]$. Hence the projection of these past innovations onto the shock λ_{t+h} allows \tilde{Y}_{t+h} to partially capture the dependence of beliefs of past shocks.

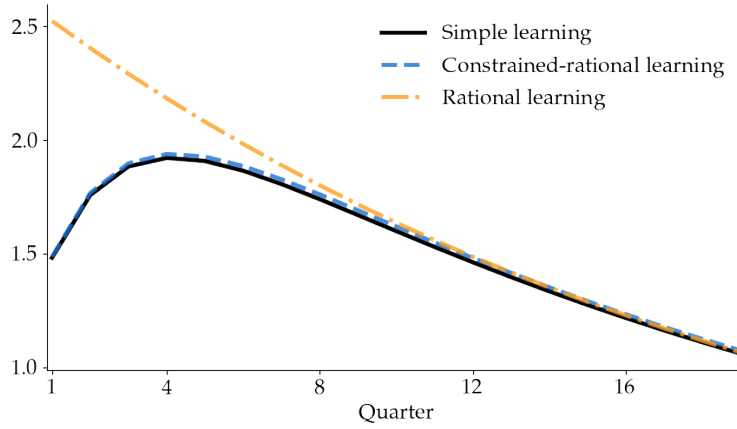


Figure 9: Output impulse responses under different forms of Bayesian learning

Note: Each line represents the impulse response of output to a transitory demand shock under different learning assumptions. I omit period zero because it does not contain an expectational response due to the staggered timing assumption.

Current output Y_t is determined by households who base their consumption spending on all future output expectations $\{E_{t-1}[Y_{t+h}]\}_{h>0}$. Because expectations of output at each

horizon- h imperfectly captures the history-dependence of belief feedback on past shocks, the constrained-rational and simple perceived laws of motion result in a significant degree of dampening in realized output Y_t due to this impairment in forward reasoning.

Figure 9 displays the response of output to a transitory shock under all of the previously described perceived laws of motion. The response of output under rational learning is immediate and monotonically decreasing, similar to a typical full-information rational expectations impulse response in a standard HANK model. Additionally, it is much larger than its imperfect learning counterparts because it accounts for the full set of dynamic general equilibrium expectation feedback effects. Interestingly, the response of output under constrained-rational learning is virtually indistinguishable from simple learning. I elaborate on this further after contrasting the responses of component beliefs.

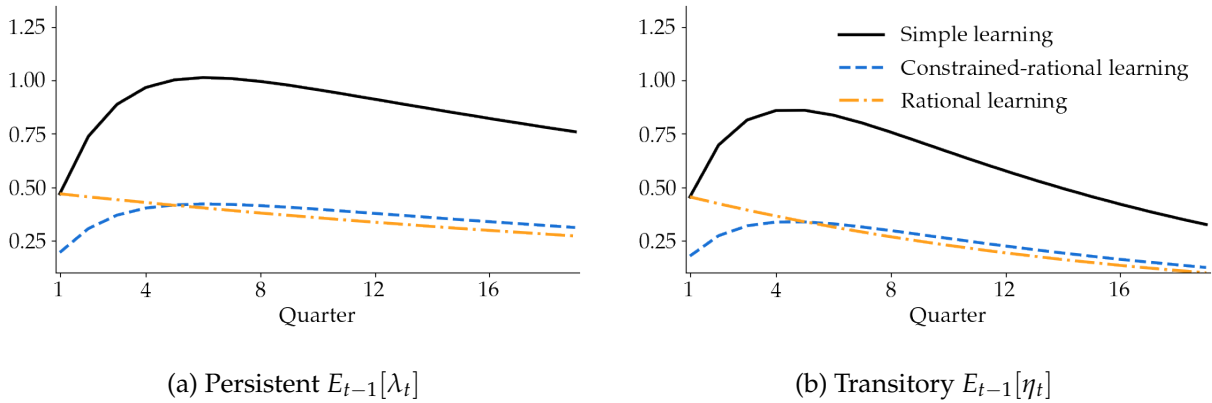


Figure 10: Component belief impulse responses under different forms of Bayesian learning

Note: Each line represents the impulse response of component beliefs to a transitory demand shock under different learning assumptions. I omit period zero because it does not contain an expectational response due to the staggered timing assumption.

While the output response is similar under imperfect learning, the behavior of component beliefs differ significantly. Figure 10 displays the responses of persistent and transitory component beliefs to a transitory shock. Under simple learning, all changes in output are inferred to be due to changes in the underlying shock components. The reinforcing feedback of component beliefs into equilibrium output unanchors expectations under simple learning relative to the other perceived laws of motion which partially account for this equilibrium feedback in their belief formation. In contrast, component beliefs under constrained-rational learning more closely resembles rational learning.

Why is the output response under constrained-rational learning more similar to simple learning, if its component beliefs are more similar to rational learning? To explain this, it is useful to consider the relative magnitude of the response of output to a given change in belief components. Contrasting simple and constrained-rational learning, we see that beliefs respond less under constrained-rational learning but deliver the same output response. As discussed previously, the degree of amplification of beliefs is much larger under constrained-rational learning because it accounts for some of the belief feedback. However, we see that the degree of amplification is still muted compared to rational learning which accounts for the full quantity of belief feedback.

The role of the belief multiplier χ Let us now consider how the belief multiplier χ affects the evolution of component beliefs in the rational and constrained-rational cases. In the rational case, the belief multiplier χ does not enter the component belief law of motion at all because there is no belief feedback wedge. The reason is expectations update optimally by accounting for belief feedback into equilibrium output irrespective of its size.

$$\mathbb{E}_t[\varepsilon_{t+1}] = \mathbf{F}\mathbb{E}_{t-1}[\varepsilon_t] + \mathbf{g}' \underbrace{(\mathbf{1}\varepsilon_t - \mathbb{E}_{t-1}[\varepsilon_t])}_{\text{Forecast error } Y_t - \mathbb{E}_{t-1}[Y_t]}$$

Given expectations $\mathbb{E}_{t-1}[\varepsilon_t]$ are predetermined and fully accounted for in the rational learning perceived law of motion, the steady state Kalman gain \mathbf{g} remains the same as in the simple learning case and is also unaffected by the multiplier χ .

Conversely, we see that in the constrained-rational case, the belief multiplier χ enters into the component belief law of motion resulting in a similar wedge to the simple learning case

$$\mathbb{E}_t[\varepsilon_{t+1}] = \mathbf{F}\mathbb{E}_{t-1}[\varepsilon_t] + \mathbf{g}' \underbrace{(\mathbf{1}\varepsilon_t + \tilde{\mathbf{a}} \odot (\chi\mathbf{h} - \mathbf{1})\mathbb{E}_{t-1}[\varepsilon_t])}_{\text{Forecast error } Y_t - \mathbb{E}_{t-1}[Y_t]}$$

where projection coefficients $\tilde{\mathbf{a}} := (\tilde{a}, \tilde{b})$ and \odot is the element-wise (Hadamard) product.

Because the projection coefficients, which are functions of the belief multiplier χ , directly load on the belief components λ_t, η_t in the constrained-rational perceived law of motion, the endogenous Kalman gains \mathbf{g} are now affected by χ . This intuition for this is as follows. Households do not explicitly account for belief feedback in their perceived law of motion. Nonetheless in estimating coefficients $\tilde{\mathbf{a}}$ on components λ_t, η_t to best fit the observed dynamics of output they partially pick up the influence of expectations feedback because λ_t, η_t are functions of past component innovations embedded in expectations. This appears to them as if output fluctuations are directly more sensitive to λ_t, η_t changes than just the unit direct shock effect would suggest, causing the endogenous gain \mathbf{g} to be lower when the multiplier χ is larger.

The differences in gains \mathbf{g} determine the difference in the initial period response of component beliefs in Figure 10. Even though the gain \mathbf{g} is lower in the constrained-rational case, which would suggest that output fluctuations should be less sensitive to changes in component beliefs, the projection coefficients $\tilde{\mathbf{a}}$ are typically larger when χ is larger, which goes in the opposite direction and amplifies the output response. On net these two forces cancel each other out, resulting in similar responses of output under simple and constrained-rational learning.

5 Policy implications of macroeconomic inertia

This section discusses novel policy considerations that arise under constrained learning and contrast them with typical policy transmission outcomes in full-information rational expectations HANK models. Under constrained learning, it is no longer desirable to be infinitely-responsive to demand-driven fluctuations because of the risk of destabilizing expectations. Gradual monetary policy approaches, in the form of a highly inertial Taylor rule, fail to stabilize output as effectively relative to the full-information rational expectations benchmark. The key reason is the inability of constrained learning to account for the future equilibrium impacts of current policy commitments. This channel also results in delayed amplification of

fiscal stimulus when debt repayment is slow.

5.1 Simple Taylor rules

The typical monetary policy prescription in response to demand shocks is to completely close the output gaps they induce, which aligns with the welfare aims of inflation stabilization in standard New Keynesian economies (Blanchard and Galí 2007). This divine coincidence will likewise hold in my setting, assuming firms expectations are the same as households. Therefore I use the discounted path of squared deviations of output from steady state as a simple welfare measure to contrast counterfactual policy rules, which do not affect the steady state.

$$\mathcal{L} = \sum_{t=0}^{\infty} \beta^t \gamma_t^2 \quad (28)$$

I consider first the full-information rational expectations equilibrium response to a transitory shock η_t . Given the unnormalized aggregate demand equation

$$Y_t = \frac{1}{\beta\omega(1+\sigma\phi)} \left(\underbrace{(1-\beta\omega-\beta\omega\sigma\phi)}_{\text{Belief multiplier } \chi} \sum_{h=1}^{\infty} (\beta\omega)^h \mathbb{E}_t[Y_{t+h}] + \eta_t \right)$$

The equilibrium solution is given by $Y_t = b\eta_t$ where the coefficient b is

$$b = \underbrace{\frac{1}{\beta\omega(1+\sigma\phi)}}_{\rightarrow 0 \text{ as } \phi \rightarrow \infty} \underbrace{\left(1 - \frac{1-\beta\omega-\beta\omega\sigma\phi}{1+\sigma\phi}\right)^{-1}}_{\rightarrow (1-\beta\omega)^{-1} \text{ as } \phi \rightarrow \infty}$$

Because welfare is given by the discounted squared loss of output, the optimal choice of the Taylor coefficient that completely closes the output gap is for the monetary authority to be infinitely responsive $\phi \rightarrow \infty \implies b \rightarrow 0$. Further, welfare loss strictly decreases as ϕ increases for any finite ϕ . This shows that in the standard full-information rational expectations setting, a counterfactual policy that is more responsive to demand shocks is always welfare-improving.

However, when agents form expectations with simple and constrained-rational learning the optimal policy prescription differs. Simple learning yields the aggregate demand equation

$$Y_t = \underbrace{\frac{1-\beta\omega-\beta\omega\sigma\phi}{1+\sigma\phi}}_{\rightarrow -\beta\omega \text{ as } \phi \rightarrow \infty} \left(\frac{\rho_\lambda}{1-\beta\omega\rho_\lambda} E_{t-1}[\lambda_t] + \frac{\rho_\eta}{1-\beta\omega\rho_\eta} E_{t-1}[\eta_t] \right) + \underbrace{\frac{1}{\beta\omega(1+\sigma\phi)}}_{\rightarrow 0 \text{ as } \phi \rightarrow \infty} (\lambda_t + \eta_t)$$

In the infinitely-responsive ϕ limit, output is perfectly stabilized at the steady state if component beliefs are fully anchored $E_{-1}[\lambda_0] = E_{-1}[\eta_0] = 0$. Unlike in the full-information rational expectations case, if ϕ is not taken fully to the infinite limit but instead is finite and sufficiently large then the component beliefs $E_t[\varepsilon_{t+1}]$ and consequently output Y_t itself will be destabilized. Higher monetary responsiveness is therefore effective only up to a point, a limitation that is similarly demonstrated in Eusepi et al. (2024).

Figure 11 demonstrates that this behavior also holds in the constrained-rational learning case. The shared reason in both simple and constrained-rational learning is the expectation

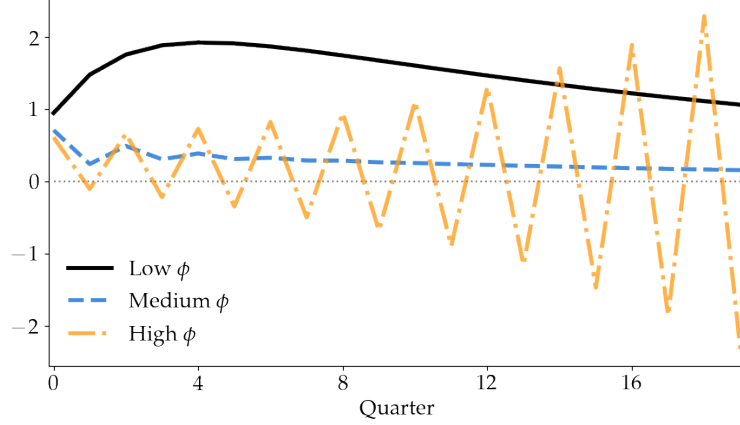


Figure 11: Output (de-)stabilization under different Taylor rule ϕ

Note: Each line represents the impulse response of output to a transitory demand shock in an economy with different Taylor rule coefficients ϕ .

feedback wedge that appears in the belief component law of motion is increasingly negative as ϕ increases. The intuition is by consuming more on the basis of positive component beliefs, the monetary authority leans heavily against consumption by raising interest rates and inducing a contraction in output. This causes households to misinfer that the shock components were actually realized to be negative and larger in magnitude than previously anticipated. The result is an increasingly unstable negative feedback loop, resulting in the explosive oscillation of the high ϕ case shown in Figure 11.

However, with mildly elevated responsiveness in the medium ϕ we see not only a reduced level response of output to the shock but also the absence of output inertia. Even though there is an expectation wedge in the component belief law of motion that in principle contributes to inertia, by choosing a Taylor coefficient ϕ that sets the belief multiplier χ close to zero enables the monetary authority to shut down the expectation feedback loop that unanchors expectations and results in inertia.

Because there is no expectation feedback wedge in rational learning, its behavior resembles that of full-information rational expectations. In particular, considering again the normalized rational learning equilibrium in Equation (27) and taking the $\phi \rightarrow \infty$ limit, the coefficients on component beliefs $E_{t-1}[\lambda_t], E_{t-1}[\eta_t]$ approach -1 . Unnormalizing Y_t, \tilde{Y}_t by the static general equilibrium feedback $\frac{1}{\beta\omega(1+\sigma\phi)}$, we see that similarly to the full-information rational expectations case as $\phi \rightarrow \infty$, fluctuations in Y_t, \tilde{Y}_t are dampened toward 0.

In choosing an optimal level of responsiveness to demand shocks, a monetary authority facing households with learning constraints should not respond as forcefully as in rational benchmarks because of the risk of destabilizing expectations.

5.2 Inertial Taylor rules and monetary policy gradualism

A popular Taylor rule specification includes a lagged or “inertial” term

$$r_t = \rho r_{t-1} + \phi Y_t$$

Early justifications for this approach were based on observed inertia in interest rate policy (Clarida et al. (1998)). However whether the policy rules themselves were inertial or were simply responding to inertial economic conditions remained debated (Rudebusch (2005)). Other justifications for inertial policy rules include uncertainty about the effects of policy Sack (1998) and their ability to implement optimal allocations when forward-looking agents understand the dynamic implications of policy commitments as in (Woodford (1999)).

I expand briefly on this latter reason by demonstrating the inability of constrained-rational and simple learning to fully understand dynamic policy commitments. The intuition for this closely resembles the expectation feedback mechanism discussed in the previous section. Just as constrained households are unable to fully internalize the equilibrium feedbacks of future expected output changes on current output, so too are they unable to internalize the effects of current policy commitments on future expected output which in turn has equilibrium consequences for current output.

The aggregate demand equation for output Y_t for arbitrary subjective expectations E_t , where households understand the inertial form of the policy rule and its parameters yields

$$Y_t = - \underbrace{\frac{\sigma \bar{\phi}}{1 + \sigma \bar{\phi}} \left(\sum_{\ell=1}^{\infty} \rho^\ell Y_{t-\ell} \right)}_{\text{Policy commitments in } r_{t-1}} + \frac{1 - \beta\omega - \beta\omega\sigma\bar{\phi}}{1 + \sigma\bar{\phi}} \sum_{h=1}^{\infty} (\beta\omega)^{h-1} E_t[Y_{t+h}] + \frac{1}{\beta\omega(1 + \sigma\bar{\phi})} \varepsilon_t$$

The “effective” Taylor coefficient $\bar{\phi} = \frac{\phi}{1 - \beta\omega\rho}$ demonstrates that whether policy responds contemporaneously via ϕ or with a delay via ρ , there is a way to equate their effective contribution toward current equilibrium output Y_t conditional on future expectations $\{E_t[Y_{t+h}]\}_{h>0}$. Hence, in response to an unanticipated shock at time-0, absent pre-existing policy commitments $r_{-1} = 0$ and fixing a given path of future expectations $\{E_t[Y_{t+h}]\}_{h>0}$ the response of time-0 output Y_0 should be the same for a continuum of regimes (ρ, ϕ) that induce the same effective $\bar{\phi}$.

However, the crucial step in the above consideration is that the path of future expectations was held fixed. Consider if households correctly perceived time- $t + h$ output used to inform time- t consumption which determines time- t output in equilibrium.

$$\tilde{Y}_{t+h} = - \underbrace{\frac{\sigma \bar{\phi}}{1 + \sigma \bar{\phi}} \left(\sum_{\ell=1}^{\infty} \rho^\ell \tilde{Y}_{t+h-\ell} \right)}_{\text{Function of } \{\varepsilon_{t+h-\ell}\}_{\ell>0}} + \frac{1 - \beta\omega - \beta\omega\sigma\bar{\phi}}{1 + \sigma\bar{\phi}} \underbrace{\sum_{j=1}^{\infty} (\beta\omega)^{j-1} E_{t+h}[Y_{t+h+j}]}_{\text{Function of } \{\varepsilon_{t+h-\ell}\}_{\ell\geq 0}} + \frac{1}{\beta\omega(1 + \sigma\bar{\phi})} \varepsilon_{t+h}$$

By correctly perceiving future output at time- $t + h$, households understand that current policy decisions which respond to current shocks will persist into time- $t + h$ with persistence ρ . Hence, two regimes with the same effective $\bar{\phi}$ would exhibit different equilibrium responses of output at time-0 if households perceptions correctly detected that the regime with higher

policy rule persistence ρ would continue to respond more forcefully in future periods to the time-0 shock.

However, when learning rules are restricted to load on contemporaneous shocks as in the constrained-rational and simple learning cases where \tilde{Y}_{t+h} can only be a function of ε_{t+h} , we see both expectation feedback in $\{E_{t+h}[Y_{t+h+j}]\}_{j>0}$ and lasting effects of current policy commitments on future output $\{\tilde{Y}_{t+h-\ell}\}_{\ell>0}$ must be partially ignored. This is again because contemporaneous shocks ε_{t+h} cannot span the space of all past shocks $\{\varepsilon_{t+h-\ell}\}_{\ell>0}$.

To demonstrate the consequences for welfare, I utilize the discounted squared output loss \mathcal{L} in Equation (28) from before and consider two policy regimes. I call the first policy regime the “swift” policy regime, (ρ^S, ϕ^S) , and the second one the “gradual” policy regime, (ρ^G, ϕ^G) , where the swift regime exhibits less inertia $\rho^S < \rho^G$ and greater contemporaneous responsiveness $\phi^S > \phi^G$. I choose these regimes to equate their welfare loss from a transitory shock under a full-information rational expectations benchmark.

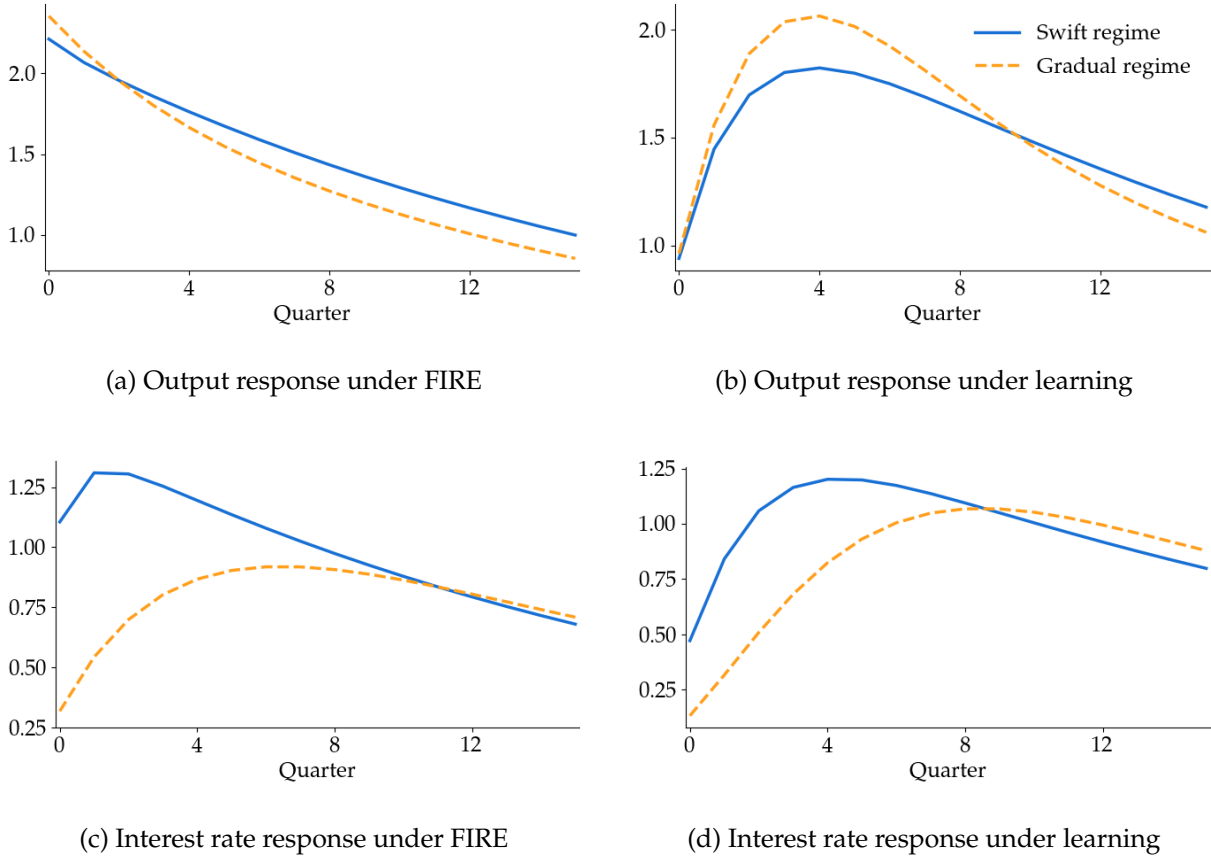


Figure 12: Output and interest rate impulse responses across monetary policy regimes

Note: The top panels represent the impulse responses of output to a transitory demand shock and the bottom panels the analogous responses for the real interest rate. The left column plots the impulse responses under full-information rational expectations (FIRE), and the right column under constrained learning.

Figure 12 demonstrates the responses to a transitory shock of output in the top panel and interest rates in the bottom panel for the swift and gradual regimes. The left column of responses are under the full-information, rational expectations (FIRE) benchmark and the right

column are with constrained-rational learning. Focusing first on the FIRE case, we see that under both regimes output responds immediately, where interest rates in the swift regime rise by more initially bringing output down by more. However, this difference only lasts for two quarters before output in the gradual regime crosses the swift regime even though interest rates in the gradual regime have yet to catch up to the swift regime. This occurs because households rationally understand the accumulated effects of interest rate changes will persist for a long time and reduce consumption spending accordingly.

In contrast, under learning we see that output continues to be less contained in the gradual than in the swift regime until gradual regime interest rates exceed those of the swift regime. Figure 13 demonstrates the difference in current-period discounted welfare $-\beta^t \gamma_t^2$ between the two regimes. Because these regimes were chosen to equate total welfare loss under full-information rational expectations, the area under the blue curve in Figure 13 integrates to 1. We see that the swift regime achieves higher initial welfare for the first two quarters by responding more forcefully but the gradual regime slowly makes up for the welfare difference in the long-run. However, with learning because the gradual regime is less effective at containing output in the short-run due to frictions households face in forward reasoning, the initial differences in welfare loss are too large to be offset by persistently higher rates and a smaller output response in later periods.

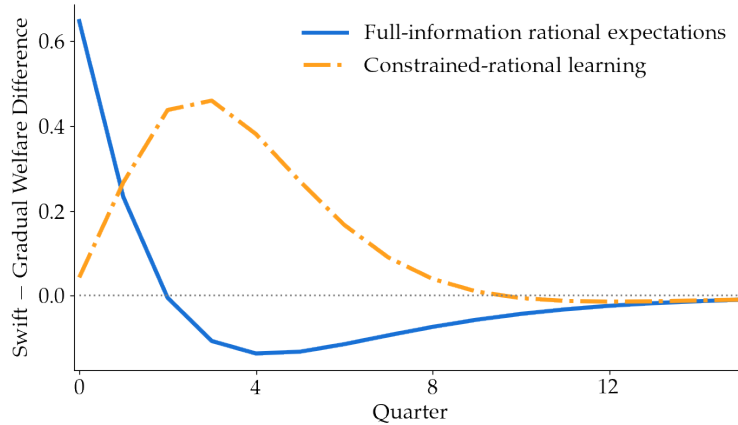


Figure 13: Welfare differences between monetary policy regimes

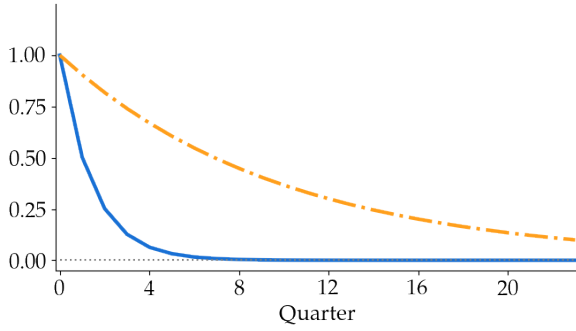
Note: The measure of welfare loss is the discounted squared output deviation each quarter. Each line corresponds to the difference in welfare loss incurred between the swift and gradual policy regime under a different model of expectation formation. When the lines exceed zero, the swift regime incurred a lower discounted welfare loss in that quarter and vice versa. The regimes were chosen such that the area between the blue curve and zero integrates to zero.

5.3 Deferred financing and the delayed impacts of fiscal stimulus

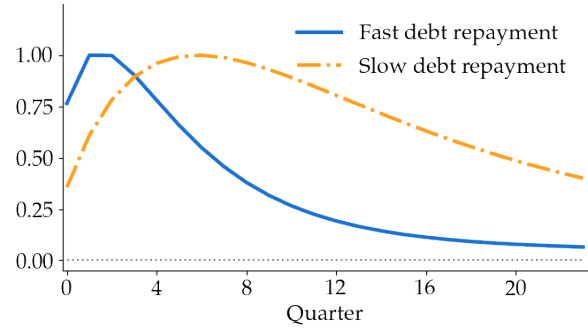
One of the key differences in the policy implications of heterogeneous-agent versus representative-agent macroeconomic models are their responses to fiscal stimulus (Auclert et al. 2024, Angelos et al. 2023). Representative-agent models have Ricardian equivalence and hence the effects of government spending or transfer policies are unaffected by the timing of financing. Conversely, deficit-financed spending and transfers induce large and immediate output responses

in heterogeneous-agent models. Further, the magnitude of these responses increase the further financing is delayed.

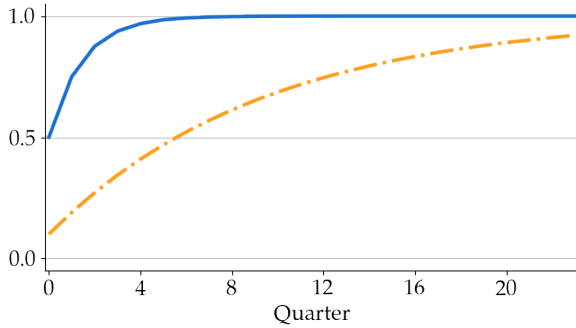
When households face learning constraints, as considered in this paper, there are additional implications of financing delays for the time profile of output in response to fiscal stimulus. In particular, deferred financing can delay the onset of fiscal stimulus and potentially reduce its effectiveness if the policymaker desires immediate results. Prolonging deficits additionally stretches out the cumulative response of output across a much longer horizon, running the risk that stimulus will last longer than intended and beyond the initially desired period of fiscal support. The propagation channels that induce these effects are similar to those in governing expectation feedback and prior monetary policy commitments.



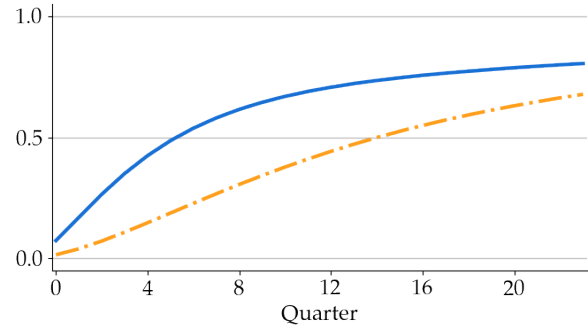
(a) Normalized response under FIRE



(b) Normalized response under learning



(c) Discounted cumulative response under FIRE



(d) Discounted cumulative response under learning

Figure 14: Output impulse responses across debt repayment regimes

Note: The top panel displays the output impulse response under each debt repayment regime, where the peak response is normalized to one. The bottom panel displays the share of the cumulative impulse response of output, discounted by the inverse gross interest rate.

I consider a simple form of fiscal policy that resembles the setting in [Angeletos et al. \(2023\)](#). The government issues real-valued debt B_t that is financed by a lump-sum tax T_t . Lump-sum taxes adjust to repay debt gradually, where the speed of repayment is given by $\delta \in (0, 1)$. The

linearized government budget constraint and tax rule are given by

$$B_t = \frac{1}{\beta}(B_{t-1} - T_t)$$

$$T_t = \delta B_{t-1} - (1 - \delta)\zeta_t$$

I assume there is no outstanding government debt in steady state $B = 0$, and ζ_t denotes an i.i.d deficit shock which I will use in the following policy exercise. By assuming debt is real-valued, I omit the possibility that surprise inflation erodes the real value of debt through nominal revaluation so we can still maintain our focus on real output alone. In addition, we now need to enforce asset market clearing between household wealth and government debt.

$$A_t = B_t$$

Given this setting we can again derive an aggregate demand equation that determines equilibrium output that is analogous to Equation (13) in [Angeletos et al. \(2023\)](#) but without the real interest rate peg.

$$Y_t = \frac{1}{1 - \chi} \left(\frac{(1 - \beta\omega)(1 - \omega)(1 - \delta)}{1 - \omega(1 - \delta)} (B_{t-1} + \zeta_t) + \chi \sum_{h=1}^{\infty} (\beta\omega)^h E_t[Y_{t+h}] + \varepsilon_t \right)$$

where the belief multiplier $\chi := (1 - \beta\omega - \beta\omega\sigma\phi)$ as before.

Figure 14 displays the response of output to a time-0 deficit shock ζ_0 under fast (large δ) and slow (small δ) debt repayment regimes. The top panel displays the response of output with its peak period normalized to one, and the bottom panel displays the cumulative response of output, discounted by the inverse steady state gross interest rate $(1 + r)^{-1} \equiv \beta$ with a total response normalized to one. The left column displays the responses under a full-information rational expectations (FIRE) benchmark and the right column under constrained-rational learning.

In the FIRE case, we see that the initial response of output to a one-time fiscal transfer is peaked on impact and monotonically decreasing. A large share of the discounted cumulative response of output $\sum_{t=0}^{\infty} (1 + r)^{-t} Y_t$, which is a commonly-used measure of the size of fiscal stimulus ([Mountford and Uhlig 2009](#)), also occurs at relatively short horizons. In the FIRE case, half of the discounted cumulative output response occurs immediately under the fast debt repayment regime and after five quarters in the slower repayment regime. In contrast, with constrained-learning there is a difference in the peak output response of one year between regimes and ten quarters for the discounted cumulative response, more than double the gap under FIRE.

6 Conclusion

This paper demonstrates that canonical heterogeneous-agent models are not just consistent with aggregate consumption inertia but fundamentally contribute to its emergence. I first show that the minimal structure imposed by these models yield model-implied impulse responses that closely resemble observed consumption inertia. I then adopt a learning model

that matches the over-extrapolation bias displayed in the expectations data to identify the features of expectations that cause inertia to arise. An interaction between over-extrapolation bias and the belief multiplier, a key model quantity representing the size of equilibrium amplification, determines whether inertia emerges and how protracted it is.

The learning frictions that result in inertial amplification yield additional costs of monetary policy gradualism and the deferred financing of fiscal deficits. Under rational expectations these policy approaches can produce a large and immediate consumption response because of households ability to accurately reason far into the future. In the learning model I consider, where households far-horizon reasoning is constrained, delayed policy action induces expectations to unanchor which lengthens policy transmission lags.

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